

Hybrid Fuzzy Monte Carlo Agent-Based Modeling of Workforce Motivation and Performance in Construction

Abstract

Purpose: This paper covers the development of a methodology for hybrid fuzzy Monte Carlo agent-based simulation (FMCABS) and its implementation on a parametric study of construction crew performance.

Design/methodology/approach: The developed methodology uses fuzzy logic, Monte Carlo simulation, and agent-based modeling to simulate the behavior of construction crews and predict their performance. Both random and subjective uncertainties are considered in model variables.

Findings: The developed methodology was implemented on a real case involving the parametric study of construction crew performance to assess its applicability and suitability for this context.

Research limitations/implications: This parametric study demonstrates a practical application for the hybrid FMCABS methodology. Though findings from this study are limited to the context of construction crew motivation and performance, the applicability of the developed methodology extends beyond the construction domain.

Practical implications: This research will help construction practitioners to predict and improve crew performance by taking into account both random and subjective uncertainties.

Social implications: This research will advance construction modeling by allowing for the assessment of social interactions among crews and their effects on crew performance.

Originality/value: The developed hybrid FMCABS methodology represents an original contribution, as it allows agent-based models to simultaneously process all types of variables (i.e., deterministic, random, and subjective) in the same simulation experiment, while accounting for

23 interactions among different agents. In addition, the developed methodology is implemented in a
24 novel and extensive parametric study of construction crew performance.

25 **Keywords:** Hybrid simulation; agent-based modeling; Monte Carlo simulation; fuzzy logic;
26 construction; motivation; crew performance

27 **Paper type:** Research paper

28 **Introduction**

29 Construction simulation is the process of developing and executing computer-based models
30 of construction systems (e.g., construction processes and project management practices) to
31 understand their underlying behaviors (AbouRizk, 2010). Simulation methods, such as agent-
32 based modeling (ABM), system dynamics (SD), discrete event simulation (DES), and Monte Carlo
33 simulation, have been used to solve construction problems. Each of these simulation methods
34 offers its own unique capabilities in modeling construction systems (Raoufi et al., 2016). However,
35 models based on one simulation method alone have limitations, primarily due to their inability to
36 capture all aspects of complex construction systems.

37 Hybrid simulation (i.e., integration of two or more simulation methods) offers the potential to
38 combine the strengths of multiple methods. Recently, simulation researchers have made efforts to
39 leverage the advantages of hybrid simulation to develop hybrid simulation frameworks for
40 modeling dynamic and complex construction systems. Although these frameworks and models are
41 suitable for the simulation of construction systems, this research is still in its early stages of
42 development, and there are research gaps that need to be filled in the area of hybrid simulation.
43 The applicability of current hybrid simulation frameworks needs to be tested and expanded for
44 different types of construction applications. In addition, in order to improve the modeling of
45 construction systems, hybrid simulation frameworks and models must be advanced to allow the

46 assessment of different types of variables simultaneously. To address this gap, this paper provides
47 an innovative hybrid fuzzy Monte Carlo agent-based simulation (FMCABS) methodology that
48 allows for the assessment of both random and subjective uncertainties in the same simulation
49 environment.

50 One of the main contributions of this paper is the extension of a hybrid FMCABS
51 methodology, which allows agent-based models to simultaneously process all types of variables
52 (i.e., deterministic, random, and subjective) in the same simulation experiment, while accounting
53 for interactions between different agents. Previous research on construction crew performance
54 focused either on a single experiment, or on a scenario-based analysis using limited simulation
55 runs and limited variations of model parameters. Thus, a major contribution of this paper beyond
56 existing work, in particular Raoufi and Fayek (2020), is the implementation of the developed
57 methodology in a novel and extensive parametric study of construction crew performance.

58 **Literature review of existing hybrid simulation research**

59 Models based on one simulation method alone have limitations in the assessment of
60 construction systems, primarily due to their inability to capture different types of variables:
61 deterministic (i.e., crisp), random (i.e., stochastic), and subjective (i.e., fuzzy) and relationships
62 (e.g., agent interactions) simultaneously. Hybrid simulation was developed to address the
63 limitations of the one-simulation method by enabling integration with other methods. However,
64 the term hybrid simulation has been used in existing literature to define a range of different models,
65 such as simulation models that incorporate both continuous and discrete variables (e.g., system
66 dynamics–discrete event simulation (SD-DES) models) (Nasirzadeh et al., 2008), models
67 integrating two or more simulation methods (e.g., agent-based modeling–system dynamics (ABM-
68 SD) models) (Nasirzadeh et al., 2018), models integrating simulation with fuzzy logic (Gerami

69 Seresht et al., 2018; Raoufi et al., 2018;), and models integrating simulation with other analytical
70 methods (e.g., simulation integrated with optimization) (Brailsford et al., 2019).

71 *Hybrid simulation models of system dynamics and discrete event simulation*

72 One major area of hybrid simulation research has focused on developing SD-DES
73 frameworks, methodologies, and models. SD is a simulation method used for modeling the
74 dynamic behavior of complex systems that involve interdependent components with time-varying
75 interactions, as well as multiple feedback processes (Nasirzadeh et al., 2008). DES is a simulation
76 method used for modeling systems where changes occur at discrete points in time. DES is an
77 appropriate method for modeling process-type systems (e.g., earthmoving operations), in which
78 several activities are executed in a sequence and for a number of repetitions.

79 Two fundamental differences between DES and SD make the integration of these two methods
80 difficult. Firstly, DES has discrete state changes, while SD has continuous state changes. Secondly,
81 DES models a system as a network of queues and activities, while SD models a system as a
82 network of stocks and flows. Due to these differences, many early hybrid SD-DES simulation
83 packages and models relied more heavily on either SD or DES, with the addition of very limited
84 features from the other method (Brailsford et al., 2019; Chatha and Weston, 2006).

85 Recently, better methodologies have been proposed for the development of hybrid DES and
86 SD models, which address the aforementioned challenges. Helal et al. (2007) proposed a hybrid
87 SD-DES methodology to simulate manufacturing enterprise systems, while maintaining the
88 integrity of the two simulation methods and not allowing one to dominate the other. Alvanchi et
89 al. (2011) proposed a hybrid SD-DES architecture that controls the interaction between the SD and
90 DES models to prevent the overloading of hybrid models caused by excessive calculations.
91 Another hybrid modelling framework was proposed by Moradi et al. (2015), which combines SD

92 and DES to simulate the continuous and operational variables affecting the performance of
93 construction projects. A hybrid SD-DES framework was also developed by Hwang et al. (2016)
94 for immediate facility restoration planning after a catastrophic disaster. Finally, Morgan et al.
95 (2017) provided a framework to compare the features of various SD-DES frameworks, such as
96 form and frequency of interactions in the hybrid SD-DES model.

97 *Hybrid simulation models using ABM*

98 Although the literature on hybrid SD-DES simulation is extensive, there are very few studies
99 that focus on integration of ABM with other simulation methods. Mahdavi and Hastak (2004)
100 developed a hybrid ABM–SD model, which uses SD modules built within the agents of an ABM
101 module to quantify the effect of adaptive bidding strategies. Their hybrid ABM-SD model enables
102 the comparison of bidding strategies by utilizing regular and adaptive agents. Lorenz and Jost
103 (2006) compared simulation techniques and emphasized the need to develop hybrid approaches
104 that use DES, SD, and ABM. They developed an initial concept idea for an orientation framework
105 that aligns purpose, object characteristics, and methodology for choosing and/or integrating DES,
106 SD, and ABM. However, Lorenz and Jost (2006) did not propose a methodology or model for
107 hybridization of any of these simulation methods. Djanatliev and German (2013) developed a
108 hybrid simulation methodology, which uses SD to generate agents dynamically from an SD model,
109 and then uses the generated agents in an ABM-DES hybrid model for modeling the effects of
110 medical products on agents in hospitals. Although the authors used SD, ABM, and DES methods
111 in their work, they only used the output of the SD model as the input for their ABM-DES hybrid
112 model. Nasirzadeh et al. (2018) developed a hybrid SD-ABM framework, which was then used by
113 Khanzadi et al. (2018) to develop a labor productivity model.

