

University of Alberta

A STUDY OF LATER PHASE STATIC SINGLE ASSIGNMENT IN THE OPEN
RESEARCH COMPILER

by

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A thesis submitted to the Faculty of Graduate Studies and Research in partial fulfillment of the requirements for the degree of **Master of Science**.

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*If you have no voice, scream;
if you have no legs, run;
if you have no hope, invent.*

- Cirque du Soleil's *Alegria*

Abstract

Static single assignment (SSA) is an intermediate code representation used in contemporary production compilers. In processor architectures that implement predicated execution, the intermediate code is typically converted out of SSA form before later phases in the compilation process. In such architectures, the elegant framework provided for code optimizations by SSA is not available after predication is used to eliminate conditional expressions. Thus such compilers cannot benefit from SSA in later compiler phases. ψ -SSA is a new intermediate representation that allows the maintenance of SSA after if-conversion.

This thesis introduces ψ -SSA in a later phase of the Open Research Compiler (ORC). Most traditional SSA algorithms use a worklist to process the nodes in the Control Flow Graph representation of the program when building the SSA form. We propose an improvement to the SSA construction algorithm that reduces both the number of worklists processed as well as the size of the initial set of nodes in some of the remaining worklists. We measure the gains of this improvement in the standard SPEC CINT2000 benchmark suite.

To the memory of Dr. Cyril P. Coombs,
who valued education as highly as anyone else I have ever known.

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List of Symbols

\prec_c	congruence class order
ϕ_{cc}	ϕ -congruence class
$A(x)$	set of nodes containing definitions of x
ADT	augmented dominator tree
$B_i.level$	level number for node B_i
BB	basic block
CFG	control flow graph
DF	dominance frontier
DF^+	iterated dominance frontier
DF_{local}	local dominance frontier
DF_{up}	dominance frontier to be passed up
EDF	edge dominance frontier
<i>equidom</i>	equidominates
GTN	global temporary name
I	interference graph
<i>idom</i>	immediate dominator
IPA	interprocedural analysis
J	join set
J^+	iterated join set
J-edge	join edge
L_{in}	live-in set
L_{out}	live-out set
LNO	loop nest optimizations
M	merge relation
OP	operation
ORC	Open Research Compiler
PSSA	predicated static single assignment
$S_\phi(x)$	minimum set of join nodes requiring a ϕ -function for x
SPEC	Standard Evaluation Performance Corporation
SSA	static single assignment
TN	temporary name
WHIRL	Winning Hierarchical Intermediate Representation Language
Z_{B_i}	zone associated with node B_i
$z[B_i]$	zone size of Z_{B_i}

Chapter 1

Introduction

Static Single Assignment (SSA) is a modern intermediate code representation that aids dataflow analysis by ensuring that each use of a variable can only be associated with one definition. The SSA form is traditionally removed well before the code generator in a production compiler. In particular, the SSA algorithm has not been capable of maintaining its form after predication is used to eliminate conditional branches. Architectures that support predication generally do not use SSA in later phases. Hence, code transformations that occur after predication in supported architectures cannot reap the benefits afforded by the elegant SSA framework.

In this thesis, a method for constructing the SSA form in a later phase of the Open Research Compiler (ORC) is presented. More importantly, an algorithm for allowing SSA after if-conversion, called ψ -SSA, is discussed. ψ -SSA combines traditional SSA techniques with ideas incorporating the unique properties of predicated code. Using this method, SSA can be maintained throughout global instruction scheduling. Our initial experiments suggest that building and removing the SSA form in the ORC code generator does not significantly increase compile-time, nor add an overwhelming number of instructions to the baseline results. As well, run time performance is not degraded by the additional work performed during the SSA algorithm.

Current SSA construction algorithms use a worklist method to identify nodes in the Control Flow Graph where ϕ -functions have to be inserted. This thesis suggests an improvement to this technique whereby individual worklists are compared for equality. If two sets to be iterated over by a worklist are identical, one of the worklists can be eliminated, thus reducing the amount of work performed by the algorithm. Additionally, if one set is a subset of the other, the number of elements

in the second worklist can be decreased. On average, 45% of worklist elements to be processed can be saved when the subset relationship is detected.

We begin this thesis with a presentation of background material required to discuss the remainder of the document in Chapter 2. Then, Chapter 3 formally introduces the concept at the heart of this work, SSA. Using the key ideas from Chapter 3, Chapter 4 gives an overview of the current state of the art with respect to SSA. The three main ϕ -placement techniques are introduced in detail with fully expanded examples. As well, the process of removing the SSA form is discussed, focusing on three techniques currently being studied. The issue of predicated SSA is then the topic of Chapter 5, where the methods discussed are extensions to the traditional SSA algorithms of Chapter 4.

The work of this thesis is performed on the ORC, which is thus the subject of Chapter 6. The ORC's current capabilities are discussed, as well as the modified code generator that results from including ψ -SSA. Our suggested improvement to the SSA ϕ -placement algorithm comes next in Chapter 7, where opportunities for improvement on the ORC are identified. Finally, Chapter 8 presents an experimental evaluation of the modified code generator with respect to compile and run times, instructions inserted, and instructions executed, for a selection of programs from the SPEC CINT2000 benchmark suite. Directions for future work are discussed in Chapter 9, with conclusions tying the entire thesis together found in Chapter 10.

1.1 Contributions of this Thesis

This thesis is a comprehensive study of the effects of SSA in a later phase of the compilation process. The major contributions of this thesis include:

1. A detailed examination of current SSA algorithms, using step-by-step examples to illustrate their behaviour. SSA methods for predicated code are also discussed. Particular attention is given to the ψ -SSA technique, which is examined with examples.
2. A proof showing that the iterated join set of a set of nodes can be calculated as the union of the iterated join sets of its partitions.
3. An improvement to the standard ϕ -placement algorithm, based on the proof from item 2, that reduces both the number of worklists processed as well as the

size of the initial set of nodes in some of the remaining worklists. We quantify this enhancement using a selection of the SPEC CINT2000 benchmark suite.

4. A preliminary experimental evaluation of SSA in a later phase of the ORC. The modified ORC code generator includes an implementation of ψ -SSA, which extends the SSA form through global instruction scheduling.¹
5. The first measurements of the effects of later phase SSA on compile and run times, the number of instructions inserted, and the number of those executed using the later phase SSA algorithm.²

¹The source code for the later phase SSA implementation was written by Arthur Stoutchinin. I contributed with the porting to an ORC environment and with the testing on an Itanium2-based machine.

²These numbers are preliminary and are based on an initial implementation. Several improvements to this implementation are planned, and once more definitive results are available, a publication will be prepared. Therefore, we are requesting that the publication of this thesis be withheld for a year.

Chapter 2

Background Material

Most definitions found in this section are paraphrased from Aho *et al.* [1]. Exceptions are noted.

Definition 1. A *basic block (BB)* is formed by a sequence of consecutive statements in which flow of control enters at the beginning and only leaves at the end.

Definition 2. A *control flow graph, $CFG = G(V, E)$* , is a directed graph representing the flow of control in a program, where V is a set of basic blocks and an edge $(B_i \rightarrow B_j) \in E$ indicates that the execution of the program may be transferred from the basic block B_i to the basic block B_j .

In Figure 2.1, B_0 is the start node and B_6 is the end node of the CFG. Nodes B_2 and B_3 are *successors* of node B_1 and *predecessors* of node B_4 .

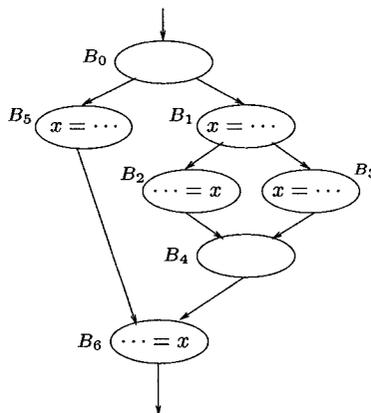


Figure 2.1: A control flow graph

Definition 3. Within a basic block, there is a *point* between any two consecutive statements, as well as a point before the first statement, and a point after the last statement.

Figure 2.2 shows some points for the CFG of Figure 2.1. Note that the edge from node B_1 to node B_3 contains 2 points.

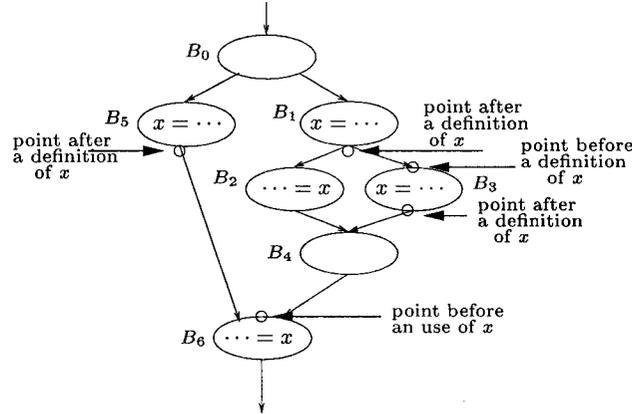


Figure 2.2: Points in a CFG

Definition 4. A *path* from p_1 to p_n is a sequence of points p_1, p_2, \dots, p_n such that for each $i : 1 \leq i \leq n - 1$, either

1. p_i is the point immediately preceding a statement and p_{i+1} is the point immediately following that statement in the same block; *or*
2. p_i is the end of some block and p_{i+1} is the beginning of a successor block.

We often refer to paths in terms of the basic blocks in which their points appear. Given a collection of points such that $p_i \in B_i, p_j \in B_j, \dots, p_n \in B_n$, then a path that includes p_i, p_j, \dots, p_n may be referred to as the path B_i, B_j, \dots, B_n .

Definition 5. A *definition* of a variable x is a statement that assigns a value to x .

In the CFG in Figure 2.1, the statements in basic blocks B_1, B_3 , and B_5 are all definitions of x .

Definition 6. Let statement S_i define a variable x and statement S_j have x as an operand. If there is a path P from S_i to S_j that contains no other definitions of x , then S_j *uses* the value of x defined by S_i .

The statement in node B_2 of the CFG in Figure 2.1 uses the value of x defined in node B_1 , since the path from B_1 to B_2 contains no other definitions of x . We say that the definition of x from B_1 *reaches* B_2 . If another definition did occur along the single path from B_1 to B_2 , the definition found in B_1 would be *killed*.

Definition 7. A statement S_i that defines a variable x *kills* all previous definitions of x that reach S_i along the paths that include S_i .

In Figure 2.1, the definition of x in node B_1 is killed along the path B_1, B_3, B_4 since B_3 contains a definition of x , but is not killed along the path B_1, B_2, B_4 .

When multiple definitions of a variable x appear in a CFG, we are interested in the points that a given definition of x reaches.

Definition 8. Suppose that a variable x is defined in a statement S_i in a node of a $CFG = G(V, E)$. We say that S_i 's definition of x is *live* at point p_j in G if:

1. there is at least one path from S_i to p_j in which x is not killed; and
2. there exists a path from p_j to a use of x that contains no definition of x [33].

Definition 9. Two variables x and y in a program *interfere* if there exists a point p_i in the graph in which both variables are live.

Definition 10. The *live-in* set of a basic block B_i (denoted $L_{in}(B_i)$) is the set of all variables live on entry to B_i , while the *live-out* set of B_i (denoted $L_{out}(B_i)$) is the set of variables live upon exit from B_i .

We want to know how individual CFG nodes relate to each other. The concept of *dominance* is important because it enables the compiler to prove that some definitions cannot reach some uses of a variable.

Definition 11. Suppose B_0 is the start node of a $CFG = G(V, E)$. Consider two nodes B_i and B_j . If every path in G from B_0 to B_j goes through B_i , then B_i *dominates* B_j . Every node dominates itself. If B_i dominates B_j and $B_i \neq B_j$, then B_i *strictly dominates* B_j [18].

In the CFG of Figure 2.1, node B_0 dominates every node in the graph. Node B_1 dominates nodes B_1, B_2, B_3 , and B_4 . Node B_1 does not dominate node B_6 because there is another path from B_0 to B_6 , namely the path B_0, B_5, B_6 . A convenient representation of the dominance relationships among nodes in a CFG is given by the *dominator tree*.

If there exists a downward path P from node B_i to B_j in a directed graph, then B_i is an *ancestor* of B_j and B_j is a *descendant* of B_i . These relationships are *strict* if $B_i \neq B_j$.

Definition 12. Suppose B_0 is the start node of a $CFG = G(V, E)$. The corresponding *dominator tree* for G has B_0 as its root, and each node B_i dominates its descendants in the tree.

The dominator tree corresponding to the CFG in Figure 2.1 is given in Figure 2.3. Nodes B_2 , B_3 and B_4 are *children* of node B_1 and B_0 is the *parent* of nodes B_1 , B_5 and B_6 . The terms parent and child will be reserved for the dominator tree, while predecessor and successor will reference the CFG. Also, the terms descendant and ancestor will be used in conjunction with the dominator tree. In Figure 2.3, node B_0 is an ancestor of every other node, while node B_2 is a strict descendant of nodes B_0 and B_1 .

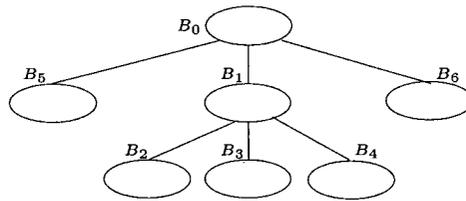


Figure 2.3: A dominator tree

We can also associate a *level* with nodes in the dominator tree.

Definition 13. A *level number* for a node B_i in the dominator tree (written $B_i.level$) is the depth of B_i from the root of the tree [32].

In Figure 2.3, $B_0.level = 0$, $B_1.level = B_5.level = B_6.level = 1$, and $B_2.level = B_3.level = B_4.level = 2$.

Definition 14. Suppose that B_0 is the start node of a $CFG = G(V, E)$. Consider a node B_i in G . The *immediate dominator (idom)* of B_i is the last strict dominator of B_i on any path from B_0 to B_i [18].

The children of a node B_i in a dominator tree are all immediately dominated by B_i . In Figure 2.3, node B_0 immediately dominates nodes B_1 , B_5 and B_6 . Node B_1 immediately dominates nodes B_2 , B_3 , and B_4 .

Definition 15. Consider a node B_i in a $CFG = G(V, E)$. The *dominance frontier (DF)* of B_i is the set of all nodes $B_j \in V$ in G such that B_i dominates a predecessor of B_j , but B_i does not strictly dominate B_j itself [18].

There are different ways to find the dominance frontier of a CFG node B_i . We can start by identifying all the nodes that B_i dominates. These nodes are found by searching the subtree rooted at B_i in the dominator tree. For example, to find the dominance frontier of B_1 in the CFG of Figure 2.1, we start by finding the nodes that are dominated by B_1 , as shown in Figure 2.4(a). We now want to check the successors of these nodes. The set of successors is indicated by the rectangle in Figure 2.4(b). We are looking for successors that are not themselves strictly dominated by B_1 . Thus, $DF(B_1) = \{B_6\}$.

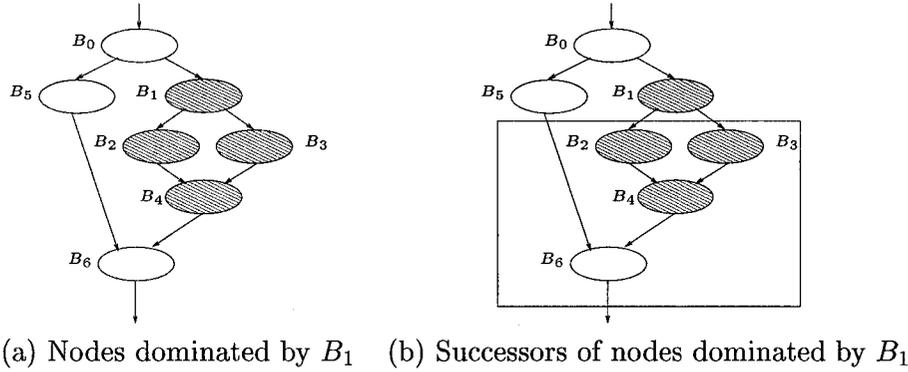


Figure 2.4: Finding a dominance frontier

Another computation method for finding the dominance frontier requires the *local dominance frontier* and the dominance frontier *passed* to a node B_i from nodes that B_i immediately dominates.

