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APPLICATION OF POLY-MOR FOAM AS INSULATION FOR SINGLE WYTHE MASONRY WALLS

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Executive Summary

Unfinished single-wythe concrete masonry walls are common among warehouse and industrial buildings because they are relatively inexpensive to construct while simultaneously providing security and durability due to superior resistance to impact, fire, weather, insects, and corrosion. However, single-wythe masonry provides low thermal resistance (R-value) and can be a significant source of heat loss. Masonry walls meeting certain criteria were exempted from the insulation requirements of the 1997 Model National Energy Code of Canada for Buildings (MNECB). Under the 2011 National Energy Code of Canada for Buildings (NECB), masonry walls will no longer be exempted. Further, the insulation requirements have been increased significantly in the new Code. These new Code requirements, concerns regarding global climate change, and rising energy prices have given rise to the need for inexpensive and efficient insulation options for building envelope assemblies, especially single-wythe masonry.

A pilot investigation was conducted involving three different application procedures and two different material densities applied at three different thicknesses. The goal was to evaluate the effectiveness of POLY-MOR closed-cell polyurethane foam as an insulating material and determine the best possible insulation procedure. Seven masonry wall mock-ups were built at the University of Alberta's I.F. Morrison Structural Engineering Laboratory. POLY-MOR then performed fourteen different test applications of their closed-cell polyurethane foam as an insulating material. High and low-density foams were used in three different procedures: spray-applied, filled formwork, and core grouting. For the spray applied and filled formwork procedures, 25mm, 51mm, and 76mm (1 in, 2 in, and 3 in) thick applications were tested. The actual thickness of application varied considerably in the spray applied procedure, but was uniform in the filled formwork procedure.

Tests were performed according to ASTM standards to determine the density and thermal conductivity of the foam in each of the fourteen specimens. The lightest foam, weighing approximately 40 kg/m³ (2.50 lb/ft³), was obtained from the low-density filled formwork procedure. The heaviest foam weighed approximately 104 kg/m₃ (6.49 lb/ft³) and came from the high-density spray applied procedure. The low-density filled formwork procedure also yielded the most favourable thermal properties, with a thermal conductivity of just 0.0252 W/m·K. This corresponds to a thermal resistance of RSI-0.0397 per millimetre (R-5.72 per inch). The high-density foam of the filled formwork procedure was the next best insulation, with a thermal resistance of RSI-0.0333 per millimetre (R-4.80 per inch). This was followed closely by the low-density spray applied foam at RSI-0.0312 per millimetre (R-4.50 per inch).

Using the results of the ASTM thermal conductivity tests, two-dimensional heat flow simulations were carried out using the software THERM. It was found that filling the cores is a very ineffective method of insulating masonry walls because the webs of the concrete blocks act as thermal bridges. Using the low-density filled formwork procedure, minimum thicknesses of 114mm (4¹/₂ in) for above ground walls and 83mm (3¹/₄ in) for below ground walls are necessary for a 200mm block wall to meet the requirements of the NECB for Edmonton and other regions in Zone 7A.

The low-density filled formwork procedure appears to be the most viable insulation option. In addition to superior thermal resistance that is comparable with some of the best insulations available on the market today, the procedure also produces a uniform thickness and the lightest weight foam. Maximizing the thermal resistance has the effect of minimizing the amount of useable floor space consumed by insulation. By producing a uniform thickness, waste is minimized and the quality of workmanship is less dependent on the experience level of the applicator. Finally, minimizing the weight of the foam reduces the material costs and the weight of insulation added to the structure. The only noteworthy drawback appears to be the labour and material costs associated with the formwork. It is believed that this may be overcome by either leaving the forms in place or by making the forms modular and easily reused.

Since the foam may require finishing with fire resistant materials, it is possible that forms made of gypsum wallboard could be left in place after insulating and then painted by others. If modular formwork is pursued, it would have to be durable and easy to assemble, disassemble, and transport. A "non-stick" coating to prevent adhesion between the forms and the insulation would be essential to minimizing costs associated with reusable formwork. Finally, exterior application of the insulation may be the most economical method of making single-wythe masonry walls Code compliant. The masonry on the interior side of the insulation is the best way to utilize its thermal mass. Additionally, no additional fire protection is necessary because masonry inherently possesses exceptional fire resistance. The uniform surface produced by the filled formwork procedure could easily be finished with EIFS ("acrylic stucco") base and finish coats.

POLY-MOR closed-cell polyurethane foam appears to possess immense potential as insulating material, not only for walls, but also for roofs, slabs on ground, and underground pipes. While it was demonstrated that there are some insulation products with marginally superior thermal resistance already available on the market, POLY-MOR polyurethane foam could still be a competitive insulation if other properties of the foam are also exploited.

APPLICATION OF POLY-MOR FOAM AS INSULATION FOR SINGLE WYTHE MASONRY WALLS

1.0 Introduction

Unfinished single-wythe concrete masonry walls are commonly used in warehouse and industrial settings to enclose the building. Single-wythe concrete masonry walls are relatively inexpensive to construct while simultaneously providing security and durability due to superior resistance to impact, fire, weather, insects, and corrosion. The main drawback of single-wythe walls is that they provide little thermal resistance. Under the recently superseded Model National Energy Code of Canada for Buildings (MNECB), single-wythe masonry walls meeting certain criteria were exempted from being insulated (NRCC 1997). The new National Energy Code of Canada for Buildings (NECB) has significantly stricter energy efficiency guidelines for building envelope design and provides no exemption for masonry walls (NRCC 2011). This, in addition to growing concerns regarding anthropogenic effects on the environment and increasing energy prices, has given rise to the need for an inexpensive and efficient option to insulate singlewythe masonry walls. The purpose of this investigation was to evaluate the effectiveness of POLY-MOR polyurethane foam as an insulating material and determine the best procedure for applying the foam.

Three different application methods were investigated using two different foam densities and three different thicknesses. POLY-MOR foam was applied to unfinished single-wythe concrete masonry walls. The polyurethane foam was applied by spraying, formwork filling, or core grouting. Tests were conducted according to ASTM standards to determine the density and thermal conductivity of the foam in each application. A two-dimensional heat flow simulation was then used to determine the effective RSI-value of masonry walls with the different insulation configurations. Although the test specimens were concrete block walls, the results of the investigation could be relevant for insulating slabs, roofs, and other wall constructions.

2.0 Methodology

Seven concrete block masonry wall specimens were constructed by journeyman masons at the University of Alberta's I.F. Morrison Structural Engineering Laboratory in Edmonton. The walls were built using standard 200mm normal weight 20MPa concrete block masonry units and standard 10mm tooled mortar joints. The blocks were laid in a running bond pattern, three units wide by five units high (1200mm x 1000mm). The cores of the wall specimens were left un-grouted. Figure 1 shows the seven wall specimens shortly after construction, prior to the application of any foam.



