University of Alberta

Identification of Shared and Distinct Gene-disease Associations Among Multiple Related Diseases and Multiple Subtypes of a Disease

by

Conrado Franco-Villalobos

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Abstract

Genome-wide association study (GWAS) is an approach with high-throughput genotyping to uncover genetic susceptibilities of complex diseases. However, the genetic susceptibilities discovered usually carry very small risk increments. Additionally, the current approach to assess whether these genetic associations are shared among a group of diseases relies mainly on statistical significance alone, ignoring biologically relevant information such as magnitude and direction of the associations.

The methodology proposed takes into account not only strength and direction of the associations but also the resemblance of the biological mechanism by using logic regression to generate a graphical representation of the similarity of the associations. We found evidence that 149 genetic associations have certain degree of uniqueness with Crohn's Disease, Rheumatoid Arthritis, and Type I Diabetes while 11 were shared between at least 2 diseases. Additionally, the gene-level analysis of TB cases stratified by age, strain, and lineage identified 3 new susceptibility genes (*ZFHX1B*, *FER*, and *FAM77*) associated with different TB subgroups.

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List of Abbreviations

GWAS	Genome-Wide Association Study
SNP	Single-Nucleotide Polymorphism
CD	Crohn's Disease
T1D	Type I Diabetes
RA	Rheumatoid Arthritis
TB	Tuberculosis
WTCCC	Wellcome Trust Case Control Consortium
EAI	East African Indian
GVS	Genetic Variation Score
BF	Bayes Factor

Chapter 1 Introduction

1.1 Thesis Organization

This paper-based thesis was prepared in accordance to the Faculty of Graduate Studies and Research (FGSR) of the University of Alberta guidelines. The thesis is organized as follows:

Chapter 2 - First manuscript

Identification of shared and distinct genes: Crohns Disease, Type I Diabetes & Rheumatoid Arthritis in WTCCC data

Chapter 3 - Second manuscript

Novel Tuberculosis Susceptibility Genes Discovered by Logic Regression: a Stratified Analysis in Thai Population

Chapter 4 - Summary and Conclusions

1.2 Rationale

Autoimmune diseases are chronic conditions that involve an inappropriate response of the body to non-harmful substances and tissues in the body. This type of disorders are thought to arise due to a combination of genetic and environmental factors. The familial clustering of autoimmune diseases as well as association of multiple disorders in single individuals suggest that there might be common genetic susceptibility factors shared among this type of diseases [1].

Genome-wide association studies (GWAS) is a high-throughput approach currently used to uncover genetic susceptibilities of complex diseases by examining many genetic variants of individuals to assess if any of them is associated with a trait [2]. GWAS has also been used to assess shared and/or unique genetic susceptibilities of multiple diseases that are hypothesized to be biologically related [3] [4] [5]. However, the current approach widely used in GWAS to assess whether genetic variants are commonly or uniquely associated with multiple diseases overlooks relevant information by focusing largely or sorely on statistical significance.

To our knowledge, the current approach to assess whether genetic associations are shared among a group of diseases fails to take into consideration relevant information such as the magnitude and direction of the genetic effect which could potentially lead to inaccurate inferences about the sharedness of the associations. Chapter 2 of this thesis proposes a method that aims to provide a better insight of the genetic associations with a group of diseases by not only taking into account statistical significance, but also strength, direction, and similarity of the biological association. This Chapter also presents a test of the methodology using the Wellcome Trust Case Control Consortium (WTCCC) GWAS data of Crohn's Disease, Rheumatoid Arthritis, and Type I Diabetes [6].

GWASs have identified thousands of genetic variants associated with complex diseases and traits providing a better understanding of their genetic etiology. However, most of these genetic variants carry small risk increments which can only explain a small proportion of the clustering observed in family studies leading to a phenomenon called *missing heritability* [7]. Most human geneticists hypothesize that additional variants that have not been discovered can provide the explanation of this phenomenon. Specifically, many quantitative geneticists and biologists recognize that interactions might be responsible for the missing heritability phenomenon since they can greatly affect the heritability calculations and they are rarely investigated in GWASs [8].

Chapter 3 investigates whether genetic interactions can uncover novel susceptibility loci for tuberculosis (TB) in Thai. The analysis was performed on different subgroups stratified by age (> 45 years, \leq 45 years) [9], TB strain (ancient, modern), or TB lineage (Beijing, EAI, *other*) with shared controls. An additional analysis was performed to assess whether the associations uncovered by the stratified GWASs were shared with other subgroups.

1.3 Research Questions

Chapter 2

- 1. Do p-values provide enough information to assess whether a genetic associations is shared among a group of diseases?
- 2. Does taking into account strength, direction, and similarity of the biological association provide better insight of the sharedness of genetic associations among a group of diseases?

Chapter 3

- 1. Does stratified analysis of SNP-SNP interactions uncover new genetic TB susceptibilities in Thai?
- 2. Are the newly discovered genetic susceptibilities shared among different TB subgroups?

1.4 Hypotheses

Chapter 2

- P-values alone do not provide enough information to assess whether a genetic association is shared among a group of diseases and can lead to inaccurate inferences.
- Taking into account strength, direction, and similarity of the biological association provide better insight and a stricter definition of the sharedness of genetic associations among a group of diseases.

Chapter 3

- SNP-SNP interactions are responsible for a proportion of the TB susceptibility and explain to a greater extent the TB genetics.
- Some of the genetic susceptibilities are shared while others are unique for certain TB subgroups.

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Chapter 2

Identification of shared and distinct genes: Crohns Disease, Type I Diabetes & Rheumatoid Arthritis in WTCCC data

2.1 Introduction

Autoimmune diseases, such as Crohn's Disease (CD), Type I Diabetes (T1D), and Rheumatoid Arthritis (RA), are hypothesized to share similar genetic factors given the disease mechanisms and the observed clustering of diseases within families [1]. Crohn's disease is a type of inflammatory bowel disease characterized by the presence of abdominal pain, fever, and bowel obstruction or diarrhea with passage of blood, mocus or both [2]. Type I Diabetes results from an autoimmune destruction of β -cells in the pancreas which causes defects in insulin secretion, action, or both [3]. Rheumatoid Arthritis is an inflammatory disease that affects mainly the joints of the hands and feet as the result of over-expressed degradative enzymes which destroy articular tissues [4].

Although it has been suggested that CD, T1D, and RA share similar genetic etiology due to their autoimmune nature and a number of articles has been published addressing this scientific hypothesis, most of the approaches taken to identify common susceptibility loci has been rather simplistic and statistically oriented with a lack of biological relevance [5] [6]. The most common type of study involves performing a systematic review of previously reported susceptibility loci in genome-wide association studies (GWAS) for each individual disease and compare the findings across the diseases. If a loci was found to be significantly associated with two or more diseases, the association is considered "shared", if it was significantly associated with a single disease, it is considered "distinct". For example, it has been reported that gene *PTPN22* is commonly associated with CD, T1D, and RA [7]. The main limitation about this type of studies is that they don't take into consideration the strength and direction of the associations as well as the commonality of the SNPs encompassed in the reported genes.

Another approach, similar to the one discussed previously, has gone further in understanding the genetic etiology of autoimmune diseases. It has been reported that SNPs/genes *rs917997/IL18RAP* and *rs1738074/TAGAP* are commonly associated with Type I Diabetes and Celiac Disease by analyzing the association of SNP-disease independently of the other disease. The authors go further in the discussion section by noting that the minor allele in both SNPs is negatively associated with Type I Diabetes but positively associated with Celiac Disease suggesting opposite biological effects [8]. However, this approach still lacks an analysis of the strength of the associations which might indicate a minor/major role in the underlying biological mechanism depending on the disease.

Novel approaches that have tried to address the issues of incorporating the strength and direction of the associations include the calculation of a *Genetic Variation Score* (*GVS*) for each disease-SNP pair given by GVS[d, s] = $sign(log(OR[d, s])) \times log(p-value[d, s])$ where d, s, and OR represent a specific disease, a specific SNP, and the odds ratio of the association, respectively. After calculating the *GVS* vector for each disease, a correlation coefficient is calculated as an estimate of the degree of genetic concordance between pairs of diseases. In the formula, the term sign(log(OR[d, s])) captures the direction of the association while the log(p-value[d, s]) term is supposed to capture the strength of the association [9]. Although the direction of the association is effectively captured by this score, there is a statistical misconception that p-value indicates the strength of an association while it is a function of the sample size and can be changed by the sample size. Furthermore, the calculation of a correlation coefficient between pairs of vectors just gives an idea of the overall tendency of the statistical significance of the SNP-disease associations.

Even though the methodologies mentioned above fail to address some important issues in the analysis of shared and distinct genetic variants among a group of diseases, they have the advantage that they can be performed based solely on summary statistics (i.e., odds ratios and *p*-values) without requiring the raw data. Additionally, the computational requirements are relatively low which make the analyses easy to perform.

