

# From Adaptive Testing to Personalized Adaptive Testing:

Applications of Machine Learning Algorithms

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# Outline

1. Beyond adaptive testing
2. Recommender systems (RS)
3. Two RS applications in adaptive testing

Special Section  
on Europe Region



How AI and Science  
Are Shaping Each Other  
Global Supply Chain  
Disruption and Resilience  
Digital Twins and AI as Pillars of  
Personalized Learning Models



<https://dl.acm.org/toc/cacm/2022/65/4>

contributed articles

DOI:10.1145/3478281

**Personalized learning models can cut student dropout rates, boost student success, improve the integration of online and on-site students, better support teachers in mixed-teaching modalities, enhance accessibility, and more.**

BY MARCO FURINI, OMBRETTA GAGGI, SILVIA MIRRI,  
MANUELA MONTANGERO, ELVIRA PELLE, FRANCESCO POGGI,  
AND CATIA PRANDI

## Digital Twins and Artificial Intelligence

### as Pillars of Personalized Learning Models

MODERN EDUCATIONAL SYSTEMS have not really evolved enough to meet the needs of modern students.<sup>21</sup> No wonder, the percentage of dropouts from university studies is quite high (40% in the U.S. and 10% in Europe<sup>29</sup>). The university student profile has changed over the years. While yesterday's students were mainly full-time, today's students face challenges such as work commitments, family obligations, financial constraints, physical impairments, and learning models that do not adequately engage students or help them understand core concepts.<sup>11</sup> One might think that this issue concerns only those

who fail to complete their studies, but this is view is shortsighted. Today's educational system deficiencies will affect the welfare of tomorrow's society.

To improve current learning models, academic institutions around the world agree that the time has come to improve the world of education—moving from a traditional approach—where learning is standardized and available only to those with access to educational buildings—to a new paradigm that enables students to personalize their educational pathway, so they can progress at their own pace.<sup>19,21</sup> Future learning models must address key concerns, such as reducing dropout rates, supporting students with psycho-physical impairments, integrating on-site and online students, and personalizing the learning experience.

Digital twins—digital replicas of students—and artificial intelligence (AI) will be the pillars of innovation, accessibility, and personalization in future learning models.<sup>19</sup> The good news is that we can build these models today: AI algorithms have made great strides in recent years, and the use of technology in education has increased enormously. Indeed, while the COVID-19 pandemic has, on one hand, strongly hampered the learning process for many people around the world, it has, on the other

#### » key insights

- The time has come to revolutionize current educational systems, which are too rigid and cannot adequately support students who have work commitments, family obligations, financial constraints, and physical impairments.
- AI and digital-twin technology are helping to transform cities into smarter versions of themselves, supporting the Industry 4.0 revolution, and improving health services, but these technologies have rarely been used in the educational sector.
- AI and the digital-twin approach can be used to build personalized, inclusive, and accessible learning models. These models will have a tremendous social, cultural, and economic impact, and they will make it possible to meet some sustainable development goals set by the United Nations General Assembly.

IMAGE BY ANDRÉ J. BERNIS. ILLUSTRATION BY DEBORA VENTURI

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# Digital Twins and Artificial Intelligence

## as Pillars of Personalized Learning Models

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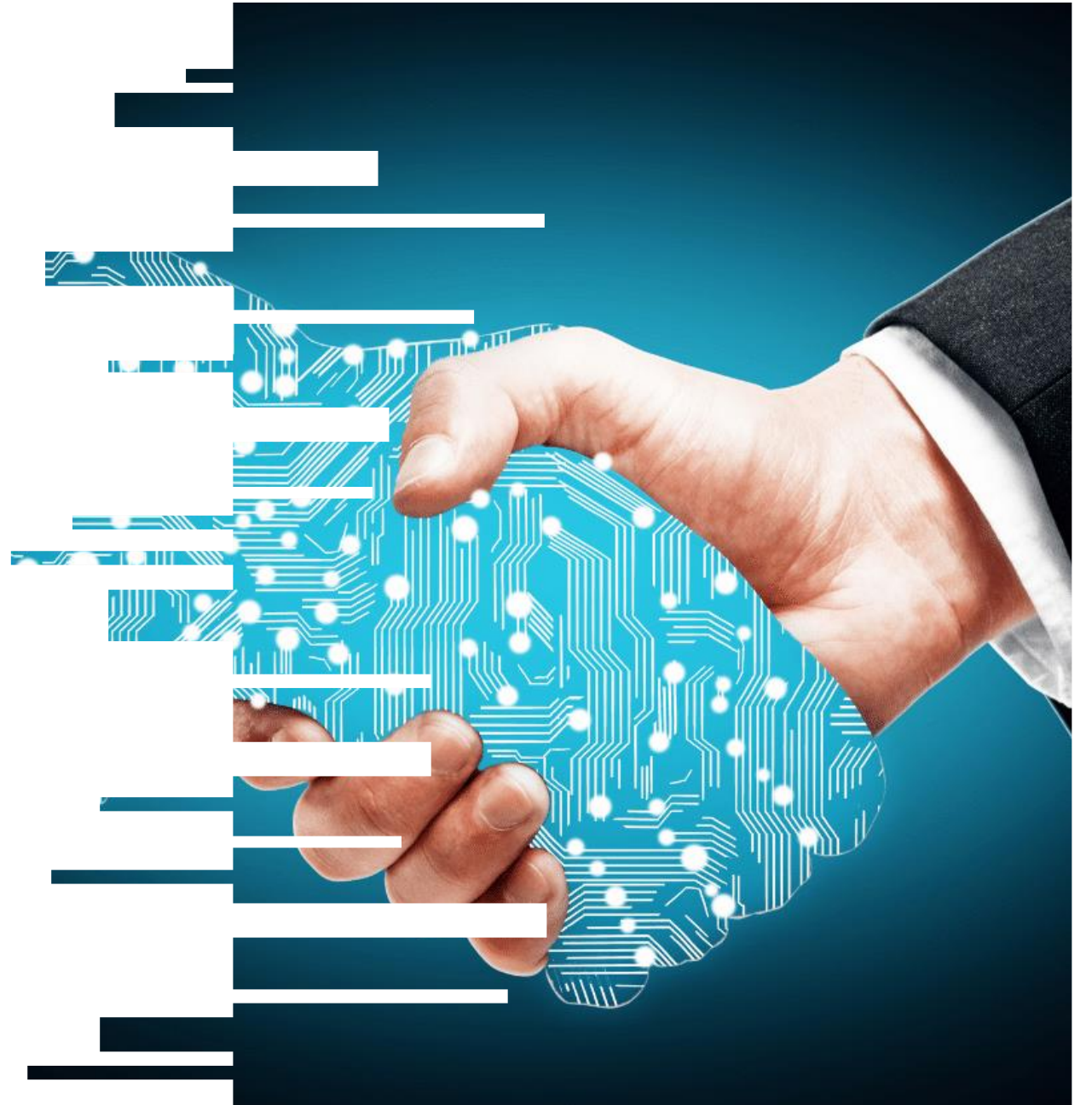
■ The time has come to revolutionize current educational systems, which are





“A **digital twin** is a digital replica of a physical entity, and it is created by combining pieces of data from various sources.”

[Furini et al. \(2022\)](#)



## STUDENT

- Academic background
- Study habits
- Subject preferences
- Cognitive characteristics
- Learning behaviors
- Digital educational material consumption



