

1 **Fuzzy Agent-Based Multi-criteria Decision-Making Model for Analyzing Construction**
2 **Crew Performance**

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17 **Abstract**

18 Selecting economically feasible policies for maximizing crew motivation and performance is a
19 multifaceted problem, and each aspect of the process poses considerable unique challenges for
20 construction practitioners. Fuzzy agent-based modeling (FABM) addresses some of the challenges
21 of predicting crew performance (e.g., it accounts for both subjective uncertainties and crew
22 dynamics), but strategy selection is a decision-making problem that is also compounded by expert
23 disagreements, insufficient information, and differing stakeholder priorities. This paper proposes

24 a methodology for integrating multi-criteria decision-making (MCDM) with fuzzy agent-based
25 modeling (FABM) to develop a decision support model that simulates the complex relationships
26 and social interactions between crews and crew members for use in decision-making. This model
27 also accounts for dynamic construction environments and captures the subjective factors that
28 influence crew motivation and performance. The contributions of this paper are twofold. First, it
29 proposes a methodology that will help improve decision-making processes in construction by
30 expanding the scope of MCDM through integration with FABM. Second, it develops a fuzzy
31 agent-based multi-criteria decision-making model that helps construction practitioners adopt
32 economically feasible strategies for improving the motivation and performance of construction
33 crews. Furthermore, the proposed methodology can be adapted to several construction problems
34 to help decision makers prioritize and select from several strategies intended to improve different
35 crew performance measures.

36 **Author keywords:** Fuzzy agent-based modeling; multi-criteria decision-making; construction;
37 crew performance; fuzzy logic

38 **Introduction**

39 Agent-based modeling (ABM), a technique for simulating or modeling systems that considers the
40 emergent behaviors and interactions of several “agents” (e.g., crew members, supervisors, etc.)
41 with each other and the environment, is a useful tool for exploring the potential outcomes of
42 multiple scenarios. In the complex environment of construction decision-making, ABM allows
43 practitioners to explore multiple simulations and reach an appropriate “decision space,” which is
44 a set of options (i.e., scenarios) that are at the disposal of decision makers (Klein et al. 2009).
45 However, ABM does not account for all the challenges decision makers face in the construction
46 industry, such as changing contexts and subjective uncertainty. Raoufi and Fayek (2018c)

47 therefore developed fuzzy agent-based modeling (FABM), which integrates fuzzy logic with
48 agent-based models, making it possible to address construction-related problems that are highly
49 dynamic and involve subjective uncertainties. After applying FABM to a problem, the decision
50 maker still has to evaluate the consequences of each scenario and make a selection. When a
51 problem involves only one single criterion, the choice is straightforward as the decision maker
52 simply needs to choose the scenario with the highest preference rating. However, when scenarios
53 with multiple criteria are involved, considerations related to the weights of criteria, preference
54 dependence, and conflicts among criteria complicate the problem and more sophisticated methods
55 must be used (Tzeng and Huang 2011). One such method is multi-criteria decision-making
56 (MCDM), which is capable of evaluating alternative scenarios in terms of several criteria (i.e.,
57 objectives) while accounting for experts' preferences (Shahdany and Roozbahani 2016).

58 In a motivation-related context, the problem of selecting strategies to improve crew
59 motivation and performance can be considered a multi-criteria decision-making problem that
60 involves experts (i.e., stakeholders who are responsible for the success of the project). Because
61 construction is a dynamic process that is influenced by different factors, selecting the right strategy
62 is a combination of a simulation problem and a decision-making problem. The decision-making
63 component focuses on improving a performance measure by processing several alternatives and
64 considering objectives (e.g., cost and schedule) while selecting variables for use in the simulation.
65 The simulation aspect of the problem is the analysis of input measurements to produce an output
66 for a given performance measure, such as crew performance. A comprehensive model needs to
67 simulate the crew performance output and incorporate the assessment of several variations of
68 inputs (i.e., parameters) and crew performance outputs for use in selecting the right strategy (i.e.,
69 combination of specified inputs).

70 To address both the decision-making and simulation aspects of the strategy selection problem,
71 an approach is required that incorporates an MCDM model with a simulation technique that uses
72 fuzzy logic principles (i.e., FABM). The MCDM model incorporates the multiple, sometimes
73 conflicting opinions of experts and FABM simulates the subjective and dynamic nature of
74 construction problems, enabling practitioners to select effective strategies for improving a given
75 performance measure (e.g., crew motivation or crew performance). However, even though MCDM
76 and ABM have been used extensively in construction as standalone techniques, there is a gap in
77 the literature on incorporating MCDM with FABM. This paper develops a methodology for
78 integrating MCDM and FABM and illustrates the methodology with an analysis of a real-world
79 case study of improving construction crew motivation and performance.

80 The paper is organized as follows: A literature review of MCDM in construction is presented,
81 followed by a literature review of ABM, its applications in construction, and its use and limitations
82 in decision-making. Next, a methodology for integrating FABM and MCDM into a fuzzy agent-
83 based decision-making (FABM-MCDM) model is proposed. A case study on crew motivation and
84 performance is then used to illustrate the model. Finally, conclusions and recommendations for
85 future research are presented.

86 **Literature Review**

87 ***Multi-criteria Decision-Making***

88 Decision-making is a critical aspect of construction-related processes (e.g., policy making,
89 budgeting, risk and safety, planning and scheduling, bidding and tendering, productivity and
90 performance, etc.). These processes usually require that several criteria be analyzed before a
91 decision is made, usually in an environment of differing stakeholder priorities, insufficient

92 information, and expert disagreements. MCDM is an analytic method that assesses the advantages
93 and disadvantages of different alternatives based on a set of multiple criteria (Pirdashti et al. 2009).

94 A study by Zardari et al. (2015) classifies MCDM approaches as elementary methods, unique
95 synthesis criterion methods, or outranking methods. Elementary methods involve no
96 computational requirements; they are simple and best suited for problems involving a single
97 decision maker who is choosing between very few alternatives. These methods can also fall under
98 the category “non-compensatory decision-making,” which is when the positive attributes of an
99 alternative cannot compensate for the negative attributes of another alternative; in such situations,
100 the alternatives are quickly evaluated with minimal effort and an acceptable loss of accuracy. For
101 example, pros and cons analysis, max-min and min-max methods, the lexicographic method, and
102 elimination by aspect belong to this category. The unique synthesis approach entails aggregating
103 varying points of view into a single function that will be optimized. This approach is based on the
104 use of utility functions that can be applied to transfer the raw performance values of alternatives,
105 in terms of diverse criteria, to a common dimensionless scale, usually in the interval [0,1]. Some
106 examples include the simple multi-attribute rating technique (SMART), multi-attribute utility
107 theory (MAUT), the technique for order of preference by similarity to ideal solution (TOPSIS),
108 multi-attribute value theory (MAVT) and the analytic hierarchy process (AHP). The use of utility
109 maximization and the selection of the alternative(s) with the highest value can make the unique
110 synthesis approach a compensatory method. In compensatory methods, the positive (i.e., equal or
111 higher) value of one attribute can compensate for the negative value of another attribute (Lee and
112 Anderson 2009). Outranking synthesis methods, the third category, involve developing an
113 outranking relationship that represents the preferences of the decision maker using available
114 information. When the nature of decision-making does not allow compensatory relationships to be

115 established for use as parameters, or if the decision maker has a preference structure of a non-
116 compensatory nature (Vetschera and Almeida 2012), outranking methods can be effectively used
117 to good effect. Some of the methods in this category introduce discrimination (e.g., indifference
118 or preference) thresholds at each criterion level to locally model the decision maker's preference.
119 Examples include ELimination and Choice Expressing REality (ELECTRE) and the preference
120 ranking organization method for enrichment evaluation (PROMETHEE).

