Design of FPGA-based Accelerators for Deflate Compression and Decompression using High-Level Synthesis

by

Morgan Ledwon

A thesis submitted in partial fulfillment of the requirements for the degree of

Master of Science

 in

Integrated Circuits and Systems

Department of Electrical and Computer Engineering

University of Alberta

 $\bigodot\,$ Morgan Ledwon, 2019

Abstract

As the volumes of data that are transmitted over the internet continue to increase, data compression is becoming increasingly necessary in order to efficiently utilize fixed data storage space and bandwidth. The Deflate compression algorithm is one of the most widely used lossless data compression algorithms, forming the basis of the .zip and .gzip file formats as well as the Hypertext Transfer Protocol (HTTP). The provision of Field-Programmable Gate Arrays (FPGAs) to implement hardware accelerators alongside conventional Central Processing Unit (CPU) servers in the Internet cloud is becoming increasingly popular. The ability for FPGAs to be rapidly reprogrammed and the inherently parallel resources that they provide makes FPGAs especially well suited for certain cloud-computing applications, like data compression and decompression. High-Level Synthesis (HLS) is a relatively new technology that enables FPGA designs to be specified in a high-level programming language like C or C++, instead of a hardware description language, as done conventionally, and enables designs to be implemented at a faster pace. This thesis examines the design and implementation of FPGA-based accelerators for both Deflate compression and decompression using high-level synthesis.

In Deflate compression, a balance between the resulting compression ratio and the compression throughput needs to be found. Achieving higher compression throughputs typically requires sacrificing some compression ratio. In Deflate decompression, the inherently serial nature of the compressed format makes task-level parallelization difficult without altering the standard format. In order to maximize the decompression throughput without altering the format, other sources of parallelism need to be found and exploited. Both our compressor and decompressor designs were specified in C++ and synthesized using Vivado HLS for a clock frequency of 250 MHz on a Xilinx Virtex UltraScale+ XCVU3P-FFVC1517 FPGA. Both were tested using the Calgary corpus benchmark files. In the design of the compressor, many different areas of the design that affect the trade-off between compression ratio and compression throughput, such as the hash bank architecture and hash function, are examined. Our implemented compressor design was able to achieve a fixed compression throughput of 4.0 GB/s while achieving a geometric mean compression ratio of 1.92 on the Calgary corpus. In the design of the decompressor, various FPGA hardware resources are utilized in order to increase the amount of exploitable parallelism such that the decompression process can be accelerated. Our decompressor design was able to achieve average input throughputs of 70.73 MB/s and 130.58 MB/s on dynamically and statically compressed files, respectively, while occupying only 2.59% of the Lookup Tables (LUTs) and 2.01% of the Block Random-Access Memories (BRAMs) on the FPGA.

Preface

Chapter 4 of this thesis has been published as M. Ledwon, B.F. Cockburn, and J. Han, "Design and evaluation of an FPGA-based hardware accelerator for Deflate data decompression," in IEEE Canadian Conference of Electrical and Computer Engineering (CCECE), 2019, pp. 195-200. The design work and manuscript composition was done by myself with supervision and manuscript edits contributed by B.F. Cockburn and J. Han.

Acknowledgements

I would like to thank my supervisors, Bruce Cockburn and Jie Han, for giving me the opportunity to work alongside them and for providing guidance during my MSc program. Thank you Bruce for helping me overcome the many challenges and road blocks I encountered during my work and thank you for showing confidence in me even when I wasn't confident in myself.

I would like to thank the members of our industrial collaborator, Eideticom, specifically Roger Bertschmann, Stephen Bates, and Saeed Fouladi Fard, for proposing the idea for this project, for supporting the funding for this project, and for giving me the opportunity to work together with them. Thank you Saeed for the technical advice and assistance throughout the duration of the project.

I would like to thank the Natural Sciences and Engineering Research Council of Canada (NSERC) for providing grant funding for this project and I would like to thank the Government of Alberta for awarding me three Queen Elizabeth II graduate scholarships.

Contents

1		oduction	1
	1.1	Motivation	1
	1.2	Outline	4
2	Bac	kground	5
-	2.1	The Deflate Lossless Compression Algorithm	5
		2.1.1 Algorithm Details	$\tilde{5}$
		2.1.2 Dynamic Table Construction	10
		2.1.3 Compressed Format Details	11
	2.2	The Calgary Corpus Benchmark	13
	2.3	Literature Review	15
	2.0	2.3.1 Works Related to Compression	15
		2.3.2 Works Related to Decompression	24
	2.4		$\overline{32}$
	2.1	Summary	02
3		I CONTRACTOR	34
	3.1		35
	3.2	Final Design	36
		3.2.1 LZ77 Encoder	37
		3.2.2 Hash Function	43
		3.2.3 Huffman Encoder	47
	3.3		48
	3.4	Discussion	51
	3.5	Summary	54
	Б		-
4		1 0	56
	4.1	Initial Design	56
	4.2	0	60
			61
			64
		4.2.3 LZ77 Decoder	66
		4.2.4 Byte Packer	70
	4.3	Testing and Results	71
	4.4	Discussion	75
	4.5	Summary	78
5	Con	clusion	80
0	5.1		80
	$5.1 \\ 5.2$	Evaluation of Vivado HLS	81
	$5.2 \\ 5.3$		83
	0.0		00
Re	efere	nces	85

Appendix A	LZ77 Encoder Source File	89
Appendix B	LZ77 Encoder Header File	100
Appendix C	Huffman Encoder Source File	103
Appendix D	Huffman Encoder Header File	109
Appendix E	Code Tables File	111
Appendix F	Huffman Decoder Source File	115
Appendix G	Huffman Decoder Header File	131
Appendix H	Symbol Tables File	133
Appendix I	Static Decoding Tables File	134
Appendix J	Literal Stacker Source File	137
Appendix K	Literal Stacker Header File	141
Appendix L	LZ77 Decoder Source File	142
Appendix M	LZ77 Decoder Header File	157
Appendix N	Byte Packer Source File	158
Appendix O	Byte Packer Header File	165

List of Tables

2.1	Deflate Literal/Length Symbol Table and Corresponding Static	
	Codes [2]	9
2.2	Deflate Length Symbol Definitions Table [2]	9
2.3	Deflate Distance Symbol Definitions Table [2]	9
2.4	Deflate Code Length Symbol Definitions Table [2]	10
2.5	The Calgary Corpus Benchmark Files [26]	13
2.6	Past Hardware-Accelerated Deflate Compressors	23
2.7	Past Deflate Decompression Accelerators	32
$3.1 \\ 3.2 \\ 3.3$	Compressor FPGA Resource Utilization	49 50 50
$\begin{array}{c} 4.1 \\ 4.2 \\ 4.3 \\ 4.4 \end{array}$	Decompressor FPGA Resource Utilization Dynamically-Encoded Calgary Corpus Decompression Results Statically-Encoded Calgary Corpus Decompression Results FPGA-based Decompressor Design Comparison	71 73 73 74

List of Figures

2.1	LZ77 Compression Example
2.2	Standard String Matching Using Hash Tables
2.3	Deflate Block Types12Calgary Corpus File Compression Using zlib15
2.4	Calgary Corpus File Compression Using zlib
2.5	LZ77 Sliding Window Architecture
2.6	Scalable Compressor Pipeline Block Diagram
2.7	Compression Ratio and Area Trade-offs with PWS 21
2.8	Two-Pass Speculative Parallelization
2.9	Area-Efficient Huffman Table
01	Commence Dia de Dia mana
3.1	Compressor Block Diagram
3.2	LZ77 Encoder Pipeline Diagram37Hash Bank Architecture38
3.3	
3.4	LZ77 Encoder Match Filtering Example 40
3.5	LZ77 Encoder Output Window Example
3.6	Hash Function Calculation Example
3.7	Hash Function Experimentation Results
3.8	Huffman Encoder Pipeline Diagram
3.9	Hash Bank Design Trade-offs
4.1	Initial Decompressor Architecture
4.2	Coarse Function Scheduling Diagram
4.3	Final Decompressor Architecture
4.4	Huffman Decoder State Diagram
4.5	Huffman Decoder Static Timing Diagrams
4.6	Area-Efficient Huffman Table Decoding Example
4.7	Huffman Decoder Dynamic Timing Diagrams
4.8	Literal Stacker Operation
4.9	Circular Buffer BRAM Cyclic Partitioning
	LZ77 Circular Buffer Access Example 1
4 11	LZ77 Circular Buffer Access Example 2
4 12	Byte Packer Operation
1.14	

List of Abbreviations

- **ALM** Adaptive Logic Module 18, 21, 23, 49, 50
- ASCII American Standard Code for Information Interchange 8, 13, 27, 45
- **ASIC** Application-Specific Integrated Circuit 2, 3, 15
- BRAM Block Random-Access Memory iii, ix, 22, 23, 29–31, 36, 38, 49–52, 54, 56, 57, 63, 66, 67, 71, 74, 77, 78, 81
- **CAD** Computer-Aided Design 3
- **CPU** Central Processing Unit ii, 2, 3, 15, 16, 18, 21, 23, 24, 26, 31, 35
- **CTZ** Count Trailing Zeroes 39
- **DMA** Direct Memory Access 49, 72
- **DRAM** Dynamic Random-Access Memory 22
- **EOB** End-of-Block 8, 10, 12, 24, 25, 28, 56, 62
- **FF** Flip-Flop 22, 23, 29, 49–51, 71, 74
- **FIFO** First-In, First-Out 29, 56, 57, 60, 61, 64, 66, 71, 75
- **FPGA** Field-Programmable Gate Array ii, iii, viii, 2–4, 15, 16, 18, 19, 21–25, 28–32, 34–36, 48–50, 54, 56, 67, 71, 74, 77, 78, 80–82
- FSM Finite-State Machine 61
- **FVP** First Valid Position 39, 40
- **GPU** Graphics Processing Unit 2, 3, 16, 24, 28, 32
- **HLS** High-Level Synthesis ii, 3
- **HTTP** Hypertext Transfer Protocol ii, 5
- **II** Initiation Interval 35, 39, 48, 49, 62, 66, 70, 71, 78, 82
- **IP** Intellectual Property 3, 31, 74, 81
- LUT Lookup Table iii, 22, 23, 28–32, 34, 49–51, 62, 71, 74, 77, 81
- **MUX** Multiplexer 23, 38, 39, 76
- **PWS** Parallel Window Size ix, 15, 17–22, 24, 34, 35, 37, 40, 41, 43, 44, 49, 51, 52, 54

 ${\bf ROM}\,$ Read-Only Memory 16, 20, 23, 47, 62

 ${\bf RTL}\,$ Register-Transfer Level 48, 83, 84

Chapter 1 Introduction

1.1 Motivation

Data compression is used to save data storage space and to more effectively utilize fixed installed communication bandwidth. In today's information age, the volumes of data that are collected, processed, and then transmitted over the Internet continue to increase. Consequently, efficient software and hardware implementations of data compression and decompression algorithms are becoming increasingly valuable. Higher compression ratios¹ allow more data to be packed into the same storage space. In addition, faster compression and decompression engines facilitate faster data transmission.

There are two main types of data compression: lossy and lossless. In lossless compression, the data must be completely restored from a compressed form to its original content following decompression. Conversely, lossy compression is performed on data where loss of information can be tolerated and the compression process can be accelerated by sacrificing some hopefully less important information from the data. For example, the quality of audio and visual data can be degraded to an acceptable extent using lossy compression algorithms (e.g., MPEG-4 for video compression [1]) in order to reduce the data bandwidth for multimedia streaming when necessary. However, many types of data (e.g., financial data, literature, textual documentation, software code,

¹The compression ratio is the ratio between the size of the uncompressed data and the size of the compressed data. A higher compression ratio is generally preferred. E.g., a compression ratio of 2.00 means a compressed file is half the size of its uncompressed form.

genomic data) cannot tolerate any loss in fidelity, so they must be compressed losslessly. Because no information loss can be tolerated, lossless compression cannot be accelerated as aggressively as lossy compression.

Deflate [2] is one of the most widely used lossless compression algorithms today, forming the basis for the widely used .zip, .gz, and .png compressed file formats [3]. In Deflate compression, there is an inverse relationship between the compression time and the compression ratio. Typically, more time can be spent compressing data in order to achieve a greater compression ratio (up to a certain point). Conversely, the compression process can be accelerated by performing less aggressive compression, which is more likely to provide a lower compression ratio. A balance needs to be struck when choosing how much time to spend on compression while still making the process worthwhile (by maximizing the compression ratio) and cost competitive (by minimizing the energy and hardware area usage).

In Deflate decompression, the compression ratio of the received compressed data has already been determined by the compressor and thus the compression ratio is no longer a design parameter that can be traded off in order to increase the speed of decompression. The goal in decompression is to restore the original data as quickly as possible with minimized implementation costs. Unfortunately, the inherently serial format of the Deflate standard makes acceleration difficult using parallel processing strategies. As described later, the standard Deflate compressed format can be altered to easily facilitate acceleration through parallel decompression, but this approach requires deviating from a standard that is already widely being used. Other methods of accelerating the decompression process that respect the constraints of the standard are understandably preferred.

Hardware accelerators are computing platforms that can be used to accelerate certain classes of computations beyond the capabilities of software running on conventional computer Central Processing Units (CPUs). Hardware accelerators are typically implemented using moderately parallel multi-core CPUs, massively parallel Graphics Processing Units (GPUs) [4], Field-Programmable Gate Arrays (FPGAs) [5]–[7], and Application-Specific Integrated Circuits (ASICs). Coinciding with the cloud computing paradigm [8], hardware accelerators are now commonly integrated within cloud servers to accelerate certain algorithms. For example, Amazon Web Services provide access to FPGA-embedded cloud instances (called F1 instances) on a pay-as-you-need basis [9].

There are generally two main methods of accelerating a computation workload [10]: by increasing the clock frequency or by performing more operations of the workload in parallel per clock cycle. Due to the breakdown of Dennard scaling [11], clock frequencies can no longer be substantially scaled up anymore without exceeding practical power and thermal limitations, leaving parallelization as the main solution for accelerating computations [10]. FPGAs and GPUs have massively parallel architectures that often enable them to exploit parallelism more effectively and directly than is possible with CPUs. ASIC designs can be fully customized to achieve the maximum performance for a desired algorithm, but they come at the cost of longer design time, greater engineering risk, high mask costs and, therefore, higher implementation costs.

FPGAs have many advantages. They can be quickly reprogrammed such that accelerator designs can be altered or changed easily as needed. The flexible programmable fabric of hardware resources in an FPGA allows various low-level optimizations to be made to designs, for example, using minimized precision bit-widths (i.e., integer bit widths of any size, not just of powers of two) for storage and computation to save time, area, and power. FPGA-based designs can be developed, verified, and encapsulated as Intellectual Property (IP) blocks that can be later instantiated and easily interfaced together, giving the ability to create modular pipelined designs that can be optimized for maximum throughput.

FPGA designs are typically expressed in a hardware description language like VHDL [12] or Verilog [13]. A relatively new Computer-Aided Design (CAD) technology called "high-level synthesis" (HLS) aims to make FPGA design quicker and easier by allowing designers to specify the required system behaviour in a higher-level language like C or C++, which is then synthesized and optimized automatically into a hardware design (i.e., an FPGA configuration). Although the idea of high-level synthesis was proposed over 30 years ago, it wasn't until recently that the quality of results provided by high-level synthesis solutions became good enough for the technology to become viable [14]. Vivado HLS [15] is the name of the high-level synthesis tool released by Xilinx in 2013 for synthesizing designs for use on Xilinx FPGAs.

This thesis investigates the challenges associated with optimizing and accelerating both Deflate compression and decompression using custom accelerator hardware configurations on FPGAs. Our goal for compression is to design an accelerator that can provide competitive compression throughputs (on the order of multiple GB/s) while maintaining sufficient compression ratios (above 2.00). Our goal for decompression is to design an accelerator that achieves the highest throughputs possible without making any assumptions about the compressed data or making any changes to the standard compressed Deflate format. We aim to do this using an FPGA as the hardware accelerator platform and high-level synthesis as the means of creating the designs, specifically targeting Xilinx FPGAs and using the Vivado HLS tool.

1.2 Outline

The outline of the thesis is as follows: Section 2.1 in Chapter 2 provides background information on the Deflate compression algorithm and format. Sections 2.3.1 and 2.3.2 describe other works related to compression and decompression, respectively. The design of our compressor is described in Chapter 3 and the design of our decompressor is described in Chapter 4. Finally, the results of our work are summarized and suggestions for future work are given in Chapter 5.

Chapter 2 Background

2.1 The Deflate Lossless Compression Algorithm

Deflate is a lossless compression algorithm (and resulting data format) [2] that forms the basis for many widely used file formats. It was originally created by Philip Katz to be used in his software application PKZIP [16] and was shared in the public domain. The Deflate format was later utilized by Jeanloup Gailly and Mark Adler in their open-source software application, gzip [17], and the software library, zlib [18], which was created in order to facilitate the usage of the PNG lossless compressed image format. As a result, Deflate is now commonly used by many different compression and decompression applications [19]. The most notable of these applications include the Hypertext Transfer Protocol (HTTP) standard as well as the aforementioned .zip [20], .gz [21], and .png [22] file formats. Each of these compressed file formats includes a header and footer wrapper that encloses the binary Deflate compressed data payload. Before the Deflate file format is given, we will first describe the basic compression algorithm. Some aspects of the Deflate compression algorithm may vary depending on the implementation, as long as the resulting compressed data adheres to the format described in [2].

2.1.1 Algorithm Details

The Deflate compression algorithm is actually the concatenation of two other well-known compression algorithms: it performs 1) byte-level compression us-



Figure 2.1: An example of LZ77 compression. Note: the physical representation of the length-distance pairs is not defined in the Deflate specification as they will eventually be replaced with Huffman codes. How the length-distance pairs are represented in between the LZ77 encoding and the Huffman encoding is left up to the compressor implementation.

ing a variation of LZ77 encoding [23] followed by 2) bit-level compression using Huffman encoding [24]. Since the LZ77 encoding format is patented, Deflate describes a similar but more general algorithm for replacing duplicated strings. A data file to be compressed is scanned and repeating strings of characters are replaced with length-distance pairs, as shown in Fig. 2.1. As each byte of the file is read, it is recorded in a history buffer and any potential previous matches are sought in that buffer. The length-distance pairs correspond to the length of a match and the distance back within the history buffer that it occurred. In the Deflate format, matching strings of lengths of up to 258 bytes long and match distances of up to 32,768 bytes are allowed. It is desirable to match the longest possible string in the input to a previously stored string in order to compress the greatest number of bytes into a single length-distance pair.

The Deflate specification recommends using chained hash tables to find potential matching strings, though any match-finding method can be used. Typically, a fixed-width sliding window is used, which slides across the sequence of input bytes, as shown in Fig. 2.2a. A string of bytes, the number of which is chosen by the compressor, are taken from the input sequence, hashed (i.e., compressed into a fixed-length hash signature), and looked up in a primary hash table, which contains the positions of all of the most recently hashed and stored strings. If more than one string maps to the same hash signature, the table will contain a link chaining from that signature's position in the primary hash table to a secondary hash table. A chain of such links can be traversed to find all the positions of matching strings that have the same hash value,



Figure 2.2: A standard approach to performing string matching is using a sliding window and chained hash tables.

as shown in Fig. 2.2b. These potential matches are then compared to the current input sequence and the longest match is used to replace those input bytes with a length-distance pair. In order to achieve greater compression, more time can be spent searching for the longest possible match. Limiting the search for a match will save time but may lower the obtained compression ratio. A compressor that is focused on maximizing the compression ratio will thus, in general, need to spend more time performing the LZ77 matching step.

After LZ77 encoding, the data is split into blocks for Huffman encoding. The sequence of unmatched literals and length-distance pairs in each block, which are both referred to as symbols, will be encoded by replacing each symbol with a variable-length codeword. Huffman codes¹ are a type of prefix code, which means that the code for one symbol will never be the prefix of another code. In Deflate, the Huffman codes used are also canonical, which means that all of the codes of the same length have consecutive binary values. This means that the Huffman code tables can be recreated using only the sequence of code lengths [25]. There are two different Huffman encoding methods used by Deflate: static (or fixed) and dynamic. In static encoding, the Huffman codes used are all from pre-defined tables that are listed in the Deflate specifications [2]. These tables are not included with the compressed data. In dynamic encoding, the Huffman codes are created based on the frequencies of the symbols in each block (measured during the preceding LZ77 encod-

¹Following the convention used in the Deflate literature, the *codewords* in a Huffman code will themselves be referred to as Huffman *codes*.

ing stage). The most frequently occurring symbols are typically assigned the shortest Huffman codes in order to achieve the greatest amount of compression. Each dynamically encoded block will have a unique set of dynamic codes that are optimized for the symbols in that block. The dynamic code tables for each dynamic block are encoded along with the compressed data and are used by the decompressor to decode the data during decompression. Though considerably more complicated, encoding Deflate blocks using dynamic Huffman codes instead of static codes allows greater compression ratios to be achieved.

There are actually two Huffman code tables used for each block: one for literals and lengths (shown in Table 2.1), and the other for distances (shown in Table 2.3). This can be done because a distance code will only ever follow a length code, which allows the same binary codes (with different meanings) to be re-used between the two tables. There is also one special symbol, called the End-of-Block (EOB) marker, that is included in the literal/length Huffman table. Symbols 0 to 255 directly correspond to the American Standard Code for Information Interchange (ASCII) literal values 0 to 255, symbol 256 is the EOB marker, and symbols 257 to 287 are the length symbols, which are described in Table 2.2. Note that length symbols 286 and 287 are not actually used for encoding but are, rather, used in the construction of the Huffman code. The distance table (Table 2.3) contains 30 different distance symbols from 0 to 29. Each length and distance symbol corresponds to a base length or distance value and may be followed by a number of extra bits. These extra bits correspond to a binary offset that is added to the base length or distance value after decoding.

In Deflate static Huffman encoding, the literal/length codes are from 7 to 9 bits long (shown in Table 2.1) and the distance codes are fixed-length 5-bit codes that are just the binary values of their symbols (e.g., the static code for distance symbol 5 is 0b00101). In dynamic encoding, both the literal/length and distance codes can be from 1 to 15 bits long. In both forms of encoding, static and dynamic, the length codes may be followed by 0 to 5 extra bits (as shown in Table 2.2) and distance codes may be followed by 0 to 13 extra bits (as shown in Table 2.3).

Symbol Type	Symbol Decimal	Static Code	Static Binary
	Values	Lengths	Codes
Literal	0 - 143	8 bits	00110000 - 10111111
	144 - 255	9 bits	110010000 - 111111111
End-of-block	256	7 bits	0000000
Length	257 - 279	7 bits	0000001 - 0010111
	280 - 287	8 bits	11000000 - 11000111

Table 2.1: Deflate Literal/Length Symbol Table and Corresponding Static Codes [2]

Table 2.2: Deflate Length Symbol Definitions Table [2]

Length	Length	Extra	Length	Length	Extra	Length	Length	Extra
Symbol	Values	Bits	Symbol	Values	Bits	Symbol	Values	Bits
257	3	0	267	15, 16	1	277	67 - 82	4
258	4	0	268	17, 18	1	278	83 - 98	4
259	5	0	269	19 - 22	2	279	99 - 114	4
260	6	0	270	23 - 26	2	280	115 - 130	4
261	7	0	271	27 - 30	2	281	131 - 162	5
262	8	0	272	31 - 34	2	282	163 - 194	5
263	9	0	273	35 - 42	3	283	195 - 226	5
264	10	0	274	43 - 50	3	284	227 - 257	5
265	11, 12	1	275	51 - 58	3	285	258	0
266	13, 14	1	276	59 - 66	3			
260	15, 14	1	276	<u> 9</u> 9 - 00	3			

Table 2.3: Deflate Distance Symbol Definitions Table [2]

Distance	Distance	Extra	Distance	Distance	Extra	Distance	Distance	Extra
Symbol	Values	Bits	Symbol	Values	Bits	Symbol	Values	Bits
0	1	0	10	33 - 48	4	20	1025 - 1536	9
1	2	0	11	49 - 64	4	21	1537 - 2048	9
2	3	0	12	65 - 96	5	22	2049 - 3072	10
3	4	0	13	97 - 128	5	23	3073 - 4096	10
4	5, 6	1	14	129 - 192	6	24	4097 - 6144	11
5	7, 8	1	15	193 - 256	6	25	6145 - 8192	11
6	9,10	2	16	257 - 384	7	26	8193 - 12288	12
7	13 - 16	2	17	385 - 512	7	27	12289 - 16384	12
8	17 - 24	3	18	513 - 768	8	28	16385 - 24576	13
9	25 - 32	3	19	769 - 1024	8	29	24577 - 32768	13

2.1.2 Dynamic Table Construction

As mentioned above, the dynamic Huffman codes used are unique to each dynamic block, so the dynamic code tables need to be included in the compressed data along with each block. In order to include the tables while ensuring that they take up as little space as possible, they are compressed using the following method. Since the Huffman code tables are canonical, they can be recreated using only the sequence of code lengths in the table. An algorithm for constructing a Huffman table using a sequence of code lengths as well as an example are given in Section 3.2.2 of [2]. In Deflate, this sequence follows the order of the literal/length symbol values from 0 to 287. For example, the first code length in the sequence will be for symbol 0, followed by the code length for symbol 1, etc. This sequence is immediately followed by the sequence of code lengths for the distance symbols 0 to 29. Any unused symbols are given code lengths of 0 and if they come at the end of the sequence, they are deleted from the sequence in order to save space. At a minimum, there will be 257 literal/length code lengths in the sequence (for the 256 literals plus the EOB symbol) and 1 distance code length (indicating that no length-distance pairs exist in the data). Once the full sequence of code lengths is input and the number of codes of each length is counted, the codes can be reconstructed starting from the smallest code length.

The code length sequence used to reconstruct the Huffman tables is also compressed using a combination of run-length encoding and Huffman encoding. A 19-symbol Huffman code table, shown in Table 2.4, is used to encode the code length sequence. In this table, symbols 0 to 15 correspond to code lengths 0 to 15, while symbols 16, 17, and 18 are used to encode runs of re-

Table 2.4: Deflate Code Length Symbol Definitions Table [2]

Code Length Symbol	Meaning
0 - 15	Code lengths 0 - 15
16	Copy previous code length 3 - 6 times (2 extra bits).
17	Repeat code length of 0, 3 - 10 times (3 extra bits).
18	Repeat code length of 0, 11 - 138 times (7 extra bits).

peating code lengths. Again, unique codes are created for these symbols and so another sequence of code lengths must be included in order to reconstruct this table. This sequence of "code length" code lengths is included in the compressed block in the following fixed order: 16, 17, 18, 0, 8, 7, 9, 6, 10, 5, 11, 4, 12, 3, 13, 2, 14, 1, 15. The first four code lengths are always included in this sequence while the rest appear in the order of the likelihood that they will be used. Code lengths for the symbols 8, 7, and 9 come first as they are the most likely code lengths to be used while code lengths of 1 and 15 are relatively rare and so they appear at the end of the sequence. As done before with the literal/length and distance code length sequence, any unused code lengths at the end of the sequence are removed. The process of reconstructing the Huffman tables for a dynamic data block is described step-by-step as follows:

- 1. The number of literal/length codes, distance codes, and code length codes is read from the compressed block.
- 2. The sequence of "code length" code lengths is read and the number of codes of each length is counted.
- 3. The "code length" code length count is used to construct the code length Huffman table.
- 4. This code length Huffman table is used to read and decode the sequence of code lengths for the literal/length and distance code tables.
- 5. The literal/length and distance code length counts are used to construct the literal/length and distance Huffman tables.

2.1.3 Compressed Format Details

As described above, a file compressed using Deflate is split into blocks of arbitrary size which are then each Huffman encoded individually. None of the binary data within a static or dynamic Deflate block is guaranteed to be byte-aligned. In a dynamic block, the last bit of the code length sequence is immediately followed by the first bit of the first Huffman code in the data.

EOB						
Dynamic Block						
essed Data EOB						
Stored Block						
ressed Data						

Figure 2.3: Deflate block types and their contents (not to scale).

Since the codes are variable-length, each code must be decoded one at a time, bit-by-bit, starting with the first Huffman code. The length of a Deflate block is unknown until the EOB code has been found and decoded. The beginning of the next block begins immediately after the EOB code. Besides static and dynamic blocks, a third type of block exists that is called a *stored* block, which contains uncompressed data. Stored blocks are typically used in order to avoid attempting to compress data which cannot be usefully compressed further, for example, data which has already been compressed, in order to prevent expanding the data². Figure 2.3 shows the structures of the three different block types. Each block begins with a 3-bit header that is composed of two flags: BFINAL (1 bit), which indicates whether a block is the last block. The BTYPE value is 0b00 for stored blocks, 0b01 for static blocks, and 0b10 for dynamic blocks.

There are a few subtle but critical pieces of information about how the compressed data is actually stored. In the Deflate format, all of the data elements (i.e., Huffman codes, block headers, code lengths, etc.) are packed into bytes starting with the least significant bit of the byte. All of these elements, except for Huffman codes, are packed with their least significant bit first while the Huffman codes are packed with their most significant bit first. This means that the Huffman codes are effectively reversed in bit order while

²The amount of expansion that can occur will depend on the compressor implementation. In the worst case scenario, zlib adds 5 bytes per 16 kB stored block (an overhead of about 0.03%). The zlib wrapper also adds 6 bytes of overhead to the file [18].

all other data elements appear in the correct bit order (i.e., most significant bit to least significant bit). Each byte of compressed Deflate data is meant to be processed from right to left with new bytes being appended to the left as they are read.

2.2 The Calgary Corpus Benchmark

The Calgary corpus [26] is a dataset composed of 14 files of various data types with different sizes that has been commonly used as a benchmark in compression and decompression research. This benchmark has been used by many other researchers whose work is described in Section 2.3. For purposes of comparison, we also use the Calgary corpus to measure the performance of both our compressor and decompressor designs. Table 2.5 describes the 14 different Calgary corpus files. The type of data contained within a file plays a key factor in the compression ratios achieved as well as the speed of compression and decompression.

As mentioned above, dynamic Huffman blocks can be used to get higher compression ratios than static blocks. This makes sense because the dynamic blocks use Huffman codes that are tailored to the statistics of each block while static blocks use standard Huffman codes that are a compromise for all types of data files. Figure 2.4 shows the difference in compression size of the Cal-

File Name	Size (bytes)	Description
bib	111,261	Bibliography containing ASCII text in Unix "refer" format
book1	768,771	Fiction book containing unformatted ASCII text
book2	610,856	Non-fiction book containing ASCII text in Unix "troff" format
geo	102,400	Geophysical seismic data in 32-bit number format
news	377,109	USENET batch file containing ASCII text
obj1	21,504	Object code executable of file "progp"
obj2	246,814	Object code executable of Macintosh program
paper1	53,161	Technical paper containing ASCII text in Unix "troff" format
paper2	82,199	Technical paper containing ASCII text in Unix "troff" format
pic	513,216	1728x2376 bitmap image
proge	39,611	Source code file written in C
progl	71,646	Source code file written in LISP
progp	49,379	Source code file written in Pascal
trans	93,695	Transcript of terminal session

Table 2.5: The Calgary Corpus Benchmark Files [26]

gary corpus files when compressed using static codes versus dynamic codes. These numbers were obtained by compressing the files using zlib with the default settings³. The arithmetic mean (average) compression ratio across the dynamically compressed corpus is 3.51 and the geometric mean is 3.19. For the statically compressed files, the arithmetic mean is 3.03 and the geometric mean is 2.76. Both means are described here because both figures of merit are reported by the compression related works described in Section 2.3.1. Compared to the arithmetic mean, the geometric mean places more weight on each value averaged and will therefore always be lower. This makes it more useful when averaging numbers with widely different values (like the very large compression ratio of the "pic" file and the very small compression ratio of the "geo" file). While the arithmetic mean is obtained by dividing the sum of a set of n values like so:

$$\frac{1}{n}\sum_{i=1}^{n}a_{i} = \frac{a_{1} + a_{2} + \dots + a_{n}}{n}$$

the geometric mean is obtained by taking the nth root of the product of n values as follows:

$$\left(\prod_{i=1}^{n} a_i\right)^{\frac{1}{n}} = \sqrt[n]{a_1 a_2 \dots a_n}$$

By using dynamically created Huffman codes instead of static codes, the compression ratios are improved by an average of 15.7%. However, using dynamic Huffman encoding requires more time to perform both compression and decompression. During compression, the symbol frequencies need to be measured and the code tables need to be constructed before encoding. In decompression, the compressed code length sequence needs to be read and used to reconstruct the code tables. When using static codes, encoding/decoding can begin immediately using the fixed standard code tables.

³The zlib compression settings include compression effort (the amount of the time to spend searching for matches), history buffer size, sliding window size, and compression strategy (Huffman encoding only without LZ77 encoding, static Huffman encoding only without dynamic, etc.) among other things.



Figure 2.4: Compression of the Calgary corpus using zlib with the default compression settings.

2.3 Literature Review

2.3.1 Works Related to Compression

In this section, a few of the most recent and most significant published designs of FPGA-based Deflate compression accelerators are described. Many compression accelerators have been developed over the years for a variety of hardware platforms, including CPUs and ASICs, but only FPGA designs are analyzed in detail here since FPGA-based accelerators are the main focus of this thesis. These designs share a similar architecture composed of a constantthroughput pipeline that compresses a fixed number of bytes in every clock cycle using a parallel sliding window. The size of this window is often referred to as the Parallel Window Size (PWS). The main focus of these designs appears to be on the LZ77 encoding portion, which is the more complicated of the two stages of Deflate compression. Instead of spending time searching for matches, only one clock cycle is spent obtaining potential matching strings and comparing them to the strings in the sliding window. Afterwards, only the best matches that are found within the window constraint are kept. Multiple potential matches are looked up and compared simultaneously with multiple substrings within the sliding window in every cycle in order to quickly compress the data at a constant rate. How the data history is stored and how potential matches are found will greatly impact the performance and area of the design. Most seemingly throughput-focused designs perform the Huffman encoding using static codes only. This restriction greatly simplifies the interface between the LZ77 encoder and the Huffman encoder as the data can be encoded as soon as it is received using the fixed standard code tables stored in Read-Only Memories (ROMs). Although these FPGA-based compressor designs typically provide lower compression ratios than are possible with software compressors, they are able to compress data at a much faster rate. The FPGA-based compressor designs examined are described chronologically below. The design of our compressor, described in Chapter 3, was influenced by each of these designs.

The authors of [27] designed an FPGA-based accelerator for Deflate compression using OpenCL and Intel/Altera's OpenCL compiler. OpenCL is a high-level C-like programming language that can be used to specify hardware acceleration kernels for parallel computing platforms that include CPUs, GPUs, and/or FPGAs. Their design appears to be heavily based on the Verilog architecture described in [28] by researchers at IBM. Reference [28] is unfortunately no longer available for access. In traditional LZ77 encoder designs, the history dictionary, which contains all of the previous input bytes arranged in chronological order, and the hash table, which contains the positions of previously hashed strings, occupy two separate memories. Multiple single-byte reads may be required to read an entire string from the history dictionary unless the memory is partitioned to allow for more read ports that can be accessed in parallel. Multiple copies of the history dictionary can be used to allow conflict-free simultaneous lookup of multiple strings, however, hash collisions (i.e., when two or more strings produce the same hash signature) can still occur into the hash table and these collisions will reduce the number of positions that can be read and written, resulting in potential matches being missed and thus leading to a reduction of the compression ratio. In the design in [27], the history dictionary and the hash table are combined into the same memory. This memory stores entire strings (instead of individual bytes) as



Figure 2.5: The LZ77 sliding window architecture from [27] with a PWS of 4. Every dictionary is accessed simultaneously by every one of the substrings.

well as their positions. When the hash signature of an input string is given to the memory, a similar string with the same hash signature is returned. These returned strings are then compared byte-by-byte with the substrings within the sliding window in order to find matches.

Fig. 2.5 shows the sliding window architecture from [27] with a PWS of 4 bytes, though in the actual design, a PWS of 16 was used. In every clock cycle, 16 bytes are read from the input stream and are shifted into a 32-byte wide sliding window (twice the length of the PWS). Each byte in the first half of the 32-byte window is the start of a 16-byte substring, with a total of 16 staggered substrings occupying the entire window. For each 16-byte substring in the 32-byte window, a hash value is calculated in parallel and then looked up in 16 different dictionaries. Sixteen 16-byte potential matches are obtained from each dictionary for each substring for a total of 256 potential matches. The 16 different history dictionaries are replicated 16 times so that each one has 16 read ports and all 16 substring reads can occur simultaneously without the possibility of hash conflicts. Each substring in the parallel window is then written to one of the 16 dictionaries. The dictionaries are indexed using a 10-bit hash signature and have 1024 indexes each, which each store a 16-byte string and its position. The 256 potential matches are compared to the 16 window substrings and the longest match for each substring is kept. Since the substrings and the potential matches are 16 bytes long, the longest possible match length is 16 bytes. The 16 best matches are then filtered using a series of filters. Matches that are overlapped by matches from the last iteration and matches that overlap each other in the current iteration are filtered away using last-fit heuristics. The matches in the window are replaced with markers and are then Huffman encoded. In this architecture, the Huffman trees are created by software executing on a CPU and are then passed to the FPGA for encoding. Whether only static or dynamic Huffman encoding is used is not disclosed. The symbols are encoded and a series of barrel shifters are used to align the variable-length codes.

Throughout the paper the authors describe certain changes that they made to the OpenCL code in order to optimize it for running on FPGAs. Though the code may be functionally equivalent, certain OpenCL syntaxes may lead to inefficient hardware synthesis. For example, long adder chains, which tend to use more logic area and have greater delay, may be selected by the compiler instead of faster balanced adder trees. These optimization techniques are also applicable when using Vivado HLS to synthesize C/C++ as done in our research. Like in [28], which was the basis of their design, they also mapped their design for an Intel/Altera Stratix V A7 model FPGA. For comparison, the design in [28] had a clock frequency of 200 MHz and an input throughput of 3.0 GB/s. In [27], although they report that their design processes 16 bytes every clock cycle, they achieved an input throughput of 2.84 GB/s with a clock frequency of 193 MHz, which seems to imply that their final design actually used a PWS of 15 bytes, not 16, since a design that processes 16 bytes/cycle at 193 MHz should have a throughput of 3.088 GB/s. Their design has a depth of 87 stages compared to the 17-stage design in [28] and uses more chip area. Reference [27]'s design uses 47% of the logic and 70% of the RAM on the StratixV A7 chip, which one could reasonably interpret to be 110,318 of the 234,720 ALMs⁴ and 1,792 of the 2,560 M20K memory blocks, while the design from [28] only uses 45% of the logic (105,624 ALMs) and 45% of the RAM (1,152 M20Ks). The advantage of [27]'s design comes from the enhanced productivity that comes from using OpenCL instead of Verilog, though it comes at the cost of less-efficient area usage. They evaluated their design

⁴Adaptive Logic Modules (ALMs) are the standard logic cell used in Intel/Altera FPGAs.

using the Calgary corpus and achieved a geometric mean compression ratio of 2.17 across the entire corpus, which is the highest value of the compressor designs compared here. This may be because they use software-created dynamic Huffman tables, while the other designs only utilize static Huffman encoding. It may also be because of the fully connected hash dictionary architecture that they used, which is not susceptible to hash collisions.

Reference [5] describes an FPGA-based compressor design that was created by researchers from Microsoft in response to [27] and [28]. Their design was programmed in SystemVerilog also for use with an Intel/Altera Stratix V FPGA. They use a pipelined parallel window architecture that is scalable to other sizes. In their design, they use the traditional method of separately storing the string match positions in a hash table and the data history in a dictionary. In order to reduce hash table lookup conflicts, the hash table is split into multiple banks, where each bank contains a subset of the possible hash indexes; using more banks reduces the likelihood of two hashed values accessing the same bank. In their design, they use 32 hash banks to index 65,536 hash values (2,048 indexes per bank). These hash banks are also run at double the clock frequency that is used by the rest of the system to allow two reads and two writes to be made to each bank in every clock cycle. This allows two hash values to access the same bank without conflict; any further accesses must be dropped, however, which negatively impacts the compression ratio. In order to store multiple positions for each match, each hash bank can also be split into multiple depth levels with each containing a different previous position. When a hash bank is accessed, all stored previous positions are read simultaneously, the oldest position is shifted out, and the latest input position is shifted in. This technique of hash bank depth levels is described but does not appear to have been used in the final design by [5].

A block diagram of the scalable pipeline architecture from [5] is shown in Fig. 2.6. Although their design is scalable in terms of window size, for illustration, a design with a PWS of 16 bytes will be described. In every cycle, up to 16 positions are obtained from the hash tables and are simultaneously looked up in 16 copies of the history dictionary. Each dictionary copy is partitioned



Figure 2.6: The scalable compressor pipeline architecture from [5].

to have 16 read ports so that 16 consecutive bytes can be read simultaneously (the history dictionaries store individual bytes, not entire strings). Sixteen 16byte strings are returned and compared to the substrings in the input window. A series of match selection stages iteratively filter out conflicting matches in a similar manner as was done in [27]. The selected matches for the window are then Huffman-encoded across multiple pipeline stages. In order to maintain the same steady throughput on both the LZ77 encoding and Huffman encoding portions of the pipeline, only static Huffman codes are used. As LZ77 encoded windows are written out, their contents are passed through to static codebook ROMs to be immediately encoded. If dynamic codes were to be used, the Huffman encoding portion would not be able to begin until the first block from the LZ77 encoding portion was finished and the dynamic code tables were assembled. This would also require an intermediate storage space between the two Deflate stages for holding the LZ77 encoded data (this approach is investigated in [29]). In each stage of the Huffman encoder, one of the window boxes is encoded and then shifted and ORed into an encoded window using barrel shifters. A double buffer, which is located at the output of the pipeline, collects the encoded windows. When the double buffer is over half full, the lower half writes its data to the output.