Figure 1 – Seven concrete masonry wall specimens

2.1 Application of POLY-MOR Polyurethane Foam

Professionals from POLY-MOR Canada Inc. insulated the concrete masonry wall specimens using fourteen variations on the application of closed-cell polyurethane foam. These variations are summarized below in Table 1.

Designation	Foam	Procedure	Thickness
LD-S-1	Low-density	Spray applied	25mm (1 in)
LD-S-2	Low-density	Spray applied	51mm (2 in)
LD-S-3	Low-density	Spray applied	76mm (3 in)
HD-C-1	High-density	Filled formwork	25mm (1 in)
HD-C-2	High-density	Filled formwork	51mm (2 in)
HD-C-3	High-density	Filled formwork	76mm (3 in)
LD-S-1	Low-density	Spray applied	25mm (1 in)
LD-S-2	Low-density	Spray applied	51mm (2 in)
LD-S-3	Low-density	Spray applied	76mm (3 in)
HD-C-1	High-density	Filled formwork	25mm (1 in)
HD-C-2	High-density	Filled formwork	51mm (2 in)
HD-C-3	High-density	Filled formwork	76mm (3 in)
LD-G	Low-density	Grouting	n/a
HD-G	High-density	Grouting	n/a

Table 1 – Schedule of Variations of POLY-MOR Foam Insulation Application

The polyurethane foam was applied using three different application procedures: spray-applied, filled formwork, and grouting. The spray application was performed using a nozzle at a distance of approximately one metre (3'-3") from the face of the wall (Figure 2). Since there is a delay between when the product comes in contact with the wall and the when the foam fully expands, the applicator must judge when enough material has been deposited to achieve the desired thickness. Figure 3 shows that the actual thickness of the spray applied foam varied considerably over the surface of the wall. The low-density spray-applied foam had a rough, bubbly surface appearance and texture (Figure 4), while the surface of the high-density spray applied foam was smoother in texture and looked somewhat runny (Figure 5).



Figure 2 – Spray application of POLY-MOR in progress.

The filled formwork procedure was carried out using temporary forms to accommodate 25mm, 51mm, and 76mm (1 in, 2 in, and 3 in) thicknesses of foam on the surface of the wall. The forms were built of 19mm (³/₄ in) particleboard. A plastic sheet taped to the inside of the form prevented the foam from adhering to the particleboard, but had to be replaced with each use of the form. Polyurethane foam was then injected into the formwork using an appropriate attachment at the end of the nozzle (Figure 6). Clamps placed around the perimeter held the form in place under the pressure of the expanding foam. The foam hardened very quickly and the formwork was removed within five minutes of application. The formwork ensured a uniform thickness of application and created a smooth and even surface appearance. The grouting procedure was similar, except that foam was injected in the cores of the hollow blocks (Figure 7).



Figure 3 – Variation in the actual thickness of low-density (left) and high-density (right) spray-applied foam.



Figure 4 – Rough, uneven surface appearance of the low-density spray-applied foam



Figure 5 – Smooth, uneven surface appearance of the high-density spray-applied foam



Figure 6 – Filled formwork foaming procedure in progress.



Figure 7 – Wall specimen with foam grouted cores.

2.2 Determining Density

The density of the foam was calculated in order to investigate the effect of application procedure on density and the effect of density on thermal conductivity. Three samples of the polyurethane foam were obtained from each of the fourteen application procedures. The density of each sample was determined in accordance with ASTM D792o8, "Standard Test Methods for Density and Specific Gravity (Relative Density) of Plastics by Displacement."

To determine the density, a representative sample is first weighed in air (*a*). The sample is then submerged in demineralized water at a temperature of 23.0° C (73.4° F). For plastics that are less dense than water (like polyurethane foam) it is necessary to attach a metallic sinker. The sinker used in this investigation weighed 2.27 kg (5.0 lb). The fully submerged sample, along with the sinker and container, are weighed in the water (*b*). Finally, the sinker and container are weighed in the water without the sample (*w*). The weight of the submerged sample alone is the difference between *b* and *w*, and is directly proportional to the volume of the sample. After correcting for temperature (if required)¹, the specific gravity of the sample is calculated using the following formula:

sp gr 23/23°C =
$$\frac{a}{(a+w-b)}$$
 (1)

The bulk density of the sample can then be calculated by multiplying the specific gravity by 997.5 kg/m³ (62.27 lb/ft³), which is the density of water at $23^{\circ}C$ (73.4°F).

2.3 Determining Thermal Conductivity

The thermal conductivity of the polyurethane foam samples was determined in accordance with ASTM D5930-09, "Standard Test Method for Thermal Conductivity of Plastics by Means of a Transient Line-Source Technique". Figure 8 shows the test apparatus during calibration.

In Figure 8, the data logger is identified by the letter A, the constant power source is identified by the letter B, letter C designates the probe inserted into a piece of DOW STYROFOAMTM. The STYROFOAMTM has a known thermal conductivity of 0.0288 W/m·K (0.0167 BTU/hr·ft·°F), and is used to calibrate the probe (DOW Building Solutions 2006).

To determine the thermal conductivity of the test specimens, a 229mm (9 in) probe was inserted into the foam of each wall mock-up. To obtain a representative sample of the conductivity, tests were conducted in four separate locations on each of the

¹ If the water temperature differs from 23.0°C, a correction procedure given in ASTM D792-08 is necessary.



Figure 8 – Thermal conductivity test set-up during calibration.

fourteen mock-ups and the results were averaged. The probe was connected to a constant power source and a data logger. The power released along the length of the probe caused an increase in temperature, which was then measured by a series of thermocouples along the length of the probe.

Each test took approximately 15 minutes for the temperature inside the sample to stabilize, after which the temperature was plotted against the natural logarithm of the time of the test. The slope of the linear portion of the resulting graph was then used in the following formula to determine the thermal conductivity of the sample:

$$\lambda = \frac{CQ}{4\pi \cdot Slope} \tag{2}$$

$$Slope = \frac{T_2 - T_1}{\ln(t_2/t_1)}$$
 (3)

In Equation (2), λ is the thermal conductivity of the sample (W/m·K), Q is the heat output per unit length (W/m), *Slope* is the slope of the temperature – log time graph (measured in K), and *C* is the probe constant. *Slope* is calculated from Equation (3), where T_1 and T_2 are the temperatures at two different times, t_1 and t_2 , respectively. The probe constant *C* is determined by calibration test of a sample with known thermal conductivity. In this investigation, the probe was calibrated between each application method tested, and the calibration value *C* varied between 0.85 and 0.90.

2.4 Determining Thermal Resistance

2.4.1 Thermal Resistance of a Material

The thermal resistance of a material is calculated according to Equation (4) - by dividing the thickness of the layer (*L*) by the thermal conductivity of the material (λ). The thickness of the layer is measured in the direction of heat flow. For walls, floors, roofs, and other plate-like elements, the direction of heat flow is generally perpendicular to the surface.

$$R = \frac{L}{\lambda} \tag{4}$$

2.4.2 Thermal Resistance of an Assembly

Equation (4) is used to determine the thermal resistance of material. However, within most wall constructions, layers are not made entirely of one material. Examples include timber frame stud walls and hollow masonry blocks. Layers built of different materials in parallel may have a significant effect on the overall thermal resistance because heat will flow more readily through the more conductive material. There are two approximate methods for estimating heat flow by hand calculations: the Parallel Path method and the Isothermal Planes method. These methods are described below and real examples have been provided in Appendix B: Hand Calculations.

