

Evaluating Risk Response Strategies on Construction Projects Using a Fuzzy Rule-Based System

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Abstract – The development and implementation of risk response strategies contributes to effective risk management processes in construction organizations. Risk response strategies need to be developed and implemented as follows: first, all possible risk responses for each given risk event of a project are identified; next, each risk response is evaluated to determine its effectiveness; then, for each risk event of the project, the optimal risk response is identified and implemented; and finally, the risk events and responses are consistently monitored. The existing literature confirms that there is a lack of research on evaluation criteria for risk responses, making it difficult to determine their effectiveness. This paper presents research that fills this gap by developing a way to evaluate the effectiveness of risk response strategies using a fuzzy rule-based system (FRBS) that consists of three inputs and one output. The inputs of the FRBS are the affordability and the achievability of risk responses and the controllability of risk events; the output is the effectiveness of the risk response. The application of fuzzy ranking methods instead of crisp ranking methods allows the model to mimic three human attitudes towards risk: risk averse, neutral, and risk taking. The proposed model lays the foundation for an automated evaluation of risk response strategies and provides a decision support tool for experts in the field.

Keywords – Risk management; risk response; fuzzy logic; FRBS

1 Introduction

Risk management is vital for achieving business objectives on construction industry projects. Current trends in the construction industry are towards bigger and more complex projects, which can result in a greater amount of risks and uncertainties [1]. These risks can cause failures in terms of cost overruns, schedule delays, environmental damages, and fatal injuries. In general, risk management processes include identification, qualitative analysis, quantitative analysis, risk response planning, and monitoring and control [2]. First, risk events need to be identified and documented. These risk events should be analyzed by qualitative methods so they can be prioritized based on probability and impact. Next, quantitative risk analysis must be performed to model the combined effects of randomly occurring risk events and to develop a synthesized view of the overall effects of risk events on the project. Then, risk responses should be identified, evaluated, and implemented to mitigate occurrence probability and/or the negative impacts of risk events. Finally, the overall effectiveness of the risk management process needs to be monitored, reviewed, and controlled on a regular basis. The effectiveness of the risk response is the extent to which the risk events' probabilities and/or impacts are reduced as a result of implementing the risk responses.

A large amount of the research on risk management acknowledges the importance of risk response planning [3]. Hillson [4] argues that identifying and analyzing risks and uncertainties is clearly vital for the risk management process, as it is not possible to address risks that are not identified or that are poorly analyzed. Risk response planning is considered an important step for effective risk management; it is a process that is complementary to risk identification and analysis; and without risk response planning, only limited benefits can be had from the risk management process [4]. Risk response strategies need to be developed and implemented as follows: first, all possible risk response strategies for each given risk event of the project are identified. Next, each risk response strategy is evaluated to determine its effectiveness. Then, for each risk event, the optimal risk response strategy is identified and implemented. Finally, the risk events and the response strategies are consistently monitored.

Although some researchers have developed optimization-based methods for selecting an optimal set of risk responses [5], the application of these methods on real projects can be a complex and costly process due to the effort and amount of data that are required. Moreover, these models account for only a limited number of criteria, namely time, cost, and quality, which can lead to the selection of risk responses that are cost effective but unfeasible in terms of technology, environment, and achievability. Optimization-based approaches have low transparency (i.e., they operate in such a way that it is not easy for others to see what actions are performed) during the process of selecting the optimal set of risk responses. Employing approaches with the ability to address the abovementioned weak points can result in more realistic, applicable, and feasible risk responses—a fuzzy ruled-based system (FRBS) is just such an approach. The existing literature confirms that there is a lack of research on evaluation criteria for risk response strategies, making it difficult to determine their effectiveness. The objectives

55 of this paper are to (1) identify appropriate criteria for evaluating risk responses; (2) develop an FRBS to determine
 56 the effectiveness of risk responses; and (3) develop a fuzzy ranking method for selecting the most effective risk
 57 responses.

58 This paper is organized as follows. First, a brief literature review of risk management and risk response
 59 planning in construction projects is presented, followed by a discussion about the application of fuzzy logic
 60 methods in the risk management process. Second, evaluation criteria for risk responses are identified and an FRBS
 61 is developed for determining the effectiveness of risk responses; a fuzzy ranking method is then applied to rank
 62 the risk responses based on their effectiveness (determined by the FRBS) on construction projects. Third, a
 63 hypothetical example is provided to illustrate the proposed framework. Finally, conclusions are presented and
 64 future extensions of the current research are discussed.

