

Dendrite growth in undercooled Al-rich Al-Ni melts measured on Earth and in Space

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The dendrite growth velocity in Al₇₅Ni₂₅ melts has been measured in a containerless procedure as a function of undercooling using an electromagnetic levitation technique both in the Earth laboratory and in Space on board the International Space Station. The growth shows an anomalous behavior inasmuch as the growth velocity decreases with increasing undercooling, confirming previous experiments on Earth. Within the scatter of experimental data, results obtained on Earth and in Space do not show significant differences. Thus, convection effects as origin of the anomalous growth characteristics can be excluded. However, high speed video recording exhibits multiple nucleation events in front of the growing solid/liquid interface. This effect is identified as the origin of the anomalous dendrite growth characteristics in undercooled melts of Al-rich Al-Ni melts.

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Introduction

The properties of materials produced by solidification from melts are governed by crystal nucleation and subsequent crystal growth. Each solidification process needs an undercooling prior to solidification in order to initiate crystal nucleation and to drive the solidification front. At small undercoolings, a stable solid phase is formed whereas at large undercoolings the excess Gibbs free energy of the liquid also allows the solidification of metastable solid phases. Hence the profound understanding of these processes is of fundamental importance for materials design from the melt and materials processing [1, 2]. Nucleation [3] and dendrite growth [2] have been intensely studied during the past. As far as dendrite growth is concerned, the velocity of the dendrites propagating through the volume of the melt has been measured as a function of undercooling [2]. By far in most cases, the velocity monotonically increases with increasing undercooling. Within the theory of dendrite growth this is easily understood by the fact that the driving force for growth is also continuously increasing with undercooling.

More recently, an opposite behavior has been found. One may distinguish two different cases. In glass forming metallic alloys, the growth velocity, V , increases with undercooling, ΔT ,

but passes through a maximum and decreases with further increase of the undercooling. This has been verified in electrostatic levitation experiments of CuZr and NiZr, in which large undercoolings are achieved ranging up to the temperature regime above the glass transition temperature [4]. The observation of a maximum in $V(\Delta T)$ has been explained by a competition of the counteracting effects of the driving force which increases with undercooling on the one hand, and the strong decrease of atomic diffusion with the increase of undercooling on the other hand. At small undercoolings the driving force dominates, whereas at large undercoolings the decreasing atomic diffusion controls the growth kinetics. Alternatively, a negative gradient in the growth velocity versus undercooling relation has been reported for Al-rich Al-Ni alloys too [5]. However, these alloys do not form metallic glasses, since their glass transition temperature is low compared with that of glass formers. In particular, the maximum undercoolings, even by containerless processing, are far above the glass transition temperature, wherein the strong decrease in atomic diffusion characteristic of glass formation is not encountered. This anomalous behavior of the growth kinetics in undercooled melts of Al-rich Al-Ni alloys is thus not yet understood.

In the present work, several physical effects are discussed as origin of the anomalous growth behavior in Al-Ni alloys. These include forced convection by external electromagnetic fields, inverse melting, and phase competition during solidification. Recent simulations have analysed the influence of convection on crystal growth [6] which has also been investigated experimentally during parabolic flights under conditions of reduced gravity [7]. The influence of forced convection on the growth kinetics as found in an Al₅₀Ni₅₀ alloy [8] is investigated by comparative measurements of dendrite growth as a function of undercooling of an Al₇₅Ni₂₅ alloy using electro-magnetic levitation both on Earth and in Space. In space the forces needed for compensation of disturbing accelerations are smaller than the electromagnetic forces needed to compensate the gravitational accelerations on Earth by about three orders of magnitude. Consequently, forced convection in the case of experiments in Space is very much reduced. Moreover, we investigate the effect of different growth kinetics of various phases which may compete during solidification. Inverse melting [9] of the alloy is investigated for deep undercoolings [10]. Eventually, we analyse high quality video images taken by a high-speed video camera in electromagnetic levitation experiments in Space. Thanks to the reduced convection, the video frames allow for a direct observation of different solidification phenomena when the quiescent melt is deeply undercooled prior to solidification. That makes it possible to determine the physical origin of the anomalous growth behavior of Al-rich Al-Ni alloys, i.e. the negative gradient in the $V(\Delta T)$ relation at large undercoolings. The results will also be compared with microtomography observations of Impulse Atomized (IA) droplets (a type of drop tube) where the droplets experience very limited convection during rapid solidification.

Experimental

Samples were prepared from the high purity alloy constituents (6N in case of Al [11] and 5N in case of Ni) by arc melting in a high purity Ar atmosphere. The growth velocity as a function of undercooling in the Earth laboratory was measured by an electromagnetic levitation facility that is equipped with a high-speed camera in order to observe the propagation of the solid-liquid interface during solidification. Equivalent experiments were conducted on board the International Space Station (ISS) in the reduced gravity environment using the multiuser facility Electro-Magnetic Levitator (EML) developed by the European Space Agency (ESA) and the German Aerospace Center (DLR). The EML is in operation since 2014. Details of the experimental facilities are described elsewhere [12]. The IA experiments were carried out using 4N Al and Ni. The composition of the alloy atomized was Al₈₀Ni₂₀ with a similar solidification path expected to the Al₇₅Ni₂₅ studied using the EML. Details of the IA experiments are found elsewhere [13]

Results and Discussion

According to the phase diagram of Al-Ni several peritectic reactions are expected for the Al₇₅Ni₂₅ alloy. Figure 1 gives a section of the Al-Ni phase diagram on the Al-rich side onto which the temperatures at which velocity-undercooling measurements have been made. From the phase diagram it is obvious that three phases are involved in the peritectic reactions of Al-rich Al-Ni alloys. These are the intermetallic phases AlNi (B2-phase), Al₃Ni₂ and Al₃Ni.