The Parallel Path method is the simpler of the two and it assumes that heat flows strictly in one direction. This assumption is valid if parallel materials have the same resistance, but results in overestimating the overall thermal resistance when this criterion is not satisfied. However, the accuracy of the Parallel Path method is often sufficient, particularly in the case of typical timber frame construction. Mathematically, the parallel path method is described by Equations (5) to (8):

$$R_{ij} = \frac{L_{ij}}{k_{ij}} \tag{5}$$

$$R_{iT} = \sum_{j=1}^{n} R_{ij} \tag{6}$$

$$R_T = \left[\sum_{i=1}^m \frac{A_i}{R_{iT} \cdot A}\right]^{-1} \tag{7}$$

$$A = \sum_{i=1}^{m} A_i \tag{8}$$

Where

A = total cross-sectional area of the assembly, perpendicular to the flow of heat $A_i =$ cross-sectional area of the ith parallel path, perpendicular to the flow of heat $L_{ij} =$ length of the jth element of the ith parallel path, parallel to the flow of heat $R_T =$ overall thermal resistance of the materials (excludes surface air films) $R_U =$ overall thermal resistance of the assembly, including the surface air films $R_{iT} =$ sum of all resistances along the ith parallel path $R_{ij} =$ thermal resistance of the jth element of the ith parallel path $k_{ij} =$ thermal conductivity of the jth element of the ith parallel path

The Isothermal Planes method implies that heat will flow preferentially through elements with lesser resistance and yields a lower-bound estimate of the thermal resistance (Enermodal Engineering Ltd 1996). The Isothermal Planes method yields accurate estimates when considering hollow concrete masonry (Van Geem 1985). The Isothermal Planes method is described mathematically by Equations (9) to (12):

$$R_{ij} = \frac{L_i}{k_{ij}} \tag{9}$$

$$R_i = \left[\sum_{j=1}^n \frac{A_{ij}}{R_{ij} \cdot A}\right]^{-1} \tag{10}$$

$$A = \sum_{j=1}^{n} A_j \tag{11}$$

$$R_T = \sum_{i=1}^m R_i \tag{12}$$

Where

A = total cross-sectional area of the assembly, perpendicular to the flow of heat A_{ij} = cross-sectional area of the jth parallel path in the ith layer L_i = length of the ith layer, parallel to the direction of heat flow R_T = overall thermal resistance of the materials (excludes surface air films) R_U = overall thermal resistance of the assembly, including the surface air films R_i = effective thermal resistance of the ith layer R_{ij} = thermal resistance of the jth parallel path of the ith layer R_{ij} = thermal conductivity of the jth parallel path of the ith layer

For greater accuracy, it is necessary to use two-dimensional heat flow equations. Computers are better suited to solving these equations. The hand calculation methods described above were used to estimate the thermal resistance in order to provide a check value to ensure that the results of the computer simulations were correct. In this investigation, the computer program THERM 6.3 was selected to perform the required

transfer calculations. THERM is freely available download heat to from http://windows.lbl.gov/software/therm/therm.html. THERM can provide overall or partial heat transfer coefficient U-values of an assembly in addition to several possible visual outputs, which include isotherms, coloured infrared, heat flux vectors, and constant heat flux contours. Since the program uses the finite element method to simulate steady-state heat transfer in two dimensions (Finlayson et al. 1998), THERM meets the requirements of the Model National Energy Code of Canada for Buildings (MNECB) and NECB for providing an evaluation method that is deemed equivalent to performing ASTM C 1363 laboratory tests (NRCC 1997, 2011).

Figure 9 depicts the typical geometry of the 190mm concrete masonry units used to build the test specimens. This was the geometry used in THERM, with the inclusion of half the head joint on either end. On this type of block, only the flange would be bedded with mortar, so the head joint would be about 10mm thick by 50mm deep on each flange (100mm total depth of mortar, with 90mm air gap in between).



Figure 9 – Measured geometry of the blocks used in the test specimens.

Figure 10 depicts the simplified geometry that was used to perform the hand calculations. The cross-sectional area of the block is essentially unchanged, though the material has been redistributed slightly to simplify the calculations.

The bed joint was modeled separately, since THERM does not model in threedimensions. The flared face shell provides about 46mm to be bedded with mortar; however, some mortar is typically squeezed out when the block is laid down. The excess mortar is removed from the exterior, but within the block the mortar may extend several millimetres. It is assumed herein that the bed joint is 10mm thick by 50mm deep on each face (100mm total depth of mortar, with 90mm air gap in between). Figure 11 and Figure



Figure 10 - Simplified geometry used for hand calculations

12 depict the geometry of the bed joint modeled in THERM for blocks with unfilled and foam filled cores. In the case of the foam-filled blocks, it is assumed that the area of the foam is exactly equal to the opening in the block, which is narrower than the dimensions of the cores in Figure 9 because the webs and face shells are flared 10mm. This assumption is conservative because the foam can be expected to expand and at least partially fill the 10mm gap between successive courses, but the extent of this expansion is unknown and believed unlikely to be 100%. The overall thermal resistance of the wall was calculated by combining the results of the two analyses using the parallel path method. Since the difference in thermal resistance offered by the block and the bed joint is small and the bed joints account for only 5% of the total area, it is adequate to use this approximation in favour of three-dimensional modeling.



Figure 11 - Bed joint geometry for blocks with unfilled cores



Figure 12 – Bed joint geometry for blocks with foam-filled cores.

Part 2 of both MNECB 1997 and NECB 2011 requires that heat flow tests on building assemblies be carried out setting the temperature of the warm side to $35^{\circ}C$ ($95^{\circ}F$) and the temperature of the cool side to $13^{\circ}C$ ($55.4^{\circ}F$) (NRCC 1997, 2011). These temperatures were used in the THERM simulations. Also in accordance with Part 2 of the MNECB, the air films and air cavities were modeled using the effective thermal resistance values provided in Appendix C of the MNECB (NRCC 1997). Namely, these values are RSI-0.03 and 0.12 (R-0.17 and 0.68) for the exterior and interior surface films, respectively, and RSI-0.18 (R-1.02) for non-reflective, unventilated air spaces greater than 40mm ($1^{9}/_{16}$ in) (NRCC 1997). The same values are also given in ASHRAE (2009).

Since THERM uses thermal conductivity as an input, the air spaces were modeled as a solid element with an apparent thermal conductivity that would yield an RSI-value of 0.18 for the length of the air space. Air films are included automatically in THERM, but rather than forcing THERM to model their effective resistances identically to the RSIvalues of 0.03 and 0.12, their convection coefficients were set to 99 999 W/m²·K, effectively giving each film an RSI-value of 0.00001 m²·K/W. By removing the effects of the air films, the simulations from THERM were in essence providing thermal characteristics for only the materials, and the overall assembly properties could be determined by simply adding the RSI-values for the exterior and interior surface films.