121 Modeling MCDM problems using different techniques is likely to produce different results,
122 and ease of applicability and accuracy must be considered when choosing which technique to use
123 to solve the problem. The popularity of the AHP in the areas of engineering, management,
124 economics, and sociology stems from its ease of use, its flexibility to integrate both qualitative and
125 quantitative properties, the extensive literature on the topic, and its ability to deal with tangible
126 and intangible criteria (Lee 2014). Sabzi and King (2015) evaluated six popular outranking
127 methods using the same decision matrix to simulate the MCDM process for flood management:
128 simple additive weights (SAW), comprehensive programming (CP), TOPSIS, AHP, ELECTRE
129 and VIKOR. Because of the AHP's aforementioned qualities, Sabzi and King (2015) chose to use
130 this method to process information in the decision matrix and perform multiple pairwise
131 comparisons of alternatives in terms of criteria.

132 *Agent-Based Modeling*

133 Since the first construction-related ABM models were developed in the early 2000s, the
134 application of ABM in construction has increased significantly in areas such as supply chain
135 management, claims management, infrastructure management, equipment management, bidding
136 strategies, procurement, site safety, and workers' behavior (Jabri and Zayed 2017). Eid and
137 El-adaway (2017) presented a decision-making framework that used ABM to capture a host

138 community's ever-changing recovery process in the aftermath of a natural disaster. Some
139 researchers have proposed methods of integrating ABM and other models. Ben-Alon and Sacks
140 (2017) proposed a hybrid model of ABM and building information modeling (BIM) to better study
141 production systems in construction that can capture the motivation and behavior of individual
142 crews and workers, as well as their interactions within a physical and process environment; this is
143 difficult to accomplish with other simulation methods (e.g., discrete event simulation). Cheng et
144 al. (2018) integrated ABM and BIM to simulate accidents on offshore oil and gas platforms to
145 evaluate and improve evacuation planning. Xiao et al. (2018) used ABM to study, from economic
146 and ecological perspectives, the impact of water demand management on the behaviors of different
147 municipal and industrial users. Raoufi and Fayek (2018c) advanced the application of FABM
148 approaches to handle uncertainties related to construction when measuring crew motivation and
149 performance.

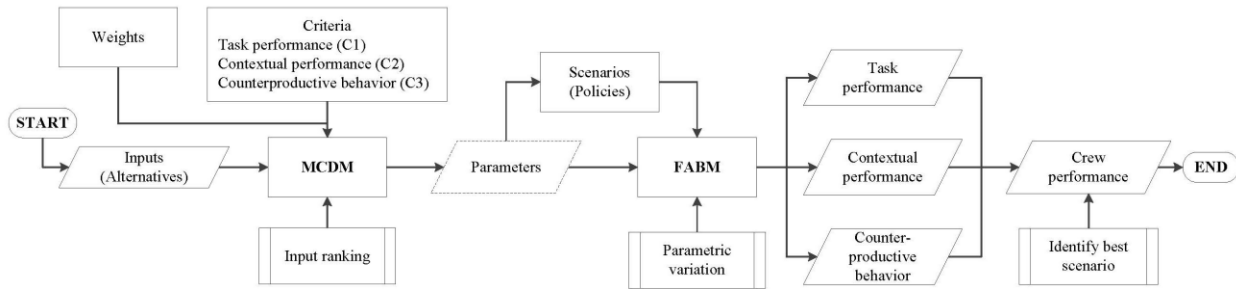
150 ABM can be directly used for decision-making when the decision-making elements have been
151 explicitly modeled (Bernhardt et al. 2007) and the mechanisms of the decision-making of agents
152 (i.e., individuals) have been properly explained (Lee 2014). For example, Eid and El-adaway
153 (2018) proposed a holistic sustainable disaster recovery approach using a decision-making
154 framework that employs ABM; Wang (2013) used ABM in the design of a collaborative decision-
155 making process to improve congestion and delays in air traffic; and Yang et al. (2009) applied
156 ABM in a decision support system for inventory management. However, for some problem
157 contexts (e.g., improving crew performance) where proposed strategies for output improvement
158 differ based on company objectives and experts' assessments and where the selection of
159 alternatives has to be weighed in terms of multiple, sometimes conflicting criteria, using ABM
160 alone can become computationally demanding. In these cases, focusing on ABM's ability to carry

161 out simulations with different parameters, boundaries, and constraints and combining the model
162 with proven decision-making tools can help produce a more applicable model. The work of
163 Marzouk and Mohamed (2018) reflects such an approach, as they integrated simulation results
164 from ABM and BIM into an MCDM model to evaluate the evacuation performance of buildings
165 under different scenarios in case of fire emergency. However, detailed studies on incorporating the
166 subjective nature of construction environments into ABM and using those models to evaluate
167 several scenarios for use in decision-making are lacking. Incorporating a decision-making tool into
168 ABM, specifically FABM, can therefore prove useful as it enables scenario analysis and decision-
169 making to improve performance measures for several types of construction problems.

170 **Fuzzy Agent-Based Multi-criteria Decision-Making Model Development**

171 When working to improve construction crew motivation and performance, practitioners must be
172 able to both simulate the subjectivity and dynamism of the problem and select the strategy that
173 will best satisfy a given set of objectives. An appropriate tool must therefore be developed that can
174 handle subjective variables in simulation with the use of fuzzy logic concepts, capture dynamism
175 with the use of dynamic modeling tools such as ABM, and process several simulation outputs in
176 order to select solutions targeted to improve chosen criteria with the use of MCDM. This section
177 presents a methodology for integrating FABM with MCDM to develop such a model. The data set
178 and initial simulation model (i.e., FABM) were obtained from Raoufi and Fayek (2018c) and
179 expanded to enable the development of the integrated model. The fuzzy agent-based–multi-criteria
180 decision-making model (FABM-MCDM) has two major components, as highlighted in Fig. 1. The
181 first component is the MCDM analysis, in which the AHP is used to rank alternatives, which are
182 the inputs to the model. The second component is the FABM technique, in which a parametric
183 study is applied to rank scenarios according to their outputs, which are performance measures (i.e.,

184 task performance, contextual performance, and counterproductive behavior). These two
 185 components of the FABM-MCDM model are described in the following section.



186
 187 **Fig. 1.** FABM-MCDM model.

188 ***Multi-criteria Decision-Making Model Component***

189 The purpose of the MCDM component in the FABM-MCDM is to rank the inputs of the model
 190 according to their influence on the outputs. Inputs with a significant influence on crew performance
 191 will be ranked and used as parameters for the model’s second component (i.e., FABM).

192 The inputs, shown in Table 1, are labeled “alternatives” (Alt.). Since the AHP was adopted
 193 for this study, pairwise comparisons are used to rank the alternatives according to their importance
 194 for three criteria (i.e., task performance [C1], contextual performance [C2], and counterproductive
 195 behavior [C3]). At the same time, pairwise comparisons will also be used to weight the criteria, as
 196 the importance of each criterion depends on the project context. The importance levels of the three
 197 criteria (AHP Level 1) are aggregated to form the goal of the hierarchical structure (i.e., crew
 198 performance), as shown in Fig. 2. The sub-criteria (AHP Level 2) inform the experts who are
 199 completing the pairwise comparison decision matrix as to what metrics are used to produce each
 200 of the performance measurements at Level 1. This allows experts to give emphasis to the
 201 performance metrics that are more relevant to their project when performing the pairwise
 202 comparisons for the criteria matrix.

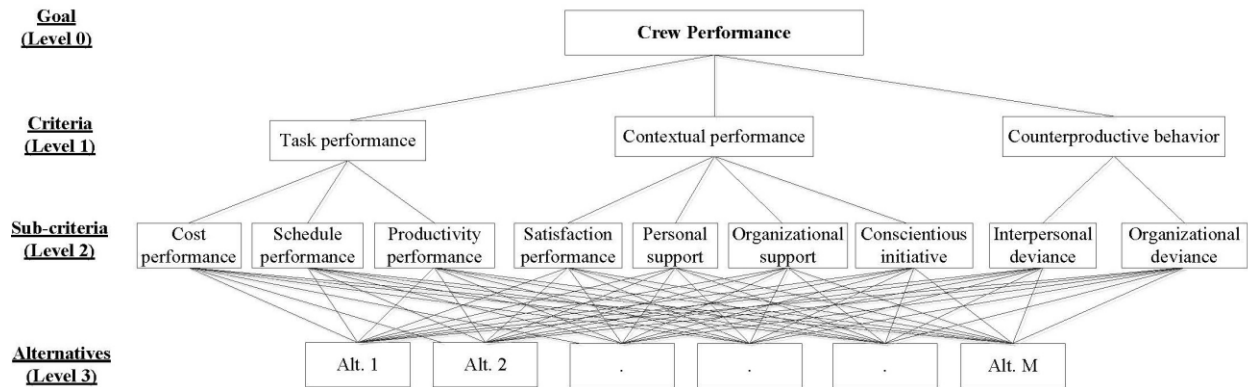


Fig. 2. Hierarchical structure of crew performance.