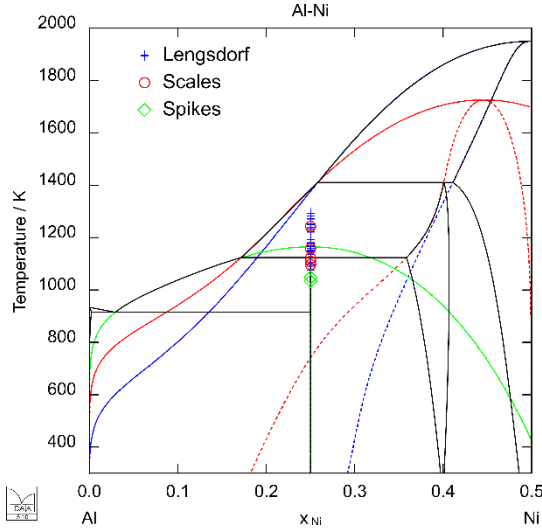


Figure 1: Al-Ni phase diagram including metastable extensions of the liquidus (solid) and solidus (dotted) lines for AlNi₃ (green), Al₃Ni₂ (red) and AlNi (blue) phases. Also shown are the temperatures at which velocity measurements have been made for Al₇₅Ni₂₅ on Earth [5] and in microgravity.

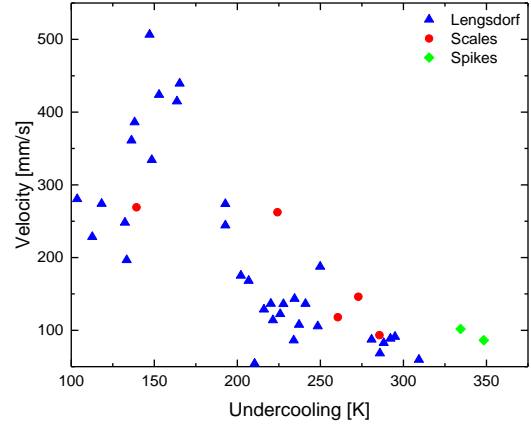


Figure 2: Dendrite growth velocity as a function of undercooling measured on Earth (triangles) and in microgravity (circles) for alloy Al₇₅Ni₂₅. Data of the terrestrial experiments are taken from ref. [5]. The color of the circles denotes the growth morphology observed by the high-speed camera, scales (red) and spikes (green).

In 1987, Blatter and van Almen [14] detected a very unusual phase transformation behavior of a Ti₇₀Cr₃₀ thin film evaporated on a tungsten substrate. Laser quenching preserved the initial amorphous phase, annealing the film at 1073 K yield a crystalline β phase, and surprisingly subsequent annealing at 873 K restored the amorphous phase. If the amorphous phase is considered as a frozen liquid this finding was analysed with respect to the phenomenon of inverse melting [9]. This means that during cooling of a liquid, the liquid transforms to a crystalline phase at a temperature T_x below the liquidus temperature T_L , but by further cooling the liquid phase reappears at a temperature $T_i < T_x < T_L$, i.e. the crystal remelts. This phenomenon would differ from the phase transformation behavior of binary alloys showing a retrograde monovariant line in their phase diagram. In this case, a crystal is formed at temperatures below the liquidus temperature and upon further cooling the crystal partly remelts. In this case remelting is associated with phase separation. On the other hand, inverse melting means complete remelting of the primary crystal upon cooling. Consequently, the Gibbs free energy of the liquid, G_l , and of the crystal, G_x , should cross twice if the temperature is continuously lowered from temperatures above the liquidus temperature T_l , first at a crystallisation temperature $T_x < T_l$, and at the temperature of inverse melting $T_i < T_x < T_l$. It is remarkable that, from the viewpoint of thermodynamics, the liquid phase formed at T_i has to have a lower entropy $S = -(\partial G/\partial T)_P$. That is very unusual, certainly not possible in case of pure metals. However, in case of alloys the circumstances may differ. Neutron diffraction studies on

deeply undercooled Al-Fe-Co [15, 16] and $Ti_{72.5}Fe_{27.5}$ [17] alloys show a rapid increase of the degree of both topological and chemical short-range-order. On the other hand, solidification studies of deeply undercooled intermetallic phases give evidence of the formation of highly metastable disordered superlattice structures [18]. To further elucidate the hypothesis of inverse melting to be the origin of the anomalous growth kinetics of deeply undercooled Al-rich Al-Ni alloys we refer to *in situ* diffraction studies of phase selection in $Al_{68.5}Ni_{31.5}$ [19] alloy using high intensity synchrotron radiation. These experiments indicate primary crystallization of the B2 phase of intermetallic AlNi over the entire undercooling range accessible in the levitation experiments. After primary solidification, the B2 phase transforms via a peritectic reaction to Al_3Ni_2 at the corresponding peritectic temperature. In a third crystallization process, the intermetallic Al_3Ni phase is formed from $L + Al_3Ni_2$. From these findings we exclude inverse melting to be the origin of the anomalous dendrite growth behavior of Al-rich Al-Ni alloys. The B2 phase does not form an amorphous phase. According to work by Turnbull, the glass transition temperature of such systems is expected to be very small, around $0.3 T_l$ [20]. Taking $T_l \approx 1950$ K for the AlNi B2 phase, its glass transition temperature is estimated to be around $T_g \approx 585$ K. This means it is far away from the temperature of the undercooled melt, even at the maximum undercooling of $\Delta T \approx 350$ K achieved in the space experiments, $T \approx T_l - 350$ K ≈ 1600 K. Therefore, we exclude inverse melting to be the physical origin of the anomalous dendrite growth behavior of Al-rich Al-Ni alloys.