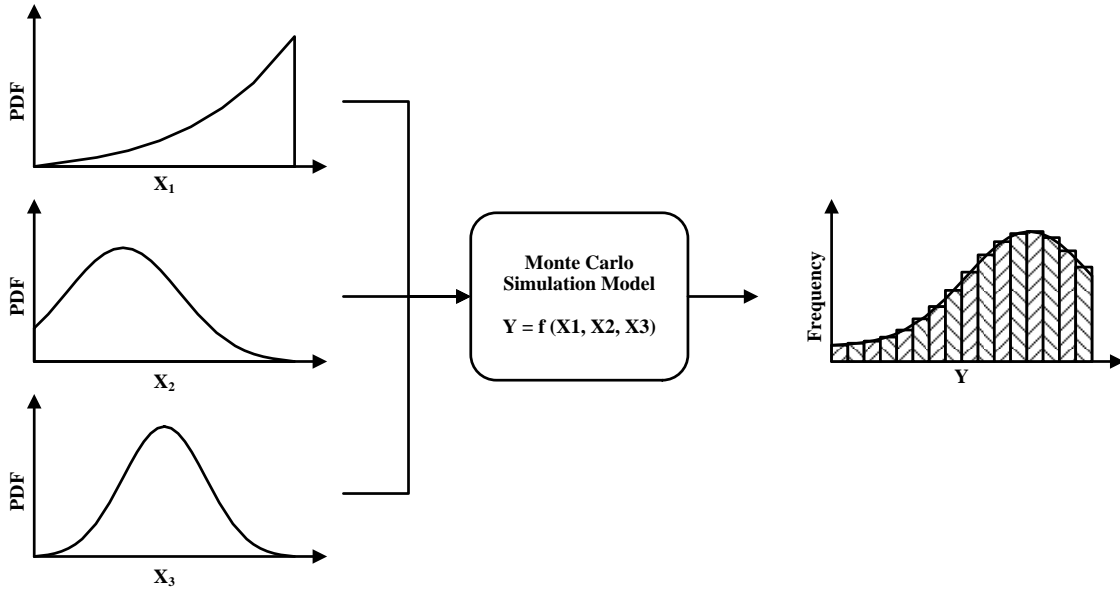
114 ***Hybrid simulation research gaps***

115 A review of existing literature indicates that research on hybrid simulation, which integrates
116 ABM with other simulation methods is in its early stages of development, as compared to hybrid
117 simulation methodologies and models that integrate SD and DES. Hybrid ABM research has
118 recently gained more attention, including the integration of ABM with DES and SD (Nasirzadeh
119 et al., 2018). The current hybrid simulation models provide more powerful simulation tools, but
120 most of these hybrid models only process deterministic and random variables. Therefore, there is
121 a need to advance research on hybrid ABM simulation and its applications by allowing all types
122 of variables to be processed in the same hybrid ABM. This paper bridges the gap in hybrid ABM
123 simulation research by integrating ABM with Monte Carlo simulation and fuzzy logic, developing
124 a methodology for hybrid fuzzy Monte Carlo ABM, and implementing the developed methodology
125 in a real construction case. The developed methodology and its application enables the assessment
126 of all three types of variables in the same hybrid ABM.

127 **Fuzzy Monte Carlo simulation method**

128 In simulation modeling, uncertainty has traditionally been represented by random variables,
129 which are in turn determined by probability density functions (PDFs) based on probability theory.
130 Therefore, in many previous ABM studies related to the construction domain, the use of PDFs and
131 Monte Carlo simulation for experimentation with random variables enabled the handling of
132 random uncertainty in ABM.

133 Figure 1 shows the Monte Carlo simulation method. In this model, the histogram provided for
134 the output variable Y is based on the PDFs of the input variables X_1 , X_2 , and X_3 .



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Figure 1. Monte Carlo simulation method.

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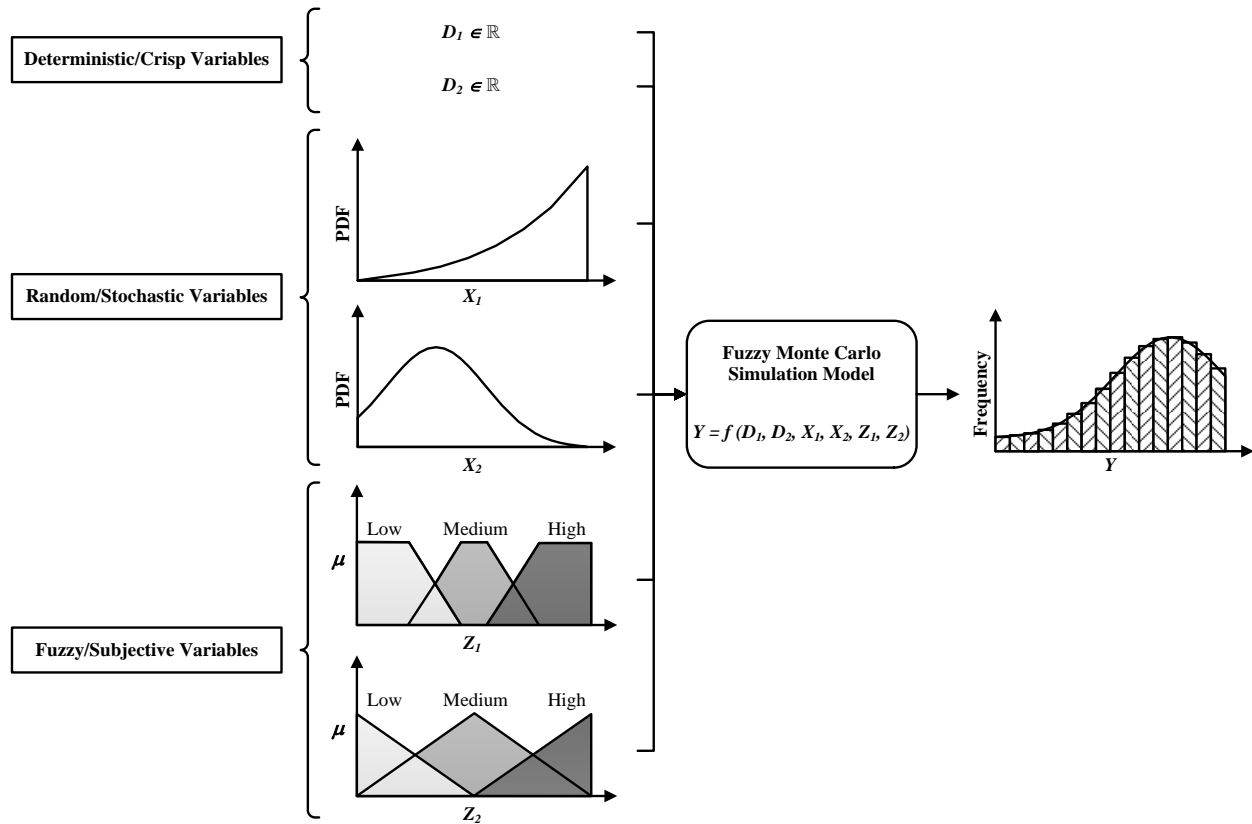
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However, probability theory and PDFs only address random uncertainty, but not the subjective uncertainty associated with the vagueness of subjective information. Subjective uncertainty may arise from the subjective assessment of precise variables by humans (e.g., high temperature); from variables that are not precisely measurable or defined by deterministic or random values (e.g., crew motivation); or from relationships that cannot be precisely represented either by mathematical formulae or regression equations (e.g., the relationship between crew motivation and crew performance). Thus, there was a need to develop a hybrid methodology in ABM that allows handling of both types of uncertainties in construction contexts. Zadeh (2015) introduced fuzzy set theory to handle subjective uncertainty. In addition, research by Raoufi and Fayek (2020) demonstrates how to integrate fuzzy logic and Monte Carlo simulation in ABM. This fuzzy Monte Carlo simulation methodology uses a combination of probability theory and fuzzy set theory to simultaneously handle random and subjective uncertainties in the same construction model. Figure 2 shows the simulation method and the three different types of input variables that a fuzzy Monte Carlo simulation model can handle. Deterministic variables D_1 and D_2 were identified, based on

151 their exact value in the fuzzy Monte Carlo simulation model. Random variables X_1 and X_2 were
 152 determined using PDFs, and subjective variables Z_1 and Z_2 were determined using membership
 153 functions.