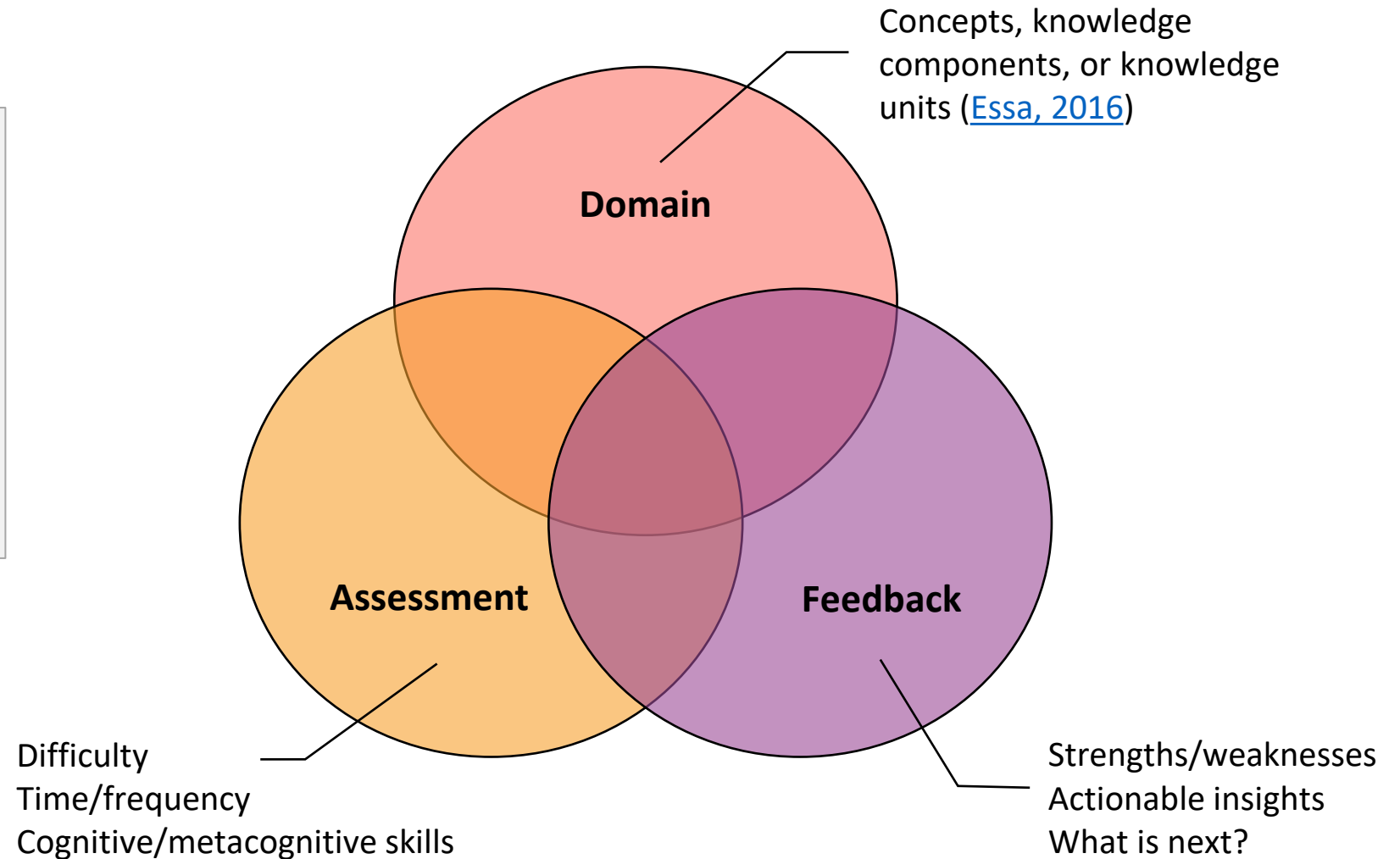
## DIGITAL TWIN

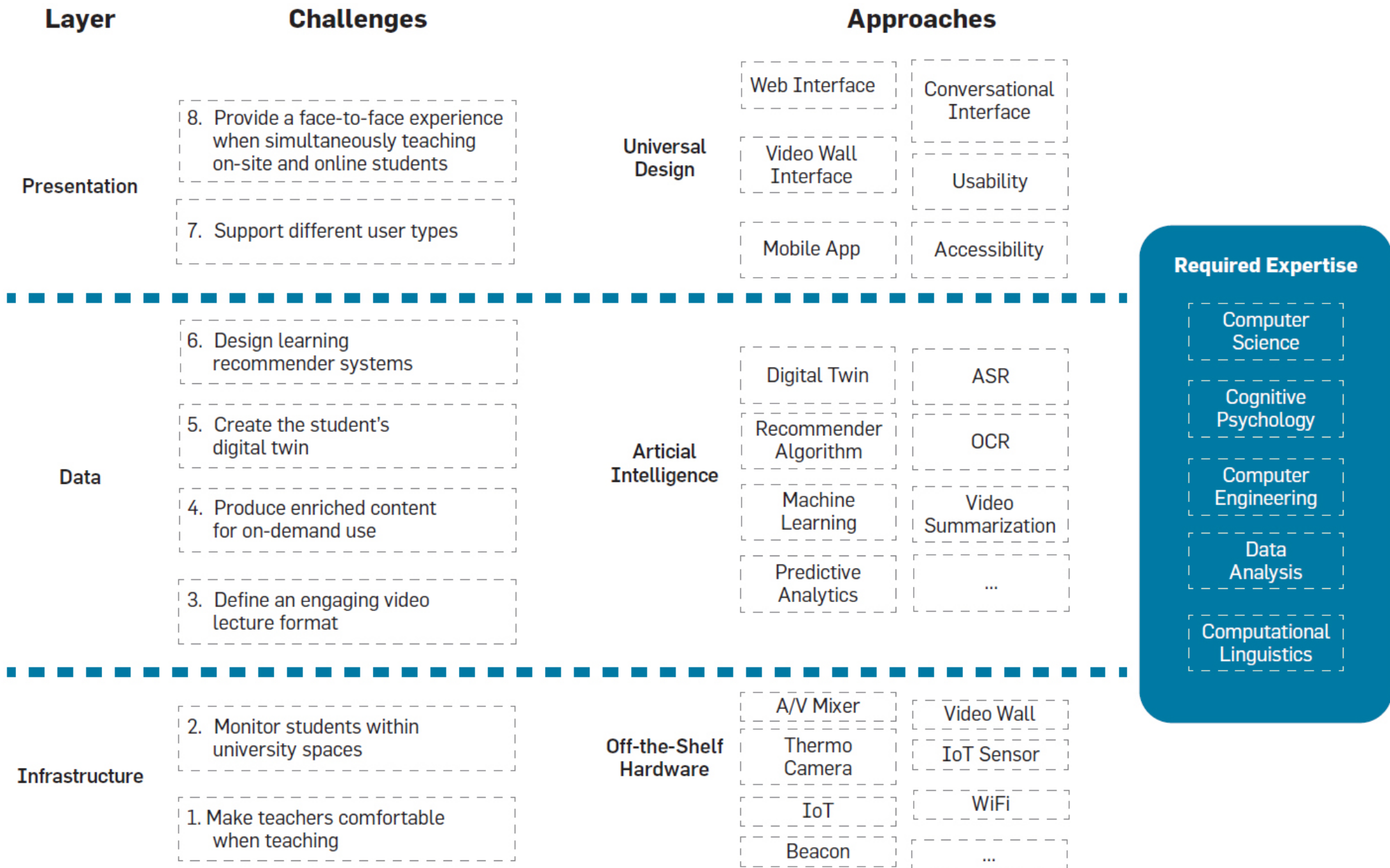
- Digital student records
- Online learning activities
- Digital learning behaviors
- Data from digital assessments
- Learner knowledge space
- Interactions with learning materials

