Modifications to Reduce the Minimum Thermal Source Temperature of the ST05G-CNC Stirling Engine

by

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Abstract

An experimental study has been executed with two main objectives. The applicability of the second order modeling approach for low thermal source temperature Stirling engines was assessed, and modifications to improve the low thermal source temperature performance of an ST05G-CNC Stirling engine were studied.

A test rig was fabricated, which featured a modified ST05G-CNC Stirling engine equipped with instrumentation to measure gas and coolant temperatures, gas pressures, output torque, crankshaft position, and coolant flow rate. Novel aspects of the test rig include high speed buffer pressure measurements, and separation of the water jacket into two independent zones.

A second order mathematical model was assembled drawing from the literature. The model could use either the ideal isothermal model or the ideal adiabatic model as a reference cycle. Imperfect heat transfer, regenerator enthalpy loss, flow friction, mechanical friction, appendix gap loss, and conduction loss were calculated based on the reference cycle results. It was shown that the two reference cycles studied give increasingly similar results as the thermal source temperature declines.

Three modifications to the engine were tested experimentally: The piston diameter was decreased from 85 mm to 44 mm, the crankcase volume was increased from 3.20 L to 7.83 L, and the dead volume of the working space was reduced from 0.877 L to 0.745 L. All together the modifications reduced the minimum thermal source temperature from 242 °C to 145 °C, with a constant thermal sink temperature of 21 °C. The reduced piston diameter and increased

crankcase volume were shown experimentally to increase the shaft power of the engine at low thermal source temperatures by reducing forced work and crankcase gas spring hysteresis. The reduction in dead volume had an immeasurable influence on the shaft power, but shifted some heat rejection duty from the connecting pipe and power cylinder water jackets to the cooler water jacket.

Agreement between experimental results and model predictions was evaluated individually for sub-components of the mathematical model. Correspondence between predicted and measured indicator diagrams was found to worsen with decreasing thermal source temperature. The trend was attributed to the greater influence of losses neglected by the reference cycles at lower thermal source temperatures. Since all other components of the model rely on the reference cycle for their input parameters, the implications of reference cycle errors are farreaching. Neglect of losses in the reference cycle simulation is fundamental to the second order modeling approach. The validity of this assumption has been shown to break down as thermal source temperature declines.

With consideration of the experimental data, replacement of the heater head was recommended as a means of reducing the minimum thermal source temperature further. By replacing the heater with something similar to the current cooler, low thermal source temperature performance could be improved by reducing temperature drop between the thermal source and the engine working fluid, and by reducing conduction loss.

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Preface

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List of Symbols

Roman Alphabet Symbols

а	parameter in finite piston speed loss calculation, $a \equiv \sqrt{3\gamma}$	-
Α	surface area	m ²
A _{cond}	cross-sectional area of conduction path	m ²
A _r	regenerator surface area (includes matrix and inside of	m²
1	housing)	
A _{flow}	cross-sectional area in the flow direction	m ²
b	appendix gap width	m
С	specific heat capacity	J/kgK
c_p	specific heat at constant pressure	J/kgK
C_v	specific heat at constant volume	J/kgK
C _{FPS}	average gas molecule speed for finite speed loss calculation	m/s
Dr_1	length of the displacer desaxe offset	m
Dr_2	length of the displacer crank arm	m
Dr_3	length of the displacer connecting rod	m
_	distance between crankshaft rotational axis and wrist pin for	
Dr_4	displacer slider crank mechanism	m
	portion of variable compression space volume controlled by	
DV_c	the displacer	m ³
d	diameter, or hydraulic diameter	m
d_{wire}	diameter of regenerator wire	m
Ε	mechanism effectiveness	-
f	frequency	Hz
-	Reynolds friction factor, equal to the Fanning friction factor	
f_{Re}	multiplied by the Reynolds number	-
F	force	Ν

g	gravitational acceleration	m/s ²
h	specific enthalpy	J/kg
h_{conv}	convective heat transfer coefficient	W/m ² K
k	thermal conductivity	W/mK
L	length	m
М	total mass in the engine	kg
m	mass	kg
'n	mass flow rate	kg/s
m_{flux}	mass flux	kg/m²s
N_B	Beale number, $N_B \equiv \frac{\dot{W}_{shaft}}{f V_{swp} P_{mean}}$	-
N_{Pr}	Prandtl number, $N_{Pr} \equiv \frac{c_p \mu}{k}$	-
N_{Re}	Reynolds number, $N_{Re} \equiv \frac{\rho u d}{\mu}$	-
N _{St}	Stanton number, $N_{St} \equiv \frac{h}{\rho u c_p} = \frac{N_{Nu}}{N_{Re} N_{Pr}}$	-
NTU	number of transfer units, $NTU \equiv \frac{hA_{regen}}{mc_p}$	-
N_W	West number, $N_W \equiv N_B \frac{(T_H + T_C)}{(T_H - T_C)}$	-
p	pressure	Ра
p_{i}	average pressure for current volume change increment	Ра
p_{mean}	mean cycle pressure	Ра
Pr_1	length of the piston desaxe offset	m
Pr_2	length of the piston crank arm	m
Pr_3	length of the piston connecting rod	m
Pr_4	distance between crankshaft rotational axis and wrist pin for piston slider crank mechanism	m
PV _c	portion of variable compression space volume controlled by the piston	m ³
¶	volumetric porosity	-
ġ	heat transfer rate per unit mass	W/kg

Q	heat	J
Q_{rloss}	regenerator enthalpy loss per cycle	J
Ż	heat transfer rate	W
\dot{Q}_{app}	rate of energy loss in the appendix gap	W
\dot{Q}_{cond}	conductive heat transfer rate	W
\dot{Q}_{rej}	heat rejection rate	W
R	specific ideal gas constant	J/kgK
S	stroke	m
t	time	S
Т	temperature	К
T _{error}	temperature error in simple heat exchanger model iterative loop	К
и	specific internal energy, or mean gas velocity	J/kg or m/s
U	internal energy	J
V	volume	m ³
<i></i> <i>V</i>	volume flow rate	m ³ /s
V _{swp}	swept volume of the piston	m ³
W	piston speed	m/s
W	work	J
W_f	forced work	J
W_{flow}	work lost to flow friction	J
W_i	indicated work, calculated area of the indicator diagram	J
δW_{FPS}	incremental work lost due to finite piston speed	J
Ŵ	power	W
\dot{W}_{shaft}	shaft power, measured at the output shaft	W
x	linear distance	m
Ζ	height	m

Greek Alphabet Symbols

α	thermal diffusivity	m²/s
Δ	prefix to indicate a change	-
γ	specific heat ratio	-
ε	regenerator effectiveness	-
η_{th}	thermal efficiency	-
θ	crank angle (maximum engine volume occurs at $\theta = 0$)	rad
5.0	angle measured from right-side horizontal to displacer crank	
$D\theta_2$	arm	rad
$P\theta_2$	angle measured from right-side horizontal to piston crank arm	rad
5.0	angle measured from right-side horizontal to displacer	
$D\theta_3$	connecting rod	rad
5.0	angle measured from right-side horizontal to piston connecting	
$P\theta_3$	rod	rad
μ	dynamic viscosity	Pas = kg/ms
ρ	density	kg/m ³
τ	torque	Nm
	phase angle between engine pressure variations and displacer	,
arphi	motion	rad
ω	angular frequency	rad/s

Subscripts

0	value at a reference point	-
b	buffer space (crankcase)	-
С	compression space	-
ck	compression space-cooler interface	-
cycle	pertaining to the engine cycle	-
С	thermal sink	-
СС	crankcase	-
CV	control volume	-
disp	displacer	-
е	expansion space	-
g	prefix to indicate a gas temperature	-
h	heater	-
he	heater-expansion space interface	-
h_1	hot gas inlet temperature for simple heat exchanger model	-
h_2	hot gas outlet temperature for simple heat exchanger model	-
Н	thermal source	-
HEX	heat exchanger	-
i	place holder for engine component subscript	-
ideal	pertaining to an assumed ideal scenario	-
in	into the control volume	-
k	cooler	-
kr	cooler-regenerator interface	-
k_1	cold gas inlet temperature for simple heat exchanger model	-
<i>k</i> ₂	cold gas outlet temperature for simple heat exchanger model	-
max	maximum value	-
min	minimum value	-
net	net value considering inflow and outflow	-
new	newly calculated value in iterative loop	-
old	previously calculated value in iterative loop	-

out	out of the control volume	-
pist	piston	-
r	regenerator	-
rej	rejection	-
rh	regenerator-heater interface	-
shaft	shaft work or power after all losses are included	-
W	prefix to indicate a wall temperature	-
x	along the x-direction	-

Chapter 1. Introduction and Literature Review

The following chapter begins with a brief discussion of the motivation for this research. Next, background information relevant to this thesis is explained. This includes a targeted description of Stirling engine operating principles, types, and mathematical models. The open literature is then surveyed regarding three main areas: Second order mathematical models, the ST05G Stirling engine, and low temperature difference Stirling engines. The chapter concludes by outlining the remainder of the thesis.

1.1 Motivation

Global concern for the health of the environment, coupled with rising fuel costs, are currently motivating research in electricity production from unconventional sources. An abundant, but largely untapped, energy resource is heat at temperatures below 232 °C [1]. Sources of this low-grade heat include industrial process waste heat [1], flat plate solar collectors, and geothermal reservoirs.

To utilize low grade heat resources for electricity production, a heat engine which can run on a low thermal source temperature is required. Since heat engines operating on small temperature differences are inherently inefficient, candidate engines must be inexpensive to build and maintain, to be commercially viable [1]. A modular design, which can be sized to match a variety of heat sources, is also desirable.

The Stirling engine is a closed cycle, externally heated, reciprocating engine, with attributes that make it a potential candidate for distributed electricity production from low grade heat sources [2]. Stirling engines typically use non-toxic, inert working fluids and may be pressurized to increase their power density [3]. With no valves, pumps, or turbines, the Stirling is relatively simple compared to other externally heated engines such as the Rankine or Ericsson. A group of Stirling units may be mechanically coupled together to create an engine of any desired power output; however, above a threshold power the multi-unit Stirling engine will be equal in complexity to its competitors, and thus lose its main advantage.

Competing technologies for low grade heat recovery include the organic Rankine cycle and the thermoelectric generator. Current technology for the organic Rankine cycle is suitable for electrical power outputs in the range of 200 - 2~000 MW [4]. This leaves room for application of the Stirling engine to smaller scale low grade heat recovery systems. Thermoelectric generators have the advantage of simplicity over the Stirling engine, as they have no moving parts; however, their high cost and relatively low efficiency make them commercially unfeasible for most applications [5].

To date, most of the Stirling engine literature deals with engines built for source temperatures above 500 °C. It is unclear whether theory developed for high temperature engines will be directly applicable to low source temperature designs. Understanding the differences between

high and low thermal source temperature Stirling engines will allow knowledge developed for high temperature designs to be applied to low temperature difference designs with confidence.

1.2 Stirling Engine Operating Principles

The following section is based on the explanation of Stirling engine operation given by West [6].

Consider the device depicted in Figure 1.1 below. A reciprocating element called the displacer separates a hot expansion space from a cold compression space. The cylinder walls of the expansion space are maintained at a high temperature relative to the walls of the compression space, which are maintained at a low temperature. A pressure gauge shows the current pressure of the gaseous working fluid in this sealed system. A narrow duct provides a connection between the compression and expansion spaces, and will allow gas to pass between them if the displacer is moved.

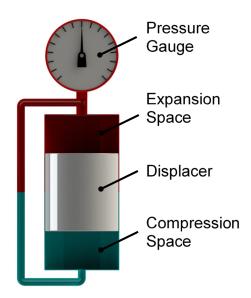


Figure 1.1: CAD Model of Displacer Cylinder, after West

In Figure 1.2, the effect of moving the displacer is illustrated. With most of the working fluid displaced to the cold compression space, as shown in Figure 1.2 (a), the average temperature of the working fluid is decreased relative to the case of Figure 1.1. Since the volume has not changed and the system is sealed, the system pressure decreases as indicated by the pressure gauge. Figure 1.2 (b) displays the inverse situation, in which the pressure has increased due to an increase of the average temperature of the working fluid. Heat has been transferred through the cylinder walls to bring about these average temperature changes.

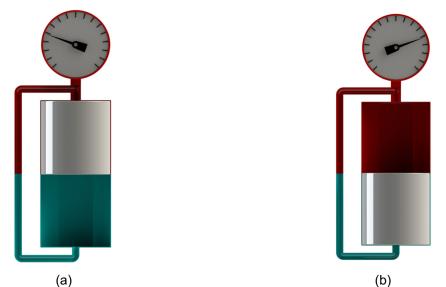


Figure 1.2: CAD Model of a Displacer Cylinder (a) Working Fluid Displaced to the Compression Space (b) Working Fluid Displaced to the Expansion Space

Although this device is an interesting way to observe ideal gas behavior, it is not an engine. True, reciprocating the displacer will move heat through the device, but since there is no change in volume, no work can be extracted. In fact, a small amount of work must be expended to overcome mechanical friction between the displacer and the cylinder, and fluid friction in the connecting duct.

To produce an engine, a piston and power cylinder are added, as presented in Figure 1.3 below. The piston separates the working space from the buffer space, which is usually the open atmosphere or a pressurized crankcase. Motion of the piston changes the volume of the working space, allowing work to be transferred to and from the engine.

With the displacer held stationary, and infinite heat transfer capability assumed for the displacer cylinder walls, moving the piston back and forth will isothermally expand and compress the working fluid. The pressure of the system will rise and fall proportionally with the changing volume, but no net work will be done in a complete cycle of the piston. Any work extracted from the system will need to be returned to bring the piston back to its original position.

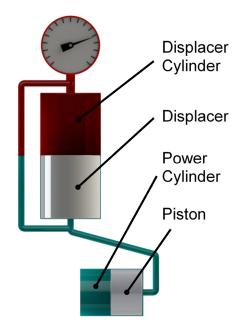


Figure 1.3: CAD Model of a Displacer Cylinder and Power Cylinder

To operate as an engine, the components shown in Figure 1.3 move through the cycle shown in Figure 1.4 below. This is known as the ideal Stirling cycle. Since all four processes are reversible if carried out at infinitesimal speed in the absence of friction, the ideal Stirling cycle has the same efficiency as the Carnot cycle. This is the textbook definition, and it offers little insight regarding the operation of real Stirling machines. The realities of friction, finite time, and finite heat transfer negate any aspiration of reaching the Carnot efficiency.

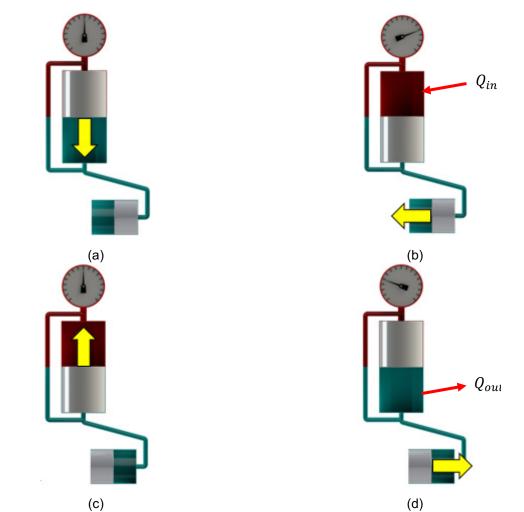


Figure 1.4: Four Processes Comprising the Ideal Stirling Cycle (a) Isochoric Heat Addition (b) Isothermal Expansion (c) Isochoric Heat Rejection (d) Isothermal Compression

In practice, the cylinder walls make very poor heat transfer surfaces, because their surface area to volume ratio is low. Dedicated heat exchangers are typically added to Stirling machines to move heat through the engine more quickly. These are shown in Figure 1.5. More effective heat exchangers allow a faster running speed and hence, a greater power output. The heater conveys heat from the thermal source to the working fluid, while the cooler conveys heat from the working fluid to the thermal sink.

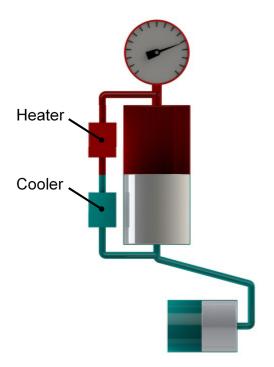


Figure 1.5: CAD Model of Displacer Cylinder, Power Cylinder, and Heat Exchangers

The optimal heat exchanger design will weigh the heat transfer benefit against the negative effects of flow friction and internal volume. Typical Stirling engine heat exchanger geometries include slots, tubes, annular gaps, and flat plates. Since the fluid properties and the heat transfer requirements of the heater and cooler are different, they are often geometrically different from each other.

Another component that is often added to real Stirling machines is the regenerator. It is placed between the heater and the cooler as indicated by Figure 1.6. The regenerator absorbs heat as the working fluid passes through it on its journey from the expansion space to the compression space. This reduces the amount of heat that must be rejected in the cooler to bring the working fluid down to the compression space temperature. The stored heat is returned to the working fluid as it moves back into the expansion space, reducing the load on the heater.

If the heater and cooler alone are effective enough to change the temperature of the working fluid to the desired limits, then the addition of a regenerator will increase the efficiency of the engine by decreasing the heat transferred between the thermal source and sink, but decrease the power output by adding flow friction. More often, the heat exchangers alone are not enough to change the temperature of the working fluid as desired. In this case, adding a regenerator can increase both the power and the efficiency of the engine.

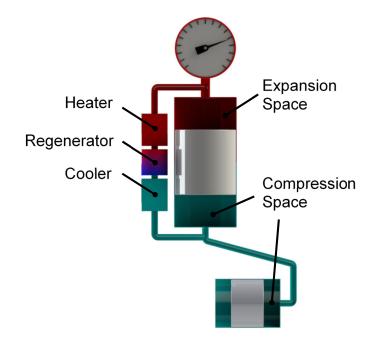


Figure 1.6: CAD Model of Five Component Stirling Machine

Like the heater and cooler, thorough regenerator design will consider the effects of heat transfer/storage, flow friction, and internal volume on the engine. Examples of regenerator geometries include densely packed fine wire mesh, randomly stacked fibers, stacked sintered wire screens, and layered foil.

Real Stirling engines also need some method of moving the piston and the displacer to drive the working fluid through an approximate Stirling cycle. For kinematic Stirling engines, this is done using a drive mechanism. A rich variety of drive mechanisms have been explored in the literature. Nearly all of them stray from the ideal cycle, by imparting continuous, near-sinusoidal motion onto the piston and displacer.

1.3 Types of Stirling Engines

Stirling engines are generally classified into three categories based on the arrangement of their components. A schematic of each type is given in Figure 1.7 below.

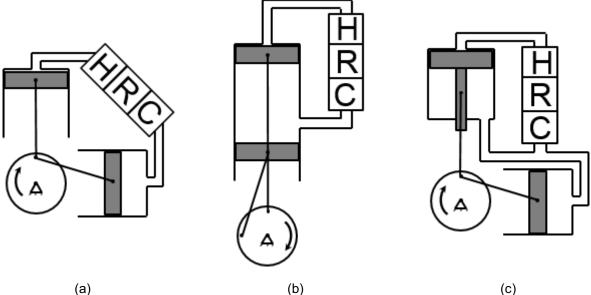


Figure 1.7: Three Main Stirling Engine Layouts (a) Alpha Type (b) Beta Type (c) Gamma Type

Both the beta and gamma types employ a piston and a displacer to move the working fluid through its cycle. The example engine used in previous figures would be considered a gamma type Stirling machine, because the displacer and the piston are in separate cylinders. In beta type engines, the piston and displacer share a common cylinder.

Alpha engines differ from betas and gammas in that they have two pistons rather than a piston and a displacer. The two pistons move together to displace the gas, and they move individually to expand and compress the gas. Alphas have the advantage of simpler flow geometry; however, they also have the disadvantage of a high temperature seal in the expansion space. Betas and gammas can easily avoid this high temperature seal by using a long displacer with the seal at the cold end. Alpha units can also be arranged to form a double acting engine, with a Stirling cycle running on either side of each piston.

Betas simplify manufacturing by requiring only one cylinder. The piston and displacer strokes often overlap, using the engine volume efficiently. Fitting the displacer drive rod through the piston in a low friction leak-free way presents a challenge for beta designs. For low temperature difference engines, in which the displacement process involves a much greater volume of gas than the volume change process, betas can become impractical, because the displacer stroke becomes much larger than the piston stroke.

Since gamma machines have separate cylinders for the piston and the displacer, the bore of each need not be the same. This simplifies the mechanism for low temperature difference engines.

1.4 Model Classification/Overview

The next section reviews the Stirling engine modeling approaches available in the literature. The first sub-section states the conservation laws on which Stirling engine models are based, and relates them to the categories in which Stirling engine models are typically classified. Models relevant to this research are then explained in further detail.

1.4.1 Conservation Laws

While Stirling engine models range in scope and complexity, they are built using a common set of tools: Conservation laws for mass, momentum, and energy, and an equation of state for the working fluid [7]. The one dimensional mathematical statements for each of these are given below for future reference [7]. For the conservation laws, both the engineering thermodynamics (Eulerian), and the flow field (Lagrangian) descriptions are given. The most complicated Stirling engine models include all three conservation laws, an equation of state, and a statement of conservation of energy for the engine walls [7]. The simplest models use only mass conservation, and an equation of state [7].

Equations (1.1a) and (1.1b) are expressions of mass conservation in Eulerian and Lagrangian reference frames, respectively.

$$\sum_{in} \dot{m} - \sum_{out} \dot{m} = \frac{dm}{dt}$$
(1.1a)

$$\frac{\partial \rho}{\partial t} + \frac{\partial}{\partial x}(\rho u) = 0 \tag{1.1b}$$

Expressions of momentum conservation are given below in Eqs. (1.2a) and (1.2b). Equation (1.2a) is the Eulerian description commonly used in engineering thermodynamics, while Eq. (1.2b) is the Lagrangian description used in fluid mechanics. Equation (1.2b) is known as the one-dimensional Navier-Stokes equation.

$$\sum_{x} F + \sum_{in} (\dot{m}u_x) - \sum_{out} (\dot{m}u_x) = \frac{\partial}{\partial t} (Mu_x)_{CV}$$
(1.2a)

$$\frac{\partial u}{\partial t} + u \frac{\partial u}{\partial x} + \frac{1}{\rho} \frac{\partial p}{\partial x} - g_x - \frac{\mu}{\rho} \frac{\partial^2 u}{\partial x^2} = 0$$
(1.2b)

The law of conservation of energy is listed below. Equation (1.3a) gives the engineering thermodynamics interpretation and Eq. (1.3b) gives the flow field description.

$$\sum_{in} \dot{m} \left(h + \frac{1}{2}u^2 + gz \right) - \sum_{out} \dot{m} \left(h + \frac{1}{2}u^2 + gz \right) + \dot{Q} - \dot{W} = \frac{\partial E}{\partial t}$$
(1.3a)

$$\frac{\partial}{\partial t} \left[\rho \left(c_v T + \frac{1}{2} u^2 \right) \right] - \dot{q} \rho = -\frac{\partial}{\partial x} \left[\rho u \left(c_v T + \frac{p}{\rho} + \frac{1}{2} u^2 \right) \right]$$
(1.3b)

Finally, Eq. (1.4) gives the ideal gas equation of state, commonly used in Stirling engine analysis.

$$pV = mRT \tag{1.4}$$

1.4.2 Classification of Models

Martini [8], and Chen and Griffin [9] classified Stirling engine modeling approaches in the early 1980s. Their distinctions are in common use today. First order models can be solved without the aid of a computer and require few details of the specific design [8]. They are semiempirical, and are typically used only to get a first-cut understanding of the capability of a proposed Stirling engine [9]. Examples include the Beale and West number correlations, and the Schmidt model derated by an empirical loss factor. Second order models begin by assuming that the losses present in real Stirling engines can be calculated individually, and algebraically added to the results of an idealized reference cycle to give the final power and efficiency [8], [9]. Common reference cycles are the ideal isothermal model, and the ideal adiabatic model [10]. Third order models begin by discretizing the engine into a series of control volumes or nodes [9]. The one dimensional conservation laws are then solved numerically, often with further simplifications [8]. This approach is more computationally expensive than the second order approach, but accounts for the interactions between loss mechanisms more faithfully [8].

Scaling using dynamic similarity has been proposed by Organ as an alternative design approach for Stirling engines [7], [11], [12]. In this method, the variables governing the Stirling

engine problem are combined into dimensionless groups using the Buckingham-Pi theorem. Use of the Buckingham-Pi theorem for Stirling engines is also demonstrated clearly by Prieto [13]. By keeping the dimensionless groups constant, it is possible to scale an engine of known performance, called the prototype, into a derivative engine of a different physical size, or working fluid [7], [11], [12]. Strict dynamic similarity requires perfect geometric similarity, i.e. all linear dimensions of the prototype are multiplied by the same factor to obtain the linear dimensions of the derivative [7], [11], [12].

1.4.3 Beale and West Number Correlations

The Beale and West number correlations are based on trends observed in performance data collected for a group of engines [6]. They are both considered first order models [8].

The Beale number was determined by plotting the power outputs of a group of engines as a function of the product of their mean cycle pressure, p_{mean} , frequency, f, and piston swept volume, V_{swp} [6]. Most of the engines chosen had heater temperatures of ~650 °C [6]. A line of best fit was established for the plot, and the slope of that line was called the Beale number [14]. The Beale number of an engine is calculated based on measured performance using

$$N_B = \frac{\dot{W}_{shaft}}{f V_{swp} p_{mean}} \tag{1.5}$$

Note that the Beale number depends on the operating point chosen. In SI units, the Beale number based on the original group of engines, is 0.15 [6]. Using this value, the potential shaft power of an engine can be roughly estimated for a given combination of frequency, piston swept volume, and mean pressure.

West suggested an additional factor for the correlation, to account for engines having different source and sink temperatures [6]. Applying this factor yields

$$N_W = N_B \frac{(T_H + T_C)}{(T_H - T_C)}$$
(1.6)

The West number, N_W , in SI units was determined to be 0.25 using the same group of engines as used for the Beale number [6].

The lowest source temperature of the engines used in either of the correlations was 340 °C. Their applicability to engines of lower source temperatures is questionable.

1.4.4 Reference Cycles

Second order modeling approaches, by definition, rely on reference cycles to determine a baseline power and efficiency, from which individually calculated losses may be subtracted. The two most commonly used reference cycles are the ideal isothermal model, and the ideal adiabatic model described by Urieli and Berchowitz [10].

1.4.4.1 Ideal Isothermal Model [10]

The ideal isothermal model considers a five-component model of the engine, as shown in Figure 1.8 below. From left to right the components are called the compression space, cooler, regenerator, heater, and expansion space. It is assumed that each component is maintained at a constant temperature during the cycle. This implies infinite heat transfer rates are possible or that speed is infinitesimal. The control volume formulations for conservation of mass and energy, and the ideal gas equation of state are applied to calculate pressure, work, heat transfer, and efficiency. The following assumptions are made [10]:

- 1 Heat exchangers and regenerator have infinite convective heat transfer coefficients and negligible flow friction.
- 2 Constant pressure spatially throughout the engine. For a given engine geometry, working fluid and operating point, pressure is a function of crank angle only.
- 3 Perfect sealing. No mass transfer across sealing surfaces.
- 4 The working fluid behaves as an ideal gas.
- 5 Engine is at cyclic steady state. Each complete cycle matches the previous one.
- 6 The kinetic and potential energies of the working fluid are negligible.
- 7 The working fluid has constant specific heats.

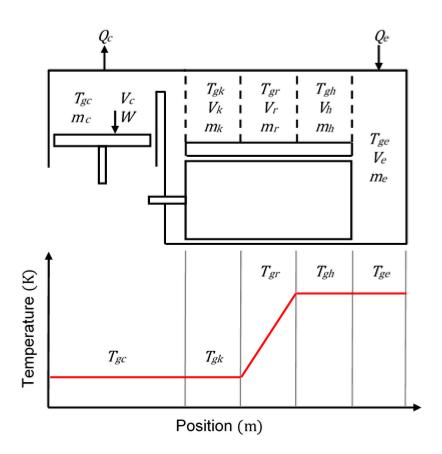


Figure 1.8: Schematic and Temperature Profile for the Ideal Isothermal Model

The following ideal gas relations for enthalpy and internal energy will be used in the derivation.

$$dh = c_p(T)dT \cong c_p dT$$
 $du = c_v(T)dT \cong c_v dT$ (1.7)

The derivation begins with a statement of mass balance.

$$M = m_c + m_k + m_r + m_h + m_e \tag{1.8}$$

Substituting the ideal gas law, Eq (1.4), and isolating the pressure yields

$$p = MR \left(\frac{V_c(\theta)}{T_{gk}} + \frac{V_k}{T_{gk}} + \frac{V_r}{T_{gr}} + \frac{V_h}{T_{gh}} + \frac{V_e(\theta)}{T_{gh}} \right)^{-1}$$
(1.9)

where $V_c(\theta)$ and $V_e(\theta)$ are the crank angle dependent volumes of the compression and expansion spaces and T_r is the regenerator mean effective temperature. Assuming a linear temperature profile in the regenerator, the regenerator mean effective temperature can be shown to be

$$T_{gr} = \frac{T_{gh} - T_{gk}}{ln\left(\frac{T_{gh}}{T_{gk}}\right)}$$
(1.10)

which takes the variation of density in the regenerator into account [10].

Since the heater, cooler, and regenerator have fixed volumes, work can only be transferred through the compression and expansion spaces. The total work is the sum of the work done in these two spaces, i.e.

$$W = W_c + W_e = \oint p dV_c(\theta) + \oint p dV_e(\theta) = \oint p \left(\frac{dV_c(\theta)}{d\theta} + \frac{dV_e(\theta)}{d\theta}\right) d\theta$$
(1.11)

To determine the heat transfer during the cycle, consider the control volume formulation of conservation of energy, Eq. (1.3a). Assuming kinetic and potential energies of the working gas are negligible, and realizing that the engine components have at most one inlet and one outlet, Eq. (1.3a) reduces to

$$\dot{m}_{in}h_{in} - \dot{m}_{out}h_{out} + \dot{Q} - \dot{W} = \frac{\partial U}{\partial t}$$

Substituting the ideal gas relations for internal energy and enthalpy, Eqs. (1.7), yields

$$\dot{m}_{in}c_{p,in}T_{g,in} - \dot{m}_{out}c_{p,out}T_{g,out} + \dot{Q} - \dot{W} = c_{v}\frac{\partial(m_{net}T_{g,CV})}{\partial t}$$

In the heat exchangers and working spaces, the temperature is constant, so

$$T_{g,in} = T_{g,out} = T_{g,CV} = T$$

$$c_{p,in} = c_{p,out}$$

and

$$c_{v}\frac{\partial(m_{net}T)}{\partial t} = c_{v}T\frac{\partial m_{net}}{\partial t} = c_{v}T\dot{m}_{net}$$

These allow further simplification of the conservation of energy equation to

$$c_p T(\dot{m}_{in} - \dot{m}_{out}) + \dot{Q} - \dot{W} = c_v T \dot{m}_{net}$$

Solving for \dot{Q} gives

$$\dot{Q} = c_v T \dot{m}_{net} - c_p T (\dot{m}_{in} - \dot{m}_{out}) + \dot{W}$$

Noting that

$$\dot{m}_{net} = \dot{m}_{in} - \dot{m}_{out} = \dot{m}$$

The equation for \dot{Q} can be written as

$$\dot{Q} = \dot{m}T(c_v - c_p) + \dot{W}$$

or

$$\dot{Q} = -\dot{m}RT + \dot{W}$$

since for an ideal gas

$$c_v - c_p = -R$$

Of interest, is the net heat transferred over a complete cycle. To calculate this, the simplified conservation of energy equation must be integrated.

$$Q = \oint \dot{Q} = -RT \oint \dot{m} + \oint \dot{W}$$

Since the engine is assumed to be at cyclic steady state, there is no net mass transfer over a complete cycle,

$$\oint \dot{m} = 0$$

and what remains is

$$Q = \oint \dot{W} = W$$

So, in the compression and expansion spaces

$$Q_c = W_c$$
 and $Q_e = W_e$

Since no work is done in the heat exchangers,

$$Q_h = Q_k = 0$$

The ideal isothermal model equation set is summarized in Table 1.1 below. Note that the efficiency for the ideal isothermal model is equal to the Carnot efficiency, because all losses have been ignored, and isothermal expansion and compression processes are reversible. Volumes unswept by the piston and displacer are commonly referred to as "dead volume" and are typically kept to a minimum when designing Stirling machine heat exchangers. Inspection of the pressure equation below reveals that if the volumes of the heat exchangers and regenerator are large relative to the swept volumes of the compression and expansion spaces, the pressure variation amplitude will be low. Also, since component volumes are divided by their corresponding temperatures, dead volume in cold components of the engine will have a greater influence than dead volume in hot components. Experiments have identified operating conditions under which an increase in dead volume leads to an increase in indicated power [12]. The ideal isothermal model is blind to this phenomenon.