Definition 16. Consider a node B_i in a $CFG = G(V, E)$. The *local dominance frontier* (DF_{local}) of B_i is the set of successors of B_i that are not strictly dominated by B_i [18].

Consider node B_2 from Figure 2.1. We know from the dominator tree in Figure 2.3 that B_2 does not strictly dominate any nodes. The set of successors of B_2 is shown by the rectangle in Figure 2.5. The local dominance frontier can then be found by subtracting the set of nodes strictly dominated by B_2 from the set of successors of B_2 . Since B_2 does not strictly dominate any node, the local dominance frontier of B_2 is just its set of successors. Thus, $DF_{local}(B_2) = \{B_4\}$. Similarly, $DF_{local}(B_3) = \{B_4\}$.

Definition 17. Consider a node B_i in a $CFG = G(V, E)$. The dominance frontier of B_i that can be *passed up* (DF_{up}) to the immediate dominator of B_i is the set

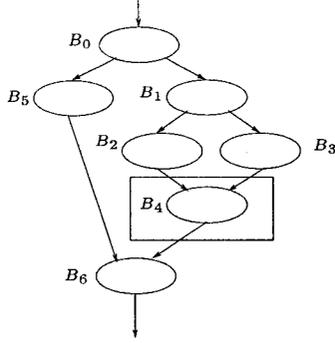
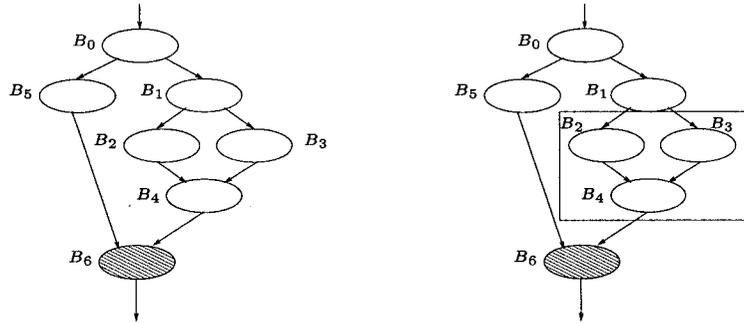


Figure 2.5: Finding a local dominance frontier

of nodes in the dominance frontier of B_i that are not strictly dominated by the immediate dominator of B_i [18].

Consider node B_4 of Figure 2.1. We want to compute $DF_{up}(B_4)$. From Figure 2.3, the immediate dominator of node B_4 is node B_1 . We need $DF(B_4)$. From Figure 2.3, we know that node B_4 only dominates itself. The only successor of B_4 is B_6 . Since B_6 is not strictly dominated by B_4 , $DF(B_4) = \{B_6\}$, shown in Figure 2.6(a). We also need the set of nodes strictly dominated by $idom(B_4) = B_1$, as indicated by the rectangle in Figure 2.6(b). We are looking for shaded nodes not found in this rectangle (*i.e.*, nodes in $DF(B_4)$ that are not strictly dominated by B_1). Thus, $DF_{up}(B_4) = \{B_6\}$.



(a) Dominance frontier of B_4 (b) Nodes strictly dominated by B_1

Figure 2.6: Finding a dominance frontier passed up to an immediate dominator

The dominance frontier can also be computed using Equation 2.1 [18].

$$DF(B_i) = DF_{local}(B_i) \cup \bigcup_{B_j \in Children(B_i)} DF_{up}(B_j) \quad (2.1)$$

Recall that the children of a node are found by looking at the dominator tree.

Using Equation 2.1, the dominance frontier of node B_1 in Figure 2.1 can be calculated:

$$\begin{aligned} DF(B_1) &= DF_{local}(B_1) \cup \bigcup_{B_j \in Children(B_1)} DF_{up}(B_j) \\ &= DF_{local}(B_1) \cup (DF_{up}(B_2) \cup DF_{up}(B_3) \cup DF_{up}(B_4)) \end{aligned}$$

The local dominance frontier of B_1 is the set of nodes strictly dominated by B_1 subtracted from the set of successors of B_1 . Thus, $DF_{local}(B_1) = \{B_2, B_3\} - \{B_2, B_3, B_4\} = \emptyset$.

For the dominance frontiers being passed up to B_1 , it has already been shown that $DF_{up}(B_4) = \{B_6\}$. Nodes B_2 and B_3 do not pass up anything to B_1 . Since each of B_2 and B_3 only dominates itself, and their common successor is node B_4 , B_4 is the only element in each of their dominance frontiers. B_4 itself is strictly dominated by node B_1 , and it therefore does not contribute to the dominance frontier of B_1 . Thus, $DF_{up}(B_2) = DF_{up}(B_3) = \emptyset$.

The final equation then becomes

$$\begin{aligned} DF(B_1) &= DF_{local}(B_1) \cup (DF_{up}(B_2) \cup DF_{up}(B_3) \cup DF_{up}(B_4)) \\ &= \emptyset \cup (\emptyset \cup \emptyset \cup \{B_6\}) \\ &= \{B_6\} \end{aligned}$$

The result of Equation 2.1 is the same as was computed using Definition 15.

Chapter 3

Static Single Assignment

Within compiler research, much work has been done towards effective code analysis and optimization techniques. Traditionally achieved with def-use and use-def chains,¹ code analysis techniques have matured. Now, methods for understanding and improving code focus on the relationships among individual statements and basic blocks [25]. Briggs *et al.* argue that the *static single assignment* (SSA) form is a sparse representation of these relationships [7].

Definition 18. A program is in *static single assignment* form if each variable is defined only once.

An SSA form is attractive for compiler code analysis because it reduces the complexity of dataflow analysis. In SSA each variable has a single definition, thus whenever a use of the variable is encountered, there is only one place in the code where the value consumed by that use could have been produced. Allen and Kennedy claim that the most important benefit of the SSA form is the improved performance of optimization algorithms such as constant propagation, forward substitution of expressions, and induction-variable substitution [3]. In particular, an entire category of dependences that arise from reusing variables (resulting in an anti-dependence) or reassigning variables (resulting in an output dependence) can be eliminated, called *false dependences*. Then, the program analysis is left only with true dependences (arising from flow dependences that cannot be eliminated by SSA) with which to contend [38].

Consider the sample code in Figure 3.1. The code shown in Figure 3.1(a) is not in SSA form, since there are two definitions of x and y . In this example, a simple

¹Def-use chains are lists that associate with each definition of a variable the possible run-time uses of that definition. Similarly, use-def chains map definitions of a variable that could be associated with a particular use [3].

renaming of variables produces the SSA form shown in Figure 3.1(b).

$x \leftarrow 3;$	$x_1 \leftarrow 3;$
$y \leftarrow x;$	$y_1 \leftarrow x_1;$
$x \leftarrow 4;$	$x_2 \leftarrow 4;$
$y \leftarrow x;$	$y_2 \leftarrow x_2;$
(a) Non-SSA form	(b) SSA form

Figure 3.1: Simple conversion into SSA

Now consider the code of Figure 3.2. The code in Figure 3.2(a) is not in SSA form, since two definitions of x exist in two distinct control flow paths. By renaming the variables, the code of Figure 3.2(b) is produced.

if $x > a$	if $x_1 > a$	if $x_1 > a$
$x \leftarrow a;$	$x_2 \leftarrow a;$	$x_2 \leftarrow a;$
else	else	else
$x \leftarrow b;$	$x_3 \leftarrow b;$	$x_3 \leftarrow b;$
$y = x;$	$y_1 = ?;$	$y_1 = \phi(x_2, x_3);$
(a) Non-SSA form	(b) Partial SSA form	(c) SSA form

Figure 3.2: Conversion into SSA form

In the final statement of Figure 3.2(b), the value of x assigned to y_1 depends on which path is executed at runtime. The potential for a use to be associated with more than one definition occurs at the first node that belongs to two distinct paths in the CFG. Such nodes are called *join nodes* [19].

Alpern and Rosen first introduced a ϕ -function, which is an abstraction used in the join node, to “decide” which definition to use [4, 30]. Figure 3.2(c) shows the example code in SSA form.

ϕ -functions are found in the SSA intermediate code representation, and are not executable. Inserting ϕ -functions can be done trivially by determining every variable used in a join node. Let x be a variable used in a join node B_j . Then we need to look at definitions of x that are live on entry to B_j . A ϕ -function can be inserted at the point following each such definition of x . However, the number of ϕ -functions that are actually required can be much smaller than those inserted by this method. Inserting unnecessary ϕ -functions increases the compilation time.

Let x be a variable defined in two or more basic blocks in a $CFG = G(V, E)$.

$S_\phi(x)$ is defined as the minimum set of join nodes in V that must receive a ϕ -function for x . A method for computing $S_\phi(x)$ is required. Let $A(x)$ be the set of nodes in V that contain a definition of x . Clearly, $DF(A(x)) \subset S_\phi(x)$. However, a ϕ -function is itself a definition of x , therefore an iterated method to compute $S_\phi(x)$ is needed. Based on this formulation, the notion of dominance frontiers from Chapter 2 can be extended to sets of nodes.

When constructing the SSA form of a program, if a variable x has multiple definitions, it is desirable to insert a collection of ϕ -functions for x at a time instead of just a single ϕ -function. We therefore want to analyze sets of nodes [18]. Let X be a set of CFG nodes. Then,

$$DF(X) = \bigcup_{B_i \in X} DF(B_i) \quad (3.1)$$

In Section 4.1.1, we will examine the relationship between the *iterated dominance frontier* and where ϕ -functions should be placed.

Definition 19. Given a set of CFG nodes X , the *iterated dominance frontier* (DF^+) of X is the limit of the following sequence [18]:

$$DF_1 = DF(X) \quad (3.2)$$

$$DF_{i+1} = DF(X \cup DF_i) \quad (3.3)$$

We make a key assumption during the analysis of a CFG. To ensure that we never have a variable that is used without being previously defined, we assume that all variables are defined in the start node of the CFG. Code analysis is therefore simplified, as we can always assume there is a single definition with which to associate a use.

Definition 20. Suppose X is a subset of nodes in a $CFG = G(V, E)$ such that the start node is in X . The *join set* (J) of X is then the set of all nodes $B_j \in V$ for which distinct nodes $B_i, B_k \in X$ exist where a pair of paths B_i, \dots, B_j and B_k, \dots, B_j intersect only at B_j [19].

Definition 21. Given a set of CFG nodes X , the *iterated join* (J^+) of X is the limit of the increasing sequence [18]:

$$J_1 = J(X) \quad (3.4)$$

$$J_{i+1} = J(X \cup J_i) \quad (3.5)$$

Cytron *et al.* showed that $S_\phi(x) = J^+(A(x))$, *i.e.*, the minimum set of nodes that require a ϕ -function for a variable x is the iterated join of the set of nodes that define x [19].

Many algorithms have been developed for constructing the SSA form of a program. Among these algorithms, techniques for ϕ -function placement and variable renaming have been developed. However, since the ϕ -function has yet to be found in an instruction set of a machine architecture, the “function” is still not executable. In fact, an instruction that decides which control path was taken is unlikely to exist. Because the function cannot be executed, it must be eliminated before code generation, since there is no code corresponding to the ϕ -function. Therefore, ϕ -function removal methods are also of interest. The algorithms for all the phases of SSA construction and removal are presented in Chapter 4.

Chapter 4

SSA Algorithms

4.1 Algorithms for ϕ -Function Insertion

The insertion of ϕ -functions is widely thought to be the core of the SSA construction problem. Several algorithms were proposed for deciding where ϕ -functions should be placed.

4.1.1 Cytron *et al.*

The primary ϕ -placement method still used in many compilers was presented by Cytron *et al.* in 1989 [18], and further elaborated on in 1991 [19]. This method uses dominance frontiers to determine where the ϕ -functions should be placed. The relationship between dominance frontiers and ϕ -functions is established by Theorem 1 [19].

Theorem 1. *The set of nodes that need ϕ -functions for any variable x is the iterated dominance frontier $DF^+(A(x))$. Equivalently,*

$$J^+(A(x)) = DF^+(A(x)) \quad (4.1)$$

Cytron *et al.* compute the dominance frontiers needed for their ϕ -placement algorithm using Equation 2.1.

The algorithm takes a $CFG = G(V, E)$ and V as input. Also required for each node $B_i \in V$ is $DF(B_i)$, as well as $A(x)$ for each variable x in G . The main loop of this worklist algorithm iterates for every variable. For each variable, a worklist, W , represents the nodes being processed. Suppose an iteration of the algorithm's main loop is working on a variable v . W is initialized to $A(v)$. Then, if $B_i \in W$, a ϕ -function is inserted in every $B_j \in DF(B_i)$, and B_i is removed from W . Recall that a node with a ϕ -function for v is itself in $A(v)$. Thus for every $B_i \in W$, each

```

y live-in
if (y > 1)
  x = 2
else if (y < 1)
  x = 3
else x = 10
for (i = 0; i < y; i ++){
  if (x > y)
    x ++
  else
    x --
}
return(x + y)
x, y are live-out

```

Figure 4.1: Pseudo-code for the running example

$B_j \in DF(B_i)$ is also relevant, and therefore included in W . The algorithm ends when $W = \emptyset$.

Consider Figure 4.2, the CFG for the running example in Figure 4.1. The only non-empty dominance frontiers for this example are given in Figure 4.3. Let $S_\phi(x)$ be the set of nodes that are assigned ϕ -functions for variable x .

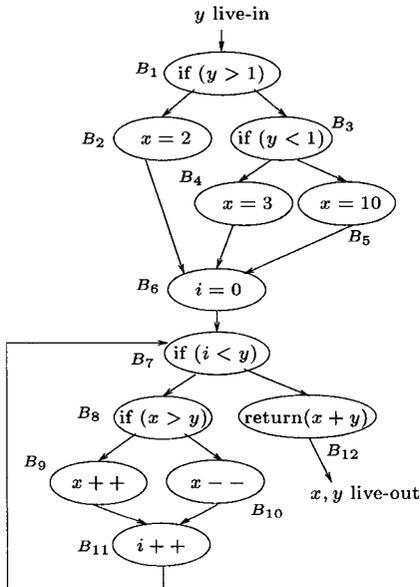


Figure 4.2: CFG for the running example

The loop iteration for x begins by initializing $W = A(x) = \{B_2, B_4, B_5, B_9, B_{10}\}$. Based on the dominance frontiers of these nodes, $S_\phi(x) = \{B_6, B_{11}\}$, and nodes B_2 ,

$$\begin{array}{ll}
DF(B_2) = \{B_6\} & DF(B_9) = \{B_{11}\} \\
DF(B_4) = \{B_6\} & DF(B_{10}) = \{B_{11}\} \\
DF(B_5) = \{B_6\} & DF(B_{11}) = \{B_7\}
\end{array}$$

Figure 4.3: Dominance frontiers for the running example

B_4 , B_5 , B_9 and B_{10} are removed from W . Then each of nodes B_6 and B_{11} need to be analyzed, and are thus added to W . Since $DF(B_{11}) = \{B_7\}$, node B_7 is added to $S_\phi(x)$ and nodes B_6 and B_{11} are eliminated from W . Node B_7 must itself be processed, and is appended to W . Since $DF(B_7) = \emptyset$, B_7 is taken from W and there are no additional nodes to include in W . Thus, $S_\phi(x) = \{B_6, B_7, B_{11}\}$, and ϕ -functions for x can be added to nodes B_6 , B_7 and B_{11} . With $W = \emptyset$, this loop iteration is complete. The main loop will then proceed for every variable in the CFG.