65 **2 Overview of Risk Response Evaluation and Selection Approaches**

66 Risk response planning involves reducing the negative impact and probability of occurrence of risk events to
 67 ensure project success. Identified risk responses need to be evaluated, and the optimal risk response needs to be
 68 implemented for each risk event. Several researchers have developed decision support systems for evaluating and
 69 selecting risk responses using different approaches, including the trade-off approach [4, 6, 7], the zonal-based
 70 approach [8, 9], mathematical modeling and optimization [5, 3, 10–13], and a combination of these approaches
 71 and fuzzy logic [14].

72 The trade-off approach makes trade-offs between parameters—such as cost, time, and quality—that are either
 73 risk event-related or risk response-related in order to evaluate a set of risks. Kujawski [6] makes trade-offs that
 74 account for a project’s objective requirements and project stakeholders’ subjective preferences. Risk responses
 75 are selected based on the cost of implementing each risk response compared with the probability of project success
 76 when the risk response is implemented. Hillson [4] argues that the effectiveness of proposed risk responses must
 77 be assessed based on appropriateness (i.e., the correct level of risk response according to the severity of the risk
 78 event, ranging from a crisis response to a “do nothing” response), affordability (i.e., the cost effectiveness of the
 79 risk response), achievability (i.e., how realistically achievable or feasible the risk response is, either technically
 80 or in terms of a respondent’s capability and authority), agreement (i.e., the consensus and commitment of
 81 stakeholders), and allocation (i.e., the responsibility of and accountability for implementing the risk response).
 82 Qazi et al. [7] develop a model for selecting a set of optimal risk responses by measuring the impacts of different
 83 combinations of risk responses on the objective function of a project. In zonal-based approaches, two-dimensional
 84 diagrams are applied to assess the regions of the risk responses using one of two common assessment tools: (1) a
 85 matrix that features different factors in a two-dimensional diagram and (2) a two-axis graph that maps risk
 86 responses based on the values of the two dimensions.

87 Using an optimization-based approach, Fan et al. [5] suggest a model for assessing the effectiveness of risk
 88 responses based on three criteria: risk event controllability, risk response costs, and project characteristics. Kayis
 89 et al. [10] employ five heuristic algorithms to minimize the cost of implementation within the constraints of the
 90 implementation budget and acceptable risk effects for new product development. Zhang and Fan [11] maximize
 91 the sum of estimated risk response effects (i.e., they reduce the expected loss of the risk event) after risk response
 92 strategy implementation using a method for selecting risk responses with an integer linear programming (ILP)
 93 model. Zhang [12] uses an ILP model that accounts for the cost of implementation and the determined budget for
 94 risk responses. Wu et al. [13] propose a multi-objective decision-making model for the selection of risk responses
 95 that minimize total expected losses, total expected schedule delays, and total expected quality reduction. An
 96 optimization model is used to minimize expected time loss, expected cost loss, and expected quality loss. To
 97 calculate the coefficients of the objective function, a fuzzy analytic hierarchy process (FAHP) is employed as a
 98 technique to guide the risk analysts [14].

99 **3 Developing the Risk Response Evaluation and Selection Approach**

100 In order to develop the proposed FRBS for the evaluation of risk responses, appropriate evaluation criteria are
 101 identified, which are the inputs of the FRBS. The output of the FRBS is the effectiveness of the risk responses.
 102 Based on the output of the FRBS, the risk responses are then ranked using a fuzzy ranking method that allows the
 103 model to mimic the three human attitudes towards risk: risk averse, neutral, and risk taking.

104 **3.1 Evaluating Risk Responses: Identifying Inputs and Outputs**

105 This study uses three criteria to evaluate risk responses: affordability of the risk response, achievability of the
 106 risk response, and controllability of risk events. These criteria make up the three inputs of the FRBS, and its output
 107 is the effectiveness of the risk response strategy. There is a positive correlation between the controllability of a
 108 risk event and the effectiveness of its risk response. For example, even if you implement a risk response with high
 109 affordability and high achievability, the risk response will not be effective in addressing a risk event with low
 110 controllability. Therefore, the FRBS developed for the evaluation of risk responses needs to evaluate both risk
 111 events and their identified risk responses in order to identify the most effective risk responses. Subjective system

112 variables (evaluation criteria) are represented by triangular fuzzy membership functions, which are commonly
 113 used in engineering applications.