The authors of [5] synthesized their design with various PWS values from 8 to 32 bytes and obtained performance results for each. With a PWS of 16



Figure 2.7: The effect of varying the PWS on a) the compression ratio on the Calgary corpus and b) the hardware area cost (Figures from [5]).

bytes, their design can compress at an input throughput of 2.8 GB/s with a clock frequency of 175 MHz. The pipeline has 58 stages and it achieves a mean compression ratio of 2.05 on the Calgary corpus. It is unspecified whether this is an arithmetic mean or geometric mean. While the throughput of their design is slightly less than that of [27] and [28] for a 16-byte PWS, their design is much more area-efficient. It uses 39,078 ALMs, which is about one third of the area of the other two designs. Unfortunately, the number of memory blocks used is not disclosed. Their architecture is also designed to be easily scalable to various window widths. As they found from their results, shown in Fig. 2.7, the compression ratio increases logarithmically with the window width while the area for most modules increases quadratically, meaning that diminishing returns are obtained when scaling the window width increasingly high. A 32-byte PWS design has an input throughput of 5.6 GB/s and average compression ratio of 2.09 but uses 2.8 times more chip area than the 16-byte PWS design.

In [6], which focuses on task co-scheduling between CPUs and FPGAs, a compression accelerator is developed using Vivado HLS. Since the focus of paper is not on accelerating compression, minimal details on their compressor design are shared and their results are not very competitive. They based their design on [27] and [5] and used a similar 16-byte PWS pipeline. They used a Xilinx Kintex UltraScale KU115 FPGA with a clock frequency of 200 MHz and achieved a peak bandwidth of 2.8 GB/s. This is less than the expected bandwidth of 3.2 GB/s because of pipeline bubbles (i.e., unused clock cycles) caused by accessing the FPGA external Dynamic Random-Access Memory (DRAM). When compressing the Calgary corpus, they achieved a geometric mean compression ratio of 1.73. Their design uses 12.6% of the Lookup Tables (LUTs) and 4.9% of the Flip-Flops (FFs) on the KU115 chip, which is 83,583 of the 663,360 LUTs and 65,009 of the 1,326,720 FFs. The number of Block Random-Access Memories (BRAMs) used is not disclosed.

As reported in [5], single-engine compressor designs start to become unscalable for very wide PWS values. Consequently, the authors of [7] focused on using multiple compressor engines in parallel in order to improve the compression throughput while maintaining area efficiency. By increasing the number of compressors instead of increasing the PWS, the throughput can be increased while the area usage scales linearly instead of quadratically. This comes at the cost of reduced compression ratios as multiple compressors cannot compress as efficiently as a single compressor due to match opportunities being lost. As also discovered in [5], the compression ratio increases minimally with a wider PWS. This disappointing improvement is because matches of length 24 and 32 are, in practise, rarely encountered in most data files. For these reasons, the authors of [7] chose to use a PWS of 16 bytes for their compressors.

Along with designing a multi-engine compression system, the authors of [7] also made a few improvements over the single compressor design from [5]. Instead of running the hash banks at double the system clock frequency, which limits the overall system clock frequency, they chose to run them using the same clock frequency in order to achieve a higher overall clock frequency. They also use the hash bank architecture with multiple depth levels to store and compare with more previous matches. They use a combination of the banked hash table design from [5] and the combined hash table dictionary from [27]. Their compressor design uses one hash dictionary containing both strings and positions that is split into 32 banks, with each bank having 3 depth levels. At every clock cycle, the 16 substrings in the input window are hashed and will attempt to access one of the 32 banks. Each accessed

bank returns a string and position from each of the 3 depth levels. Instead of mapping the strings read from each bank back to the substring that accessed it for comparison, which would require 16-byte wide Multiplexers (MUXs), they perform the comparisons at the output of each bank before mapping the best match length to each substring, which only requires 5-bit wide MUXs (as the lengths of the matches can only be from 0 to 16). The comparisons can be performed at each bank with the input substrings as they are written to the bank since the read takes place one clock cycle before the write operation. This MUX optimization helps to reduce the area consumption and improve the clock timing. As with previous designs, they perform the Huffman encoding portion using static codes only and using a series of pipeline stages composed of ROM encoders and shift-OR operations.

Each compressor has a clock frequency of 200 MHz and can compress 3.2 GB/s. One compressor engine on its own occupies 38,297 ALMs and is able to achieve an average compression ratio of 2.10 on the Calgary corpus. For comparison with previous works, [27] and [5], they implement a multi-engine compressor on a Stratix V FPGA, which has enough area to fit three compression engines on it. This provides a collective input compression throughput of 9.6 GB/s and an average compression ratio of 2.05. They also implement a four-engine compressor design on a larger Intel Arria 10 FPGA capable of compressing 12.8 GB/s with a compression ratio of 2.03. They found, however, that the CPU-FPGA interface ends up limiting these throughputs to practical values of 3.9 GB/s for the three-engine compressor and 10.0 GB/s for the four-engine compressor.

A summary of all the previous works described is shown in Table 2.6. For

Reference	FPGA	Language	Clock	Input	Area Utilization	Compression
	Platform		Frequency	Throughput		Ratio
[28] (2013)	Stratix V A7	Verilog	200 MHz	3.00 GB/s	105,624 ALMs, 1,152 M20Ks	?
[27] (2014)	Stratix V A7	OpenCL	193 MHz	$2.84~\mathrm{GB/s}$	110,318 ALMs, 1,792 M20Ks	(Geo.) 2.17
[5] (2015)	Stratix V	SystemVerilog	$175 \mathrm{~MHz}$	$2.80~\mathrm{GB/s}$	39,078 ALMs, ? M20Ks	2.05
[6] (2018)	KU115	C/C++	200 MHz	$2.80~\mathrm{GB/s}$	83,583 LUTs, 65,009 FFs,	(Geo.) 1.73
		(Vivado HLS)			? BRAM18Ks	
[7] (2018)	Stratix V	?	200 MHz	$3.20~\mathrm{GB/s}$	38,297 ALMs, ? M20Ks	2.10

 Table 2.6: Past Hardware-Accelerated Deflate Compressors

a fair comparison, the results shown for [5] are for a PWS of 16 bytes and the results shown for [7] are for one compressor engine. The geometric mean compression ratios are identified in the table while the remaining means are uncertain to be geometric or arithmetic. As seen from Table 2.6, although they provide lower compression ratios than software compressors (from Section 2.2: zlib achieves geometric mean compression ratios of 3.19 and 2.76 using dynamic and static compression, respectively), FPGA-based compression accelerators can achieve throughputs on the order of multiple GB/s. This is orders of magnitude faster than software implementations, which can typically compress around 50 MB/s⁵, with some implementations reaching over 300 MB/s [30][31]. GPU-based compression accelerators seem to be rarer but also perform on the scale of hundreds of MB/s [32]. Of the above described FPGA-based compressor designs, the one from [27] stands out for achieving the highest possible compression ratios using a fully connected hash dictionary design, while the design from [7] appears to be the fastest and most scalable singlecore compressor design. These two designs, in particular, influenced our design the most.

2.3.2 Works Related to Decompression

To perform Deflate decompression (sometimes referred to as Inflate), the two main encoding stages, Huffman encoding and LZ77 encoding, need to be reversed. The ability to perform these processes in parallel, however, is significantly hampered by the Deflate compressed format. First, the Huffman encoded blocks need to be parsed and decoded but, as mentioned in Section 2.1, the locations of the boundaries between the blocks are completely unknown. This means each block must be processed serially until the EOB marker has been decoded, which impacts the ability to perform Huffman decoding on more than one block in parallel.

There is one technique for overcoming the problem of finding exploitable

⁵The multi-core server workstation that was used to perform the design and synthesis work in this thesis, containing an i7-3930K CPU and 32 GB of RAM, was able to achieve an average input compression throughput of 7.74 MB/s when dynamically compressing the Calgary corpus.

parallelism called *speculative parallelization*. Once the EOB code is known (either by identifying a block as static or by assembling its dynamic code tables), the compressed data can be scanned ahead for the block's EOB code. If a block's EOB code is found (and therefore the next block boundary is located), the next block can begin being Huffman decoded in parallel with the current block. Unfortunately, the possibility of finding false-positive boundaries exists due to 1) the absence of byte-alignment in the compressed format and 2) the extra bits that follow the length and distance codes, which can mimic the EOB code. Deflate blocks can also be any size and a compressed file could even be composed of only a single Deflate block, meaning that block boundaries can be difficult to find or even be non-existent. It is for these reasons that the process is speculative and any potential speedup obtained is statistical.

Speculative parallelization helps to accelerate the Huffman decoding process but it leaves unaddressed the LZ77 decoding process, which is also difficult to parallelize. Since the length-distance pairs can have distances up to 32,768 bytes away and because Deflate blocks can be any size, it is possible for a length-distance pair to point to data held in another block. This inter-block dependency prevents LZ77 decoding from being performed on multiple blocks in parallel. Some proposed solutions to these problems by related works will be examined. Since the number of published works on decompression accelerator designs is much smaller than on compression accelerators, a broader look will be taken at various papers across different platforms beyond just FPGAbased designs. Decompression throughput can be measured at the input (i.e., bytes of compressed data processed per second) or the output (i.e., bytes of uncompressed data processed per second) and will be specified as such when known.

In paper [33], the authors propose a configurable software algorithm for speculative parallelization. In this algorithm, they add two tests to validate the accuracy of a prospective block boundary. The first test checks the 3-bit block header that follows a block boundary; if BTYPE is 0b11, corresponding to an erroneous block, the boundary is known to be false. The second test is an attempt to perform Huffman table reconstruction for a dynamic Huffman
block; a false boundary may cause errors to occur during the table construction process. It is still possible for false-positive boundaries to pass both of these tests and, if so, it isn't until the first Huffman decoder has processed up to the point that the second decoder started from that it is known for certain, whether or not the speculative work done is valid. The scanner in their algorithm is configurable with different parameter settings like "minimum block length" and "speculated range" in order to aid with boundary prediction. In order to parallelize the LZ77 portion of decompression, they rely on the presence of stored blocks within the compressed file. Since zlib has the tendency to create stored blocks with sizes above 16 kB, the 32 kB history buffer of an LZ77 decoder can be filled using two consecutive stored blocks. This creates a point in the data stream where the LZ77 decoding can be done in parallel. As the authors of [33] found, however, the presence of these stored blocks is unreliable. Many compressed files do not contain any stored blocks at all, and those files that do may not have the blocks uniformly distributed to take advantage of. Because of this, [33] reports speedups of only 1.24 to 1.80 times faster than sequential software decompression (actual decompression throughputs are not given).

The authors of [34] expand on the work done in [33] and implement a speculatively parallel decompression algorithm using Apache Spark [35], a software framework for parallel computing. Using this, multiple speculative threads are spawned across a cluster of CPUs and are each given parts of the compressed file to decompress in parallel. Each thread performs tests to check for falsepositive boundaries as done in [33] and any invalid threads are cancelled. Once all threads are finished, the results are merged and output. In the worst-case scenario, the data is decompressed sequentially using a single thread. No information is given on if and how the LZ77 decoding process is performed in parallel. Using a cluster of six CPUs (containing a total of 24 threads), they achieve average input decompression throughputs between 18 and 24 MB/s, which is a speedup of about 2.6 times compared to sequential decompression (about 7 MB/s).

The authors of [36] investigated the feasibility of randomly accessing parts



Figure 2.8: A diagram showing the two-pass speculative parallelization method (Figure from [36]).

of compressed DNA files, specifically of the FASTQ format [37], and developed a parallel decompression algorithm to accelerate this. These FASTQ files contain DNA sequences and are typically very large, requiring them to be compressed losslessly using an algorithm like Deflate. Because of the Deflate format, in order to access even a small portion of the large FASTQ file, the entire compressed file must be decompressed. For this reason, the authors investigated the ability to begin decompressing a file from a random point within it. Like previous works, they use speculative parallelization to find block boundaries where decompression can be started. FASTQ files are a text-based format that contains byte-aligned ASCII characters with values from 0 to 127. The authors exploit this as another way of testing for falsepositive block boundaries. If a literal character outside of the range is decoded, the speculated block is invalid. In order to parallelize the LZ77 decoding process, they perform two passes on the data. On the first pass they perform LZ77 decoding on each block and skip any back-references that point to undetermined data. Then the data is passed through a second time and the skipped back-references are resolved. A diagram showing this process is shown in Fig. 2.8. While decompressing compressed FASTQ files using 32 threads in parallel, they are able to achieve average input decompression throughputs of 611 MB/s.

As can be seen from the previous paragraphs, the standard Deflate format makes parallelization of the processes difficult. The authors of [4] attempt to overcome these problems by altering the format. By making relatively simple

changes to the Deflate format, they could achieve tremendous decompression speedups. In their so-called "Gompresso" format, each Deflate block is a fixed size and is split up further into sub-blocks. The size of each of these sub-blocks is included in a file header at the beginning of the compressed file, allowing each sub-block to be easily parsed and Huffman decoded in parallel. Since the blocks in the format are compressed in parallel as well, LZ77 back-references between blocks don't exist. This means LZ77 decoding of each block can also be performed in parallel. The authors take things a step further and include the option of preventing nested back-references within a block, eliminating intra-block dependencies as well. This allows a single block to be processed by multiple threads in parallel. The authors implemented their Gompresso compression/decompression framework using GPUs and were able to achieve average output decompression throughputs of over 13 GB/s. This throughput was limited by the PCIe interface and was actually closer to 16 GB/s ignoring data transfer rates. In order to take advantage of these impressive decompression speeds though, the files needed to be compressed using the Gompresso format.

The following related works are decompressor designs implemented using FPGAs. Instead of attempting to parallelize the Huffman and LZ77 decoding processes, these designs aim to exploit the parallel resources on FPGAs in order to accelerate them. The authors of [38] describe a two-core pipelined system composed of a Huffman decoder and an LZ77 decoder. For simplicity, the Huffman decoder is only capable of decoding static Huffman blocks. The Huffman decoder has a 32-bit wide input interface. Since static literal/length codes are anywhere from 7 to 9 bits long, they can be decoded by taking 9 bits from the input and looking them up in a 512-index LUT⁶. The table identifies the data as a literal, a length, or the EOB symbol. If the symbol is a length, the extra bits are obtained and the following 5-bit distance code is looked up in another LUT. The Huffman decoder takes 3 clock cycles to decode a literal and 6 cycles to decode a length-distance pair. The authors claim that the Huffman

⁶All 9-bit codes will appear once in the table, all 8-bit codes will appear twice, and all 7-bit codes will appear four times.

decoder is also capable of processing dynamic codes if the Huffman code tables are recreated off-chip and then given to the FPGA-based accelerator core. Since the dynamic codes can be up to 15 bits long, however, this would require two 32,768 index LUTs to decode both literals/lengths and distances in the same manner. Following decoding, the literal or length-distance pair is then written to the output. In between the Huffman decoder and LZ77 decoder is a First-In, First-Out (FIFO) memory that alleviates stalling between the two cores and allows them to be run at different clock frequencies. The LZ77 decoder is responsible for resolving all of the length-distance pairs and contains a circular buffer with enough space to hold the last 32,768 bytes. This circular buffer is assembled using dual-port BRAMs so that read and write operations can be performed simultaneously. The LZ77 decoder will record literals in the buffer as it receives them and passes them to the output. When it receives a length-distance pair, it reads 1 byte of the back-referenced string from the circular buffer every clock cycle while writing it back to the head of the buffer and the output. The Huffman decoder has a clock frequency of 160 MHz while the LZ77 decoder has a clock frequency of 212 MHz. Their design was synthesized for a Xilinx XC4VFX12 FPGA and both cores together occupied 128 FFs (2%), 387 LUTs (3%), and 18 RAMB16s (50%). They tested their design using static-Huffman-only compressed versions of the Calgary corpus and achieved a maximum output throughput of 205.71 MB/s, a minimum output throughput of 79.26 MB/s, and an average output throughput of 158.64 MB/s.

The authors of [39] implemented a single-core zlib decoder as part of an expandable zlib decoding system for FPGAs. The system was designed to incorporate multiple zlib decoders to allow for the decompression of multiple files in parallel. Much of their work describes how they directly translated the software code of the zlib library into VHDL hardware code. This included strategies like adapting function inputs and outputs into buffers for streaming as well as changing the dynamically allocated arrays into statically defined FIFOs and BRAMs. Their design is capable of processing both static and dynamic Huffman codes but the amount of time required to decode each



Figure 2.9: The area-efficient Huffman table memory design from [40].

was unfortunately not disclosed. Their design was synthesized for a Xilinx XC5VLX110T FPGA and has an area utilization of 20,596 LUTs (29%) and 11 BRAM tiles (7%). With a clock frequency of 120 MHz, their zlib decoder was able to achieve a maximum input throughput of 125 MB/s. The test files they decompressed and the average throughput speeds were not described.

In [40], the authors implement an FPGA-based decompressor core that uses an efficient Huffman table memory design. As mentioned above when describing reference [38], in order to decode the dynamic 15-bit Huffman codes directly using LUTs, 32,768 index tables are required. Since there are only 286 literal/length symbols and 30 distance symbols, the majority of the table entries would be duplicates for all of the codes that are less than 15 bits. The authors of [40] came up with a design that slightly complicates the decoding process but is able to fully utilize a 286-index table for literal/lengths and a 32-index table for distances. As mentioned in Section 2.1, the Huffman codes used by Deflate are canonical, meaning that all of the codes of each length have consecutive values. This means if the base address and base value for each code length are recorded, each code can be looked up relative to its base address. This process involves comparing the unknown-length code bits to the 15 different base code values to determine the actual bit-length of the currently held code. Then the address for the code is calculated using its base address and it can be decoded using the table, as shown in Fig. 2.9. This design was used by us in our Huffman decoder and is described in more detail in Section 4.2.1. Few other details regarding the design in [40] were given. It was designed as a decompressor core to be used as part of a multi-core system for an Intel/Altera Cyclone III 80 FPGA. The FPGA resource utilization is not described. The authors report a maximum decompression throughput of 300 MB/s but they do not list the test files decompressed or give average values. It is unknown whether this throughput was measured at the input or the output. They also do not specify whether this result is from using one core or multiple cores in parallel.

A proprietary decompression IP core created by Cast Inc. is available for purchase on Xilinx's website [41]. Though many details of the design are not disclosed, it can be used as a point of comparison. Their core is stated to output 3 bytes per clock cycle on average and operates with a clock frequency of 125 MHz, which equates to an average output throughput of 375 MB/s. When processing static-only compressed files, the core can run at a frequency of 165 MHz for an output throughput of 495 MB/s. One sample implementation is given for a Xilinx XCKU060 FPGA: when configured for dynamic mode the core uses 8,250 LUTs and 29 BRAM tiles (58 BRAM18Ks) and when configured for static-only mode the core uses 5,392 LUTs and 10.5 BRAM tiles (21 BRAM18Ks).

Table 2.7 shows a summary of all the decompression related works described in this section. The throughputs are specified as average or maximum and input or output values as disclosed in their respective works. As seen from the results, FPGA-based decompression accelerators are able to provide input throughputs on the order of hundreds of MB/s, much higher than most software decompressors are able to, which typically have values around 20 MB/s⁷. The results from [4] show that simple alterations to the standard Deflate format can allow for tremendous improvements in decompression throughput. While the strategy of speculative parallelization is a good idea for potentially

⁷The multi-core server workstation that was used to perform the design and synthesis work in this thesis, containing an i7-3930K CPU and 32 GB of RAM, was able to achieve an average input decompression throughput of 17.14 MB/s on the dynamically compressed Calgary corpus.

Reference	Platform	Throughput	Details
[33] (2013)	Software	1.24-1.80x speedup	Over sequential decompression
[34] (2017)	Software	18-24 MB/s (average, input)	Using 24 threads on ApacheSpark
[36] (2019)	Software	611 MB/s (average, input)	On FASTQ format files with 32 threads
[4] (2016)	GPU	13 GB/s (average, output)	On Gompresso format files
[38] (2007)	FPGA	158.64 MB/s (average, output)	On static-only Calgary corpus files
[39] (2009)	FPGA	125 MB/s (max, input)	Unknown test files
[40] (2010)	FPGA	300 MB/s (max)	Unknown test files
[41] (2016)	FPGA	375 MB/s (average, output)	On unknown dynamic test files
		495 MB/s (average, output)	On unknown static test files

 Table 2.7: Past Deflate Decompression Accelerators

speeding up decompression, other more reliable strategies for improvement still remain, like harnessing the inherent parallelism available in FPGAs. The work done in [39] made us aware of the challenges associated with performing dynamic Huffman decoding using LUTs while the design in [40] provided a useful solution to this problem. All of the designs showcase the importance of testing decompression using a standard benchmark of test files, as the types of files being decompressed play a critical role in the decompression throughputs that are achievable.

2.4 Summary

In this chapter, we described the background information on Deflate and explored works related to Deflate compression and decompression. In Section 2.1, we detailed the Deflate compression algorithm and format, and in Section 2.2 we briefly described the Calgary corpus benchmark, which we will use to test our designs. In Section 2.3.1, we described the design progression of related works on FPGA-based compression accelerators. Current state-of-theart compressor designs utilize a constant-throughput pipeline with a parallel sliding window in order to rapidly perform LZ77 matching, thereby sacrificing compression ratio in order to maximize compression throughput. In Section 2.3.2, we explained some of the fundamental limitations of the Deflate format that prevent the parallelization of decompression and examined a variety of works that attempt to work around these limitations. Though the number of published FPGA-based decompressor designs is relatively small, we were able to find a few that provided useful ideas upon which to base our design.

Chapter 3 Compressor Design

Our plan for an FPGA-based compressor design was to follow the current state-of-the-art architecture as used by most other related works (described in Section 2.3.1) and to improve the resulting compression throughput and compression ratio further while implementing our design using Vivado HLS. This architecture utilizes a parallel sliding window (of PWS bytes) to perform LZ77 matching on multiple substrings at a time. The compressor design is pipelined to compress data at a fixed rate using static Huffman encoding only. Performing the Huffman encoding operation is relatively simple as it involves encoding characters using tables stored in FPGA LUTs and then shifting and OR-ing together the various bit-width codes in the output window. Most of the focus of previous designs appears to be on the LZ77 encoder and on maximizing the compression throughput. As pointed out in [7], in order to increase the compression throughput of a compressor system, it is more sustainable to utilize multiple compressor cores than it is to increase the PWS of a single compressor. Match lengths (which are limited by the PWS value) greater than 16 bytes are also rare, and so the consensus seems to be that increasing the PWS for the purposes of achieving higher compression ratios is not worth it. Utilizing multiple parallel compressors results in less-efficient matching being performed (due to each compressor relying only on its own data history) and causes the compression ratio to decrease slightly. Most previous designs have focused on maximizing the compression throughput even at the cost of a lower compression ratio. Currently, however, the maximum achievable throughputs obtained by multi-compressor architectures are being bottle-necked by the CPU-FPGA interface as reported by [7]. For the above reasons, we chose to focus on implementing a single compressor core design with the goal of achieving high compression ratios while still maintaining competitive throughput values. The proposed compressor has PWS value of 16 bytes and will utilize a constant-throughput pipeline by performing static Huffman encoding only. Both the LZ77 encoder and Huffman encoder will be pipelined with an Initiation Interval (II) of 1, meaning that they can read in new input data (i.e., 16 bytes) every clock cycle. Our desired clock frequency is 250 MHz (4 ns period), which, when compressing 16 bytes per clock cycle, would provide a compression throughput of 4.0 GB/s. Unlike most other earlier works on compressor cores, our designs were implemented using Vivado HLS in order to evaluate the capabilities and limitations of high-level synthesis.

3.1 Initial Design

Since our focus lay more on increasing the compression ratio than increasing the throughput, our initial design adopted the dictionary architecture from [27], which had the highest geometric mean compression ratio of all the previous works when compressing the Calgary corpus. This design differs from the others in how it uses a fully connected dictionary design instead of a hash banking design. Enough dictionaries and dictionary copies are used so that each of the 16 substrings in the window (with a PWS of 16) is able to look up 16 potential matches for a total of 256 total match comparisons being performed in every clock cycle. Because of the fully connected design, no hash collisions can occur and, as a result, no matches are ever dropped, which leads to higher compression ratios than in other designs, where potential matches are dropped as a result of hash collisions. This type of fully connected dictionary architecture comes at a cost, however. Each stored string requires 16 bytes while their positions will require another 4 bytes (if we assume 32-bit positions are being used). With a 10-bit hash value, each dictionary will have 1024 indexes (as in [27]) and will be replicated 16 times to allow uncontested access. In total: 20 bytes \times 1024 indexes \times 16 dictionaries \times 16 copies = 5,242,880 bytes of storage required. On a Xilinx FPGA, this requires 2048 BRAMs (BRAM18Ks specifically) for the strings and 512 BRAMs for the positions totalling 2560 BRAMs altogether, which is more BRAMs than most contemporary FPGAs provide. Assuming that the number of available BRAMs is not an issue, the other problem that we encountered with this design was with meeting clock timing due to all of the extra routing delays incurred by the relatively large layout area. Vivado HLS was easily capable of synthesizing a design that could logically meet timing; however, following implementation in Vivado, the design ended up requiring a clock period around 7 ns due to all of the routing delays, which is almost double that of our target clock period of 4 ns. Because of this massive difference, we decided to change our design to one that would require fewer BRAMs and, consequently, would be easier to meet post-route timing.

3.2 Final Design

A block diagram of our final compressor design is shown in Fig. 3.1. It is composed of only two cores, an LZ77 encoder and a Huffman encoder, both of which were specified in C++ and synthesized using Vivado HLS. Both of the cores have AXI-Stream interfaces [42], a standard interface used by Xilinx FPGA systems to facilitate high-speed unidirectional data transfers in streaming architectures. The AXI-Stream interface functions using handshake



Figure 3.1: Final compressor block diagram with AXI-Stream interfaces described.

signals (not shown in the block diagram), which consist of a forward travelling TVALID signal and a backwards travelling TREADY signal. TDATA is the name of the main AXI-Stream data-carrying channel, while the remaining signals, TKEEP, TUSER, and TLAST, are optional sideband signals. The TKEEP signal is used by multi-byte data streams to indicate which bytes in the current transfer are valid, the TLAST signal is used to indicate the last transfer in a data stream, and the TUSER signal can be employed by the AXI-Stream user for passing any other desired data alongside TDATA. In our case, we use the TUSER signal in between the two encoders in order to indicate which bytes are matched literals, unmatched literals, or length-distance pairs. This is explained in further detail below.

3.2.1 LZ77 Encoder

As mentioned before, we followed the same structure as other previous works and used the parallel pipelined LZ77 encoder design with a PWS of 16 bytes. A block diagram describing the stages of the LZ77 encoder pipeline is shown in Fig. 3.2. At every clock cycle, 16 bytes of data are read from the input stream and shifted into a 32-byte window. Across this 32-byte window are 16 staggered substrings, each 16 bytes long (see Fig. 2.5). It is these 16 substrings that will attempt to be matched with previous strings in order to replace them with length-distance pairs. To do this, the first 5 bytes from each substring



Figure 3.2: LZ77 encoder pipeline diagram.

are taken and hashed to generate 16 hash signatures. The hashing process is explained in more detail later in Section 3.2.2. We used the hash bank architecture from [7], which utilizes 32 hash banks with each bank having 3 depth levels. Each of our hash banks has 512 indexes in order to fully utilize the BRAM storage space, as shown in Fig. 3.3a. These hash banks are accessed by the 16 substrings based on their hash signatures with priority given to the last substring first, since last-fit match selection is performed later. If a substring is granted access (i.e., another substring has not already accessed its desired bank), that substring will be written to the bank and location that its hash signature addresses. Otherwise, the substring is dropped and is not recorded or compared with previous strings. As the substrings are recorded in the dictionary banks, new strings are recorded in the top depth bank while each previously stored string is written from one depth to the next, effectively shifting each of the strings down a level with the oldest string being discarded. At the same time, the previous strings from each depth level are read and compared to the input substrings to find potential matching strings. With a depth of 3 levels, 3 potential matches are read and compared to each input substring that was granted access, as shown in Fig. 3.3b. We used the MUX optimization from [7], in which the match comparisons are performed at the output of the banks so that only the resulting best match length needs to be MUXed back to the substring window. Since the match length can only be



Figure 3.3: a) The hash bank architecture that was used in the final design. b) The match comparisons are performed at the outputs of the banks before being MUXed back to the substring window.

from 0 to 16, 5-bit wide MUXes can be used instead of 16-byte wide MUXes.

As was done in [27], we perform the match comparisons by comparing each byte simultaneously and storing the Boolean result of each byte compared as a bit in a bit-string. This is done instead of comparing each byte sequentially and incrementing the length for each matching byte, as this approach would result in an inefficient and relatively long select-adder chain. In order to convert the resulting bit-string back into an integer value, we invert it and use the built-in Count Trailing Zeroes (CTZ) operator¹. The longest match length out of all of the potential matches is kept and MUXed back to the substring window. Following this, each substring in the window will have a match length. Substrings that were not granted bank access are given match lengths of 0. Since the matches found for each substring will conflict, the matches need to be filtered in some manner. We followed the last-fit match selection heuristic used in [27], in which the last match in the window is always kept as it is more likely that later matches will be longer than earlier ones. One consequence of allowing matches to span from the front half of the sliding window to the second half is that matches found in the current iteration may conflict with matches in the following iteration. The last match selected is used to calculate the First Valid Position (FVP) in the window for the next iteration, where the window bytes have not already been replaced with a length-distance pair. As explained in [27], there is a feedback path from the computation of the FVP, which is used in the next iteration. In order to prevent pipeline bubbles from occurring and the II from being greater than 1, the FVP needs to be calculated as soon as possible. As a result, once the FVP for the next iteration is calculated, it cannot be changed by any of the match filters that follow.

To perform match selection, we again utilize a bit-string of 16 bits, with each bit indicating the validity of a match within the window. As matches are filtered, these bits are set to 0. As can be seen from Fig. 3.2, 26 of the 43 pipeline stages are used for match-filtering. The filtering process is split across four main filters, which we have called Filters A to D. In Filter A, which

 $^{^1\}mathrm{See}$ the "C Builtin Functions" section of the Vivado HLS User Guide [43] for more information.

directly follows the best match selection stage, matches that have lengths less than 3 or distances greater than 32,768 are filtered out (as defined by the Deflate specifications). Next, in Filter B, the matches are compared to the FVP in the window and any matches with characters that have been covered by the previous iteration are filtered. Following this, the FVP for the next iteration is calculated and the filters that follow can no longer alter this value. Here we have also used the match "reach" heuristic from [27]. The reach of each match is defined as its position in the window plus the length of its match, representing how far a match length reaches within the window. Using this, in Filter C, the reach of each match is compared to the others in order to find matches that have the same reach as each other. In these cases, the match with the longer length can be kept instead, even though it may not necessarily be the last match, as this will not alter the FVP. In the final filter, Filter D, the last-fit match selection is performed in which earlier matches that conflict with later matches in the window are filtered. As an improvement over previous



Figure 3.4: LZ77 encoder match filtering example. In this example, the PWS is 8 bytes. After filtering, only matches 3 and 6 are kept.

works, we have also implemented match trimming functionality to Filter D. When an earlier match is about to be filtered for conflicting with a later one, the filter will attempt to trim the earlier match (down to a maximum of 3 bytes) so that both matches can be kept. An example showing all four of the match filters being used is shown in Fig. 3.4.

We will refer to the outputs from the 16 substring locations in the sliding window as "boxes". Following filtering, each box will be classified as containing a matched literal, an unmatched literal, or a match (i.e., where the beginning of a match occurs) and will be prepared for the output to the Huffman encoder. The AXI-Stream TUSER signals are used to classify each box using a 2-bit flag: 0b00 for matched literals, 0b01 for unmatched literals, and 0b11 for matches. All of the boxes following a match, up to the match length, are the matched literals and are cleared and flagged so that they can be removed from the compressed data stream. The boxes containing matches are filled with the length and distance of the match while unmatched literal boxes are filled with the literal bytes from the sliding window, as shown in Fig. 3.5. In a lengthdistance pair, the length requires at least 4 bits (for values 3 to 16) and the distance requires at least 15 bits (for values 1 to 32,768), together occupying 19 bits. This means that each output box needs to be 3 bytes (24 bits) wide in order to fit a length-distance pair, requiring a total of 48 bytes (384 bits) for all 16 boxes. We do this so that each output box can be classified and filled simultaneously. The alternative is to fill these boxes one at a time and spread the length-distance pairs across multiple boxes (requiring fewer output bytes), but this requires sequentially filling each box. Packing the length-distance pairs into a single box as opposed to multiple boxes also allows the Huffman encoder to encode each box separately and concurrently instead of having to

Box								
TUSER	00	01	01	10	00	00	10	00
TDATA	0	Lit	Lit	LD	0	0	LD	0

Figure 3.5: LZ77 encoder output window example that follows the previous example from Fig. 3.4 (with a PWS of 8).

obtain the length and distance bits from multiple boxes. Consequently, the interface between the LZ77 encoder and Huffman encoder (as shown in Fig. 3.1) is as follows: TDATA is composed of 16 3-byte boxes for a total width of 384 bits, TUSER is composed of 16 2-bit flags classifying each box, and TLAST signals the last transfer of the stream.

The most difficult challenge encountered when designing the LZ77 encoder was meeting clock timing after implementation and routing in Vivado. Even after deviating from our original design, as described in Section 3.1, this still proved to be a major problem. Vivado HLS is only aware of the logic synthesis stage of design and has no control over implementation and routing, which is performed by Vivado as a separate and subsequent step. As a result, Vivado HLS would synthesize designs that would easily meet timing from a logic delay standpoint, but would be impossible to meet timing after routing. The implemented designs would be prone to high routing congestion and large setup time violations. Even when performing high-effort implementation runs in Vivado that would attempt to reduce congestion and over-estimate net delays, timing still could not be met. The two main areas that seemed to be the largest contributors to the problem were the bank-access allocation stages and the best-match-length selection stages.

We ended up solving this timing problem using two main solutions. The first was the manual addition of extra pipeline stages to the design in Vivado HLS in order to reduce the routing delay between pipeline stages. As Vivado HLS is not aware of routing, it will only automatically add more pipeline stages when necessary to meet logic timing, not routing timing. The second solution was increasing the "clock uncertainty" parameter setting in Vivado HLS. This setting forces Vivado HLS to restrict the logic delay to a maximum portion of the clock period, allowing more room for routing delay later on. We ended up using a clock uncertainty of 0.8 ns, which restricted all synthesized logic delays to 3.2 ns. Using these two solutions, we were able to get the LZ77 encoder design to meet the target 4 ns (250 MHz) timing.

3.2.2 Hash Function

Since the LZ77 encoder design that we use performs match finding at a constant rate (and therefore more time cannot be spent searching for better matches), the only other design parameter that is left affecting the output compression ratio besides the dictionary architecture (i.e., the size and number of banks), the PWS value, and the type of Huffman encoding used is the hash function. Since we had to switch away from a hash dictionary design that was immune to hash conflicts, as explained in Section 3.1, we also have to be aware of how susceptible our chosen hash function is to hash conflicts as dropped matches seem to impact the compression ratio significantly. No hash function is able to prevent the occurrence of hash conflicts completely; however, we can aim to make the probability of conflicts as low as possible. The hash function should be provided enough information from the bytes in the sliding window to be able to find potential matching strings but not so much information that match finding becomes too strict and potential matches become too difficult to find. Out of all of the previous works examined in Section 2.3.1, only one, [27], describes the hash function that was used. This hash function is the following:

Algorithm 1: Hash Function from [27]
Input: $curr_window[2 \times PWS]$, array of 8-bit ints
Output: $hash[PWS]$, array of 10-bit ints
1 for $i \leftarrow 0$ to <i>PWS-1</i> do
$2 hash[i] = (curr_window[i] \ll 2) \oplus (curr_window[i+1] \ll 1) \oplus 2$
$(curr_window[i+2]) \oplus (curr_window[i+3]);$

An example of how this hash function is used to generate hash signatures using the substrings within the sliding window is shown in Fig. 3.6. We used this function as the starting point for our hash function experimentation. Since our design uses 32 banks with 512 indexes each (for a total of 16,384 indexes), we used a 14-bit hash value. The top 5 bits of the hash value determine the bank while the bottom 9 bits determine the bank index. In order to reduce the number of bank conflicts, we want the top 5 bits to be as random as possible



Figure 3.6: An example showing how the bytes from the substrings in the sliding window are used to calculate 10-bit hash signatures using the hash function from [27]. In this example, only the first two calculations are shown. With a PWS of 16, there would be 16 of these calculations.

so that hash values are distributed evenly across all of the banks.

Our first attempts at improving the hash function involved varying the amount of shifting done on each byte before XORing them together. Since we wanted the upper 5 bits to receive the most amount of randomness, we shifted the 4 input bytes left far enough so that each one affected the upper 5 bits in some way. We then tried adding more input bytes to the hash function. We found that hashing 5 input bytes instead of 4 showed an improvement but hashing 6 bytes was worse. We believe this is because 6 bytes provides too much information resulting in the match finding becoming too strict. The reason for this is because when 6 bytes of a string are used to generate the hash value, match lengths of 3, 4, or 5 become harder to find, as each additional byte of information scrambles the hash value further. We also experimented with using two separate hash functions: a 5-bit function for the bank and a 9-bit hash function for the index, both utilizing the input bytes in different ways. We found, however, that these generally gave worse results than one 14-bit hash function. We believe this may be because of how bits were dropped from the 8-bit inputs when they were incorporated into the 5-bit hash value, resulting in poorer bank distribution.

Following this, we experimented with multiplication instead of shifting. In Vivado HLS, certain bit-wise operations are optimized automatically if more efficient operations can be performed instead. For example, multiplying a number by 31 is automatically optimized into "left-shift by 5 bits" and "subtract 1" operations. Taking the modulo of a "power of two" number simply selects the lower order bits of a number while division by powers of two performs right-shifts. This is generally an advantage of HLS but it can lead to confusion when attempting to understand the synthesized output, which is necessary when identifying areas where your design can be improved. We found that replacing the left-shift operations with multiplication operations that shifted by the same amount but also subtracted gave better results.

The next major change that we tried was combining the input bytes sequentially instead of concurrently. Up until now, the hash function involved manipulating the input bytes in various ways before XORing all of them together to get the final result. Instead, we tried performing something similar to a rolling hash function, where each input byte is incorporated into the hash one-at-a-time. From here, we experimented with shifting and multiplying by various values as well as XORing or adding the results to the hash. We then began performing various rotations on the hash function in-between incorporating the input bytes. We found that some hash functions worked better to improve the compression results of the non-ASCII data files, like geo and pic, while others work better on ASCII text data files. As a result, it was difficult to find a hash function that worked well across all of the different files in the Calgary corpus. In total, we tried about 100 different variations of hash functions. The compression ratio results from all of the different hash functions that we tried are shown in Fig. 3.7. As can be seen from this figure, most of the functions tested provided compression ratios within the range of 1.80 to 2.00, with a few outliers falling below this range. The best hash function tested provided arithmetic and geometric mean compression ratios of 2.00 and 1.92, respectively, on the Calgary corpus. This hash function is the following:

Algorithm 2: Our Chosen Hash Function **Input:** $curr_window[2 \times PWS]$, array of 8-bit ints **Output:** *hash*[*PWS*], array of 14-bit ints 1 for $i \leftarrow 0$ to *PWS-1* do $hash[i] = (curr_window[i] \times 31) \oplus (curr_window[i+1]);$ $\mathbf{2}$ hash[i].rrotate(4);3 $hash[i] = (hash[i] \times 3) \oplus curr_window[i+2];$ $\mathbf{4}$ hash[i].rrotate(4); $\mathbf{5}$ $hash[i] = (hash[i] \times 3) \oplus curr_window[i+3];$ 6 hash[i].rrotate(4); $\mathbf{7}$ $hash[i] = (hash[i] \times 3) \oplus curr_window[i+4];$ 8



(b) Histogram

Figure 3.7: Compression ratio results from experimenting with various hash functions.

3.2.3 Huffman Encoder

Fig. 3.8 shows a diagram of the final pipelined Huffman encoder. Compared to the LZ77 encoder portion of the compressor design, the Huffman encoder is much simpler. Since only static Huffman codes are to be used in the design, the literals and length-distance pairs received from the LZ77 encoder can be quickly encoded using static codebook ROMs. Following this, the variable length codes just need to be packed together using a series of shift and OR operations. As mentioned above in Section 3.2.1, we designed the interface between the two encoders so that each box passed between the two can be encoded independently of the others. Each box from the LZ77 encoder is passed through a symbol encoder, which checks the type of symbol in the box (either a matched literal, unmatched literal, or length-distance pair) and encodes it accordingly. Unmatched literals and length-distance pairs are encoded using ROMs and their codes and accompanying extra bits are assembled and output. If a matched literal is received, it is removed from the stream by replacing it with a code and code length of 0. Once encoded, the codes as well as their bit-lengths are given to a window packer, which is responsible for shifting the codes and packing them into an encoded window of bits. The encoded window contains enough space for codes from each of the 16 boxes. The longest possible encoded size of a 16-box input window is 15 9-bit literal codes followed by a 26-bit length-distance code (7-bit length, 1 extra length



Figure 3.8: Huffman encoder pipeline diagram.

bit, 5-bit distance, 13 extra distance bits) for a total of 161 bits. While it is impossible for there to be two consecutive 161-bit encoded windows (as the following window would have 15 matched literal boxes), it is possible for there to be two consecutive windows with more than 128 bits each. Therefore, the size of our output stream needed to be at least 256 bits wide to allow data to be written out in every clock cycle. At the end of the pipeline is an output window packer which contains a double buffer that is 512 bits wide. When the buffer contains more than half that amount, it writes the lower 256 bits to the output stream.