Cytron and Ferrante continued their work in 1995 with improvements to their original algorithms [21]. In particular, the new work avoids computing all the dominance frontiers by producing an order to determine the entire DF relation. Using the order ensures that no elements of the DF relation will be skipped. They focus on two cases. The more general case checks, for an edge $(B_i \rightarrow B_j)$ in the CFG, nodes in the dominator tree between the immediate dominator of B_j and B_i , which have been established in the DF relation. The order used is a reverse depth-first numbering, hence nodes are processed if their immediate dominators have decreasing depth-first numbers.

The alternate case encompasses nodes that are siblings in the dominator tree. The pre-determined order from the general case is not applicable, since both nodes have the same immediate dominator. A new relationship is needed [21].

Definition 22. Consider a node B_i . The *equidominates* of B_i are those nodes with the same immediate dominator as B_i . Equivalently,

$$equidom(B_i) = \{B_j \mid idom(B_j) = idom(B_i)\} \quad (4.2)$$

The equidominates are partitioned into blocks of nodes that are contained in each other's iterated dominance frontiers. However the cost of computing individual dominance frontiers is avoided. The required order is then computed based on the edges between equidominates.

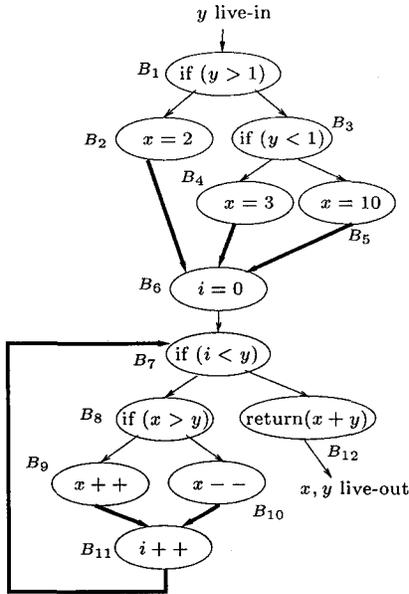


Figure 4.4: J-edges of the CFG for the running example, shown in bold print

This method avoids the computation of all dominance frontiers, and also the recursive iteration through the nodes in the dominance frontiers of the worklist nodes.

The final form that Cytron and Ferrante have presented is *pruned* SSA [12]. This method only places a ϕ -function for x at a join node if x is used within or after the join node, *i.e.*, x is live at the entry point of the join node. This strategy differs from the original algorithm, which places ϕ -functions at all join nodes.

4.1.2 Sreedhar and Gao

The next ϕ -placement method was introduced in 1995 by Sreedhar and Gao [32]. This algorithm requires the construction of a *DJ-graph*, a modification of the traditional dominator tree. The DJ-graph contains all dominator tree edges (referred to as *D-edges*), as well as a set of *J-edges* [32].

Definition 23. An edge $(B_i \rightarrow B_j)$ in a $CFG = G(V, E)$ is a *join edge (J-edge)* if B_i does not strictly dominate B_j .

A DJ-graph can be constructed by inserting join edges from the CFG into the dominator tree. Figure 4.4 indicates the J-edges of the CFG from Figure 4.2 in bold print. Figure 4.5(b) shows the DJ-graph corresponding to the dominator tree of the CFG shown in Figure 4.2. J-edges are indicated by dotted lines in the graph. Also given in the figure are the node levels.

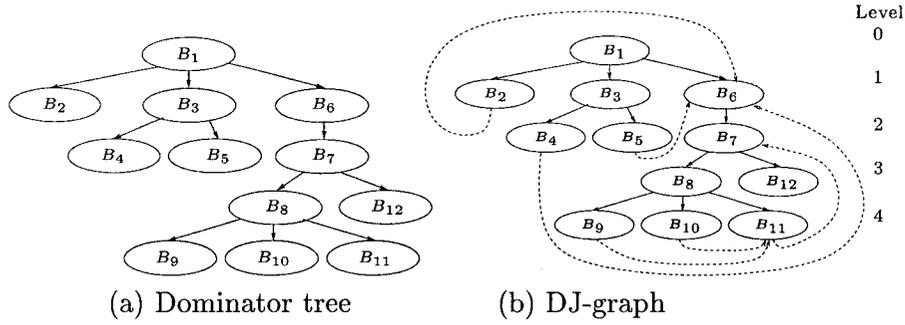


Figure 4.5: Constructing the DJ-graph for the running example

This algorithm takes as input a DJ-graph and a subset of CFG nodes, N_α , and returns $DF^+(N_\alpha)$. It begins by initializing an array PB to N_α , with indices based on the level numbers of the individual nodes.¹ The start level is set to be the highest level. Then, each level represented in the PB is processed by visiting each node in that level stored in PB . Say node B_i of level l is the current node being processed. For each successor B_j of B_i , if $(B_i \rightarrow B_j)$ is a J-edge, then B_j is included in DF^+ and is placed in PB . If $(B_i \rightarrow B_j)$ is a D-edge, B_j is recursively processed.

Consider the example in Figure 4.2. Let $N_\alpha = A(x) = \{B_2, B_4, B_5, B_9, B_{10}\}$. We then initialize $PB = N_\alpha$. Processing higher level nodes first means nodes B_9 and B_{10} from level 4 are examined. $(B_9 \rightarrow B_{11})$ is a J-edge (see Figure 4.5(b)), thus $DF^+ = \{B_{11}\}$, and $PB = PB \cup \{B_{11}\}$. Node B_{10} 's only outgoing J-edge is with node B_{11} , which is already in DF^+ . Now we process node B_{11} in level 4. $(B_{11} \rightarrow B_7)$ is a J-edge, therefore $DF^+ = \{B_{11}, B_7\}$, and $PB = PB \cup \{B_7\}$. We continue processing at level 2 with node B_4 . $(B_4 \rightarrow B_6)$ is a J-edge, hence $DF^+ = \{B_{11}, B_7, B_6\}$ and $PB = PB \cup \{B_6\}$. The only other J-edges in the DJ-graph are directed to node B_6 , thus we are done, and ϕ -functions for x can be added to nodes B_6 , B_7 , and B_{11} . This process can be repeated with other initial sets; in particular, with the sets representing assignments of the other variables in the CFG.

4.1.3 Bilardi and Pingali

The third ϕ -placement algorithm was first introduced by Bilardi and Pingali in 1995 [28]. In 2003, they revisited the description of the original algorithm in an extensive comparative study of SSA construction techniques [5, 6]. This algorithm uses a

¹ PB refers to the ‘‘PiggyBank’’ used in Sreedhar and Gao’s algorithm [32].

new data structure, the *augmented dominator tree*. First, the dominance frontier is defined in terms of edges instead of nodes.

Definition 24. Suppose $(B_i \rightarrow B_j)$ is an edge in a $CFG = G(V, E)$. If $B_i \neq idom(B_j)$, then the edge $(B_i \rightarrow B_j)$ is an *up-edge* [5].

Definition 25. An edge $(B_i \rightarrow B_j)$ is in the *edge dominance frontier (EDF)* of a node B_k if B_k dominates B_i and B_k does not strictly dominate B_j [5].

In the Cytron *et al.* definition of a dominance frontier given in Definition 15, the node B_j would be in the dominance frontier of B_k .

Definition 26. Let B_k be a node in a $CFG = G(V, E)$ such that an edge $(B_i \rightarrow B_j) \in EDF(B_k)$. Then, $B_j \in DF(B_k)$ [5].

Finally, we need to know which nodes are *boundary nodes*. Several ways of determining boundary nodes were discussed in [5]. For example, a simple problem formulation defined a node to be a boundary node if it is a leaf node in the dominator tree. It was also suggested that every node could be initialized as a boundary node. In practice, however, boundary nodes are defined by Definition 28.

Definition 27. A *zone* is a smaller tree created by partitioning the dominator tree. The zone associated with a tree node B_i is denoted Z_{B_i} . The *zone size* of Z_{B_i} is $z[B_i]$ [5].

Definition 28. A node B_i is a *boundary node* if:

1. B_i is a leaf node in the dominator tree; or
2. $(1 + \sum_{B_j \in children(B_i)} z[B_j]) > (\beta \times |EDF(B_i)| + 1)$,

where $\beta \geq 0$ is a parameter used to control the space and query-time tradeoffs [5].²

Definition 29. A node B_i in the dominator tree is an *interior node* if B_i is not a boundary node [5].

Definition 30. The zone size of a node B_i is computed by the following [5]:

$$z[B_i] = \begin{cases} 1 + \sum_{B_j \in children(B_i)} z[B_j], & \text{if } B_i \text{ is an interior node.} \\ 1, & \text{if } B_i \text{ is a boundary node.} \end{cases} \quad (4.3)$$

²For the remainder of this discussion, it can be assumed that $\beta = 1$. This β value produced the best results in the experiments of [5], and was encouraged for use by the authors.

Definition 31. The *augmented dominator tree (ADT)* consists of a number of structures [5]:

1. a dominator tree capable of producing top-down and bottom-up traversals.
2. the depth-first search number (equivalently, the level number, discussed in Section 4.1.2) for each node of the tree.
3. a boolean value for each node indicating whether or not it is a boundary node.
4. a list of CFG edges corresponding to a particular node B_i . The list is $EDF(B_i)$ if B_i is a boundary node. If B_i is an interior node, the list consists of the CFG up-edges sourced at B_i .

The *ADT* for the example in Figure 4.1 is given in Table 4.1.

Node	Level	Boundary Node?	List
B_1	0	T	6, 6, 6
B_2	1	T	6
B_3	1	F	
B_4	2	T	6
B_5	2	T	6
B_6	1	T	7
B_7	2	T	7
B_8	3	T	7, 11, 11
B_9	4	T	11
B_{10}	4	T	11
B_{11}	4	T	7
B_{12}	3	T	

Table 4.1: The *ADT* for Figure 4.1

The algorithm, based on the *ADT* data structure, takes as input a set of nodes and returns the set of *merge nodes* where ϕ -functions are to be placed.

Definition 32. Suppose B_0 is the start node of a $CFG = G(V, E)$. The *merge relation* (M) is a binary relation on nodes defined as a set of pairs, (B_i, B_j) such that $B_i \in V$ and $B_j \in J(\{B_0, B_j\})$. The *merge set* of B_i is the set of all nodes B_j such that $(B_j, B_i) \in M$ [5].

The relationship between merge nodes and ϕ -functions is given in Theorem 2.

Theorem 2. *The iterated dominance frontier is the same as the merge relation. That is [5],*

$$DF^+ = M \tag{4.4}$$

The input set of nodes are initialized as a priority queue, PQ , using the node levels as keys. The dominator tree is also required, and all nodes from the input set are marked in the tree. The main loop of the algorithm iterates while PQ is not empty, taking the next deepest node B_i from PQ for processing. Then each node from the list for B_i described in Definition 31, part 4, is studied. If the immediate dominator of the current list node is a strict ancestor of B_i , then it is a merge node, and is added to M . If the node was not marked in the dominator tree, it is marked and inserted in PQ for future processing. Finally, if B_i is not a boundary node, then we recursively visit all children of B_i that aren't marked.

Consider the example in Figure 4.1. Let the input set $S = A(x) = \{B_2, B_4, B_5, B_9, B_{10}\}$. Also, $PQ = S = \{B_2, B_4, B_5, B_9, B_{10}\}$. Using the level as the key to PQ means nodes B_9 and B_{10} are processed first. The list for node B_9 consists just of node B_{11} . From Figure 4.5(a), we know that the immediate dominator of node B_{11} is node B_8 , which is a strict ancestor of node B_9 . Thus, node B_{11} is a merge node and $M = M \cup \{B_{11}\}$. Node B_{11} is not in S , thus it is not marked in the dominator tree. It is then marked and $PQ = PQ \cup \{B_{11}\}$. The ADT in Table 4.1 shows that node B_9 is a boundary node, therefore this loop iteration is finished. We next process node B_{10} , whose only list element is node B_{11} , which is already in M . Then node B_{11} itself is examined, since its level is also 4. Node B_{11} 's list consists of node B_7 , whose immediate dominator is node B_6 , a strict ancestor of node B_{11} . Thus, $M = \{B_{11}, B_7\}$. Node B_7 is not in S , hence it is marked in the dominator tree and $PQ = PQ \cup \{B_7\}$. Node B_{11} is also a boundary node. Node B_4 , with the next highest level number, is then extracted from PQ . Node B_6 is the only node in node B_4 's list. Node B_6 's immediate dominator is node B_1 , a strict ancestor of all other nodes. Node B_6 is a merge node and $M = \{B_{11}, B_7, B_6\}$. Node B_6 is not in S , thus it is marked and added to PQ . And node B_4 is a boundary node. From Table 4.1, we can see that all the lists of the remaining nodes contain nodes that have already been added to M , therefore we are done. ϕ -functions for x can then be added to nodes B_6 , B_7 , and B_{11} . To obtain the required ϕ -functions for other variables, other input sets can be used; namely, $A(v)$ for all other v .

4.2 Variable Renaming

The renaming of variables that subsequently occurs during SSA construction is much less studied in the literature. Cytron *et al.* propose renaming variables using a top-down traversal of the dominator tree [19]. During this pass, arrays of stacks are accessed to find the next available variable for an assignment, or the previous definition that should now be referenced. The array is indexed by the original variable name, and the stacks contain the replacement subscripts. By visiting a specific node, statements associated with that node, beginning with any ϕ -functions, are processed in sequential order. Only variables referenced in the statement are handled.

Briggs *et al.* presented improvements to this algorithm in 1998 [7]. They proposed pushing a subscript on the stack only at the first definition of a variable x in the block. Then, subsequent definitions would overwrite the subscript, thus taking away the pure stack nature of the data structure. Information would have to be maintained as to which variables had subscripts pushed into a particular block. To restore the original state of the stack, the algorithm reads the already-pushed list, and pops subscripts from that list.

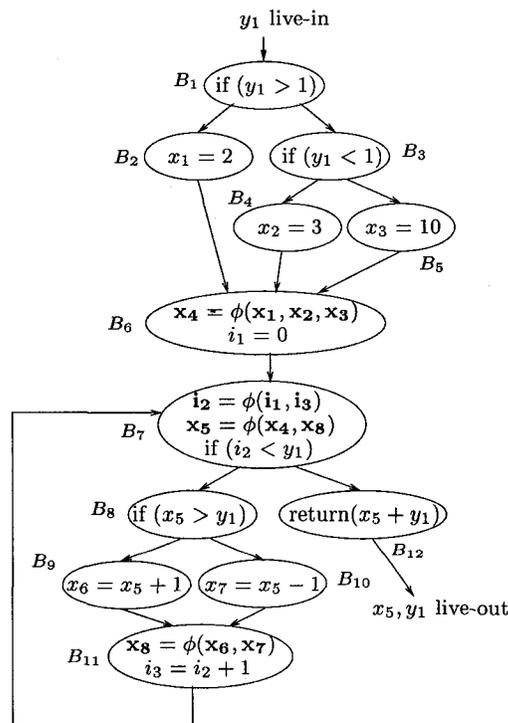


Figure 4.6: The SSA form of Figure 4.1

The SSA form of our running example is given in Figure 4.6. This product results from any of the techniques discussed in Sections 4.1 and 4.2. Added ϕ -instructions are shown.

4.3 Discussion

Cytron *et al.*'s algorithm from Section 4.1.1 is widely thought to be the easiest of the three presented algorithms to implement, although they each produce the same result. It is thus still found in many production compilers today. Since the algorithm is based on the dominance frontiers of individual nodes, the calculation of these structures is crucial in compile-time analysis. Consider a CFG with N nodes, E edges, A_{tot} number of assignments and M_{tot} number of references to variables. Let DF be the mapping from nodes to their dominance frontiers,³ and $avg(DF)$ be the weighted average of the sizes $|DF(B)|$. X is the set of all nodes in the CFG. Then the total running time of the algorithm is the time required to compute the dominance frontiers, along with the time to place ϕ -functions and the time to rename variables [19]. That is,

$$Time = O\left(\sum_{B \in X} |DF(N)|\right) + O(A_{tot} \times avg(DF)) + O(M_{tot}) \quad (4.5)$$

Now let T be the overall size of the original program, calculated by:

$$T = \max\{N, E, A_{orig}, M_{orig}\} \quad (4.6)$$

The worst-case running time is then [19]:

$$Time_{worst} = O(T^2) + O(T^3) \quad (4.7)$$

The authors argue that in practice, the calculation is actually linear.