The investigations of phase selection during solidification of the undercooled melt of the $Al_{75}Ni_{25}$ alloy indicate that three intermetallic phases, AlNi, Al_3Ni_2 and Al_3Ni , are involved in the solidification process until the entire liquid is transformed to solid [21]. That is compatible with the temperature-time-profiles recorded on $Al_{75}Ni_{25}$ alloy during the space experiments. Figure 3 shows such a temperature-time-profile recorded during solidification of an $Al_{75}Ni_{25}$ sample upon an undercooling of $\Delta T = 224$ K prior to solidification. Three reactions are visible through the release of the heat of transformations and its impact on the temperature curve measured. The first one is identified as the primary crystallization of AlNi B2 phase, the second one the peritectic reaction involving the Al_3Ni_2 intermetallic phase and the third one the formation of Al_3Ni phase from the $L + Al_3Ni_2$. Further cooling could even have shown evidence of a fourth reaction due to the final eutectic transformation at lower temperature corresponding to the coupled growth of Al_3Ni and Al-rich lamellae [22]. It is emphasized that the distance on the time axis between the various phase reactions depends strongly on the undercooling achieved prior to solidification. Hence, it may be argued that a competition of various phases during solidification could lead to a negative gradient in the $V(\Delta T)$ relationship provided the velocity measurements are integral and the phase fractions F depend essentially on the undercooling. Under such circumstances an average velocity V can be estimated as:

$$V = \frac{(F_A V_A + F_B V_B + F_C V_C)}{F_A + F_B + F_C} \quad \text{with } A: AlNi; B: Al_3Ni_2; C: Al_3Ni \quad (1)$$

We have computed the dendrite growth velocities of the various phases involved in the solidification of $Al_{75}Ni_{25}$ alloy using the sharp interface theory of dendrite growth in undercooled melts [23]. The results of these computations are shown in Figure 4. All three curves show qualitatively the same characteristics: a monotonic increase with undercooling. Since the slope of all curves is very similar, it is very unlikely that the anomalous growth kinetics of $Al_{75}Ni_{25}$ alloy can be understood according to equation 1 assuming a dependence of the phase fractions of the various phases with a change of undercooling.

Phase-field modelling has also been employed to simulate the growth of the B2 AlNi and Ni_2Al_3 phases from their undercooled parent melt. This is a coupled thermo-solutal simulation [24], however as a computational expedient the Lewis number, Le (= thermal diffusivity/solute diffusivity), has been set artificially low to 100. Similar results are found as

in case of sharp interface modeling (cf. figure 4), as demonstrated in Figure 5. The most obvious discrepancy is that, as with all standard materials, the growth velocity increases with increasing undercooling, rather than decreasing as observed experimentally. This poor agreement between observation and model, which is not only quantitative but qualitative (i.e. the incorrect trend is observed) would suggest that either (i) there is some unique physics for the Al-Ni system which is not considered in the existing model or (ii) the behavior of the Al-Ni system could in principle be described by the physics already built into the model but, for whatever reason, this behavior is not captured with sufficient fidelity. The response of the system to increasing Lewis number may be instructive. Increasing Le from 100 to 500 resulted in an average increase in V of 27%, while further increases in Le had minimal effect on V . This is in contrast to previous investigations on solid solution alloys [25], where a similar increase in Le resulted in an increase of 290% in the growth velocity, V , while increasing further from $Le = 500$ to $Le = 10,000$ leads to a further 400% increase in V . This would suggest growth in Al-Ni is under full solutal control, which would be consistent with the very steep slope of the liquidus line, $|m| = 41.74 \text{ K at}\%^{-1}$ and $|m| = 32.27 \text{ K at}\%^{-1}$ for AlNi and Al₃Ni₂ respectively at 1300K and $c = 30 \text{ at}\% \text{ Ni}$. Consequently, very small changes in the solute concentration at the tip could potentially lead to large variations in the interface temperature.

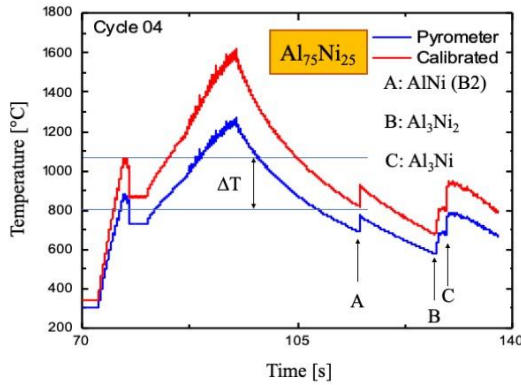


Figure 3: Temperature-time-profile measured during solidification of Al₇₅Ni₂₅ in Space upon an undercooling of $\Delta T \approx 224 \text{ K}$. The red curve gives the data of the pyrometer calibrated by the correct emissivity. Three phase formation temperatures are observed labelled A, B, C.