114 *Affordability* refers to the cost-effectiveness of risk responses, where the amount of time, effort, and money
 115 spent on addressing a risk should not exceed the available resources for implementing risk responses. One way to
 116 measure the cost-effectiveness of risk responses is to use the risk reduction leverage (RRL) factor, which can be
 117 calculated by converting the impact of the risk event into a monetary value (for example, the cost of delay and/or
 118 the cost of negative impacts on quality) [4]. RRL represents the ratio of the increase in risk event exposure to the
 119 cost of risk response implementation. RRL can be calculated by dividing the difference between the risk responses'
 120 cost impacts before and after implementation by the implementation cost (see Equation (1)) [4].

$$RRL = \frac{(\text{Cost Impact})_{\text{before response}} - (\text{Cost Impact})_{\text{after response}}}{\text{Cost of response}} \quad (1)$$

121 Hillson [4] proposes that responses with high effectiveness in terms of affordability should have RRL values
 122 above 20. Responses with medium effectiveness have RRL values ranging from 1 to 20, and RRL values of less
 123 than 1 can be labelled as having low effectiveness (i.e., they are ineffective) because their implementation cost is
 124 more than what they might save later. Thus, the fuzzy membership functions for affordability are defined as low
 125 (less than 1), medium (between 1 and 20), and high (more than 20).

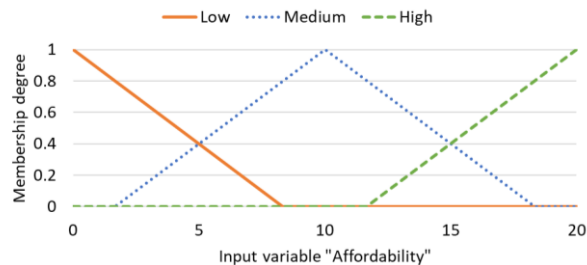
126 *Achievability* refers to the feasibility of a risk response in terms of three considerations: the technical
 127 complexity of the proposed risk response, the capability of the respondent, and the authority of respondent [4].
 128 According to Fan et al. [5], the complexity of a risk response may stem from technical obstacles, political obstacles,
 129 limited access to information, or conflict resolution obstacles. Three fuzzy membership functions of achievability
 130 can be defined, namely low, medium, and high achievability.

131 Miller and Lessard [15] define *controllability* as the likelihood that the probability of occurrence of a risk
 132 event can be changed. This criterion describes the nature of the risk situation. Risk events with a low degree of
 133 controllability include occurrences such as natural disasters, while risk events with a high degree of controllability
 134 are caused by scheduling and budget problems. The latter can be addressed more effectively than the former by
 135 implementing an identified risk response [5]. Although the controllability value of a risk event is the same for all
 136 of its related risk responses, this criterion can be used to ascertain whether risk responses meet the threshold for
 137 effectiveness, which can be determined by risk decision makers. As with affordability and achievability,
 138 controllability can be categorized into three fuzzy membership functions, namely low, medium, and high.

139 3.2 Evaluating Risk Responses Using an FRBS

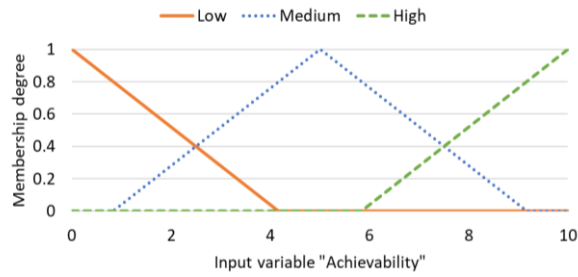
140 An FRBS is a methodology for modeling human logical thinking and decision-making. These systems use
 141 membership functions and fuzzy rules to make a decision [16]. An FRBS can be developed with either data or
 142 expert judgments using one of the few approaches proposed in the literature. Fuzzy c-means (FCM) clustering
 143 can be employed when there is access to historical data [17]. Expert judgments can be applied to develop an FRBS
 144 when historical data is unavailable [18, 19]. In this paper, the FRBS for the evaluation of risk responses is
 145 developed using expert judgments. The membership functions of three inputs and one output are determined based
 146 on documented literature using MATLAB® R2018b.