Sreedhar and Gao's DJ-graph algorithm for placing ϕ -functions presented in Section 4.1.2 is in fact linear. Given a dominator tree, the DJ-graph can be constructed in $O(E)$ time, just the time required to insert the J-edges. It was shown that [32]:

Theorem 3. *The time complexity of Sreedhar and Gao's algorithm is $O(|E|)$.*

Now let V be the number of variables in the CFG. Sreedhar and Gao's method takes as an initial set the set of assignments to a particular variable. The algorithm

³Assume for all of these calculations that the dominator tree is available. It has been shown that the dominator tree computation is $O(E)$ [23, 22].

will have to be performed for each variable in the CFG to produce the complete set of iterated dominance frontiers. Therefore, the actual time to compute the SSA form of a program using this method is:

$$Time = O(E) + |V| \times O(|E|) + O(M_{tot}) \quad (4.8)$$

The final algorithm presented in Section 4.1.3 was that of Bilardi and Pingali, which places ϕ -functions based on another new data structure, the *ADT*. Let E_{up} be the set of up-edges in the CFG. It was shown that [5]:

Theorem 4. *The ADT for a given CFG can be constructed in time*

$$Time_{ADT} = O(|E_{up}| + (1 + 1/\beta) \times |N|) \quad (4.9)$$

Given that the version of the algorithm presented here uses $\beta = 1$, Equation 4.9 becomes:

$$Time_{ADT} = O(|E_{up}| + 2|N|) \quad (4.10)$$

Let F be the number of extractions from the *PQ* data structure and K be the number of keys used by the *PQ* implemented as a heap. Then the ϕ -function placement algorithm was shown to be [5]:

$$Time_{\phi\text{-function}} = O(|N| + |E_{up}| + |V|/c) + O(F + K), \quad c \text{ constant} \quad (4.11)$$

The final running time of Bilardi and Pingali's method is then:

$$Time = O(|E_{up}| + 2|N|) + O(|N| + |E_{up}| + |V|/c) + O(F + K) + O(M_{tot}), \quad c \text{ constant} \quad (4.12)$$

From the experience of producing the examples seen throughout Section 4.1, it was easy to rank the algorithms in practice. Sreedhar and Gao's method was the easiest to work through, since the DJ-graph made visualizing the process straightforward. Cytron *et al.*'s algorithm was easy to understand, since it is rooted in original theory without additional structures to learn. It simply requires the basic concepts that the other algorithms use only as a starting point. It is also the most familiar, as it appears in most compilers. However, the enhancement of a concrete data structure could be beneficial. Bilardi and Pingali's technique was very complicated. There were quite a few structures and values to keep track of, and this process was tedious. The idea was not intuitive.

Since the dominator tree is readily available, Cytron *et al.*'s algorithm is still probably the easiest to implement, as no new data structure is required. However, constructing a DJ-graph from the dominator tree should require little extra time. The main concern therefore with Sreedhar and Gao's method would be the additional space requirements for a structure only required for one purpose. Bilardi and Pingali's method also needs an additional structure for this single task, but the cost of building the elaborate *ADT* is not worth the supposed rewards.

4.4 Conversion out of SSA

After SSA translation, a code representation ensues that contains non-executable instructions. Further compilation phases, such as instruction scheduling and register allocation, require the removal of these ϕ -functions.

Trivially, the removal process can be achieved by inserting many copy instructions into the modified code, one for each definition of a variable. Consider Figure 4.7. In our example, five copies for x are inserted, one in each of nodes B_2, B_4, B_5, B_9 and B_{10} . These ensure that when the common uses of x occur in nodes B_8, B_9, B_{10} and B_{12} , the correct definition will be used. Then the ϕ -instructions in nodes B_6, B_7 and B_{11} are no longer necessary, and are removed. A similar process is used for i . The added instructions are indicated in bold print.

The number of copies will increase according to the original code size and complexity. Methods for minimum copy insertion are desired.

Sreedhar *et al.* have proposed three methods for translating out of the SSA form [33]. These methods use a variety of techniques, ranging from brute-force insertion of copies to using both dataflow and *interference graph* information.

Definition 33. Consider a $CFG = G(V, E)$ such that x and y are variables in G . An *interference graph* (I) can be used to indicate if x and y interfere. Let each variable in G represent a node in I . If x and y interfere, then there is an edge between the nodes representing x and y in I .

4.4.1 Naive Translation

Using this method, copies are inserted for all variables *referenced* in a ϕ -instruction.

Definition 34. Given a ϕ -instruction of the form $x = \phi(x_1, x_2, \dots, x_n)$, x and all the source operands x_1, \dots, x_n are said to be *referenced* in that instruction.

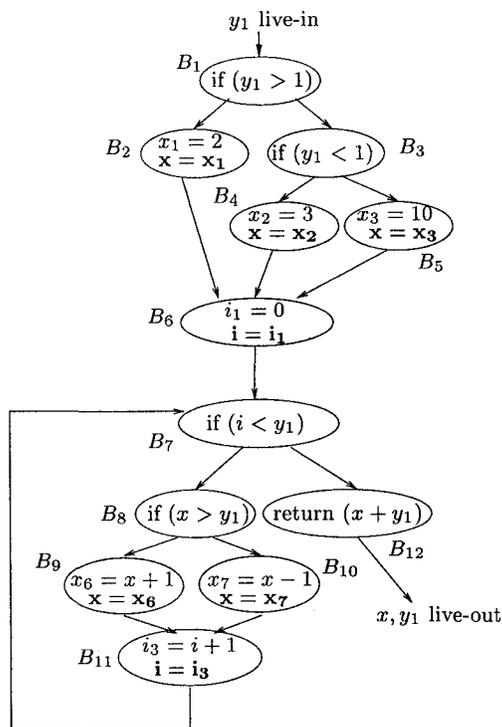


Figure 4.7: The result of naively inserting copies to remove the SSA form

Contrary to the preliminary example presented in Figure 4.7, this technique will also add copies for the target of the ϕ -instruction. The result of applying the Naive Translation Method to our running example can be seen in Figure 4.8. Added copies are indicated in bold print.

Let's investigate the ϕ -instructions for x in Figure 4.6. Since there are three instructions, three copies of the form $x_i = x$ will be required for each target operand x_i . Similarly, there are seven ϕ -function source operands x_j that require copies of the form $x = x_j$. These copies ensure that the correct value is accessed during uses of x . However, the ten copies for a single variable x seems excessive. Improvements are needed.

In production compilers, however, SSA will never be translated into and out of directly without its benefits being maximized. In this regard, we can assume that several optimizations will occur between the SSA form construction and SSA removal. Sreedhar *et al.*'s remaining translation methods are best seen in this altered context. For this discussion, we will focus on a slightly modified example, shown in Figure 4.9. Here, some instructions have been re-arranged, and some basic blocks removed, as can happen after compiler optimizations.

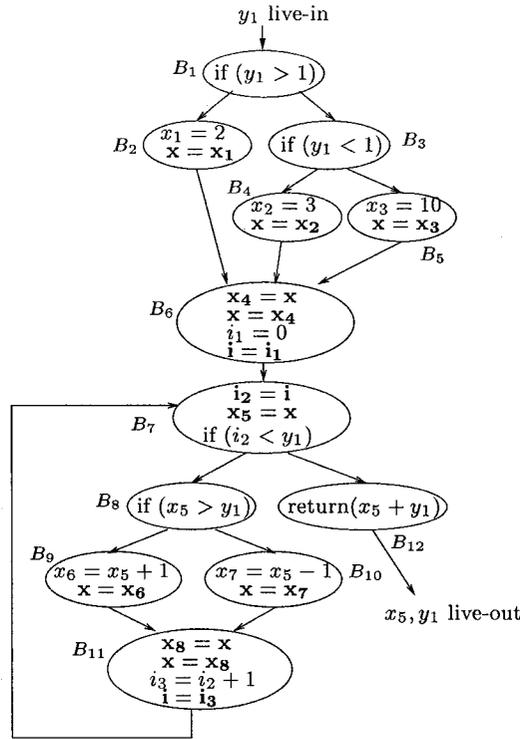


Figure 4.8: Translating out of SSA using Sreedhar *et al.*'s first method

4.4.2 Translation Based on Interference Graph Update

This translation method sees the insertion of copies only for variables whose live ranges interfere. Cytron and Gershbein present a special definition of liveness with respect to ϕ -instructions [20]. In particular, if a ϕ -function x_ϕ is in basic block B_j , then each use of a ϕ -function source operand x_i is associated with the end of the corresponding predecessor to B_j through which x_i reaches B_j . ϕ -functions are expected to occur at the beginning of the basic block in which they appear. Given these assumptions, the subsequent definition follows.

Definition 35. Consider a source operand x_i of a ϕ -instruction x_ϕ that occurs in basic block B_j . Let basic block B_i be the block through which x_i reaches x_ϕ . x_i is *live* along the path from the point right after its definition to the final point in B_i . The ϕ -instruction target x is *live* along the path from the point right after its definition to the point right before its last use.

Given Definition 35, target operands of a ϕ -function cannot be live at the same time as the source operands of that ϕ -function. We can thus eliminate all of the copies related to ϕ -function target operands from Figure 4.8. The result of removing

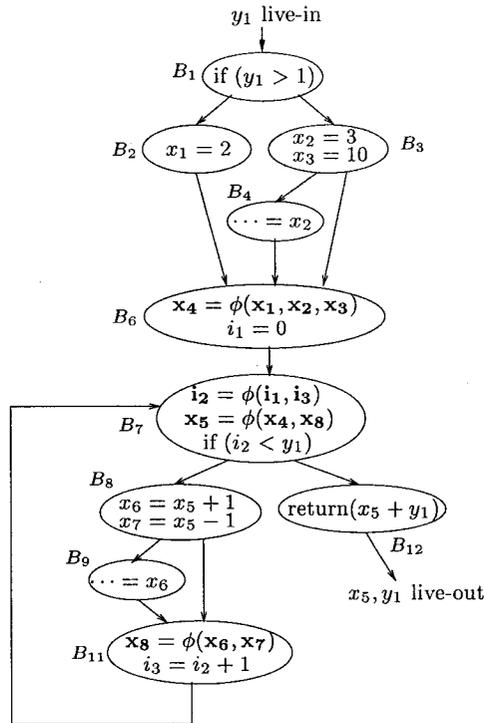


Figure 4.9: Modified example

the SSA form from Figure 4.9 is given in Figure 4.10.

Let's study the x ϕ -instructions from Figure 4.9. We must determine which referenced variables from ϕ -functions interfere. The three copies required for the three ϕ -function targets are automatically eliminated. Since only x_2 and x_3 of the operands for the ϕ -function defining x_4 interfere, the copy for x_1 is unnecessary. The main x variable is then propagated throughout the code, and we are left with four copies for x .

This result is a significant improvement for a small example. Of course, there is a cost for examining each variable's live range, but with such benefits, it is worth the additional checks. Section 4.4.3 analyzes the effects of further steps.

4.4.3 Translation Based on Data Flow and Interference Graph Updates

With this method, copies are inserted based on live ranges that interfere, and the live-in and live-out sets of the variables involved. Eliminating interferences between ϕ -instruction source operands can be done exclusively with live-out sets, while eliminating those between target and source operands requires the live-in sets as well. It is the most effective of Sreedhar *et al.*'s methods.

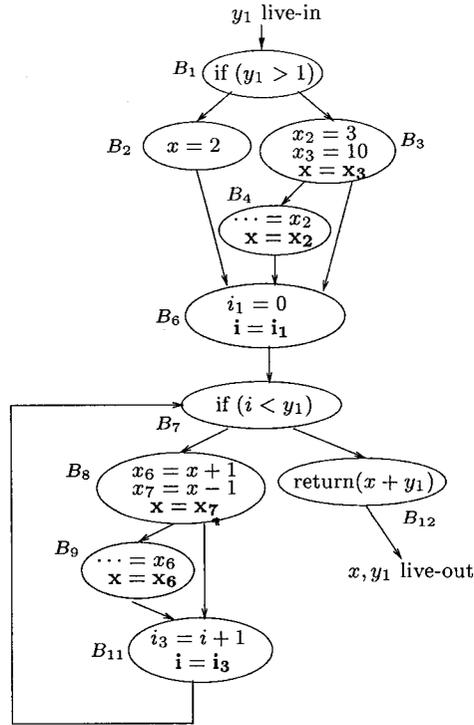


Figure 4.10: Translating out of SSA based on live range interference

Definition 36. Two variables x and y are in the same ϕ -congruence class (denoted by ϕ_{cc}) if they are referenced in the same ϕ -instruction, or there exists a resource z such that y and z are referenced in the same ϕ -instruction, and x and z are referenced in the same ϕ -instruction [33].

Intuitively, two variables are congruent if they are referenced in the same ϕ -instruction, or referenced transitively between ϕ -instructions. We want two congruent variables to be able to receive the same representative name. It can be compared to register allocation by colouring, where variables that do not interfere can be assigned to the same register [11]. Similarly, if two variables occur in the same ϕ -congruence class, we would like for them to get renamed to the same representative name upon removal of the SSA form.

A fundamental property for this translation is the ϕ -Congruence Property, a slight modification on which is presented here [33].

Property 1. (ϕ -Congruence Property) All occurrences of variables that belong to the same ϕ -congruence class in a program may be replaced by the same representative name. After all variables in the ϕ -instruction have been replaced, the ϕ -instruction can be eliminated without violating the original semantics of the pro-

gram, and thus the SSA form can be removed.

As Property 1 states, congruent variables may be renamed the same, but this renaming is not always possible. Interfering variables within a ϕ -congruence class should be handled by the insertion of copies. In fact, there are four cases to be studied with respect to the ϕ -congruence classes.⁴ A ϕ -congruence class is initialized so that a variable in a ϕ -instruction belongs to its own class; hence, $\phi_{cc}(x_i) = \{x_i\}$. Given a variable x_i , the basic block through which its definition reaches the ϕ -instruction is denoted B_{x_i} .

1. If $[\phi_{cc}(x_i) \cap L_{out}(B_{x_j}) \neq \emptyset] \wedge [\phi_{cc}(x_j) \cap L_{out}(B_{x_i}) = \emptyset]$, then the copy $x_i' = x_i$ is needed in B_{x_i} . This copy ensures x_i and x_j are added to different ϕ -congruence classes.
2. If $[\phi_{cc}(x_i) \cap L_{out}(B_{x_j}) = \emptyset] \wedge [\phi_{cc}(x_j) \cap L_{out}(B_{x_i}) \neq \emptyset]$, then the copy $x_j' = x_j$ is needed in B_{x_j} .
3. If $[\phi_{cc}(x_i) \cap L_{out}(B_{x_j}) \neq \emptyset] \wedge [\phi_{cc}(x_j) \cap L_{out}(B_{x_i}) \neq \emptyset]$, then two copies, $x_i' = x_i$ in B_{x_i} and $x_j' = x_j$ in B_{x_j} .
4. If $[\phi_{cc}(x_i) \cap L_{out}(B_{x_j}) = \emptyset] \wedge [\phi_{cc}(x_j) \cap L_{out}(B_{x_i}) = \emptyset]$, then one of the copies $x_i' = x_i$ in B_{x_i} or $x_j' = x_j$ in B_{x_j} is needed. The final decision is made at a later stage of the translation process.

When all required copies have been added, the variables denoted by x_i' can be replaced by a representative name.