2.2 Materials and Methods

2.2.1 Logic Regression Gene-level Association Analysis

The proposed method involves gene-level association analysis by incorporating specific forms of SNP-SNP interactions that are biologically meaningful. Specifically, we investigated two forms of interactions: the first is SNP-SNPintersection which states that multiple SNPs need to have their respective high-risk genotypes in order for the disease-risk to be elevated (i.e., SNP-Aand SNP-B). The second form of interaction is SNP-SNP union which states that any of the SNPs needs to have their respective high-risk genotype in order for the disease-risk to be elevated (i.e., SNP-A or SNP-B). To incorporate these interaction into our analysis, we used logic regression to explore the best set of SNP-SNP interactions that are associated with the phenotype of interest [10]. Logic regression is a technique used to model an outcome (e.g., phenotype) using intersections and unions of potential binary predictors, such as SNP genotypes (i.e., indicator of the minor allele homozygous) as potential predictors. In the context of set theory, intersection and union are called Boolean operations because they act on binary variables. The logic regression model has the form shown in Eq. 2.1 where Y is the binary phenotype (i.e., disease and controls), $\beta_0, ..., \beta_p$ are the parameters, and $L_0, ..., L_p$ are Boolean combinations of SNP genotype indicators which are also called *logic trees*. Logic regression has been succesfully applied to SNP data analysis with selected candidate genes as well as GWAS to explain to a greater extent the disease genetics of highly heritable diseases [11] [12] [13].

$$logit (E[Y]) = \beta_0 + \beta_1 L_1 + \beta_2 L_2 + \dots + \beta_p L_p$$
(2.1)

Logic regression was performed on each gene independently 20 times varying the seed for the random number generator at the beginning of the stochastic search of logic regression. The seed variation allows us to search more broadly the solution space and diminish the probability of converging to a local optimum.

To evaluate the evidence of association, we also perform logic regression using the same genotype data but with 20 sets of permuted phenotype labels; each of the 20 is fit 20 times varying the starting random seed. This procedure allows us to perform a statistical significance test by obtaining an approximate distribution of the test statistic under the null hypothesis by comparing the likelihood of the original vs. the phenotype-permuted label models. These comparisons yield an approximate Bayes Factor (BF) for each gene. BF can be used as a measure of statistical evidence. Here we use it merely as a test statistic and for calculating a *p-value*. Specifically, the *p-value* for each gene is calculated as the proportion of all permuted BF values of all genes larger than the gene's observed BF. This calculation takes into account properly the multiple testing.

2.2.2 Shared vs. Distinct Gene Analysis using Logic Regression

The method is composed of two stages. In the first stage, we perform logic regression on each gene for each of the three diseases independently as described in Subsection 2.2.1. After determining which genes are strongly associated with each individual disease, we proceed with the next step but restricting the analysis to genes that achieved statistical significance in at least one disease. The second step involves performing several logic regression analysis by merging data from diseases and controls in order to evaluate to what degree the gene can differentiate between groups of diseases and controls.

For each of the genes that were found to be strongly associated with at least one disease, we perform additional logic regression analyses by combining any of the disease groups and the control group to create two new groups (e.g., Disease 1 & Disease 2 vs. Control) or taking any two of the groups (e.g., Disease 1 vs. Disease 2). The newly created groups could be interpreted as a fictional cluster of subjects with characteristics that averages both groups involved. The purpose of these extra analyses is to use the deviance of the logic regression model as a measure of whether the combining of the two groups was biologically appropriate. Two diseases truly sharing the association can be combined and should give a similar association as when each disease was evaluated for the association. Multiple diseases can show individual significance for the association but when combined may show no association if the biological association underlying the statistical association is not identical across the diseases.

Since the deviance is a function of the sample size and different phenotipic groups are merged, there will be an innate bias towards higher deviance values among those comparisons involving more than 2 groups (e.g., Disease 1 & Disease 2 vs. Controls). To address this issue, we perform a robust standardization of the deviances to make them comparable given by:

$std_{dev} = (dev_{ori} - MEDIAN[perm_{dev}])/IQR[perm_{dev}]$

where dev_{ori} is the deviance calculated with the original data and $perm_{dev}$ is a vector of the 20 deviances calculated with the randomly permuted phenotype labels. At the end of this analysis and assuming 3 diseases under study (D1, D2, D3) with shared controls (CL), we obtain a total of 18 standardized deviances coming from all the 6 pairwise comparisons among those 4 groups (3 diseases + controls), as well as 12 comparisons of those 4 groups and selected new phenotypic groups created by merging group pairs (i.e., D1 & D2, D1 & D3, D2 & D3, D1 & CL, D2 & CL, D3 & CL) in such a way that no group appears twice in a comparison (e.g., D1 & D2 vs. D1 is not performed, but D1 & D2 vs. D3 is). A comprehensive list of the source of the 18 deviances can be found in the last code-comment section of Appendix A.1.

The standardized deviances can be interpreted as "distances" of biological similarity of the gene-disease association among the different groups. The smaller the standardized deviance is between 2 groups, the more we suspect the groups are biologically similar with respect to the gene-disease association. The distance (standardized deviance) given by the logic regression models involving merged data (e.g., Disease 1 & Disease 2 vs. Controls) can be interpreted as the distance between the midpoint of the two merged groups (e.g., Disease 1 & Disease 2) and the third one (e.g., Controls).

After calculating the distances between groups, we perform an *uncon*strained nonlinear optimization [14] to estimate the best set of coordinates on a 3-dimensional euclidean space for highly significant gene-disease associations on at least 1 disease. The best solution is the set of coordinates that minimizes the sum of the errors between the estimated distances based on the coordinates and the calculated distances based on the standardized deviances. We opted for minimizing the sum of the errors rather than the vector of errors because the later gives higher fitting priority to longer distances. The errors whose sum we want to minimize are given by:

$$\epsilon = dist([G1_x, G1_y, G1_z]\&[G2_x, G2_y, G2_z]) - dist_{empirical}$$

where $dist([G1_x, G1_y, G1_z]\&[G2_x, G2_y, G2_z])$ is a function that returns the Euclidean distance between two sets of coordinates corresponding to groups G1 and G2 and $dist_{empirical}$ is the distance (standardized deviance) from the experiments mentioned previously.

Once we get the best estimate of the set of coordinates for each group, we proceed to plot these points, as well as pairwise distances, to get a visual representation of the degree of sharedness of the gene-disease associations. If two disease groups are close to each other, we expect the association to be shared. If two disease groups are separated from each other, we expect that the underlying biological mechanism acts in a different way for each disease, even though the gene-disease association might be highly significant for both diseases.

The method was tested on the Wellcome Trust Case Control Consortium (WTCCC) dataset of Crohn's Disease (1748 subjects), Type I Diabetes (1963 subjects), and Rheumatoid Arthritis (1860 subjects) and shared controls (2936 subjects) [15]. The list of candidate genes were obtained based on the work of Sharaf Eldin *et al.* entitled *Within-Gene Interactions in GWAS Identifies* Novel Susceptibility Loci - WTCCC Revisited as well as [11] and consisted of 158 genes which showed strong evidence of association with at least one of the diseases under study. These studies also limited the number of logic trees to 2 and the number of SNPs interacting in the model to 5 due to the high computational requirement of the stochastic search for the optimum solution in a high-dimensional space of the logic regression.

2.3 Results

In this section, we present some key examples to illustrate the method and the different scenarios that were found followed by a summary of the findings by categorizing genes based on the potential sharedness of the association among the 3 diseases.

We analyzed gene HLA-DRA in Chromosome 6 which was strongly associated with each of CD, T1D, and RA. The distance plot for this gene is shown in Figure 2.1. We can observe that all disease groups are far away from each other and CD is close to the Control group. This suggests that the strength of the association differs greatly between CD and T1D & RA. We can also tell by the distances and locations that the three diseases are strongly associated with HLA-DRA but with a different underlying biological mechanism among them. Additionally, we can analyze the individual logic regression models to get a better understanding of the SNP interactions that might be ocurring.

Table 2.1 shows a small effect of gene *HLA-DRA* on Crohn's disease odds ratios which range from 0.63 to 1.61. On the other hand, Tables 2.2 and 2.3 show a stronger effect on the Type I Diabetes and Rheumatoid Arthritis odds ratios which range from 1.00 to 32.28 and 1.00 to 6.24, respectively. We can also note that most of the SNPs that appeared in the model for each individual disease are unique for the particular disease and the strength of the associations vary broadly.

Although it has been reported by several studies that HLA loci associations are shared among autoimmune diseases [5] [16] [17], these results suggest that, even though all diseases were found to be associated with gene HLA-DRA, each of them follows its own biological mechanism so it would be inaccurate to call this association "shared".



Figure 2.1: Distance plot of gene *HLA-DRA*. † indicates statistical significance.

Table 2.1 :	Logic	structures,	frequencies,	and	associated	Crohn's	Dis-
ease odd	ls ratio	s of the HL	A-DRA gene	e			

SNP	rs9268831	rs9268877	rs7194	rs9268862	rs3135393			
Genotype	TT	AG or GG	AG or GG	AA	AG or GG	L	ogic-based	
Cases	420 (24.03%)	1521 (87.01%)	1057 (60.47%)	950 (54.35%)	535 (30.61%)	R	isk Groups	
Controls	717 (24.42%)	2526 (86.04%)	1879(64.00%)	1633 (55.62%)	976 (33.24%)	1		
Logic 1	((AND)	OR) A	AND		Free	Frequency OR	
Logic 2						Cases	Controls	
		Logic	1 = NO		Logic $2 = NO$	677	862	1.61
Logic-based		Logic 1	= YES		Logic $2 = NO$	536	1098	1.00
Risk Groups		Logic $2 = YES$	531	963	1.13			
	Logic 1 = YES				Logic $2 = YES$	4	13	0.63

Table 2.2: Logic structures, frequencies, and associated Type I Diabetes odds ratios of the HLA-DRA gene

SNP	rs9268831	rs3129877	rs9268645	rs5000563	rs9268877				
Genotype	TT	AA or AG	CG or GG	GG	GG	1	Logic-based		
Cases	638 (32.50%)	1273 (64.85%)	1638 (83.44%)	226 (11.51%)	1233~(62.81%)	I	Risk Group	5	
Controls	717 (24.42%)	1460 (49.73%)	1777 (60.52%)	263 (8.96%)	1111 (37.84%)				
Logic 1	((OR) AN	D (OR)		Frequency OR			
Logic 2						Cases	Controls		
		Logic 1	= NO		Logic 2 = NO	48	958	1.00	
Logic-based		Logic 1	= YES		Logic 2 = NO	682	867	15.71	
Risk Groups		Logic 1 = NO				104	413	5.03	
		Logic 1	= YES		Logic $2 = YES$	1129	698	32.28	