$p(\theta) = MR\left(\frac{V_c(\theta)}{T_{gk}} + \frac{V_k}{T_{gk}} + \frac{V_r \ln\left(\frac{T_{gh}}{T_{gk}}\right)}{T_{gh} - T_{gk}} + \frac{V_h}{T_{gh}} + \frac{V_e(\theta)}{T_{gh}}\right)^{-1}$	Pressure
$Q_{c} = W_{c} = \oint p \frac{dV_{c}}{d\theta} d\theta$ $Q_{e} = W_{e} = \oint p \frac{dV_{e}}{d\theta} d\theta$	Heat Transferred
$W = W_c + W_e$	Work Done
$\eta = \frac{W}{Q_e} = 1 - \frac{T_{gc}}{T_{gk}}$	Efficiency

Table 1.1: Ideal Isothermal Model Equation Set [10]

For the special case of sinusoidal volume variations, the ideal isothermal model can be integrated analytically to give a closed form solution. This analysis was first performed by Gustav Schmidt in 1871 [15] and now bears his name. The volume variations differ for the three engine layouts. The Schmidt analysis multiplied by a loss factor of 0.3 to 0.4 has been used as a first order model [8].

The assumptions used in the derivation of the ideal isothermal model are unrealistic for most real Stirling engines. A direct result of the isothermal model is that all heat transfer occurs in the cylinders. If this were the case, the heat exchangers would be redundant [10]. In most Stirling machines, the cylinders are not designed for heat transfer. Cylinders typically have a low surface area to volume ratio, and expansion and compression processes are typically very short. For example, the ST05G Stirling engine expansion space has a surface area to volume ratio of 0.208 cm⁻¹, compared to 22.0 cm⁻¹ in the cooler, and at 500 RPM, the expansion process happens in 0.06 s. Thus, in most Stirling machines, adding heat exchangers is an improvement over relying on heat transfer in the cylinders. The ideal isothermal model also ignores important losses that occur in real engines; hence, alone, it gives an incomplete picture of Stirling engine operation.

1.4.4.2 Ideal Adiabatic Model [10]

The ideal adiabatic model is thought to be a more realistic reference cycle for most practical Stirling engines [10]. The same five component model is considered; however, the compression and expansion spaces are assumed to be adiabatic, so their temperatures vary with the engine pressure. The schematic and temperature profile for the ideal adiabatic model are shown in Figure 1.9. Again, the ideal gas equation of state, and the conservation laws for mass and energy are applied to produce the equation set. The result is a system of ordinary differential equations that must be solved numerically. Other than adiabatic working spaces, the ideal adiabatic model begins with the same assumptions as the ideal isothermal model.

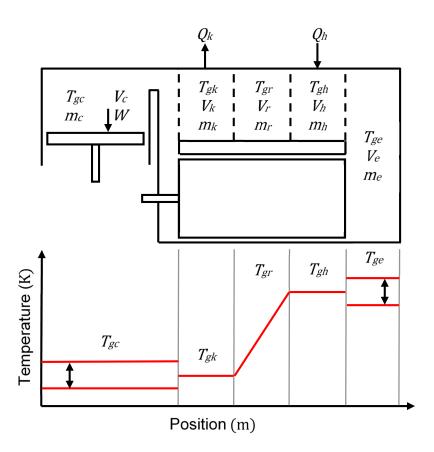


Figure 1.9: Schematic and Temperature Profile for the Ideal Adiabatic Model

First, conditional temperatures are defined for the inlets to the compression and expansion spaces.

$$T_{gck} = \begin{cases} T_{gc}(\theta) & \frac{dm_{ck}}{d\theta} > 0 \\ T_{gk} & \frac{dm_{ck}}{d\theta} \le 0 \end{cases} \qquad T_{ghe} = \begin{cases} T_{gh} & \frac{dm_{he}}{d\theta} \ge 0 \\ T_{ge}(\theta) & \frac{dm_{he}}{d\theta} < 0 \end{cases}$$
(1.12)

These temperatures depend on the direction of flow. The interface temperatures are equal to the upstream temperatures.

The derivative of the ideal gas equation of state with respect to time will also be needed. It is calculated as follows

$$\frac{\partial}{\partial t} \{ pV = mRT \}$$

$$\frac{\partial}{\partial t} \{ ln(pV) = ln(mRT) \}$$

$$\frac{\partial}{\partial t} \{ ln(p) + ln(V) = ln(m) + ln(R) + ln(T) \}$$

$$\frac{1}{p} \frac{\partial p}{\partial t} + \frac{1}{V} \frac{\partial V}{\partial t} = \frac{1}{m} \frac{\partial m}{\partial t} + \frac{1}{T} \frac{\partial T}{\partial t}$$
(1.13)

The following ideal gas relations will also be used

$$R = c_p - c_v \qquad \qquad \gamma = \frac{c_p}{c_v} \qquad \qquad c_p = \frac{R\gamma}{(\gamma - 1)} \qquad \qquad c_v = \frac{R}{(\gamma - 1)} \qquad (1.14)$$

Consider a statement of conservation of mass for the engine, as in the isothermal model.

$$M = m_c + m_k + m_r + m_h + m_e$$

This time, take the derivative of the mass equation with respect to time

$$0 = \dot{m}_c + \dot{m}_k + \dot{m}_r + \dot{m}_h + \dot{m}_e \tag{1.15}$$

For the heat exchangers and regenerator, the volumes and temperatures have been assumed to be constant. This allows simplification of Eq. (1.13) to

$$\frac{1}{p}\frac{\partial p}{\partial t} = \frac{1}{m}\frac{\partial m}{\partial t}$$
$$\frac{\partial m}{\partial t} = \dot{m} = \frac{m}{p}\frac{\partial P}{\partial t} = \frac{V}{RT}\frac{\partial p}{\partial t}$$
$$\dot{m} = \frac{V}{RT}\frac{\partial p}{\partial t}$$
(1.16)

Substituting Eq. (1.16) into Eq. (1.15) generates

$$0 = \dot{m}_c + \frac{1}{R} \frac{\partial p}{\partial t} \left(\frac{V_k}{T_{gk}} + \frac{V_r}{T_{gr}} + \frac{V_h}{T_{gh}} \right) + \dot{m}_e$$
(1.17)

Next, the conservation of energy is applied to the compression and expansion spaces. Since it is assumed that there is no heat transfer in these spaces, and they each only have one inlet/outlet, Eq. (1.3a) reduces to

$$\dot{m}c_pT - \dot{W} = c_v \frac{\partial(mT)}{\partial t}$$
(1.18)

Using the ideal gas relations and the definition of the rate of work, and simplifying, this becomes

$$\frac{dm}{d\theta} = \frac{1}{RT} \left(p \frac{dV}{d\theta} + \frac{V}{\gamma} \frac{dp}{d\theta} \right)$$
(1.19)

where the time derivatives have been changed to theta derivatives by multiplying through by $\frac{dt}{d\theta}$. Substituting Eq. (1.19) into Eq. (1.17) and rearranging provides a differential equation for pressure as a function of crank angle.

$$\frac{dp}{d\theta} = \frac{-\gamma p(\theta) \left(\frac{1}{T_{gck}} \frac{dV_c}{d\theta} + \frac{1}{T_{ghe}} \frac{dV_e}{d\theta}\right)}{\left(\frac{V_c(\theta)}{T_{gck}} + \gamma \left(\frac{V_k}{T_{gk}} + \frac{V_r}{T_{gr}} + \frac{V_h}{T_{gh}}\right) + \frac{V_e(\theta)}{T_{ghe}}\right)}$$
(1.20)

To calculate the mass accumulation and mass flow for each component, the following equations, based on conservation of mass, are used

$$\frac{dm_c}{d\theta} = -\frac{dm_{ck}}{d\theta} \tag{1.21}$$

$$\frac{dm_k}{d\theta} = \frac{dm_{ck}}{d\theta} - \frac{dm_{kr}}{d\theta}$$
(1.22)

$$\frac{dm_r}{d\theta} = \frac{dm_{kr}}{d\theta} - \frac{dm_{rh}}{d\theta}$$
(1.23)

$$\frac{dm_h}{d\theta} = \frac{dm_{rh}}{d\theta} - \frac{dm_{he}}{d\theta} \tag{1.24}$$

$$\frac{dm_e}{d\theta} = \frac{dm_{he}}{d\theta} \tag{1.25}$$

Note that mass flows towards the expansion space are considered positive.

The differential equation for the work done by the engine is

$$\frac{dW}{d\theta} = p\frac{dV_c}{d\theta} + p\frac{dV_e}{d\theta}$$
(1.26)

To calculate the heat transferred in the heat exchangers and regenerator, the conservation of energy equation is applied. Since no work is done in these spaces, and kinetic and potential energy are neglected, Eq. (1.3a) simplifies to

$$\dot{m}_{in}c_{p,in}T_{in} - \dot{m}_{out}c_{p,out}T_{out} + \dot{Q} = c_v \frac{\partial(m_{net}T)}{\partial t}$$
(1.27)

Using the ideal gas equation and realizing that the volume is constant in the heat exchangers and regenerator, the right side of the equation may be rewritten as

$$c_{v}\frac{\partial(m_{net}T)}{\partial t} = c_{v}\frac{\partial(\frac{pV}{RT}T)}{\partial t} = \frac{c_{v}}{R}\frac{\partial(pV)}{\partial t} = \frac{c_{v}}{R}\frac{\partial p}{\partial t}V + \frac{c_{v}}{R}\frac{\partial V}{\partial t}p = \frac{c_{v}}{R}\frac{\partial p}{\partial t}V$$
(1.28)

Applying Eq. (1.28) to Eq. (1.27), isolating the heat transfer variable, and writing in terms of crank angle rather than time gives the following heat transfer equations for the cooler, regenerator, and heater.

$$\frac{dQ_k}{d\theta} = c_v \frac{V_k}{R} \frac{dp}{d\theta} - c_p \left(\frac{dm_{ck}}{d\theta} T_{gck} - \frac{dm_{kr}}{d\theta} T_{gkr}\right)$$
(1.29)

$$\frac{dQ_r}{d\theta} = c_v \frac{V_r}{R} \frac{dp}{d\theta} - c_p \left(\frac{dm_{kr}}{d\theta} T_{gkr} - \frac{dm_{rh}}{d\theta} T_{grh}\right)$$
(1.30)

$$\frac{dQ_h}{d\theta} = c_v \frac{V_h}{R} \frac{dp}{d\theta} - c_p \left(\frac{dm_{rh}}{d\theta} T_{grh} - \frac{dm_{he}}{d\theta} T_{ghe}\right)$$
(1.31)

where constant specific heats have been assumed, and the time derivatives have been converted to crank angle derivatives.

Finally, since the heat exchangers and regenerator have been assumed to be isothermal

$$T_{gkr} = T_{gk} (1.32)$$

The ideal adiabatic model equation set is summarized in Table 1.2 below. It consists of six ordinary differential equations and 15 algebraic equations. Urieli and Berchowitz [10] solved the differential equations simultaneously using the fourth-order Runge-Kutta method. The Runge-Kutta method requires that the system of equations is presented as an initial value problem. The method of Urieli and Berchowitz [10], is to set the initial compression and expansion space temperatures to the cooler and heater temperatures, respectively. The equations are then solved

for several complete cycles until the values of the variables at the beginning of the cycle match those at the end of the cycle, within a specified tolerance.

While the ideal adiabatic model offers more detailed information than the ideal isothermal model and is thought to be more realistic for most Stirling engines, it still ignores losses which degrade the power and efficiency of real engines. To form a complete second-order model, these losses must be quantified individually and added to the ideal cycle results.

Table 1.2: Ideal Adiabatic Model Equation Set

$\frac{dp}{d\theta} = \frac{1}{\left(\frac{V_c(\theta)}{T_{gc}}\right)}$	Pressure			
$\frac{dm_c}{d\theta}$				
	$m_{k} = \frac{pV_{k}}{RT_{gk}} \qquad m_{r} = \frac{pV_{r}}{RT_{gr}} \qquad m_{h} = \frac{pV_{h}}{RT_{gh}}$ $m_{e} = M - (m_{c} + m_{k} + m_{h} + m_{e})$			
	$T_{gc} = \frac{pV_c}{Rm_c} \qquad T_{ge} = \frac{pV_e}{Rm_e} \qquad T_{gr} = \frac{T_{gh} - T_{gk}}{\ln\left(\frac{T_{gh}}{T_{gk}}\right)}$			
$T_{gck} = \begin{cases} T_{gc}(\theta) & \frac{dr}{dt} \\ T_{gk} & \frac{dr}{dt} \end{cases}$	Conditional Temperatures			
$\frac{dm_k}{d\theta} = \frac{m_k}{p} \frac{dp}{d\theta}$	$\frac{dm_r}{d\theta} = \frac{m_r}{p} \frac{dp}{d\theta}$	$\frac{dm_h}{d\theta} = \frac{m_h}{p} \frac{dp}{d\theta}$		
	$\frac{dm_{ck}}{d\theta} = -\frac{dm_c}{d\theta}$		Mass Accumulation and	
	$\frac{dm_{kr}}{d\theta} = \frac{dm_{ck}}{d\theta} - \frac{dm_k}{d\theta}$			
	Mass Flows			
$\frac{dQ_k}{d\theta} = c_v \frac{V}{H}$	Work and Heat			
$\frac{dQ_r}{d\theta} = c_v \frac{V}{H}$	Transfer			
$\frac{dQ_h}{d\theta} = c_v \frac{V}{H}$				

1.5 Decoupled Losses

Losses are added to the heat input rate, power output, and heat rejection rate of the reference cycle to obtain more accurate results. Martini classified losses as either heat losses, which are added to the reference cycle heat input rate, or power losses which are subtracted from the reference cycle power output [8]. Urieli and Berchowitz point out that some losses can affect both the power output and the heat transfer rates [10]. For example, flow friction impedes the motion of the displacer leading to a power loss, but it also produces heat which affects the heat input and rejection rates. Calculation of decoupled losses, and methods for adding them to the reference cycle, is typically what differentiates second order models in the literature. The following subsections introduce the loss mechanisms that are typically accounted for in second order Stirling engine models.

1.5.1 Regenerator Enthalpy Loss

An ideal regenerator will heat the working fluid to the heater temperature on the cold blow, and cool the working fluid to the cooler temperature on the hot blow [10]. Real regenerators do not achieve these temperatures. The difference between the actual enthalpy change of the working fluid as it passes through the regenerator, and the theoretical maximum enthalpy change is called the regenerator enthalpy loss. A common method of calculating this loss is using the simple heat exchanger model, which will be described in detail below.

1.5.2 Conduction Loss

Ideally, all the heat supplied to a Stirling engine passes through the working fluid and contributes to the thermodynamic cycle before being rejected to the thermal sink. In reality, a portion of this heat bypasses the thermodynamic cycle entirely, conducting through the engine walls, the displacer, or the working fluid itself. These conduction paths are typically minimized in Stirling engine design, with focus on the regenerator housing and displacer, since they have the most severe thermal gradients [3].

1.5.3 Appendix Gap Loss

It is common for displacers to have an overall length greater than their stroke, with a seal at the cold end [6], [10]. This is done to reduce the material requirements for the displacer seal [6]. The resulting annular gap that surrounds the displacer is called the appendix gap.

Heat and mass transfer occurring in the appendix gap induce losses. Second order models typically consider the appendix gap loss to be comprised of two components: shuttle loss, and pumping loss [6], [10]. Shuttle loss is the conduction of heat from the hot cylinder walls of the expansion space to the cold cylinder walls of the compression space, enhanced by the motion of the displacer [6], [8], [10]. The pumping loss is associated with the gas flow in and out of the appendix gap driven by the changing engine pressure [6], [10]. An optimum appendix gap width exists at which the sum of these loss mechanisms is minimized [6], [10], [16], [17].

1.5.4 Mechanical Friction

Mechanical friction refers to friction within the bearings and seals of the drive mechanism, defined here as the device which transmits power from the working fluid to the output shaft, and imparts motion on the displacer and piston. Two methods of quantifying mechanical friction are prominent in the Stirling engine literature. The first forms a component of the finite speed thermodynamics treatment of the Stirling cycle introduced by Petrescu et al., and contains empirical factors that are not given [18]. The second was developed by James R. Senft and considers not only the friction inherent in the mechanism, but also the amount of energy transferred through the mechanism [19]–[27]. Senft's methods will now be explained, as extensive use of them is made throughout this thesis.

When energy is transmitted through the drive mechanism, a portion of it is lost due to friction. The ratio of the energy transmitted by the mechanism, to the energy supplied to the mechanism, is termed the mechanism effectiveness, E.

$$E = \frac{\text{energy transmitted by mechanism}}{\text{energy supplied to mechanism}}$$
(1.33)

The mechanism effectiveness depends on the loads and speeds of the mechanism components, which vary with the position of the mechanism; however, for slider-crank mechanisms common in Stirling engines, the mechanism effectiveness is approximately constant [20].

The pressure on the backside of the piston will be referred to as the buffer pressure. The net force on the piston is determined by considering both the workspace pressure and the buffer space pressure. In general, there are periods of the cycle in which the net force on the piston is opposite to its direction of travel. The work done by the piston in these scenarios is called forced work. Areas of forced work for a Stirling engine cycle are highlighted in red on the indicator diagram in Figure 1.10 below. The black line represents the buffer pressure, and the blue loop represents the engine pressure. Total volume of the working space is plotted on the horizontal axis.

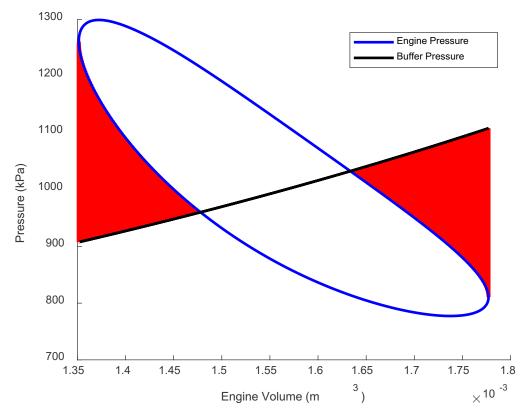


Figure 1.10: Indicator Diagram Showing Forced Work

The energy required to perform forced work comes from the flywheel. During periods of forced work, extra energy is removed from the flywheel to overcome friction in the mechanism. Similarly, the engine must supply extra energy to overcome friction while replenishing the flywheel. Areas of forced work are not directly subtracted from the engine cycle; they are subject to friction twice. The amount of forced work depends on the buffer pressure, and on the cycle shape. The negative effect of forced work depends on the mechanism effectiveness.

Assuming a constant mechanism effectiveness, E, the shaft work, W_{shaft} , is related to the indicated work, W_i , and the forced work, W_f , by Eq. (1.34) below [27].

$$W_{shaft} = EW_i - \frac{W_f}{E} + EW_f \tag{1.34}$$

Each term on the right-hand side has a clear physical significance. The first term represents the case absent of forced work, in which the indicated work is directly reduced by the mechanism effectiveness. In this case, energy flows through the mechanism in one direction only: from the engine to the flywheel. The second term describes work which is stored in the flywheel by the engine, for later use in overcoming forced work. The negative sign indicates energy removed from the engine. The third term is the energy which returns from the flywheel to perform forced work.

Nearly all Stirling engine optimization studies focus on indicated work, rather than shaft work. It is possible to have cycles with high indicated work, that will not run due to the presence of excessive forced work [27]. It is also possible to have cycles with no forced work at all. A simple way to reduce the amount of forced work for a Stirling engine is to reduce the overall volume change by reducing the piston swept volume. If an engine is optimized for maximum shaft work, some forced work will be present. The optimum amount of forced work depends on the mechanism effectiveness. Senft recommends erring on the side of less forced work, to improve the life of the mechanism [27].

1.5.5 Flow Friction

Flow friction reduces the power of real Stirling engines by resisting the flow of working fluid through the engine [8]. Prediction of this loss is difficult due to the flow conditions present in Stirling engines: Unsteady, compressible flow with sudden changes in temperature and geometry. Approaches in the literature include direct use of steady flow correlations, steady flow correlations with a quasi-steady approach, oscillating flow correlations, and computational fluid dynamics simulations. The simple model described by Urieli and Berchowitz includes a quasi-steady method for estimating the flow friction loss, and will be described in further detail below.

1.5.6 Gas Spring Hysteresis

Gas springs are sometimes found in Stirling engines, and come with inherent losses [10]. For example, in the ST05G Stirling engine, the crankcase acts as a gas spring when it is compressed and expanded by motion of the piston. At steady state, the walls of a gas spring will equilibrate at an intermediate average temperature [6]. When gas is compressed, its temperature rises, and it

gives up heat to the walls of its container. During expansion, the gas cools and heat is absorbed from the walls at a lower temperature than it was given up. In a complete cycle, there is no net heat flow between the gas and the walls, but there is a loss of work [6]. Equations for prediction of gas spring hysteresis loss derived from first principles are provided by Urieli and Berchowitz [10]; however, the assumptions used to derive them are invalid in the case of the ST05G engine. Gas spring hysteresis can be measured as the area of the gas spring indicator diagram [28].

1.5.7 Heat Transfer Hysteresis

Heat transfer hysteresis loss is the same phenomenon as gas spring hysteresis, occurring inside the working space [6]. Calculation of this loss would involve determination of finite heat transfer rates in all engine components. It is typically not included in second order models.

1.5.8 Seal Leakage

Three types of seal leakage can reduce the power output of real Stirling engines: Leakage past the displacer, leakage past the piston, and leakage to the outside. Leakage past the displacer results in a decrease in the temperature difference between the expansion and compression spaces. This reduces the displacer's ability to change the engine pressure, and results in a decrease in power. Piston seal leakage decreases the net force across the piston, reducing the work extracted, and ultimately the engine power. Leakage from inside the engine to the environment reduces the engine power by necessitating the use of an auxiliary compressor to maintain the engine fill pressure.

1.5.9 Piston Finite Speed Loss

The idea of finite piston speed loss in Stirling engines seems to have originated with Petrescu et al. [18], [29]. They refer to change in the effective pressure felt by the piston due to pressure waves generated by piston motion [29]. According to Petrescu et al., the work lost due to finite piston speed, δW_{FPS} , for an incremental volume change, dV, is given by

$$\delta W_{FPS} = p_i \left(\pm \frac{aW}{c_{FPS}} \right) dV \tag{1.35}$$

where

$$a = \sqrt{3\gamma}$$
 and $c_{FPS} = \sqrt{3RT}$ (1.36)

Here, P_i and w are the average pressure and piston speed during the incremental volume change, and c is the average speed of the gas molecules. The sign of the term in brackets is chosen so that the equation increases the work of compression and decreases the work of expansion [18].

1.5.10 Auxiliary Component Losses

A complete Stirling engine system would include auxiliary components such as a coolant pump, fuel pump, working fluid compressor, power control system, etc. These components would reduce the power output if driven by the engine. They are typically not included in academic Stirling engine research, and will not be considered here.

1.6 The Simple Heat Exchanger Model

The Simple model, described by Urieli and Berchowitz [10], [30], is a popular approach for including the flow friction and imperfect heat transfer losses of the heater, cooler, and regenerator in a second order model based on the ideal adiabatic reference cycle.

The heat transfer performance of a regenerator may be described by a parameter called the regenerator effectiveness, ε , which varies between 1, for a perfect regenerator, and 0, for no regeneration [10]. Urieli and Berchowitz define the regenerator effectiveness with reference to the ideal adiabatic model as follows [10].

$$\varepsilon \equiv \frac{\left(\begin{array}{c} \text{Actual heat transferred unidirectionally from the} \\ \text{regenerator to the working fluid in a complete cycle} \right)}{\left(\begin{array}{c} \text{Unidirectional heat transfer from the regenerator to} \\ \text{the working fluid predicted by the ideal adiabatic model} \end{array}\right)}$$
(1.37)

Nomenclature is defined below in terms of a counter flow heat exchanger analogy.

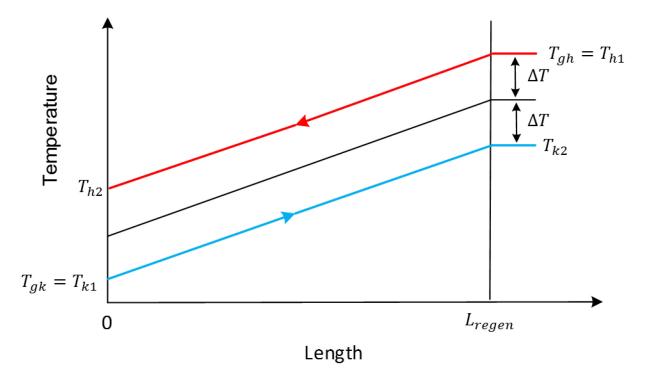


Figure 1.11: Fluid and Matrix Temperatures Defining Nomenclature for Regenerator Effectiveness, after Urieli and Berchowitz [10]

With reference to Figure 1.11, the regenerator effectiveness may also be written as

$$\varepsilon = \frac{(T_{h1} - T_{h2})}{(T_{h1} - T_{k2})} \tag{1.38}$$

Since the mass flows and heat capacities in both directions are equal over a complete cycle,

$$2\Delta T = T_{h2} - T_{k2} \tag{1.39}$$

Substituting Eq. (1.39) into Eq. (1.38) yields

$$\varepsilon = \frac{1}{1 + \frac{2\Delta T}{T_{h1} - T_{h2}}}$$
(1.40)

Now, the conservation of energy, Eq. (1.3a), is applied to the hot stream, and simplifies to

$$\dot{Q} = \dot{m}c_p(T_{h1} - T_{h2}) \tag{1.41}$$

Using Newton's Law of Cooling, \dot{Q} , can also be written as

$$\dot{Q} = 2hA_r\Delta T \tag{1.42}$$

where h is a convective heat transfer coefficient which describes the process of heat transfer from the hot stream to the regenerator matrix to the cold stream. Substitution of Eqs. (1.41) and (1.42) into Eq. (1.40) gives

$$\varepsilon = \frac{1}{1 + \frac{\dot{m}c_p}{h_{conv}A_r}} \tag{1.43}$$

or

$$\varepsilon = \frac{NTU}{1 + NTU} \tag{1.44}$$

where NTU represents the number of transfer units defined as

$$NTU = \frac{N_{St}A_r}{2A_{flow,r}} \tag{1.45}$$

The factor of two in Eq. (1.45) is added because the Stanton number, N_{St} , is typically defined for only a single gas to matrix heat transfer process rather than for two. Urieli used the following steady flow Stanton number correlation from Kays and London for mesh regenerators [10], [31].

$$N_{St} = \frac{0.46 N_{Re}^{-0.4}}{N_{Pr}} \tag{1.46}$$

Using the regenerator effectiveness, and the reference cycle result for heat transfer in the regenerator, the regenerator enthalpy loss is calculated as

$$Q_{rloss} = (1 - \varepsilon)(Q_{r,ideal,max} - Q_{r,ideal,min})$$
(1.47)

where the second factor on the right-hand side represents the unidirectional heat transfer from the regenerator to the working gas predicted by the ideal adiabatic model.

The convective heat transfers in the heater and cooler may be written as

$$Q_{k,ideal} = h_{conv,k} A_k (T_{wk} - T_{gk})$$

$$Q_{h,ideal} = h_{conv,h} A_h (T_{wh} - T_{gh})$$
(1.48)

The heater and cooler must transfer additional heat to overcome the regenerator enthalpy loss. Including this, Eqs. (1.48) become

$$(Q_{k,ideal} - Q_{rloss}) = h_{conv,k}A_k (T_{wk} - T_{gk})$$

$$(Q_{h,ideal} + Q_{rloss}) = h_{conv,h}A_h (T_{wh} - T_{gh})$$
(1.49)

Equations (1.49) can be rearranged to give the mean effective gas temperatures of the heater and cooler as

$$T_{gk} = T_{wk} - \frac{(Q_{k,ideal} - Q_{rloss})}{\overline{h_{conv,k}}A_k}$$

$$T_{gh} = T_{wh} - \frac{(Q_{h,ideal} + Q_{rloss})}{\overline{h_{conv,h}}A_h}$$
(1.50)

where the overbar indicates that the convective heat transfer coefficient is averaged spatially across the heat exchanger.

To obtain the convective heat transfer coefficients, the Blasius turbulent steady flow friction factor correlation

$$f_{Re} = 0.0791 N_{Re}^{0.75} \tag{1.51}$$

is used with Reynolds simple analogy:

$$h = \frac{f_{Re}\mu c_p}{2dN_{Pr}} \tag{1.52}$$

The simple model also includes an estimation of the power lost due to flow friction. Taking the compression space temperature as the reference point, pressure drops of the heat exchangers and regenerator are subtracted from the expansion space temperature. This leads to the following expression for the work output of the engine in one cycle [30].

$$W = W_e + W_c = \oint p \frac{dV_c}{d\theta} d\theta + \oint (p - \sum \Delta p) \frac{dV_e}{d\theta} d\theta$$
$$W = \oint p \left(\frac{dV_c}{d\theta} + \frac{dV_e}{d\theta}\right) d\theta - \oint \sum \Delta p \frac{dV_e}{d\theta} d\theta = W_{ideal} - W_{flow}$$
(1.53)

So, the total work lost per cycle due to flow friction is [30]

$$W_{flow} = \int_{0}^{2\pi} \left[(\Delta p_k + \Delta p_r + \Delta p_h) \frac{dV_e}{d\theta} \right] d\theta$$
(1.54)

The individual pressure drops for the cooler, regenerator, and heater are calculated using the following equation [30].

$$\Delta p_i = -2 \left(\frac{f_{Re} \mu V m_{flux} L}{m d^2} \right)_i \tag{1.55}$$

Reynolds friction factors for the heater and cooler are calculated using Eq. (1.51). For mesh regenerators. Eq. (1.56) below is used [31].

$$f_{Re} = 54 + 1.43 N_{Re}^{0.78} \tag{1.56}$$

The Reynolds number, N_{Re} , is calculated using the following equation.

$$N_{Re} = \frac{|\rho u|d}{\mu} \tag{1.57}$$

The factor in absolute value brackets is calculated at each crank angle increment from the results of the reference cycle calculation. The hydraulic diameter, d, is calculated as

$$d = \frac{4V_{HEX}}{A_{HEX}} \tag{1.58}$$

for slotted heat exchangers and

$$d = \frac{d_{wire} \P}{1 - \P} \tag{1.59}$$

for wire mesh regenerators [30].

Numerical solution of the simple model follows the algorithmic approach shown in Figure 1.12 below.

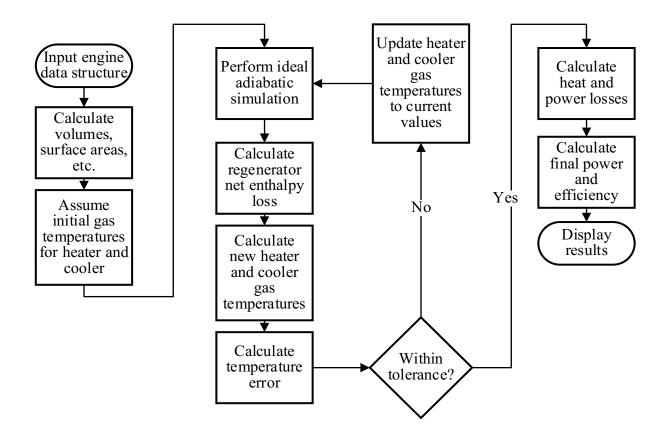


Figure 1.12: Algorithmic Approach for the Simple Model

Written in steps, the solution procedure is:

1. Set the heater and cooler wall temperatures to the thermal source and sink temperatures respectively.

- 2. Perform an ideal adiabatic simulation.
- Using the mass flow results from the ideal adiabatic simulation, calculate the average Reynolds number in the regenerator.
- Use the average Reynolds number to calculate the Stanton number in the regenerator via Eq. (1.46).
- 5. Calculate the number of transfer units in the regenerator using the Stanton number and Eq. (1.45).
- 6. Use the number of transfer units to calculate the regenerator effectiveness with Eq. (1.44).
- 7. Calculate the regenerator enthalpy loss by substituting the ideal adiabatic model results and the regenerator effectiveness from the previous step into Eq. (1.47).
- 8. Use the regenerator enthalpy loss and the convective heat transfer coefficients to calculate the mean effective gas temperatures in the heater and cooler using Eqs. (1.50).
- 9. Calculate the "temperature error" using the following formula.

$$T_{error} = \left| T_{gh,old} - T_{gh,new} \right| + \left| T_{gk,old} - T_{gk,new} \right|$$
(1.60)

where the suffixes *old* and *new* refer to the previous and current iterations of the loop.