Using these conditions, the translated code in Figure 4.11 is produced. Compared with Figure 4.10, we have eliminated two copies, the copy in node B_3 and the one in node B_8 . Consider the variables x_2 and x_3 from Figure 4.9, where $B_{x_2} = B_4$ and $B_{x_3} = B_3$. We know that $\phi_{cc}(x_2) = \{x_2\}$ and $\phi_{cc}(x_3) = \{x_3\}$. We can also determine that $L_{out}(B_{x_2}) = L_{out}(B_4) = \emptyset$ and $L_{out}(B_{x_3}) = L_{out}(B_3) = \{x_2\}$. Given the first case described previously, we check $\phi_{cc}(x_2)$ versus $L_{out}(B_{x_3})$. That is, $\phi_{cc}(x_2) \cap L_{out}(B_{x_3}) = \{x_2\} \cap \{x_2\} = \{x_2\} \neq \emptyset$. We also look at $\phi_{cc}(x_3)$ and $L_{out}(B_{x_2})$. Thus, $\phi_{cc}(x_3) \cap L_{out}(B_{x_2}) = \{x_3\} \cap \emptyset = \emptyset$. Hence, variables x_2 and x_3 satisfy the first case of the four to be checked, and only the copy $x_2' = x_2$ is needed in B_{x_2} . The copy in B_3 is therefore unnecessary, and not included. Upon renaming

⁴Budimlić *et al.* discussed a similar approach in [8], where variables are compared for interference by checking the liveness information for the blocks in which the respective variables are defined.

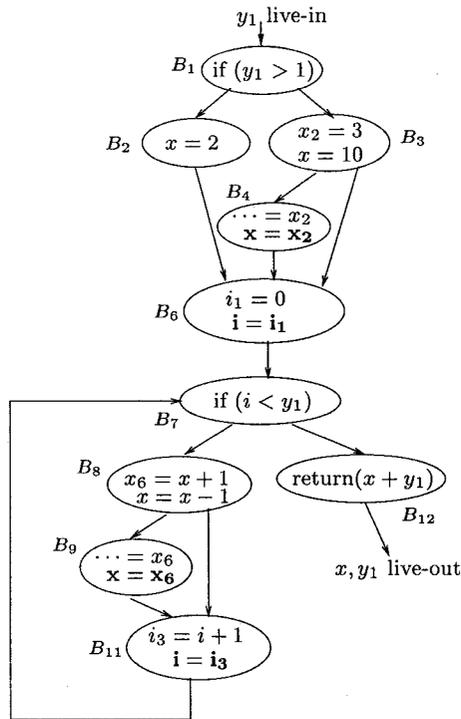


Figure 4.11: Translating out of SSA based on live range interference and dataflow information

by the representative name, the actual copy $x = x_2$ is added in node B_4 . A similar analysis can be performed for the variables x_6 and x_7 in nodes B_8 and B_9 to see that only the copy $x = x_6$ is required in B_9 , and the copy from B_8 in Figure 4.10 is unnecessary.

4.4.4 Comparison of Individual Translation Methods

As can be seen by the examples presented in Sections 4.4.1, 4.4.2 and 4.4.3, Sreedhar *et al.*'s three translation techniques produce a variety of results, even on small pieces of code. Even though the results are all correct, some are more desirable than others. In particular, producing fewer inserted copies will result in a smaller number of extra instructions to be executed, and an ultimate decrease in additional run-time. However, an overhead is incurred during the increased work performed by translation methods 2 and 3. In Chapter 8, the actual costs and benefits of methods 1 and 2 will be examined.

In terms of working with the individual translation methods, there are clear differences in usability. The naive method is straightforward, as copies are inserted exclusively for variables referenced in ϕ -instructions. Working with this method

simply entails iterating through the ϕ -instructions to see which variables are referenced.

A little more thought is required to examine the live ranges of variables as performed in the second translation method. Since the liveness information has already been computed at an earlier stage of the compilation process, the additional work needed is minimal. It is simply a matter of maintaining and updating the liveness information throughout the SSA construction and removal phase. The benefits seem obvious, since even in our small example more than half of the copies included using the first method could be eliminated by exploring liveness properties.

The third translation method, however, requires extra processing which at present is not needed by other compilation phases. The calculations necessary to implement ϕ -congruence classes may not be worth the additional effort. Besides analyzing the liveness information, the ϕ -congruence classes must also be compared to the live sets. It is not yet clear if the added compile-time restrictions will be alleviated by significant runtime benefits. However, as was seen by the small example of Section 4.4.3, the major gains were realized between methods 1 and 2, and much smaller improvements were achieved through method 3.

Chapter 5

SSA for Predicated Code

5.1 Predication

Traditional SSA only applies to code with branches by “choosing” the path that the program execution followed. However, the technique of *if-conversion*, introduced by Allen *et al.* in 1983 [2], eliminates conditional branches and changes the flow of a program [3]. It enables the compiler to treat control dependences as data dependences. If-converted code is sequential, but removing control flow is not allowed to change the semantics of the program. With conditional branches removed, decisions are made based on *predicates* [29, 27]. Each statement is assigned a logical expression, that if evaluated true results in the statement being executed. The predicates themselves are defined by statements inserted in the program. If a program statement has no explicit predicate, the predicate is assumed to be true, and the statement is always executed.¹

Recall the example from Chapter 4 in Figure 5.1(a). There are three occurrences of conditional branches associated with if-statements. By performing if-conversion, these branches will be eliminated. Figure 5.1(b) gives the if-converted form. Note that in Figure 5.1(b), we have explicitly stated that x is live-in. We are utilizing the assumption from Chapter 3 that every variable is defined in the start node of the CFG. The previous forms of our example defined x in every control flow path before its first use, and thus an initial definition was never needed for analysis. When we introduced predicates through if-conversion, and removed the control flow, the initial definition of x was necessary.

SSA as it has been defined does not deal with predicated code. The transforma-

¹For this discussion, the predicate p_0 will be the always true predicate, thus statements assigned to p_0 will always be executed.

<pre> <i>y</i> live-in if (<i>y</i> > 1) <i>x</i> = 2 else if (<i>y</i> < 1) <i>x</i> = 3 else <i>x</i> = 10 for (<i>i</i> = 0; <i>i</i> < <i>y</i>; <i>i</i> ++){ if (<i>x</i> > <i>y</i>) <i>x</i> ++ else <i>x</i> -- } return(<i>x</i> + <i>y</i>) <i>x, y</i> are live-out </pre>	<pre> <i>x, y</i> live-in (<i>p</i>₀) <i>p</i>₁, <i>p</i>₂ = (<i>y</i> > 1) (<i>p</i>₁) <i>x</i> = 2 (<i>p</i>₂) <i>p</i>₃, <i>p</i>₄ = (<i>y</i> < 1) (<i>p</i>₃) <i>x</i> = 3 (<i>p</i>₄) <i>x</i> = 10 (<i>p</i>₀) <i>i</i> = 0 label: (<i>p</i>₀) <i>p</i>₅, <i>p</i>₆ = (<i>i</i> < <i>y</i>) (<i>p</i>₅) <i>p</i>₇, <i>p</i>₈ = (<i>x</i> > <i>y</i>) (<i>p</i>₇) <i>x</i> ++ (<i>p</i>₈) <i>x</i> -- (<i>p</i>₅) <i>i</i> ++ (<i>p</i>₅) br: label (<i>p</i>₆) return(<i>x</i> + <i>y</i>) <i>x, y</i> are live-out </pre>
(a)	(b)

Figure 5.1: (a) Example from Figure 4.1; (b) If-converted example

tion has no way of “deciding” which statements are executed based on the predicate information. Consider Figure 5.1(b). There are three predicated assignments to x before x is used. After applying the SSA algorithm to this code, there is still no decision as to which value of x to use. Traditional SSA is not sufficient to deal with this situation, since many definitions of a variable can still reach a use in a single control-flow path [35].

It is not desirable for SSA to ignore if-converted code. If-conversion is a popular and useful optimization technique since branches can hinder most compiler analyses. Current production compilers translate out of SSA form well before if-conversion occurs to avoid the problem. However, it is a natural extension to want code in SSA as long as possible within intermediate representations, to maximize the benefits SSA can afford.

5.2 ψ -SSA

Stoutchinin and de Ferriere introduced an SSA algorithm for predicated code in 2001 [35]. They suggested that their technique could benefit Linear Assembly Optimizers

and just-in-time compilers,² as well as managing inlined predicated assembly code in higher level programs. These advantages are especially prevalent in architectures with support for predication, such as the target architecture for this work, the Intel Itanium processor [16].

The algorithm presented in [35], called ψ -SSA, is an extension of the traditional SSA representation. The technique inserts ψ -functions at predicate join points, similar to the ϕ -function insertion of SSA. The operands of the ψ -function represent the predicated definitions that reach a particular program point. Only the first operand can be associated with an unconditional assignment. The algorithm first inserts ψ -functions after conditional assignments to variables, and then performs the entire SSA procedure, including ϕ -function placement.

Figure 5.2 gives the code of Figure 5.1(a) in SSA form, including the transformation into ψ -SSA. Notice in Figure 5.2 that there are two fewer ϕ -functions than in the SSA code of Figure 4.6. Since ψ -SSA is applied after if-conversion, many of the ψ -functions are simply if-converted ϕ -functions. The construction given in Figure 5.2 is a preliminary form. On subsequent passes of the algorithm, ψ -function operands that are defined by another ψ -function will be inlined into the operand list. This transformation allows for predicated code reordering.

As with any SSA transformation, reverting the code back into an executable form is necessary. This translation is usually non-trivial since an assortment of optimizations may have been performed by this stage in the compiler. Similar to the naive method of translation out of the SSA form presented in Section 4.4.1, a predicated copy instruction could be inserted for every ψ -function operand. This translation technique could result in excess copies being inserted.

As part of the work in [35], a translation algorithm was presented to remove the ψ -SSA form. This method makes associations between related predicated assignments and creates a representative live range for the related assignments. The fundamental idea behind the algorithm is that of a ψ -congruence class.

Definition 37. Two variables x and y belong to the same ψ -congruence class (and are said to be congruent to each other) if they are referenced in the same ψ -function, or there exists a variable z such that x is congruent to z and z is congruent to y [35].

²Linear Assembly Optimizers take programs written in a linear assembly input language and translate it into the traditional assembly language used at assembly and linkage-time [35]. Just-in-time compilers convert Java bytecodes into executable instructions.

```

 $x_0, y_1$  live-in
(p0)  $p_1, p_2 = (y_1 > 1)$ 
(p1)  $x_1 = 2$ 
(p0)  $x_2 = \psi(x_0, x_1)$ 
(p2)  $p_3, p_4 = (y_1 < 1)$ 
(p3)  $x_3 = 3$ 
(p0)  $x_4 = \psi(x_2, x_3)$ 
(p4)  $x_5 = 10$ 
(p0)  $x_6 = \psi(x_4, x_5)$ 
(p0)  $i_1 = 0$ 
label:
(p0)  $i_2 = \phi(i_1, i_3)$ 
(p0)  $p_5, p_6 = (i_2 < y_1)$ 
(p0)  $x_7 = \phi(x_6, x_{11})$ 
(p5)  $p_7, p_8 = (x_7 > y_1)$ 
(p7)  $x_8 = x_7 + 1$ 
(p0)  $x_9 = \psi(x_7, x_8)$ 
(p8)  $x_{10} = x_9 - 1$ 
(p0)  $x_{11} = \psi(x_9, x_{10})$ 
(p5)  $i_3 = i_2 + 1$ 
(p5) br: label
(p6) return( $x_{11} + y_1$ )
 $x_{11}, y_1$  are live-out

```

Figure 5.2: ψ -converted form of Figure 5.1(b)

Definition 37 is closely related to Definition 36 presented in Section 4.4.3. We want to replace all variables in the same ψ -congruence class with a single representative name upon translation out of the ψ -SSA form. Let x_i be an element of a ψ -congruence class. x_i actually corresponds to the live subrange beginning at x_i 's predicated definition and ending with x_i 's last use not in a ψ -function. The renaming is then possible since each ψ -congruence class represents a single live range, the union of the non-overlapping subranges.

The *congruence class order*, \prec_c , is used to relate elements in a single ψ -congruence class, and help maintain the original program semantics.

Definition 38. Given two variables x and y , $x \prec_c y$ if [35]:

1. the definitions of x and y may be live at the same time; *and*
2. x precedes y in the operand list of some ψ -function, or there exists a variable z such that x precedes z in the operand list of some ψ -function, and y and z

are referenced in some ψ -function with $z \prec_c y$.

The ψ -SSA form must maintain a certain consistency, defined by the following conditions [35]:

1. Assignments to variables within each ψ -congruence class must occur in the congruence class order.
2. Live subranges corresponding to elements of each ψ -congruence class cannot interfere.

Often, transformations such as code motion may result in a non-consistent ψ -SSA form. In this situation, copy instructions must be inserted to restore the code's consistency. When the code is once again consistent, the renaming process can proceed. The result of translating the example of Figure 5.2 both out of ψ -SSA and SSA can be seen in Figure 5.3(a). Note that dead code has been removed at this stage as well. Figure 5.3(b) gives the final code product after eliminating redundant copies. The resultant code includes 4 extra instructions over the original if-converted form. This overhead can be justified by the additional optimization opportunities presented by the complete SSA form.

5.3 Predicated SSA

Carter *et al.* first introduced the notion of applying SSA to predicated code in 1999 [9, 10]. Their technique, Predicated SSA (PSSA), is designed for the *Trimaran System* (Version 1.0) [37] and uses *hyperblocks* [24].

Definition 39. A *hyperblock* is a set of predicated basic blocks with one entry point at the beginning of the region, but one or more exit points from locations throughout the region.

A hyperblock consists of basic blocks, which are included in the hyperblock through profiling. Information about execution frequency, basic block size and operation latencies is compiled. A hyperblock should maximize optimization and scheduling opportunities by combining basic blocks of different control flow paths. Ideal blocks to include within a hyperblock are small and infrequently executed, with few hazardous instructions [24].³ If branches in eligible basic blocks have both true

³Hazardous instructions include procedure calls and memory accesses that are not readily resolvable.

x, y live-in	x, y live-in
(p_0) $p_1, p_2 = (y_1 > 1)$	(p_0) $p_1, p_2 = (y_1 > 1)$
(p_1) $x = 2$	(p_1) $x = 2$
(p_2) $p_3, p_4 = (y_1 < 1)$	(p_2) $p_3, p_4 = (y_1 < 1)$
(p_3) $x = 3$	(p_3) $x = 3$
(p_4) $x = 10$	(p_4) $x = 10$
(p_0) $x_6 = x$	(p_0) $i_1 = 0$
(p_0) $x = x_6$	(p_0) $i = i_1$
(p_0) $i_1 = 0$	label:
(p_0) $i = i_1$	(p_0) $p_5, p_6 = (i < y_1)$
label:	(p_0) $x_7 = x$
(p_0) $p_5, p_6 = (i < y_1)$	(p_5) $p_7, p_8 = (x_7 > y_1)$
(p_0) $x_7 = x$	(p_7) $x = x_7 + 1$
(p_5) $p_7, p_8 = (x_7 > y_1)$	(p_0) $x_9 = x$
(p_7) $x = x_7 + 1$	(p_8) $x = x_9 - 1$
(p_0) $x_9 = x$	(p_5) $i_3 = i + 1$
(p_8) $x = x_9 - 1$	(p_5) $i = i_3$
(p_0) $x_{11} = x$	(p_5) br: label
(p_0) $x = x_{11}$	(p_6) return($x_7 + y_1$)
(p_5) $i_3 = i + 1$	x_7, y_1 are live-out
(p_5) $i = i_3$	
(p_5) br: label	
(p_6) return($x_7 + y_1$)	
x_7, y_1 are live-out	

(a)

(b)

Figure 5.3: (a) After removal of SSA and ψ -SSA from Figure 5.2;
(b) Final code product after redundant copy removal

and false targets within the hyperblock, the branches get if-converted. A property of the hyperblock is that it contains no cyclic dependences.

PSSA processes the hyperblock in top-down order, and takes two forms: Control PSSA, which is used on predicate-defining operations; and Normal PSSA, which applies to all other instructions. The algorithm introduces a new predicate OR operation, that defines predicates on blocks by taking the logical OR of multiple predicates. *Full-path predicates* are also used, along with path-sensitive analysis, to determine under which conditions an individual variable reached a join point [9].

Definition 40. A *full-path predicate* is a collection of predicates representing the unique path along which an operation is valid.