Table 2.3: Logic structures, frequencies, and associated Rheumatoid Arthritis odds ratios of the HLA-DRA gene

SNP	rs9268853	rs9268645	rs3177928	rs3129877	rs9268853			
Genotype	TT	CC	GG	GG	CT or TT	L	ogic-based	
Cases	437 (23.49%)	442 (23.76%)	1248 (67.10%)	967 (51.99%)	1341 (72.10%)	R	isk Groups	
Controls	1180 (40.19%)	1159 (39.48 %)	2120 (72.21%)	1476 (50.27%)	2544 (86.65%)]		
Logic 1	(OR)					Free	quency	OR
Logic 2				OR) A	AND)	Cases	Controls	
	Logic	Logic $1 = NO$		Logic 2 = NO			489	6.24
Logic-based	Logic 1	Logic $1 = YES$		Logic 2 = NO				2.35
Risk Groups	Logic $1 = NO$		Logic $2 = YES$			546	858	2.61
	Logic 1	= YES		Logic $2 = YES$		252	1034	1.00

Gene *PTPN22* illustrates a different possible scenario: the gene was found to be strongly associated with RA & T1D but not CD. It can be seen from Figure 2.2 that T1D and RA are clustered together and far from the CD and Control group. This suggests that the biological mechanism of this gene is the same for RA and T1D so the association could be shared among them, but distinct from CD. We can obtain a better insight of the SNP interactions by looking at the logic trees of the individual models.



Figure 2.2: Distance plot of gene *PTPN22*. † indicates statistical significance.

Table 2.4: Logic structures, frequencies, and associated Crohn's Disease odds ratios of the PTPN22 gene

SNP	rs1217414	rs2488457	rs2488457	rs1217414			
Genotype	GG	CC or CG	CC	AA	I	ogic-based	
Cases	922~(52.75%)	1693 (96.85%)	1150 (68.79%)	160 (9.15%)	R	isk Groups	
Controls	1573 (53.58%)	2814 (95.84%)	1869 (63.66%)	212(7.22%)	1		
Logic 1	((AND) OR)				Frequency O		OR
Logic 2					Cases	Controls	
	Logic $1 = NO$			Logic $2 = NO$	219	448	0.81
Logic-based	Logic $1 = YES$			Logic $2 = NO$	1369	2276	1.00
Risk Groups	Logic $1 = NO$			Logic $2 = YES$	0	0	
		Logic $1 = YES$		Logic $2 = YES$	160	212	1.25

Table 2.5: Logic structures, frequencies, and associated Type I Diabetes odds ratios of the PTPN22 gene

SNP	rs2488457	rs1217414	rs3789609	rs2488457			
Genotype	CC or CG	GG	CC	CC	Logic-based		
Cases	1818 (92.61%)	1091 (55.58%)	1023 (52.11%)	1062 (54.10%)	Risk Groups		
Controls	2814 (95.84%)	1573 (53.58%)	1431 (48.74%)	1869~(63.66%)			
Logic 1	((A	ND) O	R)		Free	Frequency OI	
Logic 2						Controls	
		Logic $1 = NO$	Logic $2 = NO$	146	122	2.23	
Logic-based		Logic $1 = YES$	Logic $2 = NO$	755	945	1.49	
Risk Groups		Logic $2 = YES$	304	456	1.24		
		Logic $1 = YES$		Logic $2 = YES$	758	1413	1.00

Table 2.6:	Logic structure	s, frequencies,	and	associated	Rheumato	oid
Arthritis	odds ratios of t	he PTPN22 ge	ene			

SNP	rs2488457	rs3789609	rs1217414	rs2488457			
Genotype	CG or GG	TT	AA or AG	CC or CG	L	ogic-based	
Cases	844 (45.38%)	137 (7.37%)	806 (43.33%)	1739 (93.49%)	R	isk Groups	;
Controls	1067 (36.34%)	255 (8.69%)	1363 (46.42%)	2814 (95.84%)	1		
Logic 1	(OR	(OR (AND))			Free	Frequency	
Logic 2					Cases	Controls	
		Logic $1 = NO$			0	0	
Logic-based	Logic $1 = YES$			Logic $2 = NO$	121	122	1.82
Risk Groups	Logic $1 = NO$			Logic $2 = YES$	1014	1869	1.00
		Logic $1 = YES$	5	Logic $2 = YES$	725	945	1.41

The logic tables for gene *PTPN22* and the diseases show that T1D and RA might share the association since the SNPs and the risk-increasing alleles involved in the models match while CD does not show a strong association with the gene. Although, given that only 4 SNPs were in the gene, high similarity of the models is expected. The difference in the distance from T1D and RA to

the Control group could be attributed to the strength of the association since *PTPN22* is showing bigger odds ratios while also being further away from the Control group compared to RA.

Based on our analyses, out of 158 genes, we have evidence supporting that 3 gene-disease associations are shared among all 3 diseases, 4 between T1D & RA, 3 between CD & RA, and 1 between CD & T1D. It can be noticed that the vast majority of the associations are distinct for a specific individual disease. These results suggest that most of the traditional and novel approaches overestimate the degree of sharedness of the genetic etiology of diseases since they are based only on significance without taking into account strength and direction of association.

2.4 Discussion

The methodology proposed here is based on a strict definition of "shared" association. By using this approach, we take into account not only singledisease significance, direction, and strength of the gene-level associations when making inferences, which are measures relevant to single SNPs analysis, but also incorporate the idea of how a set of SNPs of a gene are associated with the diseases. This strict definition of "shared" association was used because even if 2+ diseases are associated with the loci with the same OR direction, it does not mean they share the biological association (e.g., through the same biological pathway).

The higher accuracy of the method requires a significant amount of computational time due to the neccesity of fitting additional logic regression models on top of the high computational time required by the gene-level logic regression GWAS analysis. We reduced the computational demand of the logic regression by limiting the number of SNPs interacting in the model which makes the search not comprehensive and more complex interactions will not be discovered. Despite the limitation imposed by fixing the number of SNPs interacting in the logic regression models, we were able to demonstrate the potentially erroneous inferences that can arise when assessing whether a genetic association is shared or distinct among a group of diseases if only limited information such as p-values and odds ratios are used. For most of the associations studied in this paper, the results suggest some degree of uniqueness in the gene-disease associations which indicate a potentially different biological role of the genes on the etiology of each disease.

The methodology was designed to be applied to GWASs using the same genotyping platform which might present a limitation when working with cross-platforms studies. In case the platforms differ among disease groups, we could adapt the method to allow the analysis to be done. One way to overcome this limitation is by using just the matching SNPs across platforms which could significantly reduce the number of available SNPs to work with and the results might not represent the single-disease analysis results. Another alternative could be to select proxies for the non-matching SNPs based on proximity (if any) to compensate for the mismatch. A third more elaborate approach would involve an imputation process before the single-disease analysis [18].

There has been an increasing attention paid to pathway analysis in GWAS [19]. The methodology proposed could be extended to candidate pathwaylevel analysis with some adaptations. The main challenge with pathway-level analysis is the computational demand and convergence since the number of SNPs involved would be high and the solution space to explore would be big increasing the chances of convergence to a local optimum if the space is not explored appropriately.

Future work involves quantifying the variance of the association strength and direction possibly by using a random-effects model. This would allow us to obtain disease-specific estimates of effect and statistically test their significance making able to quantify the sharedness of the gene-disease associations.

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Chapter 3

Novel Tuberculosis Susceptibility Genes Discovered by Logic Regression: a Stratified Analysis in Thai Population

3.1 Introduction

Tuberculosis (TB) is an infectious disease caused by *Mycobacterium tubercu*losis and it is one of the leading causes of death in developing countries. The infection is generally transmitted by droplets generated during abrupt respiratory movements such as coughing. Tuberculosis infection can be either active or latent, depending on the presence or absence, respectively, of symptoms, which usually involve cough, chest pain, shortness of breath, fatigue, weight loss, fever and night sweats. Latently infected people cannot transmit the disease to other people but remain at risk of becoming actively infected [1].

While environmental factors play major roles in TB infection, the role of genetics in the active infection of tuberculosis has been acknowledged by several family studies [2] [3] [4]. Further genome-wide association studies (GWAS) have discovered susceptibility loci such as single-nucleotide polymorphisms (SNPs) rs3024505 and rs9373180 of genes IL10 and IFNGR1, respectively [5]. However, these findings are still far from explaining the heritability of tuberculosis as it is common for most GWASs of complex diseases [6].

Recently, a new GWAS uncovered a new susceptibility locus by empirically stratifying the TB case group as young (≤ 45 years old) and old patients (> 45 years old) in Thai and Japanese populations. SNP *rs6071980* of the *HSPEP1-MAFB* region was found to be significantly associated with TB with odds ratios of 1.82 and 1.81 for young Thai and Japanese populations, respectively [7]. Given the success of novel approaches to explore SNP-SNP interactions such as logic regression to explain complex disease genetics in GWASs [8], we hypothesize novel suceptibility genes could be discovered by following a similar approach on stratified TB cases.

To explore SNP-SNP interactions in our TB GWAS analysis, we propose using logic regression which incorporates SNP intersection, union and combinations of them to assess whether a group of SNPs are jointly associated with a stratified phenotype [9]. As mentioned before, logic regression has been succesfully applied to groups of SNPs but mostly based on candidate genes due to the high computational demand [10] [11] [12]. To further analyze whether the gene-disease associations are shared among the stratified groups, we propose to do a shared vs. distinct analysis as described in Chapter 2.