154
 155 **Figure 2.** Fuzzy Monte Carlo simulation method.

156 In Figure 2, the output of the fuzzy Monte Carlo simulation model Y is represented by a
 157 histogram, which was generated using D_1 , D_2 , X_1 , X_2 , Z_1 , and Z_2 . The final output of the fuzzy
 158 Monte Carlo agent-based simulation depends on the type of output of the fuzzy agent-based model
 159 (i.e., a subjective variable or a deterministic variable). When the output of the fuzzy agent-based
 160 model is a subjective variable, the output of fuzzy Monte Carlo agent-based model is a fuzzy
 161 random variable. When the output of the fuzzy agent-based model is a crisp variable, the output of
 162 fuzzy Monte Carlo agent-based model is a histogram that shows the frequency with which each

163 output value was observed over all simulation runs. The present research used the above fuzzy
164 Monte Carlo simulation method in order to develop a hybrid FMCABS methodology, which was
165 then implemented on a parametric study of construction crew performance.

166 **Methodology for hybrid fuzzy Monte Carlo agent-based simulation**

167 *Defining the types of variables for the hybrid fuzzy Monte Carlo agent-based simulation model*

168 Three types of variables were defined in the hybrid FMCABS model discussed in this paper:
169 deterministic variables; random variables; and subjective variables. The types of variables in a
170 hybrid FMCABS model should be defined based on past literature and/or actual field data (if
171 available).

172 The subjective variables in a hybrid FMCABS model should also be defined. Any variables
173 that are not precisely measurable or defined by deterministic or random values involve subjective
174 uncertainty (e.g., crew motivation), and should be considered as subjective variables. All
175 subjective variables should be determined by membership functions using previous research or
176 actual field data. The remaining variables that do not incorporate subjective uncertainty are either
177 random (e.g., susceptibility, meaning the probability that interaction among crews leads to changes
178 in crew motivation) or deterministic variables (e.g., crew size). Those variables that involve
179 random uncertainty are random variables and should be determined by probability density
180 functions (PDFs) using previous research or actual field data. Variables that do not show any
181 uncertainty (e.g., crew size) are deterministic and are specified by numeric values. In the present
182 research, variables (i.e., deterministic, random, and subjective) were selected based on actual field
183 data.

184 *Developing the main simulation environment*

185 Simulation model parameters and methods were defined in the main simulation environment.
186 Agent type and population were the model parameters. In addition, the following methods were
187 defined: agent creation; contacting the fuzzy inference system at simulation run time; simulation
188 methods (e.g., Java functions) for running experiments; and methods for obtaining and
189 representing the results of simulations.

190 *Defining the characteristics of each agent class*

191 Agent classes were used to model different type of agents in the system. The hybrid FMCABS
192 model can include several classes of agents. Each agent class has its own unique characteristics,
193 including attributes, behaviors, and interactions. The next sections discuss how to determine the
194 characteristics of agent classes.

195 *Determining agent attributes*

196 Each agent can have different attributes (e.g., crew size), which need to be defined by different
197 types of variables (e.g., deterministic, random, or subjective) in the hybrid FMCABS model. All
198 of these variables are determined using actual field data when field data are available. If field data
199 are not available, they can be determined using previous research or expert judgement. In the case
200 that none of these sources are available, variables can be hypothetically defined by the user to
201 experiment with different simulation scenarios.

202 Probabilistic variables are mostly determined by curve fitting using statistical distributions
203 that are based on available field data (Raoufi and Fayek, 2018c; Azar and Ansari, 2017). Subjective
204 variables are defined by membership functions using one of two available types of methods:
205 expert-driven or data-driven methods. Expert-driven methods include horizontal, vertical, pairwise
206 comparison, intuition, inference, and exemplification methods (Fayek and Lourenzutti, 2018).

207 Data-driven methods include fuzzy machine learning techniques (e.g., fuzzy clustering). Fuzzy C-
208 means (FCM) clustering is a machine learning technique, where each data point belongs to each
209 cluster and is defined by a membership value ranging from zero to one (Bezdek, 2013).

210 In this paper, FCM clustering was used to develop the membership functions of subjective
211 variables. Membership functions, which are shown as linguistic terms, express the degree to which
212 a data point representing a subjective variable (e.g., crew motivation) belongs to a fuzzy set (e.g.,
213 low motivation). Gaussian membership functions were used to represent the subjective variables
214 of agents, as they are continuous and smooth functions, and are suitable for optimization. The
215 Gaussian membership function is shown below in Equation 1.

$$216 \quad A = e^{-\left[\frac{(x-\mu)^2}{2\sigma^2}\right]}, \quad (1)$$

217 where x represents the value of the subjective variable, A represents the membership function for
218 a linguistic term, μ is the modal value, and σ is the standard deviation. The modal value and
219 standard deviation of each membership function were determined using FCM clustering (Pedrycz
220 2013; Raoufi and Fayek 2018c).

221 Determining agent behavioral rules

222 The type of behavior of each agent needs to be defined by agent behavioral rules, which are
223 mathematical representatives of what agents decide to do, based on the state of the system at both
224 current and previous time steps (Dash et al., 2003). Several methods have been used to define
225 agent behavioral rules. For example, behavioral rules may be defined from simple rules using
226 mathematical formula, or from conditional rules to more complex rules using regression models
227 or fuzzy relationships.

228 In some of the previous research on ABM, agent behavioral rules were defined using
229 mathematical formulae and regression equations (Papadopoulos, 2016). Both of these methods are

230 useful in ABM models when the system involves random uncertainty, but they are not equipped
231 for handling subjective uncertainty. In order to model agent behavioral rules in a system that
232 involves subjective uncertainty, fuzzy rules must be defined to represent agent behavior. Several
233 methods have been suggested for defining fuzzy rules in this context. Ahn and Lee (2015) used
234 past literature on theories of human behavior to determine rules for agents' absence behavior. This
235 method is useful if there are no data available but there is reliable literature. Garro and Russo
236 (2010) developed an expert-oriented methodology for agent-based modeling; they used an expert-
237 driven approach (i.e., using domain expert judgment) to define agent behavioral rules. This
238 approach is limited, as it relies heavily on human judgment, but it is useful when there is lack of
239 actual data and there is access to a sufficient sample of domain experts. Cui and Hastak (2006)
240 developed an agent-based learning model for bidding decision making, which used system
241 dynamics to model the learning process of agents in order to improve the performance of bidding
242 decisions. Recently, data-driven approaches (e.g., fuzzy machine learning techniques) have been
243 introduced to define agent behavioral rules. Data-driven approaches use actual data to generate
244 agent-behavioral rules. Raoufi and Fayek (2018c) described a set of methodological steps for
245 generating fuzzy rules, which represent agent behavioral rules in a system, using fuzzy clustering
246 (e.g., FCM clustering). FCM clustering minimizes an objective function, which represents the sum
247 of squared distances of data instances to cluster centers. In this paper, FCM clustering was used to
248 define agent behavioral rules of construction crews from collected field data, as well as the
249 membership functions representing agent attributes.