When processing the hyperblock, if an assignment is reached, Normal PSSA is

invoked. The variable being defined is renamed and operands take on their already renamed versions. If the assignment is in a join block and multiple versions are live, the operation is duplicated in every incoming path with appropriate variable versions. Full-path predicates are used on these copies.

Trimaran defines a `cmpp` operation to assign values to predicates, and PSSA uses the instruction. Control PSSA is used to handle `cmpp` operations, by replacing them with one or more `cmpp` instructions that define full-path predicates for each path leading in to the block. The new `cmpp` instructions are guarded by the full-path predicate coming in to the current block.

The final step of the PSSA algorithm comes after optimizations (such as predicated speculation and control height reduction [9]) have been performed, when extra code is removed and copies are inserted to restore the code's consistency.

5.4 Comparison of ψ -SSA and PSSA

Both ψ -SSA and PSSA are attempting to remove conditional control flow from a program to enable potential optimization opportunities that were previously unseen. However, the methods employed to achieve this goal are quite different. For example, the architects of PSSA do not implement ϕ -functions, claiming additional dependences would be added, thus making the hyperblock schedule longer. This exclusion results in instances of incomplete SSA code, leaving some SSA optimizations to falter. The main goal of PSSA is scheduling instructions at the earliest cycle, hence the loss of SSA potential is minor. Since ψ -SSA builds on the established SSA algorithm, maximum benefits can be achieved from both SSA and its predicated version.

The fundamental difference between PSSA and ψ -SSA is its usability. Since PSSA was implemented as part of the *Trimaran System*, which is a simulation system, adding the new predicate OR instruction was trivial. On a real architecture, such as the target IA-64, adding new instructions is not straightforward. A work-around is suggested in [9], which involves transferring the predicate register file into a general register with the `move from predicate` instruction provided in IA-64 [14]. But with no new instructions required by ψ -SSA, it is an easier method to implement.

Chapter 6

Open Research Compiler

6.1 Existing Functionality

The Open Research Compiler (ORC) [31] is an open source compiler project intended for leading research in compiler design and optimization. Based on the MIPSPro compiler, the project is headed by Intel [15] and the Chinese Academy of Sciences [26], and is geared towards Intel's Itanium architecture [16]. The compiler gives researchers and students an opportunity to test their ideas in a competitive environment.

The ORC currently implements SSA before the code generator, which is the case with all modern production compilers. The SSA form is removed before the backend begins to generate code. The code transformation is performed using Cytron *et al.*'s algorithm, presented in Section 4.1.1. Figure 6.1 shows the flow of control in the current ORC version.¹

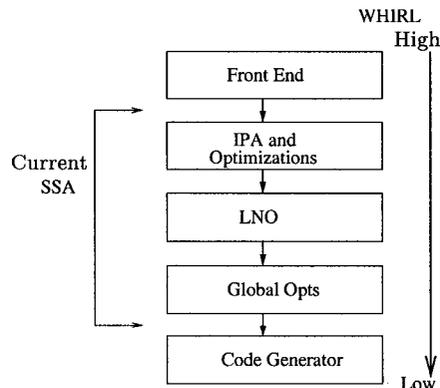


Figure 6.1: Flow of control in ORC

As Figure 6.1 indicates, the SSA transformation is performed immediately fol-

¹The work in this thesis was performed on ORC version 2.0.

Following the front end. Interprocedural analysis (IPA), interprocedural optimizations, loop nest optimizations (LNO), and global optimizations all occur within the SSA form. The intermediate transformation used by the ORC is WHIRL [36],² and the SSA has been removed by the lowest phase of WHIRL. To this point, no attempt has been made to incorporate SSA in the code generator. The existing code generator is shown in Figure 6.2.

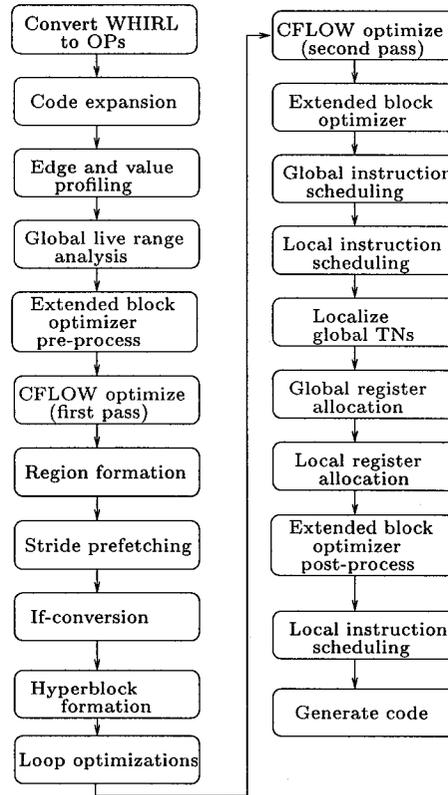


Figure 6.2: ORC's code generator

The phases of the code generator are briefly described here.

Convert WHIRL to OPs The intermediate representation used up to this point, WHIRL, is removed in favour of actual operations.

Code expansion Among the tasks performed during this phase, BBs are split into smaller units and tail calls are optimized.³

Edge and value profiling This analysis is performed for profile-directed compilation, where information is gathered at runtime to aid further compilation

²WHIRL stands for Winning Hierarchical Intermediate Representation Language.

³A tail call is a recursive call that exists at the end of the recursive function, *i.e.*, there are no further instructions past the recursive call.

decisions. Edge profiling is the traditional method used to determine frequently executed paths in the CFG, while value profiling is used on individual variables to assist in value optimizations such as constant propagation.

Global live range analysis This pass actually occurs at several points following the current stage, to update the live ranges that may have been altered by individual transformations. Live ranges are determined at a global level, for use in many phases.

Extended block optimizer pre-process Used in the extended block optimization phase, blocks are analyzed here and transformed into an extended block sequence of instructions, beyond the existing basic block.

CFLOW optimize (first pass) Control flow based optimizations are performed, including unreachable code removal and branch optimization.

Region formation Within this step, a region is built on which to perform the subsequent stages. It is desirable to have the largest area possible to optimize, without creating an unmanageable chunk of code.

Stride prefetching This phase introduces a method for choosing candidates for software prefetching using information about strides between loop iterations.

If-conversion This stage removes conditional branches via predication, as discussed in Section 5.1.

Hyperblock formation During this pass, larger chunks of predicated basic blocks are fused for analysis, as in Definition 39.

Loop optimizations The traditional loop optimizations such as loop unrolling and backedge coalescing are performed at this point.

CFLOW optimize (second pass) The same as the first pass, this phase iterates over the newly transformed code.

Extended block optimizer Peephole type optimizations are performed here, including constant propagation, redundant and dead expression elimination.

Global instruction scheduling Instructions are scheduled on a global level during this phase. The resultant schedule imposes global restrictions on the code.

Local instruction scheduling This pass schedules instructions locally, within the limitations of the schedule decided on by global scheduling.

Localize global TNs Global TNs that are able to become local variables are transformed at this stage. Local TNs are easier to handle during register allocation.⁴

Global register allocation This phase allocates registers on a global scale. Again, global dependences are introduced under which further allocations must conform.

Local register allocation Here, registers are allocated at the local level.

Extended block optimizer post-process Extended block optimizations are again performed after register allocation is complete.

Local instruction scheduling Further scheduling occurs during this phase, to allow the best schedule possible after all transformations have finished, for the actual generation of code.

Generate code Assembly language code is emitted for the target architecture.

6.2 Modified Code Generator

The work of this thesis has introduced SSA in the code generator of the ORC. Based on code originally written by Arthur Stoutchinin [34], the code was re-targeted for the Itanium processor by Stoutchinin, with later assistance from the author of this thesis. The implementation of ψ -SSA in the ORC was written by Stoutchinin and has not yet been published. Stoutchinin kindly shared his source code with me so that I could conduct the initial experimental evaluation described in Chapter 8. The SSA form is built after the global live range analysis phase, using Cytron *et al.*'s method from Section 4.1.1. There are six locations where the SSA can be removed, described in Table 6.1. Currently, methods 1 (Section 4.4.1) and 2 (Section 4.4.2) of Sreedhar *et al.* have been implemented. The choice of removal location can be made with a compile-time flag. The modified code generator's phases can be seen in Figure 6.3.

⁴A TN is a temporary name representing a variable instance in a program.

Translation level	Where the SSA removal is performed
1	after extended block optimizer preprocessing
2	after first pass of control flow optimization
3	after if-conversion
4	after second pass of control flow optimization
5	after extended block optimization
6	after global scheduling

Table 6.1: Description of SSA translation levels

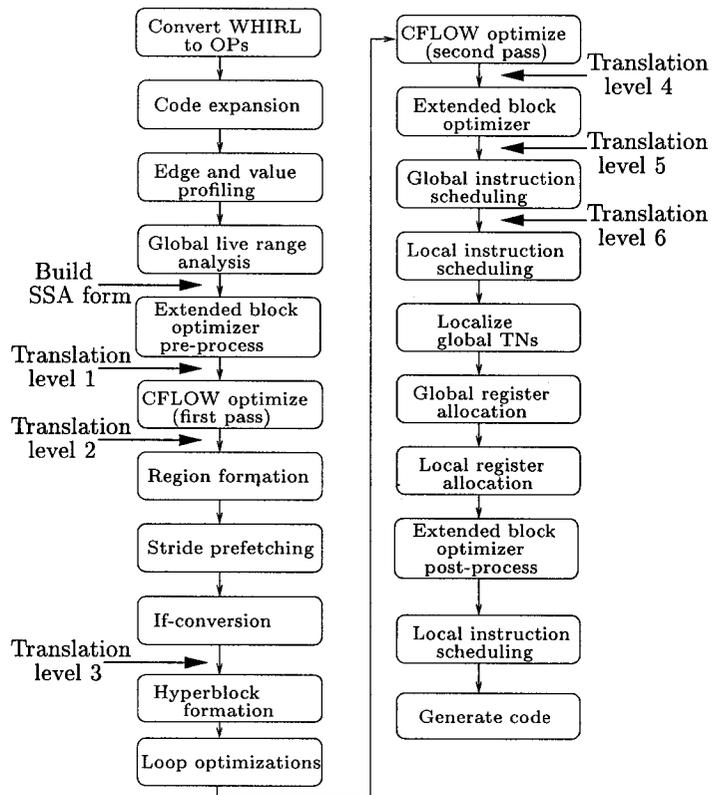


Figure 6.3: Modified ORC code generator

Consider again Figure 4.1, from Chapter 4. The sample code is presented here at various phases of the code generator using the modified compilation process at optimization level 2. Figures 6.4 and 6.5 graphically represent the CFG of the example code just before and immediately following SSA construction. Note that variables of the form t_i are intermediate values that the compiler introduces, and GTNs (global temporary names) are intermediate values relating to procedure preparation. In Figure 6.4, and for further figures, one can see an introduction of predicates well before the if-conversion phase of the compiler has occurred. Limited predication is used in earlier stages to handle some basic control flow issues.

Figure 6.6 pictures the CFG of the sample code after the SSA form has been removed following the extended block optimizer preprocessing phase. Figure 6.7 gives the sample code's representation after SSA removal subsequent to the first control flow optimization pass. Notice that the main difference between Figures 6.6 and 6.7 is the removal of node B_7 from Figure 6.7 and the inclusion of B_7 's code in node B_6 .

Figure 6.8 indicates the form of the sample code following SSA removal after if-conversion. It is obvious that the code has taken on a very different form, with the union of many smaller nodes into several larger nodes. This process was facilitated by removing most of the control flow issues via if-conversion.

It turns out that, for this small example, the code representations after levels 4 and 5 of SSA removal do not change the CFG of level 3. Thus, Figure 6.8 is sufficient to show all three translation levels.

Figure 6.9 shows the code form following SSA removal after global scheduling has passed. This code is quite different from the code of earlier stages. Based on Intel's Itanium architecture, code scheduling is performed using code blocks of three, called *bundles*. If the scheduler cannot decide on three appropriate instructions to place within a bundle, *nop*'s are inserted. These operations that perform no task are undesirable, but often necessary, depending on the code's form at the time of scheduling.