203 The pairwise comparisons are computed based on a scale of 1–7 (Saaty 2008). Discrete values
 204 between 1 and 7 are used to score the relative importance of alternatives in terms of each criterion,
 205 and the relative importance of each criterion to overall crew performance. The scores represent the
 206 following importance levels: 1 = equal importance, 3 = moderate importance, 5 = strong
 207 importance, and 7 = very strong importance; and values in between (2, 4, and 6) are compromises.
 208 For example, a score of A_{ij} ($=A_i/A_j$) indicates the relative importance of alternative i when it is

211 **Table 1.** Inputs for the FABM model.

Alt.	Inputs	Range	Description
1	Number of crews	Z+	Number of crews in the project
2	Contact rate	[0-3]	Number of times there is contact between crews per simulation time unit
3	Zealot percentage	[0,1]	Percentage of zealots in the project
4	Susceptibility	[0,1]	Probability that an interaction leads to change in motivation
5	Non-interactive motivation variability	[0,1]	The rate of change in motivation level without contact with other agents
6	Initial motivation states of crews	[0,1]	Percentages of crews in each motivation state at the start of the simulation
7	Initial state of crew-level situation	String: "unsatisfied", "satisfied"	Percentages of crews in each crew-level situation state at the start of the simulation
8	Initial state of project-level situation	String: "unsatisfied", "medium", "satisfied"	String parameter representing initial state of the project-level situation

9	Crew-level situation variability	R+	Rate of change in crew-level situation states per simulation time unit
10	Project-level situation variability	R+	Rate of change in project-level situation states per simulation time unit

212 compared with another alternative j in terms of criterion C . The rest of this section presents the
213 ranking procedure for inputs; weights are also given to each criterion based on the same procedure.
214 Each alternative matrix is a pairwise comparison of the inputs in terms of a single criterion. Eq. (1)
215 shows the pairwise matrix, where m alternatives are compared in terms of a criterion.

216

$$A_1 \quad A_2 \quad \cdot \quad A_m$$

217

$$\text{Alternative Matrix } (A) = \begin{matrix} A_1 \\ A_2 \\ \cdot \\ A_m \end{matrix} \begin{bmatrix} \frac{A_1}{A_1} & \frac{A_1}{A_2} & \cdot & \frac{A_1}{A_m} \\ \frac{A_2}{A_1} & \frac{A_2}{A_2} & \cdot & \frac{A_2}{A_m} \\ \cdot & \cdot & \cdot & \cdot \\ \frac{A_m}{A_1} & \frac{A_m}{A_2} & \cdot & \frac{A_m}{A_m} \end{bmatrix} \quad (1)$$

218 After the pairwise matrix is formed for each criterion, the next step is to calculate the
219 reciprocal matrix $[R]$, which satisfies the following three properties (Saaty 1990): reflexivity ($r_{ii} =$
220 1), reciprocity ($r_{ij} = 1/r_{ji}$), and transitivity ($r_{ik} = r_{ij} * r_{jk}$). This matrix will be used to solve the
221 eigenvalue problem shown in Eq. (2), where E is the eigenvector and λ_{\max} is the corresponding
222 maximum eigenvalue.

223

$$[R] = \begin{bmatrix} \frac{A_1}{A_1} & \frac{A_1}{A_2} & \cdot & \frac{A_1}{A_m} \\ \frac{A_2}{A_1} & \frac{A_2}{A_2} & \cdot & \frac{A_2}{A_m} \\ \cdot & \cdot & \cdot & \cdot \\ \frac{A_m}{A_1} & \frac{A_m}{A_2} & \cdot & \frac{A_m}{A_m} \end{bmatrix} \begin{bmatrix} A_1 \\ A_2 \\ \cdot \\ A_m \end{bmatrix} = \lambda_{\max} * E \quad (2)$$

224 The resulting consistency index must be checked using Eq. (3), and it must be less than 0.1
225 for the normalized eigenvector values to be used as weights for the criteria and alternatives (Saaty
226 1980). The consistency index is a measurement of the consistency of the performed comparisons
227 throughout all alternatives. For example, if alternative A_1 is more important than A_2 , and

228 alternative A2 is more important than A3, then alternative A1 needs to be more important than A3
229 in a consistent reciprocal matrix.

$$230 \quad \nu = \frac{\lambda_{max} - m}{m - 1} \quad (3)$$

231 where ν is the consistency index, λ_{max} is the maximum eigenvalue for the reciprocal matrix R, and
232 m is the number of alternatives.

233 After the consistency index is checked and found to be within the threshold, the resulting
234 eigenvector ($E_1, E_2 \dots E_m$) is normalized for use as the final weight for the corresponding value of
235 each alternative. The steps in Eqs. (2) and (3) are performed for all three criteria (i.e., C1, C2, and
236 C3). The criteria are also weighted using the same procedure, but instead of an alternative matrix,
237 as shown in Eq. (1), there will be a criteria matrix, where the weight of each criterion is obtained
238 by performing a pairwise comparison and applying the AHP procedure described in this section.
239 The final ranking for each alternative is produced by using a weighted sum to aggregate the scores
240 of each alternative for each criterion. For m alternatives and n criteria, the final ranking is obtained
241 by sorting the scores of the m alternatives, which are determined using Eq. (4), in descending order.

$$242 \quad \text{For } i = 1, m: \text{Score } (Alt_i) = \sum_{j=1}^n E_{ij} * C_j \quad \text{where, } j = 1, n \quad (4)$$

243 where E_{ij} is the weight of alternative i with respect to criterion j , and C_j is the weight of criterion
244 j .

245 The output of the MCDM model is a ranking of all the alternatives (i.e., inputs) proposed by
246 the experts. The ranking is then used to support the formulation of meaningful strategies that aim
247 to improve crew performance.

248 ***Fuzzy Agent-Based Modeling Component***

249 The FABM component of the FABM-MCDM is the integration of fuzzy logic and ABM in
250 MATLAB and AnyLogic, respectively. FABM simulates the effects of a combination of inputs

251 (see Table 1) on three criteria (i.e., task performance, contextual performance, and
252 counterproductive behavior). The main outputs of this model are variations in task performance,
253 contextual performance, and counterproductive behavior over the lifetime of the project.

254 Parametric variation is used in the proposed model because it can effectively simulate varying
255 sets of input combinations to obtain scenario analysis results. The main objective of the parametric
256 study is to reduce the number of experimental analyses that need to be performed to achieve the
257 target result, which is the best performance measure. This is done by simulating a combination of
258 input intervals for the input variables of the model at every run, rather than using single values of
259 inputs. Instead of having to simulate every possible set of input combinations, which may require
260 infinite runs, scenarios are built by specifying ranges for each input and then performing analyses
261 for all possible combinations within range. The results of FABM simulation are outputs of
262 proposed scenarios as functions of task performance, contextual performance, and
263 counterproductive behavior. The proposed scenarios are then ranked according to their effect on
264 crew performance values.

265 **Case Study**

266 The following case study illustrates the FABM-MCDM process using the analysis procedure
267 presented in the proposed model. Crew performance is defined as a function of three performance
268 metrics, namely task performance, contextual performance, and counterproductive behavior.