Our plan for the Huffman encoder design was to create a 16-stage pipeline in which each stage would take one box from the input window, encode it, and pack it into the encoded window. In every clock cycle, the input window and encoded window would be passed from one stage to the next. At the end of the pipeline is the output window packer which receives a fully encoded window in every cycle and writes it to the double buffer. With function inlining disabled in Vivado HLS, this is what ends up being synthesized. With function inlining enabled, however, Vivado HLS is able to optimize the operations performed and combine the pipeline stages together. What ends up being synthesized is a 6-stage pipeline where each input box is encoded and packed together simultaneously, as shown in Fig. 3.8. The ability for Vivado HLS to automatically optimize designs into more efficient forms is a powerful ability that gives it an advantage over traditional Register-Transfer Level (RTL) design. As with the LZ77 encoder, the Huffman encoder is pipelined with an II of 1.

3.3 Testing and Results

The two compressor cores were synthesized using Vivado HLS for a clock frequency of 250 MHz. Table 3.1 shows the FPGA resource utilization of the two cores when synthesized for a Xilinx Virtex UltraScale+ XCVU3P-FFVC1517 FPGA. The desired clock frequency and FPGA used were chosen by our industrial collaborator, Eideticom. We tested the compressor using the Calgary corpus benchmark files. A test bench was created in Vivado in which

	LUTs	FFs	BRAM Tiles
LZ77 Encoder	62,227~(15.79%)	46,225~(5.86%)	240 (33.33%)
Huffman Encoder	6,887~(1.75%)	3,554~(0.45%)	20.5~(2.85%)
Total	69,114 (17.54%)	49,779 (6.31%)	260.5 (36.18%)

Table 3.1: Compressor FPGA Resource Utilization

an AXI Direct Memory Access (DMA) core was used to stream the input data from memory to the compressor core, receive the compressed output data stream, and write it back to memory for verification. The compressed output files were decompressed and compared to their original forms in order to verify that the compressor was operating correctly. The resulting compression ratios were obtained by dividing the uncompressed size by the compressed size for each file and are shown in Table 3.2. Across the entire corpus, our compressor achieved an arithmetic mean (average) compression ratio of 2.00 and a geometric mean compression ratio of 1.92. Both compressor cores were synthesized with a pipeline II of 1, which, with an LZ77 encoder PWS of 16 bytes and a clock frequency of 250 MHz, provide an input compression throughput of 4.0 GB/s.

The results of our FPGA-based compressor design are compared to those from other previous works in Table 3.3. As mentioned in Section 2.3.1, the results from [5] are for a compressor with a PWS of 16 bytes and the results from [7] are for a single-core compressor only. By achieving a working clock frequency of 250 MHz, 50 MHz higher than the 200 MHz clock from [7], an extra 0.8 GB/s of throughput is obtained. This makes our design the fastest single core compressor out of those compared here. In terms of area, it is slightly difficult to make a direct comparison between our Xilinx-based FPGA design, with area utilization described in LUTs and FFs, and those designs using Intel/Altera-based FPGAs, which describe their area usage in ALMs. Compared to the designs that reported their memory usage, [28] and [27], our design uses about half as many BRAMs². Compared to the other compressor design that was synthesized using Vivado HLS, [6], our design uses 20% fewer

 $^{^{2}}$ BRAM18Ks can store 18k bits while M20Ks can store 20k bits. Note that the actual number of bits stored in each will depend on the word width and depth used.

File	Uncompressed	Compressed	Compression	
	Size (bytes)	Size (bytes)	Ratio	
bib	111,261	56,450	1.97	
book1	768,771	482,048	1.59	
book2	$610,\!856$	$325,\!400$	1.88	
geo	$102,\!400$	96,448	1.06	
news	$377,\!109$	$218,\!688$	1.72	
obj1	21,504	14,093	1.53	
obj2	246,814	$129,\!327$	1.91	
paper1	$53,\!161$	$28,\!636$	1.86	
paper2	82,199	45,891	1.79	
pic	513,216	$137,\!428$	3.73	
proge	39,611	$20,\!556$	1.93	
progl	71,646	30,510	2.35	
progp	49,379	$21,\!534$	2.29	
trans	93,695	39,795	2.35	
	2.00			
	1.92			

Table 3.2: Calgary Corpus Compression Results

LUTs and FFs. Our compressor design has a total of 49 pipeline stages (43 for the LZ77 encoder and 6 for the Huffman encoder), which is fewer than the 58-stage compressor from [5] and the 87-stage compressor from [27] but more than the reported 17-stage compressor from [28]. In terms of compression ratio, our mean compression ratios (both arithmetic and geometric) are lower than all other designs besides [6].

Table 3.3: FPGA-based Compressor Design Comparison

Reference	Clock	Pipeline	Input	Area Utilization	Compression
	Frequency	Depth	Throughput		Ratio
[28] (2013)	200 MHz	17	3.00 GB/s	105,624 ALMs, $1,152$ M20Ks	?
[27] (2014)	193 MHz	87	$2.84~\mathrm{GB/s}$	110,318 ALMs, $1,792$ M20Ks	(Geo.) 2.17
[5] (2015)	$175 \mathrm{~MHz}$	58	$2.80 \mathrm{~GB/s}$	39,078 ALMs, ? M20Ks	2.05
[6] (2018)	200 MHz	?	$2.80 \mathrm{~GB/s}$	83,583 LUTs, 65,009 FFs,	(Geo.) 1.73
				? BRAM18Ks	
[7] (2018)	200 MHz	?	3.20 GB/s	38,297 ALMs, ? M20Ks	2.10
This work	250 MHz	49	4.00 GB/s	69,114 LUTs, 49,779 FFs,	(Geo.) 1.92
				521 BRAM18Ks	

3.4 Discussion

Despite the considerable effort that was made to improve the compression ratio of our design, we still weren't able to achieve higher ratios than previous works. Even with the addition of match-trimming to the match-selection stages of the LZ77 encoder, which to our knowledge is not done in other designs, our compression ratios were still lower. We found that the match-trimming improved the compression ratios by about 6% while adding 3 pipeline stages and increasing LUT usage by 3% and FF usage by 1%. Considering that we used the same 32-bank, 3-depth hash bank architecture as the design from [7], which achieved an average compression ratio of 2.10, we believe that our hash function may be one contributor, despite our extensive exploration into potential hash functions, and that there may still be room for improvement. The other thing that may account for the difference in the compression ratio is the number of hash indexes used. As mentioned above, our design used 512-index banks (see Fig. (3.3a) while the size of the banks in [7] is not disclosed. For comparison, the design from [5] used 65,536 hash indexes across 32 banks (2,048 indexes per bank), requiring a 16-bit hash function.

In order to verify the effect that the hash bank architecture has on the compression ratio and memory cost, we performed a series of design explorations, shown in Fig. 3.9. Throughout these tests, we kept the PWS value constant at 16 bytes and used the same hash function as was described in Section 3.2.2 (Algorithm 2). In Fig. 3.9a, the hash bank depth is increased while the number of banks and the total number of hash indexes are held constant, showing that the bank depth can be scaled up with linearly increasing memory costs. In Fig. 3.9b, the total number of hash indexes is increased while the number of banks and bank depth is held constant. Below 16,384 indexes, the number of BRAMs used does not decrease. This is due to how the BRAM18K configuration works: in order to accommodate a word width of 128-bits (16-byte strings), 4 BRAMs at minimum are required, no matter the number of memory indexes used. The 4 BRAMs have enough space to store 512 128-bit words, above which the number of required BRAMs doubles. Each hash bank also stores 512 32-bit positions, which completely fills another BRAM for a total of 5 BRAMs minimum per hash bank. Above 16,384 total hash indexes, the compression ratio barely increases while the memory costs increase exponentially. In Fig. 3.9c, the number of hash banks is increased while the number of total hash indexes is held constant. In this figure, the BRAMs are fully utilized up to 32 banks, after which the number of indexes per bank drops below 512. In Fig. 3.9d, the number of hash banks is increased while the number of indexes per bank is held constant at 512 (therefore the total number of indexes increases as well). This figure essentially shows the combined effects of Figs. 3.9b and 3.9c, with the number of memories required increasing exponentially. Despite the minimal increase in compression ratio that is obtained by increasing the total number of hash indexes, it makes more sense to do so while increasing the number of banks in order to fully utilize the BRAM storage space. If the increased memory cost can be accommodated, increasing the number of hash banks makes the most improvement on the compression ratio. Increasing the bank depth also provides some improvement to the compression ratio at a lower cost, but the returns are diminishing for depths greater than 3, as was also reported in [7].

The hash bank architecture of our compressor could be scaled up in order to increase the compression ratios achieved, but this would be difficult to get working as our design already struggles with meeting timing due to the large routing delay. The clock frequency (and therefore throughput) could be sacrificed though in order to allow more room for a larger scale design. As discussed in Section 2.3.1, increasing the PWS value is another way to increase both the compression ratio and the throughput, but the area requirements for PWS values greater than 16 bytes quickly become unsustainable and not worth the improvement as explored in [5] and shown in Fig. 2.7. Another idea for improving the compression ratio would be to implement multiple hash functions in the compressor. Two different hash functions could be used in a pipeline in order to give each substring two chances at accessing a bank instead of just one. Different hash functions that are tailored to different data types could be used as well. If the type of data being compressed could be communicated to





a) Varying hash bank depth with 32 hash banks and 16,384 total indexes.

b) Varying total hash indexes with 32 hash banks and 3 depth levels.

c) Varying number of hash banks with 16,384 total indexes and 3 depth levels.

d) Varying number of hash banks with 512 indexes per bank and 3 depth levels.

the compressor, then it could choose to use a hash function that is likely to be better suited for matching that type of data, which would on average increase the likelihood of better compression results. Another option for improving the compression ratios would be to utilize dynamic Huffman encoding as well as static. As mentioned in Section 2.3.1, however, this complicates the pipeline design and removes the fixed throughput rate, as an intermediate storage space would be required to hold the LZ77 encoded data before the Huffman tables could be constructed and used. This type of work was investigated in [29]. The other option to improve the compression ratios is to return to a traditional compressor design, like the ones used in software, which take more time to perform match finding, as these designs still are able to provide the highest compression ratios.

To increase the compression throughput further (besides increasing the PWS value), higher clock frequencies may be used or, as recommended by [7], multiple independent compressors could be utilized in parallel. Since we were able to achieve a clock frequency of 250 MHz while being restricted to high-level synthesis, it may be possible for hand-optimized VHDL or Verilog designs to meet even higher frequencies. As we discussed earlier, this may require sacrificing some compression ratio in order to scale the hash bank architecture down enough so that routing delays are more manageable. In terms of logic delay, the bank-access allocation stages and the best-match-length selection stage were the two largest critical path areas of the LZ77 encoder design. For our current FPGA-based compressor design, with a total BRAM usage of about 36%, it may be possible to fit two independent compressor cores on a single FPGA to operate in parallel. Together they would be able to provide a collective compression throughput of 8.0 GB/s, assuming they aren't bottlenecked by the FPGA interface.

3.5 Summary

In this chapter, we described our FPGA-based Deflate compressor design. This design followed the current state-of-the-art architecture, which utilizes a fixed-

throughput pipeline and static Huffman encoding in order to rapidly perform Deflate compression. The use of Vivado HLS provided some challenges in creating a working design that was able to meet timing, but was also able to help improve the efficiency of our design through certain automatic optimizations. Despite the addition of match trimming functionality to the LZ77 encoder as well as extensive exploration on the hash function and hash bank architecture used, we weren't able to achieve higher compression ratios than previous works. Our compressor was able to achieve arithmetic and geometric mean compression ratios of 2.00 and 1.92, respectively, across the Calgary corpus benchmark. We were, however, able to meet clock timing with a clock frequency of 250 MHz, giving our compressor a throughput of 4.0 GB/s, which is higher than all other currently published single-compressor throughputs. We were also able to achieve this while being limited to using high-level synthesis.

As discussed in Section 3.4, we believe that we have still not hit the maximum limits of compression ratios achievable for these type of designs. Further exploration of possible hash functions may yield functions that are better able to prevent hash bank access conflicts from occurring. In terms of hash bank architecture, there are still many ways that compression ratios can be improved at the cost of additional area, though they may potentially require a shorter clock frequency (and therefore lower throughput) in order to meet post-route timing. Currently, instantiating multiple compressor cores in parallel is still the most efficient way to scale up compressor designs should also be achievable.

Chapter 4 Decompressor Design

Our goal in this chapter is to design a competitive FPGA-based decompressor core using Vivado HLS. The decompressor is to be fully compliant with the Deflate standard, to have the ability to process both static and dynamic Huffman-encoded blocks, and to not exploit any changes to the compressed format or make any limiting assumptions about the compressed data. In our design we focused on maximizing the decompression throughput by exploiting the parallel resources available in FPGAs. As we describe our initial and final decompressor designs, we will also mention the main limitations of Vivado HLS that we encountered and also explain how we were able to work around them in order to succeed in achieving our design goals.

4.1 Initial Design

Our initial decompressor architecture, shown in Fig. 4.1, utilizes speculative parallelization to perform the Huffman decoding operation in parallel in order to benefit from some potential speed-up. The architecture includes multiple Huffman decoder cores capable of processing static Huffman blocks only. In our design we chose to use four Huffman decoders, though any number of parallel decoders could be utilized. A "boundary detector" core at the beginning of the system pipeline scans the incoming data for the static EOB code in order to find potential block boundaries. The "data mover" core receives the data from the boundary detector (following temporary storage in a FIFO) and writes it to one of four local BRAM memories, one for each Huffman decoder. The data



Figure 4.1: Initial speculative decompressor architecture.

mover has the ability to copy data from each of the BRAMs and stream it to one of the decoders simultaneously, in order to keep each decoder busy. The purpose of the BRAMs is to store the potentially parallelizeable data and, in the result of a false boundary being discovered (and data being decoded incorrectly), allows the data to be resent to another decoder in order to be processed correctly.

The first Huffman decoder to be given data will be referred to as the "leading decoder" and is guaranteed to correctly decode the first block. Whenever a potential block boundary in the incoming data is found, a copy of the data stream from that point is also sent to another Huffman decoder to run in parallel with the leading one. The outputs of each Huffman decoder feed into FIFOs for elastic storage so that the validity of the data can be verified later on (depending on if the prospective block boundary turns out to be valid or not). If the block boundary is valid, the Huffman decoded data is sent to the "data merger" core. The data merger merges the multiple parallel data streams and continuously streams the next set of valid data from one of the FIFOs to the LZ77 decoder core. If the prospective block boundary that a Huffman decoder was starting from is found to be invalid, the corresponding FIFO is cleared and its data is discarded.

The decoded data from the leading Huffman decoder is always valid as this is the decoder that is known to be performing correct sequential decoding from the start of the file or from a confirmed block boundary. When a prospective block boundary is found and confirmed to be valid, the following block is processed in parallel correctly and the Huffman decoder that processed it becomes the new leading decoder as it now knows the correct bit position from which to continue decoding the data stream. The output block from the previous leading decoder is kept and it will now be given potentially parallel data at the next opportunity. No matter how many false or positive potential block boundaries are found, one decoder is always kept running and the file will be decompressed sequentially in the worst case. More Huffman decoders could be employed in parallel if desired. The amount of parallel Huffman decoders that will be useful, though, will depend on the speed at which they can decode and the size of the Deflate blocks in the compressed data. If the blocks in the data are small and/or the decoders are fast enough, employing more parallel decoders will be pointless as they will likely never be used. Determining the optimal number of Huffman decoders to use will require design exploration and testing on various data types.

The two data passing cores, the data mover and data merger, were originally to be created using Vivado HLS. We found, however, that the parallel nature of their operation, made implementation in Vivado HLS difficult if not impossible. This is because of one crucial limitation of Vivado HLS which we have called "coarse function scheduling". Different functions within an HLS core can be run in parallel, but they need to be scheduled to start at the same time, as illustrated in Fig. 4.2. This prevents the data mover and data merger cores from performing multiple asynchronous tasks in parallel as required. There is one way to overcome this limitation: the Vivado HLS "dataflow" pragma (a compiler directive) allows data to flow freely between function blocks; however, the use of this pragma imposes many strict constraints on the code to be synthesized. We were unable to meet these restrictions, which forbid the use of conditionally performed tasks as well as feedback between blocks. It may also be possible to split up the data passing cores into multiple HLS cores such that each operation can be carried out in parallel, but each of the sub-cores would need to be interfaced properly and be able to respond to interrupt signals. We chose to avoid designs that required complex



(b) Function execution timing

Figure 4.2: Diagram showing the coarse function scheduling limitation of Vivado HLS. a) Function chains A and B1/B2 have separate inputs and separate outputs and are completely independent from each other. b) Without the dataflow pragma, function B2 will not be scheduled to start until function A finishes. With the dataflow pragma, B2 executes as soon as B1 is finished.

interrupt handling. For these reasons, the data mover and data merger cores were written in structural level Verilog instead of using Vivado HLS, to allow us to have direct control over the structure of this part of the design.

As mentioned above, when operating on random data, the amount of Huffman decoders that would be utilized simultaneously would be dependent on the size of the Deflate blocks in the data. To compensate for this, our next plan was to modify the accompanying compressor to compress data into blocks of constantly known size which we could then take advantage of using the decompressor. This way, the data could be safely and consistently split into multiple blocks and all four (or possibly more) Huffman decoders could be fully utilized. Once the initial design was made to work, however, it was found that the downstream LZ77 decoder was unable to keep up even with only one Huffman decoder working. At this point, the decision was made to scrap the speculative parallelization architecture for the Huffman decoders and instead focus on optimizing the two main cores of the decompressor: one serial Huffman decoder and the following LZ77 decoder. The Huffman decoder was upgraded to include the ability to process dynamic Huffman blocks as well, which are significantly more complicated to process than static blocks. Our focus thus shifted from designing a fast, static-only Deflate decompressor that relied on fixed block sizes to designing a fast, fully Deflate-compliant decompressor capable of processing both static and dynamic blocks, and that made no assumptions about the block sizes in the compressed data it was given.

4.2 Final Design

A block diagram of the resulting final decompressor design is shown in Fig. 4.3. It is composed of two main cores: the Huffman decoder and the LZ77 decoder, as well as two byte-reordering cores, called the "literal stacker" and the "byte packer". The purposes of these two byte-reordering cores are described below in Sections 4.2.2 and 4.2.4. All four of the cores share the same 250 MHz clock. A balanced and efficient design was sought where the output throughput of the Huffman decoder would match the input throughput of the LZ77 decoder. A data FIFO was instantiated in the middle of the chain in order to alleviate stalling between the two decoders by providing elastic storage, as explained further below. As with our compressor design (in Chapter 3), all four cores are specified in C++ and synthesized using Vivado HLS and are interconnected with standard AXI-Stream interfaces [42]. The data width (TDATA) of all of these interfaces is 32 bits to accommodate the passing of four bytes at a time, in little-endian order. The input data width of the Huffman decoder could be increased further but was chosen to be 4 bytes in order to match the rest of the system, which was determined by the 4-byte processing capabilities of the LZ77 decoder, as explained below. The data signals are accompanied by AXI-Stream sideband signals TKEEP, TUSER, and TLAST. The 4-bit TKEEP signal is used to identify which of the four data bytes are valid in the current transfer and the TLAST signal is used to identify the last transfer of the data stream. The TUSER signal is used to differentiate between AXI-Stream



Figure 4.3: Final non-speculative decompressor architecture.

transfers containing literals and those containing length-distance pairs. The FIFO has a depth of 4096, which allows it to hold 4096 AXI-Stream transfers.

4.2.1 Huffman Decoder

The first core in the decompressor is the Huffman decoder, which is responsible for decoding the Huffman codes and outputting them as literals and lengthdistance pairs. This core differs from the others in that it uses a Finite-State Machine (FSM) architecture instead of a pipelined one. The state diagram is shown in Fig. 4.4. From the starting state, it begins by reading data from the input stream, identifying the Deflate block type from the block header, and then entering the appropriate block processing state: static, dynamic, or stored. Every time data is read from the input stream (i.e., 32 bits), it is placed into a 64-bit buffer called the accumulator. The Huffman decoder only reads new data from the input stream when it runs out of enough bits to decode the next code. Increasing the input stream data width to values larger than 32 bits would mean the Huffman decoder could go longer before reading more input data. The newly read 32 bits are appended to the left side of the accumulator (above any currently held bits) using a shift-OR operation while processed bits get shifted out the right side of the accumulator, as required. For example, after decoding a 9-bit Huffman code and determining that the code was 9 bits long, those 9 bits are then shifted out, all at once, from the accumulator. In the stored block state, the decoder will read the block length,



Figure 4.4: Huffman decoder state diagram.
LEN, and block length complement, NLEN, and verify that the two numbers are complementary (See Fig. 2.3 for the stored block structure). It will then stream LEN bytes from the input to the output. In the static block state, the decoder will continually decode static codes using the static ROM tables until it encounters the EOB code, at which point it returns to the starting state to be ready to process the next Deflate block.

The process for decoding static codes is similar to the process described in Section 2.3.1 when describing reference [38]. From the accumulator, 9 bits are read and looked up in a 512-index literal/length LUT. The table returns the type of the decoded symbol (literal, length, or EOB), the number of bits in the code (7, 8, or 9), the number of extra bits following the code, and the value of the symbol (literal value or base length value). If the symbol is a literal, it is copied unchanged to the output. If the symbol is a length, then the associated extra bits are read from the accumulator as well as the 5-bit distance code that follows that. The distance code is looked up in a 32-index LUT, which returns the distance base value and the number of extra distance bits. The final 9bit length and 16-bit distance values are calculated by adding the base values to the values of the extra bits and are written together to the 32-bit output stream. In order to tell literals apart from length-distance pairs, the 1-bit AXI-Stream TUSER signal is used. It takes the decoder 3 clock cycles to decode a static literal and 4 clock cycles to decode a static length-distance pair, as shown in Fig. 4.5. Note that these operations are not performed pipelined due to dependencies on the accumulator. In order to meet timing while pipelined, Vivado HLS synthesizes the pipeline with an II of 4 (input/output data being read/written every 4 clock cycles), which results in slower operation than a non-pipelined architecture.

When the decoder encounters a dynamic block, it processes it using two states. In the first state, it will read the sequence of code lengths and assemble the dynamic Huffman tables. Then, in the second state, it will use those code tables to decode the dynamic block. In order to build the dynamic tables, the decoder follows the five-step process described in Section 2.1. The table building process takes a variable amount of time that depends on the number



(b) Static length-distance pair processing

Figure 4.5: Huffman decoder static timing diagrams.

of code lengths in the code length sequence, the number of code lengths in the literal/length sequence, and how the literal/length code length sequence has been run-length encoded. Once the dynamic tables have been constructed and stored in BRAMs, the decoder enters the next state where it decodes the dynamic block.

As mentioned in Section 2.3.2, we used the Huffman table design from [40], which allows us to use a 286-index table for literal/length codes and a 32index table for distance codes instead of two much larger 32,768-index tables. The process for decoding a dynamic Huffman code using this architecture is as follows: During Huffman table construction, the base values and base addresses for each of the 15 different code lengths are recorded. In order to decode a code, 15 bits are taken from the accumulator and reversed (since the Huffman codes are stored in reverse order). The code bits are then compared to each of the 15 base code values, which are left-aligned to see if they are greater-than or equal to them. An example of this process is shown in Fig. 4.6. These comparisons are all performed in parallel and the highest passing comparison indicates the length of the code. It is unlikely that all 15 different code lengths will be used in the same Dynamic Huffman table so only comparisons for the code lengths that are used are performed. Once the bit-length of the code is known, the base address for its length can be retrieved. The actual code index



Figure 4.6: An example of how the length of a code is deciphered during decoding using the area-efficient Huffman table memory design from [40]. In this example, the Deflate static codes (from Table 2.1) are used for simplicity. The resulting decoded symbol in this example is length symbol 281.

is calculated by adding an offset to the base address, as shown in Fig. 2.9. This offset is obtained by subtracting the code length base value from the code bits. Once the code has been decoded, the decoder follows the same procedure as it does during static decoding: If the symbol is a literal, the literal is copied unchanged to the output stream. If the symbol is a length, the extra bits are retrieved and then the distance code is decoded using the same above process. The Huffman decoder takes 4 clock cycles to decode a dynamic literal, and 7 clock cycles to decode a dynamic length-distance pair, as shown in Fig. 4.7. As with the static decoding operations, these operations are not pipelined due to dependencies on the accumulator.

4.2.2 Literal Stacker

As will be explained further in Section 4.2.3, the LZ77 decoder has the ability to read four bytes and write four bytes in one clock cycle. While the LZ77 decoder is processing a length-distance command, it will stop reading input bytes, which causes data to start piling up inside the preceding FIFO. In order to: a) more effectively utilize the FIFO's capacity, and b) help the LZ77 decoder catch up on any data backlog, the literal stacker is included in the system pipeline. This module takes the single-byte literals output by the Huffman decoder and consolidates them into stacks of up to four bytes, as shown in Fig. 4.8. Any length-distance pairs in the stream, which occupy



(a) Dynamic literal processing



(b) Dynamic length-distance pair processing

Figure 4.7: Huffman decoder dynamic timing diagrams.



Figure 4.8: Literal stacker operation. In this example, four consecutive literal bytes occupying four consecutive AXI-Stream data transfers are combined to occupy one transfer.

all four bytes of the data width, will force the literal stacker to release its currently held stack of literals. The literal stacker uses the 4-bit AXI-Stream TKEEP signal, as it is intended to be used in the AXI-Stream standard [42], to indicate the number of literals in a stack, from one to four. The literal stacker is pipelined with an II of 1, meaning it can read new inputs in every clock cycle, and it has 2 stages.

4.2.3 LZ77 Decoder

The LZ77 decoder's main purpose is to resolve the length-distance pairs received from the Huffman decoder. It does this using a circular buffer BRAM that has 32,768 one-byte indexes, enough for storing the last 32,768 literal bytes, which is a necessary capacity since Deflate distances can back-reference up to that amount. When the LZ77 decoder receives literals, it records them in the circular buffer for future reference and also writes them out to the output (uncompressed) data stream. When it receives a length-distance pair, it looks back a "distance" number of bytes into the circular buffer and copies a "length" number of them to the head of the circular buffer as well as to the output. While copying the bytes of a length-distance pair, no more inputs are read, which usually causes incoming data to pile up safely in the FIFO before it.

As mentioned above, the LZ77 decoder has the ability to process four bytes in every clock cycle, meaning it can write one to four literals to the circular buffer at a time or copy one to four bytes of a length-distance pair at a time. Originally, it was only able to process one byte per cycle, as done by the LZ77 decoder in [38]. We found that the LZ77 decoder was functioning too slowly to keep up with the Huffman decoder because length-distance pairs were taking longer than expected to resolve (e.g., a match length of 16 bytes would stall the LZ77 decoder for 16 cycles). In order to allow the LZ77 decoder to read and write multiple bytes to the circular buffer in every clock cycle, we used cyclic partitioning. By cyclically partitioning the circular buffer BRAM by a factor of four, we split it into four separate BRAMs where each BRAM holds every fourth byte, as shown in Fig. 4.9. This way, four consecutive indexes in the circular buffer can be read from and written to in every clock cycle (eight simultaneous BRAM accesses altogether). The BRAMs in our assumed Xilinx FPGA fabric are dual-port, meaning they can be read from and written to simultaneously in the same clock cycle.

In Vivado HLS, the partition pragma can be used on an array to automatically partition it into multiple BRAMs. When using this pragma, however, we found that Vivado HLS was unable to schedule the four reads and four writes simultaneously as it could not recognize that we were accessing four consecutive memory locations, one from each partition. Many different coding schemes were tried but the tool would only ever schedule the eight BRAM accesses across four clock cycles, with one read and one write per cycle. In the end, we ended up manually partitioning the array by simply using four



Figure 4.9: Cyclic partitioning of the LZ77 decoder circular buffer BRAM into four disjoint sub-buffers.

different arrays. This way, Vivado HLS was able to schedule the four reads and four writes to the circular buffer partitions in every clock cycle, as desired.

We will refer to the four consecutive addresses read or written (one address per memory partition) as the read and write "windows". These are essentially just read and write pointers that span the width of four memory locations. During operation, these two windows will slide across the circular buffer as multiple bytes are read from the read-window location and written to the write-window location in every clock cycle. In the function pipeline, read and write operations are performed on the circular buffer simultaneously in every clock cycle. In terms of latency, however, the read operation takes place one stage before the write operation does in the pipeline, which can lead to memory access conflicts (i.e., when the same memory address is read from and written to simultaneously) in certain situations.

When the distance value of a length-distance pair is 5, 6, or 7, the readwindow will collide with the write-window on the second iteration if it is allowed to access all four partitions. To prevent this, we programmed the readwindow to keep track of how many bytes it is allowed to read before it must wrap-around to its starting location. The LZ77 decoder keeps track of both the number of length-bytes remaining (the total number of bytes to be copied) and the number of distance-bytes remaining (the number of bytes allowed to be read before the window is reset). Both of these numbers are used to determine how many reads and writes to perform in every cycle so that conflicts do not occur. An example of this is shown in Fig. 4.10.

When the distance value is from 1 to 4, the decoder enters a special state where only one read operation is performed. The decoder reads 1 to 4 bytes and then stores them in four registers, which are then used to write the bytes back to the circular buffer as many times as needed. If the distance is 1, for example, a single byte is read and copied to all four registers, allowing that byte to be written back to the circular buffer four times in every clock cycle instead of just once per cycle. An example of this is shown in Fig. 4.11. When the distance is 32,768, the read and write windows will point to the same location since the circular buffer only has 32,768 indexes. In order to prevent



Figure 4.10: Example showing LZ77 circular buffer access behaviour with a length of 5 and a distance of 5.



Figure 4.11: Example showing LZ77 circular buffer access behaviour with a length of 8 and a distance of 1.

the decoder from redundantly reading a set of bytes and writing them back to the same location, writes are prevented whenever this scenario is detected. The LZ77 decoder will simply read the bytes and write them to the output stream, while shifting the write-window forward.

The most difficult problem that we encountered when designing the LZ77 decoder was getting the pipeline to synthesize with an II of 1 with the fourbyte version in Vivado HLS. With the original one-byte version, the entire decoder was able to be pipelined by Vivado HLS with an II of 1 without problems. The four-byte version, however, would not pipeline with an II of less than 2. Initially, we were able to pipeline certain portions of the function, like the length-distance pair copying loop, but never the entire function. The performance suffered in this case due to delays incurred from frequent switching between literal operation and length-distance pair operation. Many different code iterations were tried involving various different changes in order to experiment and determine how to get the code to synthesize as desired. These changes included: separating out parts of the code into their own functions (this seems to help Vivado HLS by breaking down the problem into smaller pieces since sub-functions are synthesized on their own first before being incorporated in the top-level function), experimenting with the number of different states in the code, rewriting the code in different but functionally-equivalent ways, and changing the function interfaces to different types. In the end, a combination of the above changes led to a version of the LZ77 decoder that was able to pass synthesis with a pipeline II of 1 and a depth of 5 stages.

4.2.4 Byte Packer

Since the LZ77 decoder can output any number of bytes from one to four, the output stream will be filled with null bytes. A null byte is defined to be a byte that is either empty or that contains non-useful information that occupies one byte location in an AXI-Stream transfer [42]. These null bytes must be removed from the stream in order to create a continuously aligned (i.e., fully occupied) output stream. The byte packer performs this operation by using the TKEEP signal to identify which bytes are null bytes to be filtered out from



Figure 4.12: Byte packer operation. In this example, AXI-Stream transfers of various occupancies (3, 4, 2, and 3 bytes) are combined into a continuous aligned stream with full occupancies (4 bytes).

the stream. When a transfer of less than four bytes is received, it will align the bytes and hold on to them until more data is received, outputting only full four-byte transfers until the end of the stream is encountered, as shown in Fig. 4.12. The byte packer is pipelined with an II of 1 and a depth of 3 stages.

4.3 Testing and Results

The four decompressor cores were synthesized using Vivado HLS for a clock frequency of 250 MHz. As with our compressor design in Chapter 3, we synthesized our design for a Xilinx Virtex UltraScale+ XCVU3P-FFVC1517 FPGA, the same device used by our industrial collaborator, Eideticom. Table 4.1 shows the FPGA resource utilization of the four cores. We compressed the Calgary corpus benchmark files using the zlib software in order to create a test set to allow us to test the decompressor. As described in Section 2.2, two sets of files were created: one set compressed using static Huffman codes only, referred to as static files, and one set compressed using the default zlib settings

	LUTs	FFs	BRAM Tiles
Huffman Decoder	6,572~(1.67%)	4,975~(0.63%)	1.5~(0.21%)
Literal Stacker	261~(0.07%)	107~(0.01%)	0
FIFO	99~(0.03%)	139~(0.02%)	5~(0.69%)
LZ77 Decoder	2,243~(0.57%)	820~(0.10%)	8 (1.11%)
Byte Packer	1,013~(0.26%)	389~(0.05%)	0
Total	10,188~(2.59%)	6,430~(0.82%)	14.5 (2.01%)

Table 4.1: Decompressor FPGA Resource Utilization

(which used only dynamic Huffman codes), which we refer to as dynamic files. Before testing, the zlib headers and footers were removed from the files. As with our compressor design, we used a Vivado testbench containing an AXI DMA core, which was used to stream the compressed input data from memory to the decompressor core, receive the uncompressed output data stream, and then write it back to memory for verification. We measured the run time of the decompressor from the moment it receives the first input AXI-Stream transfer to the moment when it outputs the last uncompressed transfer. To obtain the input throughput, the compressed file size is divided by the decompression time. This is not an instantaneous throughput, but an average across the decompression time of the file. This value can be converted to an output throughput by multiplying it by the compression ratio of the file.

The results for the dynamic and static file decompression are shown in Tables 4.2 and 4.3, respectively. The maximum and minimum input throughput values in each table are shown in **bold** font. On the dynamic files, a maximum throughput value of 76.12 MB/s and a minimum throughput value of 62.74 MB/s were achieved, giving an overall average input throughput of 70.73 MB/s. On the static files, a maximum throughput of 151.64 MB/s and a minimum throughput of 101.16 MB/s were achieved, giving an average input throughput of 130.58 MB/s. In both sets of files, "book1" and "book2" gave the highest throughput values while "obj1" and "pic" gave the lowest throughput values. The fact that book1 decompressed at a faster rate than book2 when statically compressed but at a slower rate when dynamically compressed implies that the dynamic Huffman tables of book1 took longer to assemble than those from book2 did during dynamic decompression. The same pattern is seen between files obj1 and pic, with pic decompressing faster when dynamically compressed and obj1 decompressing faster when statically compressed. The input throughput values for the static files are about double those of the dynamic files. This is caused by both the delay incurred when assembling the dynamic Huffman tables as well as the fact that the Huffman decoder takes almost twice as long to decode a dynamic length-distance pair (static: 4 cycles, dynamic: 7 cycles). This large performance increase between

Compressed	Compressed	Compression	Decompression	Input Throughput
File	Size (bytes)	Ratio	Time (μs)	(MB/s)
bib	35,222	3.16	471.948	74.63
book1	313,576	2.45	4197.576	74.70
book2	206,658	2.96	2714.984	(max) 76.12
geo	68,427	1.50	1040.708	65.75
news	144,794	2.60	2017.096	71.78
obj1	10,311	2.09	164.356	(min) 62.74
obj2	81,499	3.03	1155.584	70.53
paper1	18,552	2.87	255.952	72.48
paper2	29,754	2.76	402.156	73.99
pic	$56,\!459$	9.09	896.580	62.97
progc	$13,\!337$	2.97	191.152	69.77
progl	16,249	4.41	224.060	72.52
progp	11,222	4.40	160.564	69.89
trans	19,039	4.92	262.912	72.42

Table 4.2: Dynamically-Encoded Calgary Corpus Decompression Results

 Table 4.3: Statically-Encoded Calgary Corpus Decompression Results

Compressed	Compressed	Compression	Decompression	Input Throughput
File	Size (bytes)	Ratio	Time (μs)	(MB/s)
bib	40,931	2.72	292.220	140.07
book1	384,953	2.00	2538.596	(max) 151.64
book2	243,843	2.51	1643.424	148.37
geo	80,949	1.26	668.172	121.15
news	$168,\!375$	2.24	1266.768	132.92
obj1	11,138	1.93	109.392	101.82
obj2	88,949	2.77	733.724	121.23
paper1	21,670	2.45	157.276	137.78
paper2	$35,\!499$	2.32	241.500	146.99
pic	67,529	7.60	667.552	(min) 101.16
proge	15,365	2.58	117.756	130.48
progl	18,603	3.85	138.320	134.49
progp	12,771	3.87	97.792	130.59
trans	21,424	4.37	165.472	129.47

Reference	Throughput	Area Utilization	Test Files
[38] (2007)	158.64 MB/s (avg., output)	387 LUTs, 128 FFs, 18 RAMB16s	Static Calgary corpus
[39] (2009)	125 MB/s (max, input)	20,596 LUTs, 22 BRAM18Ks	Unknown test files
[40] (2010)	300 MB/s (max)	Not disclosed	Unknown test files
[41] (2016)	375 MB/s (avg., output),	8,250 LUTs, 58 BRAM18Ks	Unknown dynamic test files
	495 MB/s (avg., output)	5,392 LUTs, 21 BRAM18Ks	Unknown static test files
This work	70.73 MB/s (avg., input),	10,188 LUTs, 6,430 FFs,	Dynamic Calgary corpus
	246.35 MB/s (avg., output),	29 BRAM18Ks	
	130.58 MB/s (avg., input),		Static Calgary corpus
	386.56 MB/s (avg., output)		

Table 4.4: FPGA-based Decompressor Design Comparison

static and dynamic files suggests that static compression should be used when rapid decompression is required, assuming that the corresponding decrease in compression ratio is acceptable. This aligns with the current trend of FPGAbased compressors only performing static compression in order to maximize the compression throughput, as seen in other works (described in Section 2.3.1) and in our own compressor (described in Chapter 3).

The results of our work and of previous FPGA-based decompressor designs are summarized in Table 4.4. Due to the unspecified test files that were used to evaluate other published decompressor designs, it is difficult to make a fair comparison with most previous works. As shown by our results, the type of data and amount of compression it has undergone make a big impact on the decompression throughputs that are achievable. If we convert our average input throughput values of 70.73 MB/s (dynamic) and 130.58 MB/s (static) to output throughput values, we get 246.35 MB/s (dynamic) and 386.56 MB/s (static). These values are comparable to the 375 MB/s (dynamic) and 495 MB/s (static) average output throughputs of the proprietary Xilinx IP core [41]. Compared to the static average output throughput of 158.64 MB/s from [38], our design is about 2.44 times faster, which is a tribute to the capabilities of high-level synthesis. In terms of resource utilization, our design uses half as many LUTs but one third more BRAMs compared to [39]. Compared to the Xilinx IP core [41], our design uses about 23% more LUTs but half as many BRAMs. We can only speculate since no design details are shared in [41], however, the extra BRAMs may be used in some sort of speculatively parallelized architecture.

As mentioned above, the FIFO in our decompressor has a depth of 4096, meaning it can store up to 4096 transfers containing either literals or lengthdistance pairs. The FIFO count can be used as a measure of the amount of stalling done by the LZ77 decoder. For most static and dynamic files, the maximum FIFO count rarely went above 30, demonstrating the LZ77 decoder's ability to keep up with the Huffman decoder. The one exception to this is the benchmark file pic, which had a dynamic max FIFO count of 1441 while the static file maxed out the FIFO at 4096. The reason for this is due to the pic file's very high compression ratio which is a result of it being compressed using many length-258 length-distance pairs. Each of these length-distance pairs takes the LZ77 decoder 65 clock cycles to resolve with it copying four bytes per cycle. The LZ77 decoder could be improved by expanding the window width even further to be able to copy eight or sixteen bytes per cycle. However, the decompression throughput would not increase significantly, except for with highly compressed files like pic or unless the Huffman decoder was improved significantly as well. The purpose of the literal stacker module was to help the LZ77 decoder to catch up on any backlogged data in the FIFO. We found that the presence of the literal stacker was able to provide throughput improvements ranging from 0 to 4%, with the biggest benefit occurring while decompressing the pic file. This speedup was also mainly seen when processing static files, as the dynamic table construction phase gives the LZ77 decoder opportunities to catch up when processing dynamic files. Due to the small added latency (2 pipeline stages) and area overhead of the literal stacker, we believe this to be a worthwhile trade-off. This speedup benefit would increase even further with a higher-throughput Huffman decoder, which would put more pressure on the LZ77 decoder.

4.4 Discussion

From the timing diagrams in Figs. 4.5 and 4.7, we can identify areas where the performance of the Huffman decoder could be improved. The most obvious improvements are in the processing of static and dynamic literals in Fig. 4.5. The "Update Accumulator" operation should be able to be performed one cycle earlier in both cases. This highlights another limitation of Vivado HLS, when the way a piece of software code is written results in inefficient synthesis for non-obvious reasons. In this case, it appears that the presence of the length-distance pair processing code causes unnecessary caution for Vivado HLS in the synthesis process. We verified this by removing the lengthdistance pair code from the Huffman decoder and, as expected, it was then able to write static literals every 2 cycles and dynamic literals every 3 cycles. Unfortunately, some experimentation with the syntax of the C code may be required to overcome such synthesis problems like these in order to achieve the expected performance.

Another improvement would be to perform the lookup of the distance code at the same time as the length code, for static length-distance pairs, as the second lookup forces an additional cycle of latency. This would require multiple prospective lookups since the bit-length of the length code is unknown until after it has been decoded. Once known, however, a MUX could be used to select the correctly decoded distance. The performance of the Huffman decoder is not necessarily limited by the critical path delay, but rather by the lookup delay since a table lookup must be performed across two clock cycles (i.e., in the first clock cycle the address is given to the table, in the second cycle the data is received from the table). Therefore, a literal will never take fewer than 2 clock cycles to output due to how it is decoded using a table.