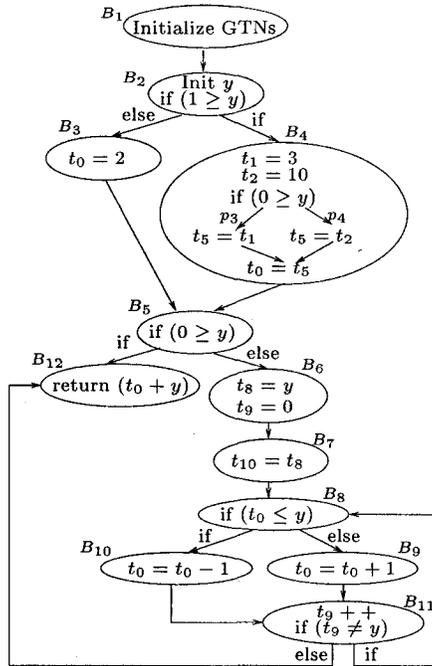


Figure 6.4: CFG for sample code before SSA construction

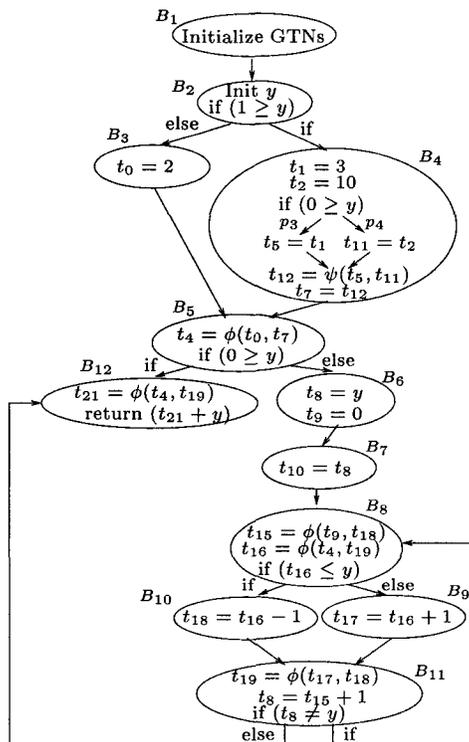


Figure 6.5: CFG for sample code after SSA construction

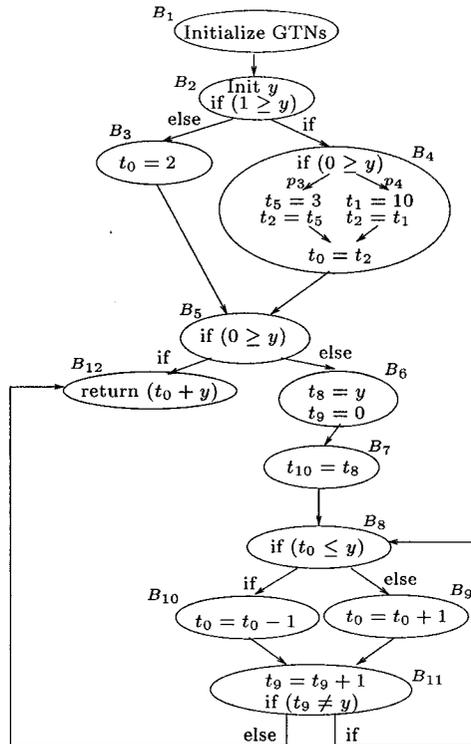


Figure 6.6: CFG for sample code after level 1 SSA removal

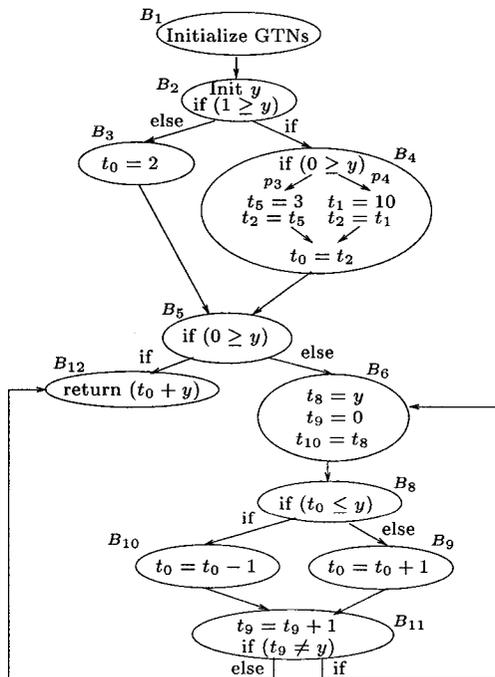


Figure 6.7: CFG for sample code after level 2 SSA removal

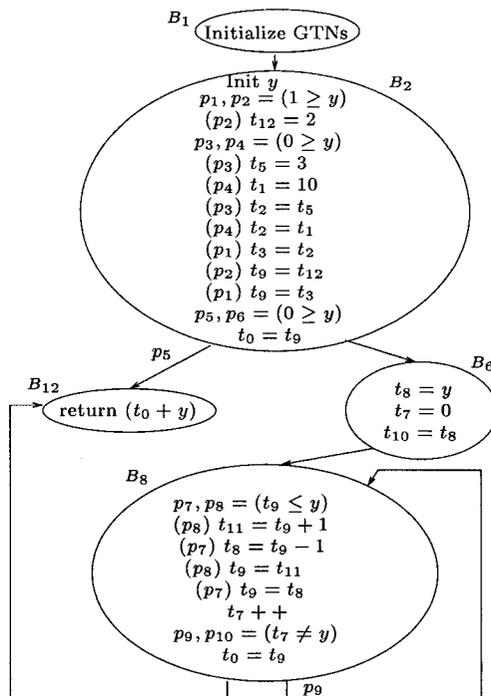


Figure 6.8: CFG for sample code after levels 3, 4 and 5 SSA removal

$B_1:$		$B_6:$	
(p_0)	Initialize GTNs	(p_0)	$t_7 = 0$
(p_0)	br: B_2	(p_0)	$t_8 = y$
$B_2:$		(p_0)	<i>nop</i>
(p_0)	Init y	(p_0)	$t_{10} = t_8$
(p_0)	$p_1, p_2 = (1 \geq y)$	(p_0)	<i>nop</i>
(p_0)	<i>nop</i>	(p_0)	<i>nop</i>
(p_0)	$p_3, p_4 = (0 \geq y)$	$B_8:$	
(p_2)	$t_{12} = 2$	(p_0)	$p_7, p_8 = (t_9 \leq y)$
(p_0)	<i>nop</i>	(p_0)	$t_7 ++$
(p_0)	$p_5, p_6 = (0 \geq y)$	(p_0)	<i>nop</i>
(p_4)	$t_1 = 10$	(p_7)	$t_{14} = t_9 - 1$
(p_2)	$t_9 = t_{12}$	(p_8)	$t_{13} = t_9 + 1$
(p_3)	$t_5 = 3$	(p_0)	$p_9, p_{10} = (t_7 \neq y)$
(p_4)	$t_2 = t_1$	(p_0)	<i>nop</i>
(p_0)	<i>nop</i>	(p_7)	$t_8 = t_{14}$
(p_3)	$t_2 = t_5$	(p_8)	$t_{11} = t_{13}$
(p_0)	<i>nop</i>	(p_7)	$t_9 = t_8$
(p_0)	<i>nop</i>	(p_8)	$t_9 = t_{11}$
(p_1)	$t_3 = t_2$	(p_0)	<i>nop</i>
(p_1)	$t_9 = t_3$	(p_0)	$t_0 = t_9$
(p_0)	<i>nop</i>	(p_0)	<i>nop</i>
(p_0)	$t_0 = t_9$	(p_9)	br: B_8
(p_0)	<i>nop</i>	(p_0)	br: B_{12}
(p_5)	br: B_{13}	$B_{13}:$	
		(p_0)	br: B_{12}
		$B_{12}:$	
		(p_0)	return($t_0 + y$)

Figure 6.9: Sample code after level 6 SSA removal

Chapter 7

Eliminating Redundant Join Set Computations in SSA

In this chapter, Cytron *et al.*'s ϕ -placement algorithm from Section 4.1.1 is revisited. The computation of join sets is at the center of that SSA construction technique. Two factors make the join set computation an interesting component for analysis. First, Cytron *et al.*'s algorithm is still the most prevalent in today's production compilers. Additionally, the bulk of the work performed by this method involves the join set. These considerations make the join set computation appealing as a point for optimization.

Theorem 7 presents the fundamental principle of this discussion. However, some preliminary results are necessary.

Theorem 5. *Let X be a subset of nodes in a $CFG = G(V, E)$ such that $X = X_1 \cup X_2$ and $X_1 \cap X_2 = \emptyset$. Then,*

$$DF(X_1) \cup DF(X_2) = DF(X_1 \cup X_2) \quad (7.1)$$

Proof. Let X be a subset of nodes in a $CFG = G(V, E)$ such that $X = X_1 \cup X_2$ and $X_1 \cap X_2 = \emptyset$. By Equation 3.1, we know that:

$$DF(X) = \bigcup_{B_i \in X} DF(B_i)$$

Thus,

$$\begin{aligned} DF(X_1) \cup DF(X_2) &= \bigcup_{B_i \in X_1} DF(B_i) \cup \bigcup_{B_i \in X_2} DF(B_i) = \bigcup_{B_i \in (X_1 \cup X_2)} DF(B_i) \\ &= DF(X_1 \cup X_2) \end{aligned}$$

□

Theorem 6. Let X be a subset of nodes in a $CFG = G(V, E)$ such that $X = X_1 \cup X_2$ and $X_1 \cap X_2 = \emptyset$. Then,

$$DF_i(X_1) \cup DF_i(X_2) = DF_i(X_1 \cup X_2) \quad (7.2)$$

such that DF_i is an element of the sequence that defines DF^+ .

Proof. Let X be a subset of nodes in a $CFG = G(V, E)$ such that $X = X_1 \cup X_2$ and $X_1 \cap X_2 = \emptyset$. The proof is by induction.

Base case: If $i = 1$, from Definition 19 we know that $DF_1 = DF(X)$. Hence:

$$DF_1(X_1) \cup DF_1(X_2) = DF(X_1) \cup DF(X_2)$$

From Theorem 5, we have:

$$DF(X_1) \cup DF(X_2) = DF(X_1 \cup X_2)$$

Thus,

$$DF_1(X_1) \cup DF_1(X_2) = DF(X_1 \cup X_2) = DF_1(X_1 \cup X_2)$$

Inductive case: Assume that $DF_i(X_1) \cup DF_i(X_2) = DF_i(X_1 \cup X_2)$ for $i = k$. Let $i = k + 1$. From Definition 19 we know that $DF_{i+1}(X) = DF(X \cup DF_i(X))$. Then,

$$\begin{aligned} DF_{k+1}(X_1) \cup DF_{k+1}(X_2) &= DF(X_1 \cup DF_k(X_1)) \cup DF(X_2 \cup DF_k(X_2)) \\ &= DF(X_1) \cup DF(DF_k(X_1)) \cup DF(X_2) \cup DF(DF_k(X_2)) \\ &= DF(X_1 \cup X_2) \cup DF(DF_k(X_1 \cup X_2)) \\ &= DF(X_1 \cup X_2 \cup DF_k(X_1 \cup X_2)) \\ &= DF_{k+1}(X_1 \cup X_2) \end{aligned}$$

□

Theorem 7. Let X be a subset of nodes in a $CFG = G(V, E)$ such that $X = X_1 \cup X_2$ and $X_1 \cap X_2 = \emptyset$. Then,

$$J^+(X) = J^+(X_1) \cup J^+(X_2) \quad (7.3)$$

Proof. Let X be a subset of nodes in a $CFG = G(V, E)$ such that $X = X_1 \cup X_2$ and $X_1 \cap X_2 = \emptyset$. Since G is a finite graph, $DF^+(X)$ must be finite. We know from Definition 19 that $DF^+(X)$ is the limit of a sequence of elements $DF_i(X)$. Equivalently,

$$DF^+(X) = \lim_{i \rightarrow \infty} DF_i(X)$$

where c is a constant. Recall from Theorem 1 that $DF^+(X) = J^+(X)$. Now

$$\begin{aligned}
J^+(X_1) \cup J^+(X_2) &= DF^+(X_1) \cup DF^+(X_2) \\
&= \lim_{i \rightarrow c} DF_i(X_1) \cup \lim_{i \rightarrow c} DF_i(X_2) \\
&= \lim_{i \rightarrow c} [DF_i(X_1) \cup DF_i(X_2)] \\
&= \lim_{i \rightarrow c} DF_i(X_1 \cup X_2) \\
&= \lim_{i \rightarrow c} DF_i(X) \\
&= DF^+(X) \\
&= J^+(X)
\end{aligned}$$

□

Consider two variables, x and y , in a program. If $A(x) = A(y)$, then $J^+(A(x)) = J^+(A(y))$. Similarly, if $A(y) \subset A(x)$, then $J^+(A(y)) \subset J^+(A(x))$. Recall that $J^+(A(x)) = S_\phi(x)$, the minimum set of nodes where ϕ -functions are required when constructing the SSA form of a program. Thus, if it can be shown that two variables have the same set of assignment nodes, then only one join set computation needs to be performed. Conversely, if one set of assignment nodes is a subset of another, two join set computations are still required. The intersection of the two sets (*i.e.*, the smaller set) will be calculated. However, the second computation (*i.e.*, the remainder of the larger set) will be smaller than the original.

The majority of the time in Cytron *et al.*'s worklist algorithm is spent iterating over the worklist W , and every variable has a worklist associated with it. In particular, the worklist has to be initialized for every variable v to $A(v)$. Then, each element $B_i \in W$ is removed from W , and a ϕ -function is inserted in every $B_j \in DF(B_i)$. As well, each B_j that now contains a ϕ -function is also inserted in W , and the process continues.

An initial analysis of individual SPEC CINT2000 benchmarks [17] indicates the opportunities for join set optimization. Table 7.1 gives a comparison between the number of times $A(y) \subseteq A(x)$ for two variables x and y and the number of worklists processed in the original implementation of the code generator's SSA construction. The percentage of work saved is the maximum number of entire worklists whose computation can be avoided by the elimination of redundant join set computations. All the calculations in this chapter were performed at SSA translation level 1 (refer

to Table 6.1) and optimization level O2 for baseline results, using Sreedhar *et al.*'s translation method \mathcal{Z} and the individual benchmarks' *test* data set.

Benchmark	Opportunities for optimization	Total number of worklists processed	Percentage of work saved
164.zip	220	2787	7.89
181.mcf	51	246	20.73
197.parser	698	17567	3.97
254.gap	3555	115686	3.07
255.vortex	1294	37372	3.46
256.bzip2	348	12089	2.88
Average	1028	30958	3.32

Table 7.1: Opportunities for eliminating redundant join set computations in SPEC CINT2000 benchmarks

Let x and y be two variables such that $A(x) = A(y)$. If this condition is detected, the worklist algorithm only needs to iterate for one of the two variables, $W = A(x) = A(y)$. The major change comes upon insertion of a ϕ -function for the variable being processed, since now there are two variables. Hence, for every $B_i \in W$ and $B_j \in DF(B_i)$, two ϕ -functions are added in B_j , one each for x and y . Performing the ϕ -function insertion in this manner eliminates an entire worklist iteration, and thus an entire join set computation, along with cutting down on accesses to the dominance frontier data structure. In practice, ϕ -functions are placed via a function call in the modified ORC SSA implementation in the code generator. Therefore, further savings can be achieved by removing a function call.

Table 7.2 shows the original opportunities presented in Table 7.1 where $A(x) = A(y)$, which is the best case scenario. In fact, more than half of the optimization possibilities explored can eliminate an entire worklist. The actual percentage of worklists avoided can be seen in Table 7.2.

Now let x and y be two variables such that $A(y) \subset A(x)$. One approach for handling this case is to split $A(x)$ into two smaller sets, $A(x_1) = A(y)$ and $A(x_2) = A(x) - A(y)$. This set division is possible since Theorem 7 determined that $J^+(A(x)) = J^+(A(x_1)) \cup J^+(A(x_2))$. Processing for $A(x_1)$ can be performed as normal. Consider here $A(x_2)$. The list of nodes that require a ϕ -function because of $A(x_2)$ will have to be computed separately as a worklist for x . Thus, savings still exists, since $A(x_1)$ and $A(y)$ are combined, and the worklist for $A(x_2)$ requires fewer iterations since $A(x_2) < A(x)$.

Benchmark	Opportunities for optimization	Total number of worklists processed	Percentage of worklists avoided
164.gzip	89	2787	3.19
181.mcf	22	246	8.94
197.parser	526	17567	2.99
254.gap	1928	115686	1.67
255.vortex	751	37372	2.01
256.bzip2	177	12089	1.46
Average	582.2	30958	1.88

Table 7.2: Instances where two join sets are equivalent in SPEC CINT2000 benchmarks

Consider the example in Figure 7.1. $A(x) = \{B_1, B_2, B_3, B_4, B_5\}$ and $A(y) = \{B_1, B_2, B_5\}$. Clearly, $A(y) \subset A(x)$. Now $A(x_1) = A(y) = \{B_1, B_2, B_5\}$ and $A(x_2) = A(x) - A(y) = \{B_3, B_4\}$. During the worklist algorithm, when $A(x)$ and $A(y)$ are compared, we can see that processing $A(y)$ will make up for most of the calculations also required by $A(x)$. Hence, when ϕ -functions are placed for y as part of the iteration for $A(y)$, we will know to also place ϕ -functions for x . Remaining now is $A(x_2)$, the elements left over from the larger set $A(x)$. The worklist will have to iterate for $A(x_2)$, however this remaining set is smaller than the original $A(x)$. We will thus perform fewer computations.

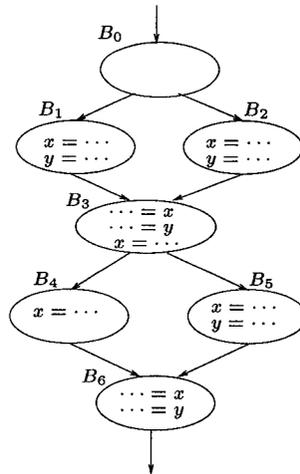


Figure 7.1: Example of sets of assignments for two variables, x and y

Table 7.3 gives the number of instances from Table 7.1 that were actually $A(y) \subset A(x)$. This case is less attractive than the $A(x) = A(y)$ situation since it requires more work. However, if it can be shown that, generally, $A(x_2)$ is much smaller than $A(x)$, then the benefits could be significant. As can be seen by Table 7.3, we are

on average saving 45% of the calculations by combining the portion of the two sets that intersect. This means that $A(x) - A(y)$ is generally 45% smaller than $A(x)$.

Benchmark	Opportunities for optimization	Average difference in size of subsets	Average percentage saved
164.gzip	131	6.79	38.38
181.mcf	29	3.45	42.99
197.parser	172	2.65	52.10
254.gap	1627	4.34	45.35
255.vortex	543	5.00	53.14
256.bzip2	171	5.65	41.33
Average	445.5	5.58	45.55

Table 7.3: Instances where one join set is a subset of another join set in SPEC CINT2000 benchmarks

Checking the relationships between these sets requires some extra calculation, but much of the work is facilitated through existing data structures in the SSA code. The one-time expense incurred to build correspondences between individual sets should be worth the benefits achieved through minimizing join set computations.

This chapter evaluated opportunities for eliminating redundant join set computations in Cytron *et al.*'s ϕ -placement algorithm. We feel that there is enough evidence to warrant implementing the join set optimization in the ORC, however time constraints leave this implementation outside of the scope of this thesis. Since the proof of concept tests were performed on a selection of the SPEC CINT2000 benchmark suite, this small optimization could be beneficial in other compilers that utilize Cytron *et al.*'s technique.