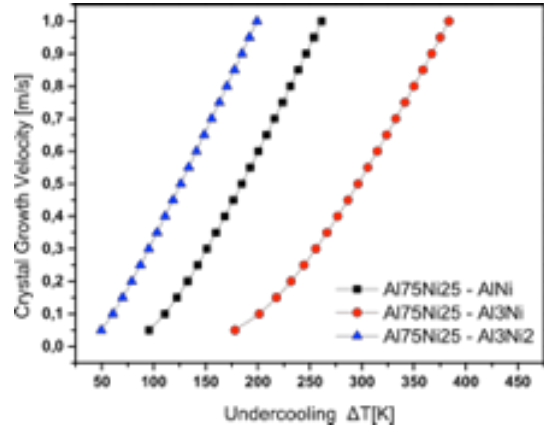


Figure 4: Dendrite growth velocities as a function of undercooling of the various phases involved in the solidification of undercooled Al₇₅Ni₂₅ alloy, AlNi (black), Al₃Ni₂ (blue) and Al₃Ni (red).

This is significant, as preliminary investigations using the Lipton Kurz Trivedi (LKT) model [26] for dendritic solidification, including a description of solidus and liquidus lines that are functions of T , indicate that the type of inverse velocity trend observed in Al-Ni could potentially be explained without recourse to any novel physics. In Figure 6 we show the LKT curves in which $|m|$ and k_E are function of ΔT (i.e. also of T). $|m|$ increasing with ΔT and k_E decreasing with ΔT will both favor lower growth velocity and, with sufficiently rapid change, can overcome the natural tendency for the velocity to increase with increasing ΔT . However, the form of the dependence of $|m|$ and k_E upon ΔT is also important. A more marked inverse velocity trend is favored if $|m|$ plotted against ΔT is convex downwards and k_E plotted against ΔT is convex upwards. This is illustrated in Figure 6 which shows the effect of a linear variation of $|m|$ and k_E (blue), $|m|$ only convex (red), k_E only convex (magenta) and both convex (green). All the curves display some common characteristics, including an initially increasing velocity followed by a local maximum beyond which the velocity decreases with further increases in ΔT . This type of behavior is exactly as displayed by the Al₇₅Ni₂₅ alloy (cf. Figure

2). It is not explicitly displayed by the other Al-Ni alloys, but according to the (plausible) assumption that $V = 0$ at $\Delta T = 0$, a local maximum must be present for all the other alloys, but at lower undercooling than assessed in the experiments reported [5].

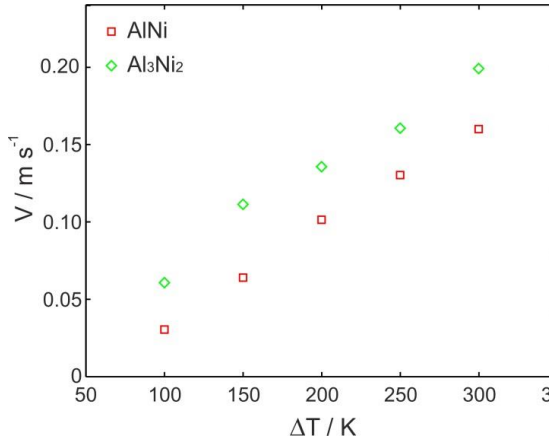


Figure 5: Calculated growth velocity as a function of undercooling estimated from the coupled thermo-solutal phase-field model. Calculation shown for primary growth of both AlNi and of Al₃Ni₂ in an undercooled melt of the Al₇₀Ni₃₀ alloy.

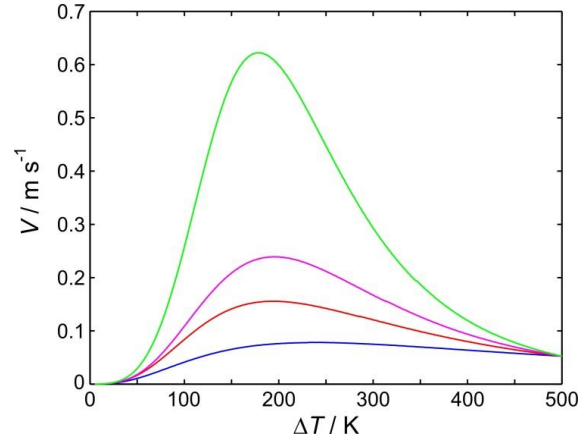


Figure 6: Exemplary LKT type calculations using undercooling dependent $|m|$ and k_E . ($|m|$ increasing with ΔT and k_E decreasing with ΔT): Blue - both $|m|$ and k_E linear; red - $|m|$ convex down and k_E linear; magenta $|m|$ linear and k_E convex up; green - $|m|$ convex down and k_E convex up.

From the discussion so far it is concluded that the anomalous growth kinetics will not be directly related to the dendrite growth mechanism. This assumption is supported by plotting the velocity not as a function of undercooling, but as a function of the nucleation temperature, T_N . The majority of the data points for $x \leq 35$ at% Ni follow a single trend, as shown in figure 7. This behavior is unusual. A common trend of velocity against T_N across alloys of different composition would not be expected; the variation in liquidus temperature with alloy composition means that a fixed value of T_N can map onto widely differing values of ΔT for the different alloys.

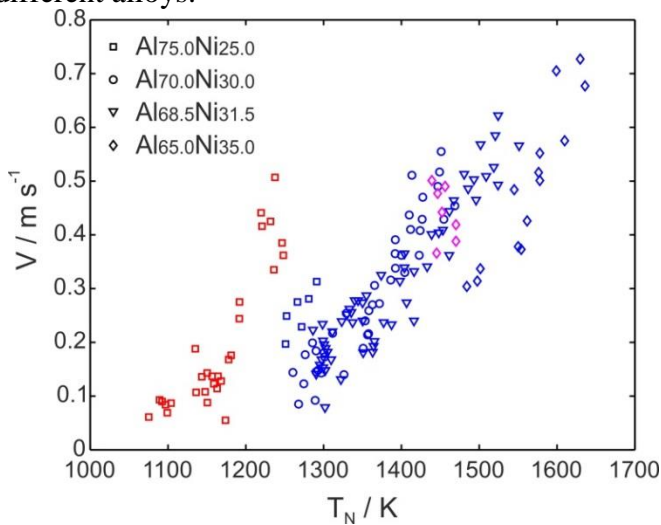


Figure 7: Growth velocity for Al- x at% Ni ($x = 25, 30, 31.5$ and 35) as a function of nucleation temperature, T_N . Red & Blue inverse velocity trend (V decreasing with ΔT), magenta normal velocity trend (V increasing with ΔT). Most data (blue) follow a single trend with T_N .