For the dynamic decoding processes, the code-length deciphering portion is currently the logical critical path. If the deciphering (which takes place once during cycles 1 and 2 in Figs. 4.7a and 4.7b, and a second time in cycles 4 and 5 in Fig. 4.7b) was able to be performed within the same clock cycle, the length and distance decoding lookups could be performed one cycle sooner, resulting in dynamic length-distance pairs being output two cycles faster. It may also be possible to pipeline the operation of the Huffman decoder if the architecture can be changed to remove the dependency on the accumulator. Optimizations of this nature may require a hand-optimized Verilog or VHDL structural-level implementation in order to achieve them; however, higher clock frequencies may also be possible this way. The prospective lookup of both length and distance codes simultaneously would be a lot more difficult to perform with dynamic codes since both codes can be from 1 to 15 bits long, meaning there are more than 15×15 (225) possibilities of code length combinations. This doesn't include the 0 to 5 extra bits that may fall in between the length and distance codes as well.

As mentioned above, the LZ77 decoder window width could be further expanded to copy more bytes of a length-distance pair at a time. Hypothetically, this could be done to the point where a length-258 length-distance pair (the longest match length possible) could be copied in a single iteration. In this case, it would require partitioning the circular buffer into 512 partitions of 64 indexes each (as 256 partitions wouldn't be enough). As explained before, though, only very highly compressed files would benefit from this type of architecture. Expanding the LZ77 decoder to be able to copy 16 bytes per cycle is probably the most effective width to expand to since the compressor-related works described in Section 2.3.1 reported that match lengths greater than 16 bytes are rare for most file types.

As shown in Table 4.1, the decompressor core occupies a relatively small area, using only 2.59% of the LUTs and 2.01% of the BRAMs on the FPGA. It is worth noting that this model of FPGA is the smallest of the Xilinx Virtex UltraScale+ product line. The compact core size allows for multiple decompressors to be utilized in parallel as part of a multi-file decompressor system. Hypothetically, a cluster of 32 decompressors would use about 83% of the LUTs and 64% of the BRAMs on the FPGA while being able to collectively provide average input decompression throughputs of 4.18 GB/s for statically encoded files and 2.26 GB/s for dynamically encoded files. This is assuming that enough LUTs remain to be able to interface with the 32 decompressors and that such a system could be routed properly.

A single decompressor core could also be improved by implementing multiple Huffman decoders in parallel as part of a speculatively parallel design, as in our original design (See Fig. 4.1). The benefits of this would be data-dependent and statistical, however, unless exploiting a fixed block size that happened to be present in the compressed data. A design incorporating multiple LZ77 decoders in parallel might be feasible but would also be complicated. The LZ77 decoders would need to be interconnected and have the ability to communicate with each other. When an LZ77 decoder encounters a back-reference to data held by another decoder, it would need to stop processing and request that data from the other decoder. A design that employs two-pass parallelization could also be created. Multiple parallel LZ77 decoders could perform a rapid first-pass on data while skipping over any back-references to unheld data. A final LZ77 decoder could collect the data from them and perform the second pass that resolves all of the remaining back-references. The final decoder would need to be fast enough to keep up with the first-pass decoders; otherwise, such a decoder would end up becoming the bottleneck. Any design incorporating multiple LZ77 decoders would also need to use multiple Huffman decoders in order to split the sequential data stream into multiple blocks.

4.5 Summary

In this chapter, we described two FPGA-based Deflate decompressor designs. As described in Chapter 2, the Deflate format makes acceleration using blocklevel parallelism difficult to achieve without altering the compressed format. Instead of exploiting block-level parallelism through speculation or using a fixed block size, our final decompressor design exploits micro-scale parallelism at the hardware level in order to accelerate the process. These exploits include pipelining at the system level (i.e., concurrently operating the Huffman and LZ77 decoders) and on the task level (i.e., the three pipelined cores operating with an II of 1). We also utilized BRAMs to perform quick decoding in the Huffman decoder and BRAM partitioning to copy multiple bytes at a time in the LZ77 decoder. By doing this, our decompressor design was able to achieve competitive throughputs with efficient hardware utilizations even while using high-level synthesis. Since most other designs don't specify the test files they used to get their results, it is difficult to make many fair comparisons. Compared to the design from [38], where the authors tested their design on a statically compressed Calgary corpus, our design is about 2.44 times faster. Our design is also comparable to the proprietary design sold by Xilinx [41], which has average output static and dynamic throughputs of 495 MB/s and 375 MB/s, respectively, while our design has average output static and dynamic throughputs of 386.56 MB/s and 246.35 MB/s, respectively.

As discussed in Section 4.4, we haven't yet fully reached the limits of exploitable parallelism in our design. Many different optimizations could be made to the Huffman decoder in order to reduce the latencies while the LZ77 decoder window width still has room to be scaled up. Multiple Huffman decoders could be implemented in a speculative parallelization architecture, but we believe this to generally be a poor trade-off. Architectures like this require extra area and provide statistical speed-ups that can't be relied on. This extra area is better spent implementing multiple independent decompressor cores in order to decompress multiple files at a time. Due to the small area of our decompressor design, a system like this would be easily achievable and would be able to achieve massive multi-file decompression throughputs, as explained in Section 4.4.

Chapter 5 Conclusion

5.1 Summary

This thesis research considered the design and implementation of FPGA-based hardware implementations of the Deflate lossless compression and decompression algorithms, using high-level synthesis. For the design of our FPGA-based compressor, we followed the current state-of-the-art architecture that many other designs have been using, which utilizes a fixed-throughput pipeline that performs static Huffman encoding only in order to rapidly compress data. Although these FPGA-based compressor designs provide lower compression ratios than software compressors, they are able to achieve compression throughputs that are a couple orders of magnitude greater. As shown in Table 3.3 and discussed in Section 2.3.1, FPGA-based compressors can achieve input throughputs ranging from 3 to 4 GB/s with mean compression ratios around 2.00, while software compressors typically compress around 50 MB/s with mean compression ratios around 3.00. Our FPGA-based compressor design was able to achieve arithmetic and geometric mean compression ratios of 2.00 and 1.92, respectively, across the Calgary corpus benchmark. Though these values are slightly lower than those achieved by other previous works, which were able to achieve values up to 2.17 [27], we were able to achieve a clock frequency of 250 MHz for our design, giving us a compression throughput of 4.0 GB/s, which is higher than the previous fastest design capable of compressing 3.20 GB/s [7]. These results were also obtained using high-level synthesis, which shows that Vivado HLS is capable of producing competitively performing designs.

In terms of Deflate decompression, the amount of published FPGA-based designs is much fewer. Despite this, we were able to find some designs with ideas that proved useful to include in our design. We also analyzed the technique of speculative parallelization, which has been performed by some software-based decompressors, and investigated how this may be performed on a hardware platform such as an FPGA. For the design of our FPGA-based decompressor, we set out to exploit the parallel hardware resources in FPGAs in order to achieve the fastest decompression throughputs possible. Doing this, we were able to achieve average input decompression throughputs of 130.58 MB/s and 70.73 MB/s for static and dynamic files from the Calgary corpus, respectively. These values correspond to output throughputs of 386.56 MB/s and 246.35 MB/s for static and dynamic files, respectively. Our design is about 2.44 times faster than the design from [38] and has comparable throughputs to the expertly-optimized proprietary IP decompressor sold by Xilinx [41], which has average output static and dynamic throughputs of 495 MB/s and 375 MB/s, respectively, though these results were achieved using unknown test files. Even though we used Vivado HLS to synthesize our decompressor core, we were still able to achieve a compact design that only utilizes 2.59% of the LUTs and 2.01% of the BRAMs on a low tier Xilinx Virtex UltraScale+ XCVU3P-FFVC1517 FPGA. On this FPGA, we could hypothetically deploy a cluster of 32 decompressor cores (while only using 83% of the LUTs and 64%of the BRAMs) and expect to achieve multi-file input decompression throughputs of 4.18 GB/s for statically compressed files and 2.26 GB/s for dynamically compressed files.

5.2 Evaluation of Vivado HLS

As part of this thesis, we evaluated the use of high-level synthesis, specifically Vivado HLS, as a tool for speeding up digital hardware design. From the results of our compressor and decompressor designs, which are summarized in the previous section, we have shown that Vivado HLS is able to create competitive designs in terms of both performance and area compared to designs specified in structural-level VHDL or Verilog. Achieving these competitive results, however, did not come easily due to some of the limitations that Vivado HLS has. In Section 3.2.1, we described the difficulties that we encountered when trying to meet post-route timing with our LZ77 encoder design. As Vivado HLS is only aware of (and therefore only has control over) the logic synthesis part of the FPGA design flow, sometimes extra effort is required in order to help a large and complex design (with significant routing delays) to meet timing following implementation. In Section 3.2.2, we explained a useful advantage of Vivado HLS with its ability to automatically optimize certain operations into simpler ones, like multiplication and division by powers of two automatically being converted into left-shift and right-shift operations. This can lead to faster and more area-efficient designs being synthesized without the user even being aware of these optimizations occurring. This was also shown in Section 3.2.3, where Vivado HLS was shown to be making design optimizations at the system pipeline level, resulting in our 16-stage Huffman encoder design being compacted down automatically into a more efficient 6-stage pipeline.

In Section 4.1, we described what we call the "coarse function scheduling" limitation of Vivado HLS. Due to how the tool operates, sub-functions within a synthesized core must be scheduled to start and finish on strict timing boundaries, preventing the asynchronous execution of multiple functions at a time. This limitation can be overcome to an extent using the Vivado HLS dataflow pragma, which allows each sub-function to operate itself independently of the others; however, this pragma itself imposes many constraints on the code to be synthesized. In Section 4.2.3, we described the difficulties that we encountered when using the partition pragma in order to automatically partition our LZ77 decoder circular buffer due to the fact that the tool could not recognize that we were accessing the memories safely without conflict. In the same section we also described the difficulties in achieving a pipeline II of 1 in our design. This difficulty was caused by the way our code was written, requiring us to rewrite our code in many functionally equivalent ways in order to find a syntax that the tool preferred. In Section 4.4, we gave another example of the same problem where the code describing our Huffman decoder has resulted in inefficient synthesis and the delay of certain operations being performed, even when it is clear that the delay is unnecessary.

Vivado HLS is a tool that comes with many useful advantages but also has many limitations. Although it enables RTL designs to be described in a highlevel software programming language, it still requires a hardware engineering design mindset. The ability for Vivado HLS to automatically optimize certain parts of a design, without explanation, is both a blessing and a curse. It requires a very low-level understanding of what is expected to be synthesized and how hardware synthesis is performed in order to be able to understand some of the decisions that Vivado HLS makes in its operation. In general, the simpler a design, the easier it will be to synthesize efficiently using the tool. When attempting to synthesize large and complicated designs that realistically should be synthesizeable, it can be frustrating working around the quirks of Vivado HLS in order to get it to create what you want. In summary, Vivado HLS is a very powerful tool to aid in the design of digital hardware that comes with the cost of having a steep leaning curve in order to be able to use effectively.

5.3 Future Work

As discussed in Section 3.4, our compressor design still has room for improvement in terms of achieving greater compression ratios. First, the hash function still may have room to be improved in order to reduce the likelihood of bank access conflicts. Second, the hash bank architecture could be scaled up in multiple ways at the cost of area and throughput in order to increase the compression ratio. Other potential ideas for improving the compression ratio include using multiple hash functions for different data types or making the major design changes necessary to be able to perform dynamic Huffman encoding as well as static encoding. There is still room for improvement in the throughput of a single-core compressor as well, before resorting to scaling up the number of compressors working in parallel. Since we were able to achieve a clock frequency of 250 MHz using high-level synthesis, it is reasonable to expect that hand-coded RTL designs should be able to surpass this number.

As discussed in 4.4, our decompressor design still has not quite exploited all available parallelism. The Huffman decoder still has plenty of inefficiencies in its implementation that could be improved and the LZ77 decoder could be easily scaled up further in order to resolve large length-distance pairs faster. Once these limits of parallelism are reached, speculative parallelization is one way of potentially achieving even greater speed-ups at the cost of additional hardware area. Due to the inherently-serial Deflate compressed format, however, improving the decompression speeds much further than currently achievable numbers will be difficult and will likely never reach the values of more easily parallelizable compressed formats. This situation is an example of where a well-entrenched and widely-used standard is effectively limiting achievable improved performance.

References

- R. Koenen. (2002). Overview of the MPEG-4 standard, [Online]. Available: https://web.archive.org/web/20100428021525/http://mpeg. chiariglione.org/standards/mpeg-4/mpeg-4.htm.
- [2] L. P. Deutsch. (1996). "RFC 1951: DEFLATE compressed data format specification version 1.3", [Online]. Available: https://www.w3.org/ Graphics/PNG/RFC-1951.
- [3] D. Salomon, *Data Compression: The Complete Reference*, 4th ed. Springer Science & Business Media, 2006.
- [4] E. Sitaridi, R. Mueller, T. Kaldewey, G. Lohman, and K. A. Ross, "Massively-parallel lossless data decompression," in the 45th Int. Conf. Parallel Processing (ICPP), 2016, pp. 242–247.
- [5] J. Fowers, J. Y. Kim, D. Burger, and S. Hauck, "A scalable highbandwidth architecture for lossless compression on FPGAs," in *IEEE* 23rd Annu. Int. Symp. Field-Programmable Custom Computing Machines (FCCM), 2015, pp. 52–59.
- [6] J. Cong, Z. Fang, M. Huang, L. Wang, and D. Wu, "CPU-FPGA Coscheduling for big data applications," English, *IEEE Design & Test*, vol. 35, no. 1, pp. 16–22, 2018.
- [7] W. Qiao, J. Du, Z. Fang, M. Lo, M.-C. F. Chang, and J. Cong, "Highthroughput lossless compression on tightly coupled CPU-FPGA platforms," in *IEEE 26th Annu. Int. Symp. Field-Programmable Custom Computing Machines (FCCM)*, 2018, pp. 37–44.
- [8] R. Buyya, C. S. Yeo, S. Venugopal, J. Broberg, and I. Brandic, "Cloud computing and emerging IT platforms: Vision, hype, and reality for delivering computing as the 5th utility," *Future Generation Computer Systems*, vol. 25, no. 6, pp. 599–616, 2009.
- [9] Amazon Web Services, Inc. (2019). Amazon EC2 F1 Instances, [Online]. Available: https://aws.amazon.com/ec2/instance-types/f1/.
- [10] J. L. Hennessy and D. A. Patterson, Computer Architecture : A Quantitative Approach, 5th ed. Burlington: Elsevier Science & Technology, May 2014, ISBN: 9780123704900.

- [11] R. H. Dennard, F. H. Gaensslen, V. L. Rideout, E. Bassous, and A. R. LeBlanc, "Design of ion-implanted MOSFET's with very small physical dimensions," *IEEE Journal of Solid-State Circuits*, vol. 9, no. 5, pp. 256–268, 1974.
- [12] "IEEE standard VHDL language reference manual," IEEE Std 1076-2008 (Revision of IEEE Std 1076-2002), 2009.
- [13] "IEEE standard for Verilog hardware description language," *IEEE Std* 1364-2005 (Revision of IEEE Std 1364-2001), 2006.
- [14] S. Lahti, P. Sjövall, J. Vanne, and T. D. Hämäläinen, "Are we there yet? A study on the state of high-level synthesis," *IEEE Transactions* on Computer-Aided Design of Integrated Circuits and Systems, vol. 38, no. 5, pp. 898–911, 2019.
- [15] Xilinx Inc. (2019). Vivado High-Level Synthesis, [Online]. Available: https://www.xilinx.com/products/design-tools/vivado/ integration/esl-design.html.
- [16] PKWARE Inc. (2019). PKZIP, [Online]. Available: https://www. pkware.com/pkzip.
- [17] J.-l. Gailly and M. Adler. (2018). gzip, [Online]. Available: https:// www.gzip.org/.
- [18] —, (2017). zlib, [Online]. Available: https://zlib.net/zlib.html.
- [19] M. Adler, Answer to: How are zlib, gzip and zip related? what do they have in common and how are they different? Dec. 2013. [Online]. Available: https://stackoverflow.com/questions/20762094/how-arezlib-gzip-and-zip-related-what-do-they-have-in-common-andhow-are-they/20765054%5C#20765054.
- [20] PKWARE Inc. (2019). ".ZIP file format specification", [Online]. Available: https://pkware.cachefly.net/webdocs/casestudies/ APPNOTE.TXT.
- [21] L. P. Deutsch. (1996). "RFC 1952: GZIP file format specification version 4.3", [Online]. Available: https://tools.ietf.org/html/rfc1952.
- [22] T. Boutell. (1997). "RFC 2083: PNG (portable network graphics) specification version 1.0", [Online]. Available: https://tools.ietf.org/ html/rfc2083.
- [23] J. Ziv and A. Lempel, "A universal algorithm for sequential data compression," *IEEE Trans. Info. Theory*, vol. 23, no. 3, pp. 337–343, 1977.
- [24] D. A. Huffman, "A method for the construction of minimum-redundancy codes," *Proc. of the IRE*, vol. 40, no. 9, pp. 1098–1101, 1952.
- [25] E. S. Schwartz and B. Kallick, "Generating a canonical prefix encoding," Communications of the ACM, vol. 7, no. 3, pp. 166–169, 1964.

- [26] T. Bell, I. H. Witten, and J. G. Cleary, "Modeling for text compression," ACM Computing Surveys (CSUR), vol. 21, no. 4, pp. 557–591, 1989.
- [27] M. S. Abdelfattah, A. Hagiescu, and D. Singh, "Gzip on a chip: High performance lossless data compression on FPGAs using OpenCL," in *Proc. Int. Workshop on OpenCL 2013 & 2014*, ser. IWOCL '14, Bristol, United Kingdom: ACM, 2014, pp. 4–9.
- [28] A. Martin, D. Jamsek, and K. Agarawal, "FPGA-based application acceleration: Case study with gzip compression/decompression streaming engine," *ICCAD Special Session C*, vol. 7, 2013.
- [29] Y. Kim, S. Choi, J. Jeong, and Y. H. Song, "Data dependency reduction for high-performance FPGA implementation of DEFLATE compression algorithm," *Journal of Systems Architecture*, vol. 98, pp. 41–52, 2019. [Online]. Available: http://www.sciencedirect.com/science/ article/pii/S1383762118306453.
- [30] V. Gopal, J. Guilford, W. Feghali, E. Ozturk, and G. Wolrich, *High performance DEFLATE compression on Intel® architecture processors*, 2011. [Online]. Available: https://www.intel.com/content/dam/www/public/us/en/documents/white-papers/ia-deflate-compression-paper.pdf.
- [31] D. Harnik, E. Khaitzin, D. Sotnikov, and S. Taharlev, "A fast implementation of Deflate," in 2014 Data Compression Conference, 2014, pp. 223– 232.
- [32] M. Chłopkowski and R. Walkowiak, "A general purpose lossless data compression method for GPU," *Journal of Parallel and Distributed Computing*, vol. 75, pp. 40–52, 2015.
- [33] H. Jang, C. Kim, and J. W. Lee, "Practical speculative parallelization of variable-length decompression algorithms," *SIGPLAN Not.*, vol. 48, no. 5, pp. 55–64, Jun. 2013.
- [34] Z. Wang, Y. Zhao, Y. Liu, Z. Chen, C. Lv, and Y. Li, "A speculative parallel decompression algorithm on Apache Spark," *Journal of Supercomputing*, vol. 73, no. 9, pp. 4082–4111, 2017.
- [35] The Apache Software Foundation. (2018). *Apache Spark*, [Online]. Available: https://spark.apache.org/.
- [36] M. Kerbiriou and R. Chikhi, "Parallel decompression of gzip-compressed files and random access to DNA sequences," May 2019. [Online]. Available: https://arxiv.org/abs/1905.07224.
- [37] H. Li. (2008). "FASTQ format specification", [Online]. Available: http: //maq.sourceforge.net/fastq.shtml.

- [38] J. Lazaro, J. Arias, A. Astarloa, U. Bidarte, and A. Zuloaga, "Decompression dual core for SoPC applications in high speed FPGA," in *IECON 2007 - 33rd Annu. Conf. IEEE Industrial Electronics Society*, 2007, pp. 738–743.
- [39] D. C. Zaretsky, G. Mittal, and P. Banerjee, "Streaming implementation of the ZLIB decoder algorithm on an FPGA," in *IEEE Int. Symp. Circuits and Systems*, 2009, pp. 2329–2332.
- [40] J. Ouyang, H. Luo, Z. Wang, J. Tian, C. Liu, and K. Sheng, "FPGA implementation of GZIP compression and decompression for IDC services," in *IEEE Int. Conf. Field-Programmable Technology (FPT)*, IEEE, 2010, pp. 265–268.
- [41] Xilinx and CAST Inc. (2016). GUNZIP/ZLIB/Inflate Data Decompression Core, [Online]. Available: https://www.xilinx.com/products/ intellectual-property/1-79drsh.html#overview.
- [42] ARM, AMBA 4 AXI4-Stream Protocol, 2010.
- [43] Xilinx Inc., UG902 Vivado design suite user guide: High-level synthesis (v2019.1), Jul. 2019. [Online]. Available: https://www.xilinx.com/ support/documentation/sw_manuals/xilinx2019_1/ug902-vivadohigh-level-synthesis.pdf.

Appendix A LZ77 Encoder Source File

LZ77_Encoder.cpp

```
#include "LZ77_Encoder.h"
  #include <utils/x_hls_utils.h>
  t_hash_size hash_func(
      ap_uint <8> in_byte0,
      ap\_uint < 8 > in\_byte1,
      ap_uint <8> in_byte2,
      ap_uint <8> in_byte3,
      ap_uint <8> in_byte4
9
  ){
10
    t_hash_size hash;
12
    hash = ((t_hash_size))in_byte0 * 31) in_byte1;
13
    hash.rrotate(4);
14
    hash = (hash * 3) \hat{} in_byte2;
    hash.rrotate(4);
16
    hash = (hash * 3) \hat{} in_byte3;
17
    hash.rrotate(4);
18
    hash = (hash * 3) \hat{} in_byte4;
19
20
    return hash;
21
  }
22
23
  void bank_access_func(
24
       t_hash_size
                            hash [WIN_SIZE],
                                                           //Input
25
       ap_uint<WIN_SIZE*8> substring_ints [WIN_SIZE],
                                                           //Input
26
                        data_pos,
                                            //Input
       ap_uint <32>
       ap_uint<NUM_BANKS> &bank_accessed_bits,
                                                       //Output
28
       ap_uint<WIN_SIZE>
                            &substring_access_bits,
                                                        //Output
29
                             associated_bank [WIN_SIZE], //Output
       t_bank_values
30
                        string_to_write [NUMLBANKS], //Output
      match_t
31
       t_bank_size
                        string_address [NUMLBANKS] //Output
32
33)
34 #pragma HLS INLINE off
   t_num_banks desired_bank [WIN_SIZE];
35
36 #pragma HLS ARRAY_PARTITION variable=desired_bank complete dim=1
   t_bank_size bank_address [WIN_SIZE];
37
```

```
38 #pragma HLS ARRAY_PARTITION variable=bank_address complete dim=1
    t_win_size associated_substring [NUMBANKS] = \{0\}; //Contains the
39
       substring number given to each bank
40 #pragma HLS ARRAY_PARTITION variable=associated_substring complete
      \dim = 1
41
42
    Bank_Access: for (int i = WIN_SIZE-1; i >= 0; i--){ //For each
      substring (starting from the bottom)
      desired_bank[i] = hash[i](HASH_BITS-1,HASH_BITS-NUM_BANKS_BITS
43
      ); //The top 5 bits of the hash value indicate the desired
      bank to be accessed
      bank_address[i] = hash[i](BANK_SIZE_BITS-1,0); //The bottom 9
44
      bits are the bank address to access
      if(bank_accessed_bits[desired_bank[i]] == 0){ // If desired
45
      bank has not already been accessed
        bank_accessed_bits [desired_bank[i]] = 1; //Set bank as
46
      accessed
        substring_access_bits[i] = 1; //Record substring as granted
47
      access
        associated_bank [i] = desired_bank [i]; //Record bank accessed
48
      by substring
        associated_substring [desired_bank[i]] = i; //Record
49
      substring given to bank
      }
50
      else{
51
        associated_bank[i] = NUMLBANKS; //Associate with null bank
      }
53
    }
54
55
    //Pass 1 of 16 substrings to each of 32 banks (Not all banks
56
      will actually be accessed)
    String_to_Bank_MUX: for (int i = 0; i < NUMBANKS; i++){//For}
      each bank
      string_to_write[i].string = reg(substring_ints[
58
      associated_substring[i]]);
      string_to_write[i].position = data_pos + associated_substring[
      i];
      string_address[i] = bank_address[associated_substring[i]];
60
    }
61
  }
62
63
64 void LZ77_Encoder(
      stream<in_strm> &strm_in,
65
      stream<out_strm> & strm_out,
66
                  input_size
      int
67
68) {
<sup>69</sup> #pragma HLS INTERFACE axis register both port=strm_in //Input
     AXI Stream
70 #pragma HLS INTERFACE axis register both port=strm_out //Output
     AXI Stream
71
    in_strm input_buff;
72
    ap_uint <8> curr_window [2*WIN_SIZE]; // Current window of data to
73
     be compressed.
```

74 75	<pre>#pragma HLS ARRAY_PARTITION variable=curr_window complete dim=1 t_hash_size hash[WIN_SIZE]; //Hash values of each substring in</pre>
10	curr_window.
76	#pragma HLS ARRAY.PARTITION variable=hash complete dim=1
77	static match_t dictionary [NUM_BANKS] [BANK_DEPTH] [BANK_SIZE]; //
	Dictionary partitioned into banks with each bank having
	multiple depth levels
	#pragma HLS RESOURCE variable=dictionary core=RAM_S2P_BRAM
	#pragma HLS ARRAY_PARTITION variable=dictionary complete dim=1
80	#pragma HLS ARRAY_PARTITION variable=dictionary complete dim=2
81	$ap_uint < 32$ > $data_pos = 0; //Marker$ to keep track of input data
	position
82	ap_uint <win_size> match_length_bits [NUM_BANKS] [BANK_DEPTH]; //</win_size>
	Bit-string of matching bytes between substring and potential
	matches
83	#pragma HLS ARRAY_PARTITION variable=match_length_bits complete
	dim=0
84	t_match_size match_length [NUM_BANKS] [BANK_DEPTH]; //Integer
	value of match length between substring and potential matches #pragma HLS ARRAY_PARTITION variable=match_length complete dim=0
85 86	t_match_size bank_best_length [NUM_BANKS]; //The value of the
80	best match length from each bank
87	#pragma HLS ARRAY PARTITION variable=bank_best_length complete dim
01	
88	ap_int <32> bank_best_position [NUM_BANKS]; //The position of the
	best match from each bank
89	#pragma HLS ARRAY_PARTITION variable=bank_best_position complete
	dim=1
90	t_bank_depth bank_best_match [NUM_BANKS]; //The depth number
	containing the best match from each bank
91	#pragma HLS ARRAY_PARTITION variable=bank_best_match complete dim
92	t_match_size window_best_length[WIN_SIZE]; //The value of the
	best match length for each substring
93	#pragma HLS ARRAY_PARTITION variable=window_best_length complete
0.4	dim=1 ap_int <32> window_best_position [WIN_SIZE]; //The position of the
94	best match for each substring
05	#pragma HLS ARRAY_PARTITION variable=window_best_position complete
50	dim=1
96	t_win_size last_match; //Position of last match in current
	window. Used to calculate FVP
97	t_win_size first_valid_pos = 0; //Marker to keep track of first
	valid match position in current window
98	t_match_size reach[WIN_SIZE]; //How far a match extends within
	the current window
99	#pragma HLS ARRAY_PARTITION variable=reach complete dim=1
100	ap_uint <32> offsets [WIN_SIZE]; // Offset of each best match found
101	#pragma HLS ARRAY PARTITION variable=offsets complete dim=1
102	ap_uint <win_size> valid_matches_bits; //Bit-string for</win_size>
	identifying valid best matches after filtering
103	ap_uint <win_size> matched_literals_bits; //Bit-string for</win_size>
10.1	locating matched literals in current window
104	out_array output_array [WIN_SIZE];

```
105 #pragma HLS ARRAY_PARTITION variable=output_array complete dim=1
     out_strm output_buff = \{0\};
106
     int num_iterations;
107
     t_match_size bytes_conflicting; //Number of bytes conflicting
108
      between two potential matches
     ap_uint <NUM_BANKS> bank_accessed_bits; //Bit-string for
109
      recording which dictionary banks have been accessed for
      writing
     ap_uint<WIN_SIZE> substring_access_bits; //Bit-string for
      recording which substrings have been granted access to a bank
     t_bank_values associated_bank[WIN_SIZE]; //Contains the bank
      number accessed by each window substring
112 #pragma HLS ARRAY_PARTITION variable=associated_bank complete dim
      =1
     match_t string_to_write [NUM_BANKS]; //String + position to be
113
      written to each bank
<sup>114</sup> #pragma HLS ARRAY PARTITION variable=string_to_write complete dim
      =1
     t_bank_size string_address [NUM_BANKS]; //Address to write string
115
       and position to
116 #pragma HLS ARRAY PARTITION variable=string_address complete dim=1
     match_t potential_match [NUM_BANKS] [BANK_DEPTH]; // Potential
      matches read from each bank and depth level
118 #pragma HLS ARRAY_PARTITION variable=potential_match complete dim
      =0
     ap_uint<WIN_SIZE*8> substring_ints [WIN_SIZE]; //Integers of each
119
        substring in current window
120 #pragma HLS ARRAY_PARTITION variable=substring_ints complete dim=1
     //Dictionary Initialization
     Dict_Init_Loop_A: for (int i = 0; i < BANK_SIZE; i++) { //For each
123
       bank entry
       Dict_Init_Loop_B: for (int j = 0; j < NUMBANKS; j++) \{ //For \}
124
      each bank
  #pragma HLS UNROLL
125
         Dict_Init_Loop_C: for (int k = 0; k < BANK_DEPTH; k++){ //For
126
        each depth level
  #pragma HLS UNROLL
            dictionary [j][k][i]. string = 0;
128
            dictionary [j][k][i]. position = -32769;
129
130
         }
       }
     }
133
     num_{iterations} = (input_{size} - 1)/WIN_{SIZE} + 1; //Calculate number
134
        of iterations (Rounded up)
     //In the first iteration, current window needs to be loaded
135
      before shifting order to fill it completely
     strm_in >> input_buff;
136
     First_Load: for (int i = 0; i < WIN_SIZE; i++){ //Load window
      with data from input buffer
138 #pragma HLS UNROLL
       \operatorname{curr}_{\operatorname{window}}[i + \operatorname{WIN}_{\operatorname{SIZE}}] = \operatorname{input}_{\operatorname{buff}} \operatorname{data}((i * 8) + 7, i * 8); //
139
      Convert from int to array (Little Endian)
```

```
}
140
141
     if (!input_buff.last) { // If first read wasn't last
142
        //Main Function Loop
143
       Main_Loop: for (int n = 0; n < (num_iterations - 1); n++){//
144
       Perform all iterations except last in loop
145
  #pragma HLS PIPELINE
  #pragma HLS DEPENDENCE variable=dictionary inter false
146
147
          Window_Shift: for (int i = 0; i < WIN_SIZE; i++){ //Shift
148
       second half of window into front half of window
            \operatorname{curr}_{\operatorname{window}}[i] = \operatorname{curr}_{\operatorname{window}}[i + \operatorname{WIN}_{\operatorname{SIZE}}];
149
          }
150
151
          strm_in >> input_buff;
152
          Load_Window: for (int i = 0; i < WIN_SIZE; i++){ //Load}
       window with data from input buffer
            \operatorname{curr}_{\operatorname{window}}[i + \operatorname{WIN}_{\operatorname{SIZE}}] = \operatorname{input}_{\operatorname{buff}} \operatorname{data}((i * 8) + 7, i * 8);
154
       //Convert from int to array (Little Endian)
155
156
          Hash: for (int i = 0; i < WIN_SIZE; i++){ //Hash each
       substring of window
            hash[i] = hash_func(curr_window[i], curr_window[i+1])
158
       curr_window [i+2], curr_window [i+3],
                 curr_window[i+4]); //Hash first four bytes of each
       substring
          }
160
161
          Pull_Substrings_A: for (int i = 0; i < WIN_SIZE; i++){ //For
162
       each substring
             Pull_Substrings_B: for (int j = 0; j < WIN_SIZE; j++) \{ //
163
       For each character in substring
               substring_ints[i]((j*8)+7,j*8) = curr_window[i+j]; //
164
       Pull substrings from current window
            }
165
          }
166
167
          bank_accessed_bits = 0; //Reset bank access flag bits
168
          substring_access_bits = 0; //Reset substring access flag
169
       bits
          //Allocate bank access to substrings
170
          bank_access_func(hash, substring_ints, data_pos,
171
       bank_accessed_bits, substring_access_bits, associated_bank,
       string_to_write , string_address);
172
          Read_Matches_A: for (int i = 0; i < NUMBANKS; i++){//For
173
       each bank
            Read_Matches_B: for (int j = 0; j < BANK_DEPTH; j++){//For}
174
       each depth level
               if (bank_accessed_bits [i] == 1) \{ //If accessed by
175
       substring
                 potential_match[i][j].string = dictionary[i][j][
176
       string_address[i]].string; //Read potential match string
```

177	<pre>potential_match[i][j].position = dictionary[i][j][</pre>
170	string_address[i]].position; //Read potential match position
178 179	}
180	}
181	, ,
182	Write_Substrings_A: for (int $i = 0$; $i < NUMBANKS$; $i++){//For}$
	each bank
183	if (bank_accessed_bits [i] == 1) { // If accessed by substring
184	<pre>dictionary[i][0][string_address[i]].string = string_to_write[i].string; //Write substring to depth 0</pre>
185	dictionary [i][0][string_address [i]]. position =
	string_to_write [i]. position; //Write position to depth 0
186	Write_Substrings_B: for (int $j = 1; j < BANK_DEPTH; j++)$ {
	//For each depth level below depth 0
187	dictionary [i] [j] [string_address [i]]. string =
	<pre>potential_match[i][j-1].string; //Write substring from depth above</pre>
188	above dictionary[i][j][string_address[i]].position =
100	potential_match $[i][j-1]$. position; //Write position from depth
	above
189	}
190	}
191	}
192	Match_Compare_A: for (int $i = 0$; $i < NUM_BANKS$; $i++){//For}$
193	each bank $1 = 0, 1 < \text{NONLDAWAS}, 1++){//101}$
194	Match_Compare_B: for (int $j = 0$; $j < BANK_DEPTH$; $j++){//For}$
	each depth level
195	Match_Compare_C: for (int $k = 0$; $k < WIN_SIZE$; $k++){//For}$
	each character
196	$match_length_bits[i][j][k] = (string_to_write[i]).$ string((k*8)+7,k*8) = potential_match[i][j].string((k*8)+7,k
	$((k*0)+7, k*0) = potential_match[1][J]. string((k*0)+7, k *8)) ? 1 : 0; //Compare strings$
197	}
198	}
199	
200	}
201	Match Longth A. for (int i = 0, i < NIMDANIZO, i) $(/D)$
202	Match_Length_A: for (int $i = 0$; $i < NUM_BANKS$; $i++$){ //For each bank
203	Match_Length_B: for (int $j = 0$; $j < BANK_DEPTH$; $j++$){ //For
	each depth level
204	$match_length[i][j] = _builtin_ctz((0b1,~))$
	<pre>match_length_bits[i][j])); //Calculate integer length</pre>
205	}
206	}
207 208	Reset_Best: for (int $i = 0$; $i < NUM_BANKS$; $i++$){ //For each
	bank
209	$bank_best_length[i] = 0; //Reset best match lengths from$
	last iteration
210	}
211	

```
Best_Match_A: for (int i = 0; i < NUMBANKS; i++){ //For each
212
       bank
           Best_Match_B: for (int j = 0; j < BANK_DEPTH; j++){ //For
213
      each depth level
              if (match_length [i] [j] > bank_best_length [i]) { //Compare
214
      matches to find best length
                bank_best_length[i] = match_length[i][j];
215
                bank_best_match[i] = j;
216
             }
217
           }
218
         }
219
220
         Best_Match_MUX: for (int i = 0; i < NUM_BANKS; i++) { //For
221
      each bank
            bank_best_position [i] = reg(potential_match[i]]
222
      bank_best_match[i]].position); //Pass position of best match
         }
223
224
         Bank_to_String_MUX: for (int i = 0; i < WIN_SIZE; i++){//For
      each window substring
            if (substring_access_bits [i] = 1) { // If substring was
226
      granted bank access
              window_best_length[i] = bank_best_length[associated_bank]
227
      [i]]; //Obtain best match length and position from associated
      bank
              window_best_position[i] = bank_best_position[
228
      associated_bank[i]];
           }
229
            else { // Otherwise, set match length to 0
230
              window_best_length [i] = 0;
231
              window_best_position [i] = 0;
232
           }
233
         }
234
235
         Calc_Valid: for (int i = 0; i < WIN_SIZE; i++) { //For each
236
      best match
            valid_matches_bits[i] = (window_best_length[i] == 0) ? 0 :
237
       1; //If the match length is not 0, the match is valid
         }
238
239
         Calc_Offset: for (int i = 0; i < WIN_SIZE; i++){ //For each
240
      substring
            offsets [i] = data_pos + i - window_best_position [i];
241
            if (offsets [i] > MAX_DISTANCE) { // Filter matches that are
242
      too far back
              valid_matches_bits [i] = 0;
243
           }
244
         }
245
246
         Filter_A: for (int i = 0; i < WIN_SIZE; i++){ //For each best
247
       match
            if (window_best_length [i] < MINLENGTH) // Filter matches
248
      with length less than 3
              valid_matches_bits [i] = 0;
249
```

```
}
250
251
         //Filter B
252
         valid_matches_bits &= ((ap_uint<WIN_SIZE>)0xFFFF <<
253
      first_valid_pos); //Filter matches covered by previous
      iteration by clearing bits up to FVP
254
         last_match = (valid_matches_bits != 0) ? (31 - __builtin_clz
255
      (valid_matches_bits)) : 0; //Calculate last match. If no valid
       matches, set to 0
256
         //Set matched_literals based on first valid position before
257
      updating it
         matched_literals_bits = decoder [first_valid_pos](0, WIN_SIZE
258
      -1);
259
         Calc_Reach: for (int i = 0; i < WIN_SIZE; i++){ //For each
260
      best match
           reach[i] = i + window_best_length[i]; //Calculate reach of
261
       all matches
         }
262
263
         //Calculate first valid position of next iteration using the
264
       reach of the last match
         //If reach of last match is greater than 16, calculate FVP.
265
      Otherwise FVP is 0.
         first_valid_pos = (reach [last_match] [MATCH_SIZE_BITS-1] ==
266
      1) ? reach [last_match] (MATCH_SIZE_BITS-2,0) : 0;
267
         //Filter matches with same reach but lower length than
268
      others
         Filter_C1: for (int i = 0; i < WIN_SIZE; i++){ //For each
269
      match
           if (valid_matches_bits [i] != 0) { // If match is still valid
270
             Filter_C2: for (int j = i+1; j < WIN_SIZE; j++){ //
271
      Compare to all valid matches 'below' this match
                if (reach[i] = reach[j]) \{ // If matches have same reach
272
      , match below has lower length
                  if(j = last_match) \{ //If last match is being
273
      filtered for a longer match
                    valid_matches_bits (WIN_SIZE-1, i+1) = 0; //Filter
274
      all matches below match i
275
                  }
                  else{
276
                    valid_matches_bits[j] = 0; //Filter match below
277
                  }
278
               }
279
             }
280
           }
281
         }
282
283
         //Filter or trim matches that conflict with later matches (
284
      last match must be kept)
```