# On the Road to Adaptive Learning Systems

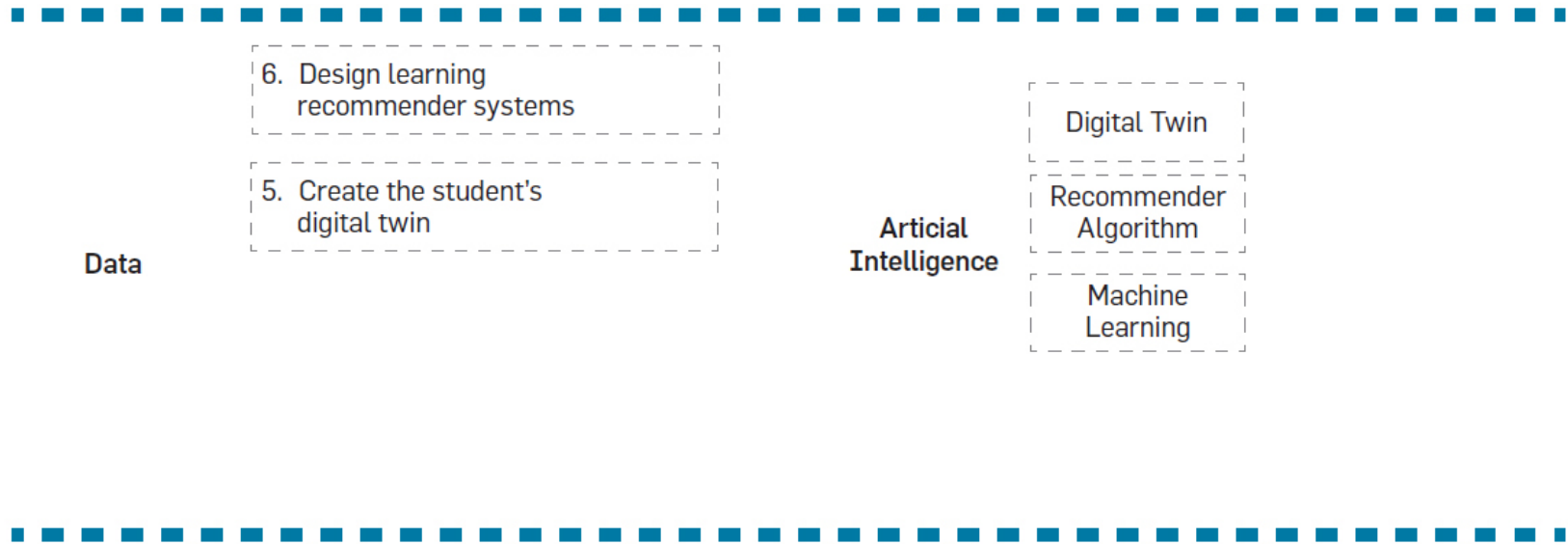
## **“Adaptive” Variables**

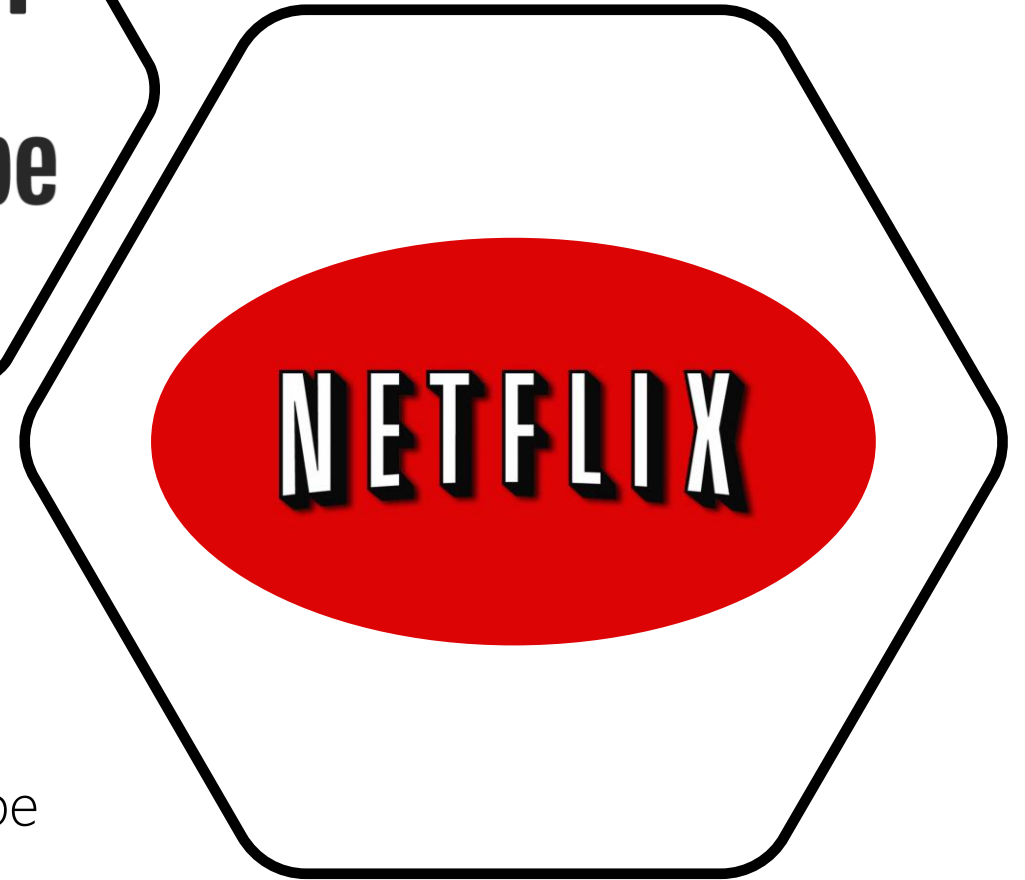
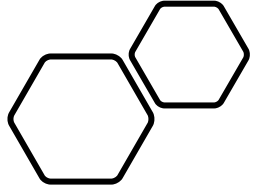
Cognitive learning styles  
Preferences and interests  
Learning progression  
Demographic variables  
([Triantafillou et al., 2007](#))