The thermal conductivity can vary significantly depending on the overall density and the aggregates used in the mix. Reported below in Table 2 are thermal conductivity values published in NRCC (1997), ACI Guide 122 (2002), and ASHRAE (2009).

Material	Density (kg/m³)	Thermal Conductivity (W/m·K)	Source
	N/A	1.1	NRCC 1997
	1920	1.40	
	1600	0.97	ASHRAE 2009
	1280	0.65	
Mortar	1920	1.39	
	1760	1.16	
	1600	0.966	ACI-122 2002
	1440	0.793	
	1280	0.644	
Concrete, sand & gravel aggregate	2400	2.3	NRCC 1997
Concrete, sand & gravel aggregate	2400	1.4 to 2.9	
(higher quartz and quartzite	2240	1.3 to 2.6	ASHRAE 2009
content results in higher conductivity)	2080	1.0 to 1.9	Abina L 2009
Concrete, unprotected, sand &	2400	2.83	
gravel aggregate <50% quartz &	2240	2.11	ACI-122 2002
quartzite	2080	1.54	
Concrete, unprotected, sand &	2400	3.17	
gravel aggregate >50% quartz &	2240	2.38	ACI-122 2002
quartzite	2080	1.70	
	2400	1.98	
Concrete, unprotected, limestone aggregate	2240	1.69	
	2080	1.44	ACI-122 2002
	1920	1.20	
	1760	1.01	

Table 2 – Thermal Conductivity of Concrete and Mortar (NRCC 1997, ACI-122 2002, ASHRAE 2009)

Though the thermal conductivity of concrete can vary considerably, the thermal resistance contribution of the concrete is only important in walls with little or no insulation. For walls with a continuous layer of insulation, the other components typically offer very little additional thermal resistance, so it is of little value to perform multiple simulations in order to investigate the effect of the concrete's thermal conductivity.

Instead, values were chosen based on what the authors have judged to be representative of typical masonry construction. The thermal conductivity of the mortar was taken to be 1.1 W/m·K, which is the value given in Appendix C of the MNECB and is

representative of a typical mortar with oven-dry density on the order of 1700 kg/m3 (106 lb/ft3) (NRCC 1997, ACI-122 2002). The concrete used to manufacture the masonry units was assumed to have an oven-dry density of 2180 kg/m3 (131 lb/ft3) and made with limestone aggregates. Further, the concrete was assumed to be unprotected from rain, which is often the case. By linear interpolation, this yields an expected thermal conductivity of 1.61 W/m·K.

3.0 Results and Discussion

3.1 Density

Three samples were obtained from each of the fourteen insulated wall specimens and tested in accordance with ASTM D792-08. The results are presented graphically in Figure 13, and summarized in Table 3.



Figure 13 - Density versus thickness or application for different foaming procedures

Sample	Density (kg/m3)	Density (lb/ft ³)	COV ²	Sample	Density (kg/m3)	Density (lb/ft ³)	COV ²
HD-S-1	100.05	6.25	2.1%	LD-S-1	67.39	4.21	3.9%
HD-S-2	107.44	6.71	2.1%	LD-S-2	50.90	3.18	6.5%
HD-S-3	104.61	6.53	13.5%	LD-S-3	50.24	3.14	6.4%
HD-C-1	67.67	4.22	6.3%	LD-C-1	38.79	2.42	4.8%
HD-C-2	67.66	4.22	12.5%	LD-C-2	38.99	2.43	2.3%
HD-C-3	82.12	5.13	7.7%	LD-C-3	42.45	2.65	2.3%
HD-G	57.11	3.57	7.6%	LD-G	53.60	3.35	5.9%

Table 3 – Average Density of Foam by Application

There does not appear to be a strong trend between thickness of application and the density of the foam. It is readily observed that from 25mm to 51mm, the high-density spray applied foam increased in density by about 7%. However, the variation in the density of the 76mm samples was considerable, and the average decreased slightly from the density at 51mm. The low-density foam exhibited decreasing density with increasing thickness in the spray applied foam, while the density increased slightly when the filled formwork procedure was used. It was also noted that the high-density foam was consistently 1.5 to 2.1 times denser than the low-density foam using either the spray applied or filled formwork procedures, while the difference was a factor of about 1.07 using the grouting procedure.

Since the thickness appears to have only a small effect on the density of the foam, it would appear adequate for estimation purposes to assume constant values of density for the different application procedures. The recommended values are presented in Table 4. However, thicknesses of application significantly greater than those investigated, or variations in the make-up of the foam and/or procedure of application may warrant further testing to verify the adequacy of these recommended values.

Typical values of the density of spray applied closed-cell polyurethane foam insulation currently on the market appear to range from about 32 to 42 kg/m³ (2.0 to 2.6 lb/ft³) (DOW Building Solutions 2011, Polyurethane Foam Systems Inc. 2010). It is readily seen that most of the applications produced foams that are denser than foam insulations currently on the market.

² COV = Coefficient of Variation.

Application Procedure	Density (kg/m ³)	Density (lb/ft ³)
Low-density, filled formwork	40	2.50
Low-density, grouting		
Low-density, spray applied	56	3.49
High-density, grouting		
High-density, filled formwork	72	4.52
High-density, spray applied	104	6.49

Table 4 - Recommended Values of Density for Estimation Purposes

3.2 Thermal Conductivity

The results of the thermal conductivity tests are summarized in Table 5, and plotted as a function of density in Figure 14:

	Conductivity	Conductivity	
Sample	(W/m·K)	(BTU/hr·ft·°F)	COV
HD-C-1	0.0296	0.0171	12.7%
HD-C-2	0.0301	0.0174	13.8%
HD-C-3	0.0304	0.0176	10.9%
LD-C-1	0.0287	0.0166	10.6%
LD-C-2	0.0227	0.0131	7.5%
LD-C-3	0.0242	0.0140	5.6%
HD-S-1	0.0500	0.0289	11.9%
HD-S-2	0.0320	0.0185	13.2%
HD-S-3	0.0383	0.0221	13.6%
LD-S-1	0.0356	0.0206	4.1%
LD-S-2	0.0323	0.0187	6.9%
LD-S-3	0.0282	0.0163	12.2%
LD-G	0.0314	0.0181	11.2%
HD-G	0.0556	0.0322	7.4%

Table 5 – Average Thermal Conductivity of POLY-MOR Polyurethane Foam

From Figure 14 it is observed that thermal conductivity generally increases with increasing density, though it appears that the application procedure itself is more important than the density, evinced by several conductivities of approximately 0.030 W/m·K (0.017 BTU/hr·ft·°F) at densities more or less within the range of 40 to 110 kg/m3 (2.5 to 6.9 lb/ft3). Considering the degree of variance in the data, it seems that it is appropriate to simply use an average thermal conductivity for each foaming procedure.