Filter_D1: for (int i = WIN_SIZE-1; i >= 0; i--) $\{//For each$ 285 match (starting from the bottom) if (valid_matches_bits [i] != 0) { // If match is still valid 286 Filter_D2: for(int j = 0; j < i; j++){ //Compare to all 287 valid matches 'above' this match $if(reach[j] > i) \{ //If above matches conflict with$ 288 this match bytes_conflicting = reach[j] - i; //Calculate number 289 of conflicting bytes if (window_best_length $[j] - bytes_conflicting >=$ 290 MIN_LENGTH) { // If match j can safely be trimmed (without decreasing length below 3) window_best_length[j] -= bytes_conflicting; //Trim 291 match j } 292else{ 293 valid_matches_bits[j] = 0; //Filter match j 294 } 295} 296 } 297 } 298 } 299 300 //Preparing output sequence 301 Prepare_OutputA: for (int i = 0; i < WIN_SIZE; i++){ //For302 each box in window output_array[i].user = (valid_matches_bits[i] != 0) ? 0b10 303 : 0b01; //If box contains a valid match, set user flag to match. 304 Otherwise set to unmatched literal } 305 306 Prepare_OutputB: for (int i = 0; i < WIN_SIZE; i++) { //For307 each box in window if (valid_matches_bits [i] != 0) { // If match is valid 308 matched_literals_bits |= (((ap_uint<WIN_SIZE>)decoder[309 window_best_length [i] >> 1) << (WIN_SIZE - window_best_length [i] - i);} //Turn match length into bit-string and OR all together 310 to find matched literals } 311 312 Prepare_OutputC: for (int i = 0; i < WIN_SIZE; i++){ //For 313 each box in window (each bit in window_matches) if $(matched_literals_bits [WIN_SIZE-1-i] = 1) \{ //If the box$ 314 contains a matched literal $output_array[i]$. user = 0b00; 315 } //Set user flag to 0 for all matched literals 316 } 317 318 Prepare_OutputD: for (int i = 0; $i < WIN_SIZE$; i++){ 319 switch(output_array[i].user){ //Based on status of output 320 box, fill data accordingly case 0b00 : //Matched Literal 321
$output_array[i]$. data = 0; //Clear box (Only useful for 322 debugging) break; 323 324 case 0b01 : //Unmatched Literal 325 output_array[i].data = curr_window[i]; //Write literal 326 break; 327 328 case 0b10 : //Match 329 assert (window_best_length [i] >= MINLENGTH); // 330 Assertions for C debugging assert (window_best_length [i] <= WIN_SIZE); 331 assert (offsets $[i] \ge 1$); 332 assert (offsets [i] <= MAX_DISTANCE); 333 334 output_array[i].data(23, 15) = window_best_length[i]; // 335 Write Length in upper 9 bits $output_array[i]$. data(14, 0) = offsets[i] - 1; //Write 336 Distance in lower 15 bits break; 337 } 338 } 339 340 Prepare_OutputE: for (int i = 0; i < WIN_SIZE; i++) { //341 Convert from array to int (Little Endian) $output_buff.data((i*24)+23,i*24) = output_array[i].data;$ $output_buff.user((i*2)+1, i*2) = output_array[i].user;$ 343 } 344 345 //Write to output stream 346 strm_out << output_buff;</pre> 347 348 data_pos += WIN_SIZE; //Increment data marker 349 } //For-num_iterations-loop 350 } 351 352 Last_Shift: for (int i = 0; i < WIN_SIZE; i++) { //Shift second 353 half of window into front half of window #pragma HLS UNROLL 354 $\operatorname{curr}_{\operatorname{window}}[i] = \operatorname{curr}_{\operatorname{window}}[i + \operatorname{WIN}_{\operatorname{SIZE}}];$ 355 356 357 //Calculate matched_literals one last time 358 matched_literals_bits = decoder [first_valid_pos](0, WIN_SIZE-1); 359 matched_literals_bits |= ~(((ap_uint<WIN_SIZE>)input_buff.keep 360 (0,WIN_SIZE-1))); //OR with TKEEP to identify null bytes at end of input stream 361 Last_OutputA: for (int i = 0; i < WIN_SIZE; i++) { //For each box 362 in window (each bit in window_matches) 363 #pragma HLS UNROLL output_array[i].user = (matched_literals_bits[WIN_SIZE-1-i] == 364 1) ? 0b00 : 0b01;

```
} //If the box contains a matched literal or null byte, set to 0
365
      b00
366
     Last_OutputB: for (int i = 0; i < WIN_SIZE; i++){
367
  #pragma HLS UNROLL
368
       switch(output_array[i].user){ //Based on status of output box,
369
       fill data accordingly
       case 0\,b00 : //Matched Literal/Null Character
370
         output_array[i].data = 0; //Clear box (Only useful for
371
      debugging)
         break;
372
373
       case 0b01 : //Unmatched Literal
374
         output_array[i].data = curr_window[i]; //Write literal
375
         break;
376
377
       }
     }
378
379
    Last_OutputC: for (int i = 0; i < WIN_SIZE; i++){ //Convert from
380
      array to int (Little Endian)
  #pragma HLS UNROLL
381
       output_buff.data((i*24)+23,i*24) = output_array[i].data;
382
       output\_buff.user((i*2)+1, i*2) = output\_array[i].user;
383
     }
384
     output\_buff.last = 1;
385
     strm_out << output_buff;</pre>
386
387
  ł
```

Appendix B LZ77 Encoder Header File

LZ77_Encoder.h

1	#include <stdio.h></stdio.h>
2	#include <string.h></string.h>
3	#include <ap_int.h></ap_int.h>
4	#include <hls_stream.h></hls_stream.h>
5	#include <assert.h></assert.h>
6	
7	using namespace hls;
8	
9	#define WIN_SIZE 16 //Compare window size.
	Sliding window is twice this
10	#define NUM_BANKS 32 //Number of dictionary banks
11	#define BANK_DEPTH 3 //Depth of each dictionary
	bank
12	$#define BANK_INDEXES (512*NUM_BANKS) //16384 //Total number of$
	hash bank indexes
13	#define BANK_SIZE (BANK_INDEXES/NUM_BANKS) //Number of indexes in
	each bank
14	#define MINLENGTH 3 //Minimum Deflate match
	length
15	#define MAX_DISTANCE 32768 //Maximum Deflate match
	distance
16	
	//Dynamic bit width definitions (Only work in C sim)
	#ifndefSYNTHESIS
19	$#define WIN_SIZE_BITS (int)(log2(WIN_SIZE-1)+1) //Number of$
	bits required to store WIN_SIZE values
20	#define BANK_DEPTH_BITS (int)(log2(BANK_DEPTH-1)+1) //Number of
	bits required to store BANK DEPTH values
21	#define MATCH_SIZE_BITS (int)(log2(WIN_SIZE)+1) //Number of
	bits required to store maximum match length (WIN_SIZE)
22	#define HASH_BITS $(int)(log2(BANK_INDEXES-1)+1) //Number of$
	hash bits required to index BANK_INDEXES (Complete hash
	function) $\frac{1}{2} define NUM DANKE DEE (int) (leg 2 (NUM DANKE 1) + 1) (Number of$
23	#define NUM_BANKS_BITS (int)(log2(NUM_BANKS-1)+1) //Number of
	bits required to index NUM_BANKS values (Top bits of hash function)
	function)

```
<sup>24</sup> #define BANK_SIZE_BITS (int)(log2(BANK_SIZE-1)+1)
                                                         //Number of
     bits required to index BANK_SIZE values (Bottom bits of hash
     function)
_{25} #else
<sup>26</sup> #define WIN_SIZE_BITS
                           4
27 #define BANK_DEPTH_BITS 2
_{28} #define MATCH_SIZE_BITS 5
29 #define HASH_BITS
                           14
30 #define NUM_BANKS_BITS
                           5
31 #define BANK_SIZE_BITS
                          - 9
32 #endif
33
34 typedef ap_uint<WIN_SIZE_BITS> t_win_size;
35 typedef ap_uint<BANK_DEPTH_BITS> t_bank_depth;
36 typedef ap_uint<MATCH_SIZE_BITS> t_match_size;
37 typedef ap_uint <HASH_BITS> t_hash_size;
38 typedef ap_uint <NUM_BANKS_BITS> t_num_banks;
39 typedef ap_uint <NUM_BANKS_BITS+1> t_bank_values; //1 extra bit to
     include the value NUMBANKS
40 typedef ap_uint<BANK_SIZE_BITS> t_bank_size;
41
  typedef struct { //Input AXI-Stream structure
42
    ap_uint<WIN_SIZE*8> data; //Array of window characters (128 bits
43
      with 16 bytes)
    ap_uint<WIN_SIZE>
                         keep; //TKEEP Signals for each byte
44
    bool last;
45
  } in_strm;
46
47
  typedef struct{ //Output Array structure
48
    ap_uint<24> data; //3-byte box for one of the window characters
49
     from LZ77 encoder
    ap_uint<2> user; //2-bit flag for identifying a box as a
50
     literal, length, distance, or matched literal
 } out_array;
51
53 typedef struct { // Output AXI-Stream structure
    ap_uint <3*WIN_SIZE*8> data; //3-byte 'boxes' for each of the
54
     window characters from LZ77 encoder
    ap\_uint < 2*WIN\_SIZE> user; //2-bit flags for identifying each box
      as a literal, length, distance, or matched literal
    bool last;
                         //AXI-Stream TLAST signal
56
57 } out_strm;
58
59 typedef struct { //Match Structure
    ap_uint<WIN_SIZE*8> string;
                                   //16-byte string, int form
60
                    position; //Position of string in history
61
    ap_int < 32 >
62 } match_t;
63
  //16- bit decoder. Given an integer index n, returns a bit string
64
     containing n ones.
_{65} const ap_uint <16> decoder [17] = {
      66
      67
      /* 2*/ 0b00000000000011,
68
```

69	/* 3*/ 0b00000000000111,
70	$/* \ 4*/ \ 0b000000000001111 \ ,$
71	/* 5*/ 0b00000000011111 ,
72	/* 6*/ 0b00000000111111 ,
73	$/* \ 7*/ \ 0b000000011111111 \ ,$
74	/* 8*/ 0b000000111111111,
75	/* 9*/ 0b000000111111111 ,
76	/*10*/ 0b000001111111111 ,
77	/*11*/ 0b0000011111111111 ,
78	/*12*/ 0b0000111111111111 ,
79	/*13*/ 0b000111111111111111,
80	/*14*/ 0b001111111111111111,
81	/*15*/ 0b0111111111111111111,
82	/*16*/ 0b1111111111111111
83]};

Appendix C Huffman Encoder Source File

```
Huffman_Encoder.cpp
```

```
1 #include "Huffman_Encoder.h"
<sup>2</sup> #include "code_tables.cpp"
  void symbol_encoder(
                                    //Input (3 bytes)
       ap\_uint < 24 >
                     data,
       ap\_uint < 2>
                                  //Input
                     type,
                                  //Output (Can be from 0 to 26 bits
       ap_uint < 26 >
                     &code,
7
      long)
                     &code_length //Output
       ap_uint < 5>
8
  ) {
9
  #pragma HLS INLINE
    ap_uint <9>
                    length;
12
    ap_uint < 15>
                    distance;
                    length_code;
    ap_uint < 8 >
13
    distance_code distance_symbol;
14
    ap_uint <13>
                    extra_distance_value;
16
    switch(type){
17
    case 0b00 : //Matched literal
18
       code = 0;
19
       code_length = 0;
20
       break;
21
22
    case 0b01 : //Unmatched Literal
23
       assert(data \ge 0);
24
       assert (data \leq 255);
25
       if(data <= 143){
26
         code_length = 8;
27
         data = data + 48; //Convert literal value to code
28
         code = data(0,7); //Mirror code and output it
29
       }
30
       else{
31
         code_length = 9;
32
         data = data + 256; //Convert literal value to code
33
         code = data(0,8); //Mirror code and output it
34
       }
35
       break;
36
```

```
37
    case 0b10 : //Match
38
      length = data(23, 15);
39
      distance = data(14,0);
40
      assert (length \geq 3); //Assertions for C debugging
41
      assert (length \leq 16);
42
43
      assert(distance \geq 0); //Distance is subtracted by 1 to fit
     within 15 bits (Done by LZ77 Encoder)
      assert (distance \leq 32767);
44
45
      //Length Encoding
46
47
      if (length \leq 10) \{ // If length is 10 or less, no extra bits in
     code length
        code_length = 7;
48
      }
49
      else{
        code_length = 8; //7-bit length code + 1 extra bit
      length -= 3; //Adjust length before looking up in table
53
      length_code = length_code_table[length]; //Length codes are
54
     pre-mirrored with extra bits included
      //Distance Encoding
56
      if (distance < 256) { // Distance is from 1 to 256
        distance_symbol = distance_code_table[distance];
58
      }
      else { // Distance is from 257 to 32768
60
        distance_symbol = distance_code_table [distance(14,7) + 256];
61
       //Top 8 bits of distance + 256
62
      extra_distance_value = distance - distance_symbol.base;
63
64
      //Concatenate codes as follows: extra distance bits, distance
65
     code (mirrored), length code (already mirrored)
      code = (extra_distance_value, distance_symbol.code(0,4),
66
     length_code(code_length-1,0));
      code_length += 5 + distance_symbol.bits; //Add distance bits
67
     to code length
      break;
68
    }
69
  }
70
71
72 template <int instance>
  void window_packer(
73
      in_stream
                  *input_window_in , //Input: Window of 3-byte boxes
74
     to be encoded
                                        //Output
      in_stream
                  *input_window_out,
75
                                        //Input: Window for packing
                  *encoded_window_in ,
      t_enc_win
76
     Huffman codes
      ap_uint <8> *encoded_bits_in, //Input: Number of bits in
77
     encoded window
      t_enc_win *encoded_window_out, //Output
78
      ap_uint <8> *encoded_bits_out //Output
79
80)
```

```
81 #pragma HLS INLINE
82
                             //Huffman code to be packed
     ap\_uint < 26 > code;
83
     ap_uint <5>
                 code_length; //Length of Huffman code
84
                 shifted_code;
     t_enc_win
85
86
     //Input window is Little Endian, process lower end first
87
     ap_uint <24> input_box = input_window_in->data((instance*24)+23,
88
      instance *24);
     ap\_uint < 2> input_type = input_window_in->user((instance*2) +1,
89
       instance * 2);
90
     symbol_encoder(input_box, input_type, code, code_length); //
91
      Encode box from input window
92
     *encoded_window_out = *encoded_window_in | (t_enc_win(code) << *</pre>
93
      encoded_bits_in); //Pack code in window
     *encoded_bits_out = *encoded_bits_in + code_length; //Update
94
      bit count of window
     assert(*encoded_bits_out \leq ENC_WIN_BITS); //C Debug: Check for
95
      encoded window overfill
96
                                             //Pass input window to
     *input_window_out = *input_window_in;
97
       output
  }
98
99
  void output_packer(
100
       t_enc_win
                            encoded_window_in, //Input: Window for
      packing Huffman codes
       ap_uint <8>
                            encoded_bits_in,
                                                //Input: Number of bits
102
       in encoded window
                                                   //In/Out
       ap_uint <OUT_WIN_BITS> &output_window,
103
                            &output_bits,
                                                 //In/Out
       ap_uint < 10>
104
       stream<out_stream>
                              &output_strm
                                                   //Output
105
  ) {
106
  #pragma HLS INLINE
107
     out_stream out_buff = \{0\};
108
109
     output_window |= ap_uint <OUT_WIN_BITS>(encoded_window_in) <<
      output_bits; //Pack encoded window in output packer
     output_bits += encoded_bits_in; //Update bit count of packer
     assert(output_bits <= OUT_WIN_BITS); //C Debug: Check for output
       window overfill
113
     if (output_bits \geq OUT_STRM_BITS) { // If packer is more than half
114
      full
       out_buff.data = output_window (OUT_STRM_BITS-1,0); //Write out
115
      bottom half of output packer
       out_buff.keep = 0xFFFFFFF; //Set all TKEEP bits high
       out_buff.last = 0;
117
       output_strm << out_buff;
118
       output_window >>= OUT_STRM_BITS; // Shift out bottom half of
119
      output packer
       output_bits -= OUT_STRM_BITS; //Update bit count of packer
120
```

```
121
     }
122
  }
123
   //Pipelined Huffman encoder for encoding all symbols of a window
124
      in parallel
   void huffman_encoder(
126
       stream < in_stream >
                           &strm_in,
       stream<out_stream> &strm_out
  ) {
128
  #pragma HLS INTERFACE axis off port=strm_out
129
  #pragma HLS INTERFACE axis off port=strm_in
130
131
     in_stream input_window0;
     in_stream input_window1;
     in_stream input_window2;
133
     in_stream input_window3;
134
     in_stream input_window4;
135
136
     in_stream input_window5;
     in_stream input_window6;
137
     in_stream input_window7;
138
     in_stream input_window8;
139
     in_stream input_window9;
140
141
     in_stream input_window10;
     in_stream input_window11;
142
     in_stream input_window12;
143
     in_stream input_window13;
144
     in_stream input_window14;
145
     in_stream input_window15;
146
     in_stream input_window16;
147
     t_enc_win encoded_window0;
148
     t_enc_win encoded_window1;
149
     t_enc_win encoded_window2;
150
     t_enc_win encoded_window3;
151
     t_enc_win encoded_window4;
     t_enc_win encoded_window5:
153
     t_enc_win encoded_window6;
154
     t_enc_win encoded_window7;
155
     t_enc_win encoded_window8;
156
     t_enc_win encoded_window9;
     t_enc_win encoded_window10;
158
     t_enc_win encoded_window11;
     t_enc_win encoded_window12;
160
     t_enc_win encoded_window13;
161
     t_enc_win encoded_window14;
162
     t_enc_win encoded_window15;
163
     t_enc_win encoded_window16;
164
     ap_uint <8> encoded_bits0;
165
166
     ap_uint <8> encoded_bits1;
     ap_uint <8> encoded_bits2;
167
     ap_uint <8> encoded_bits3;
168
     ap_uint <8> encoded_bits4;
169
     ap_uint <8> encoded_bits5;
170
171
     ap_uint <8> encoded_bits6;
     ap_uint <8> encoded_bits7;
172
173
     ap_uint <8> encoded_bits8;
```

```
ap_uint <8> encoded_bits9;
174
175
     ap_uint <8> encoded_bits10;
     ap_uint <8> encoded_bits11;
176
     ap_uint <8> encoded_bits12;
177
     ap_uint <8> encoded_bits13;
178
     ap_uint <8> encoded_bits14;
179
180
     ap_uint <8> encoded_bits15;
     ap_uint <8> encoded_bits16;
181
182
     //Initialize output_window
183
     ap_uint <OUT_WIN_BITS> output_window = 0b011; //Output buffer for
184
       packing encoded windows
     ap\_uint < 10 > output\_bits = 3; //Number of bits currently in
185
      output_packer
     out_stream out_buff = \{0\};
186
187
188
     do{
  #pragma HLS PIPELINE
189
       encoded_window0 = 0; //Clear encoded window before packing
190
       encoded_bits0 = 0;
192
       strm_in \gg input_window0; //Read an input window from the
193
      input stream
194
       window_packer<0>(&input_window0, &input_window1, &
195
      encoded_window0, & encoded_bits0, & encoded_window1, &
      encoded_bits1);
       window_packer <1>(&input_window1, &input_window2, &
196
      encoded_window1, & encoded_bits1, & encoded_window2, &
      encoded_bits2);
       window_packer <2>(&input_window2, &input_window3, &
197
      encoded_window2, & encoded_bits2, & encoded_window3, &
      encoded_bits3);
       window_packer <3>(&input_window3, &input_window4, &
198
      encoded_window3, & encoded_bits3, & encoded_window4, &
      encoded_bits4);
       window_packer <4>(&input_window4, &input_window5, &
199
      encoded_window4, & encoded_bits4, & encoded_window5, &
      encoded_bits5);
       window_packer <5>(&input_window5, &input_window6, &
200
      encoded_window5, & encoded_bits5, & encoded_window6, &
      encoded_bits6);
       window_packer <6>(&input_window6, &input_window7, &
201
      encoded_window6, & encoded_bits6, & encoded_window7, &
      encoded_bits7);
       window_packer <7>(&input_window7, &input_window8, &
202
      encoded_window7, & encoded_bits7, & encoded_window8, &
      encoded_bits8);
       window_packer <8>(&input_window8, &input_window9, &
203
      encoded_window8, & encoded_bits8, & encoded_window9, &
      encoded_bits9);
       window_packer <9>(&input_window9, &input_window10, &
204
      encoded_window9, & encoded_bits9, & encoded_window10, &
      encoded_bits10);
```

```
window_packer <10>(&input_window10, &input_window11, &
205
      encoded_window10, & encoded_bits10, & encoded_window11, &
      encoded_bits11);
       window_packer <11>(&input_window11, &input_window12, &
206
      encoded_window11, & encoded_bits11, & encoded_window12, &
      encoded_bits12);
207
       window_packer <12>(&input_window12, &input_window13, &
      encoded_window12, & encoded_bits12, & encoded_window13, &
      encoded_bits13);
       window_packer <13>(&input_window13, &input_window14, &
208
      encoded_window13, & encoded_bits13, & encoded_window14, &
      encoded_bits14);
       window_packer <14>(&input_window14, &input_window15, &
209
      encoded_window14, & encoded_bits14, & encoded_window15, &
      encoded_bits15);
       window_packer <15>(&input_window15, &input_window16, &
210
      encoded_window15, & encoded_bits15, & encoded_window16, &
      encoded_bits16);
       output_packer(encoded_window16, encoded_bits16, output_window,
212
       output_bits, strm_out);
213
     } while (!input_window0.last);
214
     output_bits += 7; //Add EOB code to end of stream (7 zeroes)
215
216
     if (output_bits >= OUT_STRM_BITS) { // If packer is more than half
217
      full, perform two final writes to stream
       out_buff.data = output_window(OUT_STRM_BITS-1,0); //Write out
218
      bottom half of output packer
       out_buff.keep = 0xFFFFFFF; //Set all TKEEP bits high
219
       strm_out << out_buff;</pre>
220
       output_window >>= OUT_STRM_BITS; //Shift out bottom half of
221
      output packer
       output_bits -= OUT_STRM_BITS; //Update bit count of packer
222
       out_buff.data = output_window(OUT_STRM_BITS-1,0); //Write out
223
      remaining data in output packer
       out_buff.keep = decoder32[(output_bits+7)/8]; //Set TKEEP
224
      using decoder. Number of bytes rounded up
       out_buff.last = true;
225
       strm_out << out_buff;</pre>
226
227
     else { // Otherwise, just one final write to stream
228
       out_buff.data = output_window(OUT_STRM_BITS-1,0); //Write out
229
      remaining data in output packer
       out_buff.keep = decoder 32 [(output_bits+7)/8]; //Set TKEEP
230
      using decoder. Number of bytes rounded up
       out_buff.last = true;
231
       strm_out << out_buff;</pre>
232
233
  ł
234
```

Appendix D Huffman Encoder Header File

Huffman_Encoder.h

```
1 #include <stdio.h>
2 #include <string.h>
3 #include <ap_int.h>
4 #include <hls_stream.h>
 #include <assert.h>
  using namespace hls;
<sup>9</sup> #define WINDOW_SIZE
                         16 //Number of boxes in input window
10 #define WINDOW_BITS
                         WINDOW_SIZE*8
_{11} #define ENC_WIN_BITS (WINDOW_SIZE-1)*9 + 26 //Bit width of
     encoded window. Longest possible enc_win is 15 9-bit literals
     and 1 26-bit LD pair = 161 bits.
12 #define OUT_STRM_BITS 2*WINDOW_BITS //Output stream bit width,
     must be power of 2 and larger than encoded window width
13 #define OUT_WIN_BITS 2*OUT_STRM_BITS //Bit width of output window
      packer, must be double that of output stream width
14
15 typedef ap_uint <ENC_WIN_BITS> t_enc_win;
16
17 typedef struct { //Input AXI-Stream structure
    ap_uint <3*WINDOW_BITS> data; //3-byte DATA 'boxes' for each of
18
     the window characters from LZ77 encoder
    ap_uint <2*WINDOW_SIZE> user; //2-bit TUSER flags for
19
     identifying each box as a literal, length, distance, or
     matched literal
    bool last:
                           //TLAST signal
20
21 } in_stream;
22
23 typedef struct { // Output AXI-Stream structure
    ap_uint <OUT_STRM_BITS>
                             data; //Compressed data output
24
    ap_uint <OUT_STRM_BITS/8> keep; //TKEEP signal for each byte of
25
     data
    bool last;
                            //TLAST signal
26
27 } out_stream;
28
29 typedef struct { // Distance code table structure
```

30	ap_uint <5> code;
31	$ap_uint < 15>$ base;
32	ap_uint <4> bits;
33	} distance_code;
34	
35	//32-bit decoder. Given an integer index n, returns a bit string
	containing n ones.
36	const ap_uint $\langle 32 \rangle$ decoder $32[33] = \{$
37	/* 0*/ 0b0000000000000000000000000000000
38	/* 1*/ 0b00000000000000000000000000000000000
39	$/* \ 2*/ \ 0b0000000000000000000000000000000000$
40	$/* \ 3*/ \ 0b0000000000000000000000000000000000$
41	$/* \ 4*/ \ 0b0000000000000000000000000000000000$
42	/* 5*/ 0b00000000000000000000000000000000000
43	/* 6*/ 0b00000000000000000000000000000000000
44	$/* \ 7*/ \ 0b0000000000000000000000000000000000$
45	/* 8*/ 0b00000000000000000000000000000000000
46	/* 9*/ 0b00000000000000000000000000000000000
47	/*10*/ 0b000000000000000000001111111111,
48	/*11*/ 0b000000000000000000000111111111111,
49	/*12*/ 0b000000000000000000001111111111111111
50	/*13*/ 0b000000000000000000001111111111111111
51	/*14*/ 0b000000000000000111111111111111111111
52	/*15*/ 0b000000000000000011111111111111111111
53	/*16*/ 0b000000000000001111111111111111111111
54	/*17*/ 0b000000000000001111111111111111111111
55	/*18*/ 0b000000000000111111111111111111111111
56	/*19*/ 0b000000000001111111111111111111111111
57	/*20*/ 0b000000000001111111111111111111111111
58	/*21*/ 0b000000000011111111111111111111111111
59	/*22*/ 0b00000000011111111111111111111111, /*23*/ 0b0000000011111111111111111111111,
60	/*23*/ 0b000000001111111111111111111111111111
61	/*25*/ 0b000000011111111111111111111111111111
62 63	/*26*/ 0b000000111111111111111111111111111111
64	/*27*/ 0b000001111111111111111111111111111111
65	/*28*/ 0b000011111111111111111111111111111111
66	/*29*/ 0b000011111111111111111111111111111111
67	/*30*/ 0b000111111111111111111111111111111111
68	/*31*/ 0b011111111111111111111111111111111111
69	/*32*/ 0b11111111111111111111111111111111111
70	};
1	

Appendix E Code Tables File

 $code_tables.cpp$

	codectables.epp
1	//Length Codes (and Code Lengths) for all possible Length Values.
2	//Pre-mirrored with extra bits added
3	$const ap_uint < 8> length_code_table[14] = {$
4	/*Length 3*/ $0b1000000$, /*7*/ //7-bit length codes with no
	extra bits
5	/*Length 4*/ 0b0100000, /*7*/
6	/*Length 5*/ 0b1100000, /*7*/
7	/*Length 6*/ 0b0010000, /*7*/
8	/*Length 7*/ 0b1010000, /*7*/
9	/*Length 8*/ 0b0110000, /*7*/
10	/*Length 9*/ 0b1110000, /*7*/
11	/*Length 10*/ 0b0001000, /*7*/
12	/*Length 11*/ $0b01001000$, /*8*/ //7-bit length codes with 1
	extra bit
13	/*Length 12*/ 0b11001000, /*8*/
14	/*Length 13*/ 0b00101000, /*8*/
15	/*Length 14*/ 0b10101000, /*8*/
16	/*Length 15*/ 0b01101000, /*8*/
17	/*Length 16*/ 0b11101000 /*8*/
18	};
19	
20	//Table for looking up the {Distance Symbol/Code, Base Value, and
	Extra Bits} of a Distance Value
21	//Since input distance is 1 less than the actual distance, the
	base values are pre-decremented by 1 as well
22	//This way the difference between the two is correct when
	calculating: extra_value = distance - base_value
23	
24	$\{0, 0, 0\}, \{1, 1, 0\}, \{2, 2, 0\}, \{3, 3, 0\}, \{4, 4, 1\},$
	$\{4, 4, 1\}, \{5, 6, 1\}, \{5, 6, 1\}, $
25	$\{6, 8, 2\}, \{6, 8, 2\}, \{6, 8, 2\}, \{6, 8, 2\}, \{6, 8, 2\}, \{7, 12, 2\},$
	$\{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, 12, 2\}, \{7, $
26	$\{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, $
į	$\{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{8, 16, 3\}, \{16, 16, 3\}, \{16, 16, 3\}, \{16, 16, 3\}, \{16, 16, 16\}, \{16, 16, 16$
27	$\{9, 24, 3\}, \{9, 24, 3\}, \{9, 24, 3\}, \{9, 24, 3\}, \{9, 24, 3\}, \{9, 24, 3\}, $
	$\{9, 24, 3\}, \{9, 24, 3\}, \{9, 24, 3\}, \{9, 24, 3\},$

28	$\{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32,$
20	$\{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10$
29	$\{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10, 32, 4\}, \{10$
30	$\begin{array}{cccccccccccccccccccccccccccccccccccc$
	$\{4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\},$
31	$\{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11, 48, 4\}, \{11$
32	$\{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12$
	5 , {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5}, {13, 64, 5},
33	$\{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12$
34	$\{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{12, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13, 64, 5\}, \{13$
35	5 , {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5}, {12, 64, 5},
	$5\}, \ \{12,\ 64,\ 5\}, \ \{12,\ 64,\ 5\}, \ \{12,\ 64,\ 5\},$
36	$\{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13$
37	$\{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 5\}, \ \{13, \ 96, \ 16\}, \ 16\}, \ 16\}, \ 16\}, \ 16\}, \ 16\}, \ 16\}, \ 16\}, \ 16\}, \ 16\}, \ 16\}, \ 16\}, \ 16\}, \ 16\}, \ 16\}, \ 16\}, \ 16\}, \ 16\}, \ 16\}, \ 16\}, \ 16\}, \ 16\}, \ 16\}, \ 16\}, \ 16\}, \ 16\}, \ 16\}, \ 16\}, \ 16\}, \ 16\}, \ 16\}, \ 16\}, \ 16\}, \ 16\}, \ 16\}, \ 16\}, \ 16\}, \ 16\}, \ 16\}, \ 16\}, \ 16\}, \ 16\}, \ 16\}, \ 16\}, \ 16\}, \ 16\}, \ 16\}, \ 16\}, \ 16\}, \ 16\}, \ 16\}, \ 16\}, \ 16\}, \ 16\}, \ 16\}, \ 16\}, \ 16\}, $
38	5 , $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$, $\{13, 96, 5\}$,
	$5\},\;\{13,\;96,\;5\},\;\{13,\;96,\;5\},\;\{13,\;96,\;5\},$
39	$\{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, \{13, 96, 5\}, $
40	$\{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, $
	$128,\ 6\},\ \{14,\ 128,\ 6\},\ \{14,\ 128,\ 6\},\ \{14,\ 128,\ 6\},$
41	$\{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, $
42	$\{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14,$
43	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$
	$128,\ 6\},\ \{14,\ 128,\ 6\},\ \{14,\ 128,\ 6\},\ \{14,\ 128,\ 6\},$
44	$\{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, $
45	$\{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14,$
46	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$
40	$128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\},$
47	$\{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, \{14, 128, 6\}, $
48	$\{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, $
	$192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, $
49	$\{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, $
50	$\{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, $
51	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$
	$192,\ 6\},\ \{15,\ 192,\ 6\},\ \{15,\ 192,\ 6\},\ \{15,\ 192,\ 6\},$
52	$\{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, $
53	$\{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, $
54	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$
0.4	192, 6, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152, 0$, $152,$
	112

55	$\{15, \ 192, \ 6\}, \ \{15, \ 192, \ 6\}, \ \{15, \ 192, \ 6\}, \ \{15, \ 192, \ 6\}, \ \{15, \ 192, \ 6\}, \ \{15, \ 192, \ 6\}, \ \{15, \ 192, \ 6\}, \ \{15, \ 192, \ 6\}, \ \{15, \ 192, \ 6\}, \ \{15, \ 192, \ 6\}, \ \{15, \ 192, \ 6\}, \ \{15, \ 192, \ 6\}, \ \{15, \ 192, \ 6\}, \ \{15, \ 192, \ 6\}, \ \{15, \ 192, \ 6\}, \ \{15, \ 192, \ 6\}, \ \{15, \ 192, \ 6\}, \ \{15, \ 192, \ 6\}, \ \{15, \ 192, \ 6\}, \ \{15, \ 192, \ 6\}, \ \{15, \ 192, \ 6\}, \ \{15, \ 192, \ 6\}, \ \{15, \ 192, \ 6\}, \ \{15, \ 192, \ 6\}, \ \{15, \ 192, \ 6\}, \ \{15, \ 192, \ 6\}, \ \{15, \ 192, \ 6\}, \ \{15, \ 192, \ 6\}, \ \{15, \ 192, \ 6\}, \ \{15, \ 192, \ 6\}, \ \{15, \ 192, \ 6\}, \ \{15, \ 192, \ 6\}, \ \{15, \ 192, \ 6\}, \ \{15, \ 192, \ 6\}, \ \{15, \ 192, \ 6\}, \ \{15, \ 192, \ 6\}, \ \{15, \ 192, \ 6\}, \ \{15, \ 192, \ 6\}, \ \{15, \ 192, \ 6\}, \ \{15, \ 192, \ 6\}, \ \{15, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 192, \ 112, \ 112, $
	$192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, 192, 6\}, \{15, $
56	$\{0, 0, 0\}, \{0, 0, 0\}, \{16, 256, 7\}, \{17, 384, 7\}, \{18, 512, 9\}, \{18, 512, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 768, 9\}, \{10, 7$
57	$512, 8$, {18, 512, 8}, {19, 768, 8}, {19, 768, 8}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}, {20, 1024, 9}
57	$\{20, 1024, 5\}, \{20, 1024, 5\}, \{20, 1024, 5\}, \{20, 1024, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 1536, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21, 156, 9\}, \{21$
	$9\},$
58	$\{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 1$
	$\{10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 10\}, \{22, 2048, 20, 20, 20, 20, 20, 20, 20, 20, 20, 20$
	$2048, 10\},$
59	$\{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 1$
	$\{10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3072, 10\}, \{23, 3$
60	$egin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$
00	11 , $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24, 4096, 11\}$, $\{24,$
	4096, 11},
61	$\{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ 11\}, \ \{24, \ 4096, \ 11\}, \ 11\}, \ \{24, \ 4096, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}$
	$11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ \{24, \ 4096, \ 11\}, \ 11\}, \ \{24, \ 11\}, \ \{24, \ 11\}, \ \{24, \ 11\}, \ \{24, \ 11\}, \ \{24, \ 11\}, \ \{24, \ 11\}, \ \{24, \ 11\}, \ \{24, \ 11\}, \ 11\}, \ \{24, \ 11\}, \ 11\}, \ \{24, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}, \ 11\}$
	$4096, 11\},$
62	$\{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 1$
	$egin{array}{cccccccccccccccccccccccccccccccccccc$
63	$\{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 11\}, \{25, 6144, 1$
	11 , $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25, 6144, 11\}$, $\{25,$
	$6144,\ 11\},$
64	$\{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 1$
	$12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 81$
	$\{192, 12\}, \{126, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, \{26, 2102, 12\}, $
65	$\{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 1$
	$\{12\}, \{12\}, \{12\}, \{12\}, \{12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 0102, 12\}, \{120, 01$
66	$\{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192,$
	$12\},\ \{26,\ 8192,\ 12\},\ \{26,\ 8192,\ 12\},\ \{26,\ 8192,\ 12\},\ \{26,\ 8192,\ 12\},\ \{26,\ 8192,\ 12\},\ \{26,\ 8192,\ 12\},\ \{26,\ 8192,\ 12\},\ \{26,\ 8192,\ 12\},\ \{26,\ 8192,\ 12\},\ \{26,\ 8192,\ 12\},\ \{26,\ 8192,\ 12\},\ \{26,\ 8192,\ 12\},\ \{26,\ 8192,\ 12\},\ \{26,\ 8192,\ 12\},\ \{26,\ 8192,\ 12\},\ \{26,\ 8192,\ 12\},\ \{26,\ 8192,\ 12\},\ \{26,\ 8192,\ 12\},\ \{26,\ 8192,\ 12\},\ \{26,\ 8192,\ 12\},\ \{26,\ 8192,\ 12\},\ \{26,\ 8192,\ 12\},\ \{26,\ 8192,\ 12\},\ \{26,\ 8192,\ 12\},\ \{26,\ 8192,\ 12\},\ \{26,\ 8192,\ 12\},\ \{26,\ 8192,\ 12\},\ \{26,\ 8192,\ 12\},\ \{26,\ 8192,\ 12\},\ \{26,\ 8192,\ 12\},\ \{26,\ 8192,\ 12\},\ \{26,\ 8192,\ 12\},\ \{26,\ 8192,\ 12\},\ \{26,\ 8192,\ 12\},\ \{26,\ 8192,\ 12\},\ \{26,\ 8192,\ 12\},\ \{26,\ 8192,\ 12\},\ \{26,\ 8192,\ 12\},\ \{26,\ 8192,\ 12\},\ \{26,\ 8192,\ 12\},\ \{26,\ 8192,\ 12\},\ \{26,\ 8192,\ 12\},\ \{26,\ 8192,\ 12\},\ \{26,\ 8192,\ 12\},\ \{26,\ 8192,\ 12\},\ \{26,\ 8192,\ 12\},\ 12\},\ \{26,\ 8192,\ 12\},\ \{26,\ 8192,\ 12\},\ \{26,\ 8192,\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ 12\},\ $
	$8192, 12\},$
67	$\{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 12\}, \{26, 8192, 1$
	12 , {26, 8192, 12}, {26, 8192, 12}, {26, 8192, 12}, {26, 8192, 12}, {26, 8192, 12},
68	$\{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27,$
	12 , $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 12288, 12\}$, $\{27, 1228, 12\}$, $\{27, 1228, 12\}$, $\{27, 1228, 12\}$, $\{27, 1228, 12\}$, $\{27, 1228, 12\}$, $\{27, 1228, 12\}$, $\{27, 1228, 12\}$, $\{27, 1228, 12\}$, $\{27, 1228, 12\}$, $\{27, 1228, 12\}$, $\{27, 1228, 12\}$, $\{27, 1228, 12\}$, $\{27, 1228, 12\}$, $\{27, 1228, 12\}$, $\{27, 1228, 12\}$, $\{27, 1228, 12\}$, $\{27, 1228, 12\}$, $\{27, 1228, 12\}$, $\{27, 1228, 12\}$, $\{27, 1228, 12\}$, $\{27, 1228, 12\}$, $\{27, 1228, 12\}$, $\{27, 1228, 12\}$, $\{27, 1228, 12\}$, $\{27, 1228, 12\}$, $\{27, 1228, 12\}$, $\{27, 1228, 12\}$, $\{27, 1228, 12\}$, $\{27, 1228, 12\}$, $\{27, 1228, 12\}$, $\{27, 1228, 12\}$, $\{27, 1228, 12\}$, $\{27, 1228, 12\}$, $\{27, 1228, 12\}$, $\{27, 1228, 12\}$, $\{27, 1228, 12\}$, $\{27$
	$12288, 12\},$
69	$\{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27,$
	$12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 1228, 12\}, \{27, 12288, 1228, 1228, 1228, 1228, 1228, 1228, 1228, 1228, 1228, 1228, 1228, 1228, 1228, 1228, 1228, 1228, 1228, 1228, 1228, 122$
-	$12288, 12\},\ \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 122$
70	$\{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{28, 1288, 12\}, \{28, 1288, 12\}, \{28, 1288, 12\}, \{28, 1288, 12\}, \{28, 1288, 12\}, \{28, 1288, 12\}, \{28, 1288, 12\}, \{28, 1288, 1288, 1288, 1288, 12\}, \{28, 1288, 1288, 1288, 1288, 1288, 1288, 1288, 1288, 1288, 1288, 1288, 1288, 1288, 1288, 1288, 1288, 1288, 1288, 1288, 1288, 1288, 1288, 1288, 1288, 1288, 1288, 1288, 1288, 1288, 1288, 1288, 1288, 1$
	$1238, 12\}, (21, 12200, 12), (21, 12200, 12), (21, 12200, 12), (21, 12200, 12), (21, 12200, 12), (21, 12200, 12), (21, 12200, 12), (21, 12200, 12), (21, 12200, 12), (21, 12200, 12), (21, 12200, 12), (21, 12200, 12), (21, 12200, 12), (21, 12200, 12), (21, 12200, 12), (21, 12200, 12), (21, 12200, 12), (21, 12200, 12), (21, 12200, 12), (21, 12200, 12), (21, 12200, 12), (21, 12200, 12), (21, 12200, 12), (21, 12200, 12), (21, 12200, 12), (21, 12200, 12), (21, 12200, 12), (21, 12200, 12), (21, 12200, 12), (21, 12200, 12), (21, 12200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (21, 1200, 12), (2100, 1200, 12), (2100, 1200, 12)$
71	$\{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 1228, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}$
	$12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 1228, 12\}, \{27, 12288, 1228, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 12\}, \{27, 12288, 1228, 1228, 12\}, \{27, 12288, 1228, 1228, 1228, 1228, 1228, 1228, 1228, 1228, 1228, 1228, 1228, 1228, 1228, 1228, 1228, 1228, 1228, 1228, 1228, 1228, 1228, 1228, 1228, 1228, 1228, 1228, 1228, 1228,$
	$12288, 12\},$
72	$\{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28, 16384, 12\}, \{28,$
	13 , {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13},
73	$\{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 16384, 16\}, \{28, 16384, 16384, 16\}, \{28, 16384, 16384, 16\}, \{28, 16384, 16384, 16\}, \{28, 16384, 16384, 16\}, \{28, 16384, 16384, 16\}, \{28, 16384, 16\}, \{28, 16384, 16\}, \{28, 16384, 16\}, \{28, 16384, 16\}, \{28, 16384, 16\}, \{28, 16384, 16\}, \{28, 16384, 1$
	13 , $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 13\}$, $\{28, 16384, 1638, 1648, 1648$, $[28, 16384, 1638, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 164$