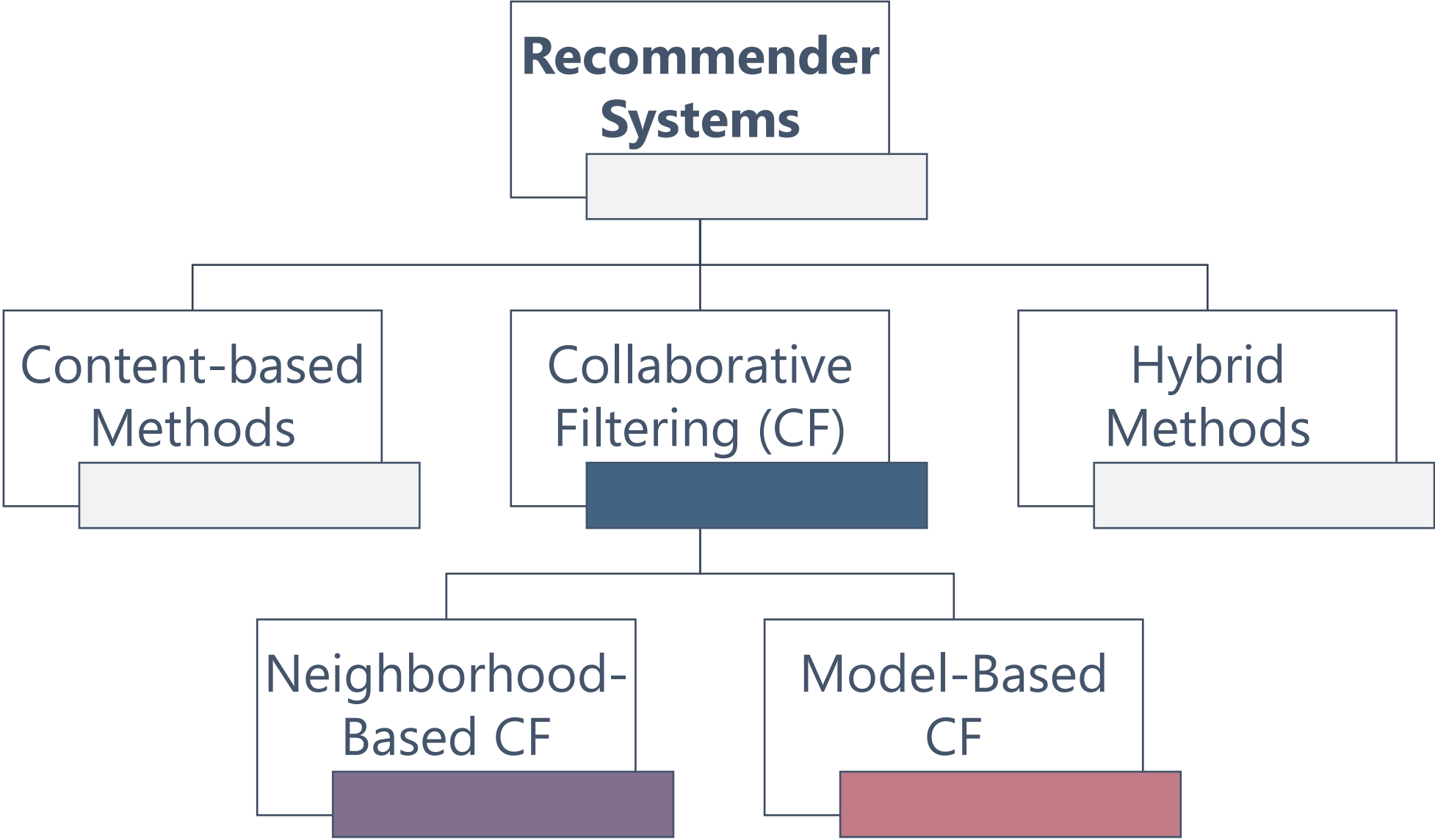


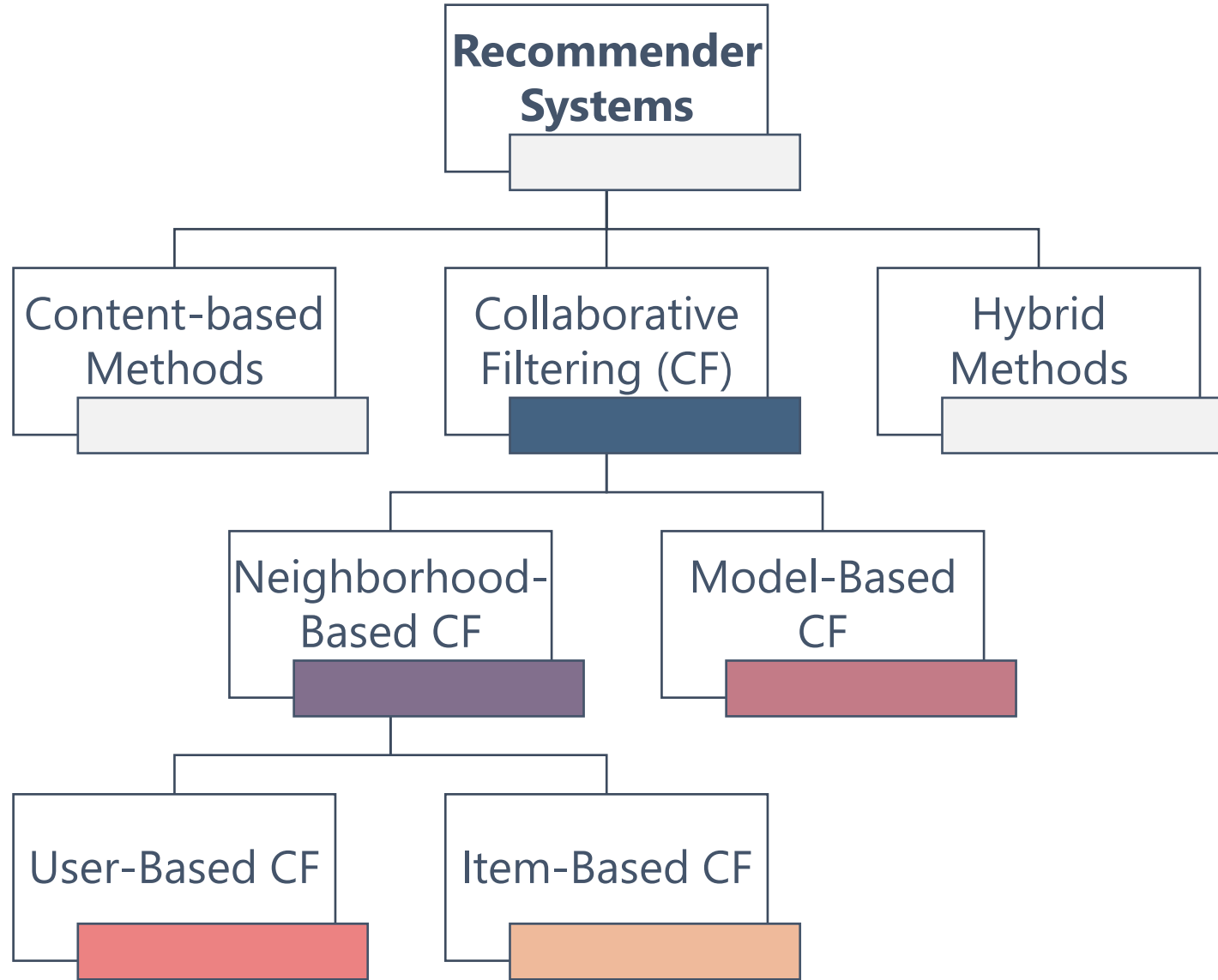




# Recommender systems

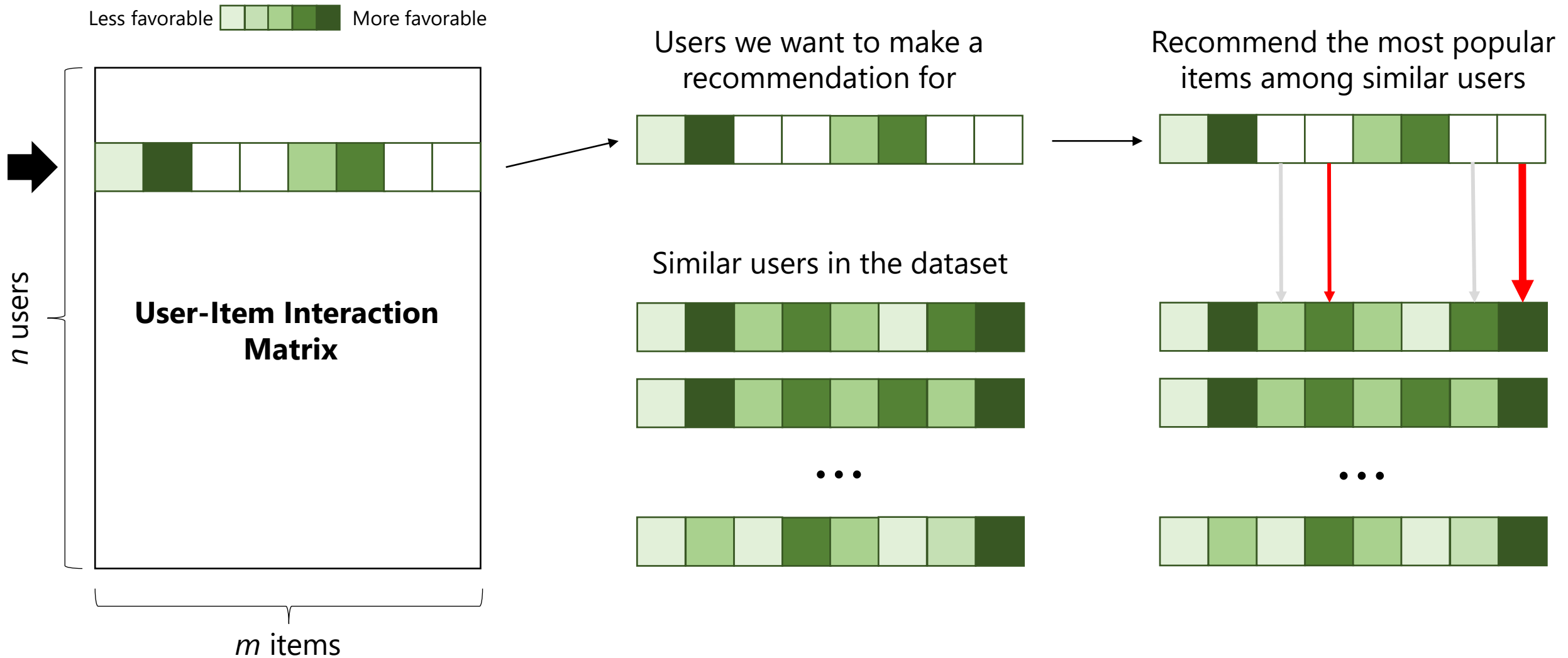
"... personalized information agents that provide recommendations: suggestions for items likely to be of use to a user" ([Burke, 2007](#))







# User-Based Collaborative Filtering



# User-Based Collaborative Filtering

- **user**  $u_i, i = 1, \dots, n$
- **item**  $p_j, j = 1, \dots, m$
- **rating**  $r_{ij}$

Step  
1

$$\text{sim}(u_i, u_k) = \cos(u_i, u_k) = \frac{\sum_{j=1}^m r_{ij} r_{kj}}{\sqrt{\sum_{j=1}^m r_{ij}^2 \sum_{j=1}^m r_{kj}^2}}, \text{ or}$$

$$\text{sim}(u_i, u_k) = \text{cor}(u_i, u_k) = \frac{\sum_{j=1}^m (r_{ij} - \bar{r}_i)(r_{kj} - \bar{r}_k)}{\sqrt{\sum_{j=1}^m (r_{ij} - \bar{r}_i)^2 \sum_{j=1}^m (r_{kj} - \bar{r}_k)^2}},$$

Step  
2

Perform  $k$ -nearest neighbors (KNN) to select the best neighbors of the target user  
(*alternatively, use a similarity threshold*)

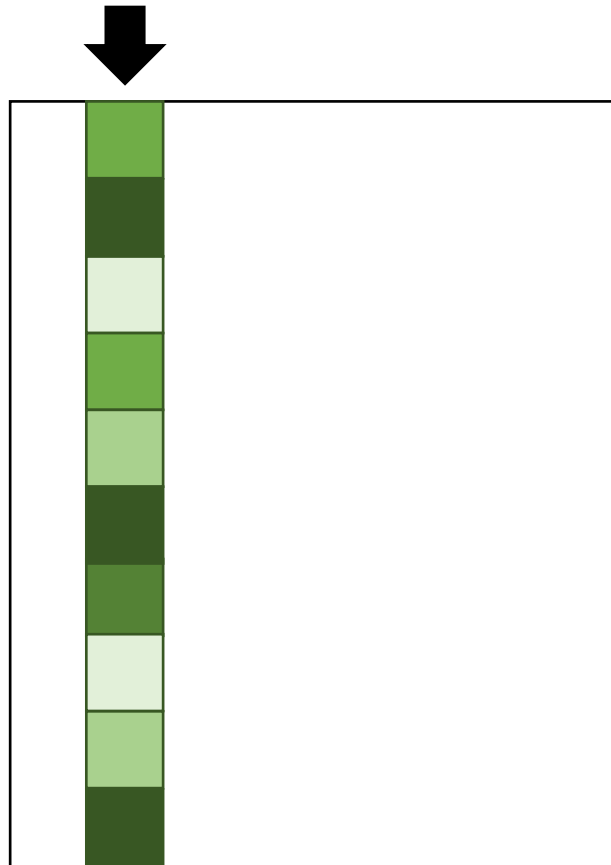
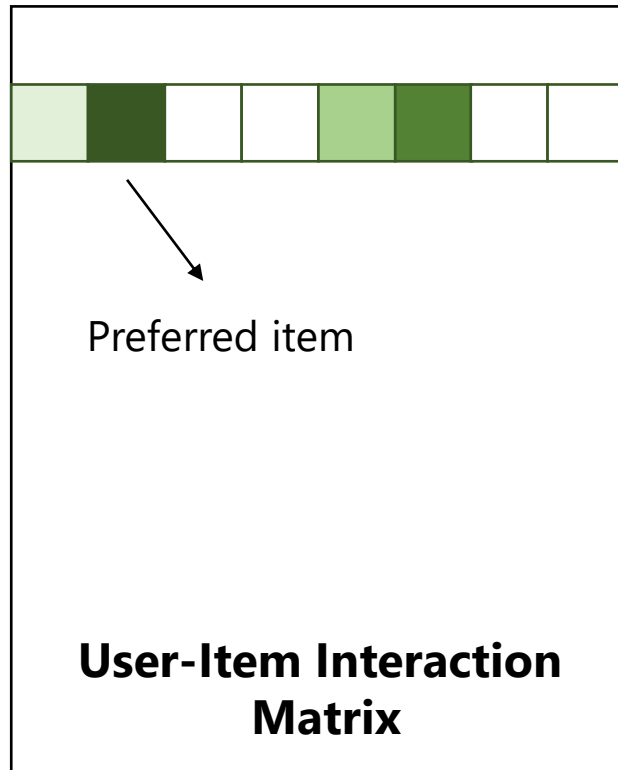
Step  
3

Predict an unknown rating for the target user based on the best neighbors identified in Step 2.