The recommended design values are presented in Table 6 and were used in the computer simulations on single-wythe concrete masonry.



Figure 14 – Thermal conductivity as a function of density.

Table 6 - Recommended Values of Thermal Conductivity for Design

Application Procedure	Conductivity (W/m·K)	Conductivity (BTU/hr·ft·°F)
Low-density spray-applied	0.0321	0.0185
High-density spray-applied	0.0401	0.0232
Low-density filled formwork	0.0252	0.0146
High-density filled formwork	0.0300	0.0174
Low-density grouting	0.0314	0.0181
High-density grouting	0.0556	0.0322

3.3 Thermal Resistance

3.3.1POLY-MOR Polyurethane Foam Insulation

The thermal resistance of the POLY-MOR polyurethane foam was calculated based on the recommended thermal conductivities presented in Table 6. Tentative design values have been presented in Table 7. For comparison, the thermal resistance of common insulating materials has been provided in Table 8. It is noteworthy that CAN/ULC S770 tests to determine the long-term thermal resistance are necessary to determine appropriate design values for use in Canada. However, the values presented in Table 7 are expected to be a reasonable approximation to the long-term thermal resistances that would be obtained from CAN/ULC S770 testing.

Application Procedure	RSI per mm (m²·K/W/mm)	R per inch (ft²·°F·hr/BTU/in)
Low-density spray-applied	0.031	4.50
High-density spray-applied	0.025	3.60
Low-density filled formwork	0.040	5.72
High-density filled formwork	0.033	4.80
Low-density grouting	0.032	4.60
High-density grouting	0.018	2.59

Table 7 – Thermal Resistance of POLY-MOR Polyurethane Foam for Various Application Procedures

From Table 7 it is clear that the low-density foam is the more efficient insulating material and that the filled formwork application yields superior RSI-values. The filled formwork procedure using low-density foam yields a thermal resistance comparable to extruded polystyrene with carbon black and some spray applied polyurethane foam insulations. It is comparable to polyisocyanurate and the best available spray applied polyurethane foams, but superior to most insulating materials (including ordinary extruded polystyrene). Using high-density foam in the filled formwork procedure reduces the thermal efficiency by about 16%, which makes it marginally less efficient than ordinary extruded polystyrene, but still superior to all types of expanded polystyrene, batt insulation, and other common insulating materials. The low-density foam in the filled formwork, but are still better than expanded polystyrene. The high-density spray applied foam is about 20% less efficient than the low-density spray applied foam, making it comparable to some types of batt insulation. The high-density foam grout yields a relatively poor thermal resistance that is comparable to perlite loose fill.

Insulation	RSI per mm	R per inch	Source
	$(m^2 \cdot K/W/mm)$	(ft ² ·°F·hr/BTU/in)	source
Mineral fibre (rock, slag, or	0.024	3.46	
glass), low-density	0.024	5.40	4
Mineral fibre (rock, slag, or	0.026	3.75	
glass), medium-density	0.020	5.75	4
Mineral fibre (rock, slag, or	0.028	4.04	
glass), high-density	0.020	4.04	4
Cellular glass	0.021	3.03	
Expanded polystyrene (EPS),	0.026	2.75	
type 1	0.020	3.75	
EPS, type 2	0.028	4.04	
EPS, type 3	0.030	4.33	
Extruded polystyrene (XPS)	0.035	5.05	NRCC 1997
Semi-rigid glass fibre sheathing	0.030	4.33	INKCC 1997
Cellulose loose fill	0.025	3.61	
Mineral fibre (rock, slag, or	0.020	2.88	
glass) loose fill	0.020	2.00	
Perlite loose fill	0.019	2.74	
Vermiculite loose fill	0.015	2.16	
Spray applied cellulosic fibre	0.024	3.46	
Spray applied glass fibre	0.026	3.75	
Spray applied polyurethane			
foam	0.042	6.06	
Polyisocyanurate sheathing	0.042	6.06	
Polyurethane sheathing	0.042	6.06	
Polarfoam PF-7300-0 SOYA			Polurethane
(Spray applied polyurethane	0.0416	6.00	Foam Systems
"soya" foam)			Inc. 2010
PlastiSpan TM Type 1 (EPS, type			
1)	0.0260	3.75	
PlastiSpan TM HD Type 2 (EPS,	0 .		Plasti-Fab Ltd
type 2)	0.0280	4.04	2006
PlastiSpan TM Type 3 (EPS, type			
3)	0.0296	4.27	
STYROFOAM TM (XPS)	0.0347	5.00	
STYROFOAM TM (XPS) with		-	
carbon black	0.0388	5.60	DOW Building
STYROFOAM TM Brand SPF CA			Solutions 2006,
(spray applied polyurethane	0.0360 to	5.19 to 5.77	n.d.a, n.d.b
foam)	0.0400		

Table 8 - Thermal Resistance of Various Insulating Materials

THERMAX TM			
(polyisocyanurate)	0.0416 to 0.0451	6.00 to 6.50	
PINK TM FIBERGLAS [®] batt			
3 ¹ /2" & 3 ⁵ /8" R-12, 5 ¹ /2" R-			
19,	0.0226 to		
6" R-20, 8½" R-28, 9½"	0.0240	3.26 to 3.45	
R-31,			
10 ¹ ⁄2" R-35, 11.8" R-40			
PINK TM FIBERGLAS [®] batt	0.0252 to		Owens Corning
3 ⁵ /8" R-14, 6" R-22.5, 11"	0.025210	3.64 to 3.86	2009, 2011
R-40	0.0200		2009, 2011
PINK TM FIBERGLAS [®] batt			
3 ¹ /2" R-14, 5 ¹ /2" R-22, 6" R-	0.0277	4.00	
24, 7" R-28			
PINK TM FIBERGLAS [®] batt	0.0303	4.36	
5 ¹ /2" R-24	0.0303	4.50	
Foamular [®] XPS	0.0347	5.00	
UltraTouch TM Denim Insulation			
batt	0.0240	3.45	
5 ¹ /2" R-19 UltraTouch TM Denim Insulation			
batt	0.0258 to	3.71 to 3.82	Bonded Logic
3 ¹ ⁄ ₂ " R-13, 5 ¹ ⁄ ₂ " R-21, 8" R-	0.0265	5.71 to 5.02	Inc. 2011
30			
UltraTouch TM Denim Insulation			
batt	0.0277	4.00	
2" R-8			
Perlite loose fill, 118 to 176	0.017 to 0.019	2.4 to 2.8	
kg/m ³	0.017 to 0.019	2.4 10 2.0	
Perlite loose fill, 65.7 to 118	0.019 to 0.023	2.8 to 3.3	The Schundler
kg/m ³	5.019 00 0.029	2.0 00 5.5	Company n.d.
Perlite loose fill, 32.1 to 65.7	0.023 to 0.026	3.3 to 3.7	
kg/m ³		۲۰٫ ≈۲ و.ر	

Considering that the filled formwork procedure yields the best thermal efficiency, in addition to the most uniform thickness and best surface appearance, it is recommended that this be the application of choice to provide insulation. The lowdensity foam is recommended because it minimizes the weight added to the structure and yields superior results with the least material. Additionally, by providing the best thermal resistance, insulating by this method will consume the least amount of useable floor area. To improve the viability of the filled formwork foam insulation procedure, it is recommended that an associated modular formwork system be developed. The formwork would have to be easily removed and reused, as taping a plastic sheet to the inside wastes both time and materials. A coating of polytetrafluoroethylene or other "non-stick" material on the form may prevent the adhesion of the foam. Alternatively, a form made of gypsum wallboard could be developed that would be left in place and then painted, thus serving the dual purpose of formwork and interior finish.