3.2 Materials and Methods

The method we proposed is a gene-level analysis that is performed by incorporating two specific forms of SNP-SNP interactions which are motivated by biological knowledge. One form of interaction is SNP-SNP intersection, which requires that multiple SNPs need to have their high-risk genotypes for the disease-risk to be elevated (i.e. SNP-A and SNP-B). The second form of interaction is SNP-SNP union, which requires the high-risk genotype of at least one of the two SNPs for the disease-risk to be elevated (i.e. SNP-A or SNP-B). Logic regression incorporates these two types of SNP-SNP interactions into the models by exploring the optimum set of SNP-SNP interactions that are associated with the disease or trait of interest [9]. By using logic regression, we model the outcome (i.e. TB case or control status) as *intersections* and *unions* of binary SNP genotype indicators. The logic regression model used has the specific form shown in Eq. 3.1 where Y is the binary phenotype (i.e. TB case and controls), $\beta_0, ..., \beta_p$ are the model parameters, and $L_0, ..., L_p$ are combinations of SNP genotype indicators which are also referred to as *logic trees*. Logic regression has been successfully applied to GWAS to explain to a greater extent the disease genetics of Crohn's Disease, a highly heritable disease [8].

$$logit (E[Y]) = \beta_0 + \beta_1 L_1 + \beta_2 L_2 + \dots + \beta_p L_p$$
(3.1)

The logic regression SNP-SNP interaction analysis we performed used only those SNPs in such a way that no pair of them within a gene were in linkage disequilibrium ($r^2 \ge 0.8$). The maximum number of *logic trees* we allowed in our models was two (L_1, L_2) with at most five interacting SNPs in total. These restrictions were specified in our models due to the large number of possible interactions to explore and the exponencially increasing computational cost associated with each additional tree or leaf. Since the search of the solution space is done stochastically by means of a simulated annealing algorithm, we fit the logic regression 20 times varying the initial random seed of the stochastic search. At the end of the 20 fitting processes, we keep the model with the lowest deviance among them. This process is also repeated with 20 sets of case-control randomly permuted labels.

The deviance of the best model in addition to the deviances of the best model with case-control labels randomly permuted allow a statistical significance test. A Bayes Factor (BF) can be obtained from this comparison, which can later be used to calculate a p-value by ordering all the BF values and then calculate the fraction of all permuted BF values smaller than the gene's observed BF. This p-value calculation incorporates the multiple testing correction and takes into account the potential for genes with more SNPs to overfit. Further analysis to assess whether the common associations for both age groups are shared or not was also carried out to determine if each gene is potentially affecting the same biological mechanism.

The samples for the genome-wide genotyping included 613 TB patients and 727 healthy controls; 206 cases were less than 45 years old, our empirical age threshold to identify young TB subjects based on the distribution of age at onset of TB in Thailand [13]. Statification by TB strain was also carried out with a total of 182 and 184 subjects with ancient and modern TB strains, respectively as well as stratification by TB lineage with a total of 140, 181, and 45 Beijing, East African-Indian (EAI), and "other" subjects, respectively. The patients were recruited from Chian Rai, Lampang, and Bangkok provinces of Thailand due to the high similarity of their populations [14]. All cases were human immunodeciency virus-seronegative when TB was diagnosed and later confirmed by microscopic identification or mycobacterial culture. The genotyping was performed using Illumina Hapmap 610 chip (Illumina, San Diego, CA, USA). For each gene, we excluded subjects with missing genotype values for any of the SNPs within it since the logic regression package cannot deal with missing values. Standard quality control was performed including Hardy-Weinburg equilibrium cutoff at p-value $< 10^{-5}$ and minimum allele frequency of 0.05. Multidimensional scaling of pairwise identity by state statistics was carried out using GenABEL package [15] and indicated three outlier samples, which were excluded. The genomic inflation factor (λ) was calculated from trend test p-values; at $\lambda = 1.02$ the level of population stratification was acceptable.

3.3 Results

The number of old and young TB cases is shown in Table 3.1 and Table 3.2, respectively, stratified by strain and lineage for those cases with available

relevant information. Lineage and strain information was not available for 247 cases. It can be observed that all Beijing cases and most "other" lineage cases were modern TB strain holders while all EAI cases were ancient TB strain holders.

	Ancient strain	Modern strain
Beijing	0	76
EAI	135	0
Other	0	24

Table 3.1: Number of old TB cases by lineage and strain.

Table 3.2: Number of young TB cases by lineage and strain.

	Ancient strain	Modern strain
Beijing	0	64
EAI	44	0
Other	1	20

3.3.1 Age-stratified analysis

We examined 18,278 genes. Out of these, 6 were found to have a strong assocation with young TB cases and 3 with old TB cases with an overlap of 2 genes among those. A summary of the findings can be found in Table 3.3. Genes ZFHX1B and FER showed a strong association with both age groups so we decided to investigate further whether the association is shared or distinct among them. Further analysis showed that the association with each gene is highly likely to be shared as shown in the Figure 3.1 since both age groups seem to be equally distant from control group and close to each other.

The shared gene ZFHX1B encodes zinc finger E-box-binding homeobox 2 proteins and has been associated with several congenital neural disorders at different levels such as Mowat-Wilson syndrome, congenital heart disease, hypospadias, and renal tract anomalies [16]. Gene emphFER encodes protooncogene tyrosine kinase protein which participates in intracellular signalling or differentiation processes [17].

Table 3.3: Genes with the strongest evidence of association	with ei-
ther young or old TB risk with chromosomal locations and	approx-
imate p-values.	

Gene	Location	Young TB p-value	Old TB p-value
ZFHX1B	2q22.3	$< 2.73 \times 10^{-6}$	$< 2.73 \times 10^{-6}$
FER	5q21.3	$< 2.73 \times 10^{-6}$	$< 2.73 \times 10^{-6}$
DAB2IP	9q33.2	3.56×10^{-5}	0.808
GNAQ	9q21.2	6.57×10^{-5}	0.364
C8orf48	8p22	$7.93 imes 10^{-5}$	0.155
C11orf16	11p15.4	8.21×10^{-5}	0.616
SH3MD2	4q32.3	9.03×10^{-5}	0.195

Table 3.4: Logic structures, frequencies, and associated old-TB odds ratios of the ZFHX1B gene

SNP	rs2052807	rs7568133	rs7565134	rs2162571	rs7565134			
Genotype	AA	AA	AA	AA	AA or AG	1	Logic-based	l
Cases	73 (18.11%)	50 (12.41%)	119(29.53%)	266 (66.00%)	223 (55.33%)	F	Risk Group	3
Controls	114 (15.90%)	76 (10.60%)	399(55.65%)	489 (68.20%)	522 (72.80%)			
Logic 1	(AN	D)				Free	quency	OR
Logic 2			((OR) .	AND)	Cases	Controls	
	Logic 1	= NO		Logic 2 = NO			282	3.33
Logic-based	Logic 1	= YES	Logic 2 = NO			9	1	31.61
Risk Groups	Logic 1	= NO	Logic $2 = YES$			123	482	1.00
	Logic 1	= YES		Logic $2 = YES$		4	2	7.02

Table 3.5: Logic structures, frequencies, and associated young-TB odds ratios of the ZFHX1B gene

SNP	rs17738837	rs12691693	rs3770305	rs6738630	rs7565134			
Genotype	AA	AG or GG	AG or GG	AA	AG or GG	L	ogic-based	
Cases	182 (88.78%)	155 (75.61%)	195 (95.12%)	312 (19.02%)	147 (71.71%)	R	isk Groups	
Controls	609 (84.94%)	515 (71.83%)	678 (94.56%)	118 (16.46%)	318 (44.35%)	1		
Logic 1	((((OR) AND) OR)				Fre	quency	OR
Logic 2						Cases	Controls	
		Logic 1 = NO				0	32	0.00
Logic-based		Logic $2 = NO$	58	367	1.00			
Risk Groups	Logic 1 = NO				Logic $2 = YES$	0	17	0.00
		Logic 1	= YES		Logic 2 = YES	147	301	3.09

Table 3.6: Logic structures, frequencies, and associated old-TB odds ratios of the FER gene

SNP	rs4957798	rs9326759	rs4957798	rs9326761	rs17391678			
Genotype	GG	AA or AG	AG or GG	AG or GG	AC or CC	L	ogic-based	
Cases	247 (61.44%)	74 (18.41%)	358 (89.05%)	114 (28.36%)	37 (9.20%)	R	isk Groups	
Controls	292 (40.44%)	139(19.25%)	541 (74.93%)	260 (36.01%)	105 (14.54%)			
Logic 1	((OR) .	AND)			Free	quency	OR
Logic 2				(0	R)	Cases	Controls	
	Logic $1 = NO$		Logic $2 = NO$		78	220	1.00	
Logic-based	Logic 1 = YES		Logic 2	2 = NO	200	198	2.85	
Risk Groups		Logic $1 = NO$		Logic 2	= YES	16	119	0.38
		Logic $1 = YES$		Logic 2	= YES	108	185	1.65

Table 3.7:	Logic	structures,	frequencies,	and	associated	young-TB
odds rati	os of th	ie FER gene	e			

SNP	rs11952637	rs9326745	rs4957798	rs12657495	rs6875865			
Genotype	GG	GG	AA or AG	AG or GG	GG	I	logic-based	
Cases	113 (54.33%)	81 (38.94%)	87 (41.83%)	42 (20.19%)	86 (41.35%)	R	tisk Groups	
Controls	446 (61.77%)	333 (46.12%)	430(59.56%)	210 (29.09%)	304 (42.11%)]		
Logic 1	((OR) .	AND)			Fre	quency	OR
Logic 2				(AN	ND)	Cases	Controls	
		Logic $1 = NO$		Logic 2	2 = NO	168	365	1.00
Logic-based	Logic 1 = YES		Logic 2	2 = NO	32	277	0.25	
Risk Groups	Logic $1 = NO$		Logic 2	= YES	6	51	0.26	
		Logic $1 = YES$		Logic 2	= YES	2	29	0.15



(a) ZFHX1B

(b) FER

Figure 3.1: Distance plots of genes ZFHX1B and FER for age-stratified TB subgroups. † indicates statistical significance.