250 *Determining agent interactions and learning*

251 Agent interactions describe how interactions occur and what happens after each interaction
252 between agents. Interactions are either static or dynamic. Dynamic interactions depend on the state

253 of other agents or the system at any point in time, while static interactions do not. When agents are
254 humans, their interactions are mostly dynamic, due to the feedback they receive from other agents
255 (e.g., observing the behavior of others) and the environment (e.g., observing changes in the
256 environment) (Azar and Ansari, 2017; Ben-Alon and Sacks, 2017). This change in the behavior of
257 agents based on the feedback received from the environment or other agents is a learning process,
258 as described by Cui and Hastak (2006). However, there are some agents (i.e., zealot agents) that
259 have static interactions and do not change their attributes or behavior following interactions with
260 others.

261 Different methods have been used to define agent interactions and agent learning, such as
262 using random interactions, mathematical formulae, regression models, and system dynamics
263 models. When agents are humans, their interactions are mostly dynamic, and their learning process
264 can be represented by mathematical formulae (Azar and Ansari, 2017; Ben-Alon and Sacks, 2017)
265 or system dynamics models (Cui and Hastak 2006). Models of behavior dynamics of humans are
266 also often used to define mathematical formulae for agent interactions in cases where agents
267 learning includes changing their behavior following interactions (Azar and Ansari, 2017; Mobilia
268 et al., 2007; Hegselmann and Krause, 2002; Deffuant et al., 2000). Mathematical formulae for
269 agent interactions and learning are used to calculate the attributes of an agent at a time step, based
270 on both that agent's attributes at previous time steps, as well as the attributes of other agents at
271 previous time steps. System dynamics for agent learning is used to define a learning loop whereby
272 agents record other agents' attributes, environment states, and actions of other agents (Cui and
273 Hastak 2006). Then agent behavior is defined based on the feedback the agent receives from other
274 agents and the environment.

275 In the present research, the mathematical equation developed by Raoufi and Fayek (2018c)
 276 shown in Equation 1 was used to represent the effect of the interactions of crew agents on the level
 277 of motivation of a crew and represents a learning process among crews. The level of motivation
 278 of a crew agent is calculated based on the level of motivation of that crew and the level of
 279 motivation of other crews on the project.

$$280 \quad M_i^t = (1 - Z \times C \times S) \times M_i^{t-1} + (Z \times C \times S) \times \frac{\sum_{j=1}^N M_j^{t-1}}{N}, \quad (1)$$

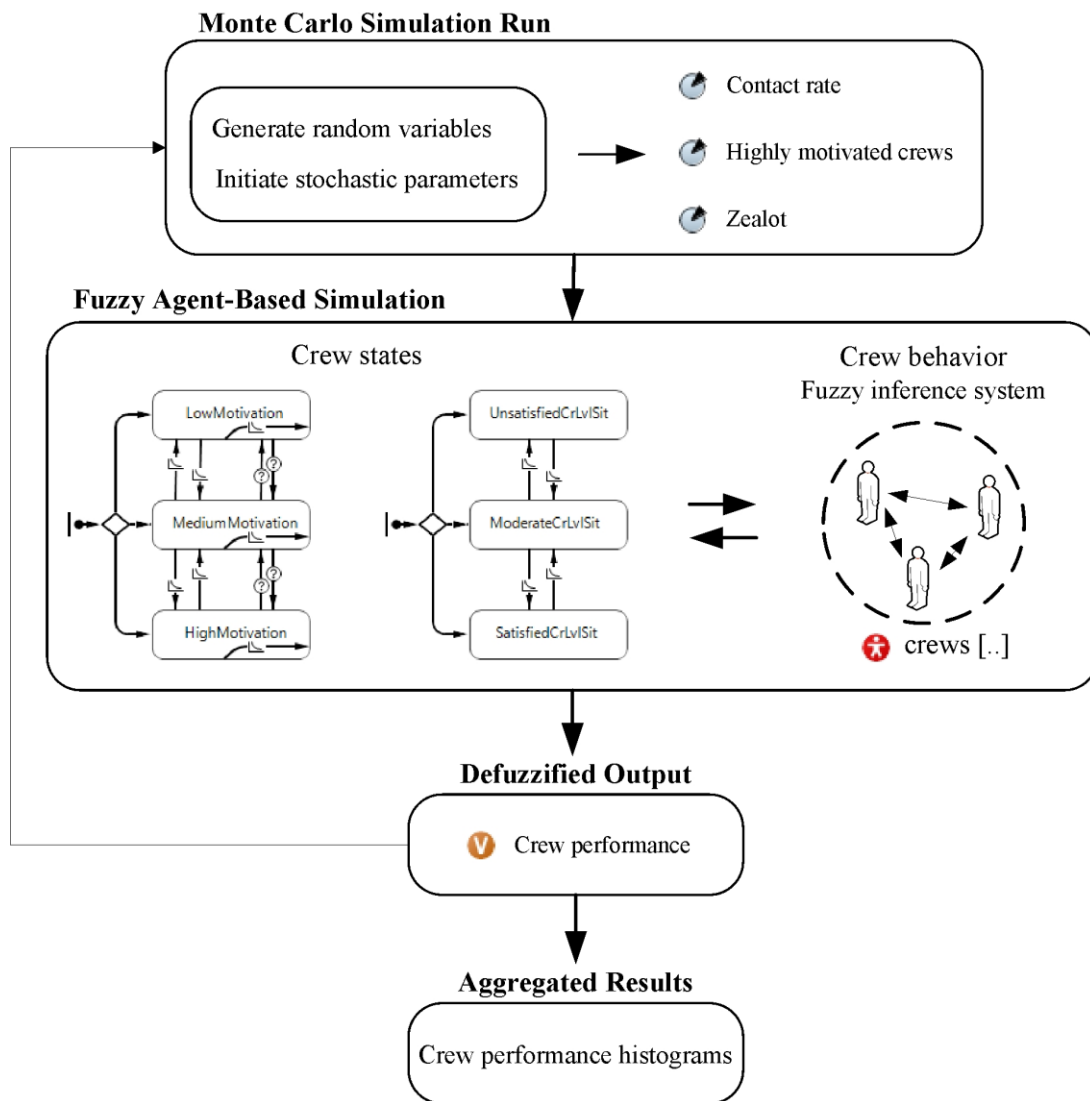
281 where i and j are crew indices, t and $t-1$ refer to the current and the previous simulation time steps,
 282 M refers to crew motivation, Z refers to the type of agent (i.e., zealot or non-zealot agent), C refers
 283 to crew agent contact rate (i.e., the rate at which crew agents contact each other over the simulation
 284 time unit), S refers to susceptibility (i.e., the probability that an interaction leads to change in
 285 motivation level), and N refers to the number of other crew agents that are interacting with crew i .

286 Z takes two binary values 0 and 1. Z is 0 when the agent is a zealot and never changes their
 287 motivation following interactions with others, and Z is 1 when the crew agent is not a zealot and
 288 may change their motivation after interacting with others. C is 0 when there is no contact between
 289 crews. When there is contact between crews, C takes positive real numbers. S takes real numbers
 290 between 0 and 1. S is 0 when there is no susceptibility, and S is 1 when there is full susceptibility.
 291 The value of S indicates how much the interacting crew agents affect the motivation level of crew
 292 agent i .