The specific conditions of reduced gravity with a quiescent state of the freely suspended liquid drop give favourable conditions for the direct observation of the intersection line of sample surface and dendritic solidification front, and the processes running in this region during propagation of the solid/liquid interface through the sample. Figure 8 shows an image sequence

from the high-speed camera for cycle 05. The video illustrates that the growth front is built by sequential nucleation events propagating along the surface, we denote them as *scales*.

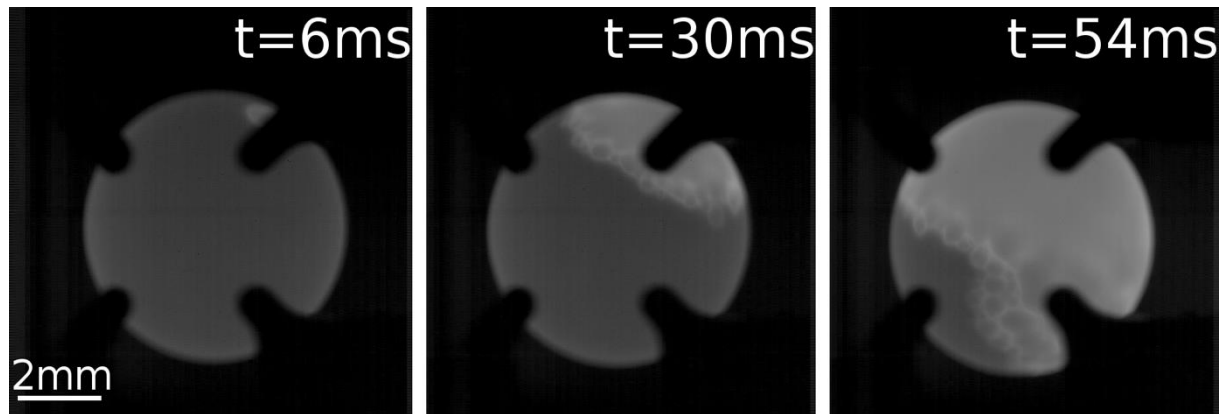


Figure 8: Image sequence of the high-speed camera of an Al₇₅Ni₂₅ alloy solidified in microgravity at an undercooling of $\Delta T=179$ K using the ISS EML multiuser facility.

The observed growth front is not dendritic, but a front of multiple nucleation events propagating along the sample surface. In Figure 9 the crystals that nucleated in front of the solidification front are bounded by circles. From each nucleation site, dendrites grow towards the center of the sample, as can be clearly seen by the orientation of the primary dendrites, as shown in Figure 10 and Ref. [27]. Multiple nucleation events have also been observed in sub-millimeter Al₈₀Ni₂₀ droplets solidified using IA, a drop-tube type technique. Rapid solidification of the samples occur during free-fall with minimal convection. Figure 11 shows select synchrotron X-ray microtomography slices of a 310 μm diameter droplet atomized in helium. Several nucleation points are observed at the surface of the droplet. Similarly to EML samples, dendrites grow towards the center of the droplet.

The idea of a feedback mechanism is put forward to explain the decreasing velocity with increasing undercooling. The increase in temperature and change in composition influence the active layer of nucleation around the growing dendrite. Crystal nucleation and growth lead to the release of heat and rejection of solute from the solid/liquid interface, which is expected (as opposed to the experimental observation) to impede nucleation in the vicinity of already existing nuclei; additional mechanisms, e.g. inward fluid flow due to solidification shrinkage at the dendrite tips need to be considered.

In the temperature range far away from the glass temperature, as in the present case of Al-Ni alloy, the nucleation rate rapidly increases with undercooling. That means that the amount of heat released at the solidification front by copious crystallization is large enough to prevent further undercooling to proceed. As a consequence, the reduction of the growth velocity continuously increases with increasing undercooling. Measuring the front velocity in the microgravity experiments reproduces this behavior as already found in previous experiments on Earth. The higher the undercooling the higher the nucleation rate and, hence, the heat released in front of the solid-liquid interface. As a consequence, the driving force for the advancement of the solidification front becomes reduced with further increasing the undercooling. In principle this new findings concerning the propagating nucleation front is essential in understanding the microstructural evolution.