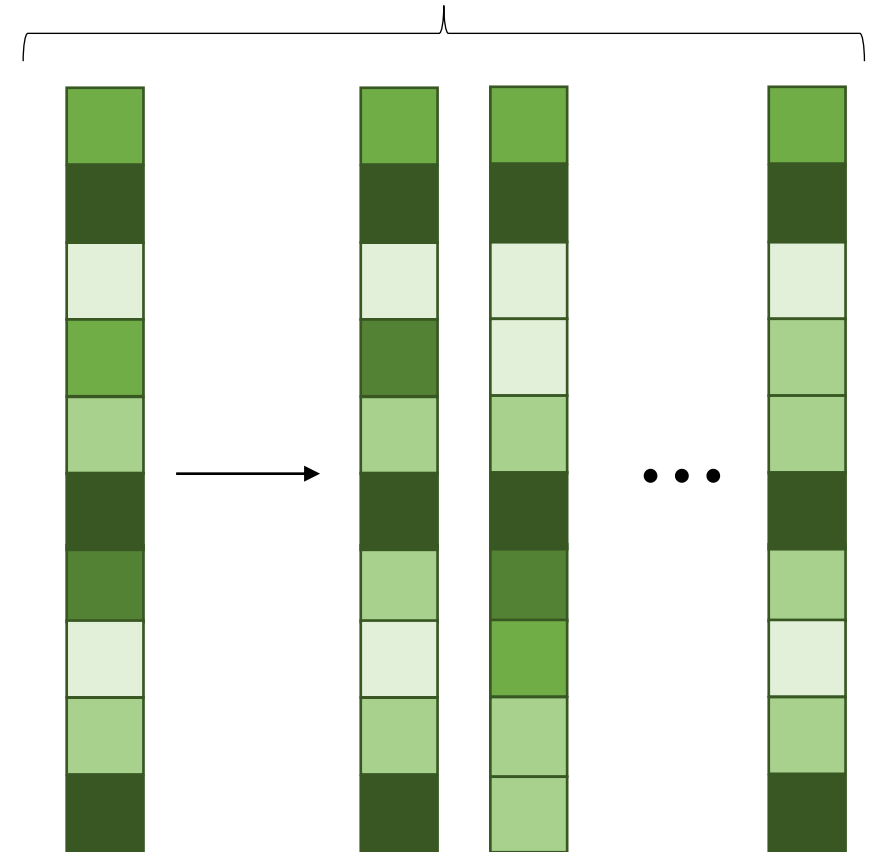
$$\hat{r}_{ij} = \frac{\sum_k \text{sim}(u_i, u_k) r_{kj}}{\# \text{ of ratings}} \quad \text{or} \quad \hat{r}_{ij} = \bar{r}_i + \frac{\sum_k \text{sim}(u_i, u_k) (r_{kj} - \bar{r}_k)}{\# \text{ of ratings}}$$

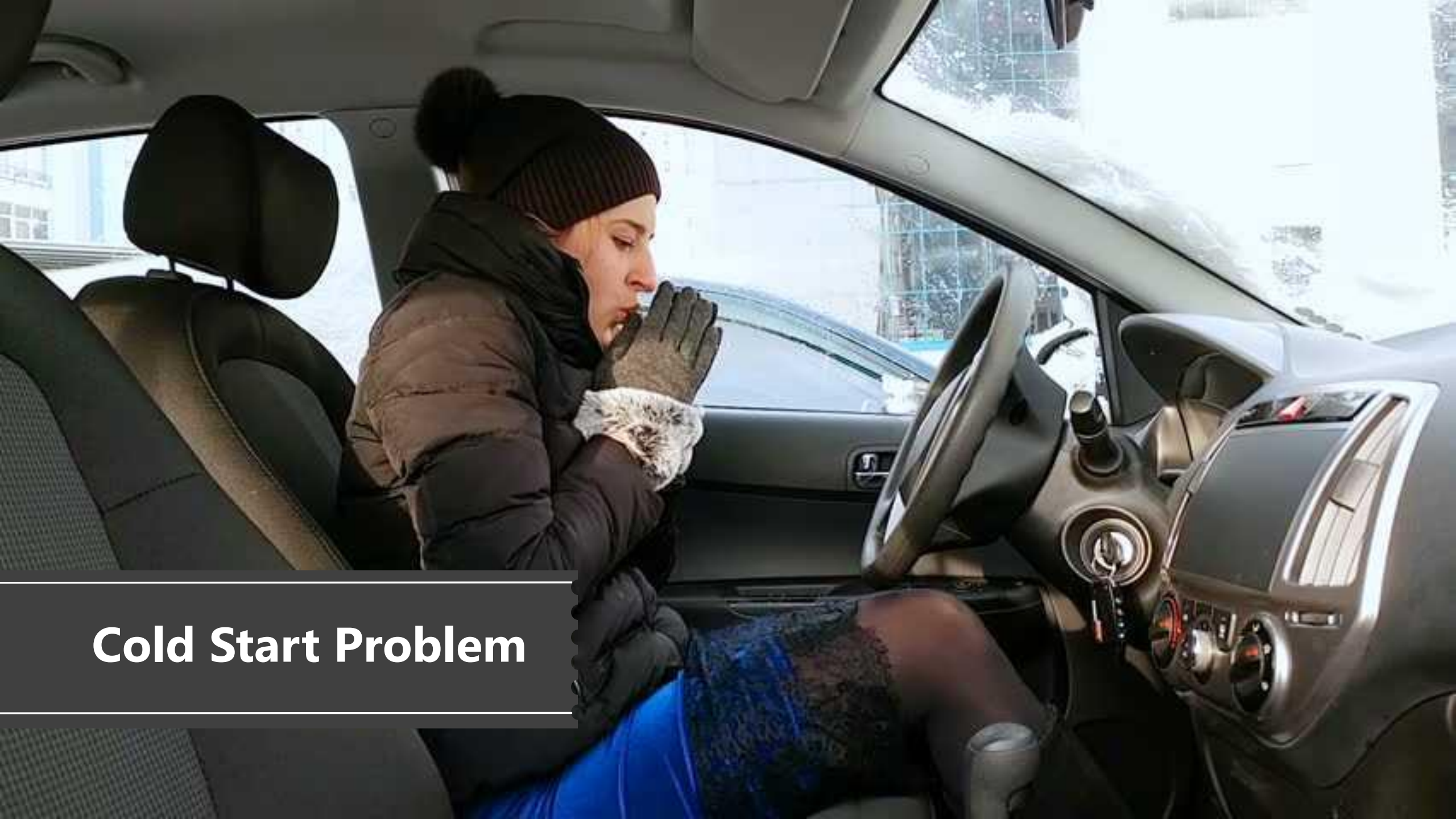
# Item-Based Collaborative Filtering

Less favorable  More favorable



Apply the KNN algorithm and find the most similar item(s)