3.3.2 Strain-stratified analysis

We found 7 genes strongly associated with either modern or ancient strains of TB although only gene ZFHX1B achieved statistical significance in the ancient strain group. A summary of the results can be found in Table 3.8. The consistent appearance of genes ZFHX1B and FER as top genes between the age-stratified and strain-stratified analyses suggests these genes play an important role in the disease etiology and a potential common biological mechanism acting on these subgroups.

Figure 3.2 presents the results of the analysis performed to assess whether the ZFHX1B and FER associations are shared between the two subgroups based on the strain stratification. The strain-stratified analysis shows a potential common susceptibility between ancient and modern TB strains as illustrated by the distance to the control group from both disease subgroups and the relatively small separation between the two disease subgroups.

To further analyze the ZFHX1B and FER gene-disease associations, we constructed the logic tables of each individual subgroup model. The odds ratios range from 0 to 26.89 with p-value of 0.130 and from 2.97 to 18.75 with p-value of 1.09×10^{-5} associated to FER gene in the modern and ancient TB strains, respectively. The odds ratios range from 0.18 to 0.68 with p-value of 0.157 and from 2.77 to 8.95 with p-value of $< 3.8 \times 10^{-6}$ associated to ZFHX1B gene in the modern and ancient TB strains, respectively.

Table 3.8: Genes with the strongest evidence of association with either ancient or modern TB strain risk with chromosomal locations and approximate p-values.

Gene	Location	Modern TB p-value	Ancient TB p-value
ZFHX1B	2q22.3	0.157	$< 3.8 \times 10^{-6}$
FER	5q21.3	0.130	1.09×10^{-5}
LOC646024	6q25.1	0.168	1.37×10^{-5}
LOC387720	10q26.2	8.21×10^{-6}	0.822
FAM77C	1p35.2	2.19×10^{-5}	0.960
LOC646952	1p21.2	2.19×10^{-5}	0.265
SALF	2p16.3	6.84×10^{-5}	0.462

Controls → Ancient^{*}→ - ← Modern

Controls -----

Ancient → 🔹 🕶 Modern

(a) ZFHX1B strain-stratified

(b) FER strain-stratified

Figure 3.2: Distance plots of genes ZFHX1B and FER for strain-stratified TB subgroups.

† indicates statistical significance.

Table 3.9: Logic structures, frequencies, and associated ancient TB strain odds ratios of the ZFHX1B gene

SNP	rs2052807	rs13002663	rs12691693	rs13413446	rs7565134			
Genotype	AA or AC	GG	AA	GG	AG or GG	L	ogic-based	
Cases	118 (65.56%)	62(34.44%)	130 (72.22%)	Risk Groups				
Controls	439(61.4%)	229 (32.03%)	316 (44.20%)					
Logic 1	(01	R) AN		Frequency		OR		
Logic 2						Cases	Controls	
		Logic 1	= NO		Logic $2 = NO$	34	341	1.00
Logic-based		Logic 1 :	= YES		Logic $2 = NO$	16	58	2.77
Risk Groups		Logic $1 = NO$				97	279	3.49
		Logic 1 :	= YES		Logic $2 = YES$	- 33	37	8.95

Table 3.10: Logic structures, frequencies, and associated modern TB strain odds ratios of the ZFHX1B gene

SNP	rs13413446	rs4662223	rs7599224	rs7565134	rs1365778				
Genotype	AG or GG	AA or AG	AA or AC	AG or GG	AG or GG	L	ogic-based		
Cases	73 (40.33%)	73 (40.33%) 66 (36.46%) 145 (80.11%) 110 (60.77%)					Risk Groups		
Controls	274 (38.82%)	74 (38.82%) 260 (36.36%) 534 (74.69%) 316 (44.20%) 4					1		
Logic 1	((OR)	AND)	OR		Frequency		OR	
Logic 2						Cases	Controls		
		Logic 1	= NO		Logic $2 = NO$	5	73	0.18	
Logic-based		Logic 1	= YES		Logic $2 = NO$	46	180	0.68	
Risk Groups		Logic 1 = NO				18	162	0.30	
		Logic 1	= YES		Logic $2 = YES$	112	300	1.00	

Table 3.11:	Logic structu	ires, freque	ncies, and	associated	ancient	\mathbf{TB}
strain odd	s ratios of the	e FER gene	÷			

SNP	rs4616948	rs17161562	rs17473831	rs4957798	rs9326761			
Genotype	GG	GG AA AC or CC			AA	Logic-based		
Cases	147 (81.22%) 147 (81.22%) 178 (98.34%)			110 (60.77%)	126 (69.61%)	Risk Groups		5
Controls	602 (83.61%)	502 (83.61%) 612 (85.00%) 720 (100.00%)			291 (40.42%) 461 (64.03%)			
Logic 1	((((OR) AND)					Frequency	
Logic 2					ID)	Cases	Controls	
		Logic 1 = NO		Logic 2	l = NO	11	4	18.75
Logic-based		Logic $1 = YES$	3	Logic $2 = NO$		72	491	1.00
Risk Groups		Logic 1 = NO			= YES	1	0	Inf
		Logic $1 = YES$	3	Logic 2	= YES	97	225	2.94

Table 3.12: Logic structures, frequencies, and associated modern TB strain odds ratios of the FER gene

SNP	rs10477929	rs12657495	rs9326758	rs3797838	rs9326758			
Genotype	AA	AG or GG	AA	1	Logic-based	l		
Cases	115 (62.84%)	115 (62.84%) 44 (24.04%) 7 (3.83%) 60 (32.79%)				Risk Groups		
Controls	491 (68.19%)	210 (29.17%)	10 (1.39%)	224 (31.11%)	10 (1.39%)			
Logic 1	AND	O ((OF	а) А	ND)		Frequency		OR
Logic 2						Cases	Controls	
		Logic 1	= NO		Logic $2 = NO$	176	676	1.00
Logic-based		Logic 1 :	= YES		Logic $2 = NO$	0	34	0.00
Risk Groups		Logic $1 = NO$				7	1	26.89
		Logic 1 =	= YES		Logic $2 = YES$	0	9	0.00

3.3.3 Lineage-stratified analysis

We found 5 genes strongly associated with either Beijing, EAI or *other* lineages of TB. Two genes achieved statistical significance in the EAI lineage subgroup, one gene in the Beijing lineage subgroup, and no gene in the *other* lineage subgroup. A summary of the results can be found in Table 3.13. The consistent appearance of genes ZFHX1B and FER as top genes among the age-stratified, strain-stratified, and lineage-stratified analyses keeps adding evidence that these genes play an important role in the disease etiology and a potential common biological mechanism acting on these subgroups.

Figure 3.3 presents the results of the analysis performed to assess whether the ZFHX1B and FER associations are shared between the three subgroups based on the lineage stratification. The lineage-stratified analysis shows a potential common susceptibility between Beijing and other TB lineages but different than the susceptibility to EAI lineage as illustrated by the close distance between Beijing and other subgroups and the significant separation between these two subgroups and the EAI lineage.

To further analyze the ZFHX1B and FER gene-disease associations, we constructed the logic tables of each individual subgroup model. The odds ratios range from 0 to 4.81 with p-value of $< 3.8 \times 10^{-6}$, from 2.97 to 17.05 with p-value of 0.127, and from 0.06 to 2.15 with p-value of 0.171 associated to FER gene in the EAI, Beijing, and other TB lineages, respectively. The odds ratios range from 0.21 to 1.68 with p-value of $< 3.8 \times 10^{-6}$, from 0.63 to 3.81 with p-value of 0.058, and from 0.00 to 15.79 with p-value of 0.165 associated to ZFHX1B gene in the EAI, Beijing, and other TB lineages, respectively.

Gene	Location	Beijing lineage	EAI lineage	Other lineage
		TB p-value	TB p-value	TB p-value
ZFHX1B	2q22.3	0.058	$< 3.8 \times 10^{-6}$	0.165
FER	5q21.3	0.127	$< 3.8 \times 10^{-6}$	0.171
LOC646024	6q25.1	0.141	5.47×10^{-6}	0.327
FAM77C	1p35.2	$< 3.8 \times 10^{-6}$	0.971	0.090
RGS6	14q24.2	0.428	0.976	6.29×10^{-5}

Table 3.13: Genes with the strongest evidence of association with TB risk in Beijing, EAI, and *other* lineages with chromosomal locations and approximate p-values.



(a) ZFHX1B lineage-stratified (b) FER lineage-stratified

Figure 3.3: Distance plots of genes ZFHX1B and FER for lineage-stratified TB subgroups.

† indicates statistical significance.