- 10. If the temperature error is below a specified tolerance, move on to step 11; otherwise, update the heater and cooler gas temperatures to the current values and rerun the loop starting from step 2.
- 11. Once the loop has converged, calculate the work lost due to pressure drops across the heat exchangers and regenerator.
- 12. Add the losses to the reference cycle results to obtain the final power and efficiency. In the original code offered on Urieli's website, [30], the regenerator enthalpy loss was added to the heat input and the pressure drop work loss was subtracted from the power output.

1.7 Second Order Models from the Literature

The literature was surveyed with a focus on second order modeling approaches. Works using the ideal isothermal model as a reference cycle will be discussed first, followed by models derived from the principles of non-equilibrium thermodynamics. Models which use the ideal adiabatic reference cycle, as is done in the present study, will be examined in detail. Lastly, shortcomings of validation schemes in the current literature regarding second order models will be highlighted.

While the ideal isothermal model provides a first-cut understanding of the Stirling cycle, its use for detailed design is limited. Kongtragool and Wongwises, [32], studied the ideal isothermal model, and extended it by adding imperfect heat transfer from the regenerator. Regenerator pressure drop was not included. They observed that a decrease in regenerator effectiveness led to a decrease in efficiency, due to an increased heat input, but left the power output unchanged. Practical regenerators influence the engine power output in two ways. They introduce a significant pressure drop, which negatively affects the engine power. Regenerators also reduce the heat transfer requirements for the heater and cooler, often leading to a larger temperature difference between the compression and expansion spaces, which increases the power output. A more detailed model by Formosa and Despesse, [33], added conduction loss, regenerator enthalpy loss, mechanical and flow friction, and heat exchanger effectiveness. They compared their results to published performance data for the GPU-3, a well-documented beta-type Stirling engine, with good agreement. Their description left out important details such as their assumed mechanism effectiveness and flow friction correlations. These parameters can easily be adjusted to "validate" a model, especially when comparing results to only one engine. A second order model which agreed perfectly with experimental data would justifiably raise suspicion due to the assumptions involved. Ahmadi et al., [34], used an isothermal model, with regenerator and heat exchanger effectiveness added as losses, in an optimization study. While optimization is the ultimate goal of any Stirling engine model, performing it on an incomplete model can lead to a non-optimum design.

Another category of second order models are those based on ideas of non-equilibrium thermodynamics. The genre is further subdivided into finite time thermodynamics and finite speed thermodynamics. Finite time approaches consider finite heat transfer rates in the engine

components, with are evaluated as functions of time. Bert et al., [35], used a finite time approach to develop a three-component numerical model of a gamma-type engine. Nusselt numbers for each component were calculated using the Colburn equation for turbulent flow in smooth tubes, corrected using an unspecified function of the length to diameter ratio of each component. Model results were overlaid on indicated power measurements with good agreement. Ding, Chen, and Sun, [36], used an analytical scheme which combined finite time thermodynamics, and the mechanical friction ideas of Senft. They studied the influence of conduction loss, regenerator enthalpy loss, and mechanical friction on predicted power and efficiency, but did not compare their results to experimental data. Punnathanam and Kotecha, [37], and Fan et al., [38], both used finite time approaches for optimizations of overall power generation systems. Finite speed thermodynamics was applied to Stirling engine analysis by Petrescu and Costea et al. [18], [29]. The group considered pressure losses due to fluid friction, mechanical friction, and pressure waves generated by finite piston speed [29]. The fluid and mechanical friction calculations were both empirical models based on experimental data from the literature [29]. Li et al., [39], formed a second order model using the ideal isothermal reference cycle, and several losses including finite piston speed. They calculated heat transfer hysteresis loss in the working space using the gas spring hysteresis equations presented by Urieli and Berchowitz [10]. The relative influence of the losses on the energy flows through the engine are presented as calculated by the model. Experimental validation considered overall performance only. Ahmadi et al., [40], argue that the finite speed thermodynamic method is superior to the finite time method, because it considers irreversibilities internal to the engine such as flow friction and mechanical friction. They compared their model to the overall power and efficiency of the GPU-3 Stirling engine at one operating point, and displayed predicted performance trends for variable source temperature, regenerator effectiveness, swept volume ratio, piston stroke, and rotational speed. Overall, the finite time and finite speed formulations have the advantage of short computation time, making them popular for optimization studies, but their semi-empirical nature limits their wide applicability.

Several examples of second order models based on the ideal adiabatic model exist in the literature. Strauss and Dobson, [41], treated the regenerator and flow friction losses differently than in the original description by Urieli and Berchowitz [10]. While the same methods were used to calculate the magnitude of each loss, the way they were added to the reference cycle

results differed. Strauss and Dobson, [41], argue that, for real engines, the heat input rate is limited by the heat source temperature; thus, it is more realistic to add the regenerator enthalpy and conduction losses to the heat rejection rate rather than the heat input rate. The gas temperature in the cooler must increase to increase the rate of heat rejection. Strauss and Dobson, [41], only considered flow friction losses in the cooler, and these were added to the heat rejection rate only. They, [41], compared their results to Urieli and Berchowitz by applying their model to the GPU-3, and found better agreement with experimental data.

Araoz et al., [42]–[45], developed a second order model and compared it to both published GPU-3 data and to data they collected from a two-unit gamma-type engine. To the original Simple model, they added mechanical friction losses using Senft's forced work approach. They also used different heat transfer correlations for the regenerator [46].Their two-unit gamma engine performed poorly relative to the manufacturer's specifications [44]. Mechanical friction was the dominant power loss mechanism according to their simulation [44]. An earlier paper, [45], reveals that their engine is buffered from above, i.e. the buffer pressure is higher than the workspace pressure during the entire cycle. This leads to excessive forced work and degrades the mechanical efficiency of the engine significantly. They assumed a constant mechanism effectiveness of 0.8 [44], which is relatively high compared to the 0.7 recommended by Senft [27].

Babaelahi and Sayyaadi, [47], [48], extended the Simple model by adding additional losses and by rederiving the original equation set with fewer assumptions. Their 2014 publication, [47], added the effect of piston seal leakage and appendix gap shuttle loss to the differential equation set. They also calculated the mechanical friction as a decoupled loss loss using finite speed thermodynamics [47]. Their later paper, [48], considered polytropic processes in the compression and expansion spaces, and solved iteratively for the polytropic index as part of its convergence scheme. Their models were compared to published results for the GPU-3.

Hosseinzade and Sayyaadi, [49], produced a second-order model by combining the ideal adiabatic reference cycle with the finite speed formulations for mechanical friction, flow friction, and finite piston speed losses integrated into the Simple heat exchanger model. Using the GPU-3 as a case study, they plotted the pressure drop due to finite piston speed as a function of crank angle and showed that it is similar in magnitude to the regenerator pressure drop. The overall

power and efficiency of their model was compared to published data on the GPU-3 at a single operating point.

Paul, [50], [51], developed a second order model for the GPU-3 as part of his PhD thesis. His additions to the Simple model included using an iterative scheme to calculate the mass of working fluid, adding heater and cooler manifolds and the appendix gap as separate components, and adding minor losses to the flow friction calculation [50]. He suggests a rule of thumb that for Stirling engines operating at a mean pressure below 3.0 MPa and at a speed above 1500 RPM, the steady, incompressible friction factor should be multiplied by 4/3 to correct for the effects of oscillating, compressible flow. Heat transfer hysteresis and flow friction were the most influential losses for the GPU-3, according to his calculations [50]. Comparisons to the measured power and heat transfer rates over a range of operating conditions were made to validate the model.

Ni et al., [52], performed experiments on a 100 W beta-type Stirling engine using air and helium working fluids and compared the results to a second order model. The model used the ideal adiabatic reference cycle and the Simple heat exchanger approach, with the addition of heat transfer hysteresis, appendix gap, piston seal leakage, and conduction losses. They compared their calculations to overall power and efficiency data over a range of operating conditions for both the GPU-3 and their 100 W beta-type engine. Measured gas temperatures were also compared to calculated results.

Second order models have the advantages of simplicity and transparency over higher order techniques. They are composed of many separate calculations, which are often semi-empirical in nature. Most published second order model validations are done by comparison with overall power and efficiency data. This makes it difficult to diagnose errors. Ideally, the individual components of a second order model should be validated individually.

1.8 The ST05G Stirling Engine

The work presented here involves a gamma type Stirling engine, designed in 1992 by Dieter Viebach to promote Stirling engine technology for electricity production from biomass combustion [53]. Ve-Ingenieure, [53], offers a set of castings for the original ST05G design, shown in Figure 1.13. They also have a version designed for CNC machine manufacturing, called the ST05G-CNC. The full drawing package for each of these versions is available on their website [53].

Table 1.3 shows the specifications of the ST05G-CNC Stirling engine from the drawing package preamble. Figure 1.13(a) shows an image of the original ST05G Stirling engine, while Figure 1.13(b) labels the main components on a sectioned solid model.

Power Output	500 W at 8.33 Hz (500 RPM)
Maximum Engine Speed	12.5 Hz (750 RPM)
Maximum Heater Head Temperature	550 °C
Working Gas Pressure	1000 kPa
Working Gas	Dry nitrogen or oil-free compressed air
Stroke	0.075 m
Displacer Bore	0.096 m
Piston Bore	0.085 m
Main Dimensions	0.410 x 0.375 x 0.780 m
Total Weight	33.5 kg

Table 1.3 Design Data for Original ST05G Stirling Engine [53]

The engine is rated at 500 W of shaft power when spinning at 500 RPM. It features a pressurized crankcase, which facilitates fill pressures up to 1000 kPa. The heater is comprised of twenty stainless steel tubes welded to the outside of the displacer cylinder. A water jacket surrounds the cooler, connecting pipe, and power cylinder. The engine is designed to run oil-free for two reasons: To eliminate the risk of combustion of atomized oil particles in the engine which could lead to an explosion, and to prevent clogging of the regenerator.

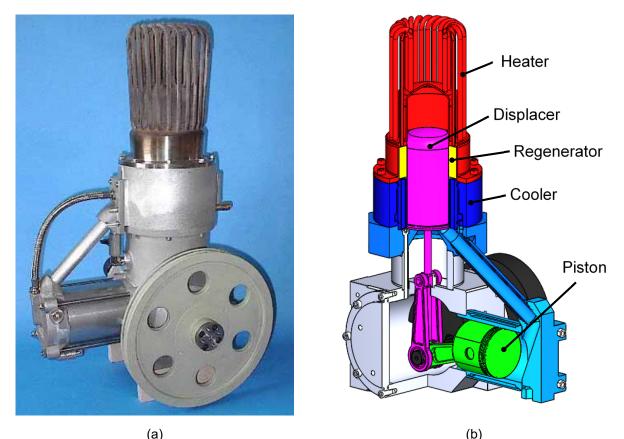


Figure 1.13: (a) Original ST05G Stirling Engine [53] (b) Sectioned Solid Model of ST05G-CNC Stirling Engine

The ST05G Stirling engine made its debut at the 1993 ISEC Stirling engine conference, [53], and since then it has been studied by both academics and Stirling engine enthusiasts. Gheith et al. contributed several publications regarding an engine similar to the ST05G. Experiments reported in their 2011 paper, [54], showed the effects of varying fill pressure, speed, coolant flow rate, and thermal source temperature. Their setup included four thermocouples on each side of the regenerator, which revealed that the average regenerator temperature was significantly higher on the power cylinder side of the engine compared to the opposite side [54]. Using the phase shift between the top and bottom thermocouples, they estimated that the axial velocity of the working fluid was twice as large on the power cylinder side, as it was on the opposite side [54]. They claimed that the difference in average pressure between the expansion and compression spaces represents the pressure drop loss of the engine, and that the difference in area between the expansion space and compression space indicator diagrams is equal to the work lost due to flow friction in a complete cycle [54]. The same group also studied the influence of the regenerator

properties on the engine performance by testing several materials and porosities [55], [56]. They recommended stainless steel with a porosity of 85 % as the best compromise between heat transfer, pressure drop, and oxidation resistance [56]. In a 2015 contribution, [57], Gheith et al. experimentally studied the effects of source temperature, fill pressure, engine speed, and coolant flow rate, with emphasis on the heater performance. The engine tested used a heater made up of 20 tubes similar to the original ST05G. Results showed that there is an optimum combination of temperature, pressure, speed, and coolant flow rate which maximizes the heat transfer rate through the heater [57]. Hachem et al., [58], compared the Stirling engine tested by Gheith et al. to an open cycle Ericsson engine, and found that the Stirling outperformed the Ericsson in specific indicated work, thermal efficiency, and exergetic efficiency. The regenerator of the Stirling engine was the reason its performance was better, and Hachem et al. point out that the Ericsson engine could achieve similar performance to the Stirling if fitted with an air preheater [58]. Another work by Hachem et al., [59], presents second order modeling results for the engine tested by Gheith et al. The model is based on the simple model of Urieli and Berchowitz [10], and includes shuttle losses and mechanical friction losses [59]. Trends predicted by the model are shown, but comparison to experimental data is minimal [59].

Bert et al., [35], [60], modeled, conducted experiments, and numerically optimized the kinematics of an engine design based on the ST05G. Their engine had a drilled-block heater head rather than the original tube cage heater [60]. Their model divided the engine into three zones and made use of the mass and energy conservation laws [35]. Only indicated power was reported for their ST05G engine [60]. Their kinematic optimization suggested discontinuous piston and displacer motion would increase power at low speed, but would decrease the maximum power at high speed relative to the original volume variations [60].

Hooshang et al., [61], [62], offer two publications concerning the ST05G Stirling engine. The first optimized a third order model of the engine for maximum power and efficiency by varying displacer stroke, frequency, and phase angle [61]. Calculations were done using helium as a working fluid [61]. The second paper reported measured crankshaft speed variations and compared them to thermodynamic and rigid body dynamic modeling results [62]. Neither paper gave a power output measurement.

Alfarawi et al., [63]–[65], analyzed the original ST05G-CNC Stirling engine through modeling and experiments. Their test rig included temperature measurements of both ends of the regenerator, the compression space, and the heater wall, pressure measurements inside the compression space, and a dynamometer for power output measurement [64]. They began by comparing their experimental results to a second order model based on the ideal adiabatic reference cycle [64]. Slider-crank volume variations, mechanical friction, appendix gap losses, and conduction losses were added to Urieli and Berchowitzs' simple heat exchanger analysis to complete their model [64]. They used Senft's forced work approach to calculate mechanical friction, and determined a constant mechanism effectiveness of 0.75 through comparison with their experimental results. They assumed a constant buffer pressure equal to the mean pressure, and their work made no mention of gas spring hysteresis loss in the crankcase. Empirical heat transfer and flow friction correlations based on steady flow experiments, [66], were used for the heat exchangers while the regenerator calculations were based on correlations specific to oscillating flow [67]. Next, they subjected the ST05G-CNC to a computational fluid dynamics simulation [63]. Their CFD results suggested that indicated power was maximized at a phase angle of 105°, and a connecting pipe internal diameter of 14 mm [63]. In their most recent paper, [65], the group performed 3D CFD calculations on mini-channel regenerators for the ST05G-CNC engine. The regenerators they simulated approached, but did not exceed, the performance of random fiber regenerators.

Table 1.4: Summary of Power	Measurements of	f Engines	Similar t	to the	ST05G-CNC	Reported in the
Literature						

Research Group	Engine Description	Maximum Indicated Power (W)	Maximum Shaft Power (W)	Operating Conditions at Maximum Shaft Power	Minimum Temperature Difference Tested (°C)
Gheith et al. [54]	Original heater head, copper wire regenerator with 90 % porosity, slightly different dimensions than the ST05G-CNC	Not reported	320	5.5 bar, Hot Source = 550 °C, Expansion Space Gas = 428.5 °C, 450 RPM	~380
Gheith et al. [55]	Same setup as above, but with a stainless-steel regenerator with 85 % porosity	Not reported	308	8 bar, Hot Source = 400 °C	275
Bert et al. [60]	Drilled block heater head, same bores and strokes as ST05G-CNC	850	Not reported	11 bar, Heater wall temperature = 700 °C, 1000 RPM, Coolant temperature = 25 °C	275
Alfarawi et al. [64]	Stock ST05G-CNC	740	470	10 bar, Hot end temperature = 650 °C, Coolant temperature = 15 °C	435

The ST05G Stirling engine has been studied by several academic groups, yet it still offers research opportunities. Pressure and temperature measurements in the crankcase have not been

performed; hence, the role of the buffer pressure has not been quantified. Experiments testing the effects of physical modifications to the ST05G-CNC Stirling engine have not been reported in the open literature. An alternative to the hot side heat exchanger would allow new heat source possibilities. Options could be expanded further by improving the engine's low temperature difference performance. Further experimental data will benefit a community of researchers currently studying the ST05G.

1.9 Low Temperature Difference Stirling Engines

Wang et al., [2], presented a recent review paper on low temperature difference Stirling engines for low grade heat recovery. They summarized experimental work done and concluded that kinematic and thermoacoustic Stirling engines had the greatest potential for low grade heat recovery applications.

Most low temperature Stirling engine prototypes use a gamma layout, and produce less than 10 W of shaft power. Pioneers of the field appear to be Ivo Kolin [68] and James R. Senft [69]. They both built small demonstration engines with power outputs in the milliwatt range. The engines of Kolin and Senft engines both used flat plate heat exchangers and operated on minimum temperature differences of 15 °C and 0.5 °C, respectively. Cinar et al., [70], investigated the effect of changing displacer material on a 3 W engine with a thermal source temperature of 160 °C. His plots demonstrate that maximum engine torque occurs at relatively low speed. He found that medium density fiberboard displacer was a superior displacer material relative to aluminum alloy due to its lower thermal conductivity and density. Kato, [71], presented indicator diagrams for a 3.34 mW gamma-type Stirling engine at thermal source temperatures of 75 - 95 °C. Results indicated that the flat plate heat exchangers performed poorly when the displacer was far away.

Larger scale low temperature difference Stirling engines have also been built and tested. Boutammachte and Knorr, [72], field-tested two solar-powered engines with 1.6 m diameter displacers that doubled as solar energy absorbers. They employed a cam mechanism to impart discontinuous motion on the displacer, and measured a performance benefit in terms of indicated work, at the expense of a more complicated mechanism and higher accelerations on the displacer. They reported a power output of 30-40 W at absorber temperatures of 50-80 °C, speeds of 30-40 RPM, and mean pressure equal to atmospheric pressure. Iwamoto et al., [73], tested a gamma-type Stirling engine with a 0.8 m displacer diameter, finned-tube heat exchangers, copper mesh regenerator, and pressurized crankcase. Their engine produced a maximum power of 146 W at 143 RPM at a gas temperature difference of 73 °C.

Kongtragool and Wongwises, [74], performed experiments on two gamma-type Stirling engines: one with two pistons and one with four. Their two and four piston engines achieved maximum power outputs of 11.8 W and 32.7 W at thermal source temperatures of 316 °C and

498 °C. They present torque and power curves as a function of speed which show similar trends to those of Cinar. Their work presents examples of engines intended for low temperature difference operation running at relatively high temperature differences.

A group led by Seth Sanders at the University of California-Berkeley, [28], [75]–[82], made significant progress towards low temperature Stirling engines for solar-thermal power generation systems. They targeted hot side temperatures in the 120 °C to 150 °C range, and built several configurations, including a crankshaft-driven gamma [78], [80], and a multi-unit free piston Stirling engine design with integrated linear alternators [28]. Der Minassians and Sanders, [28], emphasized that the cost of low temperature designs may be significantly reduced relative to high temperature designs by replacing metal parts with plastics. Their multi-unit design featured custom silicone rubber diaphragms molded in 3D-printed wax molds [77]. They used a second order modeling approach based on the ideal adiabatic model [28]. To quantify frictional losses experimentally, they performed ring-down tests on the piston and displacer [28]. These consisted of displacing the piston and displacer individually from their equilibrium positions and tracking their oscillations when released [28]. Gas spring hysteresis losses were calculated as the area of the indicator diagram measured for the gas springs [28]. Formosa et al., [82], performed experiments on a similar 3-unit free piston Stirling engine, and compared their results to an electrical network representation of the ideal isothermal model.

First order mathematical models for low temperature difference Stirling engines have been explored by Kongtragool and Wongwises [83]. They compared first order approaches for estimating the power output to experimental data from Senft's low temperature difference engines, [69], and concluded that the West number correlation was the most useful since it includes a factor that depends on the temperature difference. They obtained closest agreement when the West number was taken to be between 0.025 and 0.035.

Hoegel et al., [84], [85], modeled low temperature difference Stirling engines using a commercial third order analysis software. They compared two alpha-type Stirling engines with hot source temperatures of 750 °C and 150 °C, respectively, and identified the following differences [85]:

- The optimum phase angle for alpha engines is higher for low temperature difference engines than for high temperature difference engines. This translates to gamma and beta engines having a smaller piston swept volume relative to displacer swept volume for low temperature differences.
- 2. Low temperature difference engines run slower due to lower heat transfer rates and since flow friction has a greater influence on the total power output.
- 3. Optimum regenerator porosity is higher for low temperature difference engines.
- 4. Heat exchangers can be made identical in low temperature difference engines without reducing performance.
- 5. Heat exchangers for the low temperature engine were optimal when they had more tubes and were shorter in length than for the high temperature engine (tube diameter was fixed). This result was attributed to the following:
 - a. Flow friction influence is greater for low temperature engines, so optimum length of heat exchangers is shorter.
 - b. Heat transfer surface area is more important for low temperature engines, so the optimum number of tubes was greater.

The body of literature concerning high temperature difference Stirling engines is vast, and a substantial amount of work has also been devoted to low temperature difference designs. Relatively few works attempt to bridge the gap between the two genres, and important questions remain unaddressed: What modifications are necessary to convert a high temperature difference engine to a low temperature difference one? Are models validated at high temperature operating points still relevant at low temperature ones? Understanding the similarities and differences between these two engine categories will help solidify the Stirling engine literature, and provide insight on the design of each.

1.10 Thesis Objectives and Structure

The remainder of this thesis is divided into five chapters. Their overarching aims are to explore modifications for reduction of the minimum thermal source temperature of the ST05G-CNC Stirling engine, and to assess the validity of common second order models for analysis of low temperature difference machines.

In Chapter 2, a measurement system is developed to allow a modified ST05G-CNC Stirling engine to be evaluated experimentally. The computer controlled system includes temperature and pressure measurements at several locations on the engine, as well as torque and crankshaft position measurements. The engine is heated electrically, and cooled by a two-zone water jacket with controlled coolant flowrate and temperature. The experimental procedures, and uncertainties are stated to conclude the chapter.

The third chapter develops a second order model to predict performance of the modified ST05G-CNC engine. The model is written such that the isothermal and adiabatic reference cycles may be used interchangeably. It includes flow friction, mechanical friction, gas spring hysteresis, appendix gap loss, conduction loss, and regenerator enthalpy loss. The method of combining losses with the reference cycle results is described and sample calculations are presented to demonstrate the capabilities of the model.

Chapter 4 describes modifications made to the ST05G-CNC Stirling engine to reduce its minimum thermal source temperature. Specifically, the effects of reduced piston swept volume, increased crankcase volume, and reduced dead volume are revealed through experimentation.

In Chapter 5, the fully modified engine is compared to predictions made using the second order model developed in Chapter 3. Individual components of the model are isolated and validated against relevant experimental data as much as possible.

The final chapter presents overall conclusions, and suggests potential future work.

Chapter 2. Description of the Experimental Set-up

The following chapter provides a detailed description of the experimental set-up. It begins with a general overview of the test rig. Each subsystem is then delineated individually. Lastly, testing procedures are outlined, and experimental uncertainties are assessed.

2.1 Overview

The experimental set-up is shown in Figure 2.1 and Figure 2.2 below. A modified ST05G-CNC Stirling engine, using compressed air as a working fluid, is heated electrically and watercooled using a refrigerated bath and two peristaltic pumps. Variable loads are applied to the engine using a strap brake draped over a plastic spool. Measurements of temperature, pressure, crankshaft position, and torque are collected using a computer controlled data acquisition system.



Figure 2.1: Image of Overall Experimental Set-up

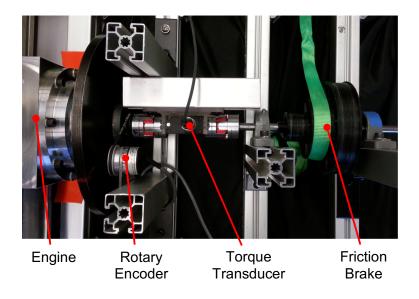
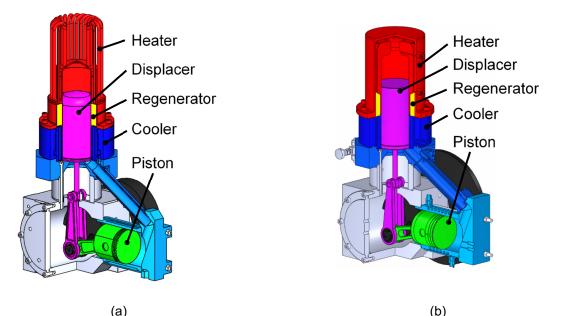


Figure 2.2: Top View of Engine Output Shaft

The test rig has several unique features which distinguish it from those of other research groups. The water jacket has been divided into two separate zones, each with their own flow rate and temperature measurements. This allows quantification of the relative influence of each zone on the overall heat rejection. The number and placement of instruments is also unique. The working fluid temperature is measured at the interfaces between the five components: compression space, cooler regenerator, heater, expansion space. The temperature and pressure of the crankcase is measured, so that the forced work and gas spring hysteresis loss can be quantified. Cold motoring tests can be performed by spinning the engine with an electric motor. Perhaps most important, the engine itself has been modified from the original ST05G-CNC design. Several modifications have been tested to determine their effects.

2.2 Modified ST05G-CNC Stirling Engine

The ST05G-CNC Stirling engine studied here was initially built with modifications to suit a solar power application. The overall solar power system was to include a Fresnel mirror solar concentrator, a thermal reservoir, a Stirling engine, and an electrical generator. The thermal reservoir was to be a solid graphite block, with a hole on one side into which the Stirling engine heater head would be inserted. The thermal reservoir was to achieve a maximum temperature of 650 °C. Figure 2.3 compares the original ST05G-CNC engine to the one built here. The drawing package for the modified design is provided in Appendix E.



(a) (b) Figure 2.3: Rendered Solid Models of (a) Original ST05G-CNC Design (b) As-Built Engine for Solar Power Application

The most significant design change is the heater head, shown in red in Figure 2.3, which has been redesigned to mate with a solid thermal reservoir. The original heater head was intended to absorb heat from gaseous combustion products, [53], and consisted of 20 stainless steel tubes welded to the displacer cylinder. Stainless steel was likely used in the original design for its corrosion resistance and creep strength - important properties in a combustion environment. The modified heater head is built of mild steel for machinability, and painted for corrosion resistance. It passes working fluid through a slotted annular gap which surrounds the displacer cylinder. Two pieces are shrink-fit together to form the heater head assembly. The inner piece was turned,

then slotted with a CNC milling machine fitted with a slitting saw. The outer piece interference fit over the inner piece, and included weld-on NPT fittings for inserting instruments. Relative to the original design, the as-built heater head has a larger internal surface area, and a smaller internal volume.

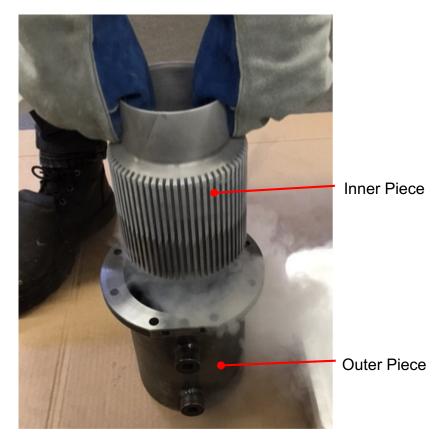


Figure 2.4: Image of Liquid Nitrogen Shrink Fit Process for Heater Head Assembly

While the basic geometry was retained, numerous minor changes were made to the engine to facilitate manufacturing, and improve sealing. These included removal of aesthetic features, consolidation of assemblies into single parts, and adjustment of static seal designs. The number of O-rings was reduced from 21 to 15 by incorporating permanent seals using silicone. All radial seal O-rings were switched to face seals to simplify assembly, and all O-rings used standard sizes. The bypass valve was brought outside the engine so that a standard valve could be used. The piston seal was changed to allow use of standard PTFE sealing rings and wear rings.

Instrumentation related changes included adding ports for working fluid pressure and temperature measurement devices. All instrument holes were made to fit 5/16"-24 straight tap

Swagelok® tube fittings, except for the heater head ports which used NPT Swagelok® tube fittings instead, since temperatures there were too high to use an O-ring seal. Sheathed thermocouples were inserted to the desired depth and swaged in place to form a seal. Outboard pressure transducers were connected to the engine volume via 1/8" stainless steel tubes swaged in place. Additional holes were added to the crankcase cover and power cylinder head for flushmount piezoelectric pressure transducers. The crankshaft was extended to facilitate connection to power measurement equipment.

Several adhesives were used during the assembly process. The three water jackets were sealed permanently using black silicone (Adhesive Sealant Black Silicone #81158, Permatex). The inlet/outlets for the power cylinder water jacket were attached using a combination of black silicone and acrylic adhesive (Scotch-WeldTM Acrylic Adhesive DP 820, 3M), because the 3M DP 820 only worked well if it stayed dry. Flange sealant (Loctite® 510TM, Henkel) was tried as a sealant for the water jackets without success. Press fit retaining compound (Loctite® 603TM, Henkel) was used for the big end bearings of the displacer connecting rods.

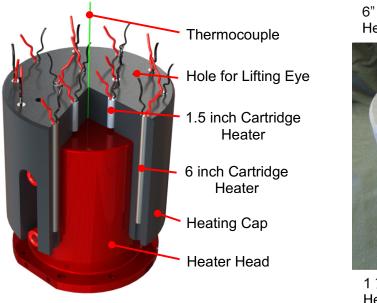
During the assembly and commissioning process, the most significant problem was the seal on the piston. The rings specified in the original ST05G-CNC design were difficult to obtain, so the piston geometry was altered to allow common pneumatic cylinder sealing rings to be substituted. The new sealing rings were made of glass reinforced PTFE, and used a nitrile O-ring backer to provide force normal to the cylinder wall. The rings were continuous, and were heated and stretched into the grooves in the piston with considerable difficulty. Once the sealing rings were fitted, inserting the piston into its cylinder was a challenge, due to the absence of a chamfer on the rim of the power cylinder bore. Ultimately, the sealing rings were too tight in the cylinder bore, and attempts to wear them in scratched the honed aluminum surface of the bore. It was determined that the sealing rings were unsuitable for the application. The author would advise against use of glass-filled PTFE in 6061 aluminum cylinders, for risk of scratching the cylinder surface. The displacer cylinder suffered a similar fate, prompting the search for alternatives. 3Dprinted nylon split rings were tested next, with disappointing results. It was decided that a 3Dprinted nylon ring would be sufficient for the displacer, but not for the piston. The final solution for the piston was a 50-durometer nitrile O-ring lubricated with PTFE grease (Magnalube-G, Saunders Enterprises Inc). While the O-ring sealed well, its durability was poor and frequent replacements were necessary during the testing campaign.

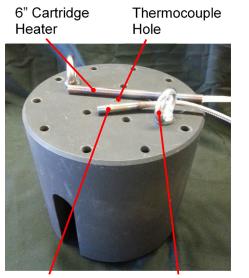
An additional sealing problem occurred during testing that proved difficult to diagnose. The displacer rod had been lightly greased during a recent reassembly, ironically, in an effort to improve its seal. The displacer rod seal is a plastic bushing press-fit into the aluminum displacer mount. The grease eventually found its way between the outside of the bushing, and its aluminum housing. The bushing slid out of the displacer mount causing the pressure between the crankcase and the working space to equalize. The crosshead on the displacer rod subsequently pushed the bushing back into place, restoring the seal. When the problem was finally pinpointed, it was remedied by removing all grease from the displacer rod, and pressing in a new bushing.

2.3 Heating System

Figure 2.5 displays the heating system used on the Stirling engine test rig. The system is comprised of a mild steel heating cap, electric cartridge heaters, power electronics, thermal insulation, and a temperature controller which receives feedback from a thermocouple mounted in the center of the cap (shown in green in Figure 2.5 (a)).

The heating cap was designed with the solar power system in mind. Its large thermal inertia was intended to simulate the graphite thermal reservoir. It has been coated with high temperature paint for corrosion resistance. Holes for the heaters are reamed only to the correct insertion depth, but are drilled all the way through. This allows the cartridge heaters to be pushed out from the bottom if necessary. A 1/16" hole in the center of the cap houses a K-type thermocouple to provide feedback for the temperature controller. Lifting eyes may be attached to the cap, as shown in Figure 2.5 (b), to facilitate removal and installation. Once assembled onto the engine, the heating cap is covered with several layers of alumina silica ceramic fiber insulation.