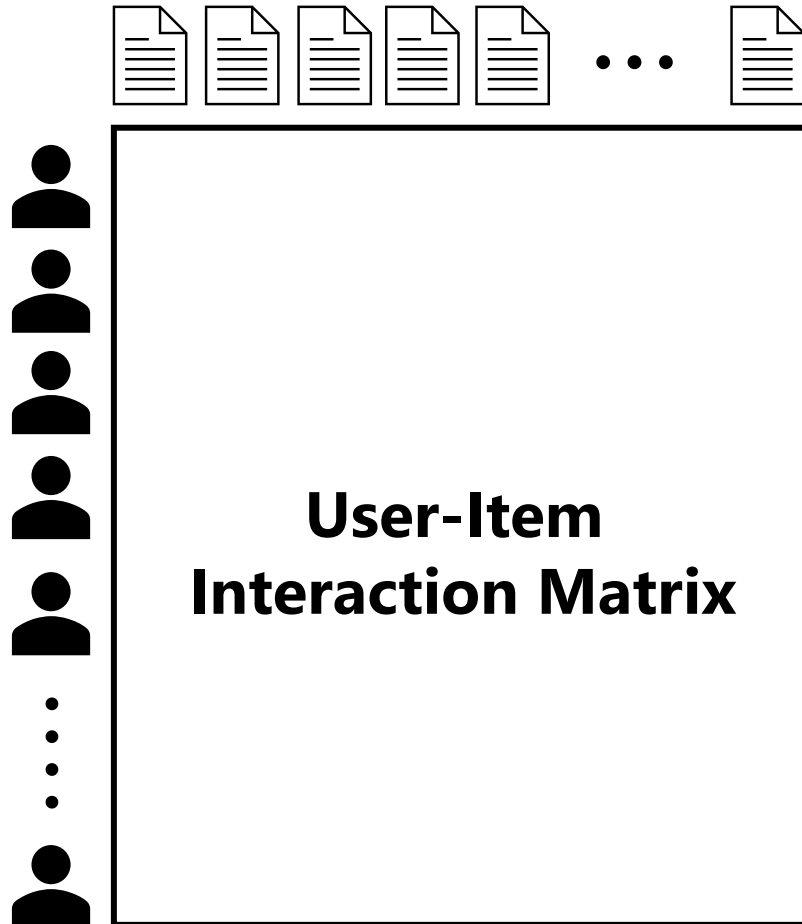
**Cold Start Problem**





Data Sparsity Problem

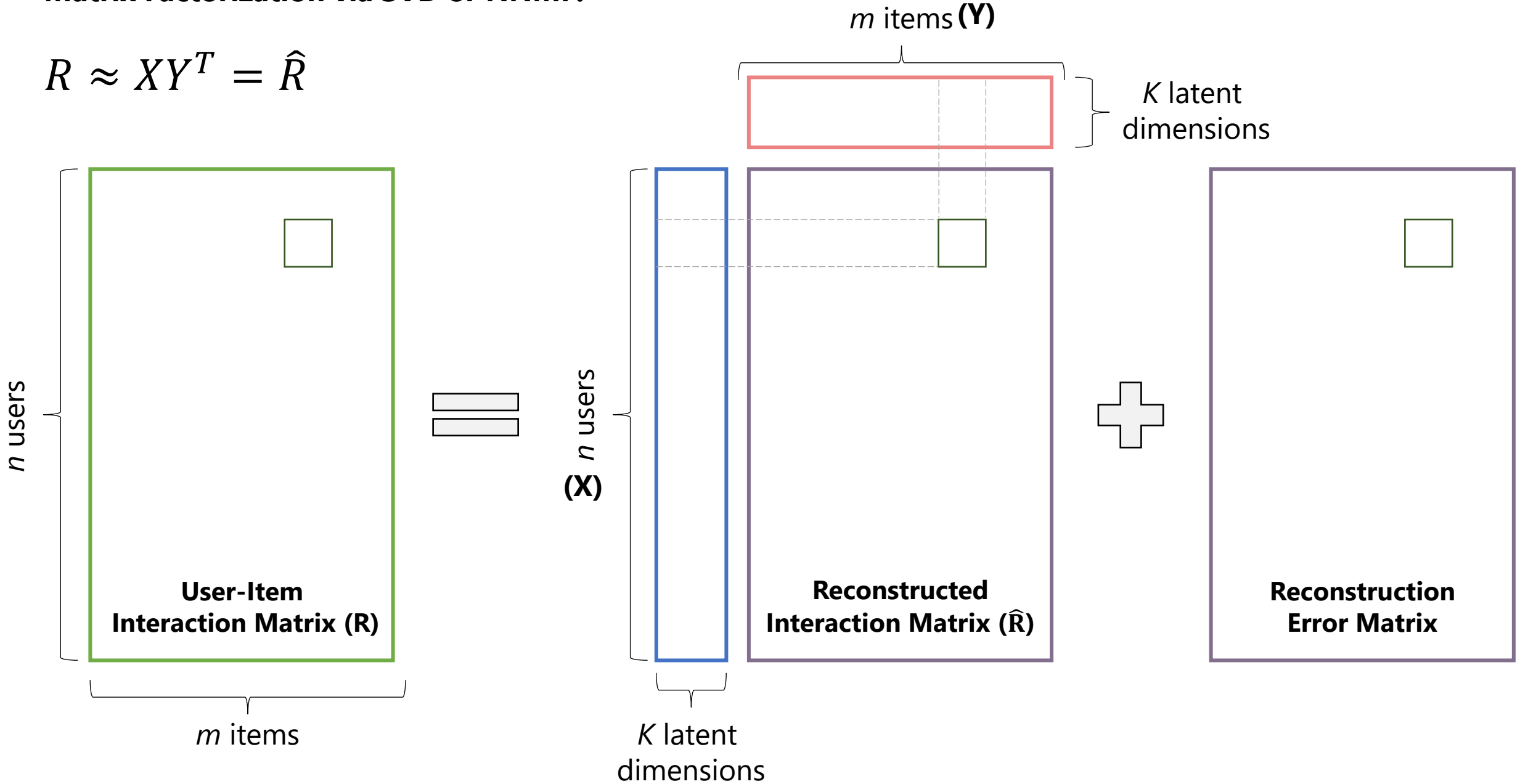
# Model-Based Collaborative Filtering

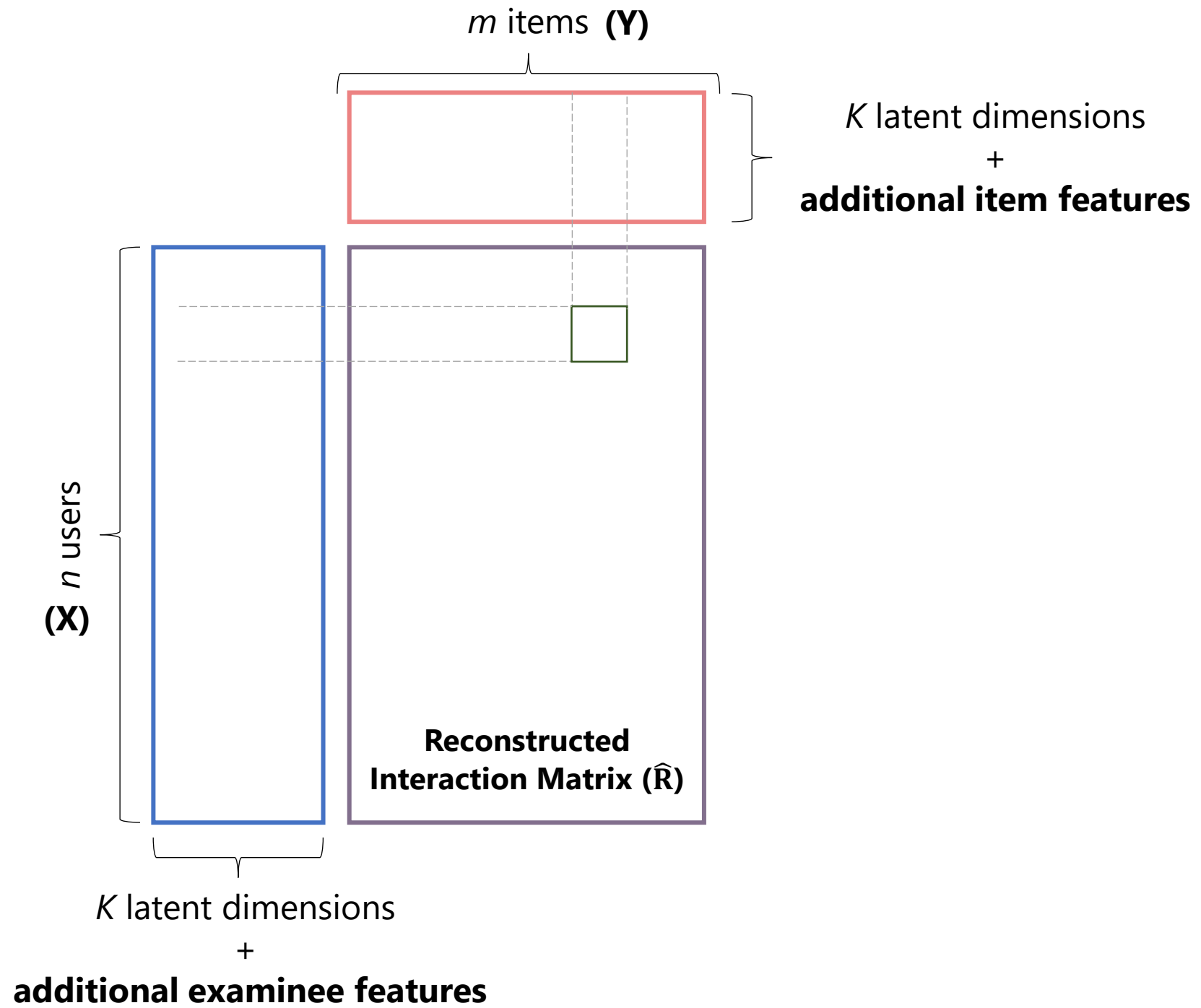


An underlying **generative** model that explains the user-item interactions.