269 First, the alternatives listed in Table 1 are ranked according to the questionnaire shown in
270 Table 2. These rankings are performed in terms of all three criteria. The criteria are weighted
271 according to the questionnaire shown in Table 3. After obtaining the weight for each alternative in
272 terms of each criterion, as well as the weight of each criterion, a weighted average aggregation is

273 performed on each alternative to obtain the overall score in terms of crew performance, as shown
 274 in Eq. (4). For example, for alternative 1 (number of crews), the overall score is:

$$\begin{aligned}
 275 \quad \text{Score}(Alt_1) &= \sum_{j=1}^n E_{1j} * C_j; \quad \text{where } n = 3 & (4) \\
 276 \quad &= E_{11}C_1 + E_{12}C_2 + E_{13}C_3
 \end{aligned}$$

277 where E_{11} , E_{12} , and E_{13} are the weights of alternative 1 in terms of criteria 1, 2, and 3, respectively,
 278 and C_1 , C_2 , and C_3 are the weights of criteria 1, 2, and 3, respectively. The data for the pairwise
 279 matrix can be obtained by following the procedure outlined in the methodology and responding to
 280 the questionnaire surveys shown in Table 2 and Table 3, which are used for ranking alternatives
 281 and criteria, respectively.

282 The resulting pairwise matrix of alternatives for task performance is shown in Fig. 3, and it is
 283 used to rank the input variables as part of the MCDM process. In this paper, the pairwise matrix
 284 for alternatives with respect to the task performance criterion is based on hypothetical data used to
 285 illustrate the methodology. The alternative matrix (A) is calculated using Eq. (1) and the resulting
 286 pairwise matrix of alternatives is shown in Fig. 3. This pairwise matrix has also been used for the
 287 contextual performance and counterproductive behavior criteria matrices.

288 **Table 2.** Questionnaire for ranking alternatives.

	-7	-5	-3	1	3	5	7
Number of crews							Zealot percentage
							Contact rate
							Susceptibility
							Non-interactive motivation variability
							Initial motivation states of crews
							Initial state of crew-level situation
							Initial state of project-level situation
							Crew-level situation variability

To rank the alternatives presented in Table 1 in terms of their contribution to the task performance objective, compare the “number of crews” parameter to each of the parameters listed on the right, using the scale above.

Zealot percentage	_____	Contact rate
	_____	Susceptibility
	_____	Non-interactive motivation variability
	_____	Initial motivation states of crews
	_____	Initial state of crew-level situation
	_____	Initial state of project-level situation
	_____	Crew-level situation variability

To rank the alternatives presented in Table 1 in terms of their contribution to the task performance objective, compare the “zealot percentage” parameter to each of the parameters listed on the right, using the scale above.

Contact rate	_____	Susceptibility
	_____	Non-interactive motivation variability
	_____	Initial motivation states of crews
	_____	Initial state of crew-level situation
	_____	Initial state of project-level situation
	_____	Crew-level situation variability

To rank the alternatives presented in Table 1 in terms of their contribution to the task performance objective, compare the “contact rate” parameter to each of the parameters listed on the right, using the scale above.

Susceptibility	_____	Non-interactive motivation variability
	_____	Initial motivation states of crews
	_____	Initial state of crew-level situation
	_____	Initial state of project-level situation
	_____	Crew-level situation variability

To rank the alternatives presented in Table 1 in terms of their contribution to the task performance objective, compare the “susceptibility” parameter to each of the parameters listed on the right, using the scale above.

Non-interactive motivation variability	_____	Initial motivation states of crews
	_____	Initial state of crew-level situation
	_____	Initial state of project-level situation
	_____	Crew-level situation variability

To rank the alternatives presented in Table 1 in terms of their contribution to the task performance objective, compare the “non-interactive motivation variability” parameter to each of the parameters listed on the right, using the scale above.

Initial state of crew-level situation	Initial state of project-level situation
	Crew-level situation variability

To rank the alternatives presented in Table 1 in terms of their contribution to the task performance objective, compare the “initial motivation states of crews” parameter to each of the parameters listed on the right, using the scale above.

Initial state of project-level situation	Crew-level situation variability
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To rank the alternatives presented in Table 1 in terms of their contribution to the task performance objective, compare the “initial state of project-level situation” parameter to each of the parameters listed on the right, using the scale above.

289 **Table 3.** Questionnaire for ranking criteria.

	-7	-5	-3	1	3	5	7	
Task performance								Contextual performance
								Counterproductive behavior

To rank the alternatives presented in Table 1 in terms of their contribution to the crew performance objective, compare the “task performance” criterion to each of the criteria listed on the right, using the scale above.

Contextual performance	Counterproductive behavior
------------------------	----------------------------

To rank the alternatives presented in Table 1 in terms of their contribution to the crew performance objective, compare the “contextual performance” criterion to each of the criteria listed on the right, using the scale above.

Number of crews	1	1/5	1/5	1	1	1/7	1	1/5	1	1
Contact rate	5	1	3	5	5	1/3	5	3	5	5
Zealot percentage	5	1/3	1	3	5	1/3	3	1	3	3
Susceptibility	1	1/5	1/3	1	1	1/7	1/3	1/3	1/3	1/3
Non-interactive motivation variability	1	1/5	1/5	1	1	1/7	1/3	1/3	1/3	1/3
Initial motivation states of crews	7	3	3	7	7	1	5	3	5	5
Initial states of crew-level situations	1	1/5	1/3	3	3	1/5	1	3	1	1
Initial states of project-level situations	5	1/3	1	3	3	1/3	1/3	1	1	1
Crew-level situation variability	1	1/5	1/3	3	3	1/5	1	1	1	1
Project-level situation variability	1	1/5	1/3	3	3	1/5	1	1	1	1

Fig. 3. Pairwise matrix of alternatives [a].

290
291

292 Next, Eq. (2) is applied to get the eigenvector and Eq. (3) is applied to get the consistency
293 index. This is done separately for each criterion. The consistency index is calculated and found to
294 be 0.082, which conforms with the maximum consistency index requirement of 0.1. The
295 normalized eigenvector, which is used as weights for the alternatives, is calculated using Eq. (2).
296 Finally, Eq. (4) is applied to obtain the weights for each alternative, which are shown in Table 4.

297 As shown in Table 4, the highest-ranked alternatives (i.e., those with a significant contribution
298 to the crew performance output) are alternatives 6, 2, 3, and 8. These inputs are used to propose
299 scenarios and study their contributions to task performance, contextual performance, and
300 counterproductive behavior. Proposed scenarios can differ according to the kinds of policies
301 experts intend to implement to improve performance output (e.g., depending on their available
302 budget, time, and resources), which are reflected in the weights experts assign to each alternative.
303 Table 5 shows crew motivation and performance improvement strategies that companies can adopt
304 and the associated values (i.e., ranges) for the input parameters used in the FABM simulation.

305 The ranges of the selected inputs (i.e., parameters) are used in the FABM simulation for
306 parametric variation. The remaining inputs are also used in the simulation, but they will have fixed
307 values that are based on data specific to the project. Scenarios that are built based on the selected
308 parameters (see Table 5) are used as inputs for the parametric variation, and are shown in Table 6.

309 Keeping “initial state of project level situation” “satisfied” in the simulation, 27 (3*3*3)
310 scenarios are simulated in the FABM for every criterion. Each scenario is labeled according to the
311 initial values of contact rate, initial high-motivation states of crews, and zealot percentage. For
312 example, scenario 1 is labeled “LLL,” which indicates low contact rate, low initial high-motivation
313 states of crews, and low zealot percentage. Results are based on mean performance, computed at
314 every time step (i.e., daily), and taking the value of the project’s last day.

315 **Table 4.** Weights for alternatives.

Alternative	1	2	3	4	5	6	7	8	9	10
Weight	0.128	0.698	0.303	0.093	0.093	1.000	0.263	0.303	0.190	0.190

316 **Table 5.** Proposed company strategies.