	$16384, 13\},$
74	$\{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 164, 164, 164, 164, 164, 164, 164, 16$
	13 , {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28,
	16384, 13},
75	$\{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 16384, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 16$
	13 , {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28,
	16384, 13},
76	$\{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 16384, 16\}, \{28, 16384, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 16$
	13 , {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648
	16384, 13},
77	$\{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 16384, 16\}, \{28, 16384, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 16$
	13 , {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 1648, 1648, {28, 1648, 1648, 1648, {28, 1648, 1648, {28, 1648, 1648, {28, 1648, {28, 1648, {28, 1648, {28, 1648, {28, 1648, {28, 1648, {28, 1648, {28, 1648, {28, 1648, {28, 1648, {28, 1648, {28, 1648, {28, 1648, {28, 1648, {28, 1648, {28, 164
	16384, 13},
78	$\{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 16384, 16\}, \{28, 16384, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 16$
	13 , {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 1648, 1648, {28, 1648, 1648, 1648, {28, 1648, 1648, {28, 1648, 1648, {28, 1648, {28, 1648, {28, 1648, {28, 1648, {28, 1648, {28, 1648, {28, 1648, {28, 1648, {28, 1648, {28, 1648, {28, 1648, {28, 1648, {28, 16
	16384, 13},
79	$\{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 13\}, \{28, 16384, 16384, 16\}, \{28, 16384, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 1648, 16$
	13 , {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 13}, {28, 16384, 1648, 1648, {28, 1648, 1648, 1648, {28, 1648, 1648, 1648, {28, 1648, 1648, {28, 1648, 1648, {28, 1648, 1648, {28, 1648, {28, 1648, {28, 1648, {28, 1648, {28, 1648, {28, 1648, {28, 1648, {28,
	16384, 13},
80	$\{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29,$
	13 , {29, 24576, 13}, {29, 24576, 13}, {29, 24576, 13}, {29, 24576, 13}, {29,
	$24576, 13\},$
81	$\{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29,$
	13 , {29, 24576, 13}, {29, 24576, 13}, {29, 24576, 13}, {29, 24576, 13}, {29,
	$24576, 13\},$
82	$\{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29,$
	13 , $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 14\}$, $\{29, 24576, 14\}$, $\{29, 24576, 14\}$, $\{29, 24576, 14\}$, $\{29, 24576, 14\}$, $\{29, 24576, 14\}$, $\{29, 24576, 14\}$, $\{29, 24576, 14\}$, $\{29, 24576, 14\}$, $\{29, 24576, 14\}$, $\{$
	$24576, 13\},$
83	$\{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29,$
	13 , $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 14\}$, $\{29, 24576, 14\}$, $\{29, 24576, 14\}$, $\{29, 24576, 14\}$, $\{29, 24576, 14\}$, $\{29, 24576, 14\}$, $\{29, 24576, 14\}$, $\{29, 24576, 14\}$, $\{29, 24576, 14\}$, $\{29, 24576, 14\}$, $\{29, 24576, 14\}$, $\{$
	$24576, 13\},$
84	$\{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29,$
	13 , $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{$
	$24576, 13\},$
85	$\{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29,$
	13 , $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{29, 24576, 13\}$, $\{$
	$24576, 13\},$
86	$\{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29,$
	$\{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29,$
	24576, 13},
87	$\{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 12\}, \{29, 24576, 12\}, \{29, 24576, 12\}, \{29, 24576, 12\}, \{29, 24576, 12\}, \{29, 24576, 12\}, \{29, 24576, 12\}, \{29, 24576, 12\}, \{29, 24576, 12\}, \{29, 24576, 12\}, \{29, 24576, 12\}, \{29, 24576, 12\}, \{29, 24576, 12\}, \{29, 24576, 12\}, \{29, 24576, 12\}, \{29, 24576, 12\}, \{29, 24576, 12\}, \{29, 24576, 12\}, \{29, 24576, 12\}, \{29, 24576, 12\}, \{29, 24576, 12\}, \{29, 24576, 12\}, \{29, 24576, 12\}, \{29, 24576, 12\}, \{29, 24576, 12\}, \{29, 24576, 12\}, \{29, 24576, 12\}, \{29, 24576, 12\}, \{29, 24576, 12\}, \{29, 24576, 12\}, \{29,$
	$\{13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 13\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}, \{29, 24576, 14\}$
	$24576, 13\}$
88 };	

Appendix F Huffman Decoder Source File

Huffman_Decoder.cpp

```
1 #include "Huffman_Decoder.h"
2 #include "symbol_tables.cpp"
  #include "static_decoding_tables.cpp"
  //Function for filling accumulator with bits from input stream.
      Input variable "num" is the number of bits to obtain.
  //If accumulator already contains the number of needed bits, no
      more are read.
  void fetch_bits(
      int num,
                            //Input
8
      stream<io_stream> &in_strm , //Input
9
      io_stream &in_buff,
                                  //In/Out
      ap_uint <8> &bit_count ,
                                      //In/Out
11
      ap_uint <64> &acc
                                  //In/Out
12
  ) {
  #pragma HLS INLINE
14
    //Inlining function automatically optimizes function usage to
15
      read one byte or two depending on input num
    if ((bit_count < num) & !in_buff.last) { // If bit_count is still
      less than num and TLAST hasn't been asserted, read another
      byte
      in_strm >> in_buff; //Read 1 byte from input stream into
17
      buffer
      acc |= (ap_uint <64>)in_buff.data << bit_count; //Append data
18
      to the left of current bits in acc. Assuming little endian
      data
      bit_count += 32; //Update number of bits in acc
19
    }
20
  }
21
22
23 //Reset code length code length counts. Takes 1 cycle
24 void reset_CL_codelength_count (ap_uint <8> CL_codelength_count [
     MAX_CL_LENGTH+1]) {
<sup>25</sup> #pragma HLS INLINE off
   for (int i = 0; i < (MAX_CLLENGTH+1); i++)
26
27 #pragma HLS UNROLL
      CL_codelength_count[i] = 0;
28
```

```
29
    }
30 }
31
32 //Reset code length code lengths. Takes 1 cycle
33 void reset_CL_codelengths(ap_uint<3> CL_codelengths[MAX_CL_CODES])
  #pragma HLS INLINE off
34
    for (int i = 0; i < MAX_CL_CODES; i++)
35
  #pragma HLS UNROLL
36
      CL_codelengths[i] = 0;
37
38
    }
39
  }
40
  //Reset length and distance code length counts. Takes 1 cycle
41
  void reset_LD_codelength_count(ap_uint<9> length_codelength_count[
42
     MAXLENLENGTH+1], ap_uint<9> distance_codelength_count [
     MAX_DIS_LENGTH+1]) {
 #pragma HLS INLINE off
43
    for (int i = 0; i < (MAX_LEN_LENGTH+1); i++)
44
  #pragma HLS UNROLL
45
      length_codelength_count[i] = 0;
46
      distance_codelength_count[i] = 0;
47
48
  }
49
50
  //Reset length code lengths. Takes 29 cycles
  void reset_length_codelengths(ap_uint<4> length_codelengths[
     MAX_LEN_CODES]) {
  #pragma HLS INLINE off
    for (int i = MIN_LEN_CODES; i < MAX_LEN_CODES; i++) { // Only last
54
      30 indexes need to be cleared, all others will always be
      filled
      //#pragma HLS UNROLL
      length_codelengths[i] = 0;
56
    }
  }
58
59
  //Reset distance code lengths. Takes 32 cycles
60
  void reset_distance_codelengths(ap_uint<4> distance_codelengths[
61
     MAX_DIS_CODES]) {
  #pragma HLS INLINE off
62
    for (int i = 0; i < MAX_DIS_CODES; i++)
63
      //#pragma HLS UNROLL
64
      distance_codelengths[i] = 0;
65
66
    ł
67
  }
68
  //Build length code table. Takes 286 cycles
69
  void build_length_table(
70
      ap_uint <4> length_codelengths [MAX_LEN_CODES],
                                                           //Input
71
      ap_uint <9> length_code_table [MAX_LEN_CODES],
                                                           //Output
72
      ap_uint <9> next_length_address [MAXLENLENGTH+1] //Input
73
  ) {
74
75 #pragma HLS INLINE off
```

```
ap_uint <4> length_codelength; //Code length of encoded Length/
76
      Literal
     L_Table_LoopC: for (int i = 0; i < MAX_LEN_CODES; i++){ //Build
77
      Length/Literal Table
78 #pragma HLS PIPELINE
       length_codelength = length_codelengths[i]; //Read Length/
      Literal code length
       if (length_codelength != 0) \{ // If the length of a code is not 0
80
         length_code_table [next_length_address [length_codelength]] =
81
      i; //At coded index, write symbol
         next_length_address [length_codelength]++;
82
       }
83
     }
84
  }
85
86
  //Build distance code table. Takes 32 cycles
87
  void build_distance_table(
88
       ap_uint <4> distance_codelengths [MAX_DIS_CODES],
89
       ap_uint <8> distance_code_table [MAX_DIS_CODES],
90
       ap_uint <8> next_distance_address [MAX_DIS_LENGTH+1]
91
  ) {
92
  #pragma HLS INLINE off
93
     ap_uint <4> distance_codelength; //Code length of encoded
94
      Distance
     D_Table_LoopC: for (int i = 0; i < MAX_DIS_CODES; i++){ //Build
95
      Distance Table
  #pragma HLS PIPELINE
96
       distance_codelength = distance_codelengths[i]; //Read Distance
97
       code length
       if (distance_codelength != 0) { // If the length of a code is not
98
       0
         distance_code_table [next_distance_address ]
99
      distance_codelength]] = i; //At coded index, write symbol
         next_distance_address [distance_codelength]++;
100
101
       }
102
  }
103
  void decode_static_block(
       stream<io_stream> &in_strm ,
                                      //Input
106
       io_stream &in_buff,
                                    //In/Out
       ap_uint <8> &bit_count ,
                                         //In/Out
108
                                    //In/Out
       ap\_uint < 64 > \&acc,
109
       bool & end_of_block ,
                                    //In/Out
110
       stream < lld_stream > &out_strm //Output
  ) {
     ap_uint<9> static_code_bits; //9 bits containing a static length
113
      /distance code, actual code length may be 7 to 9 bits long
     static_symbol length_symbol; //Decoded Length/Literal Huffman
114
      symbol
     static_symbol distance_symbol; //Decoded Distance Huffman symbol
115
     ap_uint <9> match_length; //Match length variable
116
     ap_uint <16> match_distance; //Match distance variable
117
     ap_uint<5> extra_length; //Integer value of extra length
118
```

```
ap_uint <13> extra_distance; //Integer value of extra distance
119
     lld_stream out_buff; //Buffer for writing to output stream
120
     Static_Block_Loop: while(!end_of_block){ //Continue processing a
       block until end-of-block code found
       fetch_bits (32, in_strm, in_buff, bit_count, acc);
       static_code_bits = acc(8,0); //Take in 9 bits from ACC
124
      length_symbol = static_length_table[static_code_bits]; //
125
      Decode in static literal/length table
       acc >>= length_symbol.bits;
                                     //Shift out bits from acc
126
       bit_count -= length_symbol.bits; //Update bit count
       switch (length_symbol.type(7, 4)) \{ //Check upper four bits of
128
      type
       case 0 : //Literal
129
         out_buff.data = length_symbol.base; //Write Literal to
130
      output
         out_buff.keep = 0b0001; //Update TKEEP bits to indicate
      Literal
         out_buff.user = 0;
132
         out_buff.last = 0; //Assign TLAST
133
         out_strm << out_buff; //Write to output stream
         break;
       case 1: // Length/Distance
136
         extra_length = acc \& ((1 \ll length_symbol.type(3,0)) - 1);
      //Fetch extra length bits from acc
         acc >>= length_symbol.type(3,0); //Discard extra length bits
138
       from acc
         bit_count = length_symbol.type(3,0); //Update bit count
139
      accordingly
         match_length = length_symbol.base + extra_length; //Add base
140
       and extra to get length. Can be 3-258 (9 bits)
141
         distance_symbol = static_distance_table [acc(4,0)]; //Decode
142
      in static distance table
         acc >>= STATIC_DIS_LENGTH; // Shift out bits from acc
143
         bit_count -= STATIC_DIS_LENGTH; //Update bit count
144
         extra_distance = acc \& ((1 \ll distance_symbol.type(3,0)) - 1
145
       ); //Fetch extra distance bits from acc
         acc >>= distance_symbol.type(3,0); //Discard extra distance
146
      bits from acc
         bit_count -= distance_symbol.type(3,0); //Update bit count
147
      accordingly
         match_distance = distance_symbol.base + extra_distance; //
148
      Add base and extra to get distance. Can be 1-32768 (16 bits)
149
         out_buff.data(31,23) = match_length; //Write 9-bit match
      length to output
         out\_buff.data(15, 0) = match\_distance; //Write 16-bit match
      distance to output
         out_buff.keep = 0b1111; //Update TKEEP bits to indicate
      length-distance pair
         out_buff.user = 1;
153
         out_buff.last = 0; //Assign TLAST
154
         out_strm << out_buff; //Write to output stream
155
```

```
break;
156
       case 6: //End-of-Block
157
         end_of_block = true; //Update EOB flag, exit Block loop and
158
      return to Main Loop
         break;
160
161
  }
162
163
  void decode_dynamic_block(
164
       stream < io_stream > & in_strm ,
                                       //Input
165
       io_stream &in_buff,
                                     //In/Out
166
       ap_uint <8> &bit_count ,
                                          //In/Out
167
       ap_uint <64> &acc ,
                                     //In/Out
168
       bool & end_of_block ,
                                     //In/Out
169
       stream<lld_stream> &out_strm , //Output
170
       ap_uint <9> length_codelength_count [MAXLENLENGTH+1],
171
                                                                    11
      Input
       ap_uint <9> distance_codelength_count [MAX_DIS_LENGTH+1], //
172
      Input
       ap_uint <15> base_length_values [MAX_LEN_LENGTH+1],
                                                                //Input
       ap_uint <15> base_distance_values [MAX_DIS_LENGTH+1],
                                                                //Input
174
       ap_uint <9> base_length_address [MAX_LEN_LENGTH+1],
                                                                //Input
       ap_uint <8> base_distance_address [MAX_DIS_LENGTH+1],
                                                                //Input
176
       ap_uint <9> length_code_table [MAX_LEN_CODES],
                                                                //Input
177
       ap_uint <8> distance_code_table [MAX_DIS_CODES]
                                                                //Input
178
179
  ) {
     ap_uint <15> code_bits; //15 bits containing a length/distance
180
      code, actual code length may be 0 to 15 bits long
     ap_uint <16> code_comparison; //Bit array for comparing code_bits
181
       to base_length_values
     ap_uint <4> code_length; //Deciphered length of currently held
182
      length code
     ap_uint <9> code_address; //Register for calculating length code
183
      address
     ap_uint <9> length_symbol; //Decoded Length/Literal Huffman
184
      symbol
     ap_uint<5> distance_symbol; //Decoded Distance Huffman symbol
185
     length_symbol_values length_symbol_extras;
186
     distance_symbol_values distance_symbol_extras;
187
     ap_uint<9> match_length; //Match length variable
188
     ap_uint <16> match_distance; //Match distance variable
189
     ap_uint<5> extra_length; //Integer value of extra length
190
     ap_uint <13> extra_distance; //Integer value of extra distance
191
     lld_stream out_buff; //Buffer for writing to output stream
192
193
194
     Dynamic_Block_Loop: while (!end_of_block) { // Continue processing
      a block until end-of-block code found
       fetch_bits(MAX_LEN_LENGTH, in_strm, in_buff, bit_count, acc);
195
      //Fetch 15 bits for Length/Literal code
       code_bits = acc(0,14); //Take in 15 bits from ACC and reverse
196
      them
       Length_Code_Compare_Loop: for (int i = 1; i \leq MAX_LEN_LENGTH;
197
      i++){ //Compare bits to every length base_value to find code
```

length of bits #pragma HLS UNROLL 198 $code_comparison[i] = (length_codelength_count[i] != 0) ? ($ 199 $code_bits >= (base_length_values[i] << (MAXLENLENGTH - i)))$: 0; } //Comparisons with lengths that aren't used are disabled (200 They would always be 1 since base value would be 0) code_length = MAX_LENLENGTH - (__builtin_clz(code_comparison) 201 -16; //Code length is bit position of highest passing comparison. CLZ adds 16 bits $code_bits >>= (MAXLENLENGTH - code_length); //Shift bits out$ 202 so only codelength remain $code_address = base_length_address[code_length] + (code_bits -$ 203 base_length_values[code_length]); //Address = base + offset length_symbol = length_code_table[code_address]; //Decode 204length code in lookup table //Shift out bits from acc $acc >>= code_length;$ 205 bit_count -= code_length; //Update bit count 206 if (length_symbol < 256) { // If decoded Length/Literal symbol is 207 from 0 to 255, it is a Literal out_buff.data = length_symbol; //Write Literal to output 208 $out_buff.keep = 0b0001; //Update TKEEP bits to indicate$ 209 Literal $out_buff.user = 0;$ 210 out_buff.last = 0; //Assign TLAST 211 out_strm << out_buff; //Write to output stream 212 } 213 else if $(length_symbol = 256) \{ //End-of-block symbol \}$ 214 end_of_block = true; //Update EOB flag, exit Block loop and 215return to Main Loop } 216 $else \{ //If length_symbol > 256, It is a Length \}$ 217length_symbol_extras = length_symbol_table [length_symbol-218 MIN_LEN_CODES]; //Lookup base length and extra bits in table fetch_bits (MAX_LEN_EXTRA_BITS+MAX_DIS_LENGTH, in_strm, 219 in_buff, bit_count, acc); //Fetch 20 bits for Length code extra bits and distance $extra_length = acc \& ((1 \ll length_symbol_extras.bits) - 1)$ 220 ; //Fetch extra bits from acc acc >>= length_symbol_extras.bits; //Discard extra bits from 221 acc bit_count -= length_symbol_extras.bits; //Update bit count 222 accordingly $match_length = length_symbol_extras.base + extra_length + 3;$ //Add base and extra to get length. Base Lengths 3-258 are encoded in 0-255 (8 bits) so we add 3 2.2.4 $code_bits = acc(0,14); //Take in 15$ bits from ACC and 225reverse them Distance_Code_Compare_Loop: for (int i = 1; $i \leq i$ 226 MAX.DISLENGTH; i++ //Compare bits to every distance base_value to find code length of bits

227 #pragma HLS UNROLL

I	(1, 1, 2, 3, 3, 3, 3, 3, 3, 3, 3, 3, 3, 3, 3, 3,
228	code_comparison[i] = (distance_codelength_count[i] != 0) ?
	(code_bits >= (base_distance_values[i] << (MAX_DIS_LENGTH - i
))) : 0;
229	} //Comparisons with lengths that aren't used are disabled (
	They would always be 1 since base value would be 0)
230	code_length = MAX_DIS_LENGTH - (builtin_clz(
200	$code_comparison) - 16$; //Code length is bit position of
	highest passing comparison. CLZ adds 16 bits
231	code_bits >>= (MAX_DIS_LENGTH - code_length); //Shift bits
	out so only code length remain
232	$code_address = base_distance_address [code_length] + ($
	code_bits - base_distance_values[code_length]); //Address =
	base + offset
233	distance_symbol = distance_code_table[code_address]; //
	Decode distance code in lookup table
234	acc >>= code_length; //Shift out bits from acc
235	bit_count -= code_length; //Update bit_count
	distance_symbol_extras = distance_symbol_table
236	
	distance_symbol]; //Lookup base distance and extra bits in
	table
237	fetch_bits (MAX_DIS_EXTRA_BITS, in_strm, in_buff, bit_count,
	acc); //Fetch 13 bits for Distance code extra bits
238	$extra_distance = acc \& ((1 \ll distance_symbol_extras.bits) -$
	1); //Fetch extra bits from acc
239	acc >>= distance_symbol_extras.bits; //Discard extra bits
	from acc
240	<pre>bit_count -= distance_symbol_extras.bits; //Update bit count</pre>
	accordingly
241	match_distance = distance_symbol_extras.base +
	extra_distance; //Add base and extra to get distance. Can be
	1-32768 (16 bits)
242	
243	$out_buff.data(31,23) = match_length; //Write 9-bit match$
	length to output
244	out_buff.data(15, 0) = match_distance; //Write 16-bit match
	distance to output
245	out_buff.keep = $0b1111$; //Update TKEEP bits to indicate
240	length-distance pair
246	$out_buff.user = 1;$
	$out_buff.last = 0; //Assign TLAST$
247	out_strm << out_buff; //Write to output stream
248	
249	}
250	}
251	}
252	
253	void build_dynamic_tables(
254	stream < io_stream > & in_strm , //Input
255	io_stream ∈_buff, //In/Out
256	ap_uint <8> &bit_count, //In/Out
257	$ap_uint < 64 > \&acc$, //In/Out
258	ap_uint <4> length_codelengths [MAX_LEN_CODES], //Input
259	ap_uint <4> distance_codelengths [MAX_DIS_CODES], //Input
260	ap_uint <9> length_codelength_count [MAXLENLENGTH+1], //
	Output
1	

ap_uint <9> distance_codelength_count [MAX_DIS_LENGTH+1], // 261 Output ap_uint <15> base_length_values [MAX_LEN_LENGTH+1], //Output 262 ap_uint <15> base_distance_values [MAX_DIS_LENGTH+1], //Output 263 //Output ap_uint <9> base_length_address [MAX_LEN_LENGTH+1], 264 ap_uint <8> base_distance_address [MAX_DIS_LENGTH+1], //Output 265ap_uint <9> length_code_table [MAX_LEN_CODES], //Output 266 ap_uint <8> distance_code_table [MAX_DIS_CODES] //Output 267) { 268 ap_uint <9> num_length_codelengths; //Number of Length/Literal 269 code lengths in sequence, from $257\ {\rm to}\ 286$ ap_uint <8> num_distance_codelengths; //Number of Distance code 270 lengths in sequence, from 1 to 32 ap_uint <8> num_codelength_codelengths; //Number of Code_Length 271 code lengths in sequence, from 4 to 19 ap_uint <3> CL_codelength; //Code length of encoded Code Length. 272 CLCLs can be from 0 to 7 bits long ap_uint<3> CL_codelengths [MAX_CL_CODES]; // Array for storing CL 273 code lengths ²⁷⁴ #pragma HLS ARRAY.PARTITION variable=CL_codelengths complete dim=1 ap_uint <8> CL_codelength_count [MAX_CLLENGTH+1]; //Array for counting number of times each CLCL occurs #pragma HLS ARRAY_PARTITION variable=CL_codelength_count complete 276 $\dim = 1$ ap_uint<7> base_CL_values [MAX_CLLENGTH+1]; // Calculated base 277 value for each CLCL ²⁷⁸ #pragma HLS ARRAY.PARTITION variable=base_CL_values complete dim=1 ap_uint <5> base_CL_address [MAX_CLLENGTH+1]; //Base address for 279 each CLCL base value #pragma HLS ARRAY_PARTITION variable=base_CL_address complete dim 280 =1ap_uint <5> next_CL_address [MAX_CLLENGTH+1]; // Contains the next 281 address for each CLC symbol #pragma HLS ARRAY_PARTITION variable=next_CL_address complete dim 282 =1ap_uint <5> codelength_address; // Register for calculating 283 code_length code address ap_uint<5> CL_code_table [MAX_CL_CODES]; // Table containing 284 symbols for 19 CL Codes. Codes are indexed using base_CL_addresses ap_uint <9> codelengths_received; //For counting number of code 285 lengths read from sequence ap_uint <7> codelength_bits; //7 bits containing a length/ 286 distance code length code, actual code length may be 0 to 7 bits long ap_uint <8> CL_comparison; //Bit array for comparing 287 codelength_bits to base_CL_values ap_uint <3> codelength_length; //Deciphered length of currently 288 held code length code ap_uint <5> CL_symbol; //Decoded Code Length symbol (Can be 0 to 289 18)ap_uint <9> length_symbol_counter; //Index counter for current 290 Length/Literal symbol in sequence

291	ap_uint <5> distance_symbol_counter; //Index counter for current
292	Distance symbol in sequence ap_uint <9> next_length_address [MAX_LEN_LENGTH+1]; // Contains the
293	next address for each Length/Literal symbol #pragma HLS ARRAY_PARTITION variable=next_length_address complete
	dim=1
294	ap_uint <8> next_distance_address [MAX_DIS_LENGTH+1]; //Contains
	the next address for each Distance symbol #pragma HLS ARRAY_PARTITION variable=next_distance_address
295	complete dim=1
296	ap_uint <5> previous_CL; //Register for storing found_CL for next
200	iteration
297	ap_uint <8> repeat_value; //Used by code length symbols 16, 17,
	and 18 for storing number of repetitions to perform
298	
299	reset_CL_codelength_count(CL_codelength_count);
300	reset_CL_codelengths(CL_codelengths);
301	reset_LD_codelength_count (length_codelength_count, distance_codelength_count);
302	distance_codelength_count),
302	//Read code length codes and build code length table
304	fetch_bits (14, in_strm, in_buff, bit_count, acc);
305	num_length_codelengths = $acc(4,0) + 257$; //There will always be
	at least 257 Length/Literal codes for the 256 Literals and the
	EOB code
306	num_distance_codelengths = $acc(9,5) + 1$; //There will always be
	at least 1 distance code num codelength codelengths $= coc(12, 10) + 4$; //There will always
307	num_codelength_codelengths = $acc(13,10) + 4$; //There will always be at least 4 code length code lengths (for symbols 16, 17,
	18, and 0)
308	$assert(num_length_codelengths < 287); //Max 286 Length/Literal$
	code lengths
309	$assert(num_distance_codelengths < 33); //Max 32 Distance code$
	lengths
310	<pre>assert(num_codelength_codelengths < 20); //Max 19 Code Length</pre>
311	acc $\gg = 14$; //Shift out bits from acc
312	bit_count $-=$ 14; //Update bit count
313	
314	//Build code_length table
315	//1: Count number of codes for each length
316	CL_Table_LoopA: for (int $i = 0$; $i < num_codelength_codelengths; i$
	++){
317	#pragma HLS PIPELINE
318	fetch_bits $(3, \text{ in_strm}, \text{ in_buff}, \text{ bit_count}, \text{ acc});$ CL_codelength = acc $(2,0);$ //Read 3-bit_code_length
319 320	CL_codelength = acc(2,0), // itead 5=bit code length CL_codelengths [permuted_order [i]] = CL_codelength; // Store
	code length in array in permuted order
321	CL_codelength_count[CL_codelength]++; //Take count of number
	of code lengths
322	acc >>= 3; //Shift out bits from acc
323	bit_count $-= 3;$ //Update bit count
324	}
325	//2: Calculate base value for each code length

```
CL_codelength_count[0] = 0; //Set back to 0 before calculating
326
      base values (Codes with length of 0 are unused)
     base_CL_values[0] = 0;
327
     base_CL_address[0] = 0;
328
     CL_Table_LoopB: for (int i = 1; i \le MAX_CLLENGTH; i++){ //For
329
      each possible code length
  #pragma HLS PIPELINE
330
       base_CL_values[i] = (base_CL_values[i-1] + CL_codelength_count
331
      [i-1] << 1; //Base value for a code length is based on number
       of previous code lengths
       base_CL_address[i] = base_CL_address[i-1] +
332
      CL_codelength_count[i-1]; //Base address is "number of code
      lengths" away from previous base address
       next_CL_address[i] = base_CL_address[i]; //Initialize "next
333
      address" to base address for this length
334
     ł
     //3: Assign consecutive values (addresses) to each code for all
335
      code lengths
     CL_Table_LoopC: for (int i = 0; i < MAX_CL_CODES; i++){ //For all
336
       19 code length symbols
  #pragma HLS PIPELINE
       CL_codelength = CL_codelengths[i]; //Read CL code length
338
       if (CL_codelength != 0) \{ //If the length of a code is not 0 \}
339
         CL_code_table[next_CL_address[CL_codelength]] = i;
340
         next_CL_address [CL_codelength]++;
341
       }
342
     }
343
344
     //Read encoded code length sequence and decode it using that
345
      table
     codelengths\_received = 0; //Reset code lengths received
346
     length_symbol_counter = 0; //Reset Length/Literal array index
347
      pointer
     distance_symbol_counter = 0; //Reset Distance array index
348
      pointer
     LD_Table_LoopA: while (codelengths_received < (
349
      num_length_codelengths+num_distance_codelengths)){ // Retrieve
      all code lengths in sequence
       //Sequence can be from 258 to 318 code lengths long
350
       fetch_bits (7, in_strm, in_buff, bit_count, acc);
351
       codelength_bits = acc(0,6); //Take in 7 bits from ACC and
352
      reverse them
       CL_Comparison_Loop: for (int i = 1; i <= MAX_CLLENGTH; i++){
353
      //Compare bits to every length base_value to find code length
      of bits
  #pragma HLS UNROLL
354
         CL_comparison[i] = (CL_codelength_count[i] != 0) ? (
355
      codelength_bits >= (base_CL_values[i] << (MAX_CLLENGTH - i)))
       : 0;
       } //Comparisons with lengths that aren't used are disabled (
356
      They would always be 1 since base value would be 0)
       codelength_length = MAX_CLLENGTH - (\__builtin_clz(
357
      CL_comparison) - 24); //Code length is bit position of highest
       passing comparison. CLZ adds 24 bits
```

```
codelength_bits >>= (MAX_CLLENGTH - codelength_length); //
358
      Shift bits out so only codelength remain
       codelength_address = base_CL_address[codelength_length] + (
359
      codelength_bits - base_CL_values[codelength_length]);
       CL_symbol = CL_code_table [codelength_address]; //Decode code
360
      length in lookup table
                                        //Shift out bits from acc
       acc >>= codelength_length;
361
       bit_count -= codelength_length; //Update bit count
362
       if (CL_symbol \ll 15) \{ //If decoded code length symbol is from 0 \}
363
       to 15
         if (codelengths_received < num_length_codelengths) { // If
364
      Length code length
           length_codelengths[length_symbol_counter] = CL_symbol; //
365
      Current symbol in sequence has code length of found_CL
           length_codelength_count[CL_symbol]++; //Count code length
366
           length_symbol_counter++; //Increment symbol pointer
367
         }
368
         else { // If Distance code length
369
           distance_codelengths [distance_symbol_counter] = CL_symbol;
370
       //Current symbol in sequence has code length of found_CL
           distance_codelength_count [CL_symbol]++; //Count code
371
      length
           distance_symbol_counter++;
372
         }
373
         codelengths_received++; //Increment code length counter
374
         previous_CL = CL_symbol; //Save code length for next
375
      iteration
       }
376
       else {
377
         switch(CL_symbol){
378
         case 16 : //Symbol 16: Copy previous code length 3 to 6
379
      times
           fetch_bits(2, in_strm, in_buff, bit_count, acc); //Fetch 2
380
       extra bits containing repeat value
           repeat_value = \operatorname{acc}(1,0) + 3;
381
           acc >>= 2;
                           //Shift out bits from acc
382
           bit_count -= 2; //Update bit count
383
           Copy_Previous_CL_Loop: for(int i = 0; i < repeat_value; i
384
      ++)\{ //For 3 to 6 times
             //#pragma HLS PIPELINE
385
             if (codelengths_received < num_length_codelengths) { // If
386
      Length code length
               length_codelengths[length_symbol_counter] =
387
      previous_CL; //Current symbol in sequence has code length of
      previous_CL
               length_codelength_count [previous_CL]++; //Count code
388
      length
               length_symbol_counter++; //Increment symbol pointer
389
             }
390
             else { // If Distance code length
391
               distance_codelengths [distance_symbol_counter] =
392
      previous_CL; //Current symbol in sequence has code length of
      previous_CL
```

distance_codelength_count [previous_CL]++; //Count code 393 length distance_symbol_counter++; 394 } 395 codelengths_received++; //Increment code length counter 396 } 397 398 break; case 17 : //Symbol 17: Repeat code length of zero 3 to 10 399 times fetch_bits(3, in_strm, in_buff, bit_count, acc); //Fetch 3 400 extra bits containing repeat value repeat_value = $\operatorname{acc}(2,0) + 3;$ 401 acc >>= 3;//Shift out bits from acc 402bit_count -= 3; //Update bit count 403 Repeat_Zero_CL_LoopA: for (int i = 0; $i < repeat_value$; i 404 $++)\{ //For 3 to 10 times \}$ //#pragma HLS PIPELINE 405if (codelengths_received < num_length_codelengths) { // If 406 Length code length $length_codelengths [length_symbol_counter] = 0; //$ 407 Current symbol in sequence has code length of 0 length_symbol_counter++; //Increment symbol pointer 408 } 409 else { // If Distance code length 410 distance_codelengths [distance_symbol_counter] = 0; // 411 Current symbol in sequence has code length of 0 distance_symbol_counter++; //Increment symbol pointer 412 } 413 codelengths_received++; //Increment code length counter 414 } 415 break; 416 case 18 : //Symbol 18: Repeat code length of zero 11 to 138 417 times fetch_bits(7, in_strm, in_buff, bit_count, acc); //Fetch 7 418 extra bits containing repeat value repeat_value = $\operatorname{acc}(6,0) + 11;$ 419 //Shift out bits from acc acc >>= 7;420 $bit_count = 7; //Update bit count$ 421 Repeat_Zero_CL_LoopB: for (int i = 0; $i < repeat_value$; i 422 ++){ //For 11 to 138 times //#pragma HLS PIPELINE 423 if (codelengths_received < num_length_codelengths) { // If 424 Length code length $length_codelengths [length_symbol_counter] = 0; //$ 425 Current symbol in sequence has code length of 0 length_symbol_counter++; //Increment symbol pointer 426 } 427 else{ //If Distance code length 428 distance_codelengths [distance_symbol_counter] = 0; //429Current symbol in sequence has code length of 0 distance_symbol_counter++; //Increment symbol pointer 430 431 codelengths_received++; //Increment code length counter 432 } 433

```
break;
434
         default :
435
           //Shouldn't occur, misread codes should be mostly 0s,
436
      could be other values from previous iterations if tables arent
       cleared.
           break;
437
438
         }
       }
439
     }
440
441
     //When all length and distance code lengths are received
442
     length_codelength_count[0] = 0; //Set back to 0 before
443
      calculating base values (Codes with length of 0 are unused)
     distance_codelength_count [0] = 0;
444
     base_length_values[0] = 0;
445
     base_length_address[0] = 0;
446
     base_distance_values[0] = 0;
447
     base_distance_address[0] = 0;
448
     //Calculate Base Values and Base Addresses
449
     LD_Table_LoopB: for (int i = 1; i \ll MAX_LENLENGTH; i++){ //For
450
      each possible code length
  #pragma HLS PIPELINE
451
       base_length_values[i] = (base_length_values[i-1] +
452
      length_codelength_count[i-1]) \ll 1;
       base_length_address[i] = base_length_address[i-1] +
453
      length_codelength_count[i-1];
       next_length_address[i] = base_length_address[i];
454
       base_distance_values[i] = (base_distance_values[i-1] +
455
      distance_codelength_count[i-1]) \ll 1;
       base_distance_address[i] = base_distance_address[i-1] +
456
      distance_codelength_count [i-1];
       next_distance_address [i] = base_distance_address [i];
457
     }
458
459
     //Build code tables from code lengths
460
     //Separated as functions to allow both to execute simultaneously
461
     build_length_table(length_codelengths, length_code_table,
462
      next_length_address);
     build_distance_table(distance_codelengths, distance_code_table,
463
      next_distance_address);
464
  }
465
  ap_uint<2> full_huffman_decoder(
466
       stream < io_stream > & in_strm ,
467
       stream < lld_stream > &out_strm
468
  ) {
469
470 #pragma HLS INTERFACE ap_ctrl_hs register port=return
  #pragma HLS INTERFACE axis off port=out_strm
471
  #pragma HLS INTERFACE axis off port=in_strm
472
     ap\_uint < 64 > acc = 0; //Accumulator for storing up to 32 bits at
473
      a time
     ap\_uint < 8 > bit\_count = 0; //Number of bits currently in the acc
474
     bool block_final = false; //Flag for BFINAL block header
475
     ap_uint<2> block_type; //Flag for BTYPE block header
476
```

477	io_stream in_buff = $\{0\}$; //Buffer for reading input stream. It
	is passed to functions so they can check TLAST before reading
	from stream.
478	bool end_of_block; //End-of-block flag
479	ap_uint <16> block_length;
480	ap_uint <16> block_Nlength;
481	static ap_uint $<4>$ length_codelengths [MAX_LEN_CODES] = {0}; //
	Array of code lengths for each Length/Literal symbol
482	static ap_uint $<4>$ distance_codelengths [MAX_DIS_CODES] = {0}; //
	Array of code lengths for each Distance symbol
483	ap_uint <9> length_codelength_count [MAX_LENGTH+1]; // Array
	for counting number of times each code length occurs
484	#pragma HLS ARRAY_PARTITION variable=length_codelength_count
	complete dim=1
485	ap_uint <9> distance_codelength_count [MAX_DIS_LENGTH+1]; // Array
	for counting number of times each code length occurs
486	#pragma HLS ARRAY_PARTITION variable=distance_codelength_count
	complete dim=1
487	ap_uint <15> base_length_values [MAX_LENLENGTH+1]; // Calculated
	base value for each Length/Literal code length
488	#pragma HLS ARRAY_PARTITION variable=base_length_values complete
	dim=1
489	ap_uint <15> base_distance_values [MAX_DIS_LENGTH+1]; // Calculated
	base value for each Distance code length
490	#pragma HLS ARRAY PARTITION variable=base_distance_values complete
	dim=1
491	ap_uint <9> base_length_address [MAX_LEN_LENGTH+1]; //Base address
-	for each Length/Literal code length base value
492	#pragma HLS ARRAY_PARTITION variable=base_length_address complete
	dim=1
493	ap_uint <8> base_distance_address [MAX_DIS_LENGTH+1]; //Base
	address for each Distance code length base value
494	#pragma HLS ARRAY_PARTITION variable=base_distance_address
	complete dim=1
495	ap_uint <9> length_code_table [MAX_LEN_CODES]; //For looking up
	Length/Literal symbol of a code.
496	ap_uint <8> distance_code_table [MAX_DIS_CODES]; //For looking up
	Distance symbol of a code.
497	$lld_stream out_buff = \{0\}; //Buffer for writing to output stream$
498	
499	Main_Loop: while(!block_final){ //Continue processing Deflate
	blocks until final block is finished
500	end_of_block = false; //Reset end-of-block flag
501	$fetch_bits(3, in_strm, in_buff, bit_count, acc);$
502	$block_final = acc[0];$ //Retrieve BFINAL bit
503	$block_type = acc(2, 1); //Retrieve BTYPE bits$
504	acc >>= 3; //Shift out bits from acc
505	bit_count $-= 3;$ //Update bit count
506	
507	<pre>switch(block_type){</pre>
508	case 0b00 : //Stored Block
509	acc >>= (bit_count % 8); //Discard 0 to 7 remaining
	bits to next byte boundary in acc
510	bit_count -= (bit_count % 8); //Update bit count

```
511
         fetch_bits(32, in_strm, in_buff, bit_count, acc);
         block_length(15,8) = acc(7,0); //Read upper byte of LEN
         block_length(7,0)
                              = \operatorname{acc}(15,8); //\operatorname{Read} lower byte of LEN
514
         block_Nlength(15,8) = acc(23,16); //Read upper byte of NLEN
         block_Nlength(7,0) = acc(31,24); //Read lower byte of NLEN
         if(block_length != ~block_Nlength){ //Check if LEN is 1s
      compliment of NLEN
           return 1;
518
         }
         else {
520
                             //Shift out bits from acc
           acc >>= 32;
           bit_count = 32;
                                 //Update bit count
           Stream_Stored_Block_Loop: for (int i = 0; i < block_length
523
      -4; i+=4){ //Pass LEN number of bytes through
  #pragma HLS PIPELINE
524
525
             in_strm >> in_buff;
              out_buff.data = in_buff.data;
526
              out_buff.keep = 0b1111;
              out_buff.user = 0;
528
              out_buff.last = 0;
530
              out_strm << out_buff;
           fetch_bits (32, in_strm, in_buff, bit_count, acc);
           switch(block_length % 4){ //Write remaining amount of
      bytes on last iteration (1-4)
           case 0 : //4 remaining bytes
              out_buff.data = acc(31,0);
536
              out_buff.keep = 0b1111;
                            //Shift out bits from acc
              acc >>= 32;
538
              bit_count -= 32; //Update bit count
              break;
540
           case 1 : //1 remaining byte
541
              out_buff.data = acc(7,0);
542
              out_buff.keep = 0b0001;
543
                            //Shift out bits from acc
              acc \gg = 8;
544
              bit_count -= 8; //Update bit count
545
              break:
546
           case 2 : //2 remaining bytes
547
              out_buff.data = acc(15,0);
548
              out_buff.keep = 0b0011;
549
              acc >>= 16;
                            //Shift out bits from acc
              bit_count -= 16; //Update bit count
              break:
           case 3 : //3 remaining bytes
              out_buff.data = acc(23,0);
554
              out_buff.keep = 0b0111;
                            //Shift out bits from acc
              acc >>= 24;
              bit_count -= 24; //Update bit count
              break;
558
           }
           out_buff.user = 0;
560
           out_buff.last = 0; //Assign TLAST
561
```

```
out_strm << out_buff;</pre>
562
         }
563
         break;
564
565
       case 0b01 : //Static Compressed Block
566
         decode_static_block(in_strm, in_buff, bit_count, acc,
567
      end_of_block , out_strm);
         break;
568
569
       case 0b10 : //Dynamic Compressed Block
570
         build_dynamic_tables ( in_strm , in_buff , bit_count , acc ,
              length_codelengths,
                                       distance_codelengths,
              length_codelength_count, distance_codelength_count,
              base_length_values,
                                       base_distance_values,
574
              base_length_address,
                                       base_distance_address,
                                       distance_code_table);
              length_code_table,
576
         decode_dynamic_block ( in_strm , in_buff , bit_count , acc ,
577
      end_of_block, out_strm,
              length_codelength_count, distance_codelength_count,
578
              base_length_values,
                                       base_distance_values,
              base_length_address,
                                       base_distance_address,
580
              length_code_table,
                                       distance_code_table
581
         );
582
         reset_length_codelengths(length_codelengths); //Reset_code
583
      length arrays while dynamic decoding takes place
         reset_distance_codelengths(distance_codelengths);
584
         break;
585
586
       case 0b11 : //Reserved (Error)
587
         return 2;
588
         break;
589
       }
590
     } //After last block has been processed
591
     out_buff.keep = 0; //Lower TKEEP signal
     out_buff.last = 1; //Raise TLAST signal
593
     out_strm << out_buff;</pre>
594
     return 0;
595
596
  }
```