Table 3.14: Logic structures, frequencies, and associated EAI-lineage TB odds ratios of the ZFHX1B gene

SNP	rs7565134	rs1365778	rs10185359	rs7599224	rs12691693			
Genotype	AA	AA or AG	AA or AG	AA or AC	AG or GG	L	logic-based	
Cases	50 (27.93%)	50 (27.93%) 143 (79.89%) 75 (41.90%) 1			118 (65.92%)	Risk Groups		
Controls	399(55.80%)	99 (55.80%) 606 (84.76%) 293 (40.98%)			513 (71.75%)			
Logic 1	(A	(AND (OR))				Free	quency	OR
Logic 2					ND)	Cases	Controls	
		Logic $1 = NO$		Logic 2	2 = NO	69	126	1.68
Logic-based		$\frac{1}{\text{Logic 1} + \text{YES}}$			2 = NO	25	180	0.43
Risk Groups		Logic $1 = NO$			= YES	72	221	1.00
		Logic $1 = YES$		Logic 2	= YES	13	188	0.21

Table 3.15:	Logic	structures,	frequencies,	and	associated	Beijing-
lineage TB	odds 1	ratios of the	ZFHX1B gei	ne		

SNP	rs7600752	rs7565134	rs7568133	rs10185359	rs10196335				
Genotype	AA or AG	GG	AA or AG	AA	L	ogic-based			
Cases	115 (83.94%)	115 (83.94%) 59 (43.07%) 68 (49.64%) 56 (40.88%)					Risk Groups		
Controls	549 (76.78%)	193 (26.99%)	329 (46.01%)	293 (40.98%)	115(16.06%)	1			
Logic 1	((OR)	AND)	OR		Fre	quency	OR	
Logic 2						Cases	Controls		
		Logic 1	= NO		Logic 2 = NO	79	525	1.00	
Logic-based		Logic 1	= YES		Logic $2 = NO$	43	75	3.81	
Risk Groups		Logic 1	Logic $2 = YES$	8	84	0.63			
		Logic 1	= YES		Logic $2 = YES$	7	31	1.50	

Table 3.16: Logic structures, frequencies, and associated *other*lineage TB odds ratios of the ZFHX1B gene

ſ	SNP	rs13413446	rs1035822	rs3928425	rs7599224	rs7565134				
	Genotype	AG or GG	AA or AG	AA	CC	AA	1	Logic-based		
ĺ	Cases	23 (51.11%)	20 (22.22%)	31 (68.89%)	6 (13.33%)	18 (40.00%)	F	Risk Group	s	
Ī	Controls	274 (38.32%)	73 (10.21%)	405 (56.64%)	181 (25.31%)	399 (55.80%)	1			
ĺ	Logic 1	((A	ND)	AND)			Free	quency	OR	
ĺ	Logic 2				(AN	ND)	Cases	Controls		
			Logic $1 = NO$		Logic 2	2 = NO	38	600	1.00	
	Logic-based		Logic $1 = YES$	5	Logic 2	2 = NO	7	7	15.79	
	Risk Groups		Logic $1 = NO$		Logic 2	= YES	0	103	0.00	
			Logic $1 = YES$	5	Logic 2	= YES	0	5	0.00	

Table 3.17: Logic structures, frequencies, and associated EAI-lineage TB odds ratios of the FER gene

SNP	rs4616948	rs17161562	rs17473831	rs4957798	rs9326761			
Genotype	GG	AA	AC or CC	GG	AA	1	Logic-based	l
Cases	147 (81.67%)	147 (81.67%) 146 (81.11%) 177 (98.33%)			126 (70.00%)	Risk Groups		s
Controls	602 (83.61%)	612 (85.00%)	720 (100.00%)	291 (40.42%)	461 (64.03%)			
Logic 1	((((AND) OR)					quency	OR
Logic 2				(0	R)	Cases	Controls	
		Logic 1 = NO		Logic 2	2 = NO	10	4	17.05
Logic-based		Logic $1 = YES$	5	Logic 2	2 = NO	72	491	1.00
Risk Groups		Logic $1 = NO$			= YES	1	0	Inf
		Logic $1 = YES$	5	Logic 2	= YES	97	225	2.94

Table 3.18:Logic structures, frequencies, and associated Beijing-lineage TB odds ratios of the FER gene

SNP	rs9326745	rs4365877	rs10477929	rs4957798	rs9326758			
Genotype	GG	GG	GG	AA or AG	AG or GG	L	ogic-based	
Cases	56 (40.29%)	37 (26.62%)	132 (94.96%)	Risk Groups				
Controls	333 (46.25%)	243 (33.75%)	13(1.81%)	710 (98.61%)	1			
Logic 1	((OR) .	AND)		Free	quency	OR	
Logic 2						Cases	Controls	
		Logic 1	= NO		Logic $2 = NO$	7	7	4.81
Logic-based		Logic 1 :	= YES		Logic $2 = NO$	0	3	0.00
Risk Groups		Logic 1	= NO	Logic $2 = YES$	132	635	1.00	
		Logic 1 =	= YES		Logic $2 = YES$	0	75	0.00

Table 3.19: Logic structures, frequencies, and associated *other*lineage TB odds ratios of the FER gene

SNP	rs7710223	rs4957798	rs7710223	rs7737443	rs7715208				
Genotype	AA or AG AG or GG G		GG	AA or AC	A or AC AA		Logic-based		
Cases	32(71.11%)	41 (91.11%)	13 (28.89%)	34 (75.56%) 38 (84.44%)		Risk Groups			
Controls	554 (76.94%)	539 (74.86%)	166 (23.06%)	554 (76.94%)	572 (79.44%)				
Logic 1	((OR) OR)					Frequency (OR	
Logic 2				(OR)		Cases	Controls		
	Logic $1 = NO$			Logic $2 = NO$		1	229	0.06	
Logic-based	Logic $1 = YES$			Logic $2 = NO$		31	411	1.00	
Risk Groups	Logic 1 = NO			Logic 2 = YES		13	80	2.15	
	Logic 1 = YES			Logic 2 = YES		0	0		

3.4 Discussion

The results of these gene-level analyses illustrate the power of logic-regression to uncover multiple-SNP interactions that could potentially explain the genetics of complex traits. We found strong evidence of association of 13 newly identified genes with different strains, lineages, and age groups of TB that traditional single-SNP analysis have not been able to uncover, explaining to a greater extent the genetics of TB.

Genes *FER* and *ZFHX1B* were found to be consistently associated with different age groups as well as specific strains and lineages. Gene *FER* has been found to encode a member of the FPS/FES protein-tyrosine kinase family. It is involved in the regulation of cell-cell adhesion as well as the mediation of signaling from the cell surface to the cytoskeleton [18]. Gene *ZFHX1B* encodes protein zinc finger E-box-binding homeobox 2 and mutations of this gene has been associated with Mowat-Wilson syndrome which is characterized by a number of defects such as microcephaly, mental retardation, and epilepsy, among others [19].

For our analyses, we reduced the computational intensity by limiting the case-control label permutations to 20, number of SNPs interacting to a maximum of 5, and number of logic trees to 2. These limitations make the search not comprehensive as there might be higher-order interactions that could explain the genetic TB-risk. Nevertheless, the structure permits an approximate of more complex interaction structures, far closer to them than the single-SNP analysis could approximate.

False positive results are a common concern in GWASs due to the large number of tests performed. Findings should be further validated in order to rule-out spurious associations due to population stratification or genotyping errors [20]. An alternative to reduce the computational demand of logic regression applied to data-driven approaches such as GWAS is to use a candidategenes analysis by just analyzing the highly significant genes in the primary GWAS. Adequate phenotyping is also a major concern in this type of studies to be able to discover new genetic associations. Special attention should be paid to GWAS of infectious diseases due to the possibility of controls becoming cases later on as well as the definition used as the findings can be highly sensitive to these factors [21].

Increasing attention has been paid to pathway analysis in GWAS [22]. This approach is biologically appealing because it would incorporate geneinteractions that are not currently being captured by our approach. Logic regression has the potential to be extended to pathway-level analysis but the computational requirements would be too demanding given the dimensionality of the solution space and the necessity of minimizing the possibility of converging to a local optimum. There would also be a need to incorporate biological knowledge to the pathway analysis to understand how genes interact within the pathway in order to model the interactions accurately [23].

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Chapter 4 Conclusions

4.1 Review of Hypotheses

Chapter 2

- P-values alone do not provide enough information to assess whether a genetic association is shared among a group of diseases and can lead to inaccurate inferences. – We found evidence that inferences based solely on p-values tend to overestimate the degree of sharedness of genetic associations among a group of diseases since the association might be in opposite direction, in different magnitude, and/or biologically different.
- Taking into account strength, direction, and similarity of the biological association provide better insight and a stricter definition of the sharedness of genetic associations among a group of diseases. – We found evidence that by taking into account strength, direction, and similarity of the biological association we were able to detect some disimilarities among commonly reported "shared" genetic susceptibilities. Furthermore, we found evidence that some shared associations might exist among groups of diseases that the traditional approach

wouldn't have been able to uncover if the association is not found statistically significant in one of the diseases.

Chapter 3

- SNP-SNP interactions are responsible for a proportion of the TB susceptibility and explain to a greater extent the TB genetics. We found evidence of 3 genes statistically significantly associated with different TB subgroups that, to our knowledge, haven't been reported before. Additionally, we found evidence of an additional 11 genes which were strongly associated with different TB subgroups but did not achieve statistical significance. These findings contribute to the understanding of TB genetic susceptibility.
- Some of the genetic susceptibilities are shared while others are unique for certain TB subgroups. – We found evidence that the two most statistically significant gene-disease associations, ZFHX1B and FER, were shared between > 45 and \leq 45 TB age subgroups as well as ancient and modern TB strains while these associations seem to be different among TB lineage subgroups.

4.2 Discussion

As mentioned in Chapter 2, our methodology proposed is based on a strict definition of "shared" association since we take into account not only direction and strength of the gene-disease associations, but also incorporate the structure of how a set of SNPs of a gene are associated with the diseases. This strict definition of "shared" association was used because even if a gene is statistically significantly associated with 2+ diseases, with the same odds ratio magnitude and direction, it does not mean they share the same biological association.

The stricter definition of a "shared" association used in this thesis uncovered that the traditional approach which focuses mainly on p-values overestimate the degree of sharedness. Our analysis showed that only 11 out of 158 genes that achieved statistical significance in at least one out of the three (CD, RA, T1D) GWASs could be stated as "shared" associations between 2 or more diseases. All the other genes showed hints of a certain degree of uniqueness in the association either because of the strength, direction or the SNP-SNP interactions within the gene.