Parameter	Strategy	Range	
Contact rate	Promoting interactions among crew members through interactive site orientations, safety meetings, and daily meetings	[0-1]	Low
		[1-2]	Medium
		[2-3]	High
Zealot percentage	Inclusion of crew members with a high level of experience whose motivation will not be affected by their environment; increasing the efficacy of crew members (at the individual level) through training	[0-0.33]	Low
		[0.33-0.66]	Medium
		[0.66-1]	High
Initial motivation states of highly motivated crews	Increasing commitment (engagement) at the individual and crew levels by improving relationships, belongingness, and communication between crews and crew members through team building activities; proposing incentives such as bonuses and vacation pay	[0-1]	Low
		[1-2]	Medium
		[2-3]	High
Initial state of project-level situation	Improving work/job conditions on the project by making resources readily available, such as quality equipment and other materials	"Satisfactory"	
		"Unsatisfactory"	

317 **Table 6.** Inputs used for parametric variation.

Parameters			
Contact rate	Initial high-motivation states of crews	Zealot percentage	Initial state of project-level situation
Low	Low	Low	"Satisfied"
Medium	Medium	Medium	
High	High	High	

318 **Results and Discussion**

319 This section discusses the results of the FABM-MCDM process and analysis based on the different
 320 scenarios. The 27 policies, which are a combination of three ranges of inputs (i.e., low, medium,
 321 and high), have been arranged to better capture the relationships between performance measures
 322 and variations of contact rate, initial high-motivation states of crews, and zealot percentage. The
 323 effects of variations in each input on the different performance measures (i.e., task performance,

324 contextual performance, counterproductive behavior, and crew performance) were studied
325 systematically by keeping one input constant while varying the others. For example, to see the
326 results of variations in contact rate, contact rate is kept constant for the different values of initial
327 high-motivation states of crews and zealot percentage. Thus, it is easy to observe when contact
328 rate changes from low to medium to high while all other combinations of inputs are exhausted for
329 each range of contact rate. For variations based on contact rate, scenarios 1–9 show the results of
330 low contact rate and all other possible values of initial high-motivation states of crews and zealot
331 percentage. Scenarios 10–18 and 19–27 show the results of medium and high contact rate values,
332 respectively, while varying the other inputs. Linear graphs of the performance values are made by
333 grouping the results of each set of nine scenarios, where each line traces the values for low,
334 medium, and high values of contact rate. All results have been presented in this manner.

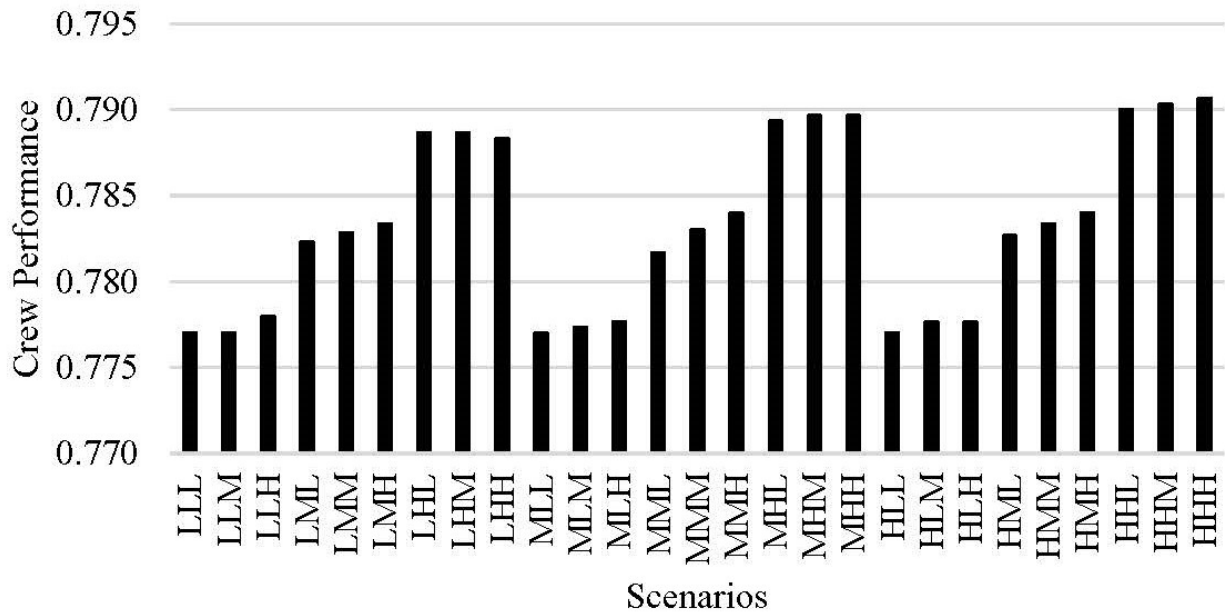
335 *Variations Based on Contact Rate*

336 The results in the category “contact rate” show the variations in performance measures (i.e., task
337 performance, contextual performance, counterproductive behavior, and crew performance) based
338 on contact rate. The results are tabulated in Table 7. As shown in Fig. 4, a general trend of
339 increasing crew performance can be seen as the contact rate increases. This increase becomes more
340 pronounced for medium and high values of initial high-motivation states. For low values of the
341 other parameters, the increase in contact rate did not have any effect. Hence, strategies intended to
342 increase crew performance by increasing contact rate have to also include an increase in either of
343 the other two parameters. An improvement to the crew performance recorded when all parameters
344 are low (i.e., scenario 1) can be obtained by adopting scenario 7 (LHL), scenario 17 (MHM), or
345 scenario 27 (HHH). All three scenarios indicate the need to keep the levels of initial high-
346 motivation states of crews higher. The choice of the scenario to be used as a strategy then depends

347 on the amount of improvement needed and the contextual situations (e.g., financial capability, time
 348 available, etc.) decision makers face when implementing a strategy. The effects of input parameter
 349 variations on task performance, contextual performance, counterproductive behavior, and crew
 350 performance are shown in Figs. 5a–5d, respectively.

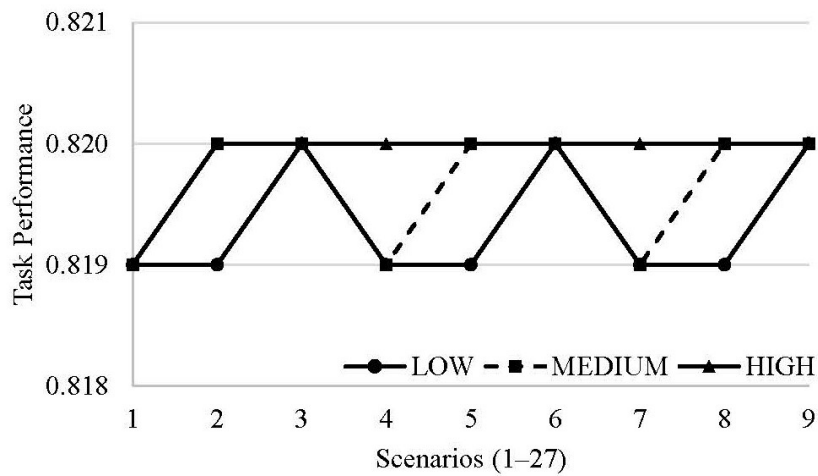
351 **Table 7.** Performance values based on contact rate.