1 ¹/₂" Cartridge Lifting Eye Heater



In total, there are 15 cartridge heaters, with a combined power rating of 5 000 W. When tested, it was found that the system draws \sim 3 291 W of electrical power when running. The heaters are rated to withstand temperatures above 650 °C. There is an outer ring of ten 3/8" x 6" heaters and an inner ring of five 3/8" x 1.5" heaters. The leads of the cartridge heaters are insulated for temperatures up to 450 °C and are routed normal to the cap to keep them as cool as possible. The heaters receive single phase power at 208 Volts.

The power supply circuit for the cartridge heaters is housed in an electrical box mounted on the test rig cart. The box is visible in Figure 2.1. It contains fuses on each of the incoming hot wires, a solid-state relay driven by the temperature controller, and bus bars to distribute power evenly to the cartridge heaters. Power to the heaters is either on or off; there is no intermediate control. All cartridge heaters receive the same voltage, since they are all connected to the same two bus bars. Both the lid and the box itself have been grounded for safety. An emergency cutoff switch has been wired into the main power cable, so that power can be quickly shut-off without going near the electrical box itself.

A temperature controller (CN8DPT-440-C24, Omega Engineering Inc.) is used to signal the solid-state relay which supplies power to the cartridge heaters. It receives feedback from a single K-type grounded junction thermocouple (KMTSS-062G-6, Omega Engineering Inc.) mounted in the center of the heating cap as shown in Figure 2.5 (a). It uses a simple on/off control scheme. The power is turned off when the cap temperature reaches the set point. Power is restored when the cap temperature drops 2 °C below the setpoint.

Experience has shown that the cap temperature will overshoot the setpoint by roughly five degrees, even though power is removed at the setpoint temperature. It has been inferred that during the heating process, there are parts of the cap which reach temperatures above that measured by the thermocouple. When the power supply is turned off, the temperature equalizes throughout the cap, bringing the temperature of the thermocouple above the setpoint.

It is useful to know the average amount of time that the heating system is on during a test, to estimate the average heat input rate. For this purpose, the voltage signal from the temperature controller is sent to a second solid state relay, in addition to the one which switches the heater power supply. A schematic of the circuit associated with this second relay, is provided in Figure 2.6 below. When the relay is closed, the voltage from the power supply is measured by the high speed DAQ device (USB-6211, National Instruments Inc.). When the relay is open, the high speed DAQ is pulled down to ground voltage through its connection to the negative terminal of the power supply. The power supply voltage was set to 8 V, with the current set as low as possible.

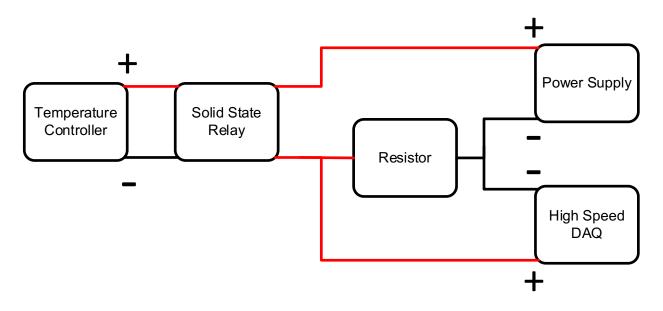


Figure 2.6: Schematic of Circuit for Heat Input Measurement System

2.4 Cooling System

The engine is cooled by a recirculating water loop. The temperature of the water is maintained by a refrigerated water bath. The engine water jackets are divided into two separate cooling zones. The flow rate through each zone is controlled by peristaltic pumps. Inlet and outlet temperatures of each zone are measured using resistance temperature detectors (RTDs). Using these measurements, the heat rejection rate may be calculated.

The water bath (12101-41, Cole-Parmer Canada Company) can heat or cool the water to maintain the setpoint. It has a cooling capacity of 900 W, which is not sufficient for heater cap temperatures above 400 °C. As a temporary solution, ice was used to maintain the water bath temperature if its cooling capacity was exceeded. The water bath has a built-in pump. This pump was used to circulate water through the engine if the peristaltic pumps were not being used.

The water jacket was divided into two separate cooling zones: The cooler, and the connecting pipe and power cylinder. The zones are shown in Figure 2.7. The cooler water jacket surrounds the internally finned tube, that contains the gaseous working fluid. The connecting pipe is double-walled, with water flowing between the inner pipe and the outer pipe. Inlet/outlets for the connecting pipe water jacket are offset to encourage water to flow in a helical pattern around the inner pipe. The power cylinder water jacket contains a large thread profile, to guide water in a helical path around the cylinder. The flow of water is from bottom to top, to aid in the removal of air bubbles when pumping begins.

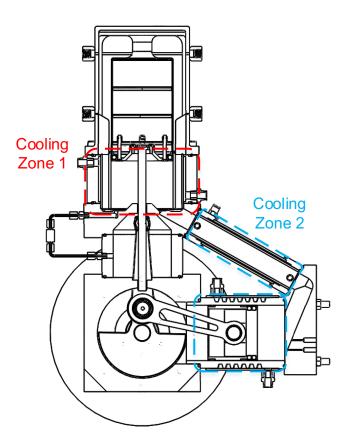


Figure 2.7: Schematic Defining the Two Cooling Zones

For preliminary tests, control of flow rate for each cooling zone was provided by acrylic flowmeters (75302113C08, King Instrument Company). The acrylic flow meters had maximum capacities of 3.5 GPM for the connecting pipe and power cylinder, and 5 GPM for the cooler. In practice, it was found that flow rates below 1 GPM were needed to obtain a measurable temperature rise across the water jackets. At these flow rates, the accuracy and consistency of the flow meters was poor.

In cases when the flow meter accuracy was insufficient, two peristaltic pumps were used (Model # 07551-20, Cole-Parmer® Masterflex® L/S® pump drives fitted with Model # 77200-62, Easy-load® II pump heads). One supplied water to the cooler, and the other supplied water to the power cylinder and connecting pipe. Both pumps were calibrated at the constant flow rates used for all tests, which were 0.800 L/min and 0.200 L/min for the cooler and connecting pipe/power cylinder, respectively. The suction line for each pump drew water from the refrigerated water bath, and water was returned to the bath after passing through the engine.

Water temperature measurements were taken at the inlet and outlet of each cooling zone using 3-wire RTDs (RTD-810, Omega Engineering Inc.), which were housed in T-fittings placed in the water hoses as close to the engine as practical. The RTD signals were conditioned using an RTD-specific data acquisition device (NI 9217 RTD, National Instruments Inc.), before reaching the data acquisition computer. Excessive noise problems during preliminary tests using grounded junction K-type thermocouples, prompted the switch to RTDs for the final version of the test rig.

2.5 Braking System

The test rig includes a braking system, used to apply various loads to the engine. Figure 2.2 shows the braking system coupled to the engine output shaft. A 3D-printed spool-shaped part is rigidly connected to the output shaft. A length of 1-inch nylon webbing passes over the spool, and rubs against it to apply a load to the engine. Weights are hung from the webbing to alter the amount of braking force. The spool also has three running surfaces, each with a different radius, which allow further load adjustment.

Initial tests were done using a bicycle disk brake to apply loads. A similar system of hanging weights was used to vary the resistance against the engine. The inconsistency of the disk brake at light loads made it unsuitable for low power testing. Light loads could not be applied without inadvertently stalling the engine.

2.6 Motoring Test System

Cold motoring tests can be performed with slight adjustments to the test rig. Figure 2.8 provides a top view of the test rig configured for a cold motoring test. An electric motor (CPM-MCVC-3441S-RLN, Teknic Inc.) is used to drive the engine crankshaft. The torque-limiting coupling protects the torque transducer from torques above 10 Nm. Torque and speed are measured by the torque transducer and rotary encoder. Cold motoring tests are safer and take less time than hot tests. They have been used to measure friction, and pressure drops across heat exchanger components.

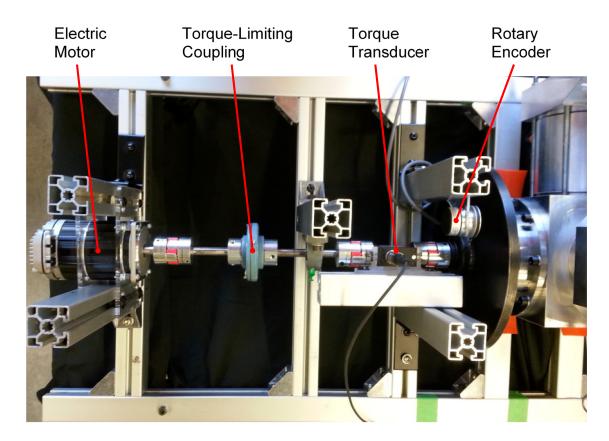


Figure 2.8: Top View of Test Rig Set-Up for Cold Motoring Tests

2.7 Instrumentation System

A block diagram of the instrumentation system is given in Figure 2.9 below. Measurements of gas temperature, gas pressure, angular position, torque, heat input rate, and heat rejection rate will be discussed in the following sub-sections. Relevant sources of error will be discussed for each.

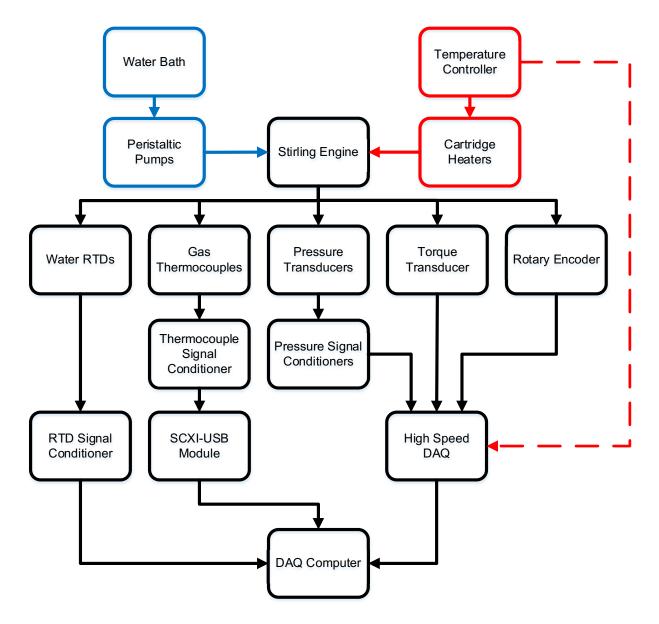


Figure 2.9: Block Diagram of Instrumentation System

2.7.1 Gas Temperature Measurement System

A total of seven gas temperature measurement locations are monitored during a typical experiment. The locations of these measurements are shown by the red stars in Figure 2.10. The temperatures of the interfaces between the five engine components are all measured. The cold side of the regenerator is measured on the right and the left side, with the aim of indicating flow asymmetry. The crankcase temperature is measured for comparison with buffer pressure calculations. The heater head may be rotated to eight different positions, to change the circumferential position of the instruments, if desired.

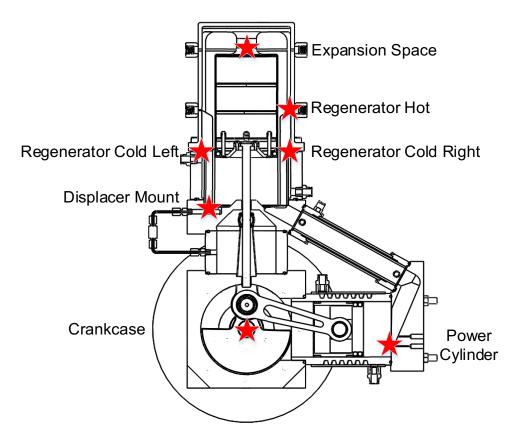


Figure 2.10: Locations of Gas Temperature Measurements

Gas temperatures were measured using exposed-junction K-type thermocouples (HKMTSS-062E-6, Omega Engineering Inc.). An example of a thermocouple used to measure gas temperature is given in Figure 2.11. The thermocouples were housed in 1/16" stainless steel sheaths. Swagelok® tube fittings sealed onto these sheaths to prevent leakage. The average junction diameter of the seven gas temperature thermocouples was measured to be 0.77 mm. Based on this, the time response of the thermocouples was estimated to be 3.6 s, and a full rotation takes 0.6 s at 100 RPM. Thus, only average gas temperatures could be used.

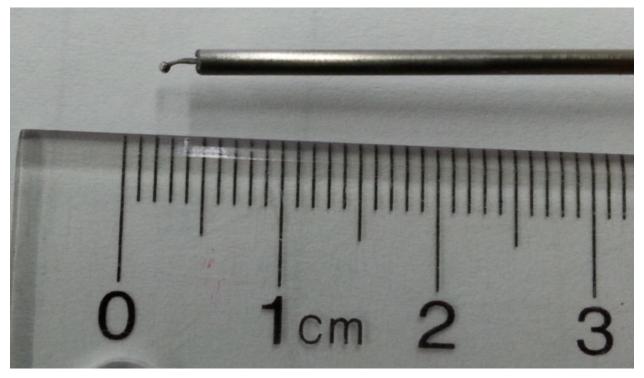


Figure 2.11: Image of Gas Thermocouple Tip

Thermocouple signals are received by a 32-channel thermocouple terminal block (TC-2095, National Instruments Inc.), passed to a DAQ chassis (SCXI-1000, National Instruments Inc.) by a thermocouple module (SCXI-1102B, National Instruments Inc.), and converted from analog to digital by a USB module (SCXI-1600, National Instruments Inc.), before reaching the DAQ computer. Gas temperature signals are typically sampled at 5 000 Hz.

Figure 2.12 is a specimen raw data set of gas temperature measurements collected while the engine was running at steady state. Regular fluctuations in gas temperature are visible in the raw data. Figure 2.13 reveals that gas temperatures vary periodically with crankshaft position. The measured amplitude and phase of these temperature swings is not expected to be accurate due to the slow response time of the thermocouples relative to the cycle frequency. All analysis here is done using gas temperatures averaged over the entire data set.

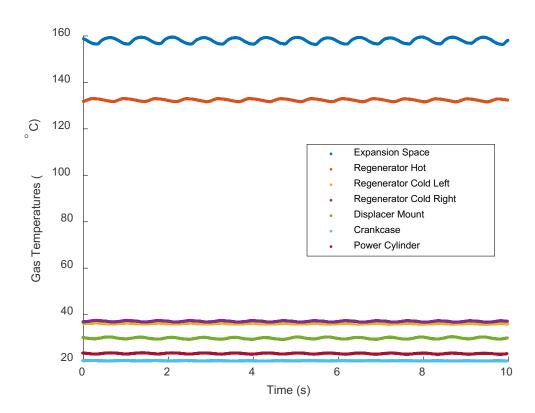


Figure 2.12: Example of Raw Data Set for Gas Temperature Measurements

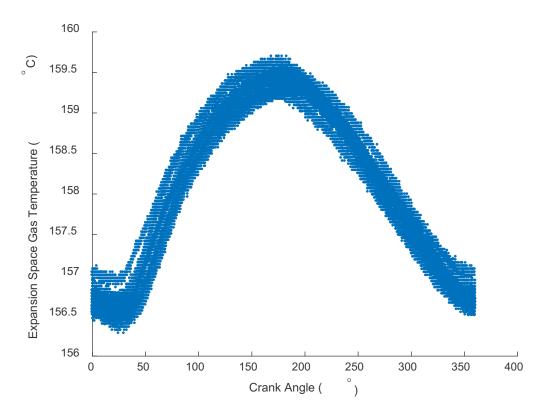


Figure 2.13: Measured Expansion Space Gas Temperature as a Function of Crank Angle

During testing, it was discovered that thermocouples would exhibit excessive electrical noise if their exposed junctions were in contact with solid parts of the engine. This was a problem for the regenerator thermocouples, which would often touch the regenerator matrix when inserted. The issue was remedied by fashioning a small wire cage to hold the regenerator material away from the thermocouple junction. Wire cages were used at the regenerator cold right and regenerator cold left thermocouple locations.

The thermocouples were calibrated by immersing them in a water bath at several different temperatures. At each temperature, a 10-second data set was taken at 5 000 Hz. The average temperature for the group of thermocouples was taken to be the "true" temperature. For each individual thermocouple, the average deviation from the true temperature was calculated. This was repeated for several temperatures. Then, a third order polynomial curve was fitted to the deviations for each individual thermocouple. Correction terms calculated by these polynomial curves were used to adjust the raw thermocouple data.

This procedure was used for all thermocouples except for those at the expansion space and regenerator hot locations. These two were omitted because they are typically measuring gas temperatures that are much higher than those reached during the calibration tests. Extrapolation of the correction term curves to these temperatures is likely to increase the error relative to taking the temperatures raw.

Figure 2.14 compares the measured temperature error before and after application of the correction terms. The marker colors in the plots identify individual thermocouples tested. The error was calculated as the difference between the measurement in question, and the overall average for that test calculated using all the thermocouples. Since the thermocouples are only being corrected relative to each other, the error shown in the plots is relative not absolute. The correction procedure improves measurements of temperature differences between thermocouples, but does not necessarily decrease the uncertainty in absolute temperature measurements.

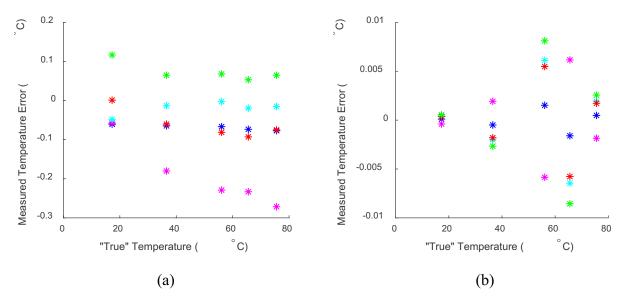


Figure 2.14: Difference between Temperature Measured by Thermocouples and Overall Average Temperature (a) Before Applying Correction Terms and (b) After Applying Correction Terms

2.7.2 Pressure Measurement System

Figure 2.15 indicates the six locations at which gas pressures may be measured. The expansion space pressure port includes a 1/8" stainless steel tube, which passes from the weld-on NPT fitting to the inlet of the expansion space. All other ports have 1/16" or 1/8" holes drilled through the engine walls. Differential measurements across the heater, cooler, and regenerator are possible using a single transducer configured as shown in Figure 2.16.

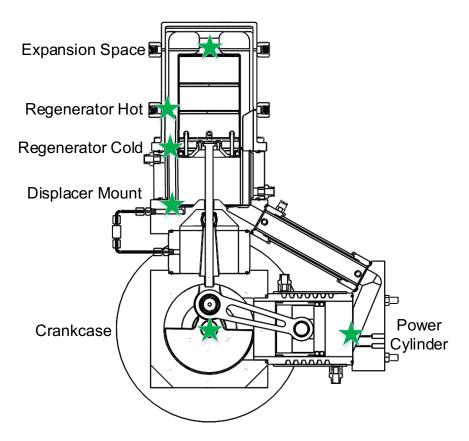


Figure 2.15: Locations of Gas Pressure Measurements

During the first round of tests, only outboard pressure transducers (DP15-50, Validyne Engineering) were used. The transducers were connected to the engine using 1/8" stainless steel tubes, which were kept as short as possible. In general, they were about 2 cm in length; however, they could be up to 12 cm if used for a differential measurement as in Figure 2.16.



Figure 2.16: Image of Tube Set-Up for Regenerator Differential Pressure Measurement

Analysis of regenerator pressure drop data, via Figure 2.17, revealed a significant problem. The figure plots data collected during a cold motoring test. Figure 2.17 (a) shows the effect of rotational speed and Figure 2.17 (b) shows the effect of fill pressure, on the measured differential pressure across the regenerator. A pressure gradient which is descending away from the crankcase appears positive in the plots. It was expected that the measured pressure curves would match each other in terms of phase, because the pressure drop is thought to be a strong function of flow velocity. Since the maximum flow velocity will occur at approximately the same crank angle for a range of speeds, the maximum pressure drop should follow. Figure 2.17 shows a significant phase difference in the regenerator pressure drop for different speeds. Losses in the holes/tubes associated with the outboard transducer system were suspected of introducing measurement lag.

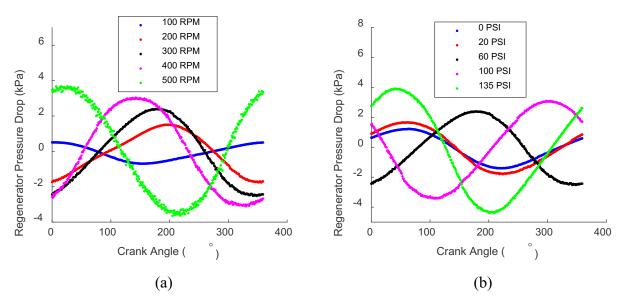


Figure 2.17: Regenerator Pressure Drop as a Function of Crank Angle for (a) Several Rotational Speeds at a Constant Fill Pressure of 414 kPa (b) Several Fill Pressures at a Constant Rotational Speed of 5 Hz

Lag in the pressure measurements could significantly skew the experimental results. To illustrate, Figure 2.18 was produced. The figure shows an experimental indicator diagram. The area inside the loop represents the work done by the engine in a single rotation of the crankshaft. The shape of the loop, when combined with the buffer pressure measurement, can be used to quantify the forced work. The black curve shows unaltered experimental data. The red and blue curves were artificially phase shifted to show the impact of pressure measurement lag. Evident from the figure, is that any phase shift in the pressure measurement will change the indicator diagram shape and area, making comparison to modeling results dubious.

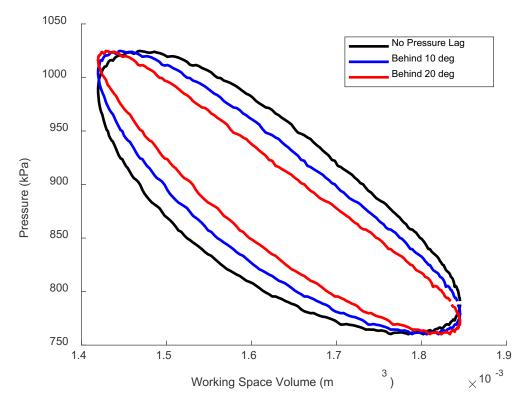


Figure 2.18: Potential Impact of Lag in Pressure Measurement on Indicator Diagram Shape

Suspicions were confirmed by performing tests with two different tube lengths, shown in Figure 2.19. The two tubes were each connected to the power cylinder measurement port and put through a series of cold motoring tests. The same transducer was used for both sets of tests. Each tube was tested at engine speeds of 100 RPM and 400 RPM, and engine pressures of 138 kPa (20 PSI) and 827 kPa (120 PSI).

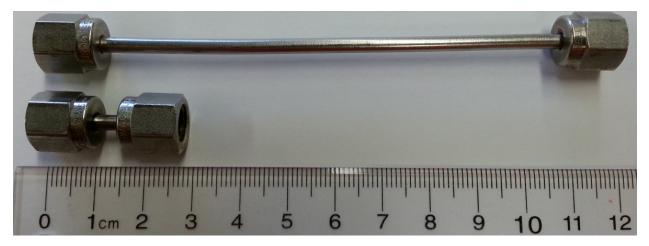


Figure 2.19: Tubes Tested to Confirm Pressure Measurement Lag

Figure 2.20 displays the results of the pressure tube test. Pressure values have been normalized to remove slight differences in fill pressure, between the two tests, from the plots. To normalize a set of data for a given speed, fill pressure, and tube length, the average of the data set was subtracted from the individual pressure samples. Inspection of the plots reveals that the tube length affects the phase lag by an amount that depends on both the speed and the pressure.

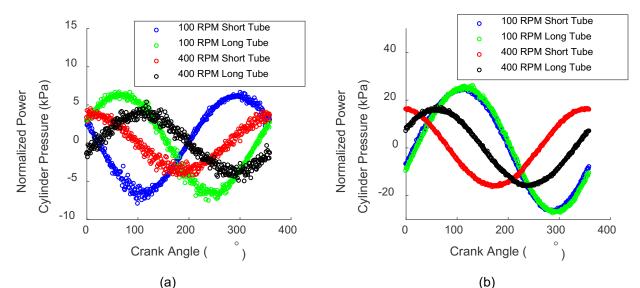


Figure 2.20: Normalized Power Cylinder Pressures for Fill Pressures of (a) 138 kPa (20 PSI) and (b) 827 kPa (120 PSI)

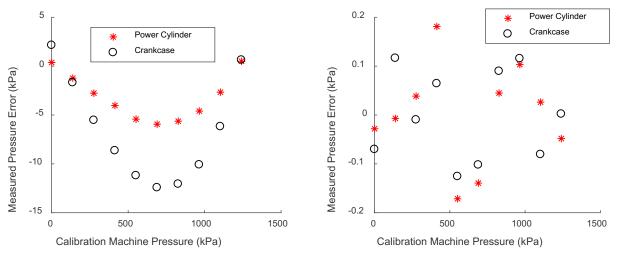
Yang et al., [86], describe a method of correcting for distortion caused by tubing in outboard transducer unsteady pressure measurements. They point out that the tubes may amplify the

pressure fluctuations, due to resonance effects, or attenuate them, due to viscous effects. Which occurs will depend on the frequency of the unsteady pressure. They also state that time-lag is introduced by using tubes, which increases the phase offset of the pressure signal for increasing frequency. The correction method that Yang et al., [86], describe, requires that a transfer function for the tube is determined experimentally, by comparison with a reference transducer mounted at the measurement location directly. Since every pressure port on the engine has a different hole and tube geometry, each would have its own unique transfer function. For many of the ports, the experiments required to determine the transfer function are not possible with the current set-up. For the power cylinder and crankcase, new pressure transducers were installed to circumvent the problem.

The new pressure transducers were mounted inside the engine, flush with the engine wall. The first transducer was mounted flush with the inside of the power cylinder head, and the second was mounted flush with the inside of the crankcase cover. Separate holes were cut to allow the new transducers to be installed alongside the old transducers, so that measurements could be compared.

The final pressure measurement system included two types of pressure transducers, their associated signal conditioners, and an analog input DAQ device. The outboard transducers (DP15-50, Validyne Engineering) could be used as single point or differential pressure measurements, depending if one or two of the transducer's ports were used. The outboard transducers also had replaceable diaphragms, which allowed the measurement range to be adjusted. For single point measurements, diaphragms rated to 1 034 kPa (150 PSI) were used. A diaphragm rated to 34.5 kPa (5 PSI) was used for differential measurements. Signals from the transducers were conditioned by a demodulator (CD280-8, Validyne Engineering), before reaching the analog input DAQ device. The flush mounted transducers (113B21, PCB Piezotronics Inc.) use the piezoelectric properties of quartz crystals to convert the pressure signal to an electrical signal. The electrical outputs pass through a signal conditioner (482C05, PCB Piezotronics Inc.) on their way to the analog input DAQ. The analog input DAQ (USB-6211, National Instruments Inc.) samples the pressure signals at cumulative rates up to 250 000 Hz. This allows resolution of the cyclic pressure variation up to the maximum rated engine speed of 12.5 Hz (750 RPM).

The outboard pressure transducers were calibrated with reference to a pressure calibration machine (DPI 603, Druck). The zero and span were adjusted on the signal conditioner for each outboard transducer individually. The transducers were then connected to the pressure calibration machine as a group, and data was collected at several static pressures. The reading on the calibration machine was taken to be the true pressure, and correction terms were determined for each transducer at each static pressure. Third order polynomial curves were fitted to the correction factors, and the equations of the curves were used to adjust the raw data. Figure 2.21 shows the reduction in measured pressure error obtained by applying the correction terms to the raw data of the outboard transducers measuring absolute pressures. Figure 2.22 presents analogous plots for the outboard transducer which measures the regenerator pressure drop.



(a)

(b)

Figure 2.21: Difference between Measured Pressure and Calibration Machine Setpoint (a) Before Applying Correction Terms and (b) After Applying Correction Terms for Outboard Transducers at the Crankcase and Power Cylinder Locations

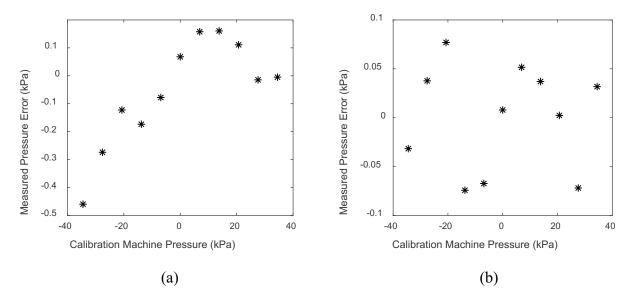


Figure 2.22: Difference between Measured Pressure and Calibration Machine Setpoint (a) Before Applying Correction Terms and (b) After Applying Correction Terms for a Single Outboard Transducer Connected between the Regenerator Hot and Regenerator Cold Locations

The flush-mount piezoelectric pressure transducers were calibrated at the factory. They are only capable of measuring dynamic pressures. When exposed to a periodic pressure, their voltage outputs will quickly center on a mean value of zero volts; hence they provide no information on the absolute pressure. Here, the outboard transducers were used to determine the absolute mean pressure, and the flush-mount transducers were used to measure the dynamic pressure. Voltages of the flush mount transducers were converted to pressures using the sensitivities provided in the factory calibration documents.

An example of raw pressure data is given in Figure 2.23. A slight difference between the two transducer types is visible. Figure 2.24 shows that the Validyne outboard transducers tend to over predict the indicated work relative to the PCB flush mount transducers.

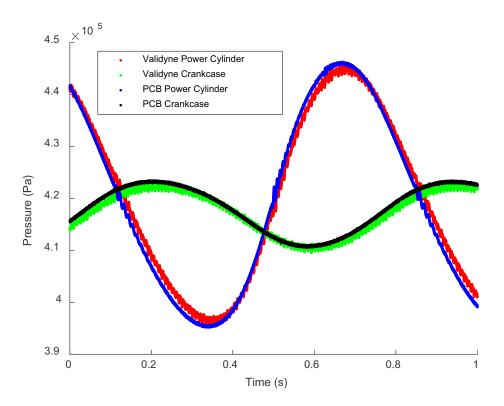


Figure 2.23: Example of Raw Data for Pressure Measurement

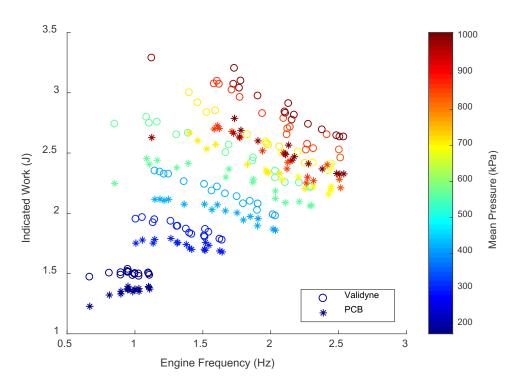


Figure 2.24: Comparison Between Validyne and PCB Pressure Transducers for Measuring Indicated Work

2.7.3 Angular Position Measurement System

The angular position of the crankshaft was measured using a 500 pulse per revolution (PPR) incremental rotary encoder (15S-19M1-0500NV1ROC-F03S1, Encoder Products Company), connected to the crankshaft with an MXL timing belt and a pair of toothed pulleys. The rotary encoder has three analog voltage outputs: A, B, and Z. The Z-output emits one PPR, and is used as a reference point. The A and B outputs each emit 500 PPR, but have a slight phase offset relative to each other. This allows rotation direction to be discerned if all three outputs are used. Since the rotation direction is always the same for this application, only the A and Z outputs were needed. The pulley on the encoder was purchased, while the pulley on the crankshaft was 3D-printed. The outer diameter and number of teeth were matched for the two pulleys.



Figure 2.25: Image of the Angular Position Measurement Set-Up

To align the angular position measurement system, the following procedure was followed. First, the crankcase cover was removed, providing a clear view of the crankshaft position. The engine was then positioned so that the working space volume was maximum (i.e. the piston was at bottom dead center). With the belt removed, the rotary encoder pulley was rotated until the Z output voltage increased to 5 V, indicating the reference point had been reached. The timing belt was then installed, and tightened by sliding the acrylic rotary encoder mount. The engine was then rotated to an arbitrary position, and returned to the position of maximum engine volume. If the Z output was confirmed to again show 5 V, calibration was complete. Otherwise, the relative position of the pulleys was re-adjusted.