The methodology has certain limitations when compared to other approaches such as the need of using the same genotyping platform and access to the raw data. The simplest way to perform the analysis in this scenario is to only use matching SNPs across the different platforms, but this might substancially reduce the number of available SNPs in the analysis. Another way to deal with different genotyping platforms is to perform an imputation process although it is computationally intensive procedure and requires specific knowledge of how to perform it.

In Chapter 3 we found that genes FER and ZFHX1B were consistently associated with different age groups as well as specific strains and lineages. To our knowledge, these genes have not been reported to be associated with TB before. The role of gene FER has been found to be encoding a member of the FPS/FES protein-tyrosine kinase family and it is involved in the regulation of cell-cell adhesion as well as the mediation of signaling from the cell surface to the cytoskeleton [1]. GeneZFHX1B encodes protein zinc finger Ebox-binding homeobox 2 and mutations of this gene has been associated with Mowat-Wilson syndrome which is characterized by a number of defects such as microcephaly, mental retardation, and epilepsy, among others [2].

The discovery of these two novel gene susceptibilities for TB keeps adding evidence of the power of logic regression to uncover new gene-disease associations and help explain to a greater extent the genetics of complex diseases that traditional SNP-level GWAS cannot achieve. For our analyses, we reduced the computational demand by permuting the case-control label only 20 times, fixing the number of SNPs interacting to a maximum of 5 as well as the number of logic trees to 2. These restrictions make the random search not comprehensive since there might be more interactions that could better explain the genetic TB-risk. Still, the model specifications used can be used as an approximate of more complex structures.

Regarding the findings in Chapter 3, false positive results are a common concern in GWASs due to the large number of tests performed. Since the analysis is not hypothesis-driven, these findings should be validated in order to rule-out the possibility of spurious associations due to population stratification or genotyping errors. Additionally, GWAS of infectious diseases are prone to the possibility of controls getting infected and become cases later in time so the findings can be biased because of these factors as well as the protocol used to identify cases [3].

4.3 Future Work

Further research aims to extend the shared gene analysis to other groups of diseases which are more challenging and time consuming due to the different platforms used for genotyping the subjects. Additionally, we need to perform a replication study to confirm our TB findings in order to rule out the possibility of spurious association due to population stratification and other factors.

Specifically, some of the research goals that arose from the work presented in this thesis are:

- To enable to quantify the degree of sharedness of the gene-disease associations and perform the appropriate statistical hypothesis tests
- Develop methods for handling multiple diseases GWASs with different genotyping platforms

• Replicate the TB study using new independent GWAS dataset

4.4 Conclusions

In conclusion, traditional analysis performed to assess whether genetic associations are shared or distinct among a group of diseases tend to overestimate the degree of sharedness because they rely mostly on p-values and statistical significance. Our approach considers a stricter definition of a "shared association" since it takes into account not only strength and direction of the association, but also a complete biological similarity. We were able to uncover some interesting patterns in the gene-disease associations the traditional and recent novel approaches are not able to do. This provides a better insight of the biological mechanism acting on each disease.

Additionally, we were able to demonstrate the power of logic regression to uncover new genetic susceptibilities and explain to a greater extent the genetics of complex diseases. We found 3 newly identified genes that were statistically significant associated with different subgroups of TB: ZFHX1B, FER, and FAM77. We additionally identified 11 genes which were strongly associated with different subgroups of TB but did not achieve statistical significance at the GWAS level.

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Appendix A

R codes

A.1 Logic Regression – WTCCC

```
args=commandArgs(trailingOnly = TRUE);
ChrNum=as.numeric(args[1]);
GeneName=as.character(args[2]);
```

```
#Load the library
library('LogicReg')
```

#DATA LOADING AND GENE SELECTION#

```
#Load the genotype file of all 3 diseases
infile=paste('A01Chr',ChrNum,'.txt',sep='')
gene=read.table(infile,sep='\t',header=TRUE)
gene=gene[as.character(gene[,4])==GeneName,]
```

```
#Total phenotype vector matching the genotype file
respTotal=rbind(as.matrix(rep('Control', 2936)),
    as.matrix(rep('CD', 1748), as.matrix(rep('T1D', 1963)),
    as.matrix(rep('RA', 1860)))
```

#LOGIC REGRESSION SETUP#

```
#Logic regression parameters
nsnp=length(unique(geneCD[,1]))
leaf=min(nsnp,5)
trees=2
```

```
#Deviances calculation function of the
#phenotype vector and genotype matrix
devianceCalc = function(resp, gene, trees, leaf){
   set.seed(1)
   dev=rep(1000000,21)
```

```
#Deviances for the original response model
```

```
for (i in 1:20){
      myfit = logreg(resp=resp,bin=t(gene[,-c(1:4)]),
      type=3, select=1, ntrees=trees, nleaves=leaf)
      if (myfit$model$score<dev[1]){</pre>
        dev[1]=myfit$model$score
      }
  }
   #Deviances for the permuted response models
   for (i in 1:20) {
      respPerm=sample(resp,length(resp),replace=FALSE)
      for (j in 1:20) {
        myfit = logreg(resp=respPerm, bin=t(gene[, -c(1:4)]),
        type=3, select=1, ntrees=trees, nleaves=leaf)
         if (myfit$model$score<dev[i+1]){</pre>
           dev[i+1]=myfit$model$score
         }
      }
  }
  return (dev)
}
#THE CODE CALLS THE FUNCTION ABOVE 18 TIMES WITH
#DIFFERENT DATA SUBSETS AND PHENOTYPE VECTORS:
#dev1. CD & T1D vs. Controls
#dev2.. CD & RA vs. Controls
#dev3. T1D & RA vs. Controls
#dev4..... CD vs. T1D & Controls
#dev5..... CD vs. RA & Controls
#dev6..... T1D vs. CD & Controls
#dev7..... T1D vs. RA & Controls
#dev8..... RA vs. CD & Controls
#dev9..... RA vs. T1D & Controls
#dev10..... CD vs. T1D & RA
#dev11..... T1D vs. CD & RA
#dev12..... RA vs. CD & T1D
#dev13..... CD vs.
                      T1D
#dev14..... CD vs. RA
#dev15..... T1D vs. RA
#dev16..... CD vs. Controls
#dev17..... T1D vs. Controls
#dev18..... RA vs. Controls
deviance=cbind (dev1, dev2, dev3, dev4, dev5, dev6, dev7, dev8,
  dev9, dev10, dev11, dev12, dev13, dev14, dev15, dev16, dev17, dev18)
outfile=paste('dev_',GeneName,'.txt',sep='')
write.table(deviance,outfile,sep='\t',
  col.names=FALSE, row.names=FALSE, guote=FALSE)
```

A.2 Logic Regression – TB

args=commandArgs(trailingOnly = TRUE);

```
ChrNum=as.numeric(args[1]);
GeneName=as.character(args[2]);
#Load the library
library('LogicReg')
#DATA LOADING AND GENE SELECTION#
#Load the genotype file of all TB cases and controls
infile=paste('A01Chr', ChrNum, '.txt', sep='')
gene=read.table(infile, sep='\t', header=TRUE)
gene=gene[as.character(gene[, 4])==GeneName,]
#Load the phenotype file of all TB cases and controls
pheno=read.table('pheno extended.txt', sep='\t',
   header=TRUE, colClasses = 'character')
#Eliminate samples with missing values
keep=which(colSums(gene=='\00')==0)
gene=gene[,keep]
pheno=pheno[keep[5:length(keep)]-4,]
#Logic regression parameters
leaf=min(5, dim(gene)[1]/2)
bin=as.matrix(t(gene[,5:dim(gene)[2]]))
class(bin) = 'numeric'
#Deviances calculation function of the
#phenotype vector and genotype matrix
devianceCalc = function(resp, gene, trees, leaf){
   set.seed(1)
   dev=rep(100000,21)
   #Deviances for the original response model
   for (i in 1:20){
      myfit = logreg(resp=resp, bin=t(gene[, -c(1:4)]),
      type=3, select=1, ntrees=trees, nleaves=leaf)
      if (myfit$model$score<dev[1]){</pre>
         dev[1] =myfit$model$score
      }
   }
   #Deviances for the permuted response models
   for (i in 1:20) {
      respPerm=sample(resp,length(resp),replace=FALSE)
      for (j in 1:20){
         myfit = logreg(resp=respPerm,bin=t(gene[,-c(1:4)]),
         type=3, select=1, ntrees=trees, nleaves=leaf)
```

```
if (myfit$model$score<dev[i+1]){</pre>
           dev[i+1]=myfit$model$score
        }
     }
  }
  return (dev)
}
#THE CODE CALLS THE FUNCTION ABOVE 6+6+18 TIMES WITH
#DIFFERENT TB DATA SUBSETS AND PHENOTYPE VECTORS
#For the age-stratified analysis:
#dev1. \leq 45 & >45 vs. Controls
\#dev2..... \leq 45 vs. >45 & Controls
#dev3..... >45 vs. < 45 & Controls
#dev4.... \leq 45 vs. > 45
#dev5..... \leq 45 vs. Controls
#dev6..... >45 vs. Controls
dev_age=cbind(dev_age1, dev_age2, dev_age3, dev_age4, dev_age5, dev_age6)
outfile=paste('devAge_',GeneName,'.txt',sep='')
write.table(dev_age,outfile,sep='\t',
  col.names=FALSE, row.names=FALSE, quote=FALSE)
#For the strain-stratified analysis:
#dev1. modern & ancient vs. Controls
#dev2..... modern vs. ancient & Controls
#dev3..... ancient vs. modern & Controls
#dev4..... modern vs. ancient
#dev5..... modern vs. Controls
#dev6..... ancient vs. Controls
dev_strain=cbind(dev_strain1, dev_strain2, dev_strain3,
  dev_strain4, dev_strain5, dev_strain6)
outfile=paste('devStrain_',GeneName,'.txt',sep='')
write.table(dev_strain,outfile,sep='\t',
  col.names=FALSE, row.names=FALSE, quote=FALSE)
#For the lineage-stratified analysis:
#dev1.... Beijing & EAI vs. Controls
#dev2.. Beijing & Other vs. Controls
#dev3..... EAI & Other vs. Controls
#dev4..... Beijing vs. EAI & Controls
#dev5..... Beijing vs. Other & Controls
#dev6..... EAI vs. Beijing & Controls
#dev7..... EAI vs. Other & Controls
```

```
#dev8..... Other vs. Beijing & Controls
#dev9..... Other vs. EAI & Controls
#dev10..... Beijing vs. EAI & Other
#dev11..... EAI vs. Beijing & Other
#dev12..... Other vs. Beijing & EAI
#dev13..... Beijing vs. EAI
#dev14.... Beijing vs. Other
#dev15..... EAI vs. Other
#dev16.... Beijing vs. Controls
#dev17..... EAI vs. Controls
#dev18..... Other vs. Controls
dev_lin=cbind(dev_lin1, dev_lin2, dev_lin3, dev_lin4, dev_lin5,
  dev_lin6, dev_lin7, dev_lin8, dev_lin9, dev_lin10, dev_lin11,
  dev_lin12, dev_lin13, dev_lin14, dev_lin15, dev_lin16,
  dev_lin17, dev_lin18)
outfile=paste('devLineage_',GeneName,'.txt',sep='')
write.table(dev_lin,outfile,sep='\t',
  col.names=FALSE, row.names=FALSE, quote=FALSE)
```