Scenario	Label	Task Performance	Contextual Performance	Counterproductive behavior	Crew Performance
1	LLL	0.819	0.752	0.760	0.777
2	LLM	0.819	0.752	0.760	0.777
3	LLH	0.820	0.754	0.760	0.778
4	LML	0.819	0.761	0.767	0.782
5	LMM	0.819	0.762	0.768	0.783
6	LMH	0.820	0.762	0.768	0.783
7	LHL	0.819	0.770	0.777	0.789
8	LHM	0.819	0.770	0.777	0.789
9	LHH	0.820	0.770	0.775	0.788
10	MLL	0.819	0.752	0.760	0.777
11	MLM	0.820	0.752	0.760	0.777
12	MLH	0.820	0.753	0.760	0.778
13	MML	0.819	0.760	0.766	0.782
14	MMM	0.820	0.762	0.767	0.783
15	MMH	0.820	0.762	0.770	0.784
16	MHL	0.819	0.770	0.779	0.789
17	MHM	0.820	0.770	0.779	0.790
18	MHH	0.820	0.770	0.779	0.790
19	HLL	0.819	0.752	0.760	0.777
20	HLM	0.820	0.753	0.760	0.778
21	HLH	0.820	0.753	0.760	0.778
22	HML	0.820	0.761	0.767	0.783
23	HMM	0.820	0.762	0.768	0.783
24	HMH	0.820	0.762	0.770	0.784
25	HHL	0.820	0.771	0.779	0.790
26	HHM	0.820	0.772	0.779	0.790
27	HHH	0.820	0.772	0.780	0.791



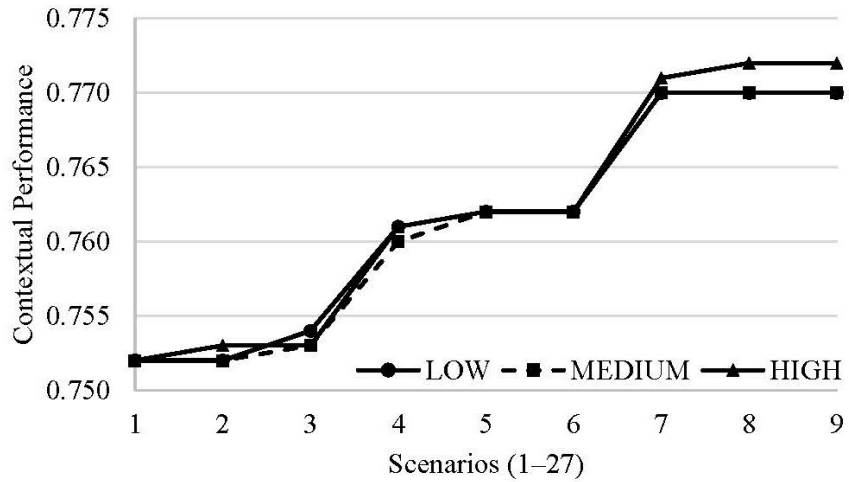
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Fig. 4. Crew performance results based on contact rate.



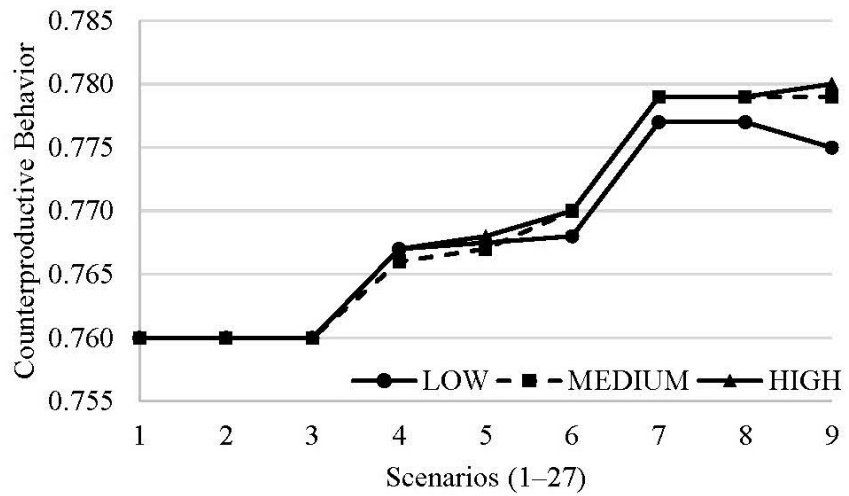
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Fig. 5a. Task performance based on contact rate.



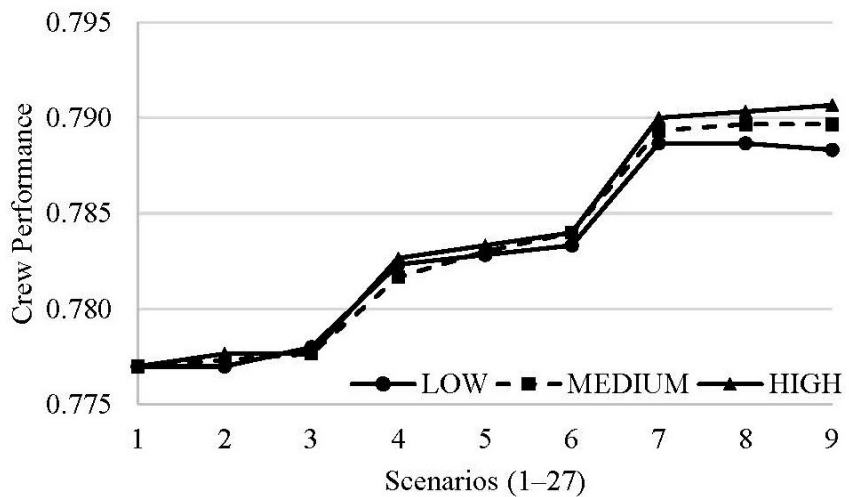
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Fig. 5b. Contextual performance based on contact rate.



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Fig. 5c. Counterproductive behavior based on contact rate.



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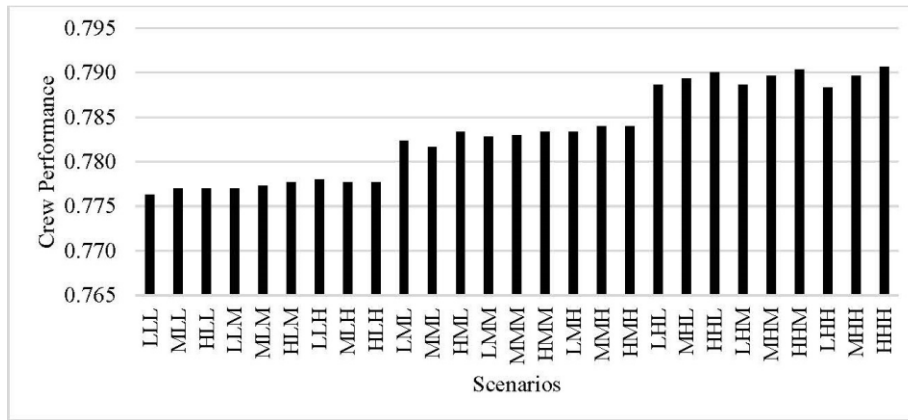
Fig. 5d. Crew performance based on contact rate.

362 The results show that a high contact rate can produce higher task performance, but the effect
363 of a high contact rate is constant throughout the rest of the policies, except HLL. Contextual
364 performance outputs did not show a significant variation based on contact rate, but they seemed to
365 be more affected by the initial high-motivation states of crews. This is consistent with the
366 performance index used to measure contextual performance that includes “helping,”
367 “cooperating,” “motivating,” “compliance,” and “initiative” (Raoufi and Fayek 2018 a, b), and it
368 is dependent on crews becoming and staying motivated.

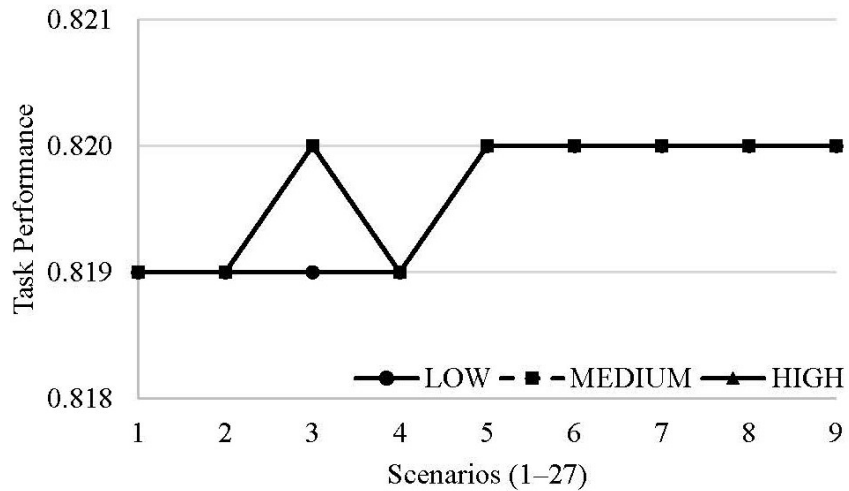
369 *Variations Based on Initial Percentage of Highly Motivated Crews*