The rotary encoder signals were collected using the same DAQ device used for the pressure signals (USB-6211, National Instruments Inc.). Only the A and Z-outputs were collected. An example of the raw data is presented in Figure 2.26. The post processing scheme started from the Z-pulses, and counted the A-pulses forward and backward from there. The result was that every sample had an A-output pulse count associated with it. The pulse count was converted to crank angle degrees with the knowledge that there are 500 A-output pulses per revolution, and that crank angle is defined to be zero when the engine volume is maximum, which coincides with the Z-pulse.

Since the rotary encoder was incremental, rather than absolute, it was crucial that the sampling rate was high enough so that no pulses were missed. At the maximum rated engine speed of 750 RPM, the A-output delivers 6 250 pulses/s. Voltages were generally sampled at 30 000 Hz, which gives 4.8 samples per pulse in this worst-case scenario.

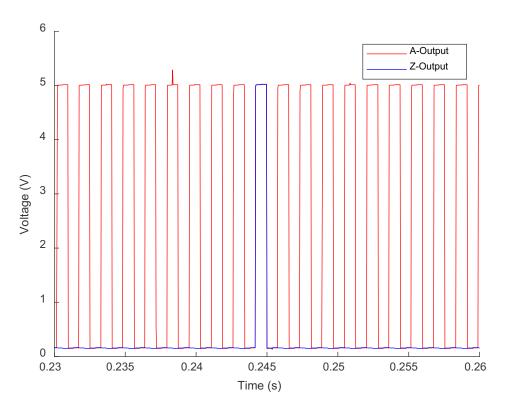


Figure 2.26: Example of Raw Data Collected from the Rotary Encoder

2.7.4 Torque Measurement System

Torque was measured using a non-contact rotary torque transducer (TRS600, FUTEK Advanced Sensor Technology, Inc.). The set-up is visible in Figure 2.2. The torque transducer was calibrated by the manufacturer. They performed a five-point calibration in both directions and included the results in the transducer shipment. A linear fit was applied to their calibration data, and the resulting equation was used to convert measured raw voltages into torques.

Figure 2.27 provides an example of raw data collected using the torque transducer, expressed as a function of crank position. The wide band of data results from plotting several engine rotations on the same axis. Periodic torque fluctuations are visible in the raw data, and their regular shape indicates a consistent load.

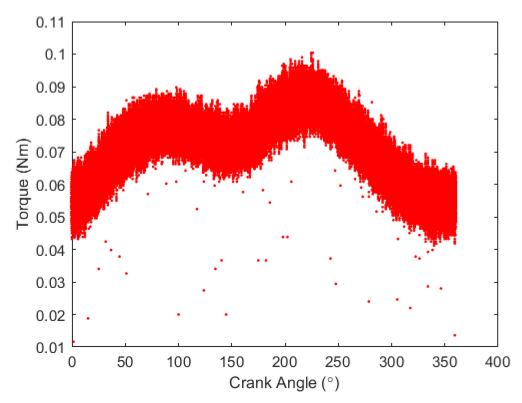


Figure 2.27: Example of Raw Data for Torque Measurement

2.7.5 Heat Input Measurement System

The heat input rate is measured by tracking the average amount of time that the heaters are on during a steady state test. This is done by logging the signal voltage emitted by the temperature controller. It was assumed that all the electrical power consumed by the heater is either absorbed by the engine or lost to the room through the insulation.

The electrical power consumed by the heating system was calculated based on the measured current and resistance of the cartridge heaters. The power consumption will vary with temperature, since the resistance of the heaters increases when the temperature increases. The test was performed at room temperature and at 60 °C, yielding power values of 3 235 W and 3 291 W, respectively. The higher value was taken as the constant power consumption of the heating system.

For tests including heat input measurements, data was collected for 30 minutes. The average heat input rate was then calculated using the following equation.

$$\dot{Q}_{in} = \begin{pmatrix} \text{Fraction of time} \\ \text{heater is on} \end{pmatrix} \begin{pmatrix} \text{Electric power consumption} \\ \text{when heater is on} \end{pmatrix}$$
(2.1)
Figure 2.28 exemplifies the heater control signal raw data. A voltage above 7 V indicates that the

heaters are switched on.

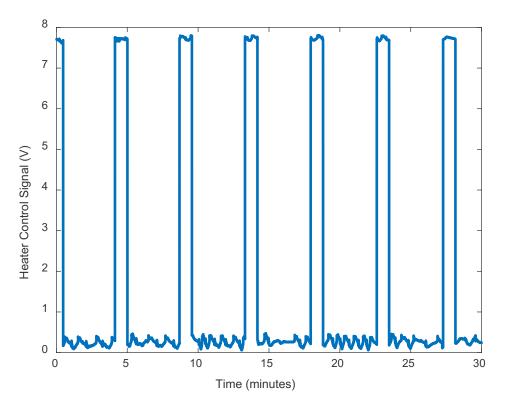


Figure 2.28: Example of Raw Data for Heater Control Signal

2.7.6 Heat Rejection Measurement System

To measure the rate of heat rejection, coolant flow rates and temperature changes were measured. The heat rejection rate was then calculated using Eq. (2.2) below.

$$\dot{Q}_{rej} = \dot{m}c\Delta T = \dot{V}\rho c\Delta T \tag{2.2}$$

The heat rejection system calibration involved calibrating the peristaltic pumps and the RTDs. The pumps were calibrated using the procedure built into the pump electronics, which involved collecting water from the pump and measuring its volume using a graduated cylinder. The RTDs were calibrated the same way as the gas temperature thermocouples. Calibration data was collected by immersing them as a group in the water bath at several temperatures. Correction terms were calculated such that the RTDs would read common temperatures at the calibration data points. By fitting third order polynomials to the calibration terms, equations were created which could be used to estimate the appropriate correction term for any desired temperature. These correction terms were applied to the raw data to decrease the uncertainty in relative temperature measurements taken between two RTDs. The effect of applying the correction terms to the raw RTD data is shown in Figure 2.29. Like the thermocouples, the correction strategy only improves the error between RTDs, and does not affect the absolute error.

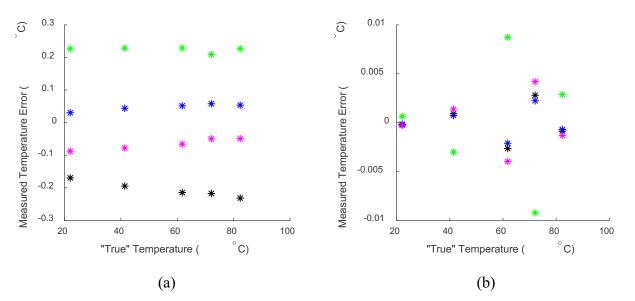


Figure 2.29: Difference between Measured Water Temperature and Overall Average Temperature (a) Before Applying Correction Terms and (b) After Applying Correction Terms

All experiments were run with water temperatures of 21 °C, which was approximately the temperature of the air in the room. This minimized the heat transferred between the outside of the engine and the surroundings during the test, which would skew the measurements.

Figure 2.30 gives measured water temperatures as a function of time for an example data set. Flow rates were adjusted to obtain a clear temperature rise across both cooling zones. Water mperatures were averaged over the data sets in the post processing routine.

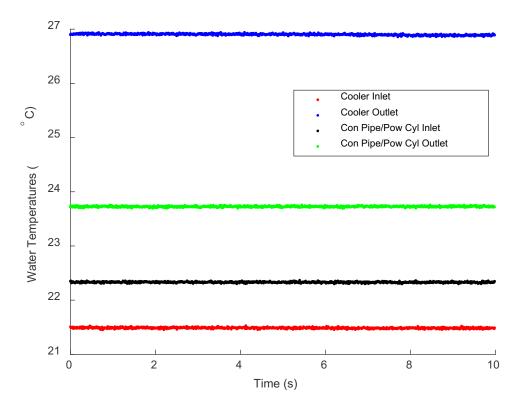


Figure 2.30: Example of Raw Water Temperatures as a Function of Time

2.7.7 Data Acquisition Software

Experimental data was recorded by an in-house DAQ software program written in LabWindowsTM CVI. A screen shot of the user interface is shown in Figure 2.31. The program features live plots of temperature, voltage, speed, torque, and power, as well as a live indicator diagram. Voltage, thermocouple, and RTD data may be sampled at different rates, and measured data is stored as text files.

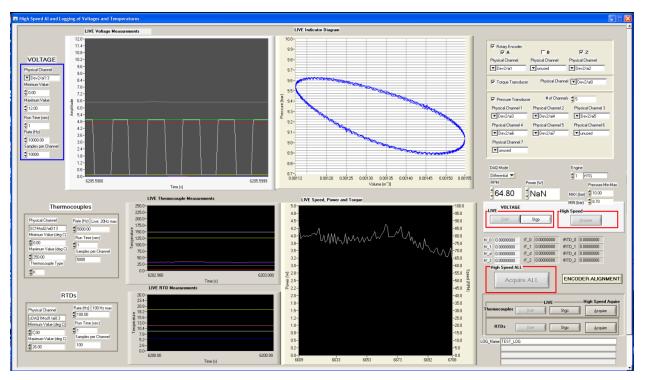


Figure 2.31: Screen Shot of Graphical User Interface for DAQ Program

2.8 Experimental Procedures

The following section lists procedures for the various tests performed with the test rig. The warm-up procedure describes how to warm-up the heating system. This is typically done with the engine stationary, to minimize wear on the seals. Procedures for general performance tests, efficiency tests, and conduction loss tests are listed next, followed by the heating system cooldown procedure. Finally, the procedure for performing a cold motoring test is described.

In general, the heating system should not be switched on until correct operation of the cooling system has been verified. Engine fill pressure changes should always be done slowly to allow the pressure inside the displacer to equilibrate. Hair should be tied back, and loose clothing should not be worn, when operating the engine.

2.8.1 Warm-Up Procedure

- 1 Check that work area is tidy and free of trip hazards.
- 2 Ensure that water bath and air compressor are plugged into separate circuits. Otherwise, they may trip the breaker.
- 3 Start the cooling system pump and check for leaks.
- 4 Start the heating system and verify correct operation at some temperature below 100 °C.
- 5 Heat engine in steps of less than 100 °C, to minimize thermal shock on the engine components.
- 6 While the engine is warming up, test the data acquisition system by collecting some sample data sets, and examining the log files.

2.8.2 Performance Testing Procedure

- 1 Set heater cap temperature and allow temperature to stabilize (this takes at least half an hour).
- 2 Use the air compressor to slowly fill the engine to the desired pressure. To avoid collapsing the displacer, all fill pressure changes should be performed at less than 2 bar per minute, according to the original ST05G-CNC drawing package from Ve-Ingenieure.
- 3 Start engine by hand while wearing a leather glove. The glove is worn to prevent the operator from scratching their hand on other test rig components when starting the engine. The engine should start very easily, with one light pull of the flywheel.

- 4 Once the engine is running, allow it to run freely until it reaches steady-state. When the engine first starts, it will rapidly consume heat stored in the heating cap. After about 10 minutes, the heating system will have cycled on and off several times, and the temperatures and engine speed should stabilize.
- 5 Collect data at various engine speeds. The engine speed is controlled using the braking system. Since both speed and torque are measured, it is not necessary to precisely control the engine speed. The engine should be allowed to reach a constant speed at each load, before the measurement is taken.
- 6 Repeat for several fill pressures, as needed.
- 7 Repeat for several heating cap temperatures, as needed.

2.8.3 Efficiency Measurement

- 1 Ensure that the water flow rate is consistent, and that the known flow rate is low enough that a measurable temperature rise exists across the engine water jackets.
- 2 Start the engine and apply a consistent load.
- 3 Allow the engine to reach steady-state.
- 4 Acquire a long data set, which includes several on/off cycles of the heating system.

2.8.4 Conduction Loss Measurement

- 1 Ensure that the water flow rate is consistent, and that the known flow rate is low enough that a measurable temperature rise exists across the engine water jackets.
- 2 Position the crankshaft at 0 $^{\circ}$ (maximum working space volume).
- 3 Collect water temperature data with the engine stationary.
- 4 Repeat for several heating system temperatures.

2.8.5 Cool-Down Procedure

- Slowly drain pressure from the engine, by loosening an instrument fitting.
 Depressurization is always done slowly to protect the displacer.
- 2 Reduce the setpoint of the water bath to 1 °C to speed up the cooling process.
- 3 Constantly supervise until the heater cap temperature is below 200 °C.
- 4 Check regularly until the heater cap temperature is below 100 °C.
- 5 Shut down water bath, temperature controller, computer, and all DAQ equipment.

2.8.6 Cold Motoring Test Procedure

- 1 Run the calibration routine for the electric motor (CPM-MCVC-3441S-RLN, Tecknic Inc.) using the Teknic ClearPath software.
- 2 Start the cooling system pump and check for leaks.
- 3 Verify correct operation of the DAQ system by taking a measurement and examining the log file.
- 4 Slowly fill engine to desired pressure.
- 5 Use motor to slowly accelerate engine to desired test speed. Allow engine temperatures to reach steady state. When driven by the motor, the engine will act as a refrigerator.
- 6 Collect data.
- 7 Repeat for several speeds, pressures, differential pressure measurements, heater head orientations, or regenerators, as needed.

2.9 Experimental Uncertainty

Sources of experimental uncertainty are discussed and summarized in this section. Appendix A contains more detailed information regarding error sources and uncertainty propagation calculations. Uncertainties in base measurements were propagated into calculated results using the procedure outlined by Wheeler and Ganji [87].

Table 2.1 outlines the estimated uncertainties for the base measurements taken using the current test rig. Uncertainties have been estimated conservatively using the manufacturer specifications. It is expected that the uncertainties will be reduced once the experimental data has been calibrated.

The most significant uncertainty is that of the torque measurements. These are of concern because the magnitude of the uncertainty is comparable to the measured result. For the torque measurement, the torque may be amplified using a gear or pulley ratio to bring it out of the noise range. This has not been done at this stage. Torque data collected to date should be viewed critically, especially in terms of absolute values.

Measurement	Instrument	Estimated Overall Uncertainty
Time	computer	0.001 s
Gas Temperatures	thermocouple (absolute measurement)	5 °C
Gas remperatures	thermocouple (relative measurement)	0.01 °C
Water Temperatures	RTD (absolute measurement)	1 °C
water remperatures	RTD (relative measurement)	0.01 °C
	outboard diaphragm pressure transducers (absolute measurement)	5 kPa
Gas Pressures	outboard diaphragm pressure transducers (differential measurement)	0.01 kPa
	flush mount piezoelectric pressure transducers	5.01 kPa
Torque	rotary torque transducer	0.05 Nm
Crank Position	incremental rotary encoder	5 °
Coolant Flow Rate	peristaltic pump	0.01 L/min
Coolant Density	N/A	5 kg/m^3
Coolant Specific Heat Capacity	N/A	5 J/kgK
Current Supplied to Heaters	multimeter	0.4 A
Resistance of Heaters	multimeter	0.1 Ω
Heating Cap Temperature	thermocouple	10 °C

Table 2.1: Estimated Overall Uncertainties for Base Measurements

Table 2.2 sums up the uncertainty propagation results for the quantities calculated here. The uncertainty in the torque measurement has led to a relatively high uncertainty in the shaft power and efficiency. The heat input rate uncertainty is also significant. It is increased by the uncertainties in the measured current and resistance of the cartridge heaters.

Calculated Quantity	Dependent Variables	Propagated Uncertainty	
Temperature Difference	gas temperatures, water	gas: 0.02 °C	
p • · · · · · · · · · · · · • · • · • ·	temperatures	water: 0.02 °C	
Engine Frequency	crank position, time	0.0087 rad/s (0.00138 Hz)	
Shaft Power	torque, engine frequency	0.25 W	
Heat Rejection Rate	coolant flow rate, coolant		
	density, coolant specific heat	2.4 W	
	capacity, water temperature	2.Τ ΨΥ	
	difference		
	current supplied to heaters,		
Heat Input Rate	resistance of heaters, fraction	49 W	
	of time heaters are on		
Efficiency	heat input rate, shaft power	0.20 %	

Table 2.2: Propagated Uncertainties for Calculated Quantities

2.10 Conclusions

A test apparatus has been assembled to study the performance of a modified ST05G-CNC Stirling engine. In addition to the engine, the set-up is comprised of heating, cooling, motoring, braking, and instrumentation systems. Relative to comparable test rigs in the literature, the one presented here has the following main differences:

- 1. The engine has been modified to suit a solid thermal source.
- 2. The cooling jacket has been separated into two zones.
- 3. Pressure and temperature measurements are taken in the crankcase, as well as in several locations in the working space.

Endeavors to improve the test system could include:

- 1. Measurements of solid surface temperatures inside the engine.
- 2. Faster time response measurements of gas temperatures.
- 3. Better control of fill pressure to make tests more repeatable.
- 4. Better resolution in the torque measurements for low torque values.

Chapter 3. Development of a Second Order Mathematical Model

Drawing from the literature, a second order mathematical model was assembled for comparison with experimental results. Israel Urieli offers an open source MATLAB code on his website [30]. His code contains the Schmidt analysis, the ideal adiabatic reference cycle, and the simple heat exchanger model, all written for alpha-type Stirling engines. Here, the code has been rewritten and extended to include slider crank volume variations for gamma engines, interchangability of the isothermal and adiabatic reference cycles, additional loss mechanisms, and features to allow virtual parameteric studies. The following chapter details these changes and presents sample calculations to show the capabilities of the model.

3.1 Calculation of Constant Volumes

The calculation of constant volumes was performed using the CAD models. Specifically, the intersect, and mass properties tools in Solidworks® were used. The CAD representation of the engine internal volume is the light blue object in Figure 3.1. The displacer and its drive rod appear in pink. The volumes of the displacer, displacer drive rod, and regenerator material are subtracted from the total engine internal volume. The volume of the power cylinder changes depending on the position of the piston. Figure 3.1 shows the minimum power cylinder volume case.

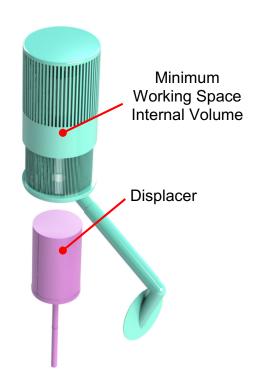


Figure 3.1: CAD Model of Engine Internal Volume and Displacer

The validity of the calculation relies on close agreement between the CAD model and the real engine, and on the accuracy of the calculation in the software. Measurements confirmed that the CAD model and real engine are a close dimensional match. Volumes calculated by the software were also measured by displacing water, and good agreement was found. This measurement was done on the dead volume reduction parts which are described in Chapter 4. The measured volume was 132 mL and the calculated volume was 131 mL.

The regenerator volume was estimated by subtracting the volume of the regenerator material from the total volume of the regenerator cavity. Information used in the regenerator volume calculation is displayed in Table 3.1 below.

Measured Mass of Regenerator Material	302.7 g
Density of 316 Stainless Steel [88]	8 g/mL
Calculated Volume of Regenerator Material	37.8 mL
Calculated Volume of Regenerator Cavity	354 mL
Calculated Regenerator Porosity	89.3 %

Table 3.1: Information Associated with Calculation of the Regenerator Volume

The volumes and surface areas of the heater and cooler were calculated in the model based on the slot dimensions and number of slots of each. These volumes were both treated as isothermal by the model. For the heater, the slot length in the model was adjusted so that the total volume calculated by the model matched the true heater volume. The resulting heater slot length was longer than the true slot length to include the volume of the disk-shaped volume at the top of the heater, and the bell-mouth entrance of the displacer cylinder. The true cooler slot geometry was input as is.

3.2 Calculation of Volume Variations

Motion of the piston and displacer leads to volume variations in the compression and expansion spaces. A mathematical description of these is required as an input to the both the ideal isothermal and the ideal adiabatic reference cycle models. The aim is to express the volumes of the compression space and expansion space as a function of crank angle, defined as zero when the working space volume is maximum. The volume of the displacer rod has been neglected in the volume variation calculations.

Cleghorn and Dechev, [89], present volume variations based on the kinematics of the slider crank mechanism. Figure 3.2 defines nomenclature for a generic slider-crank mechanism.

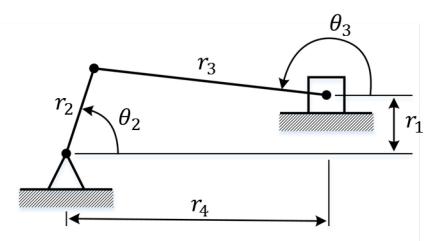


Figure 3.2: Schematic of Generic Slider-Crank Mechanism (after Cleghorn and Dechev [89])

It can be shown, [89], that for the slider-crank mechanism defined above

$$r_4 = r_2 \cos \theta_2 - r_3 \cos \theta_3 \tag{3.1}$$

where

$$\theta_3 = 180^{\circ} - \sin^{-1}\left(\frac{-r_1 + r_2 \sin \theta_2}{r_3}\right)$$
(3.2)

The piston and displacer are both driven by slider-crank mechanisms in the engine studied here. They share a crank, and the axes of their respective cylinders form an angle, β . Use of Eqs. (3.1) and (3.2) above requires careful consideration of this angle. The difference between θ_2 ,

defined above, and the crank angle, θ , measured clockwise from the point at which the workspace volume is maximum must also be understood. The real mechanism can be represented by the pair of slider-crank mechanisms shown in Figure 3.3 below. Variables with the prefix "D" are associated with the displacer and variables with the prefix "P" are associated with the piston.

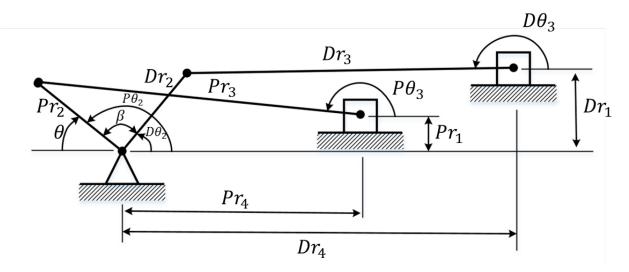


Figure 3.3: Slider-Crank Mechanism Pair Equivalent to Modified ST05G-CNC Drive Mechanism

By applying Eqs. (3.1) and (3.2) to the mechanism shown in Figure 3.3, and using geometry, the equation set shown in Table 3.2 was derived for gamma-type engines using slider-crank drive mechanisms. These equations were programmed into the thermodynamic models, and were used to convert measured crank angles into volumes when post-processing experimental data.

Table 3.2: Gamma-Type	Slider-Crank Volume	Variation Ec	uation Set

$P\theta_2 = 180^{\circ} - \theta$	$D\theta_2 = P\theta_2 - \beta$		
$Dr_{4,max} = \sqrt{(Dr_2 + Dr_3)^2 - Dr_1^2}$			
$Dr_{4,min} = \sqrt{(Dr_3 - Dr_2)^2 - Dr_1^2}$	$Pr_{4,max} = \sqrt{(Pr_2 + Pr_3)^2 - Pr_1^2}$		
$D\theta_3 = 180^{\circ} - \sin^{-1}\left(\frac{-Dr_1 + Dr_2\sin D\theta_2}{Dr_3}\right)$			
$P\theta_3 = 180^{\circ} - sin^{-1} \left(\frac{-Pr_1 + Pr_2 sin P\theta_2}{Pr_3}\right)$			
$Dr_4 = Dr_2 cos D\theta_2 - Dr_3 cos D\theta_3$			
$Pr_4 = Pr_2 cos P\theta_2 - Pr_3 cos P\theta_3$			
$DV_{c} = \frac{\pi}{4} d_{disp}^{2} (Dr_{4,max} - Dr_{4,min}) - V_{e}$	$PV_c = \frac{\pi}{4} d_{pist}^2 (Pr_{4,max} - Pr_4)$		
$V_e = \frac{\pi}{4} d_{disp}^2 (Dr_{4,max} - Dr_4)$	$V_c = DV_c + PV_c$		

These equations were programmed into the thermodynamic models, and were used to convert measured crank angles to volumes when post-processing experimental data.

For the ideal adiabatic model, the derivatives of the volume variations were also needed. These were evaluated, and the results are given in Table 3.3 and Table 3.4 below.

$\frac{\partial D\theta_3}{\partial D\theta_3} = \frac{\frac{Dr_2}{Dr_3}cosD\theta_2}{\frac{D}{Dr_3}cosD\theta_2}$
$\frac{\partial \theta}{\sqrt{1 - \left(\frac{-Dr_1 + Dr_2 sin D\theta_2}{Dr_3}\right)^2}}$
$\frac{\partial Dr_4}{\partial \theta} = Dr_2 \sin D\theta_2 + Dr_3 \sin D\theta_3 \frac{\partial D\theta_3}{\partial \theta}$
$\frac{\partial V_e}{\partial \theta} = -\frac{\pi}{4} d_{disp}^2 \frac{\partial Dr_4}{\partial \theta}$

Table 3.4: Compression Space Volume Variation Derivative Equation Set

$\frac{\partial P\theta_{3}}{\partial \theta} = \frac{\frac{Pr_{2}}{Pr_{3}}cosP\theta_{2}}{\sqrt{1 - \left(\frac{-Pr_{1} + Pr_{2}sinP\theta_{2}}{Pr_{3}}\right)^{2}}}$
$\frac{\partial Pr_4}{\partial \theta} = Pr_2 \sin P\theta_2 + Pr_3 \sin P\theta_3 \frac{\partial P\theta_3}{\partial \theta}$
$\frac{\partial PV_c}{\partial \theta} = -\frac{\pi}{4} d_{pist}^2 \frac{\partial Pr_4}{\partial \theta}$
$\frac{\partial DV_c}{\partial \theta} = -\frac{\partial V_e}{\partial \theta}$
$\frac{\partial V_c}{\partial \theta} = \frac{\partial P V_c}{\partial \theta} + \frac{\partial D V_c}{\partial \theta}$

For buffer-pressure calculations, the volume variation equation of the buffer space was also required. This equation is given below.

$$V_b = V_{b,max} - PV_c \tag{3.3}$$

Application of the volume variation equations presented above to the engine used in this research reveals that the piston and displacer motion is nearly sinusoidal. This is shown graphically in Figure 3.4 below.

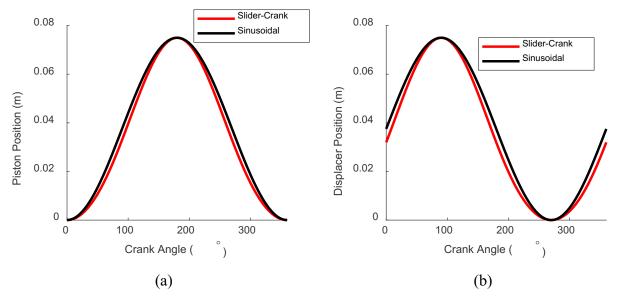


Figure 3.4: Comparison Between Sinusoidal Motion and Slider-Crank Mechanism Motion for (a) the Piston and (b) the Displacer

3.3 Calculation of Working Fluid Mass

Both the adiabatic and isothermal models take the total mass of working fluid as an input parameter. Since this is difficult to measure in the lab, it is instead calculated using the fill pressure, temperature, and engine volume. Using this approach, the calculated mass depends on the crank position, since the engine volume is crank angle dependent.

Urieli, [30], calculated the working fluid mass using the Schmidt analysis in his original code. If this mass is used as an input for a reference cycle simulation that does not have sinusoidal volume variations, the resulting mean cycle pressure will differ from that used to calculate the mass in the first place.

Paul, [50], provides an iterative method for adjusting the working fluid mass. Following Paul, the method used here begins by calculating an initial mass of working fluid using the Schmidt analysis equation and the desired mean engine pressure. Specifically, the gamma Schmidt analysis formulation given by Senft, [27], is evaluated at each crank angle degree and the average is taken to be the initial working fluid mass. This mass is then used as an input to the reference cycle model (isothermal, adiabatic, or simple), to obtain pressure as a function of crank angle. The average of this pressure is calculated and compared to the desired pressure. If the difference exceeds 0.1 %, the mass is adjusted according to Paul's formula, which reads

$$m_{new} = \left(1 + \frac{p_{mean,desired} - \bar{p}}{p_{mean,desired}}\right) m_{old}$$
(3.4)

where \bar{p} is the average engine pressure calculated from the reference cycle simulation results. The process is iterative, and typically converges in less than five iterations.

As an example, the as-built engine was simulated using the full second order model detailed in this chapter. The working fluid mass was reduced by 2.34 % using Paul's algorithm, to obtain the correct mean pressure from the simple model reference cycle. The reduced mass led to a shaft power reduction of 14.9 %.

Thus, calculation of the mass of working fluid is an important detail of any Stirling engine model and should be given consideration when comparing model performance. Ahmadi et al., [90], offer a review paper in which they compare several second order models in terms of their prediction of the performance of the GPU-3. The mass calculation procedure of each model was not investigated, and differences may have skewed the results.

3.4 Ideal/Reference Cycle

The model is written to allow reference cycles to be interchanged. For the ideal adiabatic model, the engine was comprised of five components as defined in Table 3.5 below. If the isothermal model was being used, the adiabatic components shown below were instead assumed to be isothermal.

Engine Component	Assumption	Description
Compression Space	Adiabatic	Includes piston swept volume, piston clearance volume, cylinder head, connecting pipe, displacer swept volume (on cold side of displacer), and displacer cold side clearance volume.
Cooler	Isothermal	Includes the annular slotted heat exchanger only.
Regenerator	Isothermal (Linear temperature profile)	Starts at the top of the cooler fins and ends at the bottom of the heater fins. The volume of the stainless-steel wool is subtracted from the volume of the empty cavity.
Heater	Isothermal	Includes annular slots, disk-shaped volume at the top of the heater head, and the bell-mouth entrance to the expansion space. The length of the slots was adjusted in the model to obtain the correct overall volume.
Expansion Space	Adiabatic	Includes the swept volume of the displacer (hot side) and the hot side displacer clearance volume.

 Table 3.5: Definition of Isothermal and Adiabatic Engine Components

Results from the isothermal and adiabatic reference cycles are shown as functions of heater gas temperature in Figure 3.5. The mean pressure and cooler gas temperature, were held constant at 1000 kPa and 21 °C, respectively, to produce the plots.

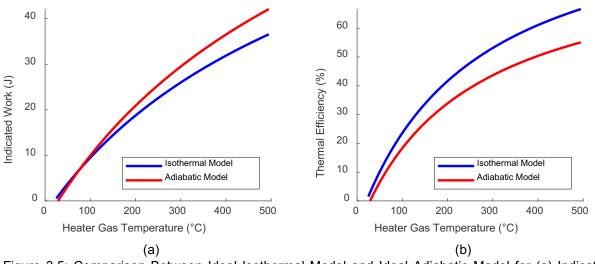


Figure 3.5: Comparison Between Ideal Isothermal Model and Ideal Adiabatic Model for (a) Indicated Work and (b) Thermal Efficiency as Functions of Heater Gas Temperature

The plots show that, at low heater gas temperatures, the two reference cycle models give similar predictions for indicated work and thermal efficiency. As the heater gas temperature increases, the ideal adiabatic model forecasts a higher indicated work and a lower thermal efficiency than the ideal isothermal model.

The temperature swings in the compression and expansion spaces of the adiabatic model lead to higher pressure swings, than in the isothermal model [10]. These pressure swings are illustrated in Figure 3.6, which gives indicator diagrams calculated by both methods, at heater gas temperatures of 500 $^{\circ}$ C and 50 $^{\circ}$ C.

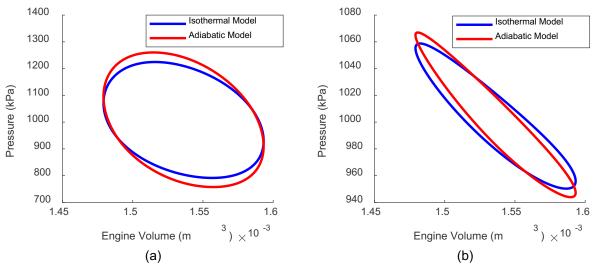


Figure 3.6: Ideal Isothermal and Adiabatic Model Indicator Diagrams for Heater Gas Temperatures of (a) 500 °C and (b) 50 °C

The lower efficiency of the ideal adiabatic model results from the mean temperatures of the expansion and compression space being below and above the heater and cooler temperatures, respectively [6], [10]. For example, gas in the adiabatic compression space, which is initially at the cooler temperature, will rise in temperature as it is compressed and make the effective temperature of the compression space higher than the cooler temperature [6].

3.5 Decoupled Loss Calculations

3.5.1 Regenerator Enthalpy Loss

The regenerator enthalpy loss was calculated following Urieli's, [30], procedure for the simple heat exchanger model exactly as described in Chapter 1. The simplified approach does not consider the properties or temperature changes of the regenerator material. It also uses steady flow heat transfer correlations.