293 **Application of the hybrid fuzzy Monte Carlo agent-based simulation model**

294 To demonstrate the applicability and suitability of the proposed hybrid FMCABS
 295 methodology, it was implemented on a parametric study of construction crew performance on a
 296 real industrial project. The hybrid FMCABS model of construction crew motivation and
 297 performance developed by Raoufi and Fayek (2020) was extended in this paper to determine the

298 effects of variations in model parameters on crew performance. The connection between
 299 MATLAB and AnyLogic was enhanced to allow parallel simulation, which in turn led to faster
 300 simulation and an increase in the number of iterations compared to previous studies. The analysis
 301 performed in this paper is novel, as previous research on crew performance either used a single
 302 experiment (Raoufi and Fayek, 2020), or compared scenarios based on a limited number of
 303 simulation runs and limited variations of model parameters (Kedir et al., 2020). Figure 3 shows
 304 the hybrid FMCABS model for the parametric study of construction crew performance.



305

306 **Figure 3.** Hybrid FMCABS model for parametric study of construction crew performance.

307 The developed FMCABS model and the parametric study of construction crew performance
308 were based on the actual field data that were previously collected from an industrial project
309 located in Alberta, Canada. Different sources were used to collect data: interviews surveys with
310 project personnel, including crew members, foremen, and project managers (Raoufi and Fayek,
311 2018a); project documents, such as time sheets, score cards, inspection test plans, schedule
312 updates, tender documents, and cost estimates; project databases, such as safety logs and change
313 order logs; observations on the work packages of the project by data collectors; and external
314 databases, such as a databases for weather data (Raoufi and Fayek, 2018b).

315 The input variables of the hybrid FMCABS model included deterministic variables (e.g.,
316 number of crews, contact rate, and zealot percentage); random variables (e.g., susceptibility,
317 motivation variability, and crew-level situation variability); and subjective variables (e.g., crew
318 motivation, crew-level situation, and project-level situation).

319 Crew motivation was determined based on four motivational factors: efficacy (Hannah et al.,
320 2016; Bandura, 1977), commitment/engagement (Cesário and Chambel, 2017; Meyer and Allen,
321 1991), identification (Lin et al., 2017; Ashforth and Mael, 1989), and cohesion (Chiniara and
322 Bentein, 2018; Beal et al., 2003).

323 The crew-level situation and the project-level situation represent factors related to the working
324 environment. Actual field data on the crew-level situation were collected from three categories:
325 task-related factors (e.g. task design), labor-related factors (e.g., the functional skills of the crew),
326 and foreman-related factors (e.g., leadership skills). Actual field data on the project-level situation
327 were collected from five categories: project characteristics (e.g., work shifts), management-related
328 factors (e.g., project management practices), work-setting conditions (e.g., weather conditions),
329 resources (e.g., tools, equipment, and materials), and safety precautions (e.g., safety training).

330 Crew motivation, the crew-level situation, and the project-level situation all affect crew
 331 performance, the latter of which is the output of the hybrid FMCABS model. Crew performance
 332 was defined by 55 key performance indicators (KPIs) across three performance metrics, namely
 333 task performance, contextual performance, and counterproductive behavior. Table 1 shows the
 334 crew performance metrics and their KPI categories.

335 **Table 1.** Crew performance metrics and KPI categories

Crew performance metrics	KPI category
Task performance	Cost performance indicators
	Schedule performance indicators
	Change performance indicators
	Quality performance indicators
	Safety performance indicators
	Productivity performance indicators
	Satisfaction performance indicators
Contextual performance	Personal support
	Organizational support
	Conscientious initiative
Counterproductive behavior	Interpersonal deviance
	Organizational deviance

336 The developed hybrid FMCABS model is able to process different types of input variables
 337 (i.e., deterministic, random, and subjective) and analyze the effect of variations in model
 338 parameters on construction crew performance. In this paper, the hybrid FMCABS model was used
 339 to perform a parametric study of construction crew performance, which determined the effect of
 340 crew contact rates, the initial percentage of highly motivated crews, and the percentage of zealots
 341 in the project on crew performance.

342 **Parametric study of crew performance**

343 Three simulation parameters that showed significant influence on crew performance were
 344 selected for this parametric study, based on past research performed by Raoufi and Fayek (2018c):

345 contact rate (i.e., the number of interactions between crews per simulation time unit), the initial
346 percentage of highly motivated crews (i.e., the percentage of crews in a high-motivation state at
347 the start of the simulation), and zealot percentage (i.e., the percentage of crews that do not change
348 their motivation following interactions with other agents).

349 Anylogic and MATLAB were used to perform the parametric study on the selected parameters
350 of the FMCABS model. The parametric study involved the performance of multiple simulation
351 experiments for each selected parameter (i.e., 26 simulation experiments for contact rate, 11
352 simulation experiments for initial percentage of highly motivated crews, and 11 simulation
353 experiments for zealot percentage), where each simulation experiment included 1000 simulation
354 runs. This configuration produced to a total of 48,000 simulation runs during the parametric study.

355 To perform the simulation experiment, several steps were followed. First, all parameters of
356 the FMCABS model were set at their actual values based on field data. Table 2 shows the actual
357 values of all parameters of the FMCABS model.

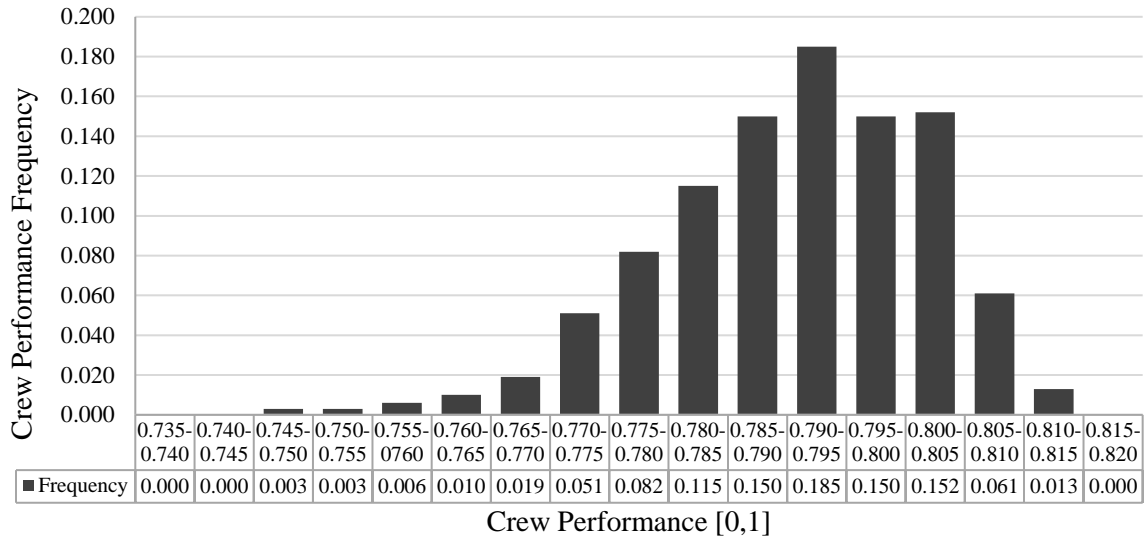
358 Second, for each simulation experiment, one of the selected parameters was incrementally
359 adjusted in value across its defined range. For example, in the first simulation experiment, all
360 parameters were set at their actual values shown on Table 2, except contact rate, which was set at
361 0. In the second simulation experiment, all parameters were set to their actual values, while contact
362 rate was set to 0.1. This increment in contact rate continued until all 26 possible values of contact
363 rate from 0 to 2.5 were explored for simulation experiments 1 to 26. Then, during the next 11
364 simulation experiments (i.e., experiments 27–37), contact rate and other simulation parameters
365 were set at their actual values, and the initial percentage of highly motivated crews was
366 incremented by a value of 0.1 across a range from 0 to 1. In the last 11 experiments (i.e.,
367 experiments 38–48), zealot percentage was incremented by a value of 0.1 across a range from