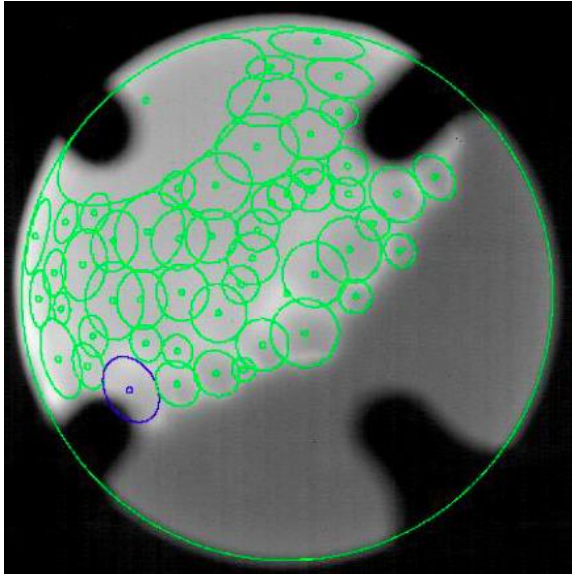


Figure 9: Image taken from the high-speed camera video during solidification of a Al₇₅Ni₂₅ sample upon an undercooling of 275 K prior to solidification using the EML on board the ISS. The green circles adumbrate the crystals which are formed by copious nucleation in front of the propagating solid-liquid interface. The first nucleation event was on the upper left side (large circle). Evaluation of experiments performed on board the International Space Station in June 2017.

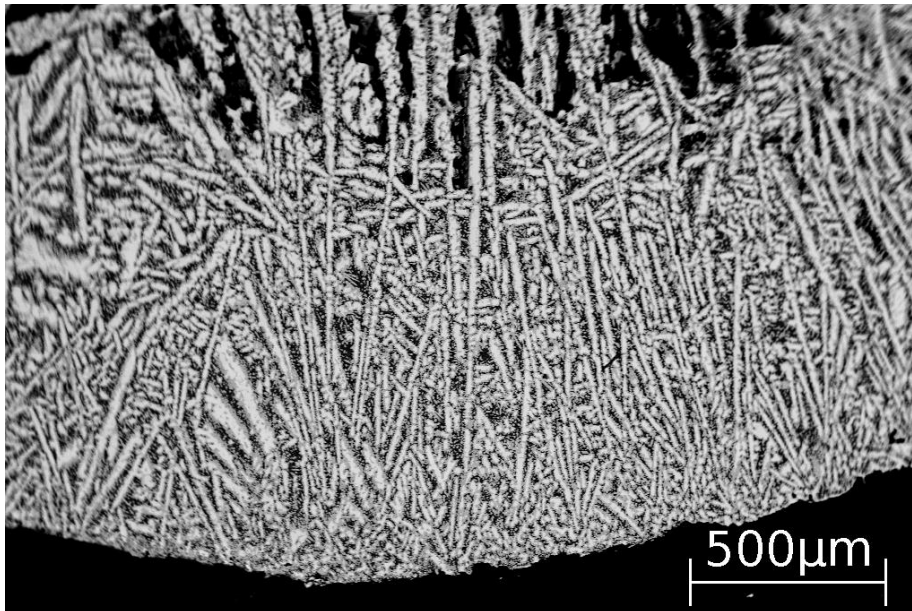


Figure 10: Microstructure of an Al₇₅Ni₂₅ alloy solidified on Earth at an undercooling of $\Delta T=85\text{K}$. Growth direction of the dendrites is from the sample surface to the center.

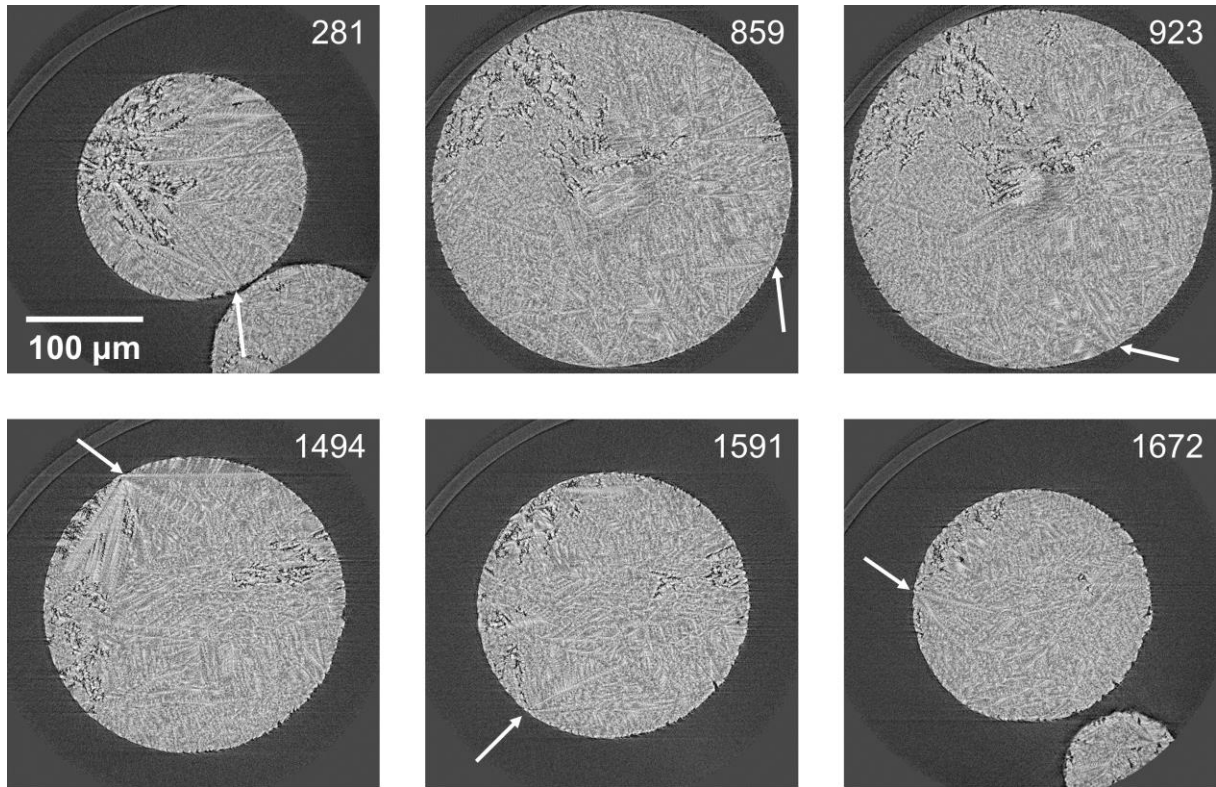


Figure 11: Select synchrotron X-ray microtomography slices of a 310 μm $\text{Al}_{80}\text{Ni}_{20}$ droplet atomized in helium. The arrows denote nucleation points at the surface of the droplets with primary dendrite arms growing towards the center of the droplet.