The low-density spray-applied foam may also be a viable insulation option. It is believed that better uniformity than was observed in the mock-ups could be achieved with more experience in the procedure. Further, while the procedure produces lower thermal resistance and variable thickness, the lack of formwork could make spray application more economical, particularly if neither of the above proposed formwork options prove to be feasible.

The high-density spray applied foam does not appear to be a viable insulation option because there are batt insulation products that are readily available with superior thermal resistance. Considering that batts are much less expensive to purchase and install than foam insulation currently on the market, high-density spray applied POLY-MOR foam is not likely to be a competitive alternative. However, it is conceivable that the highdensity foam may be desirable in some applications. Being of greater density, it has greater strength and durability, which may make the high-density foam suitable in situations where the insulation can be expected to experience heavy wear or accidental impact.

Further research would be required, but it is likely that the foam could improve certain structural characteristics of the building envelope assemblies. Possible areas to investigate are the increase in racking strength in stud framing, contribution to the flexural and compressive resistance of structural insulated panels, and contribution to blast resistance. In addition to thermal resistance, the foam will provide the benefit of reduced sound transmission and air infiltration. Closed-cell foams are typically resistant to air, water, and vapour diffusion. Further research would be necessary, but if these properties are adequate, the foam could possibly serve four different functions: insulation, air barrier, weather barrier, and vapour barrier. Such an application could eliminate several materials and many hours of labour during construction.

Because the foam resists vapour diffusion, care should be taken when applying this product to existing structures, as this could create a situation where moisture gets trapped between two vapour barriers. A notable problem is that wood rot may be accelerated if moisture is trapped against the framing. Also, consideration must be given to the fire resistance, flame spread, and smoke generation characteristics of the foam. Polyurethane is a combustible material that could release carcinogenic and noxious chemicals in a fire. It is likely that additives to the foam will be necessary to meet National and Provincial Building Code requirements related to the fire characteristics of insulation materials. Further, fire related requirements are more stringent if the foam is to be left exposed on the interior. Formwork that is made of gypsum and left in place after insulating may be a simple solution. It is also possible that foam imbibed or coated with an intumescent could meet fire resistance requirements.

3.3.2 Single-Wythe Concrete Masonry

The thermal resistance of the concrete masonry units without insulation was calculated to be RSI-0.191 m2·K/W (R-1.08 hr·ft2·0F/BTU) by the Parallel Path method and RSI-0.183 m2·K/W (R-1.04 hr·ft2·0F/BTU) by the Isothermal Planes method. The typical range for similar concrete blocks, as reported by Van Geem (1985) is RSI-0.17 to RSI-0.20 (R-0.97 to R-1.14), so it appears that the thermal conductivities chosen to represent typical construction are valid. The thermal resistance obtained from THERM was RSI-0.185. As expected, the value calculated using THERM is less than that predicted by the Parallel Path method, and greater than (but nearly equal to) the estimate provided by the Isothermal Planes method.

Description	Thermal Resistance (m²·K/W)	Thermal Resistance (ft²·°F·hr/BTU)
No insulation	0.185	1.05
Cores filled with high-density foam	0.325	1.84
Cores filled with low-density foam	0.338	1.92
25mm (1 in) spray-applied high-density foam	0.820	4.66
51mm (2 in) spray-applied high-density foam	1.454	8.26
76mm (3 in) spray-applied high-density foam	2.088	11.85
25mm (1 in) spray-applied low-density foam	0.979	5.56
51mm (2 in) spray-applied low-density foam	1.771	10.06
76mm (3 in) spray-applied low-density foam	2.564	14.56
25mm (1 in) filled formwork applied high-density foam	1.032	5.89
51mm (2 in) filled formwork applied high-density foam	1.878	10.66
76mm (3 in) filled formwork applied high-density foam	2.723	15.46
25mm (1 in) filled formwork applied low-density foam	1.194	6.78
51mm (2 in) filled formwork applied low-density foam	2.202	12.50
76mm (3 in) filled formwork applied low-density foam	3.209	18.22

Note that the values given in **Error! Reference source not found.** are for the materials alone and do not include the effective resistances furnished by the surface air films. This can be accounted for by adding RSI-0.15 (R-0.85) to include the interior and exterior surface films for a vertical wall above ground. The exterior air film is non-existent for walls below ground, so RSI-0.12 (R-0.68) should be added instead.

The NECB prescribes maximum overall thermal transmittances $(U-values)^3$ for the various elements of the building envelope based on the number of annual heating degreedays expected at the building's location. Edmonton is in Zone 7A, so the maximum thermal transmittance is 0.284 W/m²·K for walls below ground and 0.210 W/m²·K for walls above ground. Equivalently, these maximum transmittance values can be expressed as minimum resistance values of RSI-3.521 and RSI-4.762 (R-20.0 and R-27.0) respectively. From Table 9 it is apparent that thicker (> 4 in) applications of the foam and/or larger size units are required in order to satisfy the requirements of the NECB for walls above or below ground. It is also readily seen that insulating the cores provides limited benefit. Relative to a wall with no insulation, the improvement in thermal efficiency is about 80% when the cores are filled with foam. However, 25mm (1 in) of low-density foam using the filled formwork procedure uses less insulation material than grouting the cores, yet improves thermal efficiency by over 500% relative to the wall with no insulation. It is clear that thermal bridging inhibits the effectiveness of core insulation severely. A selection of the results from the THERM simulations is presented in Figure 15 to Figure 21.



Figure 15 - Isotherms (left) and coloured infrared (right) of block with low-density foam filled cores. U = $3.0292 \text{ W/m}^2 \cdot \text{K}$.

³ The thermal transmittance is the reciprocal of the thermal resistance. U = 1/R.



Figure 16 - Isotherms (left) and coloured infrared (right) of the bed joint with low-density foam filled cores. U = $1.6781 \text{ W/m}^2 \cdot \text{K}$.



Figure 17 - Isotherms (left) and coloured infrared (right) of concrete block with no insulation. U = $5.4929 \text{ W/m}^2 \cdot \text{K}$.



Figure 1 - Isotherms (left) and coloured infrared (right) of the bed joint with unfilled cores. U = $3.6910 \text{ W/m}^2 \cdot \text{K}$.