Table 2. Actual values for initial parameters of the FMCABS model

FMCABS Model Parameters	Unit	Actual value (Based on collected field data)	Selected parameters for parametric study		
			Experiment No.	Range of Values	Increment
Contact rate	\mathbb{R}^+	1.0000	1-26	[0,2.5]	0.1
The initial percentage of highly motivated crews	[0,1]	0.4286	27-37	[0,1]	0.1
Zealot percentage	[0,1]	0.2857	38-48	[0,1]	0.1
Number of crews	\mathbb{Z}^+	9			
Susceptibility	[0,1]	Beta (0.2276, 2.1886, 0.0000, 0.4286)			
Non-interactive motivation variability	[0,1]	Beta (0.1538, 13.8460, 0.0000, 0.2888)			
The initial percentage of low motivated crews	[0,1]	0.2857			
Initial states of crew-level situation	[0,1]	0.1426 for “ <i>unsatisfied</i> crew-level situation” 0.0000 for “ <i>satisfied</i> crew-level situation”			
Initial state of project-level situation	String	“ <i>medium</i> project-level situation”			
Crew-level situation variability	\mathbb{R}^+	Beta (0.3127, 9.6465, 0.0000, 0.1429)			
Project-level situation variability	\mathbb{R}^+	0.0333			

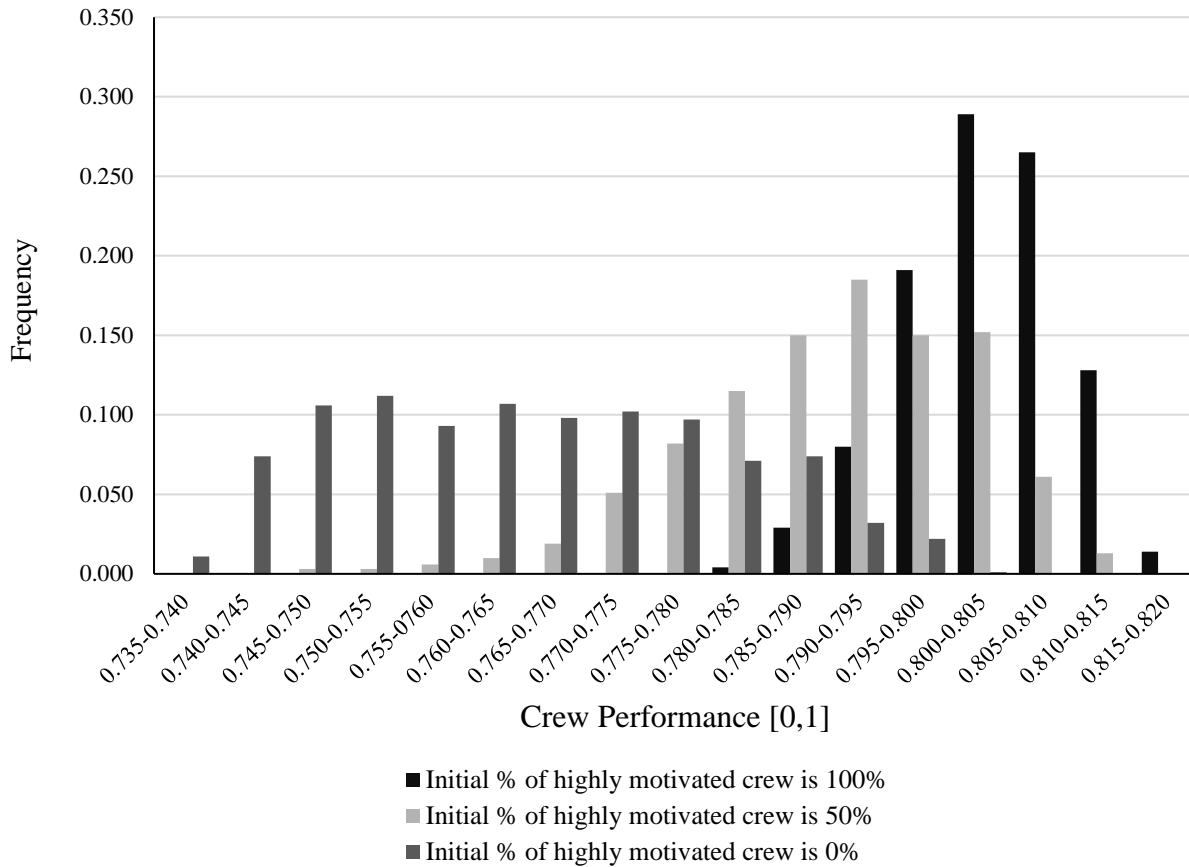
370 0 to 1 in each simulation experiment. Table 2 also shows the range of values and increments for
 371 the selected parameters in the parametric study of the FMCABS model.

372 Third, each simulation experiment was run separately for 1000 runs to determine the output
 373 of the FMCABS model for each value of the selected parameters. Finally, a histogram of the
 374 average crew performance of all crews on the project based on 1000 simulation runs was generated.



375
 376 **Figure 4.** FMCABS model output for simulation experiment 32 (1000 runs).

377 Figure 4 shows the model output for simulation experiment 32, where the initial percentage
 378 of highly motivated crews was 0.5000 and all other parameters were set at their actual values. The
 379 frequency of each category of crew performance is shown in this histogram. Figure 4 demonstrates
 380 that in this simulation experiment, the crew performance category of 0.790–0.795 occurred more
 381 frequently during the project, with a frequency of 0.185 (i.e., 18.5%). Other simulation
 382 experiments were performed to observe the effect of variations in FMCABS model parameters on
 383 crew performance. A sample of this comparison is shown in Figure 5.



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Figure 5. Comparison of three simulation experiments.

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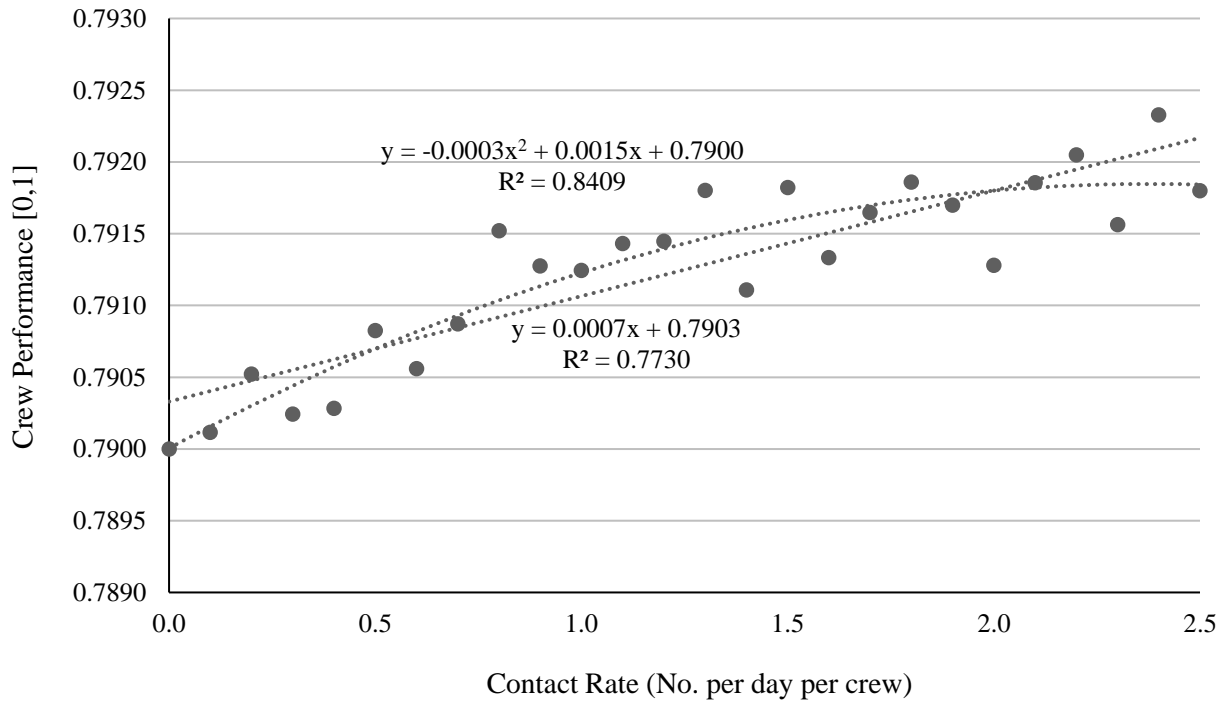
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Figure 5 shows the results of three different simulation experiments, where the initial percentage of highly motivated crews in the project was 100%, 50%, and 0%. An increase in the initial percentage of highly motivated crews resulted in higher crew performance on the project, which is in agreement with the results of past studies on construction crew motivation (Kedir et al., 2020). The present study represents a more extensive analysis of the effects of contact rate, initial percentage of highly motivated crews, and zealot percentages, as compared to previous studies of crew motivation and performance.