Appendix G Huffman Decoder Header File

Huffman_Decoder.h

```
1 #include <stdio.h>
2 #include <string.h>
 #include <ap_int.h>
3
4 #include <hls_stream.h>
 #include <assert.h>
  using namespace hls;
9 #define MAX_LEN_CODES 286 //Max 286 Length/Literal code lengths
10 #define MIN_LEN_CODES 257 //Min 257 Length/Literal code lengths
      (256 Literals and 1 End_of_block code)
11 #define MAX_DIS_CODES 32 //Max 32 Distance code lengths
<sup>12</sup> #define MAX_CL_CODES 19 //Max 19 Code Length code lengths
13 #define MAX_LEN_LENGTH 15 //Max length of Length/Literal code is
     15 bits
14 #define MAX_DIS_LENGTH 15 //Max length of Distance code is 15 bits
15 #define MAX_CLLENGTH 7 //Max length of Code Length code is 7
     bits
16 #define STATIC_MAX_LEN_LENGTH 9 //Max length of Static Length/
     Literal code is 9 bits
17 #define STATIC_MIN_LEN_LENGTH 7 //Min length of Static Length/
     Literal code is 7 bits
18 #define STATIC_DIS_LENGTH 5 // Static Distance codes are fixed
     length 5-bit codes
<sup>19</sup>#define MAX_LEN_EXTRA_BITS 5 //Max number of extra bits following
     a Length code
20 #define MAX_DIS_EXTRA_BITS 13 //Max number of extra bits following
      a Distance code
21
22 typedef struct { //Input AXI-Stream structure
    ap_uint <32> data; //Four bytes of data
23
    ap_uint <4> keep; //TKEEP Signals for each byte
                   //TLAST AXI-Stream signal
    bool last;
25
26 } io_stream;
27
 typedef struct { // Output (Literal, Length/Distance Pair) AXI-
28
     Stream structure
```

```
ap_uint <32> data; //Four bytes of data
29
    ap_uint <4> keep; //TKEEP Signals for each byte
30
                    //TUSER Signal to identify Literal(0) or Length-
    bool user;
31
     Distance pair(1)
    bool last;
                    //TLAST AXI-Stream signal
32
  } lld_stream;
33
34
  typedef struct { // Structure for Length symbol table
35
    ap_uint <3> bits; //Number of extra bits following code. Can be
36
     from 0 to 5 for lengths.
    ap_uint <8> base; //Base length value - 3. Lengths 3-258 are
37
     encoded in 0-255
38 } length_symbol_values;
39
 typedef struct { // Structure for Distance symbol table
40
    ap_uint <4> bits; //Number of extra bits following code. Can be
41
     from 0 to 13 for distances.
    ap_uint <15> base; //Base distance value from 0 to 24577
42
43 } distance_symbol_values;
44
45 typedef struct { // Structure for looking up static codes in tables
    ap_uint <8> type; //End-of-block (0110 0000), Literal (0000 0000)
46
     , or Length/Distance (0001 XXXX) (Where XXXX is number of
     extra bits)
    ap_uint <8> bits; //Number of bits in code
47
    ap_uint <16> base; //Base length/distance, or literal value
48
49 } static_symbol;
50 //The above structure was adapted from the 'code' structure used
     by zlib (defined in "inftrees.h")
```

Appendix H Symbol Tables File

symbol_tables.cpp

```
//The permuted order found when reading Code Length code length
      sequence
  const ap_uint <8> permuted_order [MAX_CL_CODES] =
       \{16, 17, 18, 0, 8, 7, 9, 6, 10, 5, 11, 4, 12, 3, 13, 2, 14, 1, 15\};
  //Each index (symbol) contains that symbols base value and extra
      bits
  //Structure: {Extra bits, Base Value-3}
  const length_symbol_values length_symbol_table [29] = \{ //Length \}
6
      Symbols 257 to 285 are indexed here from 0 to 28
       /* 0*/
                  \{0, 0\},\
                              \{0, 1\},\
                                           \{0, 2\},\
                                                        \{0, 3\},\
                                           \{0, 6\},\
       /* 4*/
                  \{0, 4\},\
                              \{0, 5\},\
                                                        \{0, 7\},\
8
       /* 8*/
                  \{1, 8\},\
                              \{1, 10\},\
                                           \{1, 12\},\
                                                       \{1, 14\},\
9
       /*12*/
                 \{2, 16\},\
                              \{2, 20\},\
                                           \{2, 24\},\
                                                       \{2, 28\},\
       /*16*/
                  \{3, 32\},\
                              \{3, 40\},\
                                           \{3, 48\},\
                                                       \{3, 56\},\
                 \{4, 64\},\
                             \{4, 80\},\
       /*20*/
                                                       \{4, 112\},\
                                         \{4, 96\},\
       /*24*/
                 \{5, 128\}, \{5, 160\}, \{5, 192\}, \{5, 224\},\
       /*28*/
                 \{0, 255\}
14
  };
15
16
  //Structure: {Extra bits, Base value}
  const distance_symbol_values distance_symbol_table [30] = {
18
19
       /* 0*/
                  \{0, 1\},\
                                  \{0, 2\},\
                                                 \{0, 3\},\
                                                                \{0, 4\},\
       /* 4*/
                  \{1, 5\},\
                                  \{1, 7\},\
                                                 \{2, 9\},\
                                                                \{2, 13\},\
20
       /* 8*/
                  \{3, 17\},\
                                  \{3, 25\},\
                                                 \{4, 33\},\
                                                                \{4, 49\},\
21
                                  \{5, 97\},\
       /*12*/
                  \{5, 65\},\
                                                 \{6, 129\},\
                                                                \{6, 193\},\
22
                                  \{7, 385\},\
       /*16*/
                  \{7, 257\},\
                                                 \{8, 513\},\
                                                                \{8, 769\},\
23
24
       /*20*/
                  \{9, 1025\},\
                                  \{9, 1537\},\
                                                \{10, 2049\}, \{10, 3073\},\
       /*24*/
                 \{11, 4097\},\
                                 \{11, 6145\}, \{12, 8193\}, \{12, 12289\},\
25
       /*28*/
                 \{13, 16385\}, \{13, 24577\}
26
27
  };
```
Appendix I Static Decoding Tables File

static_decoding_tables.cpp

//The following tables are from "inffixed.h" in the zlib library static const static_symbol static_length_table[512] = { $/* 0*/\{96,7,0\}, \{0,8,80\},\$ $\{0, 8, 16\}, \{20, 8, 115\}, \{18, 7, 31\}, \{0, 8, 112\}, \{0, 8, 48\}, \{0, 9, 192\}, \{0, 8, 112\}, \{0, 8, 112\}, \{0, 8, 112\}, \{0, 9, 192\}, \{0, 9, 192\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1$ $/* = 8*/\{16,7,10\}, \{0,8,96\}, \{0,8,32\}, \{0,9,160\}, \{0,8,0\},$ $\{0, 8, 128\}, \{0, 8, 64\}, \{0, 9, 224\}$ $/* 16*/\{16,7,6\}, \{0,8,88\}, \{0,8,24\},\{0,9,144\},$ $\{19,7,59\},\{0,8,120\},\{0,8,56\},\{0,9,208\},\$ $/* 24*/\{17,7,17\},\{0,8,104\},\{0,8,40\},\{0,9,176\},\{0,8,8\},$ $\{0, 8, 136\}, \{0, 8, 72\}, \{0, 9, 240\},\$ $/* 32*/\{16,7,4\}, \{0,8,84\},\$ $\{0, 8, 20\}, \{21, 8, 227\}, \{19, 7, 43\}, \{0, 8, 116\}, \{0, 8, 52\}, \{0, 9, 200\}, \{0, 8, 52\}, \{0, 9, 200\}, \{0, 8, 52\}, \{0, 9, 200\}, \{0, 8, 52\}, \{0, 9, 200\}, \{0, 8, 52\}, \{0, 9, 200\}, \{0, 8, 52\}, \{0, 9, 200\}, \{0, 8, 52\}, \{0, 9, 200\}, \{0, 8, 52\}, \{0, 9, 200\}, \{0, 8, 52\}, \{0, 9, 200\}, \{0, 8, 52\}, \{0, 9, 200\}, \{0, 8, 52\}, \{0, 9, 200\}, \{0, 8, 52\}, \{0, 9, 200\}, \{0, 8, 52\}, \{0, 9, 200\}, \{0, 8, 52\}, \{0, 9, 200\}, \{0, 8, 52\}, \{0, 9, 200\}, \{0, 8, 52\}, \{0, 9, 200\}, \{0, 8, 52\}, \{0, 9, 200\}, \{0, 8, 52\}, \{0, 9, 200\}, \{0, 8, 52\}, \{0, 9, 200\}, \{0, 8, 52\}, \{0, 9, 200\}, \{0, 8, 52\}, \{0, 9, 200\}, \{0, 8, 52\}, \{0, 9, 200\}, \{0, 8, 52\}, \{0, 9, 200\}, \{0, 8, 52\}, \{0, 9, 200\}, \{0, 8, 52\}, \{0, 9, 200\}, \{0, 8, 52\}, \{0, 9, 200\}, \{0, 8, 52\}, \{0, 9, 200\}, \{0, 8, 52\}, \{0, 9, 200\}, \{0, 8, 52\}, \{0, 9, 200\}, \{0, 8, 52\}, \{0, 9, 200\}, \{0, 8, 52\}, \{0, 9, 200\}, \{0, 8, 52\}, \{0, 9, 200\}, \{0, 8, 52\}, \{0, 9, 200\}, \{0, 8, 52\}, \{0, 9, 200\}, \{0, 8, 52\}, \{0, 9, 200\}, \{0, 8, 52\}, \{0, 9, 200\}, \{0, 8, 52\}, \{0, 9, 200\}, \{0, 8, 52\}, \{0, 9, 200\}, \{0, 8, 52\}, \{0, 9, 200\}, \{0, 8, 52\}, \{0, 9, 200\}, \{0, 8, 52\}, \{0, 9, 200\}, \{0, 8, 52\}, \{0, 9, 200\}, \{0, 8, 52\}, \{0, 9, 200\}, \{0, 8, 52\}, \{0, 9, 200\}, \{0, 8, 52\}, \{0, 9, 200\}, \{0, 8, 52\}, \{0, 9, 200\}, \{0, 8, 52\}, \{0, 9, 200\}, \{0, 8, 52\}, \{0, 9, 200\}, \{0, 8, 52\}, \{0, 9, 200\}, \{0, 8, 52\}, \{0, 9, 200\}, \{0, 8, 52\}, \{0, 9, 200\}, \{0, 8, 52\}, \{0, 9, 200\}, \{0, 8, 52\}, \{0, 9, 200\}, \{0, 8, 52\}, \{0, 9, 200\}, \{0, 8, 52\}, \{0, 9, 200\}, \{0, 8, 52\}, \{0, 8, 52\}, \{0, 8, 52\}, \{0, 8, 52\}, \{0, 8, 52\}, \{0, 8, 52\}, \{0, 8, 52\}, \{0, 8, 52\}, \{0, 8, 52\}, \{0, 8, 52\}, \{0, 8, 52\}, \{0, 8, 52\}, \{0, 8, 52\}, \{0, 8, 52\}, \{0, 8, 52\}, \{0, 8, 52\}, \{0, 8, 52\}, \{0, 8, 52\}, \{0, 8, 52\}, \{0, 8, 52\}, \{0, 8, 52\}, \{0, 8, 52\}, \{0, 8, 52\}, \{0, 8, 52\}, \{0, 8, 52\}, \{0, 8, 52\}, \{0, 8, 52\}, \{0, 8, 52\}, \{0, 8, 52\}, \{0, 8, 52\}, \{0, 8, 52\}, \{0, 8, 52\}, \{0, 8, 52\}, \{0, 8, 52\}, \{0, 8, 52\}, \{0, 8, 52\}, \{0, 8, 52\}, \{0, 8, 52\}, \{0, 8, 52\}, \{0, 8, 52\}, \{0, 8, 52\}, \{0, 8, 52\}, \{0, 8, 52\}, \{0, 8, 52\}, \{0, 8, 52\}, \{0, 8, 52\}, \{0, 8, 52\}, \{0, 8, 52\}, \{0, 8, 52\}, \{0, 8, 52\}, \{0, 8, 52\}, \{0, 8$ $/{*} \quad 40*/\{17,7,13\}, \{0,8,100\}, \{0,8,36\}, \{0,9,168\}, \{0,8,4\},$ $\{0, 8, 132\}, \{0, 8, 68\}, \{0, 9, 232\},\$ /* 48*/{16,7,8}, {0,8,92}, {0,8,28}, {0,9,152}, $\{20, 7, 83\}, \{0, 8, 124\}, \{0, 8, 60\}, \{0, 9, 216\},\$ $/* 56*/\{18,7,23\},\{0,8,108\},\{0,8,44\},\{0,9,184\},\{0,8,12\},$ 11 $\{0, 8, 140\}, \{0, 8, 76\}, \{0, 9, 248\},\$ $/* 64*/\{16,7,3\}, \{0,8,82\},\$ 12 $\{0,8,18\},\{21,8,163\},\{19,7,35\},\{0,8,114\},\{0,8,50\},\{0,9,196\},$ /* 72*/{17,7,11},{0,8,98}, {0,8,34},{0,9,164}, {0,8,2}, $\{0, 8, 130\}, \{0, 8, 66\}, \{0, 9, 228\},\$ $/* 80*/\{16,7,7\}, \{0,8,90\}, \{0,8,26\},\{0,9,148\},$ 14 $\{20, 7, 67\}, \{0, 8, 122\}, \{0, 8, 58\}, \{0, 9, 212\},\$ $/* 88*/\{18,7,19\}, \{0,8,106\}, \{0,8,42\}, \{0,9,180\}, \{0,8,10\},$ $\{0, 8, 138\}, \{0, 8, 74\}, \{0, 9, 244\},\$ $/* 96*/\{16,7,5\}, \{0,8,86\}, \{0,8,22\},\{64,8,0\},$ $\{19,7,51\},\{0,8,118\},\{0,8,54\},\{0,9,204\},\$ $/*104*/\{17,7,15\},\{0,8,102\},\{0,8,38\},\{0,9,172\},\{0,8,6\},$ $\{0, 8, 134\}, \{0, 8, 70\}, \{0, 9, 236\},\$ $/*112*/\{16,7,9\}, \{0,8,94\}, \{0,8,30\}, \{0,9,156\},$ 18 $\{20,7,99\},\{0,8,126\},\{0,8,62\},\{0,9,220\},\$ $/*120*/\{18,7,27\},\{0,8,110\},\{0,8,46\},\{0,9,188\},\{0,8,14\},$ 19 $\{0, 8, 142\}, \{0, 8, 78\}, \{0, 9, 252\},\$

 $/*128*/\{96,7,0\}, \{0,8,81\},\$ 20 $\{0, 8, 17\}, \{21, 8, 131\}, \{18, 7, 31\}, \{0, 8, 113\}, \{0, 8, 49\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 9, 194\}, \{0, 194\}, \{0, 194\}, \{0, 194\}, \{0, 194\}, \{0, 194\}, \{0, 194\}, \{0, 194\}, \{0, 194\}, \{0, 194\}, \{0, 194\}, \{0, 194\}, \{0, 194\}, \{0, 194\}, \{0, 194\}, \{0, 194\}, \{0, 194\}, \{0, 194\}, \{0, 194\}, \{0, 194\}, \{0, 194\}, \{0, 194\}, \{0$ $/*136*/\{16,7,10\},\{0,8,97\},\{0,8,33\},\{0,9,162\},\{0,8,1\},$ 21 $\{0, 8, 129\}, \{0, 8, 65\}, \{0, 9, 226\},\$ $/*144*/\{16,7,6\}, \{0,8,89\}, \{0,8,25\},\{0,9,146\},$ 22 $\{19,7,59\},\{0,8,121\},\{0,8,57\},\{0,9,210\},\$ $/*152*/\{17,7,17\},\{0,8,105\},\{0,8,41\},\{0,9,178\},\{0,8,9\},$ $\{0, 8, 137\}, \{0, 8, 73\}, \{0, 9, 242\},\$ $/*160*/\{16,7,4\}, \{0,8,85\},\$ 24 $\{0, 8, 21\}, \{16, 8, 258\}, \{19, 7, 43\}, \{0, 8, 117\}, \{0, 8, 53\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 9, 202\}, \{0, 202\}, \{0, 202\}, \{0, 202\}, \{0, 202\}, \{0, 202\}, \{0, 202\}, \{0, 202\},$ $/*168*/\{17,7,13\},\{0,8,101\},\{0,8,37\},\{0,9,170\},\{0,8,5\},$ 25 $\{0, 8, 133\}, \{0, 8, 69\}, \{0, 9, 234\},\$ $/*176*/\{16,7,8\}, \{0,8,93\}, \{0,8,29\}, \{0,9,154\},$ 26 $\{20, 7, 83\}, \{0, 8, 125\}, \{0, 8, 61\}, \{0, 9, 218\},\$ $/*184*/\{18\,,7\,,23\}\,,\{0\,,8\,,109\}\,,\{0\,,8\,,45\}\,,\{0\,,9\,,186\}\,,\ \{0\,,8\,,13\}\,,$ 27 $\{0, 8, 141\}, \{0, 8, 77\}, \{0, 9, 250\},\$ $/*192*/\{16,7,3\}, \{0,8,83\},\$ 2.8 $/*200*/\{17,7,11\},\{0,8,99\},\{0,8,35\},\{0,9,166\},\{0,8,3\},$ 29 $\{0, 8, 131\}, \{0, 8, 67\}, \{0, 9, 230\},\$ $/*208*/\{16,7,7\}, \{0,8,91\}, \{0,8,27\},\{0,9,150\},\$ 30 $\{20, 7, 67\}, \{0, 8, 123\}, \{0, 8, 59\}, \{0, 9, 214\},\$ $/*216*/\{18,7,19\},\{0,8,107\},\{0,8,43\},\{0,9,182\},\{0,8,11\},$ $\{0, 8, 139\}, \{0, 8, 75\}, \{0, 9, 246\},\$ $/*224*/\{16,7,5\}, \{0,8,87\}, \{0,8,23\},\{64,8,0\},\$ $\{19,7,51\},\{0,8,119\},\{0,8,55\},\{0,9,206\},\$ $/*232*/\{17,7,15\},\{0,8,103\},\{0,8,39\},\{0,9,174\},\{0,8,7\},$ 33 $\{0, 8, 135\}, \{0, 8, 71\}, \{0, 9, 238\},\$ $/*240*/\{16,7,9\}, \{0,8,95\}, \{0,8,31\},\{0,9,158\},\$ 34 $\{20, 7, 99\}, \{0, 8, 127\}, \{0, 8, 63\}, \{0, 9, 222\},\$ $/*248*/\{18,7,27\},\{0,8,111\},\{0,8,47\},\{0,9,190\},\{0,8,15\},$ $\{0, 8, 143\}, \{0, 8, 79\}, \{0, 9, 254\},\$ $/*256*/\{96,7,0\}, \{0,8,80\},\$ 36 $\{0, 8, 16\}, \{20, 8, 115\}, \{18, 7, 31\}, \{0, 8, 112\}, \{0, 8, 48\}, \{0, 9, 193\}, \{0, 8, 112\}, \{0, 8, 112\}, \{0, 8, 112\}, \{0, 9, 193\}, \{0, 9, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{0, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1, 112\}, \{1$ $/*264*/\{16,7,10\},\{0,8,96\},\{0,8,32\},\{0,9,161\},\{0,8,0\},$ 37 $\{0, 8, 128\}, \{0, 8, 64\}, \{0, 9, 225\},\$ $/*272*/\{16,7,6\}, \{0,8,88\}, \{0,8,24\}, \{0,9,145\},\$ 38 $\{19,7,59\},\{0,8,120\},\{0,8,56\},\{0,9,209\},\$ $/*280*/\{17,7,17\},\{0,8,104\},\{0,8,40\},\{0,9,177\},\{0,8,8\},$ 39 $\{0, 8, 136\}, \{0, 8, 72\}, \{0, 9, 241\},\$ $/*288*/\{16,7,4\}, \{0,8,84\},\$ 40 $\left\{ 0\,,8\,,20 \right\},\left\{ 21\,,8\,,227 \right\},\left\{ 19\,,7\,,43 \right\},\left\{ 0\,,8\,,116 \right\},\left\{ 0\,,8\,,52 \right\},\left\{ 0\,,9\,,201 \right\},$ $/*296*/\{17,7,13\},\{0,8,100\},\{0,8,36\},\{0,9,169\},\{0,8,4\},$ 41 $\{0, 8, 132\}, \{0, 8, 68\}, \{0, 9, 233\}$ $/*304*/\{16,7,8\}, \{0,8,92\}, \{0,8,28\}, \{0,9,153\},$ 42 $\{20, 7, 83\}, \{0, 8, 124\}, \{0, 8, 60\}, \{0, 9, 217\},\$ $/*312*/\{18,7,23\},\{0,8,108\},\{0,8,44\},\{0,9,185\},\{0,8,12\},$ 43 $\{0, 8, 140\}, \{0, 8, 76\}, \{0, 9, 249\},\$ $/*320*/\{16,7,3\}, \{0,8,82\},\$ 44 $\{0, 8, 18\}, \{21, 8, 163\}, \{19, 7, 35\}, \{0, 8, 114\}, \{0, 8, 50\}, \{0, 9, 197\},$ $/*328*/\{17,7,11\},\{0,8,98\},\{0,8,34\},\{0,9,165\},\{0,8,2\},$ 45 $\{0, 8, 130\}, \{0, 8, 66\}, \{0, 9, 229\},\$ $/*336*/\{16,7,7\}, \{0,8,90\}, \{0,8,26\}, \{0,9,149\},$ 46 $\{20, 7, 67\}, \{0, 8, 122\}, \{0, 8, 58\}, \{0, 9, 213\},\$

```
/*344*/\{18,7,19\},\{0,8,106\},\{0,8,42\},\{0,9,181\},\{0,8,10\},
47
        \{0, 8, 138\}, \{0, 8, 74\}, \{0, 9, 245\},\
         /*352*/\{16,7,5\}, \{0,8,86\}, \{0,8,22\},\{64,8,0\},
48
        \{19, 7, 51\}, \{0, 8, 118\}, \{0, 8, 54\}, \{0, 9, 205\},\
        /*360*/\{17,7,15\},\{0,8,102\},\{0,8,38\},\{0,9,173\},\{0,8,6\},
49
        \{0, 8, 134\}, \{0, 8, 70\}, \{0, 9, 237\},\
        /*368*/\{16,7,9\}, \{0,8,94\}, \{0,8,30\},\{0,9,157\},
50
        \{20, 7, 99\}, \{0, 8, 126\}, \{0, 8, 62\}, \{0, 9, 221\},\
        /*376*/\{18,7,27\},\{0,8,110\},\{0,8,46\},\{0,9,189\},\{0,8,14\},
        \{0, 8, 142\}, \{0, 8, 78\}, \{0, 9, 253\},\
        /*384*/\{96,7,0\}, \{0,8,81\},\
        \{0, 8, 17\}, \{21, 8, 131\}, \{18, 7, 31\}, \{0, 8, 113\}, \{0, 8, 49\}, \{0, 9, 195\},
        /* \, 392 \, * / \, \{16\,,7\,,10\}\,, \{0\,,8\,,97\}\,, \  \  \{0\,,8\,,33\}\,, \{0\,,9\,,163\}\,, \  \  \{0\,,8\,,1\}\,,
        \{0, 8, 129\}, \{0, 8, 65\}, \{0, 9, 227\}
        /*400*/\{16,7,6\}, \{0,8,89\}, \{0,8,25\}, \{0,9,147\},
54
        \{19,7,59\},\{0,8,121\},\{0,8,57\},\{0,9,211\},\
        /*408*/\{17,7,17\},\{0,8,105\},\{0,8,41\},\{0,9,179\},\{0,8,9\},
        \{0, 8, 137\}, \{0, 8, 73\}, \{0, 9, 243\},\
        /*416*/\{16,7,4\}, \{0,8,85\},\
56
       \{0, 8, 21\}, \{16, 8, 258\}, \{19, 7, 43\}, \{0, 8, 117\}, \{0, 8, 53\}, \{0, 9, 203\},
        /*424*/\{17,7,13\},\{0,8,101\},\{0,8,37\},\{0,9,171\},\{0,8,5\},
        \{0, 8, 133\}, \{0, 8, 69\}, \{0, 9, 235\},
        /*432*/\{16,7,8\}, \{0,8,93\}, \{0,8,29\},\{0,9,155\},\
58
        \{20, 7, 83\}, \{0, 8, 125\}, \{0, 8, 61\}, \{0, 9, 219\},\
        /*440*/\{18,7,23\},\{0,8,109\},\{0,8,45\},\{0,9,187\},\{0,8,13\},
        \{0, 8, 141\}, \{0, 8, 77\}, \{0, 9, 251\},\
        /*448*/\{16,7,3\}, \{0,8,83\},\
60
        \{0, 8, 19\}, \{21, 8, 195\}, \{19, 7, 35\}, \{0, 8, 115\}, \{0, 8, 51\}, \{0, 9, 199\},
        /*456*/\{17,7,11\},\{0,8,99\},\{0,8,35\},\{0,9,167\},\{0,8,3\},
61
        \{0, 8, 131\}, \{0, 8, 67\}, \{0, 9, 231\},\
        /*464*/\{16,7,7\}, \{0,8,91\}, \{0,8,27\}, \{0,9,151\},
62
        \{20, 7, 67\}, \{0, 8, 123\}, \{0, 8, 59\}, \{0, 9, 215\},\
         /*472*/\{18,7,19\},\{0,8,107\},\{0,8,43\},\{0,9,183\},\{0,8,11\},
63
        \{0, 8, 139\}, \{0, 8, 75\}, \{0, 9, 247\},\
        /*480*/\{16,7,5\}, \{0,8,87\}, \{0,8,23\},\{64,8,0\},
64
        \{19,7,51\},\{0,8,119\},\{0,8,55\},\{0,9,207\},\
        /*488*/\{17,7,15\},\{0,8,103\},\{0,8,39\},\{0,9,175\},\{0,8,7\},
65
        \{0, 8, 135\}, \{0, 8, 71\}, \{0, 9, 239\},\
        /*496*/\{16,7,9\}, \{0,8,95\}, \{0,8,31\}, \{0,9,159\},
66
       \{20,7,99\},\{0,8,127\},\{0,8,63\},\{0,9,223\},\
        /*504*/\{18,7,27\},\{0,8,111\},\{0,8,47\},\{0,9,191\},\{0,8,15\},
67
       \{0, 8, 143\}, \{0, 8, 79\}, \{0, 9, 255\}
68
  };
  static const static_symbol static_distance_table [32] = \{
69
        /* 0*/\{16,5,1\},\{23,5,257\},\{19,5,17\},\{27,5,4097\},\{17,5,5\},
70
        \{25, 5, 1025\}, \{21, 5, 65\}, \{29, 5, 16385\},\
        /* 8*/\{16,5,3\}, \{24,5,513\}, \{20,5,33\}, \{28,5,8193\}, \{18,5,9\},
71
       \{26, 5, 2049\}, \{22, 5, 129\}, \{64, 5, 0\},\
        /*16*/\left\{16\,,5\,,2\right\},\left\{23\,,5\,,385\right\},\left\{19\,,5\,,25\right\},\left\{27\,,5\,,6145\right\},\ \left\{17\,,5\,,7\right\},
        \{25, 5, 1537\}, \{21, 5, 97\}, \{29, 5, 24577\},\
        /*24*/\{16,5,4\},\{24,5,769\},\{20,5,49\},\{28,5,12289\},\{18,5,13\},
        \{26, 5, 3073\}, \{22, 5, 193\}, \{64, 5, 0\}
74
  };
```

Appendix J Literal Stacker Source File

literal_stacker.cpp

```
#include "literal_stacker.h"
2
  void literal_stacker(
      stream < lld_stream > & in_strm ,
      stream<lld_stream> &out_strm
6) {
  #pragma HLS INTERFACE ap_ctrl_none port=return
7
 #pragma HLS PIPELINE enable_flush
8
9 #pragma HLS INTERFACE axis off port=out_strm //For individual core
       synthesis
  #pragma HLS INTERFACE axis off port=in_strm
    static lld_stream in_buff;
11
    static lld_stream data_regA; //Data register to be filled with
     literals
    static ap_uint <2> state = 0;
14
    if (state == 0) { //Length-Distance State: Continue streaming LD
      pairs through until Literals are encountered
      in_strm >> in_buff;
      if (in_buff.last == 1) \{ //If last pack (No data) \}
        out_strm << in_buff; //Stream out data pack with TLAST high
18
      }
      else{
20
         if (in\_buff.user = 1) { // If data is Length-Distance pair
21
          out_strm << in_buff; //Stream out LD pair
23
        else { // If data is composed of literals
24
           if (in\_buff.keep == 0b1111) \{ //If no literals needed
25
             out_strm << in_buff; //Stream out full data pack
26
          }
27
           else { // Literals needed to fill this data pack
28
             data_regA = in_buff; //Store in RegA
29
             state = 1; //Change to literal state
30
31
           ł
        }
32
      }
33
    }
34
```

```
else if (state = 1) \{ // Literal State: Stack literals with more
35
      literals from the stream. Remain here until LD pair read
      in_strm >> in_buff; //Stream in another data pack
36
      if (in\_buff.last == 1) \{ //If last pack (No data) \}
37
        out_strm << data_regA; //Flush out datapack in RegA
38
        state = 2; //Go to flush state
39
40
      }
      else{
41
        if (in\_buff.user = 1) { // If data is Length-Distance pair
42
          out_strm << data_regA; //Flush out datapack in RegA
43
           state = 2; //Go to flush state
44
45
        }
        else { // If data is composed of literals
46
           if (data_regA.keep = 0b1111) \{ //If no literals needed (
47
     Should never happen)
            out_strm << data_regA; //Stream out full data pack
48
            data_regA = in_buff; //Move new data to regA
49
          }
50
           else if (data_regA.keep = 0b0111) \{ //1 literal needed by
     RegA
             if (in\_buff.keep = 0b0001) { // If number of literals in
     in_buff is exactly 1
               data_regA.data(31,24) = in_buff.data(7,0); //Take 1
     literal from it
               data_regA.keep = 0b1111;
                                                    //Update RegA TKEEP
54
       signal
               out_strm << data_regA;
                                                    //Stream out full
     data pack
               state = 0;
                                              //Return to LD state
56
            }
57
            else if (in_buff.keep = 0b0000) \{ //If data pack is empty
58
       (Should never happen)
              //Do nothing
            }
60
             else { // If number of literals is from 2 to 4 (more than
61
     needed)
               data_regA.data(31,24) = in_buff.data(7,0); //Take 1
62
     literal from it
                                                  //Update RegA TKEEP
               data_regA.keep = 0b1111;
63
       signal
               out_strm << data_regA;
                                                    //Stream out full
64
     data pack
               data_regA.data = in_buff.data >> 8; //Shift in_buff
65
       data and store in RegA
               data_regA.keep = in_buff.keep >> 1; //Shift in_buff
66
      TKEEP signal and store in RegA
            }
67
          }
68
           else if (data_regA.keep = 0b0011) \{ //2 literals needed by
69
     RegA
             if (in\_buff.keep = 0b0011) \{ //If number of literals in
     in_buff is exactly 2
               data_{reg}A.data(31,16) = in_{buff.data(15,0)}; //Take 2
71
     literals
```

data_regA.keep = 0b1111; //Update RegA TKEEP signal 72 $\texttt{out_strm} <\!\!< \texttt{data_regA}; \ //\texttt{Stream} \ \texttt{out} \ \texttt{full} \ \texttt{data} \ \texttt{pack}$ 73 state = 0; //Return to LD state 74 } else if $(in_buff.keep = 0b0001) \{ //If only 1 literal in$ 76 in_buff (less than needed) $data_regA.data(23,16) = in_buff.data(7,0); //Take 1$ literal data_regA.keep = 0b0111; //Update TKEEP 78 } else if $(in_buff.keep = 0b0000) \{ //If data pack is empty$ 80 (Should never happen) //Do nothing 81 } 82 else { // If number of literals is 3 or 4 (more than 83 needed) $data_{reg}A.data(31,16) = in_buff.data(15,0); //Take 2$ 84 literals data_regA.keep = 0b1111; //Update RegA TKEEP signal 85 out_strm << data_regA; //Stream out full data pack 86 data_regA.data = in_buff.data >> 16; //Shift in_buff data and store in RegA data_regA.keep = in_buff.keep >> 2; //Shift in_buff 88 TKEEP signal and store in RegA } 89 } 90 else if $(data_regA.keep = 0b0001) \{ //3 literals needed by$ 91 RegA if $(in_buff.keep = 0b0111)$ { // If number of literals in in_buff is exactly 3 $data_regA.data(31,8) = in_buff.data(23,0); //Take 3$ 93 literals $data_regA$.keep = 0b1111; 94 out_strm << data_regA; 95state = 0; //Return to LD state 96 } 97 else if $(in_buff.keep = 0b0011) \{ //If only 2 literals in$ 98 in_buff (less than needed) $data_regA.data(23,8) = in_buff.data(15,0); //Take 2$ 99 literals $data_regA.keep = 0b0111; //Update TKEEP$ 100 } else if $(in_buff.keep = 0b0001)$ { // If only 1 literal in in_buff (less than needed) $data_regA.data(15,8) = in_buff.data(7,0); //Take 1$ literal $data_regA.keep = 0b0011; //Update TKEEP$ 104 } 105 else if $(in_buff.keep = 0b0000) \{ //If data pack is empty$ 106 (Should never happen) //Do nothing 107 } 108 else { // If number of literals is 4 (more than needed) 109

```
data_regA.data(31,8) = in_buff.data(23,0); //Take 3
110
      literals
               data_regA.keep = 0b1111; //Update RegA TKEEP signal
111
               out_strm << data_regA; //Stream out full data pack
112
               data_regA.data = in_buff.data >> 24; //Shift in_buff
113
      data and store in RegA
114
               data_regA.keep = in_buff.keep >> 3; //Shift in_buff
      TKEEP signal and store in RegA
             }
           }
116
           else if (data_regA.keep = 0b0000) \{ //RegA is empty (Should )
       never happen)
             data_regA = in_buff; //Move new data to regA
118
           }
119
         }
120
       }
121
     }
     else if (state = 2) \{ //Flush state (Needed to space out writes
123
      to output stream)
       out_strm << in_buff; //Stream out LD pair
124
       state = 0; //Return to LD state
125
     }
126
127
  }
```

Appendix K Literal Stacker Header File

literal_stacker.h

1 #include <stdio.h> 2 #include <string.h> 3 #include <ap_int.h> 4 #include <hls_stream.h> #include <assert.h> using namespace hls; //Stream Format: 9 //TDATA: | 31 - Byte3 - 24 | 23 - Byte2 - 16 | 15 - Byte1 - 8 | 710 - Byte0 - 0 TKEEP2 //TKEEP: | TKEEP3 TKEEP1 TKEEP0 12 typedef struct { // Literal, Length/Distance stream structure ap_uint <32> data; //Four bytes of data ap_uint <4> keep; //TKEEP Signals for each byte 14 //TUSER Signal to identify Literal(0) or Lengthbool user; Distance pair(1)bool last; //TLAST AXI-Stream signal 16} lld_stream; 17