Figure 2 - Isotherms (left) and coloured infrared (right) of the bed joint with 25mm lowdensity foam filled formwork cavity. $U = 0.7822 \text{ W/m}^2 \cdot \text{K}$.



Figure 20 - Isotherms (left) and coloured infrared (right) of concrete block with 25mm high-density foam filled formwork cavity. $U = 0.9729 \text{ W/m}^2 \cdot \text{K}$.



Figure 21 - Isotherms (left) and coloured infrared (right) of concrete block with 50mm low-density foam filled formwork cavity. U = $0.4551 \text{ W/m}^2 \cdot \text{K}$.

The visual results of Figures 15 to 21 illustrate that heat flows preferentially through materials with lower thermal resistance, and that a continuous layer of insulation is much more effective than a discontinuous one. It is readily observed that nearly all of the temperature change occurs in the continuous insulation layer (i.e. there is a high temperature gradient in the insulation layer). Without a continuous layer of insulation there is a more gradual temperature change across the entire thickness of the wall.

Table 10 presents recommended minimum thicknesses of application to make single-wythe 190mm concrete masonry walls in Edmonton compliant with the NECB. A plan view of a typical assembly is provided in Figure 22.

Figure 22 – Foam-insulated single-wythe concrete masonry



Table 10 – Insulation Configurations using POLY-MOR Polyurethane Foam to meet the Requirements of the NECB 2011 for Single-Wythe Masonry Walls in Edmonton

Substrate	Insulating Procedure	Recommended Minimum Thickness		Overall Thermal Resistance	
		(mm)	(in)	$m^2 \cdot K/W$	hr•ft ² • ^o F/BTU
Above-ground wall	Low-density foam filled formwork	114	4 ¹ ⁄2	4.87	27.7
	High-density foam filled formwork	133	5 ¹ ⁄4	4.78	27.1
	Low-density spray applied foam	152	6	5.09	28.9
Below-ground wall	Low-density foam filled formwork	83	$3^{1/4}$	3.58	20.3
	High-density foam filled formwork	102	4	3.69	20.9
	Low-density spray applied foam	127	5	4.27	24.2

The minimum thicknesses provided in Table 10 are based on the assumption that the filled formwork procedure can produce thicknesses in 6.35mm (¹/₄ in) increments, while only 25.4mm (1 in) increments are possible with the spray application. The overall thermal resistances given are based on the corresponding insulating procedure and minimum recommended thickness. The thermal resistance furnished by the masonry wall and surface air films have been included. No other materials have been included, though it is likely that a waterproofing membrane of some kind would be present on walls below ground, and it may be necessary to finish the interior of walls with gypsum wallboard. Applying the foam on the exterior of single-wythe masonry walls may be the most economical method of making these walls Code compliant. The masonry would provide thermal mass on the interior and protect the insulation from fire, while the exterior insulation may serve as an air and weather barrier. The uniform surface produced by the filled formwork procedure could easily be finished with EIFS ("acrylic stucco") base and finish coats.

4.0 Conclusions and Recommendations

Single-wythe concrete masonry walls constructed at the University of Alberta were used as substrates for fourteen different test procedures for the application of POLY-MOR closed-cell polyurethane foam. The goal of the investigation was to determine the best application procedure for use as an insulation material. ASTM tests were conducted to ascertain the density and thermal conductivity of the foam in each of the fourteen wall mock-ups. Two-dimensional heat flow analysis software was used to simulate the insulated walls and determine the effective thermal resistance in each case. Based on the results of the investigation, the following comments, recommendations, and conclusions can be drawn:

- 1. The requirements of the NECB 2011 are much more stringent than those of the MNECB 1997. This will result in significant increases to the amount of insulation used in construction.
- 2. Due to a significant degree of thermal bridging across the webs, insulating the cores of concrete masonry furnishes minimal benefit. It is not possible to meet the requirements of NECB 2011 for above- or below-grade walls in any region in Canada using the grouting procedure alone.
- 3. The filled formwork procedure appears to be the superior application of the foam. It results in a uniform surface and provides better thermal resistance than the other application procedures investigated. The filled formwork procedure using low-density foam appears to be the most viable option.

- 4. The material and labour costs associated with the formwork could be a drawback associated with the filled formwork application procedure. It is believed that formwork that is either permanently left in place (see also Item 11) or easily reused could be solutions.
 - a. To minimize costs with reusable formwork:
 - i. The forms should be durable enough to be reused many times.
 - ii. The forms should be modular in nature so that they are relatively easy to disassemble, transport, and reassemble for use on various jobs.
 - iii. The forms should be easily removed after the foam has hardened.
 - iv. The forms should require minimal (if any) surface preparation work to prevent adhesion between the foam and the formwork. A polytetrafluoroethylene or other "non-stick" coating of the surface of the forms may suffice.
- 5. The filled formwork procedure using high-density foam is inferior to the lowdensity foam as an insulating material, but may still be an option where the insulation could be subjected to heavy wear.
- 6. If formwork costs cannot be reduced to a sufficiently low level, or if speed of completion is of vital importance, low-density spray applied foam may also be a viable option. However, a number of problems have been identified which will hinder the competitiveness of this option.
 - a. The quality of workmanship and the amount of wasted material depends more heavily on the experience of the applicator.
 - b. Even with an experienced applicator, more material waste is expected with the spray applied foam than with the filled formwork procedure.
 - c. The thermal resistance furnished by the procedure is inferior to the value reported for some rigid and spray applied foams already on the market.
- 7. Further investigations may be justified to capitalize on other properties of the foam. Quantifying the following should help make the product more marketable:
 - a. Degree of noise reduction provided.
 - b. Increase in racking strength of stud framed walls.
 - c. Increase in flexural and compressive strength in structural insulated panels.
 - d. Ability to absorb impact and blast energy.
 - e. Adequacy as an air, weather, and/or vapour barrier.

- 8. Exterior application of the insulation may be the most economical method of making single-wythe masonry walls compliant with the NECB.
- 9. Considering that the exterior application of insulation is not always possible, investigation into improving the fire resistance of the foam may be warranted. Possibilities that could be explored include:
 - a. Forms that can be left in place and are built of fire resistant materials like gypsum wallboard. These forms could be painted after insulating. The permanent formwork approach increases the cost of insulating, but it also reduces the cost of finishing.
 - b. Foam imbibed with an intumescent prior to application.
 - c. Foam coated with an intumescent after curing.

While it was demonstrated that there are some insulation products with comparable thermal resistance already available on the market, POLY-MOR polyurethane foam could still be a competitive insulation if other properties of the foam are also exploited. Though further investigation is recommended, including verification that the material meets all National and Provincial Building Code requirements for insulation materials, it appears that POLY-MOR closed-cell polyurethane foam possesses significant potential as an insulating material, not only for walls, but also for roofs, slabs on ground, and underground pipes.

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Appendix A: Unit Conversions

The following table provides unit conversion factors for various quantities presented in this report.