147 In this paper, a Mamdani fuzzy inference system is used to develop an FRBS for the evaluation of risk
 148 responses; by delivering fuzzy outputs, the Mamdani inference system facilitates the use of different
 149 defuzzification methods for fuzzy ranking. The membership functions of affordability are determined by RRL
 150 values between 0 and 20 as recommended by Hillson [4]. Figure 1 shows the membership functions of
 151 affordability.



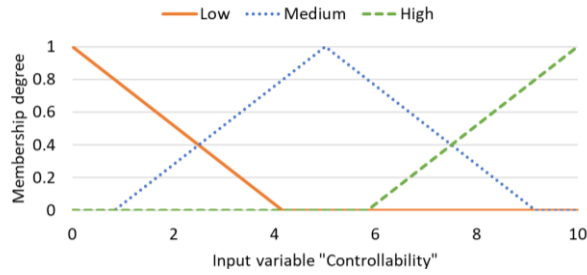
152
 153 **Figure 1.** Membership functions of affordability.

154 For the achievability and controllability membership functions, the three linguistic terms *low*, *medium*, and *high*
 155 are used, as illustrated in Figure 2 and Figure 3, respectively.



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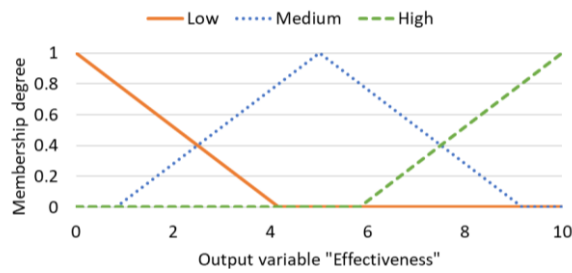
Figure 2. Membership functions of achievability.



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Figure 3. Membership functions of controllability.

160 The membership function of the FRBS output (effectiveness) is also between 0 and 1, as shown in Figure 4.



161
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Figure 4. Membership functions of effectiveness.

163 Fuzzy rules are defined as “if-then” rules. In this system, 27 if-then fuzzy rules are defined. Some of these
164 rules are presented in Table 1.

165 **Table 1.** Fuzzy rules used in the FRBS.

Rule	If			Then
	Affordability	Achievability	Controllability	Effectiveness
1	Low	Low	Low	Low
2	Low	Low	Medium	Low
3	Medium	Medium	Medium	Medium
4	Low	Medium	Medium	Medium
5	High	High	High	High
6	Medium	High	High	High

166 Figure 5 shows the three-dimensional curve that represents the mapping from inputs to output and the
167 dependency of effectiveness on controllability and affordability.

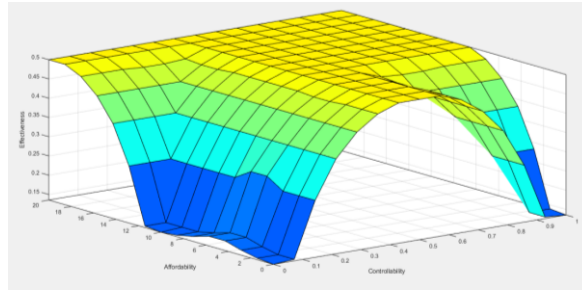


Figure 5. Three-dimensional representation of the proposed FRBS.