A scales morphology has been observed at undercoolings $\Delta T < 300$ K (cf. also the red circles in figure 2). At larger undercoolings of $\Delta T > 300$ K, the morphology of the solidification front changes. Figure 12 shows an image taken from the high-speed camera recorded during solidification of an $\text{Al}_{75}\text{Ni}_{25}$ sample undercooled by $\Delta T = 344$ K prior to solidification. The morphology of the solidification front differs from figures 8 and 9 in that spikes on a macroscopic scale are formed which are not visible during solidification of the same sample at smaller undercoolings. We denote such structures as spiked morphology (cf. green circles in figure 2). This has not been observed in terrestrial experiments. This morphology does not show the circular shape of the nuclei but an anisotropic shape.

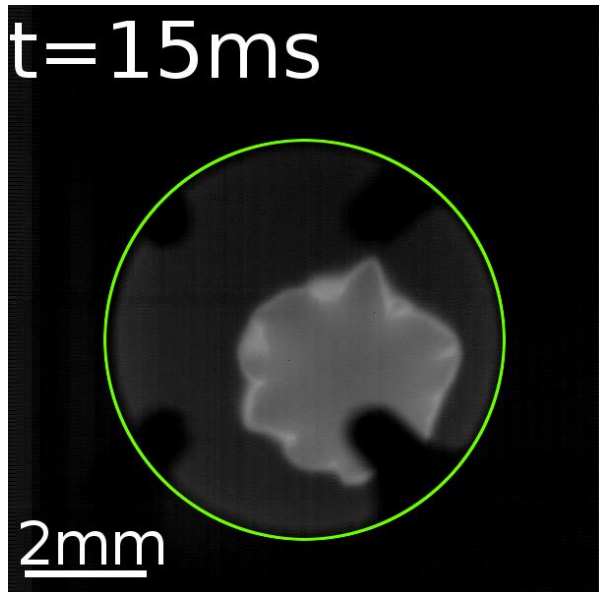


Figure 12: A spiky morphology is observed during solidification of an $\text{Al}_{75}\text{Ni}_{25}$ alloy undercooled by $\Delta T = 344$ K in the microgravity environment. Such a morphology has not yet been observed on Earth. The green circle marks the sample outline. It is emphasized that the microgravity experiments give the benefit of a strong reduction of convective flow. This special experimental condition made it possible to observe not only the spiky morphology but also the copious crystallization in front of the solid/liquid interface that may be origin of the anomalous growth behavior of undercooled Al-rich Al-Ni alloys.

Conclusions

The solidification behavior of undercooled melts of Al-rich Al-Ni alloys has been investigated and discussed. In particular, the anomalous growth dynamics, i.e. the decrease of the growth velocity with increasing driving force for crystallization (undercooling) was analysed with respect to various physical phenomena. Possible effects of forced convective flow inside the liquid sample have been studied by comparing experimental measurements of the dendrite growth velocity as a function of undercooling of $\text{Al}_{75}\text{Ni}_{25}$ samples using electromagnetic levitation on Earth (strong fluid flow) and microgravity on board the International Space Station. Also, inverse melting was subject of the search of the physical origin of anomalous dendrite growth. Dendrite growth in undercooled melts of Al-rich Al-Ni samples was simulated both by phase field and sharp interface modeling, in particular proofing the growth kinetics of the intermetallic phases AlNi , Al_3Ni_2 , and Al_3Ni which are involved in the complete solidification process of the Al-rich Al-Ni alloys. None of these investigations led to a convincing explanation of the anomalous growth characteristics of the alloys investigated. However, the space experiments allowed very clear recording of temperature-time profiles and high-speed camera videos of the propagating solidification front during solidification of the undercooled melt. That was possible since the levitated liquid drops behave much more quiescent in Space compared with levitation on Earth. The reason is that levitation on earth needs much higher levitation forces to compensate the gravitational force than the positioning forces in reduced gravity to compensate disturbing accelerations. Thus, the external influence of the alternating electromagnetic fields both on the oscillations of the drop inside the coil systems as well as the internal fluid flow motion inside the drop is very much reduced in Space. The results of these measurements allowed to directly detect and observe multiple nucleation events in front of the solid/liquid interface. Since copious nucleation leads to the release of the heat of crystallization, it leads to a reduction of the temperature gradient in front of the interface and hence to a reduction of the dendrite growth velocity. The nucleation rate steeply rising with increasing undercooling, the effect of copious nucleation becomes stronger with increasing undercooling and leads to a monotonous decrease of the dendrite growth velocity with increasing undercooling.