# Matrix Factorization via SVD or NNMF:

$$R \approx XY^T = \hat{R}$$



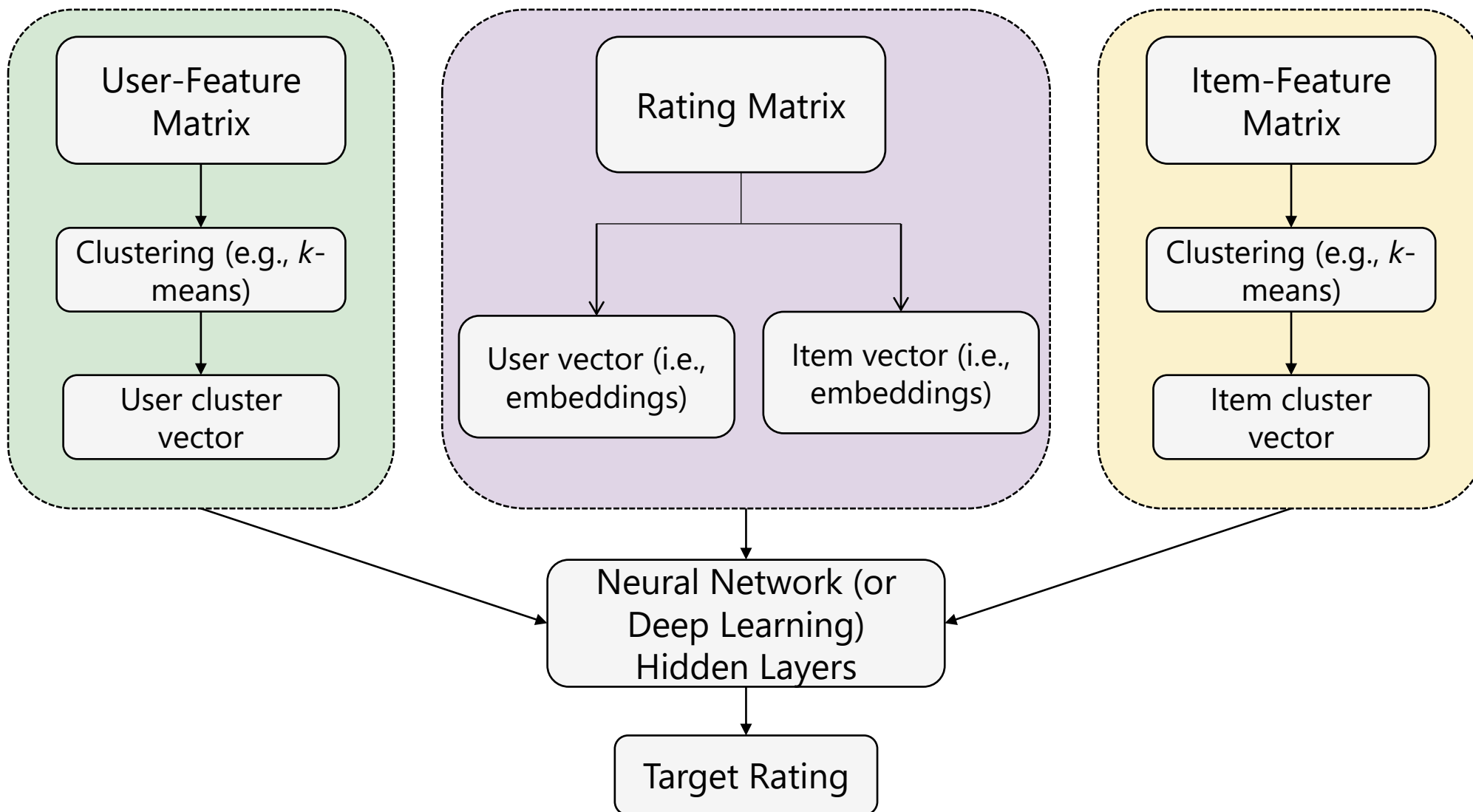




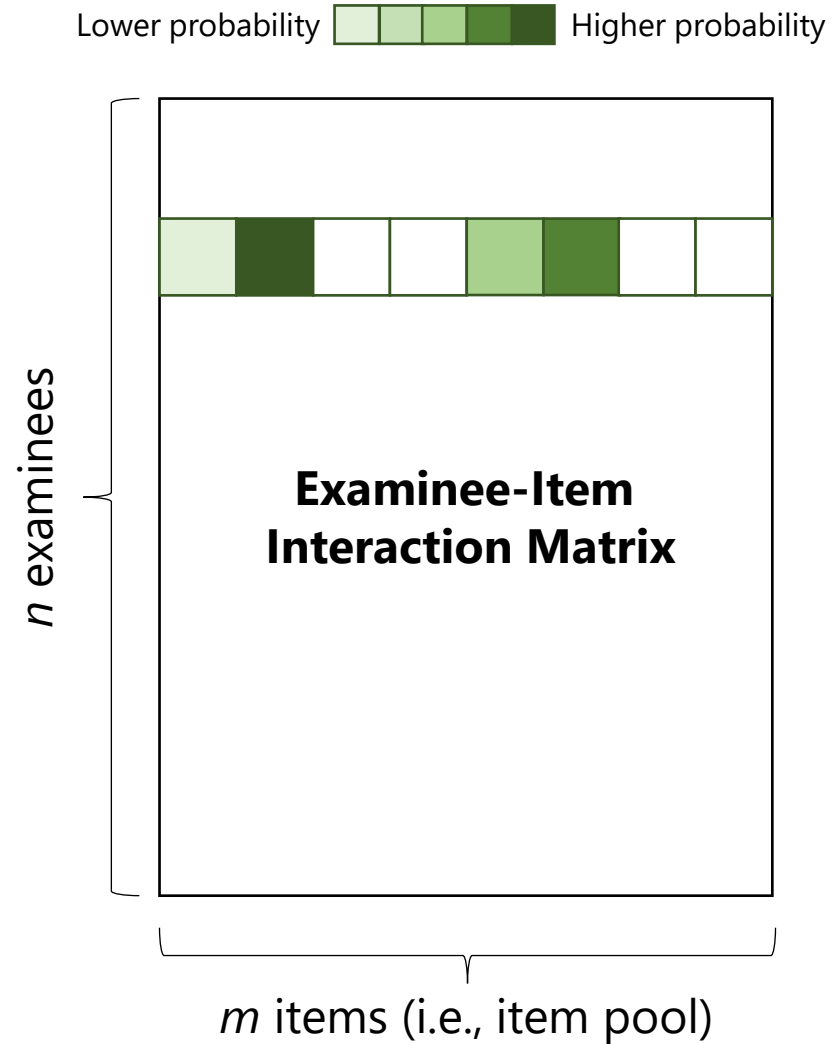
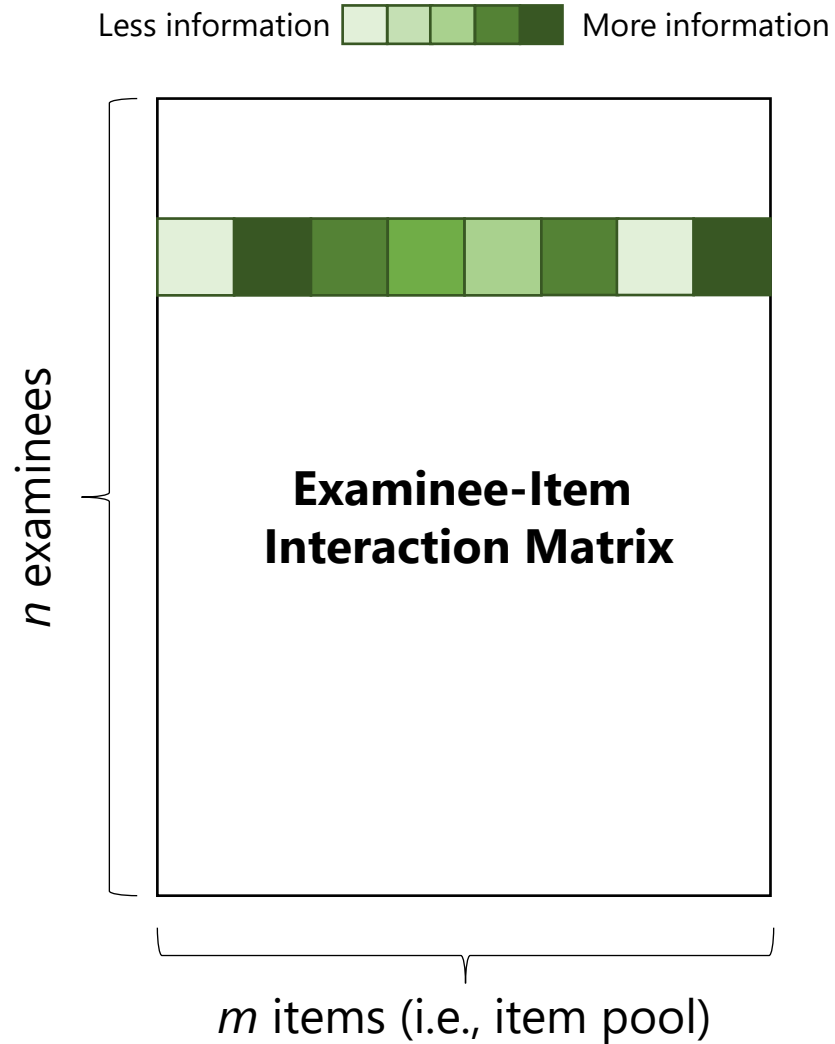
User x Item x Context

$$\hat{R} = X \times Y \times C$$

# Hybrid Recommender Systems



# Adaptive Testing via Recommender Systems (RS)





# Item Selection With Collaborative Filtering in On-The-Fly Multistage Adaptive Testing

Applied Psychological Measurement  
2022, Vol. 46(8) 690–704  
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Jiaying Xiao<sup>1</sup>  and Okan Bulut<sup>2</sup> 

## Abstract

An important design feature in the implementation of both computerized adaptive testing and multistage adaptive testing is the use of an appropriate method for item selection. The item selection method is expected to select the most optimal items depending on the examinees' ability level while considering other design features (e.g., item exposure and item bank utilization). This study introduced collaborative filtering (CF) as a new method for item selection in the *on-the-fly assembled multistage adaptive testing* framework. The user-based CF (UBCF) and item-based CF (IBCF) methods were compared to the maximum Fisher information method based on the accuracy of ability estimation, item exposure rates, and item bank utilization under different test conditions (e.g., item bank size, test length, and the sparseness of training data). The simulation results indicated that the UBCF method outperformed the traditional item selection methods regarding measurement accuracy. Also, the IBCF method showed the most superior performance in terms of item bank utilization. Limitations of the current study and the directions for future research are discussed.