Figure 6 shows the results of 26 simulation experiments, which were performed to determine the effect of variations in contact rate on crew performance. As shown in Figure 6, an increase in

395 contact rate resulted in an increase in crew performance. Linear and polynomial trendlines were
 396 also fitted to the results of the simulation experiments. The linear regression model had an R-
 397 squared value of 0.7730, while the polynomial regression model (order 2) had an R-squared value
 398 of 0.8409. Both R-squared values were substantial (i.e., more than 0.75), indicating a good fit to
 399 the results of simulation experiments (Hair et al. 2016). The regression coefficient for contact rate
 400 in the linear regression model was 0.0007, indicating that there was a significant positive
 401 relationship between contact rate and crew performance.



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Figure 6. The effect of contact rate on crew performance.

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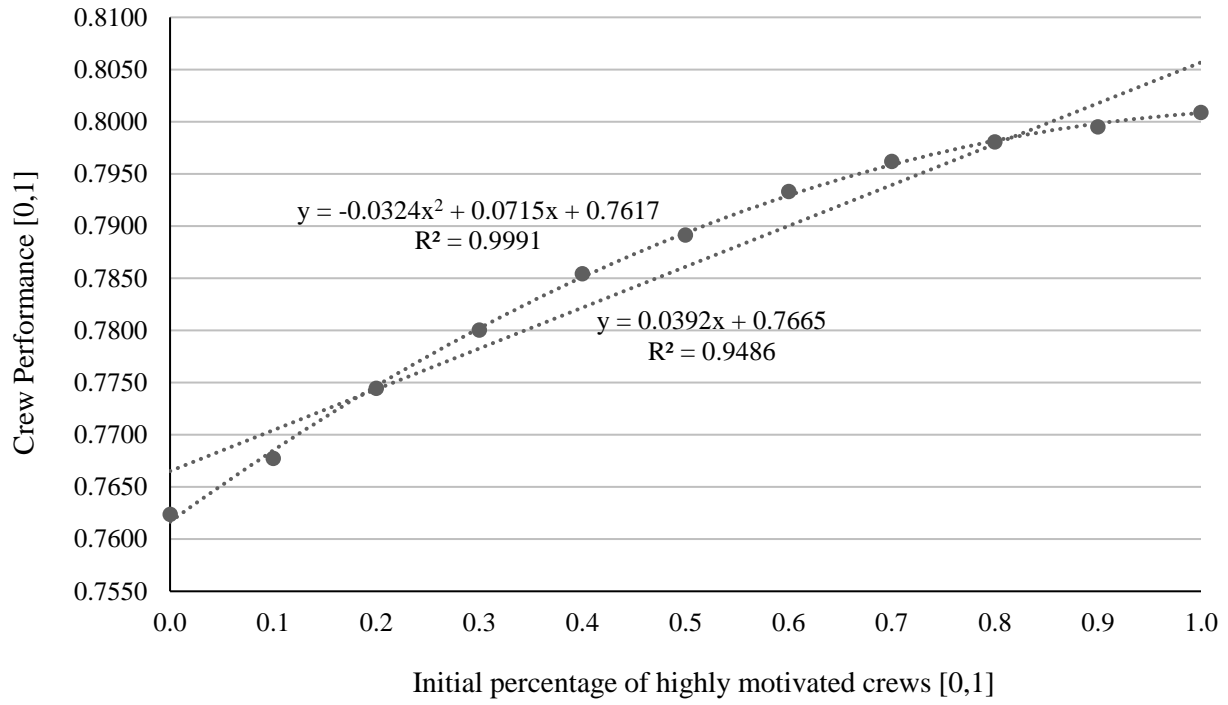
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Figure 7 shows the result of 11 simulation experiments, which were performed to determine the effect of the variations in the initial percentage of highly motivated crews on crew performance. In these simulation experiments, the initial percentage of highly motivated crews was incremented by values of 0.1 across a range from 0 to 1. For example, a value of 0.6000 for initial percentage of highly motivated crews indicates that 60% of crews were in a high motivation state at the start

409 of the simulation. The remaining crews were considered to be in a low motivation state at this
410 time. However, during the simulation experiment, the crews interact with each other, which can
411 result in the change of their motivation states. Each crew can have three states of motivation during
412 the simulation experiment: low motivation, medium motivation, and high motivation. As shown
413 in Figure 7, an increase in the initial percentage of highly motivated crews resulted in an increase
414 in crew performance. Linear and polynomial trendlines were also fitted to the results of the
415 simulation experiments. The linear regression model had an R-squared value of 0.9486, while the
416 polynomial regression model (order 2) had an R-squared value of 0.9991. Both R-squared values
417 were substantial (i.e., more than 0.75), indicating a good fit to the results of the simulation
418 experiments (Hair et al., 2016). The regression coefficient for the initial percentage of highly
419 motivated crews in the linear regression model was 0.0392, indicating that there was a significant
420 positive relationship between the initial percentage of highly motivated crews and crew
421 performance. In other words, an increase in the number of highly motivated crews at the start of
422 the project, as compared to crews with low motivation, resulted in higher crew performance on the
423 project overall.

424 Figure 8 shows the result of 11 simulation experiments, which were performed to determine
425 the effect of variations in zealot percentage on crew performance. In these simulation experiments,
426 zealot percentage was incremented by values of 0.1 across a range from 0 to 1. For example, a
427 value of 0.3000 for zealot percentage indicates that 30% of crews were zealot in nature and never
428 change their motivation when interacting with others. The remaining crews were considered non-
429 zealot, meaning they may change their motivation when interacting with others. As shown in
430 Figure 8, an increase in zealot percentage did not produce a substantial increase in crew
431 performance. Linear and polynomial trendlines were also fitted to the results of the simulation