Chapter 8

Experimental Results

The SSA framework presented in Section 6.2 allows for optimizations in the code generator to take advantage of the benefits provided by the SSA form. However, if the gains allowed by SSA are outweighed by the cost of constructing and removing the SSA form, it may not be desirable to have SSA in the code generator. Since the work of this thesis does not introduce any further optimizations throughout the later phase SSA, the real assets of having SSA in the code generator are not realized. Therefore, if the SSA construction presented here is too expensive, future code transformations within SSA may be avoided. We will show that building the SSA form does not seriously degrade performance, thus making it a viable infrastructure upon which to introduce additional code transformations

This chapter presents the preliminary experimental results that were obtained from Arthur Stoutchinin's porting of the computation of ψ -SSA to the ORC. The numbers presented in this chapter are a snapshot of an ongoing software development process. These numbers in no way represent the final expected effect of ψ -SSA on the code generation. Several improvements to this implementation are currently underway and are expected to change these numbers, perhaps in significant ways. The experiments were run on an Itanium machine (HP Itanium2-2048 processor, 1GB memory). The ORC2.0 cross compiler used code compiled on an IA-32 machine (PentiumIII, 700MHz-128). Using the cross environment, four of the SPEC CINT2000 benchmarks did not behave as expected using the baseline compiler.¹ The baseline simply has the changes to the code generator turned off, and is thus equivalent to the original ORC. These discrepancies account for the omission of the problematic benchmarks from the results presented here.

¹175.*vpr* produced unexpected output; 186.*crafty* had trouble involving the linker; 252.*eon* could not find files that it needed to include; and the source code for 253.*perlbmk* contained a syntax error.

For these experiments, ϕ -functions were inserted using the insertion algorithm of Section 4.1.1. There are two SSA removal techniques (Sreedhar *et al.*'s methods 1 of Section 4.4.1 and method 2 of Section 4.4.2) that we could use for testing. Our experiments focus on method 2, which as discussed in this thesis is the superior algorithm. We present some comparisons with method 1 to justify this decision.

The results are broken down into 3 categories: compile-time and run-time results; number of inserted instructions during SSA construction and removal; and number of actual instructions executed. All results were accumulated at optimization level O2 and used the individual benchmarks' *test* data set.

8.1 Timing Results

First of all, we would like to ensure that constructing the SSA form in the code generator does not unreasonably increase compile-time or degrade run-time performance. All timing results are presented in seconds, and are an average over 5 runs. The experiments were compiled while in single-user mode on the IA32 machine, and run while in single-user mode on the Itanium machine. The execution times were calculated using the UNIX *time* command.

The numbers listed in Table 8.1 compare SSA translation level 1 (refer to Table 6.1) and the baseline results.² On average, to compile a benchmark with later phase SSA included is 2.91% slower than without SSA. This difference is minor for the amount of extra work included. The execution time does not on average change with SSA included. Therefore, performance results have not been negatively affected by later phase SSA.

Benchmark	Compile-time (baseline)	Compile-time (SSA)	Run-time (baseline)	Run-time (SSA)
164.gzip	22.29	22.24	1.69	1.71
181.mcf	11.15	11.32	0.27	0.29
197.parser	53.50	54.91	3.89	3.83
254.gap	236.38	244.57	1.57	1.62
255.vortex	144.74	148.69	5.69	5.70
256.bzip2	11.91	12.24	7.19	7.08
Average	80.00	82.33	3.38	3.37

Table 8.1: SPEC CINT2000 benchmark compile and run times (in seconds)

²The omission of 176.*gcc* and 300.*twolf* from this, and subsequent tables, indicates that these benchmarks exhibited bugs at translation level 1 and higher.

Tables 8.2, 8.3, 8.4 and 8.5 expand on the results of Table 8.1 for 164.*gzip*, 181.*mcf*, 254.*gap*, and 256.*bzip2* at the remaining translation levels, as well as showing the percentage differences in compile and run times.³ Notice in Tables 8.2 and 8.3 that there is little deviation between the compile-times for the individual translation levels. These numbers indicate that the same cost ensues even when more work is performed, as the SSA form is maintained incrementally. Tables 8.4 and 8.5 show the expected trend, where the compile-time increases as more work is performed along later translation levels. Execution times vary greatly among the benchmarks. Tables 8.2, 8.4 and 8.5 present how the various translation levels consistently achieve better execution rates. However, Table 8.3 shows that *mcf* performs poorly across translation levels. These results are still preliminary, as the full benefits are not expected to be realized until after optimizations that exploit the properties of SSA are implemented. At this point, since we want to maintain the SSA form as long as possible, we just need to ensure that the individual translation levels do not overwhelmingly degrade performance.

Translation level	Compile-time	Time increase (%)	Run-time	Speedup (%)
0	22.29	-	1.69	-
1	22.24	-0.2	1.71	-1.2
2	22.50	0.9	1.65	2.4
3	22.95	3.0	1.65	2.4
4	23.23	4.2	1.65	2.4
5	23.10	3.6	1.67	1.2

Table 8.2: Compile and run times for *gzip* (in seconds)

Translation level	Compile-time	Time increase (%)	Run-time	Speedup (%)
0	11.15	-	0.27	-
1	11.32	1.5	0.29	-7.4
2	11.29	1.3	0.27	0
3	11.18	0.3	0.28	-3.7
4	11.37	2.0	0.27	0
5	11.28	1.2	0.28	-3.7
6	11.45	2.7	0.27	0

Table 8.3: Compile and run times for *mcf* (in seconds)

³164.*gzip* and 254.*gap* had problems at translation level 6, and were thus omitted from Tables 8.2 and 8.4, respectively.

Translation level	Compile-time	Time increase (%)	Run-time	Speedup (%)
0	236.38	-	1.57	-
1	244.57	3.5	1.62	-3.2
2	245.99	4.1	1.30	17.2
3	249.03	5.4	1.92	-22.3
4	254.08	7.5	1.41	10.2
5	256.68	8.6	1.32	15.9

Table 8.4: Compile and run times for *gap* (in seconds)

Translation level	Compile-time	Time increase (%)	Run-time	Speedup (%)
0	11.91	-	7.19	-
1	12.24	2.8	7.08	1.5
2	12.68	6.5	7.11	1.1
3	12.83	7.7	7.13	0.8
4	13.01	9.2	7.10	1.3
5	12.91	8.4	6.17	14.2
6	13.44	12.9	6.18	14.1

Table 8.5: Compile and run times for *bzip2* (in seconds)

8.2 Inserted Instructions

The next interesting measure of how the later phase SSA performed is the number of inserted instructions. Throughout the SSA algorithm, there are two distinct opportunities for additional instructions to be included in the intermediate code. Both ϕ and ψ functions are inserted, and then copies are included to remove these unexecutable instructions. It is obviously desirable that the number of extra instructions not greatly hinder the baseline performance. The number of actual instructions executed is discussed in Section 8.3.

Table 8.6 gives a summary of the number of ϕ , ψ , and copy instructions added through the process of building and removing the SSA form for translation level 1. As will be seen in Section 8.3, the weight of these inserted instructions is negligible.

Tables 8.7, 8.8, 8.10, and 8.11 expand on the results of Table 8.6 for the remaining translation levels. It is interesting to note that, on average, more copies are needed to remove the ϕ and ψ functions as the translation levels increase. As the SSA form is maintained longer, more transformations can be performed. Therefore, the analysis that results in the insertion of copies can become more difficult, resulting in more copies being required to ensure correctness.

For comparative purposes, we have also included the results for Sreedhar *et al.*'s

Benchmark	# of ϕ and ψ functions inserted	# of copies inserted
164.gzip	1089	437
181.mcf	230	67
197.parser	2364	421
254.gap	13682	6020
255.vortex	6112	1058
256.bzip2	771	211

Table 8.6: Number of ϕ , ψ and copy instructions inserted in the SPEC CINT2000 benchmarks

translation method 1 (Section 4.4.1) in Table 8.9.⁴ Method 2 outperforms method 1 in the number of ϕ -copies inserted for the individual translation methods, and thus is justified as the method of interest. Method 1 inserts many more copies than are necessary.

Translation level	# of ϕ -functions inserted	# of copies inserted	# of ψ -functions inserted	# of copies inserted
1	989	269	100	168
2	989	269	100	168
3	989	304	100	232
4	989	309	100	232
5	989	309	100	228

Table 8.7: Number of ϕ , ψ and copy instructions inserted at individual translation levels in *gzip*

Translation level	# of ϕ -functions inserted	# of copies inserted	# of ψ -functions inserted	# of copies inserted
1	193	10	37	57
2	193	32	37	57
3	193	27	37	87
4	193	25	37	87
5	193	25	37	75
6	222	25	37	75

Table 8.8: Number of ϕ , ψ and copy instructions inserted at individual translation levels in *mcf*

⁴Translation level 6 had a problem with the linker, and is thus excluded from these results.

Translation level	# of ϕ -functions inserted	# of copies inserted	# of ψ -functions inserted	# of copies inserted
1	193	619	37	57
2	193	624	37	57
3	193	564	37	87
4	193	530	37	87
5	193	530	37	75

Table 8.9: Number of ϕ , ψ and copy instructions inserted at individual translation levels in *mcf* for Sreedhar’s *et al.*’s translation method 1

Translation level	# of ϕ -functions inserted	# of copies inserted	# of ψ -functions inserted	# of copies inserted
1	10909	1959	2773	3830
2	10909	2172	2773	3848
3	10909	2292	2773	4787
4	10909	2165	2773	4791
5	10909	2209	2773	4762

Table 8.10: Number of ϕ , ψ and copy instructions inserted at individual translation levels in *gap*

8.3 Executed Instructions

The final category of measurements is the actual number of instructions executed, or retired, at runtime. These figures were obtained using the hardware performance monitoring tool *pfmon* [13]. We want to measure the increased number of instructions executed using SSA, hoping the additions do not overwhelm the original code generator’s results.

Table 8.12 indicates the differences between number of executed instructions at the baseline level versus those executed at translation level 1. A percentage indicating number of extra instructions is also included. In general, there are only an extra 0.51% of instructions executed when later phase SSA is included

Tables 8.13, 8.14, 8.16, and 8.17 expand on the results of Table 8.12 for the remaining translation levels. We can see from these tables that there is no significant change in the number of retired instructions as we proceed through the translation levels.

Comparatively, Table 8.15 gives the number of retired instructions for *mcf* using Sreedhar *et al.*’s translation method 1. On average, the naive translation method executes an extra 11% of instructions over the algorithm that uses interference graph updates.

Translation level	# of ϕ -functions inserted	# of copies inserted	# of ψ -functions inserted	# of copies inserted
1	673	86	98	125
2	673	87	98	125
3	673	114	98	175
4	673	111	98	175
5	673	113	98	171
6	818	113	98	171

Table 8.11: Number of ϕ , ψ and copy instructions inserted at individual translation levels in *bzip2*

Benchmark	Baseline	SSA	% of increase in instructions over baseline
164.gzip	4,226,267,378	4,444,772,461	5.17
181.mcf	292,144,926	296,331,818	1.43
197.parser	5,500,841,729	5,513,781,510	0.24
254.gap	1,624,134,732	1,627,696,252	0.22
255.vortex	13,186,363,361	13,199,873,707	0.10
256.bzip2	14,270,261,637	14,215,398,582	-0.38
Average	6,516,668,961	6,549,642,388	0.51

Table 8.12: Number of executed instructions for the SPEC CINT2000 benchmarks

The results presented in this chapter have shown that the later phase SSA framework adds a minimal amount of compile-time and few additional executed instructions for the SPEC CINT2000 benchmarks. As well, the run-time is not compromised by the SSA inclusion. Therefore, working with the later phase SSA by introducing further code optimizations is a competitive option for the ORC.

Translation level	# of retired instructions	% increase over baseline
Baseline	4,226,267,378	-
1	4,444,772,461	5.17
2	4,475,198,347	5.89
3	4,489,361,441	6.23
4	4,492,050,665	6.29
5	4,516,763,080	6.87

Table 8.13: Number of executed instructions at individual translation levels in *gzip*

Translation level	# of retired instructions	% increase over baseline
Baseline	292,144,926	-
1	296,331,818	1.43
2	296,331,791	1.43
3	296,002,885	1.32
4	295,647,938	1.20
5	293,062,433	0.31
6	292,946,658	0.27

Table 8.14: Number of executed instructions at individual translation levels in *mcf*

Translation level	# of retired instructions	% increase over baseline
Baseline	292,144,925	-
1	331,373,448	13.43
2	329,715,993	12.74
3	328,431,952	12.42
4	327,940,049	12.25
5	324,111,065	10.94

Table 8.15: Number of executed instructions at individual translation levels in *mcf* using Sreedhar's *et al.*'s translation method 1

Translation level	# of retired instructions	% increase over baseline
Baseline	1,624,134,732	-
1	1,627,696,252	0.22
2	1,627,086,081	0.18
3	1,634,621,472	0.65
4	1,633,378,414	0.57
5	1,633,645,871	0.59

Table 8.16: Number of executed instructions at individual translation levels in *gap*

Translation level	# of retired instructions	% increase over baseline
Baseline	14,270,261,637	-
1	14,215,398,582	-0.38
2	14,201,901,874	-0.48
3	14,216,218,572	-0.38
4	14,230,515,987	-0.28
5	14,261,806,865	-0.06
6	14,274,974,881	0.03

Table 8.17: Number of executed instructions at individual translation levels in *bzip2*

Chapter 9

Future Work

Since we expect some improvements in efficiency using Sreedhar *et al.*'s third translation technique (Section 4.4.3), it should be implemented in the ORC. Then, comparisons can be made with the two techniques already in place.

When the full framework is established, it would be of great interest to add additional optimizations into the code generator of the ORC. Besides the code transformations already in place, further benefits could be realized with the inclusion of specific optimizations geared towards the SSA form. As discussed in Chapter 8, the current implementation does not hinder performance, but does nothing to improve it. Optimizations that take full advantage of SSA could certainly result in experimental gains.

The enhancement to Cytron *et al.*'s ϕ -placement algorithm presented in Chapter 7 gives another opportunity for future work. The evidence is strong that this optimization of the traditional algorithm will produce a decreased amount of iterations through the worklist algorithm. Thus, an improvement in compile-time is possible.

A long term goal of this project is to maintain the later phase SSA algorithm even further in the code generator, at least through local instruction scheduling. Eventually, a method may be discovered for handling SSA during register allocation.

Finally, it would be interesting to evaluate the effects of later phase SSA on other compilers. However, compilers intended for architectures that support predication should benefit from this algorithm more than others.

Chapter 10

Conclusion

This thesis has presented a comprehensive study into the unique properties and wide ranging capabilities of the Static Single Assignment form. Commonly used to ease dataflow analysis, SSA is a powerful representation that produces many benefits for the code optimizations supported by it. However, not all transformations have traditionally been able to avail of the SSA form. In particular, architectures that implement predication have avoided SSA in the later stages of the compiler after if-conversion removes conditional expressions. Unfortunately, such later phase code transformations have not benefited from the elegant framework provided by the SSA representation.

Throughout the course of this thesis, ψ -SSA, a mechanism for dealing with SSA at a later compiler phase, has been presented. ψ -SSA combines traditional SSA ϕ -placement with new ideas for handling predicated execution to produce an entire SSA algorithm. Additionally, implementation details using the Open Research Compiler were disclosed. The framework for the code generator has been shown to not impose serious performance penalties on the baseline compiler, thus making the later phase SSA algorithm a viable starting point for further code optimizations.

As well, an improvement to a well-known ϕ -placement technique was suggested. Throughout this method, worklists are used to decide where ϕ -functions should be inserted. We have shown that entire worklists can be eliminated and the number of elements in some remaining worklists decreased using our augmentation. The opportunities for optimization were explored for the SPEC CINT2000 benchmark suite on the ORC. The validity of the enhancement allows future implementations to incorporate the small, but significant, change.

This thesis has demonstrated the usefulness of SSA at a later stage of the com-

pilation process. Since most production compilers avoid SSA in the code generator, we believe that many opportunities for improving the quality of code produced are lost. Using the ψ -SSA algorithm, a new framework for the code generator of the ORC is now available. We hope that this work is the beginning of a renewed focus on utilizing SSA to its full potential in later compiler phases.

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