3.3 Selecting Effective Risk Responses Using the Fuzzy Ranking Method

In the next step, the risk responses need to be ranked based on their effectiveness, so that the most effective risk response can be selected for each risk event. In order to solve decision-making problems, fuzzy ranking methods are commonly used, wherein the evaluation scores (i.e., effectiveness) of decision alternatives (i.e., risk responses) are represented by fuzzy membership functions [20, 21]. There are various fuzzy ranking methods discussed in the literature, the majority of which can be grouped into three categories based on the approaches they use to rank fuzzy numbers. The first category of fuzzy ranking methods includes those methods that rank fuzzy numbers based on their α -cuts at a pre-specified level of α [22]; thus, these methods change the fuzzy ranking problem into an interval ranking problem. The second category of fuzzy ranking methods includes those methods that use fuzzy distance measures to rank fuzzy numbers [23]. The third category of fuzzy ranking methods includes those that rank the fuzzy numbers based on their defuzzified values [21]; these methods change the fuzzy ranking problem into a simple problem of ranking crisp numbers. The first two categories of fuzzy ranking methods (i.e., α -cut-based methods and fuzzy distance-based methods) usually require that fuzzy numbers be regularly shaped (e.g., triangular or trapezoidal fuzzy numbers) [21]. However, in this paper, the output of the FRBS (i.e., the effectiveness of the risk responses) is an irregularly shaped fuzzy membership function. Therefore, in this paper, the third category of fuzzy ranking methods (i.e., ranking methods based on the defuzzified value) is used to rank risk responses based on their effectiveness. To do this, the results of the FRBS need to be defuzzified. There are various defuzzification methods proposed in the literature; the smallest of maximum (SOM), largest of maximum (LOM), and center of area (COA) methods are commonly used in different engineering applications of fuzzy logic. Figure 6 presents the three aforementioned defuzzification methods implemented on a hypothetical example of risk response effectiveness. Moreover, Figure 6 also shows how different defuzzification methods can result in different defuzzified values for risk response effectiveness.

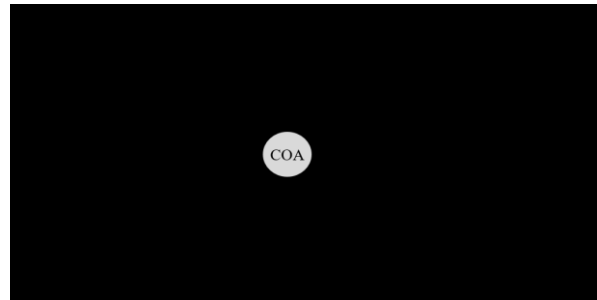


Figure 6. COA, SOM, and LOM defuzzification methods.

When ranking risk responses based on the defuzzified value of their effectiveness, the use of different defuzzification methods can mimic different human attitudes towards risk. Ranking risk responses based on the results of the SOM method means that the decision maker considers the smallest maximum value of effectiveness for each risk response and ignores all other possible values for the effectiveness of the risk response (see Figure 6). Thus, ranking risk responses based on the results of the SOM method mimics a risk-averse attitude. In contrast, ranking the risk responses based on the results of the LOM method means that the decision maker considers the largest maximum value of effectiveness for each risk response and ignores all other possible values for the effectiveness of the risk response (see Figure 6). Thus, ranking the risk responses based on the results of the LOM method mimics a risk-taking attitude. The COA, on the other hand, determines the defuzzified value of effectiveness by taking into consideration all possible values of effectiveness for each risk response. Accordingly, ranking risk responses based on the results of the COA method mimics a neutral human attitude towards risk. In this paper, the three aforementioned defuzzification methods (i.e., SOM, LOM, and COA) are used to rank risk

206 responses based on their effectiveness so that all three human attitudes towards risk can be mimicked in the
207 selection of the most effective risk responses.

208 **4 Hypothetical Example**

209 In this section, a hypothetical example is presented to demonstrate how to use the proposed approach to
210 evaluate the effectiveness of risk responses and select the most effective. Assume two risk events: (1) incomplete
211 design and (2) operation interruption due to adverse weather conditions. The first risk event can be addressed by
212 two possible risk responses: (1-1) outsourcing design to subcontractors or (1-2) employing professional design
213 teams. To mitigate the second risk event, two risk responses are possible: (2-1) schedule compression using extra
214 resources or (2-2) considering alternative construction methods, such as using precast materials. A number
215 between 0 and 10 represents achievability (where 10 is high) and another number between 0 and 10 represents
216 controllability (again, 10 is high); these numbers are determined for each risk response by expert judgment. The
217 values for each criterion can be found in Table 2.

218 **Table 2.** The input values of each risk response and its related risk event.

Risk Event	Risk Response	Affordability (RRL)	Achievability	Controllability
1	1-1	7.00	9.00	6.00
	1-2	12.00	5.00	6.00
2	2-1	7.00	6.00	2.00
	2-2	5.00	3.00	2.00

219 Since this hypothetical example is presented simply for illustrating the proposed approach, a limited number
220 of risk factors are identified for risk response evaluation. In a real construction case study, a comprehensive list
221 of risk factors such as environmental and safety risk factors may be considered for risk response evaluation. Table
222 3 shows the effectiveness values, which are based on the information in Table 2. The inputs are imported to the
223 FRBS to evaluate the effectiveness of the risk responses. Crisp numbers representing the effectiveness of the risk
224 responses are then predicted by the FRBS using three defuzzification methods (i.e., SOM, LOM, and COA) as
225 discussed in Section 3.3 and the risk responses are ranked accordingly. Table 3 presents the effectiveness of the
226 risk responses and their rankings for the two risk events.