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References

- [1] M. Asta, C. Beckermann, A. Karma, W. Kurz, R. Napolitano, M. Plapp, G. Purdy, M. Rappaz, and R. Trivedi, *Acta Mater.* **57**, 941 (2009).
- [2] D.M. Herlach, P. Galenko, and D. Holland-Moritz, *Metastable solids from undercooled melts*, Pergamon Materials Series, edited by R.W. Cahn (Elsevier, Oxford, 2007).
- [3] K.F. Kelton and AL Greer, *Nucleation in Condensed Matter: Applications in Materials and Biology*, Elsevier (2010) ISBN: 978-0-08-042147-6. (726 pp).
- [4] H. Wang, D.M. Herlach, R. Liu, *Dendrite growth in Cu₅₀Zr₅₀ glass-forming melts, thermodynamics versus kinetics*, *EPL* **105** (2014) 36001.
- [5] R. Lengsdorf, D. Holland-Moritz, D.M. Herlach, *Anomalous dendrite growth in undercooled melts of Al–Ni alloys in relation to results obtained in reduced gravity*, *Scr. Mat.* **62** (2010) 365-367.
- [6] H. Peng, D.M. Herlach, T. Voigtmann, *Crystal growth in fluid flow: Nonlinear Response effects*, *Physical Review Materials*, **1** (2017) 030401(R).
- [7] S. Reutzel, H. Hartmann, P.K. Galenko, S. Schneider, D.M. Herlach, *Change of the kinetics of solidification and microstructure formation induced by convection in the Ni-Al system*, *Applied Physics Letters* **91** (2007) 041913.
- [8] S. Reutzel, H. Hartmann, P.K. Galenko, S. Schneider, D.M. Herlach, *Change of the kinetics of solidification and microstructure formation induced by convection in the Ni-Al system*, *Appl. Phys. Lett.* **91** (2007) 041913.
- [9] A.L. Greer, *The thermodynamics of inverse melting*, *J. Less. Comm. Met.* **140** (1988) 327.
- [10] The authors thank A.L. Greer to focus our interest on inverse melting as a possible reason for anomalous dendrite growth in Al-Ni alloy melts.
- [11] We thank HYDRO Aluminium Deutschland for delivering the high purity Al for sample preparation.
- [12] D.M. Herlach, *Non-equilibrium solidification of undercooled melts*, *Metals* **4** (2014) 196 - 234.
- [13] A. Ilbagi, P. Delshad Khatibi, I.P. Swainson, G. Reinhart, H. Henein, *Microstructural analysis of rapidly solidified aluminium - Nickel alloys*, *Canadian Metallurgical Quarterly*, **50** (3) (2011) 295-302.
- [14] A. Blatter and M. von Allmen, *Reversible amorphization in laser-quenched Titanium alloys*, *Phys. Rev. Lett.* **54** (1985) 2103.
- [15] T. Schenk, V. Simonet, D. Holland-Moritz, R. Bellissent, T. Hansen, P. Convert, D.M. Herlach, *Temperature dependence of the chemical and topological short-range order in undercooled and stable Al-Fe-Co liquids*, *Europhysics Letters* **65** (2004) 34-40.
- [16] D. Holland-Moritz, T. Schenk, V. Simonet, R. Bellissent, P. Convert, T. Hansen, D.M. Herlach, *Short range order in undercooled metallic liquids*, *Materials Science & Engineering A* **375-377** (2004) 98 - 103.
- [17] D. Holland-Moritz, O. Heinen, R. Bellissent, T. Schenk, D.M. Herlach, *Short-range order of liquid Ti_{72.3}Fe_{27.7} investigated by a combination of neutron scattering and X-ray diffraction*, *Int. J. Materials Research* **97** (2006) 1–7.

-
- [18] H. Hartmann, D. Holland-Moritz, P. Galenko, D.M. Herlach, *Evidence of the transition from ordered to disordered growth during rapid solidification of an intermetallic phase*, Europhysics Letters **87** (2009) 40007 (6pp).
- [19] O Shuleshova, D. Holland-Moritz, W. Löser, G. Reinhart, G.N. Iles, B. Büchner, EPL **86** (2009) 36002.
- [20] D. Turnbull, *Under what conditions can a glass be formed?* Contemp. Phys. **10** (1969) 473.
- [21] D. Tourret, G. Reinhart, Ch.-A. Gandin, G.N. Iles, U. Dahlborg, M. Calvo-Dahlborg, C.M. Bao, *Gas atomization of Al-Ni powders: Solidification modelling and neutron diffraction analysis*, Acta Materialia **59** (2011) 6658-6669.
- [22] D. Tourret, Ch.-A. Gandin, T. Volkmann, D.M. Herlach, *Multiple non-equilibrium phase transformations: Modeling versus electro-magnetic levitation experiment*, Acta Materialia **59** (2011) 4665-4677.
- [23] P.K. Galenko and D.A. Danilov, *Model for free dendritic alloy growth under interfacial and bulk phase nonequilibrium conditions*, J. Crystal Growth **197** (1999) 992-1002.
- [24] P.C. Bollada, C.E. Goodyer, P.K. Jimack, A.M. Mullis and F.W. Yang, *Three dimensional thermal-solute phase field simulation of binary alloy solidification*, J. Comp. Phys. **287** (2015) 130-150.
- [25] J. Rosam, P.K. Jimack and A.M. Mullis, *Quantitative phase-field modeling of solidification at high Lewis number*, Phys. Rev. E **79** (2009) 030601.
- [26] J. Lipton, W. Kurz and R. Trivedi, *Rapid dendrite growth in undercooled alloys*, Acta Metallurgica **35** (1987) 957-964.
- [27] M. Reinartz, P. Paul, S. Koch, S. Burggraf, M. Kolbe, D.M. Herlach, P.K. Galenko, M. Rettenmayr, *Anomalous dendrite growth kinetics in Al-Ni revisited*. submitted to Acta Materialia.