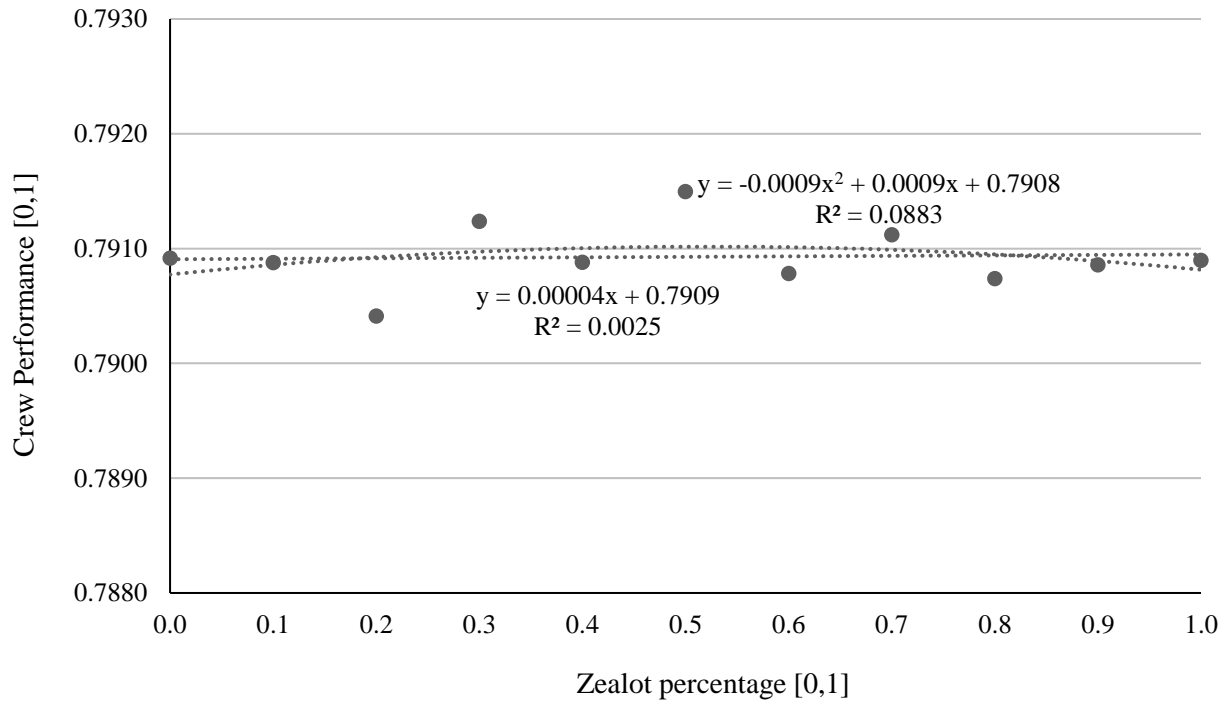


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Figure 7. The effect of the initial percentage of highly motivated crews on crew performance.



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Figure 8. The effect of zealot percentage on crew performance.

437 experiments. The linear regression model had an R-squared value of 0.0885, while the polynomial
438 regression model (order 2) had an R-squared value of 0.0025. Both R-squared values were not
439 significant (i.e., less than 0.25), indicating a poor fit to the results of the simulation experiments
440 (Hair et al., 2016). Therefore, no significant relationship was observed between zealot percentage
441 and crew performance. Although zealot percentage did not have a significant effect on crew
442 performance in this series of simulations, other studies suggest that in cases where the initial
443 percentage of highly motivated crews is high, zealot percentage can have significant effect of crew
444 performance (Kedir et al., 2020). Not having a direct effect does not indicate that zealot percentage
445 is not an important factor to consider for improving crew performance, as it might moderate (i.e.,
446 influence) the relationship of crew motivation to crew performance. Potential moderating effects
447 of zealot percentage on crew performance should be investigated in future studies.

448 **Verification and Validation**

449 This research used a combination of verification and validation methods, as suggested by
450 Lucko and Rojas (2009) for performing face validation, internal validation, external validation,
451 and construct validation for construction research; Ormerod and Rosewell (2009) for verification
452 and validation of agent-based models; and Sargent (2013) for verification and validation of
453 simulation models.

454 To verify the developed model, four steps were followed. First, all possible errors in the
455 model's mathematical equations were checked, as suggested by Ormerod and Rosewell (2009).
456 Second, all components of the model were examined by performing a structured walk-through, as
457 suggested by Sargent (2013). Third, the replicability of the results of the model was checked by
458 performing multiple simulation runs, as suggested by Ormerod and Rosewell (2009). Fourth,

459 changes in the model variables were traced during the simulation experiment, as suggested Sargent
460 (2013).

461 To validate the developed model, three steps were followed. First, the model variables (e.g.,
462 motivation) were defined based on validated concepts to ensure conceptual validity, as suggested
463 by Ormerod and Rosewell (2009), and the reliability of the measures of the variables were checked
464 to ensure validity of the collected data, as suggested by Sargent (2013). Third, time plots
465 representing graphical displays of model variables were developed for all model agents to ensure
466 operational validity, as suggested by Sargent (2013). Fourth, a sensitivity analysis was performed
467 on model parameters to identify parameters that have a significant effect on crew performance.
468 The sensitivity analysis suggests that crew performance varies due to the variations in contact rate
469 and in initial motivation states of crews, which is consistent with the results presented in Figures
470 6 and 7.

471 **Discussion**

472 Variations in crew performance were studied, based on the variations in three parameters:
473 contact rate (i.e., number of interactions between crews per simulation time unit), the initial
474 percentage of highly motivated crews (i.e., percentage of crews in a high-motivation state at the
475 start of the simulation), and zealot percentage. The results of the study indicate that there is a
476 significant influence of both contact rate and the initial percentage of highly motivated crews on
477 crew performance. However, there was no direct influence of zealot percentage on crew
478 performance based on the results of the simulation experiments. These results suggest that
479 strategies intended to increase crew performance should emphasize increases in the initial
480 percentages of highly motivated crew and in the contact rate between the crews. In addition, more
481 research is needed to understand potential moderating effects of zealot percentage on crew

482 performance. Findings from this paper suggest that moderation is an important issue to be taken
483 into consideration when the goal is to improve crew performance.

484 **Conclusions and future research**

485 In this paper, a hybrid FMCABS methodology was extended to and implemented on a
486 parametric study of construction crew performance. This methodology allows construction
487 modelers to develop simulation models that are able to account for both subjective and random
488 uncertainties. An FMCABS model of construction crew performance was developed, which
489 integrates fuzzy logic, Monte Carlo simulation, and ABM to simulate crews in construction
490 environments and predict crew performance. The developed hybrid FMCABS model was
491 implemented on a parametric study to assess the effects of contact rate, initial percentage of highly
492 motivated crews, and zealot percentage on crew performance.

493 One of the main contributions of this paper is the extension of a hybrid FMCABS
494 methodology, which allows agent-based models to simultaneously process all types of variables
495 (i.e., deterministic, random, and subjective) in the same simulation experiment, while accounting
496 for interactions between different agents. Another major contribution of this paper is the
497 implementation of the developed methodology in a novel and extensive parametric study of
498 construction crew performance. Past research on construction crew performance focused either on
499 a single experiment, or on a scenario-based analysis using limited simulation runs and limited
500 variations of model parameters. The hybrid FMCABS model of construction crew performance
501 developed by Raoufi and Fayek (2020) was extended in this paper to determine the effects of
502 variations in model parameters on crew performance. The connection of MATLAB and AnyLogic
503 was enhanced, allowing for parallel simulation and leading to faster simulation.

504 The results of the parametric study will enable construction practitioners to develop strategies
505 to increase crew performance through emphasizing increases in the initial percentage of highly
506 motivated crews and in the contact rate between crews. The results indicate that the concept of
507 emotional contagion is applicable to the relationship of crew motivation and performance.
508 Emotional contagion is the concept that a person's emotional responses trigger similar responses
509 in other people (Hatfield et al. 1994). To the extent that motivation captures emotional content, it
510 may be assumed that the logic underlying emotional contagion allows for the increase in crew
511 motivation when contacting other highly motivated crews. For instance, a worker with low levels
512 of motivation working in a crew of highly motivated members will become more motivated due
513 to his or her interactions with highly motivated crew members. The results also suggest that the
514 direct effect of zealot percentage on crew performance was not significant in the project under
515 study, but that there is a possibility of a moderating effect of zealot percentage on crew
516 performance. In the future, moderating effects of zealot percentage on crew performance should
517 be investigated. The effect of variations of other model parameters on crew performance can also
518 be studied using the methodology developed in this paper. Though the results of the parametric
519 study are limited to the context of construction crew performance, future research will investigate
520 implementation of the developed FMCABM methodology in other construction research contexts.
521 In the future, more data need to be collected to enable the modeling of emergent behavior of agents,
522 such as the changes in the behavior of crews when faced with drastic changes in their working
523 environment (e.g., changes due to the COVID-19 pandemic).

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