370 The results for this category show variations in performance measures (i.e., task performance,
371 contextual performance, counterproductive behavior, and crew performance) based on the initial
372 percentage of highly motivated crews. As shown in Fig. 6, there is a general trend of increasing
373 crew performance as the initial percentage of high motivation level increases. There is no direct
374 relationship between the influence of the other inputs and the crew performance output when the
375 motivation state is kept constant. When the initial motivation level is kept constant, variations in
376 the values of other parameters did not have a significant influence on crew performance. This lack
377 of influence is even more visible in the values of task performance, contextual performance, and
378 counterproductive behavior. Another significant finding is the level of influence the parameter
379 initial high-motivation states of crews has on crew performance. In policies 1–9, for example, for
380 low contact rate and low zealot percentage, increasing the initial high-motivation states of crews
381 from low to medium visibly improves the crew performance measure. This change is even more
382 visible for higher values of contact rate and zealot percentage. The effects of input parameter
383 variations on task performance, contextual performance, counterproductive behavior, and crew
384 performance are shown in Figs. 7a–7d, respectively. In these figures, the scenarios are grouped

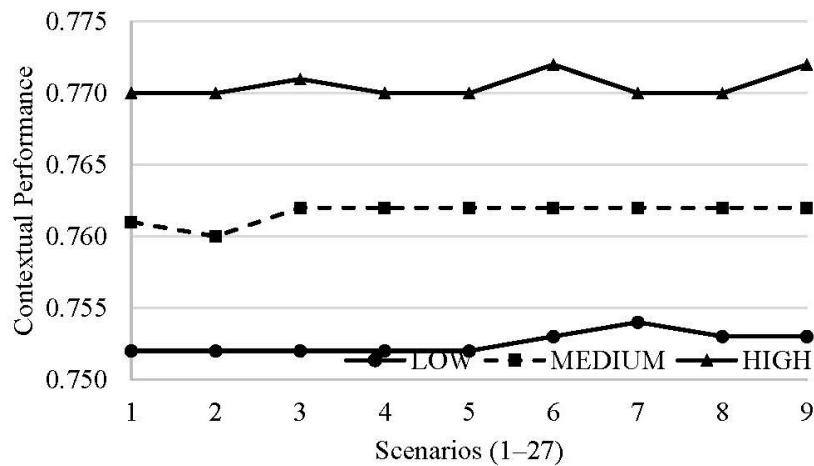
385 according to motivation state (i.e., low, medium, and high) while the values of contact rate and
 386 zealot percentage are varied.



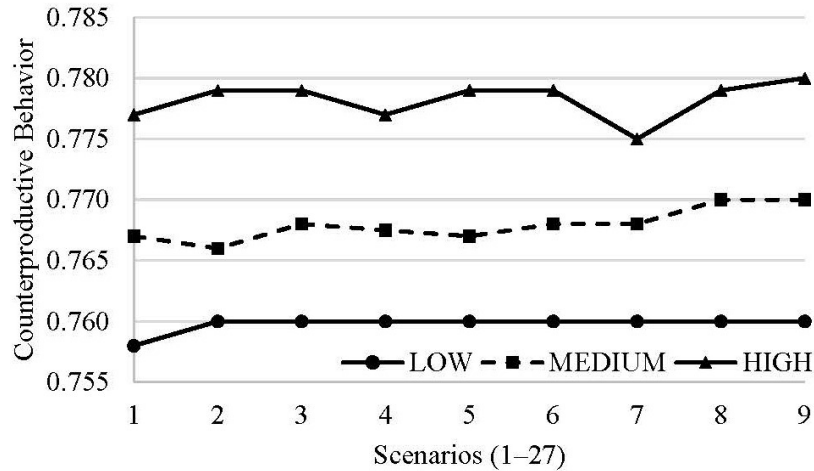
387
 388 **Fig. 6.** Crew performance results based on initial high-motivation states of crews.



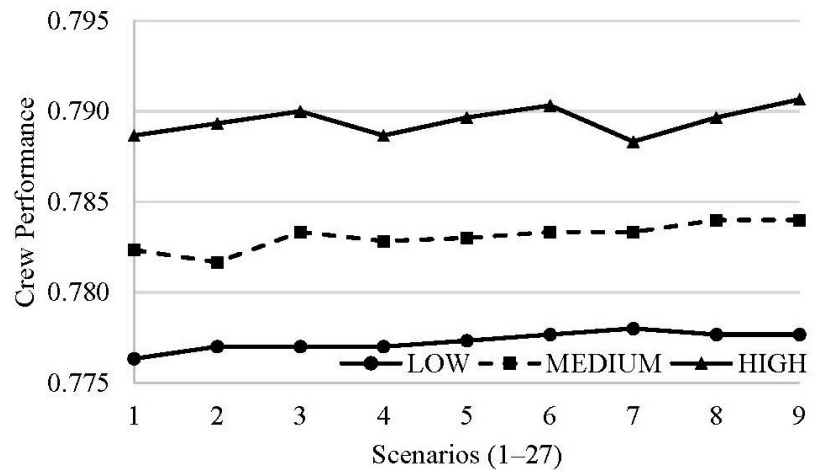
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 390 **Fig. 7a.** Task performance based on initial percentage of highly motivated crews.



391
 392 **Fig. 7b.** Contextual performance based on initial percentage of highly motivated crews.



393
394 **Fig. 7c.** Counterproductive behavior based on initial percentage of highly motivated crews.



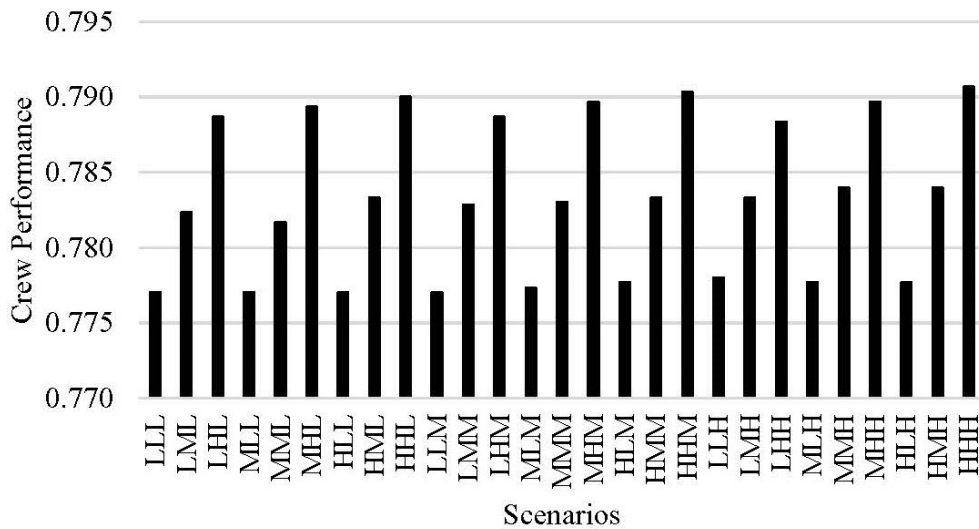
395
396 **Fig. 7d.** Crew performance based on initial percentage of highly motivated crews.

397 The results for task performance, contextual performance, and counterproductive behavior
 398 show that an increase in the initial motivation of crews produces an increase in the performance
 399 measures, especially for scenarios with a high motivation level, as shown in Figs. 7a, 7b, and 7c.
 400 Policy selection may therefore depend on which output measures are targeted for improvement
 401 and which policy provides the desired result using the least amount of resources.