227 **Table 3.** The effectiveness values of each risk response and its related risk event.

Risk Response	Effectiveness					
	(SOM)	Rank	(LOM)	Rank	(COA)	Rank
1-1	8.50	1	10.00	1	6.95	1
1-2	4.10	2	6.00	2	5.00	2
2-1	0.00	-	2.00	2	3.74	2
2-2	0.00	-	2.50	1	3.92	1

228 Table 3 presents the most effective risk response for each of the two risk events as determined by three different
229 defuzzification methods. The effectiveness value determined using the SOM defuzzification method mimics a
230 risk-averse attitude; the LOM defuzzification method mimics a risk-taking attitude; and the COA defuzzification
231 method mimics a neutral attitude towards risk. Although in this case study the rankings of the risk responses are
232 similar for each of the three defuzzification methods, on real construction projects with numerous risk responses,
233 rankings can be different for different defuzzification methods. Since higher effectiveness of risk responses is
234 favorable, in the hypothetical example, risk responses 1-1 and 2-2 should be selected for risk events 1 and 2,
235 respectively. As shown in Table 3, the values of effectiveness for risk responses 2-1 and 2-2 are equal to zero,
236 which indicates neither of these two risk responses should be applied to risk event 2 if the risk response strategy
237 is based on a risk-averse attitude. Moreover, as discussed in Section 3.1, risk responses can be rejected if their
238 effectiveness is less than a threshold value that is determined by the decision maker. For instance, assuming an
239 effectiveness value of 5 as the threshold for the risk responses' effectiveness, both risk responses for the second
240 risk event (i.e., 2-1 and 2-2) are not acceptable in this case study (refer to Table 3). In this situation, new risk
241 responses should be identified for the second risk event or its adverse effects on the project should be accepted.

242 **5 Conclusions and Future Research**

243 This paper presents a methodology for evaluating the effectiveness of identified risk responses by applying an
244 FRBS that has three inputs as evaluation criteria and that produces the effectiveness of risk responses as an output.

245 The three inputs are the affordability of each risk response, the achievability of each risk response, and the
246 controllability of related risk events. The FRBS uses the estimated crisp values of affordability, achievability, and

247 controllability to evaluate the effectiveness of risk responses according to the rules developed based on experts'
 248 opinions. The output, which is a fuzzy set, is used as an input for three different fuzzy ranking methods, one based
 249 on SOM, one based on LOM, and one based on COG (COA), to determine the most effective risk response in
 250 terms of affordability, achievability, and controllability. Applying an expert-driven FRBS and fuzzy ranking
 251 methods can help automate the evaluation of risk response strategies, and this technique delivers an expert-level
 252 risk management tool to a non-expert in the field. The contributions of this paper are threefold: first, the
 253 appropriate criteria for evaluating risk responses are identified from the literature; second, an FRBS is developed
 254 to automate the evaluation of risk responses; and third, the application of different fuzzy ranking methods is
 255 proposed to mimic the risk-taking attitude of experts for risk response evaluation.

256 On construction projects, risk events are often dependent on one another; for example, the risk of precipitation
 257 is linked to the risk of excessive soil moisture in earthmoving operations. In order to develop a comprehensive
 258 risk response planning tool, interdependencies between different risk events need to be taken into consideration.
 259 In future research, the FRBS developed in this paper will be extended to capture these interdependencies and
 260 determine the most effective risk responses for each risk event, accounting for all risk events that affect a project
 261 throughout its life cycle.

262 **6 Acknowledgments**

263 This research is funded by the Natural Sciences and Engineering Research Council of Canada (NSERC)
 264 Industrial Research Chair in Strategic Construction Modeling and Delivery (NSERC IRCPJ 428226-15), which
 265 is held by Dr. Aminah Robinson Fayek. The authors gratefully acknowledge the financial support provided by
 266 industry partners and NSERC through the Chair.

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