Quantity	in SI Units	Multiply by	= US Customary Units
Density	kg/m ³	0.06243	lb/ft ³
Length	mm	0.03937	in
Thermal Conductivity	W/m·K	0.5779	BTU/hr·ft·°F
Thermal Resistance	m ² ·K/W (RSI-value)	5.678	hr·ft ² ·°F/BTU (R-value)
Thermal Transmittance (U-value)	W/m²·K	0.1761	BTU/hr·ft ² ·°F

Appendix B: Hand Calculations

A sample calculation using the parallel flow path method is provided in Example 1 below.

Example 1: 190mm concrete masonry with no insulation.

Path 1: 50mm mortar, 90mm air space, 50mm mortar

$$R_{mortar}: \qquad \frac{50mm}{(1000\frac{mm}{m})(1.1 W \cdot m^{-1} \cdot K^{-1})} = 0.0455 \frac{m^2 K}{W}$$

$$R_{air}: \qquad 0.18 \frac{m^2 K}{W}$$

$$R_{i}: \qquad R_{mortar} + R_{air} + R_{mortar} = 0.271 \frac{m^2 K}{W}$$

$$A_{i} \qquad (10mm)(190mm) + (10mm)(390 + 5 + 5mm) = 5900mm^2$$

Path 2: 38mm face shell, 114mm air space, 38mm face shell

$$R_{\text{concrete}}: \qquad \frac{38mm}{(1000\frac{mm}{m})(1.54 W \cdot m^{-1} \cdot K^{-1})} = 0.0247 \frac{m^2 K}{W}$$

$$R_{\text{air}}: \qquad 0.18 \frac{m^2 K}{W}$$

$$R_2: \qquad R_{\text{concrete}} + R_{\text{air}} + R_{\text{concrete}} = 0.229 \frac{m^2 K}{W}$$

$$A_2: \qquad (190mm)(390 - (3)(31mm)) = 56 \ 430mm^2$$

Path 3: 190mm concrete (face shell + web + face shell).

R₃:
$$R_{concrete} = R_3 = \frac{190mm}{(1000\frac{mm}{m})(1.61 W \cdot m^{-1} \cdot K^{-1})} = 0.118 \frac{m^2 K}{W}$$
A₃:
$$(190mm)((3)(31mm)) = 17\ 670mm^2$$

Total area:

$$A_{\rm T}$$
: 5900 + 56 430 + 17 670 = 80 000 mm²

Overall Resistance of the materials:

R_T:
$$\left[\frac{5900}{(80\ 000)(0.271)} + \frac{56\ 430}{(80\ 000)(0.229)} + \frac{17\ 670}{(80\ 000)(0.118)}\right] = 0.191\frac{m^2K}{W}$$

Overall Resistance of the wall (including surface air films):

$$R_{\rm U}: \qquad 0.03 + 0.191 + 0.12 = 0.341 \frac{m^2 \kappa}{W}$$

The U-value of the assembly is the reciprocal of R_U , or 2.93 W/m²K in this example.

Example 2 is a sample calculation illustrating how the results of two analyses were combined using the Parallel Path method to approximate the overall thermal resistance of the entire wall.

Example 2: 190mm concrete masonry unit and 10mm bed joint with no insulation.

$$R_T = \left(\frac{A_1U_1}{A} + \frac{A_2U_2}{A}\right)^{-1} = \left((0.95)(5.4929) + (0.05)(3.6910)\right)^{-1} = 0.185 \frac{m^2 K}{W}$$
$$R_U = 0.03 + 0.185 + 0.12 = 0.335 \frac{m^2 K}{W}$$

A sample calculation using the method of isothermal planes is provided below.

Example 3: 190mm concrete masonry with no insulation.

Layer 1: 38mm Pathi of Layer 1: 38mm mortar $R_{1,1}$: $\frac{38}{(1000)(1.1)} = 0.0345 \frac{m^2 K}{W}$ $A_{1,1}$: 5900mm²

Path 2 of Layer 1: 38mm concrete (face shell)

R_{1,2}:
$$\frac{38}{(1000)(1.61)} = 0.0236 \frac{m^2 K}{W}$$

 $A_{1,2}$:

74 100mm²

Resistance of Layer 1:

R₁:
$$\left(\frac{5900}{(80\ 000)(0.0345)} + \frac{74\ 100}{(80\ 000)(0.0236)}\right)^{-1} = 0.0242 \frac{m^2 K}{W}$$

Layer 2: 12mm

Pathi of Layer 2: 12mm mortar

R_{2,1}:
$$\frac{12}{(1000)(1.1)} = 0.0109 \frac{m^2 K}{W}$$

A_{2,1}: 5900mm²

Path 2 of Layer 2: 12mm concrete (webs)

R_{2,2}:
$$\frac{12}{(1000)(1.61)} = 0.00745 \frac{m^2 K}{W}$$

A_{2,2}: 17 670mm²

Path 3 of Layer 2: 12mm out of 114mm core air space

R_{2,2}:
$$\frac{12}{(1000)(0.633)} = 0.0189 \frac{m^2 K}{W}$$
A_{2,2}: 56 430mm²

Resistance of Layer 2:

R₂:
$$\left(\frac{5900}{(80\ 000)(0.0109)} + \frac{17\ 670}{(80\ 000)(0.00745)} + \frac{56\ 430}{(80\ 000)(0.0189)}\right)^{-1} =$$

 $0.0136 \frac{m^2 K}{W}$

Layer 3: 90mm

Path 1 of Layer 3: 90mm mortar joint air space

R_{3,1}:
$$0.18 \frac{m^2 K}{W}$$

A_{3,1}:

Path 2 of Layer 3: 90mm concrete (webs)

R_{3,2}:
$$\frac{90}{(1000)(1.61)} = 0.0559 \frac{m^2 K}{W}$$

A_{3,2}: 17 670mm²

5900mm²

Path 3 of Layer 3: 90mm out of 114mm core air space

$$R_{3,3}: \qquad \frac{90}{(1000)(0.633)} = 0.142 \frac{m^2 K}{W}$$

A_{3,3}: 56 430mm²

Resistance of Layer 3:

R₃:
$$\left(\frac{5900}{(80\ 000)(0.18)} + \frac{17\ 670}{(80\ 000)(0.0559)} + \frac{56\ 430}{(80\ 000)(0.142)}\right)^{-1} = 0.107 \frac{m^2 K}{W}$$

Layer 4: Duplicate of layer 2

Layer 5: Duplicate of layer 1

Overall resistance of the materials:

$$R_{\rm T}: \qquad \sum_{i=1}^{5} R_i = 2(R_1 + R_2) + R_3 = (2)(0.0242 + 0.0136) + 0.107 = 0.183 \frac{m^2 \kappa}{w}$$

Overall resistance of the assembly:

 $R_{\rm U}: \quad 0.03 + 0.183 + 0.12 = 0.333 \frac{m^{2}\kappa}{W}$

U-value: 3.01 W/m²K