The hydraulic diameter of the regenerator was calculated based on the porosity, \P , and the wire diameter, d_{wire} , using [30].

$$d_r = d_{wire} \left(\frac{\P}{1 - \P}\right) \tag{3.5}$$

Figure 3.7 shows regenerator enthalpy loss dependence on these two parameters as calculated using the simple heat exchanger model. According to the figure, regenerator enthalpy loss is minimized for small wire diameter, high porosity regenerator matrices. Both parameters are involved in the hydraulic diameter calculation for the regenerator matrix, Eq. (1.59), which is one reason they affect the enthalpy loss. They also affect the loss by influencing the mass flux through the regenerator, shown in absolute value brackets in Eq. (1.57). The wire diameter and porosity of the regenerator matrix used in experiments here were 0.0508 mm, and 89 %, respectively.

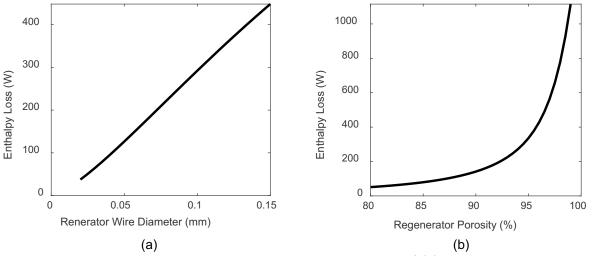


Figure 3.7: Variation in Regenerator Enthalpy Loss as a Function of (a) Regenerator Wire Diameter and (b) Regenerator Porosity

3.5.2 Conduction Loss

A one-dimensional Fourier's Law approach was used to estimate the conduction loss. A linear temperature profile in the heat flow direction and constant thermal conductivity were assumed. Radiation and convection were assumed to be negligible. A total of three conduction paths were considered. Listed in order of significance, these were

- 1. Conduction through the walls of the regenerator cavity.
- 2. Conduction through the regenerator.
- 3. Conduction through the displacer.

For each path, a representative thermal conductivity, cross-sectional area, length, and temperature drop was used. These values are provided in Table 3.6 below.

Table 3.6: Information Associated with Calculation of the Conduction Loss

Conduction Path	Thermal Conductivity (W/mK)	Cross-Sectional Area (m ²)	Length (m)	Temperature Difference
Walls of regenerator cavity	47 (Solidworks® data for AISI 1020 steel)	0.0036	0.055	Difference between heater and cooler wall temperatures
Regenerator	1.94 (Volume weighted combination of 316 stainless steel and working fluid)	0.0061	0.055	Difference between heater and cooler gas temperatures
Displacer	0.684 (Area weighted combination of 316 stainless steel and working fluid)	0.0069	0.151	Difference between expansion space and compression space average gas temperatures

Heat flow rates for each conduction path were obtained via

$$\dot{Q}_{cond} = kA_{cond}\Delta T \tag{3.6}$$

were summed to give the total conduction loss.

3.5.3 Appendix Gap Loss

Appendix gap losses occur in the annular gap around the displacer. According to Urieli and Berchowitz, [10], the appendix gap loss may be estimated using

$$\begin{split} \dot{Q}_{app} &= -\pi \frac{d_{disp}}{2} k_g S_{disp}^2 \frac{\left(T_{ge} - T_{gc}\right)}{L_{disp} b} \\ &+ \pi d_{disp} \Delta p_{cycle} b S_{disp} \omega \left[\frac{\gamma}{\gamma - 1} ln \left(\frac{T_{ge}}{T_{gc}} \right) \left(\frac{1}{2} - \frac{1}{\sqrt{\frac{\omega}{2\alpha_{wall}}}} h \frac{k_g}{k_w} \right) - \frac{1}{2} \right] sin \varphi \end{split}$$

where

b	is the appendix gap width	m
k_g	is the thermal conductivity of the working fluid	W/mK
	is the thermal conductivity of the displacer and cylinder walls,	
k_w	taken to be 47 W/mK in this case.	W/mK
S _{disp}	is the displacer stroke	m
-	is the difference between the maximum and minimum cycle	
Δp_{cycle}	pressures	Ра
	is the thermal diffusivity of the displacer and cylinder walls,	
α_w	taken to be 1.172e-05 m^2/s in this case	m2/s
	phase angle by which cycle pressure variation leads displacer	
arphi	motion	rad
ω	is the angular frequency of the engine	rad/s

The calculated appendix gap loss is plotted as a function of appendix gap width in Figure 3.8. An optimum value of the gap width occurs due to the competing influences of the shuttle loss component and the net enthalpy transport component. The shuttle loss component, which refers to the transport of heat down the cylinder walls enhanced by the displacer motion [10], decreases with increasing gap width. The net enthalpy transport component, which is related to the pumping of gas in and out of the gap caused by pressure changes in the engine [6], increases with increasing gap width. The plot predicts an appendix gap width of 1 mm will minimize the appendix gap loss for the engine studied here. This is the gap of the displacer currently installed.

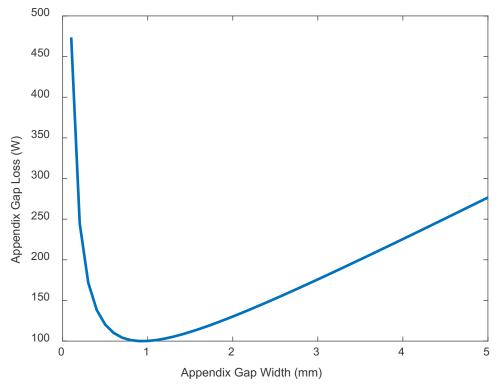


Figure 3.8: Calculated Appendix Gap Loss as a Function of Appendix Gap Width

3.5.4 Mechanical Friction and Forced Work

Senft's method, [27], of calculating mechanical friction using a constant mechanism effectiveness and the concept of forced work was implemented in the mathematical model. The mechanism effectiveness was taken to be 0.7, at the low end of Senft's suggested range for slider crank mechanisms. The pressure in the crankcase was assumed to vary adiabatically with the crankcase volume. Figure 3.9 provides an example indicator diagram with an overlaid buffer pressure curve. The areas of forced work have been highlighted in red. Areas of indicated work and forced work were numerically integrated from the results of the reference cycle calculations.

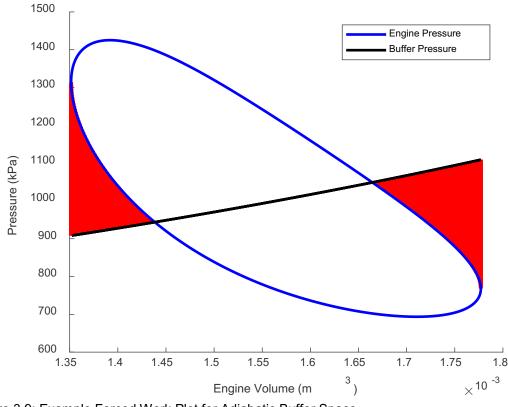


Figure 3.9: Example Forced Work Plot for Adiabatic Buffer Space

It is evident from Figure 3.9 that the amount of forced work depends on the shape of the indicator diagram and the buffer pressure curve, as well as their relative positions. The mechanical friction loss associated with forced work depends on the mechanism effectiveness.

3.5.5 Flow Friction

Flow friction in the heat exchangers and regenerator was estimated using the simple heat exchanger modeling approach, as described in Chapter 1 [30]. Entrance effects were not included. Only flow friction in the heater, cooler and regenerator were calculated. Specimen results are shown in Figure 3.10. The plots convey that the regenerator has a much greater contribution to the flow friction loss than the heater and cooler.

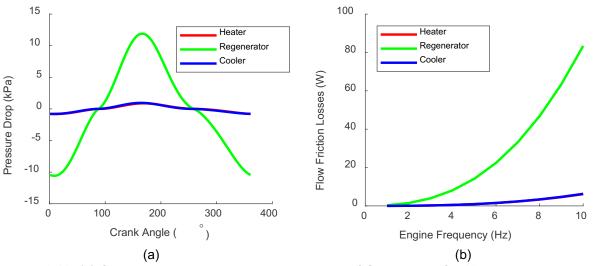


Figure 3.10: (a) Calculated Pressure Drops as a Function of Crank Angle for 10 Hz Engine Frequency (b) Flow Friction Losses as a Function of Engine Frequency

3.5.6 Losses Neglected in the Mathematical Model

Inherently, second order models overlook interactions between loss mechanisms. The calculations presented here consider the engine to be comprised of 5 homogeneous components. Effects of momentum, 3-dimensional flows, temperature and pressure dependent fluid properties, and temperature distributions across solid surfaces have not been included. Potentially computable decoupled loss mechanisms are discussed in this section.

Accurate calculation of the gas spring hysteresis loss would require knowledge of the heat transfer processes occurring in the crankcase. Urieli and Berchowitz, [10], offer a calculation for gas spring hysteresis in their book; however, application to the present problem violates several of their assumptions. The loss may be characterized empirically based on experimental data [28]. This was the approach taken here.

The effects of seal leakage have been discussed qualitatively in Chapter 1. The mathematical model developed here currently does not account for seal leakage. The most significant source of seal leakage is expected to be the displacer rod bearing. There is no dedicated seal on the displacer rod, only a plastic bushing which closely fits the rod. Maximum leakage at this location would occur at low engine speeds, when the time for leakage to occur was greatest.

Heat transfer hysteresis has been omitted due to the error involved in calculating it with the current model. Finite heat transfer rates would need to be estimated for all internal surfaces of

the engine. All wall temperatures would also need to be considered known. The loss is expected to increase with engine pressure swing amplitude.

Pressure losses due to finite speed of the pistons was not considered here. References were found which provided the equations necessary to perform the calculation, [18], [29], [49], but the derivation of these equations could not be found. The loss increases with increasing engine speed.

Energy consumed by the engine accessories would reduce the power output of a complete system. Accessories could include pumps for fuel or coolant, fans, or an alternator, depending on the application. These losses have not been considered in the modeling or experimental results presented here.

Temperature drops associated with heat transfer between the working fluid and the thermal source and sink decrease the efficiency and power output of the engine. These, like losses associated with the engine accessories would be evaluated separately from the thermodynamic model, which only considers working gas temperatures and assumed constant heat exchanger wall temperatures. Temperature drop losses have been neglected at this stage.

3.6 Addition of Losses to the Reference Cycle Results

The procedure for combining the decoupled losses with the reference cycle results is nontrivial and often differs between second order models in the literature. Losses can be added to the heat input and rejection rates, and to the power output of the reference cycle. Table 3.7 summarizes the scheme used in the current model.

Added to Reference Cycle	Decoupled Loss	Notes
	Heater flow friction and half of	Heat produced by flow friction in the heater
	regenerator flow friction	decreases the amount of heat it must take from
Heat Input	(subtract)	the thermal source
Rate	Regenerator enthalpy loss	Increases the load on both the heater and the
	Conduction loss	cooler
	Appendix gap loss	cooler
Power Output	Mechanical friction	Depends on amount of forced work and the
		mechanism effectiveness
	Flow friction	Heater, regenerator, and cooler.
	Mechanical friction	Heat produced by mechanical friction leaves
		the engine as reject heat.
Heat	Cooler flow friction and half of	Heat produced by flow friction in the cooler is
Rejection	regenerator flow friction	removed as reject heat
Rate	Regenerator enthalpy loss	Increases the load on both the heater and the cooler
	Conduction loss	
	Appendix gap loss	

Table 3.7: Scheme for Addition of Losses to Reference Cycle Results

Note that flow friction in the heater and hot side of the regenerator decrease the power output of the cycle, but they also reduce the heat input. Regenerator enthalpy loss is calculated during the reference cycle simulation using the simple heat exchange model, so its ramifications on the power output have already been accounted for. The loss is also added to the heat input and rejection rates to reflect the additional load on the heater and cooler due to imperfect regeneration. Heat produced by mechanical friction is removed from the engine as reject heat.

Conduction and appendix gap losses are assumed only to affect the heat transfer rates; hence, they decrease the efficiency but not the power output.

3.7 Sample Calculations

Using the mathematical model, virtual parametric studies are possible. Examples of model results for changing speed, pressure, and heater wall temperature are presented in Figure 3.11, Figure 3.12, and Figure 3.13, respectively. The adiabatic reference cycle model was used with a constant cooler wall temperature of 21 °C. In the plots, losses have been normalized by dividing them by the reference cycle power output to show changes in their relative influence. Imperfect heat transfer has been isolated from the simple heat exchanger model by comparing the reference cycle power output before and after the simple model has adjusted the heater and cooler gas temperatures. At this stage, trends in the model results are the focus, rather than numerical values. Quantitatively accurate results await comparison with experimental data, and adjustment of the appropriate calculation methods.

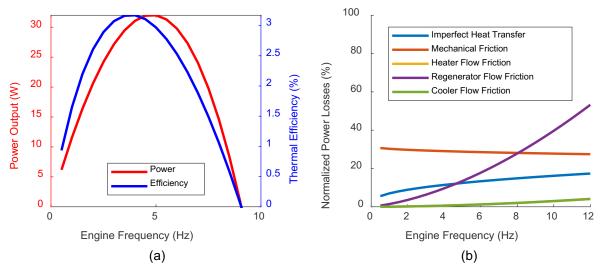


Figure 3.11: (a) Power and Efficiency Curves and (b) Normalized Power Losses as a Function of Frequency

In Figure 3.11(a), power and efficiency are observed to reach maxima, at different frequencies, before falling to zero at a common frequency. The point at which the curves cross the horizontal axis is the theoretical free running speed of the engine. Here, the power produced by the ideal reference cycle is equal to that taken away by the various power losses. Inspection of Figure 3.11(b), reveals that flow friction and imperfect heat transfer losses conspire to limit the free running speed of the engine. Mechanical friction decreases slightly due to a change in indicator diagram shape, brought about by the different gas temperatures caused by the imperfect

heat transfer loss. Regenerator flow friction is the loss which dominates at high engine speeds according to the model.

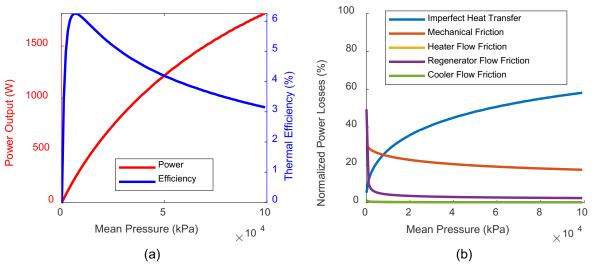


Figure 3.12: (a) Power and Efficiency Curves and (b) Normalized Power Losses as a Function of Mean Pressure

Figure 3.12 illustrates the effect of mean pressure on the power, efficiency, and power losses according to the current model. Efficiency is seen to peak, but power continues to increase as pressures climb far above what is possible in the laboratory. Inclusion of heat transfer hysteresis loss in the working space and buffer space as decoupled losses would limit the power of the engine as pressure was increased. Neglect of these loss mechanisms has led to this unrealistic trend in the power curve.

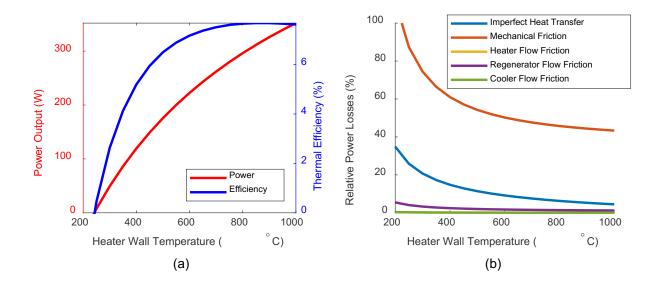


Figure 3.13: (a) Power and Efficiency Curves and (b) Normalized Power Losses as a Function of Heater Wall Temperature

Variations in engine performance as a function of heater wall temperature have been calculated and displayed in Figure 3.13. The power and efficiency curves cross the horizontal axis at the theoretical stall temperature of the engine. As heater wall temperature increases, power and efficiency follow with decreasing slope. In the case of heater wall temperature, the maximum power is limited by the material properties of the heater itself rather than by losses. As the heater wall temperature declines, all losses are seen to increase relative to the reference cycle power. Mechanical friction dominates in this case, increasing rapidly due to change in indicator diagram shape.

3.8 Conclusions

A preliminary second order model has been assembled which provides insight on engine performance trends as operating conditions vary. Advantages of the model include interchangeability of reference cycles, and isolation of the individual contributions of the decoupled losses. The model is missing several loss mechanisms, and needs to be compared with experimental data to identify areas of inaccuracy.

Chapter 4. Modifications to Reduce Minimum Thermal Source Temperature

The following chapter presents the experimental results of modifications made with the aim of reducing the minimum thermal source temperature of the engine. Three main changes were made: The piston diameter was reduced from 85 mm to 44 mm, the crankcase volume was increased from 3.20 L to 7.83 L, and the dead volume of the working space was reduced from 0.877 L to 0.745 L. The chapter begins by reporting the low thermal source temperature performance of the engine as it was originally built. The modifications are then described in detail. Finally, experimental results are presented which show the effects of the modifications on the low thermal source temperature engine performance. Throughout the chapter, and for the entirety of this thesis, the thermal sink temperature is constant at 21 °C.

4.1 Preliminary Results

The baseline low thermal source temperature performance of the engine was tested before modifications were made. With the heating system switched off, and the coolant temperature maintained at 21 °C, the engine ran until the heating cap temperature fell to 242 °C. Figure 4.1 is an indicator diagram measured near the stall point of this cool down test. The blue curve represents the measured pressure in the power cylinder, and the black curve corresponds to the measured crankcase pressure. Areas of forced work have been highlighted in red. Pressures were measured using the outboard transducers only at this stage of the experimental campaign. Pressure data from several crankshaft rotations has been averaged at each crank angle degree to produce the plot.

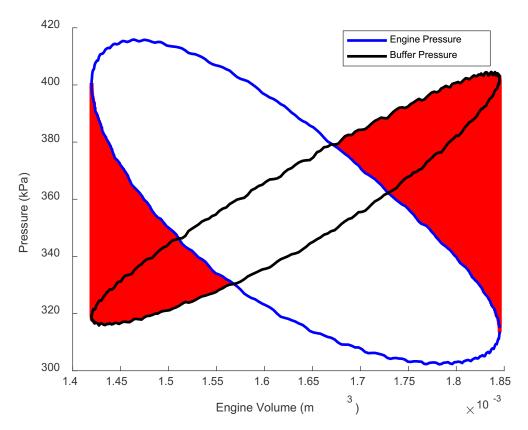


Figure 4.1: Experimental Indicator Diagram Taken Near the Cool Down Test Stall Point of the Engine As-Built

Two observations can be made regarding the buffer pressure curve in Figure 4.1. First, the pressure swings in the buffer space are seen to be of similar magnitude to those in the working

space. The resulting slope of the buffer pressure loop increases the amount of forced work relative to the constant buffer pressure case. Second, the area of the buffer pressure loop, which represents the work lost to gas spring hysteresis in the crankcase, is significant when compared to the area of the engine pressure curve. Thus, a buffer pressure curve with a slope closer to horizontal and a smaller area would lead to improved engine performance at low thermal source temperatures due to a reduction in mechanical friction and gas spring hysteresis losses.

4.2 Engine Modifications

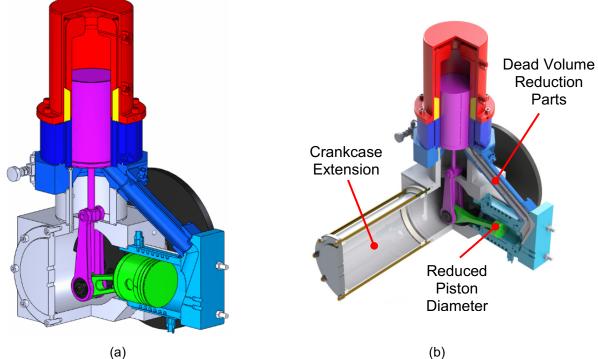


Figure 4.2: Rendered CAD Models of (a) As-Built Engine for Solar Power Application (b) Further Modifications for Low Hot Source Temperature Application

4.2.1 Modification 1: Reduced Piston Diameter

Mechanical friction and gas spring hysteresis in the crankcase have been identified as dominant losses at low source temperature operating points. Reducing the piston diameter addresses both loss mechanisms simultaneously. The smaller engine volume change results in a more circular indicator diagram with less forced work, and hence less mechanical friction. Crankcase volume changes are also reduced which decreases both the slope and the area of the buffer pressure loop on the indicator diagram, decreasing the amount of forced work and the gas spring hysteresis loss.

To reduce the piston diameter, the original aluminum piston was replaced with a graphite/glass piston-cylinder set (2KS444-3.0CP, Airpot® Corp). The piston-cylinder set was held in place by 3D printed components as shown in Figure 4.3. A new 3D-printed connecting rod was added to complete the system. The original aluminum cylinder was retained to preserve the original pressurization capability.

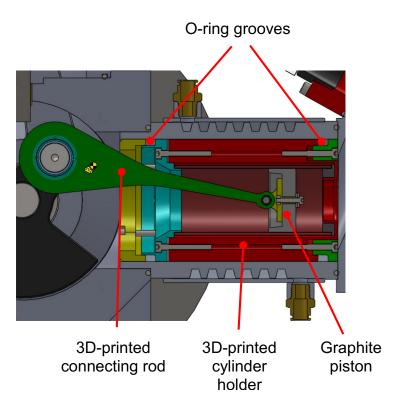


Figure 4.3: Annotated Section View of Glass Cylinder Holder

Several avenues for calculating the optimum piston diameter were explored. The results are summarized in Table 4.1 below. The first was using an empirical formula [68],

$$V_{swp} = \frac{V_{min}\Delta T}{1100} \tag{4.1}$$

presented by Ivo Kolin. The second method matched the pressure swing amplitudes induced by the displacer to those induced by the piston, while assuming ideal gas behavior and discontinuous piston and displacer motion. Further description of this method is included in Appendix B. Lastly, the second order model described in Chapter 3 was run, using the ideal adiabatic reference cycle, for a range of piston sizes to determine the size which maximized power and efficiency at a typical engine frequency of 2.5 Hz.

Method	lvo Kolin's Empirical Formula [68]	Equal Pressure Swing Amplitude from Piston and Displacer	Second Order Model Maximum Power and Efficiency at 2.5 Hz
Optimum Piston	12	47	24
Diameter (mm)	12 mm	47 mm	34 mm

Table 4.1: Optimum Piston Diameters for Thermal Source Temperature of 95 °C and Thermal Sink Temperature of 5 °C

The optimum piston diameter varies widely depending on the method used to calculate it. A 44 mm piston diameter was ultimately chosen for the prototype. This allowed use of a standard size piston-cylinder set, and left clearance for the 3D-printed connecting rod to pass through.

The engine was simulated using the second order model, for each piston size, at a heater gas temperature of 200 °C. The resulting forced work plots are displayed in Figure 4.4, while the numerical results appear in Table 4.2. While reducing the piston size has decreased the indicated work of the cycle, it has reduced the forced work by a greater margin, leading to a positive shaft work at a heater temperature where the as built engine theoretically will not run. The calculation illustrates the danger of optimizing indicated work without considering the influence of the cycle shape on mechanical friction losses.

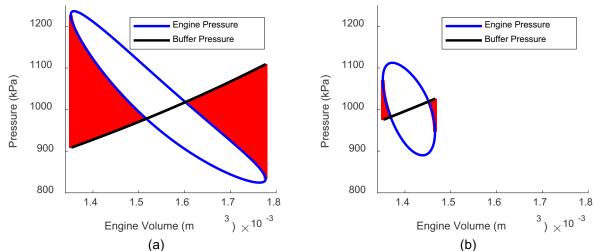


Figure 4.4: Calculated Forced Work Plots for (a) 85 mm Piston and (b) 44 mm Piston at 200 °C Heater Gas Temperature, 5 Hz Operating Frequency, and 10 bar Mean Pressure

Piston Diameter (mm)	85	44
Indicated Work (J)	40.4	16.5
Forced Work (J)	45.2	0.995
Shaft Work Assuming a Mechanism Effectiveness of 0.7 (J)	-4.67	10.8

Table 4.2: Numerical Results of Second Order Model Simulation for Reduced Piston Diameter

4.2.2 Modification 2: Crankcase Extension

Reducing crankcase pressure swings has been shown to reduce the amount of forced work and the amount of gas spring hysteresis. These pressure swings may be reduced further by increasing the crankcase volume. To accomplish this, the crankcase was extended as shown in Figure 4.5. The extension was comprised of a 6 inch O.D. mild steel pipe fitted with 3D-printed end pieces and fastened to the crankcase using the original crankcase cover, and eight threaded brass rods. The 3D-printed end pieces and the acrylic flange were fastened to the steel pipe using epoxy (Part #83000, Loctite®). The acrylic flange had an O-ring groove milled into the side facing the original crankcase. Prior to use, the extension was tested by filling it with water and pressurizing it to 10 bar for several hours.

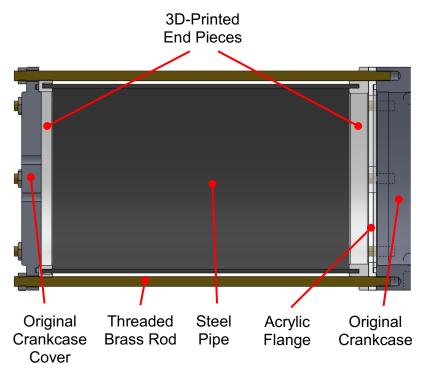


Figure 4.5: Sectioned CAD Model of Crankcase Volume Extension

4.2.3 Modification 3: Dead Volume Reduction Parts

Alfarawi et al., [63], showed, using their CFD results, that reducing the connecting pipe diameter could lead to an increase in power output. Here, dead volume reduction components were manufactured via 3D-printing and installed inside the connecting pipe, cylinder head, and displacer mount. A sectioned solid model of the parts is provided in Figure 4.6. The parts reduce the dead volume of the engine by 15 %.

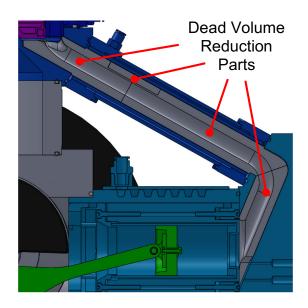


Figure 4.6: Sectioned Solid Model of Dead Volume Reduction Parts

The addition of the dead volume reduction parts has at least three potential effects on the engine. The reduction in dead volume increases the ability of both the piston and the displacer to change the pressure of the engine. Higher pressure swings should increase the indicated work, but may also influence mechanical friction, seal leakage, and heat transfer hysteresis losses. The decrease in connecting pipe diameter is also expected to increase the amount of flow friction. Finally, the plastic parts inhibit heat transfer from the working fluid to the water jacket that surrounds the connecting pipe. These conflicting effects make it unclear whether the dead volume reduction parts will lead to an increase, or a decrease, in low thermal source temperature performance.

The second order model was run with and without the dead volume reduction modification, recognizing that the effects would not be fully captured. The results are listed in Table 4.3 below. The model predicts an increase in both indicated work and forced work after installation of the dead volume reduction components. The amplitudes of the pressure and temperature swings in the adiabatic components have also been heightened. These effects are expected to change the amount of heat transfer hysteresis in the working space, which is not considered in this preliminary model. In the bottom row of the table, the dead volume reduction modification is observed to reduce the effective temperature difference between the expansion and compression spaces – a detrimental effect.

	Modifications 1 and 2 only	Modifications 1, 2, and 3
Indicated Work (J)	16.5	18.5
Forced Work (J)	0.631	0.717
Pressure Swing Amplitude (kPa)	222	252
Temperature Swing Amplitude in Expansion Space (°C)	29.9	34.0
Effective Mean Temperature Difference Between Expansion and Compression Space (°C)	153	152

Table 4.3: Modeling Results for Addition of Dead Volume Reduction Components

4.3 Experimental Results – Effect of Modifications

Experiments were performed to study the effects of the three modifications. These included power measurements, and cool down tests. For cool down tests, the heating cap was switched off with the engine running, and data was gathered until the engine stalled, with the intent of determining the minimum thermal source temperature.

The reduction in piston diameter allowed the engine to run at lower temperatures and pressures than it could with the original piston. Ideally, the engine power output would have been measured at the same operating point with both piston sizes. The limited strength of the 3D-printed components made this difficult to achieve. In fact, the small plastic part on the backside of the piston failed several times during attempts to reach the operating temperatures and pressures at which the as-built configuration ran well. It is expected that the larger piston will outperform the smaller one at high thermal source temperatures, but that the smaller one will produce more power at low thermal source temperatures. The cool down test results showed a clear difference between the two piston sizes. The 85 mm piston configuration stalled at a thermal source temperature of 185 °C.

The remaining two modifications, crankcase extension and dead volume reduction, were tested with the 44 mm piston installed. Preliminary tests were executed at three fill pressures below 500 kPa to reduce the risk of breaking the 3D-printed components. The thermal source temperature was set to 300 °C. Power tests were repeated for three engine configurations:

- 1. 44 mm piston.
- 2. 44 mm piston, and crankcase extension.
- 3. 44 mm piston, crankcase extension, and dead volume reduction components.

The experimental indicated power, shaft power, and torque as a function of speed and pressure for the three configurations are plotted in Figure 4.7, Figure 4.9, and Figure 4.8, respectively.

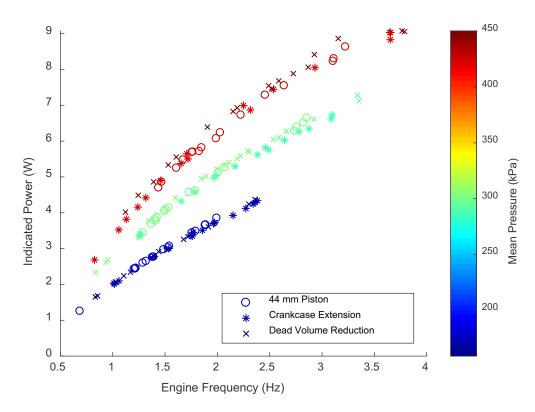


Figure 4.7: Experimental Indicated Power as a Function of Frequency for Three Modifications

The indicated power is calculated as the area of the indicator diagram multiplied by the engine frequency. As shown in Figure 4.7, the difference in indicated power was negligible between the three configurations. The addition of the crankcase extension was not expected to affect the indicated power, but the dead volume reduction parts were. The indicated power is observed to increase with frequency and mean pressure. The plot also shows that the engine was able to reach higher speeds at higher mean pressures. For the data corresponding to the highest mean pressure, differences in color between the data points indicate that mean pressure varied somewhat between tests.

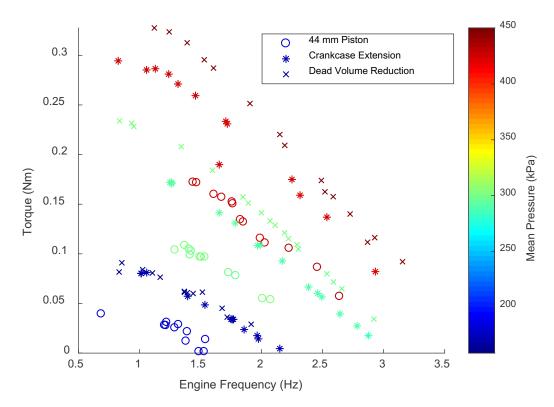


Figure 4.8: Experimental Torque as a Function of Frequency for Three Modifications

Figure 4.8 plots measured torque against engine frequency and mean pressure. Torque has clearly been improved by the addition of the crankcase extension, but the consequence of the dead volume reduction is unclear pending further test results.

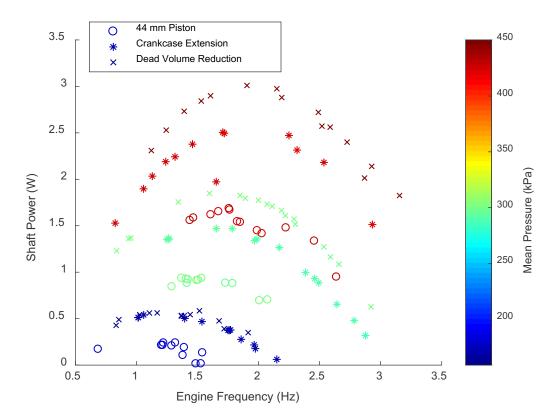


Figure 4.9: Experimental Shaft Power as a Function of Frequency for Three Modifications

In Figure 4.9, measured shaft power is plotted as a function of engine frequency and mean pressure. The shaft power is calculated by multiplying the measured torque by the measured angular frequency in radians per second. Maximum power is observed to occur at a moderate frequency which changes with mean pressure. The crankcase extension increased shaft power relative to the 44 mm piston configuration; however, the influence of the dead volume reduction parts is unclear at this stage due to inconsistencies in mean pressure between tests. For the low mean pressure case, the shaft power is unaffected, while for the higher mean pressure cases, the dead volume reduction parts appear to improve the shaft power. The marker colours indicate inconsistency in the mean pressures for the two higher pressure tests.