402 ***Variations Based on Zealot Percentage***

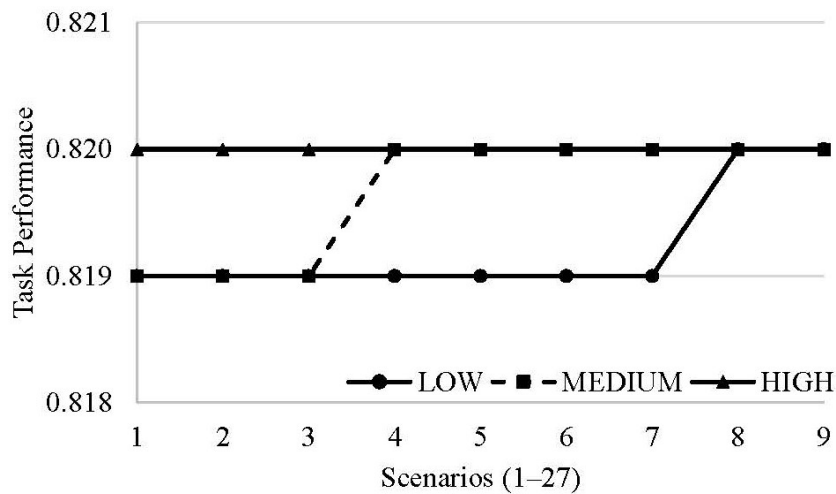
403 The results for this category show variations in performance measures (i.e., task performance,
 404 contextual performance, counterproductive behavior, and crew performance) based on zealot

405 percentage. As shown in Fig. 8, variations in crew performance occurred mainly because of
 406 variations in the initial high-motivation states of crews. Zealot percentage can be understood as a
 407 parameter that enables better performance when it is combined with other parameters, such as
 408 contact rate. The effects of input parameter variations on task performance, contextual
 409 performance, counterproductive behavior, and crew performance are shown in Figs. 9a–9d,
 410 respectively. In these figures, the scenarios are grouped according to zealot percentage (i.e., low,
 411 medium, and high) while the values of contact rate and initial high-motivation state are varied.



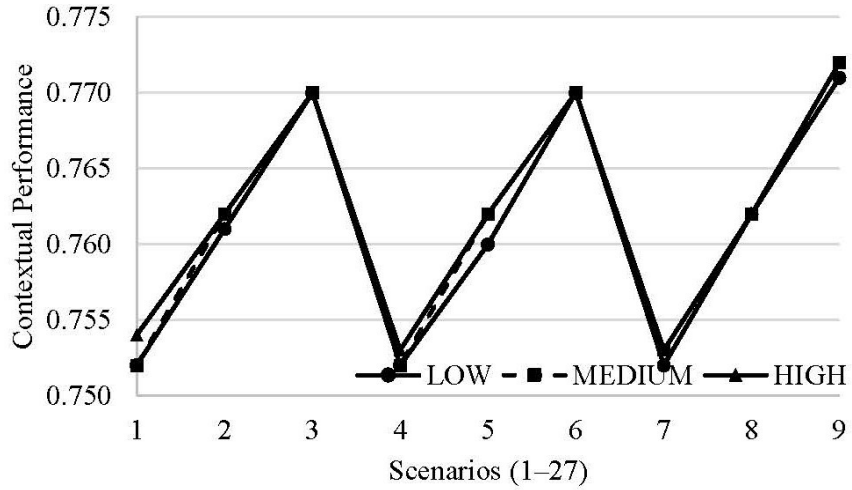
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Fig. 8. Crew performance results based on zealot percentage.



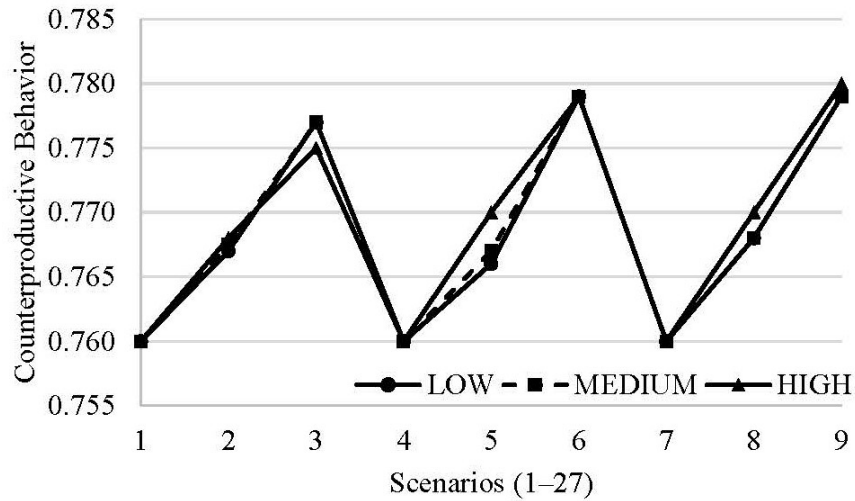
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Fig. 9a. Task performance based on zealot percentage.



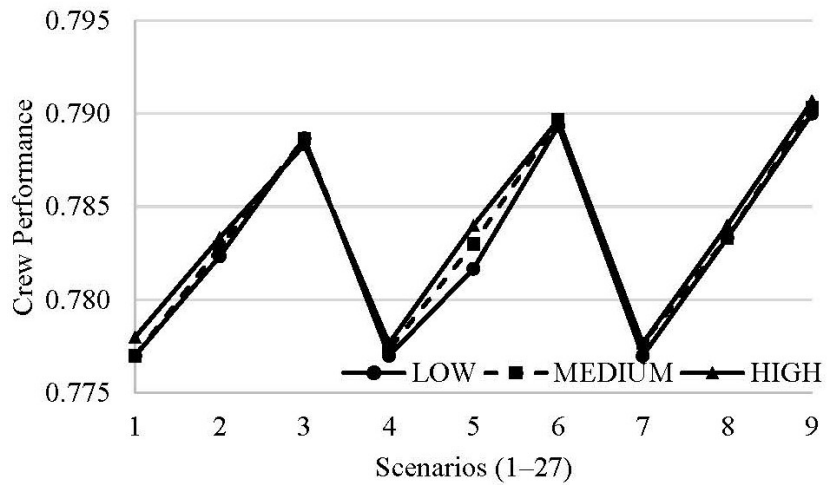
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Fig. 9b. Contextual performance based on zealot percentage.



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419

Fig. 9c. Counterproductive behavior based on zealot percentage.



420
421

Fig. 9d. Crew performance based on zealot percentage.

422 An analysis of the effect of the initial high-motivation states of crews on contextual
423 performance, counterproductive behavior, and overall crew performance shows there is a visible
424 direct correlation between the initial motivation of crews and output measures, as shown in Figs.
425 9b, 9c, and 9d. Policy selection may therefore depend on which output measures are targeted for
426 improvement and which policy provides the desired result using the least amount of resources.

427 **Conclusion**

428 In this paper, a methodology for the development of a fuzzy agent-based multi-criteria decision-
429 making (FABM-MCDM) model is provided to address the need for decision support tools for use
430 in construction, where problems exist in a dynamic environment with subjective uncertainties. The
431 methodology is then elaborated using collected field data on construction crew motivation and
432 performance. This paper demonstrates that the developed methodology is able to offer an
433 applicable and representative approach to the overall process of decision-making in construction
434 by integrating the capacity of FABM to address dynamic and subjective problems with MCDM's
435 capacity to address multiple, sometimes conflicting expert opinions.

436 The contributions of this paper are twofold. First, it proposes a methodology to integrate
437 FABM with MCDM in order to improve decision-making processes in construction. Second, it
438 develops an FABM-MCDM model that helps construction practitioners adopt economically
439 feasible strategies that improve the motivation and performance of construction crews.
440 Furthermore, the methodology proposed in the study can be adapted to several construction
441 problems to help decision makers prioritize and select from several strategies intended to improve
442 different crew performance measures.

443 In the future, sensitivity analysis of the MCDM model should be performed to analyze which
444 alternatives have the most influence on the decision-making process. When the AHP is used in

445 decision-making, changes in an individual piece of data or a minor change in the weights of criteria
446 should be studied, as these may have an influence on the ranking of inputs, and thereby on the
447 strategies that are adopted at the company level. Furthermore, the applicability of the developed
448 decision support model should be validated with data from other construction contexts (e.g.,
449 building construction) to ensure the model can be applied to the development of strategies for
450 performance improvement in other sectors of the construction industry.

451 **Data Availability Statement**

452 All data, models, and code generated or used during the study appear in the submitted article.

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