## Keywords

collaborative filtering, multistage adaptive testing, item selection, measurement accuracy

## Item Selection for On-the-Fly Multi-Stage Adaptive Testing

**Stage 1:** A pre-assembled module

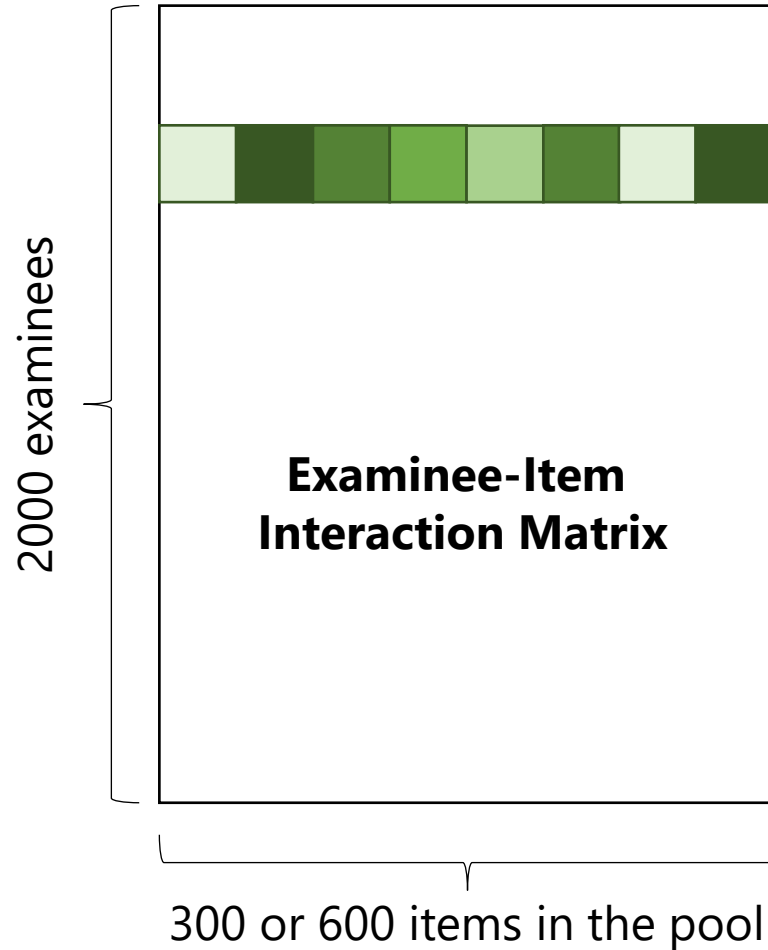
**Stages 2 & 3:** On-the-fly assembled modules via user-based and item-based collaborative filtering

No additional item or user feature used

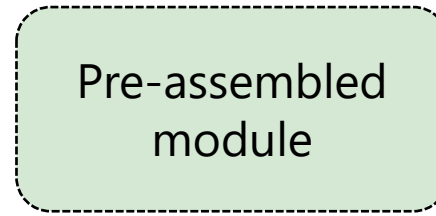
Item selection using the [recommenderlab](https://github.com/recommenderlab) package in R

<https://doi.org/10.1177/01466216221124089>

## Training Dataset



## Stage 1



10 items  
or  
20 items

## Stage 2



10 items  
or  
20 items

## Stage 3



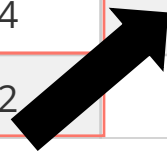
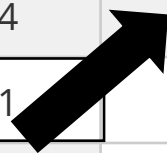
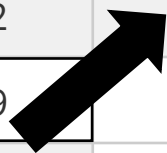
10 items  
or  
20 items

On-the-fly module assembly using:

- User-based CF (UBCF)
- Item-based CF (IBCF)
- Maximum Fisher information (MFI)

$\theta = [-3, -2.6, \dots, 2.6, 3] \rightarrow 500$  simulated examinees per ability

| Item Bank Size | Method | 30-item design |       |             |                            | 60-item design |       |             |                            |
|----------------|--------|----------------|-------|-------------|----------------------------|----------------|-------|-------------|----------------------------|
|                |        | Bias           | RMSE  | Reliability | Proportion of unused items | Bias           | RMSE  | Reliability | Proportion of unused items |
| 300 items      | UBCF   | -0.019         | 0.362 | 0.970       | 57%                        | -0.013         | 0.277 | 0.981       | 31%                        |
|                | IBCF   | -0.007         | 0.428 | 0.962       | 38%                        | 0.002          | 0.341 | 0.974       | 27%                        |
|                | MFI    | -0.016         | 0.369 | 0.969       | 59%                        | -0.013         | 0.279 | 0.981       | 32%                        |
| 600 items      | UBCF   | 0.044          | 0.464 | 0.957       | 75%                        | 0.015          | 0.335 | 0.975       | 57%                        |
|                | IBCF   | -0.010         | 0.341 | 0.973       | 66%                        | -0.010         | 0.256 | 0.984       | 51%                        |
|                | MFI    | -0.012         | 0.365 | 0.970       | 76%                        | -0.011         | 0.270 | 0.982       | 59%                        |





# Personalized Scheduling for Adaptive Tests

*What is the optimal test schedule for each student based on their learning progress?*

Progress monitoring with Renaissance's Star Reading and Star Math adaptive tests for K-12

Grade 2 ( $n = 668,324$ ) and Grade 4 ( $n = 727,147$ )

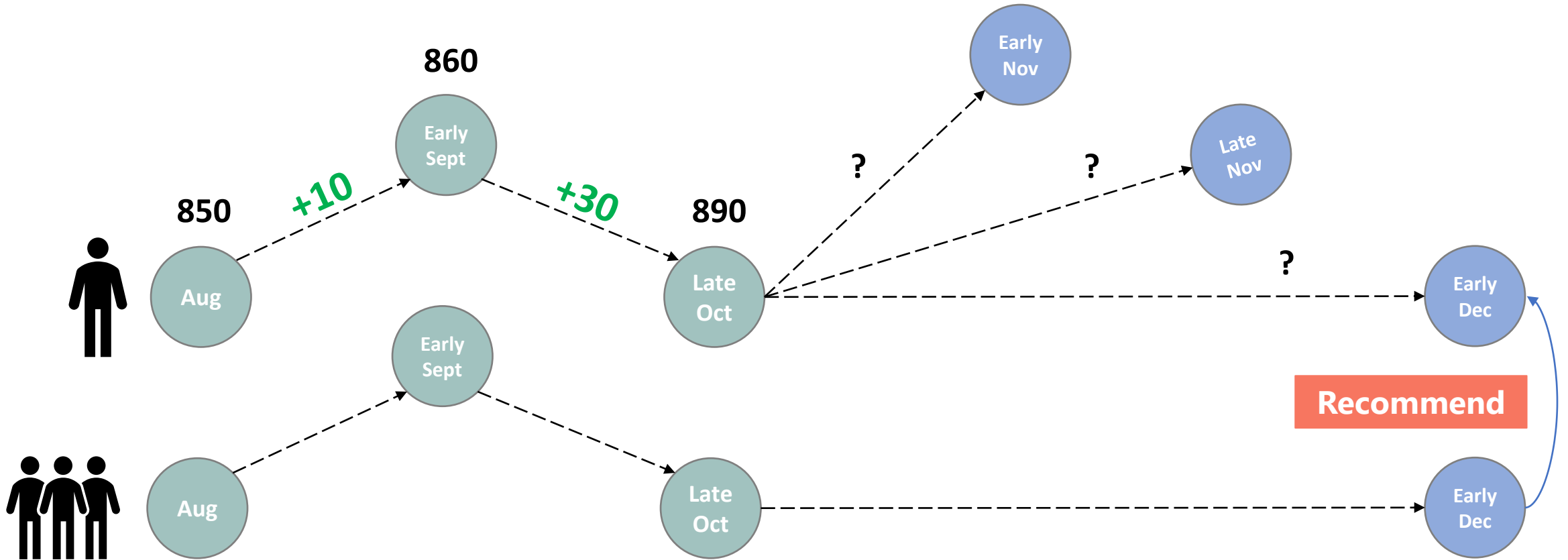
2 to 18 test administrations per student

([Bulut, Shin, & Cormier, 2022](#); [Shin & Bulut, 2022](#); [Bulut, Cormier, & Shin, 2020](#))



# User-Based Collaborative Filtering with Dijkstra's Shortest Path First Algorithm

- **Maximize** the positive and absolute score change between test administrations
- **Minimize** the number of test administrations



- Find similar students (with max score change + fewest test administrations)
- Select the most similar students based on Euclidean distance and recommend their schedule

**Standard Practice** = Schedules Determined by Teachers    **RS** = Recommender System

| Evaluation Criteria                  | Grade 2           |          | Grade 4           |          |
|--------------------------------------|-------------------|----------|-------------------|----------|
|                                      | Standard Practice | RS       | Standard Practice | RS       |
| Average number of tests administered | 5.42              | → 3.51   | 5.37              | → 3.84   |
| Average score change between tests   | 8.32              | → 12.25  | 3.49              | → 4.63   |
| Range of tests required              | (1, 18)           | → (1, 5) | (1, 17)           | → (1, 6) |
| Non-recommendable cases              | -                 | 0.05%    |                   | 0.10%    |

# Concluding Remarks

- Recommender systems can help us take a more holistic approach to designing adaptive learning systems.
  - Shifting the focus from “examinees” to “learners”
  - ~~Less psychometrics & more AI~~; an amalgamation of psychometrics and AI
- Using the auxiliary information about learners as “adaptive variables”
  - Enhanced adaptivity and precision (especially when there is no prior information on learners)
  - Prioritizing the text-taker experience (TTX) in decision-making ([Duolingo, 2021](#))
  - Driving innovation in the cycle of domain, assessment, and feedback

# Future Directions

- Recommender systems can involve real-time process data (e.g., response time) to consider test-taking engagement in adaptive testing.
- Recommender systems can be used with other psychometric models such as Bayesian Knowledge Tracing to measure mastery of content domain.
- Recommender systems utilizing deep learning algorithms can model both responses and sequential action data in adaptive learning environments.
  - [Chen et al. \(2019\)](#)'s Behavior Sequence Transformer Model
  - [Wu et al. \(2017\)](#)'s Recurrent Recommender Networks

The background features a large, light green watermark of the University of Alberta crest. The crest is circular, with the text "UNIVERSITY OF ALBERTA" at the top and "QUAECUMQUE VERA" at the bottom. The central shield contains a book, a mountain range, and a banner.

# Thank You!

For questions/comments:

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