The benefit of the crankcase extension is further illustrated in Figure 4.10, below. The large loops correspond to the engine pressure measured in the power cylinder, while the small loops represent the crankcase pressure. As expected, adding the crankcase extension left the engine pressure diagram unchanged. The crankcase pressure swing, and the area of the crankcase pressure loop, were both reduced by extending the crankcase volume. For the example in Figure

4.10, the addition of the crankcase extension reduced the forced work by 39.1 % and the gas spring hysteresis loss by 65.8 %. The figure also reveals that these effects could be reduced further if the crankcase were made even larger.

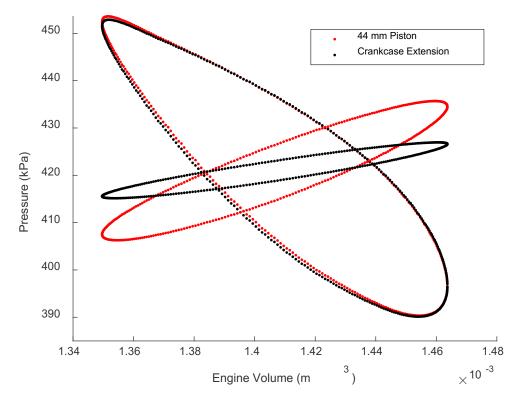


Figure 4.10: Measured Indicator Diagrams with and without the Crankcase Extension Modification

Figure 4.11 and Figure 4.12 plot measure crankcase gas spring hysteresis loss and forced work, respectively, as functions of engine frequency and mean pressure. The plots confirm that the extension of the crankcase volume reduced forced work and gas spring hysteresis for all conditions tested.

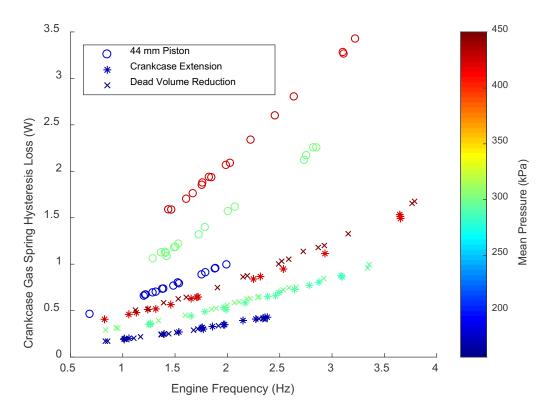


Figure 4.11: Crankcase Gas Spring Hysteresis Loss for the Three Modifications

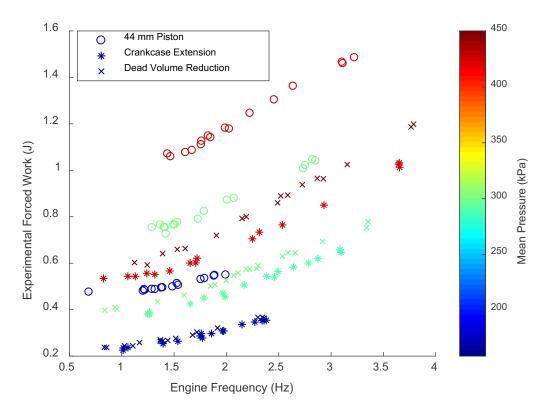


Figure 4.12: Experimental Forced Work for the Three Modifications

Further tests were deemed necessary to flush out the effect of the dead volume reduction parts. For this purpose, a second data set was collected with special attention payed to the engine fill pressure. These tests were completed at a thermal source temperature of 200 °C. The fill pressure was still difficult to duplicate between tests with, and without, the dead volume reduction parts installed. Post processing included removing outlier mean pressure data files so that mean pressures were within a range of 6 000 Pa (0.87 PSI) for the data presented below. The tests were performed with the 44 mm piston and the crankcase extension installed.

Figure 4.13 presents the indicated and shaft power results for the second data set. The addition of the dead volume reduction parts appears to have no influence on either of these results for the conditions tested.

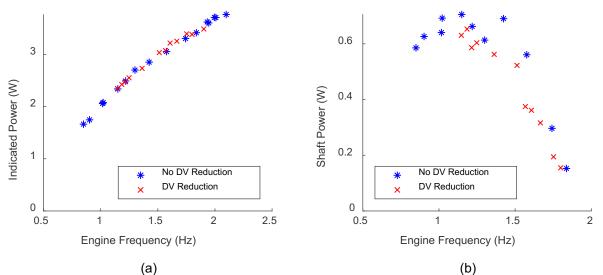


Figure 4.13: (a) Indicated Power and (b) Shaft Power as a Function of Frequency with and without the Dead Volume Reduction Parts

The only measurement that showed a distinct difference caused by the dead volume reduction is the heat rejection measurement. Heat rejection data is shown in Figure 4.14 below. The dead volume reduction components reduced the heat rejection rate in the connecting pipe and power cylinder water jacket, and increased the heat rejection rate in the cooler water jacket.

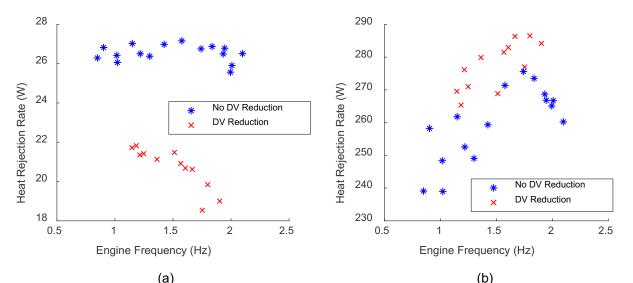


Figure 4.14: Heat Rejection Rates from (a) the Connecting Pipe and Power Cylinder and (b) the Cooler

4.4 Experimental Results – Cool Down Tests

Cool down tests were conducted to characterize the low thermal source temperature performance of the modified engine. These involved switching off the heating system with the engine running, and recording data until the engine stalled. Table 4.4 lists the minimum thermal source temperatures reached by the four engine configurations tested.

Table 4.4: Minimum Thermal Source Temperature Reached During Cool Down Tests for All Engine Configurations

Engine Configuration	Minimum Thermal Source Temperature (°C)
As-Built	242
44 mm Piston	185
44 mm Piston, and Crankcase Extension	144
44 mm Piston, Crankcase Extension, and Dead Volume Reduction	145
volume Reduction	

The results show that all modifications, except for the dead volume reduction, were successful in reducing the minimum thermal source temperature. The results shown in the table above were obtained with no load on the engine.

Additional cool down experiments were carried out in which the engine was working against a constant load. For these tests, the fully modified engine was used. Data was collected intermittently as the engine cooled. The cool down process took about an hour, and started at a heating cap temperature of $300 \,^{\circ}$ C.

As in the modification comparison tests, maintaining a constant fill pressure was challenging with the current set-up. The engine had a slow leak, so it was left connected to the air compressor during the cool down test. Even in a perfectly sealed engine, the ideal gas behavior of the working fluid would decrease the mean pressure as the thermal source temperature was reduced. Imperfections in the pressure regulator on the compressor, and the check valve on the filling tube of the engine, led to an inconsistent flow rate of air into the engine to maintain the mean pressure. At the low power levels being measured during cool down experiments, these fill pressure fluctuations may have affected the data. For example, Figure 4.15 shows that the torque, frequency, and power all decrease with decreasing thermal source temperature. The trend is

approximately linear, with a steep drop off just before the stall temperature is reached. The accompanying fill pressure data was examined while investigating this drop off, and is displayed in Figure 4.16.

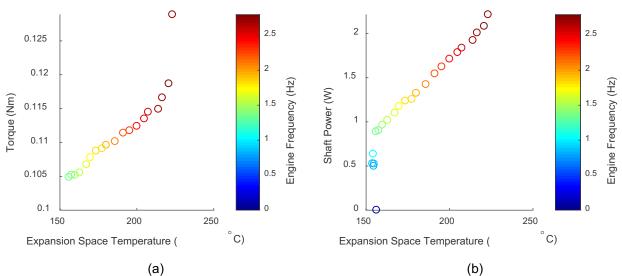


Figure 4.15: Loaded Cool Down Test Results for (a) Torque and (b) Shaft Power

In Figure 4.16, the red circles represent the mean power cylinder pressure and the black stars represent the mean crankcase pressure. Starting at an expansion space temperature of 180 °C and continuing downward, the mean pressures are observed to increase. Their rates of increase are steepest at the lowest expansion space temperatures, and the crankcase mean pressure changes at a different rate than the power cylinder mean pressure. The difference between the mean pressures of the crankcase and working space affect the amount of forced work in the cycle. Gas spring hysteresis in the crankcase also changes with crankcase mean pressure. Seal leakage characteristics are also expected to be affected by the pressure difference between the working space and the crankcase. So, the steep drop-offs in the torque and power plots of Figure 4.15 are probably caused by the steep changes in pressure visible in Figure 4.16. Further, the data collected above 180 °C expansion space temperature should show trends in expansion space temperature more faithfully, since the mean pressures were more consistent for that part of the experiment.

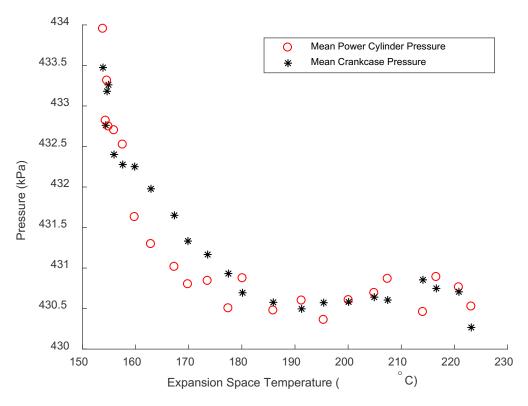


Figure 4.16: Mean Crankcase and Power Cylinder Pressures as a Function of Expansion Space Temperature for the Loaded Cool Down Test

In Figure 4.17, indicated work and forced work have been plotted for the same cool down trial. As expected, Figure 4.17 (a) shows that the indicated work diminishes with expansion space temperature. The adjacent plot indicates that the forced work has also decreased. The trends are approximately linear down to the expansion space temperature of 180 °C.

The steep drop in indicated work at an expansion space temperature of about 160 °C is counter-intuitive considering the mean pressure data of Figure 4.16. It is expected that an increase in pressure will increase the indicated work. This phenomenon is evidenced in Figure 4.7. The trend could be related to the engine speed, and the loss associated with seal leakage. Seal leakage is expected to be more severe at lower engine speeds since there is more time for mass transfer in a single cycle. There could be a speed at which seal leakage becomes the dominant loss mechanism. When this speed was reached, seal leakage losses would reduce the indicated work and the engine would slow further, leading to even more severe leakage. This compounding effect would quickly stall the engine.

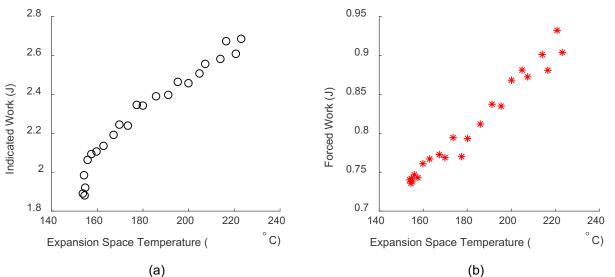


Figure 4.17: (a) Indicated Work and (b) Forced Work as a Function of Expansion Space Temperature for Loaded Cool Down Test with Fully Modified Engine

Figure 4.18 was produced with the seal leakage hypothesis in mind. The engine frequency is observed to follow a similar trend to the indicated work. Seal leakage is a plausible link between the two plots; however, verification work would require additional experiments in which the indicated power was measured for a series of speeds and leakage rates.

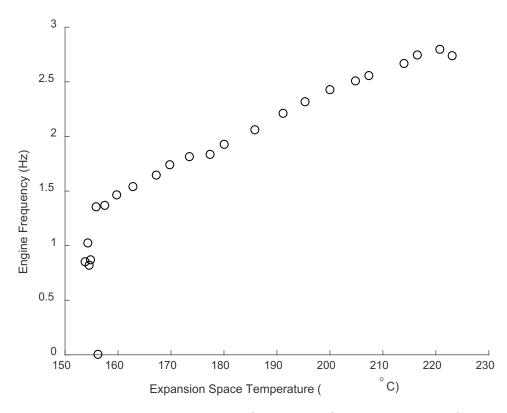


Figure 4.18: Engine Frequency as a Function of Expansion Space Temperature for the Loaded Cool Down Test

Figure 4.19 shows the indicator diagrams corresponding to the same cool down test, colored according to their expansion space temperature. Only data sets in which the expansion space temperature was greater than 180 °C were included, as these had the most consistent mean pressure according to Figure 4.16. The area of the indicator diagrams is observed to decrease with expansion space temperature. The orientation of the diagrams rotates counter-clockwise with decreasing expansion space temperature, which explains the reduction in forced work.

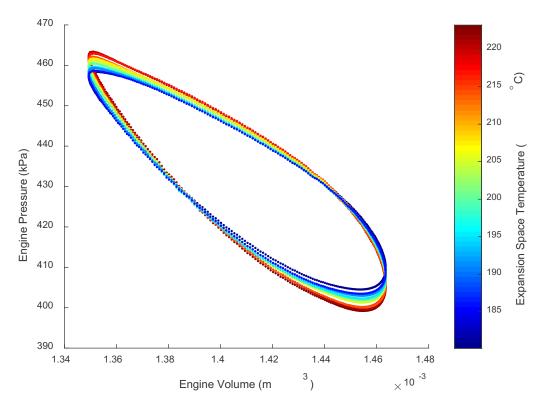


Figure 4.19: Series of Indicator Diagrams for Loaded Cool Down Test of Fully Modified Engine

It is the relative amount of forced work, compared to indicated work, which is the important quantity for engine performance. The ratio of forced work to indicated work has been plotted in Figure 4.20, as a function of expansion space temperature. The forced work ratio maintains an approximately constant average down to 180 °C, where it begins to increase rapidly. This is likely caused by the change in mean pressures indicated by Figure 4.16. The difference between the crankcase and power cylinder mean pressures strongly affects the amount of forced work. This difference changes, according to Figure 4.16, because the crankcase mean pressure changes at a different rate than the power cylinder mean pressure, when the expansion space temperature declines past 180 °C.

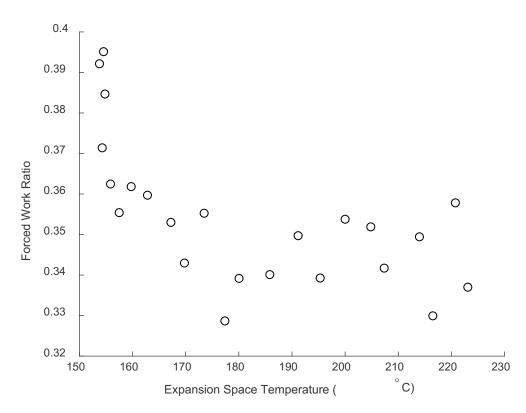


Figure 4.20: Forced Work Ratio as a Function of Expansion Space Temperature for Loaded Cool Down Test

Figure 4.21 shows that the gas spring hysteresis loss per cycle follows a similar trend to the forced work ratio for this cool down test. Again, the sudden change at 180 °C is plausibly due to the change in mean pressure, since gas spring hysteresis loss is strongly dependent on the mean pressure. This is because a larger mean pressure leads to larger pressure swings for a given change in crankcase volume. Larger pressure swings are accompanied by larger temperature swings, which encourage more heat transfer between the gas and the crankcase walls, and lead to higher hysteresis loss.

Another possibility is that the non-linear decrease in speed, which occurred at an expansion space temperature of 160 °C according to Figure 4.18, was the main cause of the abrupt changes in forced work ratio and gas spring hysteresis loss. A decrease in speed could change the indicator diagram shape due to changes in flow speed altering heat transfer rates, and due to an increase in seal leakage. This change in indicator diagram shape would influence the amount of

forced work. In the case of gas spring hysteresis, slower speed means more time for heat transfer between the gas and the crankcase walls, and a higher resulting loss.

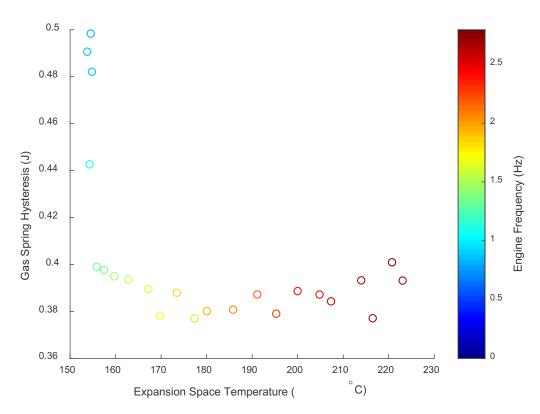


Figure 4.21: Gas Spring Hysteresis Loss as a Function of Expansion Space Temperature for the Loaded Cool Down Test

4.5 Conclusions

The as-built Stirling engine has been successfully modified to reduce its minimum required thermal source temperature. The decreased piston size and increased crankcase volume modifications improved low temperature performance by decreasing mechanical friction and crankcase gas spring hysteresis losses. The dead volume reduction parts changed the power output immeasurably, but did shift some heat rejection duty from the power cylinder/connecting pipe water jacket to the cooler water jacket. A loaded cool down test was performed with the aim of identifying barriers inhibiting lower thermal source temperature operation. Inconsistency in fill pressure, and coupled changes in temperature and speed, made the results difficult to interpret.

Stirling engines in the literature have operated on temperature differences as little as 0.5 °C, [69], so the temperatures achieved here do not represent a fundamental limit. Reducing the minimum thermal source temperature further will require further modifications, which could include

- 1. Further reductions in piston size and/or dead volume or a further increase in crankcase volume.
- 2. Changes in regenerator properties and/or heater head geometry.
- 3. Refinement of the mechanism to reduce mechanical friction.

The model needs to be improved and validated so it can be used to make more informed choices about which modifications to pursue for a desired performance change.

Chapter 5. Performance Evaluation and Model Assessment for Fully Modified Engine

In this chapter, an assessment of the second order model is made based on comparison to measured data pertaining to the fully modified engine and the final version of the test rig. The assessment follows a systematic approach, in which each sub-component of the model is evaluated independently by comparison to relevant experimental results. The chapter concludes with a comparison between measured and predicted overall performance.

5.1 Reference Cycle Indicator Diagram

Accurate prediction of the indicator diagram is the foundation of a second order model. The area of the indicator diagram represents the work done in one rotation of a lossless engine. The shape of the indicator diagram affects the calculation of decoupled losses. It is a prerequisite for the forced work method of estimating mechanical friction. Pressure swings from the indicator diagram are needed for calculation of heat transfer hysteresis, appendix gap, flow friction, regenerator enthalpy, imperfect heat transfer, and seal leakage losses. Experimentally, these losses affect the indicator diagram; hence, the true problem is a coupled one, which goes against the assumptions of the second order modeling approach.

The experimental indicator diagram was produced from data collected using the power cylinder pressure transducers, and the rotary encoder. Encoder pulses were converted to crank angles as described in Chapter 2, and rounded to the nearest degree. The result was a list of crank angles spanning several complete rotations over a ten second data set, each adjacent to a corresponding power cylinder pressure measurement. Then, all pressure measurements with the same crank angle value were averaged to produce a vector of 360 pressures, one for each crank angle degree. Volumes for each crank angle degree were calculated using the equations introduced in Chapter 3. Using these volumes and averaged pressures, the indicator diagram could be plotted and compared easily with outputs from the reference cycle models.

To compare experimental data to the reference cycle models, the measured gas temperatures and mean pressure were used as model inputs. Specifically, the average measured power cylinder pressure was taken to be the mean pressure in the model. The heater gas temperature was taken to be the average of the temperatures measured by the expansion space and regenerator hot thermocouples shown in Figure 2.10. To calculate the measured cooler gas temperature, the regenerator cold right and left thermocouple readings were averaged, and the result was averaged with the displacer mount thermocouple reading.

Figure 5.1 exhibits two experimental indicator diagrams, and their associated ideal isothermal and adiabatic model counterparts. Figure 5.1 (a) was produced using data collected with the as-built engine configuration at a heating cap temperature of 400 °C. The models are observed to approximate the measured data more closely than in Figure 5.1 (b), where the data comes from the fully modified engine at a heating cap temperature of 300 °C. Note that the mean

pressure is the same for the two plots, but the engine volume variations are different due to the difference in piston diameter. Taken together, the plots reveal that agreement between the reference cycle models and the experimental data is significantly better for the high temperature as-built engine than for the lower temperature fully modified engine. The plots typify those found for the high and low temperature testing campaigns, respectively.

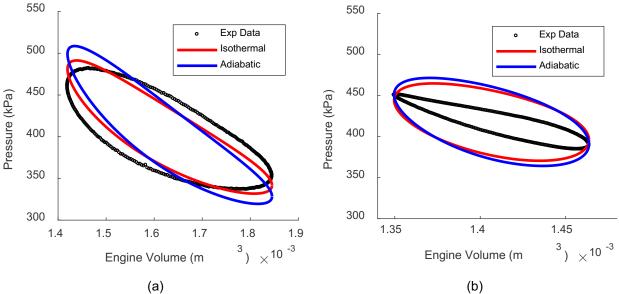


Figure 5.1: Experimental Indicator Diagrams with Overlaid Reference Cycle Models (a) As-Built Engine Running with a Heating Cap Temperature of 400 °C (b) Fully Modified Engine Running with a Heating Cap Temperature of 300 °C

Figure 5.2 presents data collected using the fully modified engine and two different heating cap temperatures. Both data sets were collected with a mean engine pressure of 414 kPa. The vertical axis gives the relative error in indicated work predicted by the isothermal and adiabatic reference cycle models. The figure demonstrates that at the lower heating cap temperature, the error in indicated work is higher for a given engine frequency. The isothermal model overshoots the measured value by a smaller amount than the adiabatic model for the conditions tested. For both heating cap temperatures, the indicated work error increases with engine speed.

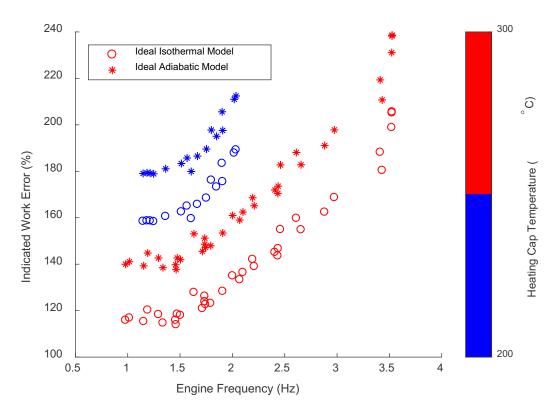


Figure 5.2: Indicated Work Error for Isothermal and Adiabatic Reference Cycle Models as a Function of Engine Frequency and Heating Cap Temperature

The reference cycle models do not include seal leakage, flow friction, heat transfer hysteresis, and other losses which influence the indicator diagram in the real system. The indicator diagram error is more severe for low temperature, low power operating points because losses neglected in the reference cycle models are more influential there, relative to the indicated work being produced. The increase in indicated work error with speed implies that, as a group, the neglected losses have a greater influence on the indicator diagram at higher speeds. The behavior is indicative of flow friction losses, which have not been accounted for in the reference cycle calculations.

The second order modeling approach assumes that the losses do not affect the indicator diagram. In fact, results from the reference cycle indicator diagram are used as inputs for the decoupled loss calculations; thus, any errors in the reference cycle indicator diagram propagate into the loss calculations. Figure 5.1 and Figure 5.2 demonstrate that, all else being equal, the

assumption of decoupled losses becomes increasingly unsound as the thermal source temperature of the engine decreases.

5.2 Crankcase Gas Spring Hysteresis

Gas spring hysteresis loss in the crankcase is calculated as the area of the crankcase indicator diagram. Since the volume amplitude is the same for the crankcase and the engine, the crankcase indicator diagram can be plotted as a function of either crankcase volume or engine volume, without affecting the area. Here, measured crankcase pressures were averaged for each crank angle degree and plotted as a function of engine volume. The area of the resulting loop was calculated numerically, and taken to be the crankcase gas spring hysteresis loss per cycle.

The measured crankcase gas spring hysteresis loss per cycle is plotted as a function of engine speed and mean pressure in Figure 5.3 below. The loss decreases slightly with speed and increases with mean pressure. Heat transfer between the gas and the crankcase walls is one of the main irreversibilities which causes gas spring hysteresis [6]. Lower speeds allow more time for heat transfer, resulting in a higher loss. Higher mean pressures lead to higher pressure swing amplitudes in the crankcase, which produce higher temperature swings, more heat transfer, and higher loss.

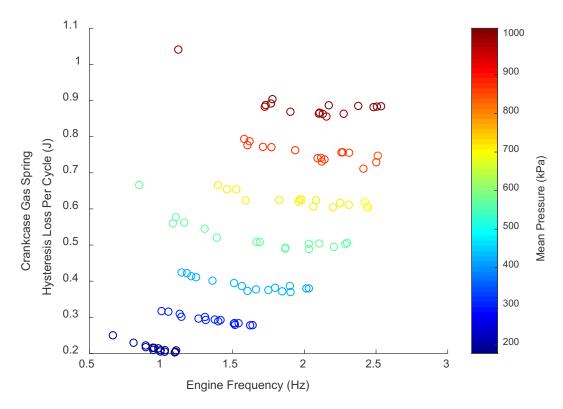


Figure 5.3: Measured Crankcase Gas Spring Hysteresis Loss for the Fully Modified Engine as a Function of Engine Frequency and Mean Pressure

A second order polynomial surface was fit to the gas spring hysteresis loss rate plotted against engine speed and mean pressure as shown in Figure 5.4. The coefficients of the fit equation, Eq. (5.1), were recorded and could be used to estimate the loss for arbitrary speed and pressure combinations. The fit was repeated for the three crankcase configurations tested: Asbuilt, 44 mm piston, and 44 mm piston with crankcase volume extension. The fit coefficients, and R^2 values are listed in

Table 5.1.

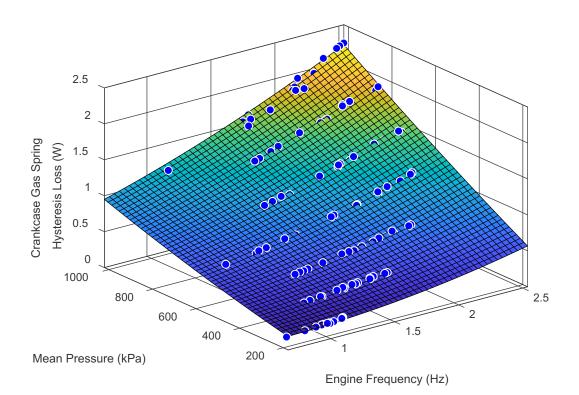


Figure 5.4: Second Order Polynomial Surface Fit to Measured Crankcase Gas Spring Hysteresis Loss Data

$$PL_{GSH} = c_1 + c_2 f + c_3 p_{mean} + c_4 f^2 + c_5 f p_{mean} + c_6 p_{mean}^2$$
(5.1)

Crankcase Configuration	<i>C</i> ₁	<i>C</i> ₂	C ₃	C4	C ₅	<i>C</i> ₆
As-Built ($R^2 = 0.9991$)	-2.855	4.902	-1.239e-5	-0.4064	2.327e-5	7.373e-12
44 mm Piston ($R^2 = 0.9997$)	0.2473	-0.1534	2.311e-7	0.07564	2.076e-6	1.975e-13
44 mm Piston + Crankcase Extension $(R^2 = 0.9994)$	0.1625	-0.2039	2.503e-7	0.09528	5.668e-7	2.293e-13

 Table 5.1: Second Order Polynomial Fit Coefficients for Crankcase Gas Spring Hysteresis Empirical

 Formula

5.3 Mechanical Friction

Mechanical friction is modeled using the forced work approach developed by James R. Senft. Models for the buffer pressure, engine pressure, and a value of mechanism effectiveness are prerequisites. It has already been shown that both the isothermal and adiabatic reference cycles represent the measured engine pressure variations poorly. This shortcoming will need to be improved for successful use of the forced work approach. Efforts to measure and model the remaining parameters will be discussed in this subsection.

Since the volume of the sealed crankcase varies while the engine is running, its pressure is not constant. Preliminary buffer pressure models assumed that the process could be represented by compression and expansion of an ideal gas in a container that was either isothermal or adiabatic. For the isothermal assumption, the crankcase pressure was calculated using the ideal gas law as

$$p_{CC,isothermal}(\theta) = \frac{m_{CC}RT_{CC}}{V_{CC}(\theta)}$$
(5.2)

For the adiabatic crankcase assumption, the crankcase pressure was calculated as

$$p_{CC,adiabatic}(\theta) = \overline{p_{CC}} \left(\frac{\overline{V_{CC}}}{V_{CC}(\theta)} \right)^{\gamma}$$
(5.3)

where the overbars denote mean values.

Figure 5.5 shows a typical crankcase indicator diagram overlaid with the two buffer pressure models shown above. The adiabatic buffer pressure assumption was found to better represent the crankcase pressure swings than the isothermal assumption. Even the adiabatic buffer pressure model falls short of the measured pressure swing amplitude. This could be the result of neglecting the volume of the displacer drive rod in the calculation of the crankcase volume variations. Seal leakage between the working space and the crankcase could also increase the crankcase pressure swings. Since the buffer pressure forms a loop, the forced work will be increased relative to that calculated using a single-line model of the buffer pressure. This adds additional error to the forced work model.

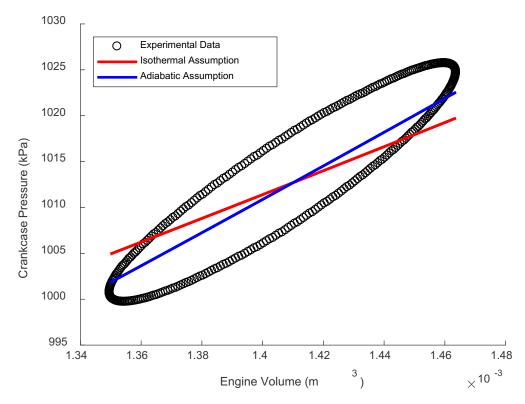


Figure 5.5: Measured Buffer Pressure with Overlaid Adiabatic and Isothermal Buffer Pressure Models

With models and experiments to determine the engine and buffer pressure curves, it is possible to calculate the amount of forced work. Graphically, this amounts to calculating the area of the red regions highlighted in Figure 3.9. Numerically, the forced work is calculated using the following algorithm¹. The inputs are vectors of engine volume, engine pressure, and buffer pressure as functions of crank angle.

- 1. Apply a central differencing scheme to the engine volume vector to calculate the volume change increment that corresponds to each engine and buffer pressure value.
- 2. For each pair of corresponding engine and buffer pressure values, calculate the difference in pressure.
- If the sign of a pressure difference vector element is opposite to its corresponding element in the volume change vector, calculate an incremental area of forced work by multiplying the two elements.
- 4. The sum of the forced work area elements is the total forced work.

¹ Personal communication with Steven Middleton.

The above method is the result of considerable effort by the author and his colleagues and has been validated by comparison to known areas.

The forced work approach assumes a constant mechanism effectiveness which represents frictional losses in the drive mechanism. The real mechanism effectiveness depends on crank position, due to the changing loads and geometry of the mechanism during operation. The most direct method of measuring the mechanism effectiveness would be to apply a known force to the piston and measure the resulting torque on the crankshaft for a series of crank positions. This could potentially be done using weights if the engine orientation was changed. The mechanism effectiveness has not been measured at this stage.

5.4 Flow Friction

The flow friction was measured using two methods. The first was a series of cold motoring tests with the engine in various stages of disassembly. Flow friction was also quantified by measuring the regenerator pressure drop, using an outboard pressure transducer, while the engine was running. This subsection examines the results of these two flow friction measurement approaches and, for the second approach only, agreement with the mathematical model.

Figure 5.6 presents the results of the cold motoring friction tests. These were performed using the test rig configuration shown in Figure 2.8. The engine was fitted with the 44 mm piston, but had the original crankcase and no dead volume reduction components during the cold motoring experiments. Input shaft power to the engine was measured, using the rotary encoder and torque transducer, for a range of engine frequencies at atmospheric pressure. The procedure was repeated for the following engine states:

- 1. Fully assembled (44 mm piston, original crankcase, no dead volume reduction components).
- 2. Crankcase cover removed.
- 3. Crankcase cover and heater head removed.
- Crankcase cover, heater head, and power cylinder head removed. A 3-D printed part was manufactured to hold the power cylinder on in the absence of the power cylinder head.
- 5. Crankcase cover, heater head, power cylinder head, and cooler removed.