Appendix L LZ77 Decoder Source File

LZ77_Decoder.cpp

```
#include "LZ77_Decoder.h"
  #define BUFF_SIZE 32768
  void read_cb(
       ap\_uint < 3> n, //Number of bytes to read (1-4)
6
       ap_uint <2> read_config , //Read configuration
7
       ap_uint <15> address0,
8
       ap_uint <15> address1,
9
       ap_uint <15> address2 ,
       ap_uint <15> address3,
       ap_uint <8> &literal0 , //Output Literals
13
       ap_uint <8> &literal1,
       ap_uint <8> &literal2,
14
       ap_uint <8> &literal3,
       ap\_uint < 8> (& circ\_buff0) [BUFF_SIZE / 4],
16
       ap\_uint < 8> (& circ\_buff1) [BUFF_SIZE / 4],
17
       ap\_uint < 8> (& circ_buff2) [BUFF_SIZE / 4],
18
19
       ap_uint <8> (& circ_buff3) [BUFF_SIZE / 4]
20)
  #pragma HLS INLINE
21
    switch(n)
22
    case 4 :{
23
      switch(read_config){
24
       case 0 :
         literal0 = circ_buff0 [address0]; //Read 4 literals from
26
      buffer
         literal1 = circ_buff1 [address1];
         literal2 = circ_buff2 [address2];
28
         literal3 = circ_buff3 [address3];
29
         break:
30
       case 1:
31
         literal0 = circ_buff1 [address0];
32
         literal1 = circ_buff2 [address1];
33
         literal2 = circ_buff3 [address2];
34
         literal3 = circ_buff0 [address3];
35
         break;
36
```

```
case 2 :
37
         literal0 = circ_buff2 [address0];
38
         literal1 = circ_buff3 [address1];
39
         literal2 = circ_buff0 [address2];
40
         literal3 = circ_buff1 | address3 |;
41
         break:
42
43
       case 3:
         literal0 = circ_buff3 [address0];
44
         literal1 = circ_buff0 [address1];
45
         literal2 = circ_buff1 [address2];
46
         literal3 = circ_buff2 [address3];
47
48
         break;
49
       }
       break;}
50
    case 3 :{
51
       switch(read_config){
52
       case 0:
         literal0 = circ_buff0 [address0]; //Read 3 literals from
54
      buffer
         literal1 = circ_buff1 [address1];
         literal2 = circ_buff2 [address2];
56
57
         break;
58
       case 1 :
         literal0 = circ_buff1 [address0];
59
         literal1 = circ_buff2 [address1];
60
         literal2 = circ_buff3 [address2];
61
         break;
62
       case 2 :
63
         literal0 = circ_buff2 [address0];
64
         literal1 = circ_buff3 [address1];
65
         literal2 = circ_buff0 [address2];
66
         break;
67
       case 3 :
68
         literal0 = circ_buff3 [address0];
         literal1 = circ_buff0 [address1];
70
         literal2 = circ_buff1 [address2];
71
         break;
72
       }
73
74
       break;}
    case 2 :{
75
       switch(read_config){
76
       case 0 :
77
         literal0 = circ_buff0 [address0];
78
         literal1 = circ_buff1 [address1];
79
         break:
80
       case 1 :
81
         literal0 = circ_buff1 [address0];
82
         literal1 = circ_buff2 [address1];
83
         break;
84
       case 2 :
85
         literal0 = circ_buff2 [address0];
86
         literal1 = circ_buff3 [address1];
87
         break;
88
       case 3 :
89
```

```
literal0 = circ_buff3 [address0];
90
             literal1 = circ_buff0 [address1];
91
             break;
92
93
          break; }
94
       case 1 :{
95
96
          switch(read_config){
          case 0 : literal0 = circ_buff0[address0]; break;
97
          case 1 : literal0 = circ_buff1 [address0]; break;
98
          case 2 : literal0 = circ_buff2 [address0]; break;
99
          case 3 : literal0 = circ_buff3 [address0]; break;
100
101
          break;}
102
       }
103
104
105
106
    void write_cb(
          ap\_uint < 3> n, //Number of bytes to write (1-4)
107
          ap_uint <2> write_config , //Write configuration
108
          ap_uint <15> address0,
109
          ap_uint <15> address1 ,
          ap_uint <15> address2,
          ap_uint <15> address3,
          ap_uint <8> literal0 , //Input Literals
          ap_uint <8> literal1 ,
114
          ap_uint <8> literal2 ,
          ap_uint <8> literal3 ,
116
          ap\_uint < 8> (& circ\_buff0) [BUFF_SIZE / 4],
          ap\_uint < 8> (& circ\_buff1) [BUFF\_SIZE / 4],
118
          ap\_uint < 8> (& circ\_buff2) [BUFF_SIZE / 4],
119
          ap_uint <8> (& circ_buff3) [BUFF_SIZE / 4]
120
    ) {
    #pragma HLS INLINE
       switch(n)
123
       case 4 :{
124
          switch(write_config){
          case 0 :
126
             circ_buff0[address0] = literal0; //Print 4 literals to
         buffer head
             \operatorname{circ}_{\operatorname{buff1}}[\operatorname{address1}] = \operatorname{literal1};
128
             \operatorname{circ}_{buff2} [\operatorname{address2}] = \operatorname{literal2};
129
             circ_buff3 [address3] = literal3;
130
             break;
          case 1:
132
             \operatorname{circ}_{buff1} [\operatorname{address0}] = \operatorname{literal0};
             \operatorname{circ}_{buff2}[\operatorname{address1}] = \operatorname{literal1};
134
             \operatorname{circ}_{\operatorname{buff3}}[\operatorname{address2}] = \operatorname{literal2};
135
             \operatorname{circ}_{buff0}[\operatorname{address3}] = \operatorname{literal3};
136
             break;
137
          case 2 :
138
             \operatorname{circ}_{buff2}[\operatorname{address0}] = \operatorname{literal0};
139
             \operatorname{circ_buff3}[\operatorname{address1}] = \operatorname{literal1};
140
             \operatorname{circ}_{buff0} [\operatorname{address2}] = \operatorname{literal2};
141
             \operatorname{circ}_{buff1}[\operatorname{address3}] = \operatorname{literal3};
142
```

```
break;
143
              case 3 :
144
                  \operatorname{circ}_{buff3}[\operatorname{address0}] = \operatorname{literal0};
145
                  \operatorname{circ}_{\operatorname{buff0}}[\operatorname{address1}] = \operatorname{literal1};
146
                  \operatorname{circ}_{\operatorname{buff1}}\left[\operatorname{address2}\right] = \operatorname{literal2};
147
                  \operatorname{circ}_{buff2}[\operatorname{address3}] = \operatorname{literal3};
148
149
                  break;
              }
              break;}
151
          case 3 :{
152
              switch(write_config){
154
              case 0 :
                  \operatorname{circ}_{buff0}[\operatorname{address0}] = \operatorname{literal0};
155
                  \operatorname{circ}_{\operatorname{buff1}}[\operatorname{address1}] = \operatorname{literal1};
156
                  \operatorname{circ}_{buff2}[\operatorname{address2}] = \operatorname{literal2};
157
                  break;
158
              case 1 :
                  circ_buff1 [address0] = literal0;
160
                  \operatorname{circ}_{buff2}[\operatorname{address1}] = \operatorname{literal1};
161
                  \operatorname{circ}_{buff3}[\operatorname{address}_{2}] = \operatorname{literal}_{2};
162
                  break;
163
              case 2 :
164
                   \operatorname{circ}_{buff2}[\operatorname{address0}] = \operatorname{literal0};
165
                   \operatorname{circ_buff3}[\operatorname{address1}] = \operatorname{literal1};
166
                  \operatorname{circ}_{buff0} [\operatorname{address2}] = \operatorname{literal2};
167
                  break;
168
              case 3 :
169
                  \operatorname{circ}_{buff3}[\operatorname{address0}] = \operatorname{literal0};
170
                  \operatorname{circ}_{buff0}[\operatorname{address1}] = \operatorname{literal1};
171
                  circ_buff1 [address2] = literal2;
172
                  break;
173
              }
174
175
              break;}
          case 2 :{
176
              switch(write_config){
177
              case 0 :
178
                   \operatorname{circ}_{buff0}[\operatorname{address0}] = \operatorname{literal0};
179
                  \operatorname{circ}_{\operatorname{buff1}}[\operatorname{address1}] = \operatorname{literal1};
180
                  break;
181
              case 1 :
182
                  \operatorname{circ}_{buff1}[\operatorname{address0}] = \operatorname{literal0};
183
                  \operatorname{circ}_{\operatorname{buff2}}[\operatorname{address1}] = \operatorname{literal1};
184
                  break;
185
              case 2 :
186
                  \operatorname{circ}_{buff2}[\operatorname{address0}] = \operatorname{literal0};
187
                  \operatorname{circ}_{buff3}[\operatorname{address1}] = \operatorname{literal1};
188
189
                  break;
              case 3 :
190
                   circ_buff3 [address0] = literal0;
                  \operatorname{circ}_{buff0}[\operatorname{address1}] = \operatorname{literal1};
192
                  break;
193
              }
194
              break;}
195
196
          case 1 :{
```

```
switch(write_config){
197
       case 0 : circ_buff0[address0] = literal0; break;
198
       case 1 : circ_buff1[address0] = literal0; break;
199
       case 2 : circ_buff2[address0] = literal0; break;
200
       case 3 : circ_buff3 [address0] = literal0; break;
201
202
203
       break;}
     }
204
   }
205
206
   //LZ77 Decoder: Takes in LZ77 commands and outputs decompressed
207
      data (4-byte version)
   void LZ77_Decoder(
208
       stream<lld_stream> &in_strm ,
209
       stream<io_stream> &out_strm
210
  ) {
211
  #pragma HLS INTERFACE ap_ctrl_hs port=return
212
  #pragma HLS INTERFACE axis off port=in_strm //Registers off
213
  #pragma HLS INTERFACE axis off port=out_strm
214
     lld_stream in_buff;
215
     lld_stream literal_buffer;
217
     io_stream out_buff = \{0\};
     ap\_uint <3> state = 0;
218
     ap_uint <9> length;
219
     ap_uint <16> distance;
220
     ap_uint <8> circ_buff0 [BUFF_SIZE/4]; //32 kiB cicular buffer
221
      split into 4 cyclical partitions
     ap_uint <8> circ_buff1 [BUFF_SIZE / 4];
222
     ap_uint <8> circ_buff2 [BUFF_SIZE / 4];
223
     ap_uint <8> circ_buff3 [BUFF_SIZE / 4];
224
     ap_uint<2> read_config; //Points to the circ_buff partition that
225
        literal0 will be read from
     ap\_uint < 2> write_config = 0; //Points to the circ_buff partition
226
        that literal0 will be written to
     ap\_uint < 8 > copy\_array [3][4];
227
  #pragma HLS ARRAY_PARTITION variable=copy_array complete dim=0
228
     ap_uint<2> copy_pointer;
229
     ap\_uint < 15 write\_addr0 = 0;
230
     ap\_uint < 15 write_addr1 = 1;
231
     ap\_uint < 15> write\_addr2 = 2;
232
     ap\_uint < 15> write\_addr3 = 3;
233
     ap_uint <15> read_addr0;
234
     ap_uint <15> read_addr1;
235
     ap_uint <15> read_addr2;
236
     ap_uint <15> read_addr3;
237
     ap_uint <15> first_read_addr;
238
     ap_uint <9> length_remaining; //Length_remaining is the total
239
      number of bytes to be written
     ap_uint <9> distance_remaining; // Distance_remaining is the
240
      number of bytes we can write before the sliding window must be
        reset
     ap\_uint < 8> literal0;
241
     ap_uint <8> literal1;
242
243
     ap_uint <8> literal2;
```

```
ap_uint <8> literal3;
244
245
     Main_Loop: while (1) {
246
247 #pragma HLS PIPELINE
248 #pragma HLS DEPENDENCE variable=circ_buff0 inter false
  #pragma HLS DEPENDENCE variable=circ_buff1 inter false
249
250
  #pragma HLS DEPENDENCE variable=circ_buff2 inter false
  #pragma HLS DEPENDENCE variable=circ_buff3 inter false
251
       if (state = 0) \{ //No Literal Held State \}
252
          in_buff = in_strm.read();
253
         if (in_buff.last) {
254
            break;
255
         }
256
          else{
257
            if (in\_buff.user == 0) { // If data is a literal
258
              literal_buffer = in_buff;
259
              state = 1;
260
            }
261
            else { //Length/Distance pair
262
              length = in_buff.data(31,23);
263
              distance = in_buff.data(15,0);
264
              assert (length >= 3); //DEFLATE min allowed length is 3
265
              assert (length \leq 258); //DEFLATE max allowed length is
266
       258
              assert (distance >= 1); //DEFLATE min allowed distance is
267
        1
              assert (distance \leq 32768); //DEFLATE max allowed
268
       distance is 32768
              read_addr0 = write_addr0 - distance;
269
              read_addr1 = read_addr0 + 1;
270
              read_addr2 = read_addr0 + 2;
271
              read_addr3 = read_addr0 + 3;
272
              read_config = read_addr0 & 3; //Modulo the read_address
273
       to find which buffer partition is read first
              first_read_addr = read_addr0;
274
              length_remaining = length;
275
              if (distance \leq 4) { // If Distance is 1, 2, 3, or 4
276
                state = 3;
                distance_remaining = length; //Distance remaining
278
       equals length, no wrap-around
279
              ł
              else if (distance \leq 7) { // If Distance is 5, 6, or 7
280
                state = 2;
281
                distance_remaining = distance; //Distance remaining
282
       before wrap-around is distance
              }
283
              else { // If Distance is 8 or greater
284
                state = 2;
285
                distance_remaining = length;
286
287
              }
            }
288
         }
289
290
       else if (state == 1) { // Have_Literal State
291
```

```
147
```

```
switch(literal_buffer.keep){
292
         case 0b0001 :
293
            write_cb(1, write_config, write_addr0/4, 0, 0, 0,
294
      literal_buffer.data(7,0), 0, 0, 0, circ_buff0, circ_buff1,
      circ_buff2 , circ_buff3 );
            write_config++;
295
            write_addr0++; write_addr1++; write_addr2++; write_addr3
296
      ++;
            break;
297
         case 0b0011 :
298
            write_cb(2,write_config,write_addr0/4,write_addr1/4,0,0,
299
      literal_buffer.data(7,0),literal_buffer.data(15,8),
                0,0,circ_buff0,circ_buff1,circ_buff2,circ_buff3);
300
            write_config += 2;
301
            write_addr0 += 2; write_addr1 += 2; write_addr2 += 2;
302
      write_addr3 += 2;
           break:
303
         case 0b0111 :
304
            write_cb(3,write_config,write_addr0/4,write_addr1/4,
305
      write_addr2/4,0,literal_buffer.data(7,0),literal_buffer.data
      (15,8),
                literal_buffer.data(23,16),0,circ_buff0,circ_buff1,
306
      circ_buff2 , circ_buff3 );
            write_config += 3;
307
            write_addr0 += 3; write_addr1 += 3; write_addr2 += 3;
308
      write_addr3 += 3;
            break;
309
         case 0b1111 :
310
            write_cb(4,write_config,write_addr0/4,write_addr1/4,
311
      write_addr2/4, write_addr3/4, literal_buffer.data(7,0),
      literal_buffer.data(15,8),
                literal_buffer.data(23,16),literal_buffer.data(31,24),
      circ_buff0 , circ_buff1 , circ_buff2 , circ_buff3 );
            write_addr0 += 4; write_addr1 += 4; write_addr2 += 4;
313
      write_addr3 += 4;
           break;
314
315
         out_buff.data = literal_buffer.data;
316
         out_buff.keep = literal_buffer.keep;
317
         out_strm << out_buff;</pre>
318
         in_buff = in_strm.read();
319
         if (in_buff.last) {
320
           break;
321
         }
322
         else{
323
            if (in\_buff.user == 0) { // If data is a literal
324
              literal_buffer = in_buff;
325
            }
326
            else { //Length/Distance pair
              length = in_buff.data(31,23);
328
              distance = in_buff.data(15,0);
329
              assert(length \ge 3); //DEFLATE min allowed length is 3
330
              assert (length \leq 258); //DEFLATE max allowed length is
331
      258
```

assert (distance >= 1); //DEFLATE min allowed distance is 332 1 assert (distance ≤ 32768); //DEFLATE max allowed 333 distance is 32768 $read_addr0 = write_addr0 - distance;$ 334 $read_addr1 = read_addr0 + 1;$ 335 $read_addr2 = read_addr0 + 2;$ 336 $read_addr3 = read_addr0 + 3;$ 337 read_config = read_addr0 & 3; //Modulo the read_address 338 to find which buffer partition is read first $first_read_addr = read_addr0;$ 339 $length_remaining = length;$ 340 if (distance ≤ 4) { // If Distance is 1, 2, 3, or 4 341 state = 3;342 distance_remaining = length; //Distance remaining 343 equals length, no wrap-around } 344 else if (distance ≤ 7) { // If Distance is 5, 6, or 7 345 state = 2;346 distance_remaining = distance; //Distance remaining 347 before wrap-around is distance ł 348 else { // If Distance is 8 or greater 349 state = 2;350 $distance_remaining = length;$ 351 } 352 } 353 } 354 } 355 else if (state == 2) { // Regular Length-Distance State356 if $(length_remaining >= 4)$ 357 if $(distance_remaining \ge 4)$ 358 read_cb(4,read_config,read_addr0/4,read_addr1/4, 359 read_addr2/4, read_addr3/4, literal0, literal1, literal2, literal3, circ_buff0 , circ_buff1 , circ_buff2 , circ_buff3); if (distance != 32768) { 360 write_cb(4, write_config, write_addr0/4, write_addr1/4, 361 write_addr2/4, write_addr3/4, literal0, literal1, literal2, literal3, circ_buff0, circ_buff1, circ_buff2, circ_buff3); } 362 = literal0; //Write 4 literals to $out_buff.data(7,0)$ 363 output buffer $out_buff.data(15,8) = literal1;$ 364 $out_buff.data(23,16) = literal2;$ 365 $out_buff.data(31,24) = literal3;$ 366 write_addr0 += 4; write_addr1 += 4; write_addr2 += 4; 367 write_addr3 += 4; $out_buff.keep = 0b1111;$ 368 if $(length_remaining == 4) \{ // If only 4 bytes were left \}$ 369 state = 0; //Return to Literal state 370 } 371 else { 372 $length_remaining = 4;$ 373 if $(distance_remaining = 4)$ { 374

distance_remaining = distance; //Reset sliding 375 window read_addr0 = first_read_addr; //Shift addresses back 376 to start $read_addr1 = first_read_addr + 1;$ 377 $read_addr2 = first_read_addr + 2;$ 378 $read_addr3 = first_read_addr + 3;$ 379 } 380 else { 381 $read_addr0 += 4$; $read_addr1 += 4$; $read_addr2 += 4$; 382 $read_addr3 += 4;$ distance_remaining -= 4;383 } 384 } 385 } 386 else if (distance_remaining == 3){ 387 read_cb(3, read_config, read_addr0/4, read_addr1/4, 388 read_addr2/4,0,literal0,literal1,literal2,literal3,circ_buff0, circ_buff1 , circ_buff2 , circ_buff3); if (distance != 32768) { 389 write_cb(3,write_config,write_addr0/4,write_addr1/4, 390 write_addr2/4,0,literal0,literal1,literal2,0,circ_buff0, circ_buff1 , circ_buff2 , circ_buff3); 391 } write_config += 3;392 write_addr0 += 3; write_addr1 += 3; write_addr2 += 3; 393 write_addr3 += 3; = literal0; //Write 3 literals to $out_buff.data(7,0)$ 394 output buffer $out_buff.data(15,8) = literal1;$ 395 $out_buff.data(23,16) = literal2;$ 396 $out_buff.keep = 0b0111;$ 397 $length_remaining = 3;$ 398 distance_remaining = distance; //Reset sliding window 399 read_addr0 = first_read_addr; // Shift addresses back to 400 start $read_addr1 = first_read_addr + 1;$ 401 $read_addr2 = first_read_addr + 2;$ 402 $read_addr3 = first_read_addr + 3;$ 403 } 404 else if (distance_remaining == 2) { 405 read_cb(2,read_config,read_addr0/4,read_addr1/4,0,0, 406 literal0, literal1, literal2, literal3, circ_buff0, circ_buff1, circ_buff2 , circ_buff3); if (distance != 32768) { 407 write_cb(2,write_config,write_addr0/4,write_addr1 408 /4,0,0,literal0,literal1,0,0,circ_buff0,circ_buff1,circ_buff2, circ_buff3); } 409 write_config += 2;410 write_addr0 += 2; write_addr1 += 2; write_addr2 += 2; 411 write_addr3 += 2; $out_buff.data(7,0)$ = literal0; //Write 2 literals to 412 output buffer

 $out_buff.data(15,8) = literal1;$ 413 $out_buff.keep = 0b0011;$ 414 $length_remaining = 2;$ 415 distance_remaining = distance; //Reset sliding window 416 read_addr0 = first_read_addr; // Shift addresses back to 417 start $read_addr1 = first_read_addr + 1;$ 418 $read_addr2 = first_read_addr + 2;$ 419 $read_addr3 = first_read_addr + 3;$ 420 } 421 else if (distance_remaining == 1) { 422 read_cb(1,read_config,read_addr0/4,0,0,0,literal0, 423 literal1, literal2, literal3, circ_buff0, circ_buff1, circ_buff2, circ_buff3); if (distance != 32768) { 424write_cb(1,write_config,write_addr0/4,0,0,0,literal0 425,0,0,0,circ_buff0,circ_buff1,circ_buff2,circ_buff3); } 426 write_config++; 427write_addr0++; write_addr1++; write_addr2++; write_addr3 428 ++;= literal0; //Read literal from out_buff.data(7,0) 429 buffer $out_buff.keep = 0b0001;$ 430 $length_remaining -= 1;$ 431 distance_remaining = distance; //Reset sliding window 432 read_addr0 = first_read_addr; // Shift addresses back to 433 start $read_addr1 = first_read_addr + 1;$ 434 $read_addr2 = first_read_addr + 2;$ 435 $read_addr3 = first_read_addr + 3;$ 436} 437 } 438 else if $(length_remaining == 3)$ { 439 if (distance_remaining >= 3){ 440 read_cb(3,read_config,read_addr0/4,read_addr1/4, 441 read_addr2/4,0,literal0,literal1,literal2,literal3,circ_buff0, circ_buff1 , circ_buff2 , circ_buff3); if (distance != 32768) { 442 write_cb(3,write_config,write_addr0/4,write_addr1/4, 443 write_addr2/4,0,literal0,literal1,literal2,0,circ_buff0, circ_buff1 , circ_buff2 , circ_buff3); } 444 = literal0; //Write 3 literals to $out_buff.data(7,0)$ 445output buffer $out_buff.data(15,8) = literal1;$ 446 $out_buff.data(23,16) = literal2;$ 447 write_config += 3;448 write_addr0 += 3; write_addr1 += 3; write_addr2 += 3; 449 write_addr3 += 3; $out_buff.keep = 0b0111;$ 450state = 0; //Return to Literal state 451} 452 else if (distance_remaining == 2) { 453

15.1	read_cb(2,read_config,read_addr0/4,read_addr1/4,0,0,
454	literal0, literal1, literal2, literal3, circ_buff0, circ_buff1,
	circ_buff2, circ_buff3);
455	$if (distance != 32768) {$
456	write_cb(2, write_config, write_addr0/4, write_addr1
	/4,0,0,literal0,literal1,0,0,circ_buff0,circ_buff1,circ_buff2,
	circ_buff3);
457	}
458	write_config $+= 2;$
459	write_addr0 += 2; write_addr1 += 2; write_addr2 += 2;
	write_addr3 $+= 2;$
460	$out_buff.data(7,0) = literal0; //Write 2 literals to$
	output buffer
461	$out_buff.data(15,8) = literal1;$
462	$out_buff.keep = 0b0011;$
463	length_remaining $-= 2;$
464	distance_remaining = distance; //Reset sliding window
465	$read_addr0 = first_read_addr; // Shift addresses back to$
	start
466	$read_addr1 = first_read_addr + 1;$
467	$read_addr2 = first_read_addr + 2;$
468	$read_addr3 = first_read_addr + 3;$
469	}
470	else if (distance_remaining == 1) {
471	read_cb(1,read_config,read_addr0/4,0,0,0,literal0,
	literal1, literal2, literal3, circ_buff0, circ_buff1, circ_buff2,
	circ_buff3);
472	if (distance $!= 32768)$ {
473	write_cb(1,write_config,write_addr0/4,0,0,0,literal0
	,0,0,0,circ_buff0,circ_buff1,circ_buff2,circ_buff3);
474	}
475	write_config++;
476	write_addr0++; write_addr1++; write_addr2++; write_addr3
	++;
477	$out_buff.data(7,0) = literal0; //Read literal from$
	buffer
478	$out_buff.keep = 0b0001;$
479	$length_remaining = 1;$
480	distance_remaining = distance; //Reset sliding window
481	read_addr0 = first_read_addr; // Shift addresses back to
	start
482	$read_addr1 = first_read_addr + 1;$
483	$read_addr2 = first_read_addr + 2;$
484	$read_addr3 = first_read_addr + 3;$
485	}
486	}
487	else if $(length_remaining = 2)$ {
488	if $(distance_remaining \ge 2)$
489	read_cb(2,read_config,read_addr0/4,read_addr1/4,0,0,
	literal0, literal1, literal2, literal3, circ_buff0, circ_buff1,
	<pre>circ_buff2 , circ_buff3);</pre>
1	if (distance $!= 32768)$ {
490	
490 491	write_cb(2,write_config,write_addr0/4,write_addr1

```
circ_buff3);
             }
492
             write_config += 2;
493
             write_addr0 += 2; write_addr1 += 2; write_addr2 += 2;
494
      write_addr3 += 2;
              out_buff.data(7,0)
                                    = literal0; //Write 2 literals to
495
      output buffer
              out\_buff.data(15,8) = literal1;
496
             out_buff.keep = 0b0011;
497
             state = 0; //Return to Literal state
498
           }
499
           else if (distance_remaining == 1) {
500
             read_cb(1,read_config,read_addr0/4,0,0,0,literal0,
501
      literal1, literal2, literal3, circ_buff0, circ_buff1, circ_buff2,
      circ_buff3);
              if (distance != 32768) {
502
                write_cb(1,write_config,write_addr0/4,0,0,0,literal0
503
      ,0,0,0,circ_buff0,circ_buff1,circ_buff2,circ_buff3);
             }
504
              write_config++;
505
              write_addr0++; write_addr1++; write_addr2++; write_addr3
506
      ++;
                                    = literal0; //Read literal from
             out_buff.data(7,0)
507
      buffer
              out_buff.keep = 0b0001;
508
             length\_remaining = 1;
509
             distance_remaining = distance; //Reset sliding window
             read_addr0 = first_read_addr; // Shift addresses back to
       start
             read_addr1 = first_read_addr + 1;
             read_addr2 = first_read_addr + 2;
513
             read_addr3 = first_read_addr + 3;
514
           }
515
         }
         else if (length_remaining = 1)
           read_cb(1,read_config,read_addr0/4,0,0,0,literal0,literal1
518
      , literal2, literal3, circ_buff0, circ_buff1, circ_buff2, circ_buff3
      );
           if (distance != 32768) {
             write_{cb}(1, write_{config}, write_{addr0}/4, 0, 0, 0, literal0
520
      ,0,0,0,circ_buff0,circ_buff1,circ_buff2,circ_buff3);
           }
           write_config++;
           write_addr0++; write_addr1++; write_addr2++; write_addr3
      ++;
                                  = literal0; //Read literal from
           out_buff.data(7,0)
      buffer
           out\_buff.keep = 0b0001;
525
           state = 0; //Return to Literal state
         }
527
         out_strm << out_buff; //Write to stream
528
       else if (state = 3) \{ // Distance <= 4, Single-Read State before 
530
       Write State
```

```
switch(distance){ //Set up copy array based on distance
      value
         case 1 :
           read_cb(1,read_config,read_addr0/4,0,0,0,literal0,literal1
      , literal2, literal3, circ_buff0, circ_buff1, circ_buff2, circ_buff3
      );
534
            copy\_array[0][0] = literal0; //Store in copy array
            copy_array[0][1] = literal0;
            copy_array[0][2] = literal0;
536
            copy_array[0][3] = literal0;
           break:
538
         case 2 :
539
           read_cb(2,read_config,read_addr0/4,read_addr1/4,0,0,
540
      literal0 , literal1 , literal2 , literal3 , circ_buff0 , circ_buff1 ,
      circ_buff2 , circ_buff3 );
            copy\_array[0][0] = literal0; //Store in copy array
541
            copy_array[0][1] = literal1;
542
            copy_array[0][2] = literal0;
543
            copy_array[0][3] = literal1;
544
           break;
545
         case 3 :
546
            read_cb(3,read_config,read_addr0/4,read_addr1/4,read_addr2
      /4,0,literal0,literal1,literal2,literal3,circ_buff0,circ_buff1
       , circ_buff2 , circ_buff3 );
            copy\_array[0][0] = literal0; //Store 0120 in copy array 0
548
            copy\_array[0][1] = literal1;
549
            copy_array[0][2] = literal2;
550
            copy_array[0][3] = literal0;
            copy_array[1][0] = literal1; //Store 1201 in copy array 1
            copy_array [1][1]
                             = literal2;
            copy\_array[1][2] = literal0;
554
            copy\_array[1][3] = literal1;
            copy\_array[2][0] = literal2; //Store 2012 in copy array 2
556
            copy\_array[2][1] = literal0;
            copy_array [2][2] = literal1;
558
            copy_array[2][3] = literal2;
           break;
560
         case 4 :
561
            read_cb(4,read_config,read_addr0/4,read_addr1/4,read_addr2
562
      /4, read_addr3/4, literal0, literal1, literal2, literal3, circ_buff0
       , circ_buff1 , circ_buff2 , circ_buff3 );
            copy\_array[0][0] = literal0; //Store in copy array
563
            copy\_array[0][1] = literal1;
564
            copy\_array[0][2] = literal2;
565
            copy\_array[0][3] = literal3;
566
           break;
567
         }
568
         copy_pointer = 0;
569
         state = 4;
       }
571
       else if (state == 4) { // Distance <= 4, Write State
572
         if (length_remaining >= 4)
            literal0 = copy_array[copy_pointer][0];
574
            literal1 = copy_array [copy_pointer][1];
575
```

 $literal2 = copy_array[copy_pointer][2];$ $literal3 = copy_array[copy_pointer][3];$ if (distance = 3) { // If distance is 3, shift copy array 578pointer $copy_pointer = (copy_pointer = 2)$? $(ap_uint < 2 >)0b00$: $(ap_uint < 2>)(copy_pointer + 1); //Increment copy pointer or$ set it back to 0 580 write_cb(4,write_config,write_addr0/4,write_addr1/4, 581 write_addr2/4, write_addr3/4, literal0, literal1, literal2, literal3 , circ_buff0 , circ_buff1 , circ_buff2 , circ_buff3); write_addr0 += 4; write_addr1 += 4; write_addr2 += 4; 582 write_addr3 += 4; $out_buff.data(7,0)$ = literal0; //Write 4 literals to 583 output buffer $out_buff.data(15,8) = literal1;$ 584 $out_buff.data(23,16) = literal2;$ 585 $out_buff.data(31,24) = literal3;$ 586 $out_buff.keep = 0b1111;$ 587 if $(length_remaining = 4) \{ // If only 4 bytes were left \}$ 588 state = 0; //Return to Literal state 589 } 590 else { $length_remaining -= 4;$ 592 } 593 } else if $(length_remaining = 3)$ { 595 $literal0 = copy_array [copy_pointer][0];$ 596 $literal1 = copy_array [copy_pointer][1];$ literal2 = copy_array[copy_pointer][2]; 598 write_cb(3,write_config,write_addr0/4,write_addr1/4, 599 write_addr2/4,0,literal0,literal1,literal2,0,circ_buff0, circ_buff1 , circ_buff2 , circ_buff3); write_config += 3;600 write_addr0 += 3; write_addr1 += 3; write_addr2 += 3; 601 write_addr3 += 3;= literal0; //Write 3 literals to $out_buff.data(7,0)$ 602 output buffer $out_buff.data(15,8) = literal1;$ 603 $out_buff.data(23,16) = literal2;$ 604 $out_buff.keep = 0b0111;$ 605 state = 0; //Return to Literal state 606 } 607 else if $(length_remaining = 2)$ { 608 $literal0 = copy_array [copy_pointer][0];$ 609 literal1 = copy_array[copy_pointer][1]; 610 write_cb(2,write_config,write_addr0/4,write_addr1/4,0,0, 611 literal0, literal1,0,0, circ_buff0, circ_buff1, circ_buff2, circ_buff3); write_config += 2;612 write_addr0 += 2; write_addr1 += 2; write_addr2 += 2; 613 write_addr3 += 2; $out_buff.data(7,0)$ = literal0; //Write 2 literals to 614 output buffer

```
out_buff.data(15,8) = literal1;
615
           out_buff.keep = 0b0011;
616
           state = 0; //Return to Literal state
617
         }
618
         else if (length\_remaining = 1){
619
            literal0 = copy_array[copy_pointer][0];
620
621
            write_cb(1,write_config,write_addr0/4,0,0,0,literal0
      ,0,0,0,circ_buff0,circ_buff1,circ_buff2,circ_buff3);
            write_config++;
622
            write_addr0++; write_addr1++; write_addr2++; write_addr3
623
      ++;
                                  = literal0; //Read literal from
624
            out_buff.data(7,0)
      buffer
            out\_buff.keep = 0b0001;
625
           state = 0; //Return to Literal state
626
         }
627
         out_strm << out_buff; //Write to stream
628
       }
629
     }
630
     out_buff.keep = 0b0000; //Set TKEEP signal
631
     out_buff.last = 0b1; //Set TLAST signal
632
     out_strm << out_buff;</pre>
633
634 }
```

Appendix M LZ77 Decoder Header File

LZ77_Decoder.h

2 #include <stdio.h> 3 #include <string.h> 4 #include <ap_int.h> #include <hls_stream.h> #include <assert.h> using namespace hls; 10 typedef struct { // Input AXI-Stream structure ${\tt ap_uint}\,{<}32\!{\!>}$ data; //Four bytes of data 11 ap_uint <4> keep; //TKEEP Signals for each byte 12//TUSER Signal to identify Literal(0) or Length-13 bool user; Distance pair(1)//TLAST AXI-Stream signal bool last; 14 15 } lld_stream; 16 17 typedef struct { // Output AXI-Stream structure ap_uint <32> data; //Four bytes of data 18 ap_uint <4> keep; //TKEEP Signals for each byte 19 bool last; //TLAST AXI-Stream signal 20 21 } io_stream;

Appendix N Byte Packer Source File

byte_packer.cpp

```
#include "byte_packer.h"
2
  unsigned char align_bytes(
      io_strm &data_reg_in,
      io_strm &data_reg_out
5
  ) {
6
  #pragma HLS INLINE
7
    unsigned char bytes_needed;
8
9
    switch(data_reg_in.keep){
10
    case 0b0000 : //All bytes Null
      data_reg_out.data = data_reg_in.data; //Pass data through
      anyway
      data_reg_out.keep = 0b0000;
13
      bytes_needed = 4;
14
      break;
16
    case 0b0001 :
      data_reg_out.data = data_reg_in.data;
17
      data_reg_out.keep = 0b0001;
18
      bytes_needed = 3;
19
      break;
20
    case 0b0010 :
21
      data_reg_out.data = data_reg_in.data >> 8; //Shift all bytes
22
      right by 8 bits
      data_reg_out.keep = 0b0001;
23
      bytes_needed = 3;
24
      break:
25
26
    case 0b0011 :
      data_reg_out.data = data_reg_in.data;
      data_reg_out.keep = 0b0011;
28
      bytes_needed = 2;
29
      break;
30
31
    case 0b0100 :
      data_{reg_out.data} = data_{reg_in.data} >> 16; //Shift all bytes
32
      right by 16 bits
      data_reg_out.keep = 0b0001;
33
```

```
bytes_needed = 3;
34
35
      break;
    case 0b0101 :
36
      data_{reg_out.data(15,8)} = data_{reg_in.data(23,16)}; //Shift
37
      second byte right by 8 bits
      data_reg_out.data(7,0) = data_reg_in.data(7,0); //Copy
38
      bottom byte
      data_reg_out.keep = 0b0011;
39
      bytes_needed = 2;
40
      break:
41
    case 0b0110 :
42
43
      data_{reg_out.data} = data_{reg_in.data} >> 8; //Shift all bytes
      right by 8 bits
      data_reg_out.keep = 0b0011;
44
      bytes_needed = 2;
45
      break;
46
    case 0b0111 :
47
      data_reg_out.data = data_reg_in.data;
48
      data_reg_out.keep = 0b0111;
49
      bytes_needed = 1;
50
      break;
51
    case 0b1000 :
53
      data_reg_out.data = data_reg_in.data >> 24;
      data_reg_out.keep = 0b0001;
54
      bytes_needed = 3;
      break;
56
    case 0b1001 :
57
58
      data_reg_out.data(15,8) = data_reg_in.data(31,24); //Shift
      upper byte right by 16 bits
      data_reg_out.data(7,0) = data_reg_in.data(7,0);
                                                             //Copy
      bottom byte
      data_reg_out.keep = 0b0011;
60
      bytes\_needed = 2;
61
      break:
62
63
    case 0b1010 :
      data_reg_out.data(7,0) = data_reg_in.data(15,8); //Shift
64
      third byte right by 8 bits
      data_reg_out.data(15,8) = data_reg_in.data(31,24); //Shift
65
      upper byte right by 16 bits
      data_reg_out.keep = 0b0011;
66
      bytes_needed = 2;
67
      break;
68
    case 0b1011 :
69
      data_{reg_out}. data(23,16) = data_{reg_in}. data(31,24); //Shift
      upper byte right by 8 bits
      data_reg_out.data(15,0) = data_reg_in.data(15,0); //Copy
      bottom two bytes
      data_reg_out.keep = 0b0111;
72
      bytes_needed = 1;
73
      break;
74
    case 0b1100 :
75
      data_{reg_out.data} = data_{reg_in.data} >> 16; //Shift all bytes
76
      right by 16 bits
      data_reg_out.keep = 0b0011;
77
```

```
bytes_needed = 2;
78
       break;
79
     case 0b1101 :
80
       data_{reg_out}. data(23,8) = data_{reg_in}. data(31,16); // Shift
81
      upper two bytes right by 8 bits
       data_reg_out.data(7,0) = data_reg_in.data(7,0);
                                                             //Copy
82
      bottom byte
       data_reg_out.keep = 0b0111;
83
       bytes_needed = 1;
84
       break:
85
     case 0b1110 :
86
87
       data_{reg_out.data} = data_{reg_in.data} >> 8; //Shift all bytes
      right by 8 bits
       data_reg_out.keep = 0b0111;
88
       bytes_needed = 1;
89
       break;
90
     case 0b1111 :
91
       data_reg_out.data = data_reg_in.data;
92
       data_reg_out.keep = 0b1111;
93
       bytes\_needed = 0;
94
       break;
95
96
     data_reg_out.last = data_reg_in.last; //Pass TLAST signal
97
98
     return bytes_needed;
99
  };
100
101
102 //byte_packer:
  //Takes in 4 byte wide (little-endian) AXI-Stream and checks
103
      accompanying TKEEP signals for presence of null bytes.
  //Will remove null bytes from stream and realign bytes into 4 byte
104
       wide continuous output stream.
  //If TLAST is asserted, will output currently held bytes
105
      regardless of having 4 bytes or not.
  void byte_packer(
106
       stream<io_strm> &in_strm ,
107
       stream<io_strm> &out_strm
108
109)
110 #pragma HLS PIPELINE enable_flush
111 #pragma HLS INTERFACE ap_ctrl_none port=return
112 #pragma HLS INTERFACE axis register both port=in_strm
113 #pragma HLS INTERFACE axis register both port=out_strm
     static io_strm in_buff = \{0\}; //Axi-Stream input buffer
114
     static io_strm data_regA = \{0\}; //First data register to be
      filled
     static io_strm data_regB = \{0\}; //Second data register to be
116
      filled, used to fill RegA
     static unsigned char bytes_neededA = 4; //Number of bytes needed
117
       to fill the data pack currently held in data_regA
     static unsigned char bytes_neededB = 4;
118
     static bool state = 0; //Current machine state, can be 1 or 0
119
120
     if (state = 0) \{ //Pass-through State: Continue streaming full \}
121
      data packs through until null bytes are encountered
```

```
in_strm >> in_buff;
122
       bytes_neededA = align_bytes(in_buff, data_regA); //Align data
123
      pack and find bytes_needed
                                   //If no bytes needed, data already
       if (bytes_neededA == 0) {
124
      aligned
         out_strm << data_regA; //Stream out full data pack
126
       }
       else if (bytes_neededA == 4) {
                                      //If data pack is all null
      bytes
         if (data_regA.last) {
                                      //And TLAST is high
128
           out_strm << data_regA; //Stream out empty data pack with
129
      TLAST high
         }
                           //Otherwise, discard empty datapack
130
       }
                                    //If bytes_needed is 1, 2, or 3
131
       else if (data_regA.last) {
                                   //And TLAST is high
132
         out_strm << data_regA; //Stream out data pack whether it is
      full or not
       }
134
       else { // Bytes needed to fill this data pack
135
         state = 1; //Change to fill state
136
       }
137
138
     else { // Fill State: Replace null bytes with true data bytes from
139
       the stream. Remain here as long as stream is discontinuous
       in_strm >> in_buff; //Stream in another data pack
140
       bytes_neededB = align_bytes(in_buff, data_regB);
                                                             //Align it
141
      and store in Register B
       switch(bytes_neededA){//Check if data is needed in RegA
142
       case 0 : //\text{Reg A} is already full of good data (Should never
143
      happen)
         out_strm << data_regA;
                                           //Stream out full data pack
144
         data_regA.data = data_regB.data >> 8; //Move RegB data to
145
      RegA
         data_regA. keep = data_regB. keep >> 1; //Move RegB TKEEP to
146
      RegA
         bytes\_neededA = bytes\_neededB;
                                               //Update number of bytes
147
       needed by RegA
         break;
148
       case 1 : //1 byte needed by RegA
149
         if (bytes_neededB == 3) { // If number of bytes in RegB is
150
      exactly 1
           data_regA.data(31,24) = data_regB.data(7,0); //Take 1 byte
       from it
                                                //Update RegA TKEEP
           data_regA.keep = 0b1111;
      signal
                                                     //Pass TLAST signal
           data_regA.last = data_regB.last;
           out_strm << data_regA;
                                                //Stream out full data
154
      pack
           state = 0;
                                          //Return to pass-through
      state
         }
156
         else if (bytes_neededB <= 2) { // If number of bytes in RegB is
157
       2 or more (more than needed)
```

```
data_regA.data(31,24) = data_regB.data(7,0); //Take 1 byte
158
       from it
           data_regA.keep = 0b1111;
                                                 //Update RegA TKEEP
159
      signal
           out_strm << data_regA;
                                                 //Stream out full data
160
      pack
161
           data_regA.data = data_regB.data >> 8;
                                                       //Shift RegB data
       and store in RegA
           data_regA.keep = data_regB.keep >> 1;
                                                       //Shift RegB
162
      TKEEP signal and store in RegA
           bytes_neededA = bytes_neededB + 1;
                                                       //Update number
163
      of bytes needed by RegA
         }
164
         else { //RegB has no useable bytes.
165
           if(data_regB.last){ //If RegB is last
166
             data_regA.last = 1;
167
             out_strm << data_regA; //Flush out datapack in RegA
168
             state = 0;
                                //Return to pass-through state
169
           } //Otherwise, read another data pack into RegB next
170
      iteration
         }
         break:
172
173
       case 2 : //2 bytes needed by RegA
         if (bytes_neededB = 2) { // If number of bytes in RegB is
174
      exactly 2
           data_regA.data(31,16) = data_regB.data(15,0); //Take 2
      bytes
           data_regA.keep = 0b1111;
176
           data_regA.last = data_regB.last;
           out_strm << data_regA;
178
           state = 0; //\text{Return to pass-through state}
179
         }
180
         else if (bytes_neededB == 3) { // If only 1 byte in RegB (less
181
      than needed)
           data_{reg}A.data(23,16) = data_{reg}B.data(7,0); //Take 1 byte
182
           data_regA.keep = 0b0111; //Update TKEEP (in case TLAST is
183
      1)
           if (data_regB.last) { // If TLAST is high
184
             data_regA.last = 1;
185
             out_strm << data_regA; //Write out regA
186
             state = 0;
                                  //Return to pass-through state
187
           }
188
           else { // Otherwise
189
             bytes_neededA = 1; //Update number of bytes needed by
190
      RegA
           }
191
         }
         else if(bytes_neededB <= 1){ // If number of bytes in RegB is
193
       3 or more (more than needed)
           data_regA.data(31,16) = data_regB.data(15,0); //Take 2
194
      bvtes
           data_regA.keep = 0b1111;
                                                  //Update RegA TKEEP
195
      signal
```

```
out_strm << data_regA;
                                                   //Stream out full data
196
       pack
           data_regA.data = data_regB.data >> 16;
                                                            //Shift RegB
197
      data and store in RegA
           data_regA.keep = data_regB.keep >> 2;
                                                         //Shift RegB
198
      TKEEP signal and store in RegA
            bytes_neededA = bytes_neededB + 2;
                                                         //Update number
199
      of bytes needed by RegA
         }
200
         else { //RegB has no useable bytes
201
            if(data_regB.last){ //If RegB is last
202
             data_regA.last = 1;
203
             out_strm << data_regA; //Flush out datapack in RegA
204
                                  //Return to pass-through state
              state = 0;
205
           } //Otherwise, read another data pack into RegB next
206
      iteration
         }
207
         break;
208
       case 3 : //3 bytes needed by RegA
209
         if (bytes_neededB = 1) { // If number of bytes in RegB is
210
      exactly 3
           data_regA.data(31,8) = data_regB.data(23,0); //Take 3
211
      bytes
           data_regA.keep = 0b1111;
212
           data_regA.last = data_regB.last;
213
           out_strm << data_regA;
214
            state = 0; //\text{Return to pass-through state}
215
         }
         else if (bytes_neededB = 2) { // If only 2 bytes in RegB (less
217
       than needed)
           data_regA.data(23,8) = data_regB.data(15,0); //Take 2
218
      bytes
           data_regA.keep = 0b0111; //Update TKEEP (in case TLAST is
219
      1)
           if (data_regB.last) {
220
              data_regA.last = 1;
221
             out_strm << data_regA; //Write out regA
222
              state = 0;
                                  //Return to pass-through state
           }
224
           else{
225
              bytes_neededA = 1;
226
           }
227
         }
228
         else if (bytes_neededB == 3) { // If only 1 byte in RegB (less
229
      than needed)
           data_regA.data(15,8) = data_regB.data(7,0); //Take 1 byte
230
           data_{regA}. keep = 0b0011; //Update TKEEP (in case TLAST is
231
      1)
           if (data_regB.last) {
232
             data_regA.last = 1;
233
             out_strm << data_regA; //Write out regA
234
                                  //Return to pass-through state
              state = 0;
235
           }
236
237
            else {
```

```
bytes\_neededA = 2;
238
           }
239
         }
240
         else if (bytes_neededB == 0) { // If number of bytes in RegB is
241
       4 (more than needed)
           data_regA.data(31,8) = data_regB.data(23,0); //Take 3
242
      bytes
           data_regA.keep = 0b1111;
                                                 //Update RegA TKEEP
243
      signal
           out_strm << data_regA;
                                                 //Stream out full data
244
      pack
245
           data_regA.data = data_regB.data >> 24;
                                                           //Shift RegB
      data and store in RegA
           data_regA.keep = data_regB.keep >> 3;
                                                         //Shift RegB
246
      TKEEP signal and store in RegA
           bytes_neededA = bytes_neededB + 3;
                                                         //Update number
247
      of bytes needed by RegA
         }
248
         else{ //RegB has no useable bytes
249
           if (data_regB.last) { // If RegB is last
250
             data_regA.last = 1;
251
             out_strm << data_regA; //Flush out datapack in RegA
252
             state = 0;
                                 //Return to pass-through state
253
           } //Otherwise, read another data pack into RegB next
254
      iteration
         }
255
         break;
256
       case 4 : //RegA is empty (Should never happen)
257
         data_regA.data = data_regB.data >> 8; //Move RegB data to
258
      RegA
         data_regA.keep = data_regB.keep >> 1; //Move RegB TKEEP to
259
      RegA
         bytes\_neededA = bytes\_neededB;
                                                //Update number of bytes
260
       needed by RegA
         break;
261
       }
262
263
264
  }
```

Appendix O Byte Packer Header File

byte_packer.h

1 #include <stdio.h> 2 #include <string.h> 3 #include <ap_int.h> #include <hls_stream.h> using namespace hls; template < int D >8 9 struct axi_strm { //D bits of data ap_uint <D> data; ap_uint <D/8> keep; //TKEEP signals for each byte 11 bool last; //TLAST AXI-Stream signal 1213 }; 14 //Stream Format: // | 31 - Byte3 - 24 | 23 - Byte2 - 16 | 15 - Byte1 - 8 | 7 -Byte0 - 0TKEEP3 TKEEP2 TKEEP1 TKEEP0 16 11 17 typedef axi_strm <32> io_strm; 18