Appendix B MATLAB codes

B.1 2D distance error calculation

function f = distance2D(x)
%Function receives as argument a vector size 3
%corresponding to the 3 non-fixed coordinates
%3 coordinates have to be fixed (to 0) to converge

```
%Declaration of dist as a global variable
%containing the standardized deviances
global dist
x(1) = x(1); %x-coordinate Disease #1
x(2) = x(2); %y-coordinate Disease #1
x(3) = x(3); %x-coordinate Disease #2
x(4) = 0; %y-coordinate Disease #2
x(5) = 0; %x-coordinate Controls
x(6) = 0; %y-coordinate Controls
%Disease #1 & Disease #2 vs Controls
f(1) = abs(sqrt((x(1)+x(3))/2-x(5))^2 + ...
   ((x(2)+x(4))/2-x(6))^2) - dist(1));
%Disease #1 vs Disease #2 & Controls
f(2) = abs(sqrt(((x(3)+x(5))/2-x(1))^2 + ...
   ((x(4)+x(6))/2-x(2))^2) - dist(2));
%Disease #2 vs Disease #1 & Controls
f(3) = abs(sqrt(((x(1)+x(5))/2-x(3))^2 + ...
   ((x(2)+x(6))/2-x(4))^2) - dist(3));
%Disease #1 vs Disease #2
f(4) = abs(sqrt((x(1)-x(3))^2 + (x(2)-x(4))^2) - dist(4));
%Disease #1 vs Controls
f(5) = abs(sqrt((x(1)-x(5))^2 + (x(2)-x(6))^2) - dist(5));
%Disease #2 vs Controls
f(6) = abs(sqrt((x(3)-x(5))^2 + (x(4)-x(6))^2) - dist(6));
%Return the sum of the vector of errors
f=sum(abs(f));
```

B.2 3D distance error calculation

```
function f = distance3D(x)
%Function receives as argument a vector size 7
%corresponding to the 7 non-fixed coordinates
%5 coordinates have to be fixed (to 0) to converge
%Declaration of dist as a global variable
%containing the standardized deviances
global dist
x(1) = x(1); %x-coordinate Disease #1
x(2) = x(2); %y-coordinate Disease #1
x(3) = x(3); %z-coordinate Disease #1
x(4) = x(4);  %x-coordinate Disease #2
x(5) = x(5);  %y-coordinate Disease #2
x(6) = x(6);  %z-coordinate Disease #2
x(7) = x(7); %x-coordinate Disease #3
x(8) = 0; %y-coordinate Disease #3
x(9) = 0; %z-coordinate Disease #3
x(10) = 0; %x-coordinate Controls
x(11) = 0; %y-coordinate Controls
x(12) = 0; %z-coordinate Controls
%Disease #1 & Disease #2 vs Controls
f(1) = pdist([x(1)/2+x(4)/2,x(2)/2+x(5)/2,x(3)/2+x(6)/2; ...
   x(10),x(11),x(12)],'euclidean') - dist(1));
%Disease #1 vs Disease #2 & Controls
f(2) = pdist([x(10)/2+x(4)/2,x(11)/2+x(5)/2,x(12)/2+x(6)/2; ...
   x(1),x(2),x(3)],'euclidean') - dist(2));
%Disease #2 vs Disease #1 & Controls
f(3) = pdist([x(1)/2+x(10)/2,x(2)/2+x(11)/2,x(3)/2+x(12)/2; \dots
   x(4),x(5),x(6)],'euclidean') - dist(3));
%Disease #1 & Disease #3 vs Controls
f(4) = pdist([x(1)/2+x(7)/2,x(2)/2+x(8)/2,x(3)/2+x(9)/2; ...
   x(10),x(11),x(12)],'euclidean') - dist(4));
%Disease #1 vs Disease #3 & Controls
f(5) = pdist([x(7)/2+x(10)/2,x(8)/2+x(11)/2,x(9)/2+x(12)/2; ...
   x(1),x(2),x(3)],'euclidean') - dist(5));
%Disease #3 vs Disease #1 & Controls
f(6) = pdist([x(1)/2+x(10)/2,x(2)/2+x(11)/2,x(3)/2+x(12)/2; ...
   x(7),x(8),x(9)],'euclidean') - dist(6));
%Disease #2 & Disease #3 vs Controls
f(7) = pdist([x(4)/2+x(7)/2,x(5)/2+x(8)/2,x(6)/2+x(9)/2; \dots
   x(10),x(11),x(12)],'euclidean') - dist(7));
%Disease #2 vs Disease #3 & Controls
f(8) = pdist([x(7)/2+x(10)/2,x(8)/2+x(11)/2,x(9)/2+x(12)/2; \dots
   x(4),x(5),x(6)],'euclidean') - dist(8));
%Disease #3 vs Disease #2 & Controls
f(9) = pdist([x(4)/2+x(10)/2,x(5)/2+x(11)/2,x(6)/2+x(12)/2; \dots
   x(7),x(8),x(9)],'euclidean') - dist(9));
```

```
%Disease #1 vs Disease #2 & Disease #3
f(10) = pdist([x(4)/2+x(7)/2,x(5)/2+x(8)/2,x(6)/2+x(9)/2; ...
   x(1),x(2),x(3)],'euclidean') - dist(10));
%Disease #2 vs Disease #1 & Disease #3
f(11) = pdist([x(1)/2+x(7)/2,x(2)/2+x(8)/2,x(3)/2+x(9)/2; ...
   x(4),x(5),x(6)],'euclidean') - dist(11));
%Disease #3 vs Disease #1 & Disease #2
f(12) = pdist([x(1)/2+x(4)/2,x(2)/2+x(5)/2,x(3)/2+x(6)/2; ...
   x(7),x(8),x(9)],'euclidean') - dist(12));
%Disease #1 vs Disease #2
f(13) = pdist([x(1), x(2), x(3); x(4), x(5), x(6)], \dots
   'euclidean') - dist(13));
%Disease #1 vs Disease #3
f(14) = pdist([x(1), x(2), x(3); x(7), x(8), x(9)], \dots
   'euclidean') - dist(14));
%Disease #2 vs Disease #3
f(15) = pdist([x(4), x(5), x(6); x(7), x(8), x(9)], \dots
   'euclidean') - dist(15));
%Disease #1 vs Controls
f(16) = pdist([x(1), x(2), x(3); x(10), x(11), x(12)], \dots
   'euclidean') - dist(16));
%Disease #2 vs Controls
f(17) = pdist([x(4), x(5), x(6); x(10), x(11), x(12)], \dots
   'euclidean') - dist(17));
%Disease #3 vs Controls
f(18) = pdist([x(7), x(8), x(9); x(10), x(11), x(12)], \dots
   'euclidean') - dist(18));
%Return the sum of the vector of errors
```

```
f=sum(abs(f));
```

B.3 2D Unconstrained Nonlinear Optimization

```
%Declaration of dist as a global variable
%containing the standardized deviances
global dist
%Initial solution guess set to 1's
x0=ones(1,3);
%Change sign of standardized deviances and make
%the remaining negatives ones to 0 + small cap
dist=max(-dist,zeros(1,6)+.01);
%Set maximum iterations to a big number and hide iteration details
options=optimset('MaxFunEvals',1000000,'Display','off');
%Get the solution
[x,fval] = fminunc(@distance2D,x0,options);
```

```
x=[x, zeros(1,3)];
```

B.4 3D Unconstrained Nonlinear Optimization

```
%Declaration of dist as a global variable
%containing the standardized deviances
global dist
```

```
%Initial solution guess set to 1's
x0=ones(1,7);
```

```
%Change sign of standardized deviances and make
%the remaining negatives ones to 0 + small cap
dist=max(-dist,zeros(1,18)+.01);
```

```
%Set maximum iterations to a big number and hide iteration details
options=optimset('MaxFunEvals',1000000,'Display','off');
```

```
%Get the solution
[x,fval] = fminunc(@distance2D,x0,options);
x=[x, zeros(1,5)];
```