The plot reveals the relative influence of mechanical friction, flow friction in different components, and gas spring hysteresis. The difference between the blue circles and the red starts is small, indicating that the gas spring hysteresis loss in the crankcase is insignificant compared to mechanical and flow friction at high engine frequencies. Removal of the heater head, which also contains the regenerator, drops the power consumption significantly, showing that flow friction in these components is a relatively large contribution to the overall friction. It could be argued that, since elimination of the heater head has broken the seal between the working space and the surroundings, any gas spring hysteresis occurring in the working space has also been jettisoned. Considering the relative influence of the gas spring hysteresis in the crankcase, the contribution of the loss in the working space is assumed to also be relatively small; hence, the

large drop in power consumption after elimination of the heater head is attributed to flow friction in the heater and regenerator. The magenta x's show the measured power consumption with the cylinder head removed. The slight decrease in power is due to the absence of flow friction occurring in the cylinder head and connecting pipe. The green dots show a further decrease in power consumption when the flow friction of the cooler is taken away. The green dots represent the mechanical friction power consumption of the engine, as all flow friction and gas spring hysteresis causing components have been removed.

Figure 5.6 proves that mechanical friction and flow friction in the heater and regenerator are the two main contributions to the overall friction at atmospheric pressure. At higher pressures, gas spring hysteresis could play a more influential role.

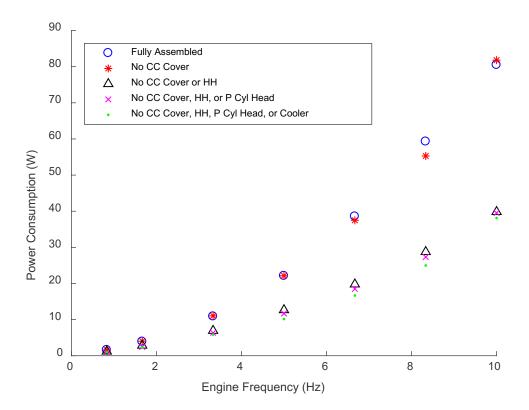


Figure 5.6: Measured Power Consumption During Cold Motoring Tests

The pressure drop across the regenerator was measured using an outboard pressure transducer connected via 1/8" stainless steel tubes to ports above and below the regenerator. Data was collected with the engine running at a heating cap temperature of 200 °C, and at a range of

frequencies and mean pressures. The effect of changing frequency and mean pressure on the measured regenerator pressure drop are exemplified in Figure 5.7 below. On the plots, measured data is represented by dashed lines, while results of the quasi-steady flow friction model are represented by solid lines. Positive pressure values indicate a pressure gradient which is declining away from the crankcase.

Figure 5.7 shows that regenerator pressure drop amplitude increases with mean pressure and engine frequency. The shape of the curves predicted by the model are similar to those measured. Pressure drops predicted by the model are symmetric about the horizontal axis, while the mean values of the measured pressure drops are below the x-axis. This could be a result of the calibration scheme used for the outboard differential pressure transducer. The curve fitted to the correction terms may have resulted in a zero offset since it was based on positive and negative pressure calibration data. The tube length of the outboard transducers has been shown to influence the measurement, in some cases, in Chapter 2. Here, since there is little phase offset between the pressure curves, it seems unlikely that the influence of the tubes was significant for these operating conditions.

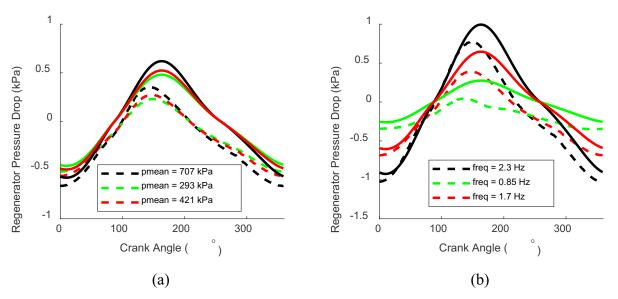


Figure 5.7: Measured Regenerator Pressure Drop as a Function of Crank Angle with Overlaid Quasi-Steady Model for (a) Three Mean Pressures at an Engine Frequency of 1.5 Hz and (b) Three Engine Frequencies at a Mean Pressure of 562 kPa (Positive Direction is from the Cold to the Hot Side of the Regenerator)

Figure 5.8 plots regenerator pressure drop amplitude as a function of engine frequency and mean pressure for the full data set collected at 200 °C heating cap temperature. The plot confirms the trend that regenerator pressure drop amplitude increases with engine frequency and mean pressure.

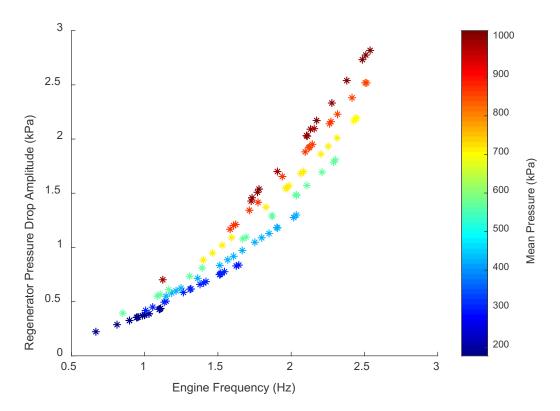


Figure 5.8: Measured Regenerator Pressure Drop Amplitude as a Function of Speed and Mean Pressure for a Heating Cap Temperature of 200 °C

In Figure 5.9, the error in regenerator pressure drop amplitude between the model and the experimental data is plotted as a function of engine frequency and mean pressure for the same data set plotted in Figure 5.8. The error was calculated as the difference between the modeled and measured pressure drop amplitude divided by the measured pressure drop amplitude, and is expressed as a percent. The plot shows that the agreement between the model and the data is closest at high speed, high pressure operating points. At low speed, low pressure operating points, agreement is relatively poor. Many low temperature difference Stirling engines operate at low speeds and mean pressures. Significant overestimation of the regenerator pressure drop

could occur when using this simple heat exchanger model to predict performance of these engines.

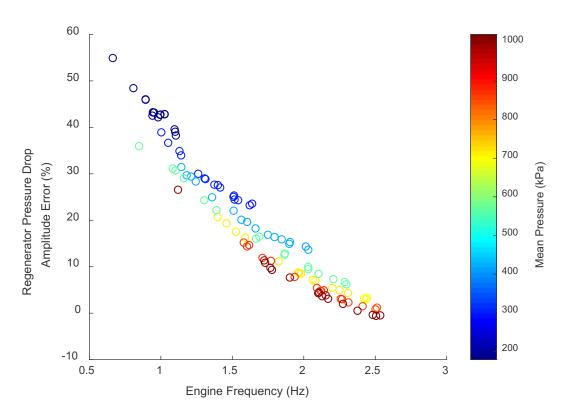


Figure 5.9: Regenerator Pressure Drop Amplitude Error as a Function of Engine Frequency and Mean Pressure

Note that, in the model, the regenerator pressure drop calculation is based on results from the ideal adiabatic reference cycle model, which has already been shown to represent the data inaccurately regarding the indicator diagram. The pressure drop calculation is also based on steady flow correlations with questionable applicability to the current problem. Further assessment of this flow friction modeling approach should continue after prediction of the indicator diagram has been improved.

5.5 Heat Exchanger Performance

The overall heat exchanger performance includes heat transfer rate, flow friction, and dead volume contribution; however, this section will focus on the heat transfer rate only. Regarding heat transfer rate, a perfect cooler would have an average gas temperature equal to the thermal sink temperature, and a perfect heater would have an average gas temperature equal to the thermal source temperature. For this research, the heating cap and water bath setpoints were taken to be the thermal source and sink temperatures, respectively.

The heat transfer performance of the heater and cooler was quantified by comparing measured gas temperatures to the heating cap and water bath setpoints. For the heater, the gas temperature was taken as the average of the expansion space and regenerator hot thermocouple measurement locations shown in Figure 2.10. To calculate the measured cooler gas temperature, the regenerator cold left and regenerator cold right thermocouple readings were averaged, and the result was averaged with the displacer mount reading. The difference between the heating cap setpoint and the average heater gas temperature is denoted the heater temperature drop, and the difference between the average cooler gas temperature and the water bath setpoint is denoted the cooler temperature drop. Ideally, these temperature drops will be as low as possible.

Figure 5.10 plots the measured heater and cooler temperature drops for a data set collected at a heating cap temperature of 200 °C using the fully modified engine. Note that the vertical axis limits are different between the two plots. Temperature drops are expressed as a function of engine frequency and mean pressure.

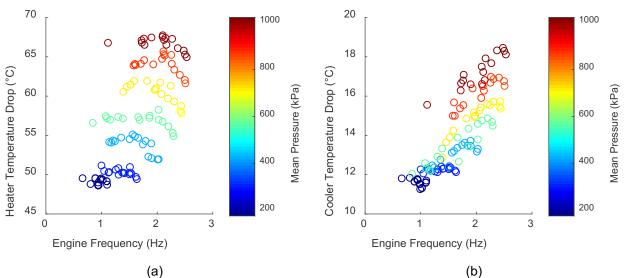


Figure 5.10: (a) Measured Temperature Drop between the Heater Gas Temperature and the Heating Cap Setpoint and (b) Measured Temperature Drop between the Cooler Gas Temperature and the Water Bath Setpoint

In both plots of Figure 5.10, the temperature drops are observed to increase with mean pressure. This trend is what would eventually lead to a peak in shaft power as the mean pressure was increased. As the pressure is increased, the engine is effectively working across a lower temperature difference.

The temperature curves in Figure 5.10 slope downwards near the end of their frequency ranges. In these areas, the temperature drops decrease even though the average mass flow rate through the heat exchangers has increased. The trend could indicate a laminar to turbulent transition or some other change in the fluid flow phenomena, which improves the heat transfer rate above a threshold frequency.

The measured temperature drop combines a series of heat transfer processes between the working fluid, and the thermal source and sink. For the cooler, heat is transferred from the coolant to the aluminum internally finned tube via convection. The heat then conducts thorough the tube walls and fins and is finally transferred to the gaseous working fluid by convection. The heat from the heating cap must conduct from the steel heating cap to the steel heater head of the engine. It then conducts through the heater head and is convected into the working fluid of the engine.

The plots in Figure 5.10 show that the temperature drop of the heater is larger than that of the cooler for a given frequency and mean pressure. The cooler has the advantage of being made of aluminum rather than low carbon steel, giving it an approximately three times higher thermal conductivity and reducing the temperature drop during the conduction process. The walls of the cooler are also 2.5 mm compared to a thickness of 6 mm for the heater head walls. The clearance fit between the heating cap and the heater head is expected to have a large contact resistance associated with it, adding to the temperature drop from the thermal source. For convective heat transfer to the working fluid, the cooler has finer, larger aspect ratio slots than the heater, which may improve its convective heat transfer performance.

Pending further experiments in which the temperatures of solid surfaces are measured, comparison with calculations is of limited use. The current model assumes a wall temperature in the heater and cooler and models the convection process using the simple heat exchanger model described in Chapter 1. Using internal and external wall temperature measurements, the conduction and convection processes could be individually modelled and validated.

Considering Figure 5.10, the minimum thermal source temperature could potentially be reduced significantly by replacing the heater with something that closely resembled the current cooler and using a liquid thermal source. The changes in flow friction and dead volume associated with the suggested heater replacement would also affect the performance, so the resulting reduction in minimum thermal source temperature may not directly correspond to Figure 5.10. The idea is a promising, but expensive, option for reducing the minimum thermal source temperature further.

5.6 Evidence of Preferential Flow

Gheith et al., [54], noted that measured regenerator temperatures were warmer on the power cylinder side of the engine than on the bypass side during their experiments. They attributed the difference in temperature to a preferential flow on the power cylinder side of the engine [54].

Figure 5.11 presents gas temperature data taken at the cold end of the regenerator. Each column of data in the plot represents a range of engine frequencies tested at a common mean pressure. Like in Gheith et al.'s experiments, the power cylinder side of the regenerator, shown by the red stars, is typically warmer than the opposite side. The plot reveals that this difference in temperature is more pronounced at low mean pressures than at high mean pressures. In the previous section, it was shown that the pressure drop across the regenerator increases with mean pressure. This high pressure drop is expected to even out the flow more effectively, and could be the reason that the temperatures are more even on opposite sides of the regenerator at higher mean pressures.

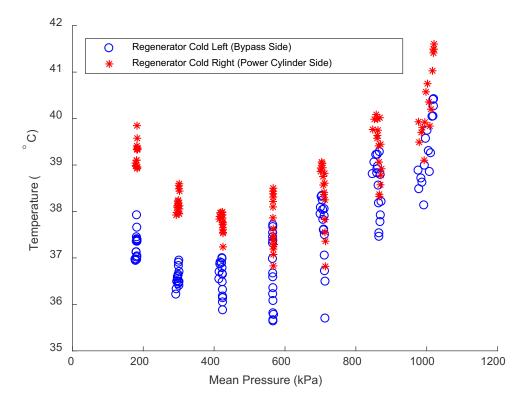


Figure 5.11: Measured Gas Temperatures at the Interface between the Regenerator and the Cooler with Engine Running at a Heating Cap Temperature of 200 °C

Evidence of preferential flow was also recorded during a cold motoring test. The engine was rotated using an electric motor at 10 Hz with a mean pressure of 414 kPa, and the pressure drop across the heater was measured. An outboard pressure transducer was connected via 1/8" stainless steel tubes to the expansion space and regenerator hot locations indicated on Figure 2.15. The test was repeated with the heater head rotated to eight azimuthal positions in 45° increments. Figure 5.12 is a polar plot showing the measured heater pressure drops in kPa. The higher pressure drop on the power cylinder side of the engine suggests a higher flow rate of gas through the regenerator on that side.

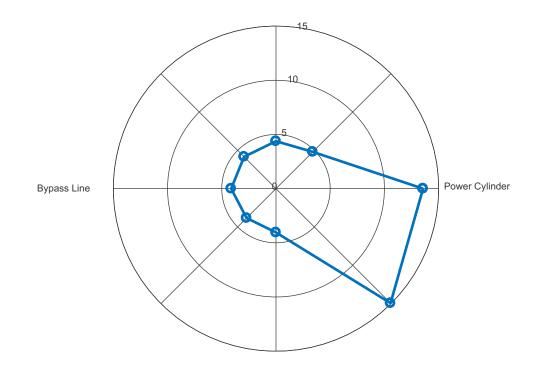


Figure 5.12: Measured Heater Pressure Drop Amplitude (in kPa) as a Function of Azimuthal Position

The preferential flow found by Gheith et al., [54], has been confirmed by measurements here. It has been shown that the issue is more significant at lower mean pressures. There is a larger opening at the bottom of the cooler on the power cylinder side due to the presence of the connecting pipe. This is expected to be the cause of the preferential flow towards that side.

5.7 Heat Lost Through the Heating Cap Insulation

Some of the heat supplied by the cartridge heaters does not enter the engine at all, rather it escapes into the surrounding air through the insulation. This loss mechanism was not accounted for in the model, but it was measured by comparing the heat input and rejection rates with the engine stationary. The measured heat loss rate is displayed as a function of heating cap setpoint in Figure 5.13 below.

It is expected that the heat loss rate will monotonically increase as the heating cap setpoint increases. The plot shows a slight decline in the heat loss rate between the heating cap setpoints of 250 °C and 300 °C. This is because the insulation was removed and refitted during the conduction loss testing which spanned several days. The 300 °C data point was collected before the insulation was removed and reinstalled, and the remaining 4 data points were collected post reinstallation.

The results convey that the heat lost through the insulation is significant. At best, it is about 31 % of the heat input for this stationary test. The problem can be reduced by adding additional layers of insulation or by substituting an alternative product with a higher thermal resistance.

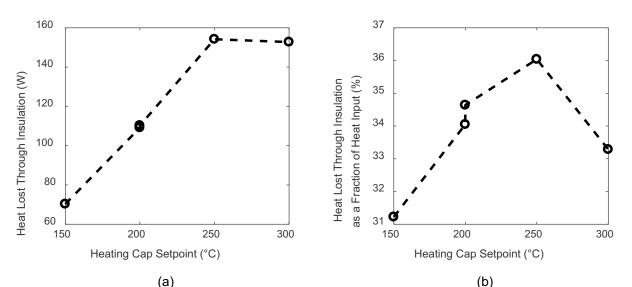


Figure 5.13: Measured Heat Loss Rate Through the Heating Cap Insulation Expressed as (a) An Energy Transfer Rate and (b) A Fraction of the Heat Input Rate

5.8 Conduction loss

The conduction loss was measured using the same procedure as the heat loss through the heating cap insulation. The engine was held stationary at operating temperature and the heat input and output rates were measured. The rate of heat removed by the coolant during the test represents the conduction loss of the engine.

In the model, the conduction loss was estimated using a one-dimensional Fourier's Law approach based on the average thermal conductivities of the relevant engine components. To compare the model to experimental results, the measured gas temperatures above and below the regenerator were used as the hot and cold side temperatures for the calculation of conduction through the regenerator and walls of the regenerator cavity. The measured gas temperatures of the expansion space and displacer mount were used for the calculation of heat conduction through the displacer.

Figure 5.14 (a) shows the measured conduction loss with the model overlaid. The model is observed to overestimate the conduction loss for the heating cap temperatures studied. A more complete experiment would include measurements of the wall temperatures during the experiment, and a more complete model would include multi-dimensional conduction, contact resistances, and temperature dependent material properties. Figure 5.14 (b) expresses the measured conduction loss rate as a fraction of the measured heat input. The fraction of input heat conducted away increases as the heating cap setpoint declines.

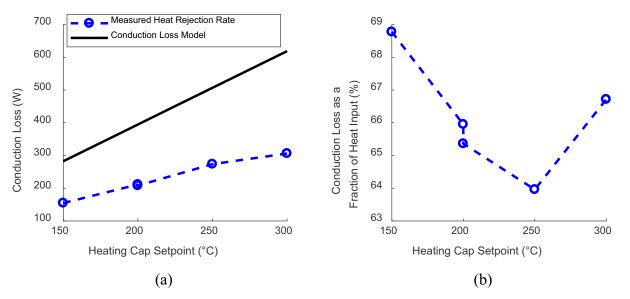


Figure 5.14: (a) Comparison between Measured and Calculated Conduction Loss Rate and (b) Measured Conduction Loss Rate Expressed as a Fraction of the Measured Heat Input

Since the gas and wall temperatures are different when the engine is running from when it is stationary, the results of this experiment will inherently have some error. It is expected that the temperature differences across the conduction paths will be less when the engine is running and so the true conduction loss will be less than that measured in a stationary test.

5.9 Relative Influence of the Cooling Zones

The water jackets of the engine were grouped into two cooling zones for testing. The first zone was the cooler water jacket, and the second zone was comprised of the connecting pipe and power cylinder water jackets connected in series. In the second zone, water flowed through the power cylinder before flowing through the connecting pipe. In both zones, water flowed from bottom to top. Each zone was circulated using an peristaltic pump, and had temperature measurements at the inlet and outlet.

Provision for water jackets complicates the engine design considerably. It is desirable to know the relative influence of the two zones under different operating conditions, so that informed decisions can be made during the water jacket design of future engines. Figure 5.15 plots the portion of the total heat rejected in the connecting pipe/power cylinder as a function of engine frequency and mean pressure. Data for the plot was collected at a heating cap temperature of 200 °C. As the pressure increases, a larger portion of the total rejected heat is removed by the connecting pipe/power cylinder zone. The trend can be explained with reference to Figure 5.10. At higher mean pressures, the average gas temperature in the cooler is higher and the working gas exits the cooler at a higher temperature. This allows the connecting pipe and power cylinder to remove a greater share of the reject heat.

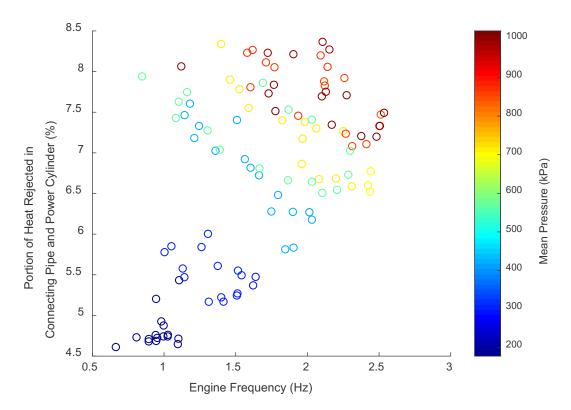


Figure 5.15: Portion of Heat Rejected in the Connecting Pipe and Power Cylinder as a Function of Engine Frequency and Mean Pressure for a Heating Cap Temperature of 200 °C

5.10 Discussion of Losses Not Measured

Ideally, each sub-component of a second order model would be validated independently to obtain improved agreement between predicted and measured overall engine performance. Using this approach, sources of error in the model are isolated; therefore, subsequent efforts to improve the model may be focused on components which contribute the largest errors. The research presented here followed this scheme as much as possible when comparing models to experimental data. The losses that were not measured are discussed in this subsection.

Regenerator enthalpy loss is calculated using the simple heat exchanger model described in Chapter 1, but it has not been measured. Measurement of this loss would require instantaneous temperature measurements collected at the hot and cold ends of the regenerator while the engine was running. From these the regenerator effectiveness could be calculated and used to quantify the regenerator enthalpy loss. The response time of the current thermocouples is too slow to use this approach.

Validation of the appendix gap loss would involve instantaneous temperature and flow field measurements in the appendix gap. This could potentially be achieved using optical diagnostic techniques, but replicating the engine conditions while remaining optically transparent would be difficult. Recall that the purpose of the appendix gap is to prevent the seal on the displacer from getting too hot. In low thermal source temperature applications, this is less of a concern. The appendix gap could potentially be removed altogether, eliminating the loss mechanism.

Seal leakage was not investigated through modeling or experiments in this research. Leakage past the displacer, leakage past the piston and displacer drive rod, and leakage of working fluid into the surrounding room are all expected to affect the performance of the real engine. Numerically, seal leakage could be accounted for during the reference cycle calculations, provided that the relation between leakage mass flow rate and pressure difference across the seal was known. Experimentally, the effects of seal leakage could be measured by introducing leaks of known size into the engine and measuring the resulting performance.

Heat transfer hysteresis, which is gas spring hysteresis in the working space, has not been calculated or measured. Like the gas spring hysteresis of the crankcase measured earlier, its calculation would involve evaluating the heat transfer and viscous dissipation processes occurring inside the engine as it was running. The calculations await the creation of a far more detailed model of the engine. In the meantime, an empirical approach could be taken, like that used for the crankcase. An option would be to spin the engine at operating temperature and pressure with the displacer held stationary, and measure the indicator diagram in the power cylinder. If this was done for a range of frequencies, temperatures, and pressures an empirical formula could be obtained via curve fitting.

Imperfect heat transfer losses are calculated using the simple heat exchanger model described in Chapter 1. Wall temperatures in the heater and cooler are assumed to be constant throughout the calculation. Experimental validation would involve gas, and wall temperature measurements. Ideally, these would be instantaneous. Using the calculated mass flow rate and surface area, and the measured wall and gas temperatures, the convective heat transfer coefficients of the heater and cooler could be determined, and their performance could be assessed.

Flow friction in the connecting pipe and cylinder head is absent from the model and the experimental data. A quasi-steady approach like that used for the heater, cooler, and regenerator could be implemented in the model as a starting point. Measurement would be possible using high speed differential pressure measurements across the associated components.

Piston finite speed loss was not included in the model nor was it measured. It is difficult to devise a measurement technique which could isolate losses caused by the speed of the piston from gas spring hysteresis and flow friction. The derivation of the equations used by other researchers could not be found by the current author, leading to skepticism of their validity. Since second order models typically overshoot experimental data, the addition of any small loss mechanism will often improve agreement if only overall shaft power and efficiency are used in the validation.

5.11 Overall Engine Performance

The section below presents plots related to the overall engine performance. Specifically, measurements of the torque, shaft power, heat rejection rate, and thermal efficiency will be presented. Comparisons will also be made to the results of the second order model. Significant errors in the model have already been identified in previous subsections. Discrepancies in overall performance results represent the accumulation of these sub-component errors.

Torque measurements as a function of engine frequency and mean pressure are plotted in Figure 5.16 below. Data for the plot was collected at a heating cap temperature of 200 °C. It is observed that peak torque occurs at minimum engine frequency. This is where the effective temperature difference is the highest and the frequency dependent losses of flow friction are the lowest. If seal leakage was significant, the torque would be expected to drop off at low speeds due to increased mass leakage per cycle. The torque curves increase with mean pressure at a diminishing rate, with the highest two mean pressures giving torque curves that are nearly identical. Increasing the pressure allows the working gas to carry more energy per unit volume. This benefit comes at the cost of reduced heat exchanger performance, as demonstrated in Figure 5.10. Eventually, further elevation of the mean pressure will decrease the torque, and an optimum mean pressure will be discovered. This optimum pressure lies above the maximum rated pressure of the engine for the conditions tested.

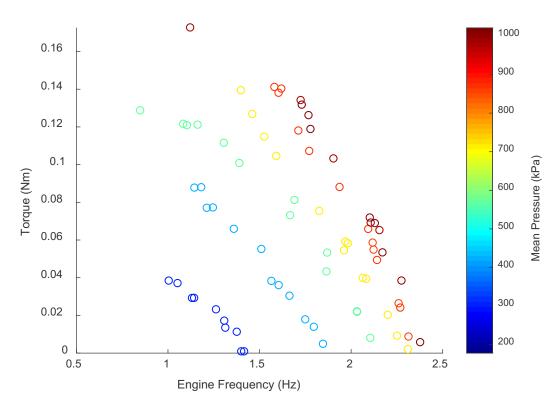


Figure 5.16: Measured Torque as a Function of Engine Frequency and Mean Pressure for a Heating Cap Temperature of 200 °C

Figure 5.17 plots measured shaft power as a function of engine frequency and mean pressure for the same data set. Shaft power declines sharply with engine frequency at this heating cap temperature as a direct result of the sharp decline in torque shown on the previous figure. The peak power frequency increases with mean pressure because flow friction and other speed dependent losses constitute a reduced fraction of the power output. Again, the benefit of increasing mean pressure is less pronounced towards the upper limit of the pressures tested, forecasting an optimum will be reached if pressure is elevated further.

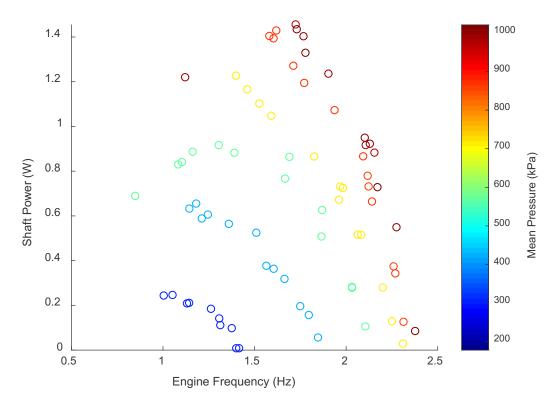


Figure 5.17: Measured Shaft Power as a Function of Engine Frequency and Mean Pressure for a Heating Cap Temperature of 200 °C

The thermal efficiency of the engine was measured by recording the average torque and heat input over a 30-minute run at approximately constant speed. For these experiments, the sampling rate for all measurements was reduced to 10 Hz, to reduce the size of the data files. At this sampling rate, speed could not be measured using the rotary encoder because missed pulses made crank position uncertain. Instead, the speed was measured before and after the test using the normal voltage sampling rate of 30 000 Hz. If the two speeds differed, the average was taken to be the speed of the test. The maximum difference between the start and end speeds of the seven efficiency tests was 0.2 Hz. Speeds were adjusted before each test using the brake. All efficiency tests were performed with a heating cap temperature of 300 °C, and a mean pressure of 430 ± 10 kPa.

Figure 5.18 plots the results of the thermal efficiency tests as a function of engine frequency. The measured thermal efficiency is less than 0.5 % under these conditions. The low efficiency values are attributed to the high heat losses through conduction and the heating cap insulation.

Appendix gap losses, and regenerator enthalpy losses also reduce the efficiency, but have not been experimentally quantified. For comparison, the Carnot efficiency at the same source and sink temperatures is 49 %. The Carnot efficiency at maximum power, calculated using the Curzon-Ahlborn relation [91], is 28 %. The two lowest frequency data points have different measured thermal efficiencies even though they were collected under the same conditions. The speeds between the two tests were the same on average, but they had different start and end speeds. One test had a frequency of 1.25 Hz at the beginning and the end of the run, while the other started the run at 1.2 Hz and finished it at 1.3 Hz. This speed difference could be the cause of the discrepancy between the two efficiency data points.

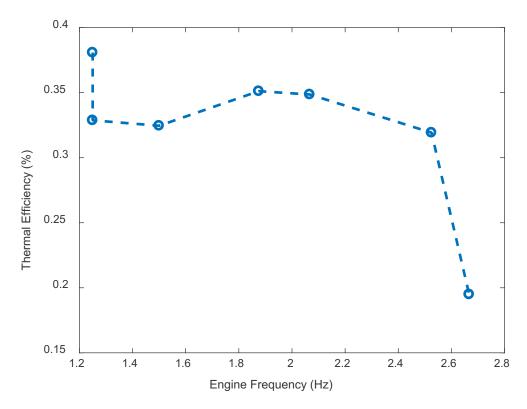


Figure 5.18: Measured Thermal Efficiency as a Function of Engine Frequency for a Heating Cap Temperature of 300 °C and a Mean Pressure of 430 kPa

The remaining plots in this section will compare experimental results to those found using the final version of the second order model. The model used the ideal adiabatic reference cycle and the decoupled losses were calculated and incorporated as described in Chapter 3, except for the following modifications:

- The heater and cooler gas temperatures were used in the walls of the regenerator cavity conduction loss calculation, rather than the thermal source and sink temperatures. The resulting conduction loss was still an overestimate compared to what was measured, but the error was reduced.
- 2. The empirical model for the crankcase hysteresis loss was implemented.
- 3. The measured heat loss through the insulation was included as a constant added to the reference cycle heat input. 135 W was added for a heating cap temperature of 300 °C, and 90 W was added for a heating cap temperature of 200 °C.

Operating conditions from the experiments were input to the model in the following way.

- 1. The average pressure measured at the power cylinder outboard pressure transducer was taken to be the mean cycle pressure in the model.
- 2. The measured engine frequency was taken to be the frequency in the model.
- 3. The measured gas temperature at the regenerator hot thermocouple location was taken to be the heater wall temperature in the model.
- 4. The average of the measured gas temperatures at the regenerator cold left and the regenerator cold right locations was taken to be the cooler wall temperature in the model.
- 5. The measured gas temperature at the expansion space thermocouple location was taken as the expansion space temperature in the model.
- 6. The measured gas temperature at the displacer mount thermocouple location was taken to be the compression space gas temperature in the model.
- 7. The average of the measured gas temperatures at the expansion space and regenerator hot thermocouple locations was taken to be the heater gas temperature in the model.
- 8. The measured gas temperatures at the regenerator cold left and regenerator cold right thermocouple locations were averaged, and the result was averaged with the measured gas temperature at the displacer mount thermocouple location to calculate the cooler gas temperature for input to the model.

In Figure 5.19, the measured heat input rate has been plotted with corresponding results from the second order model as a function of engine frequency. The red stars represent experimental data and the blue circles represent model results. The plot was produced using the same data set

as for Figure 5.18. The model overestimates the heat input rate for all conditions tested. This is partly due to the overestimation of the conduction loss highlighted in a previous section, and may also be the result of losses neglected in the model. There is no clear trend with frequency in either the data or the model, and the error in the model is approximately constant for the conditions tested.

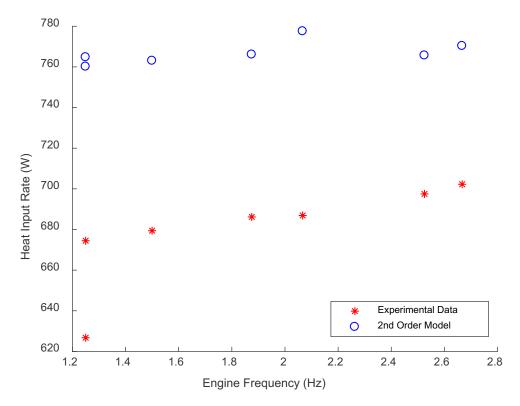


Figure 5.19: Measured Heat Input Rate with Overlaid Second Order Model for a Heating Cap Temperature of 300 °C and a Mean Pressure of 430 kPa

In Figure 5.20, the measured thermal efficiency has been overlaid by corresponding second order model results. The data and the model follow a similar trend, both indicating an optimum speed of approximately 2.1 Hz, where the thermal efficiency is maximized. The second order model over-predicts the measured thermal efficiency for the conditions tested. Since it has already been shown in Figure 5.19 that the model overestimates the heat input, this means that the power output must also be overstated by the second order model.

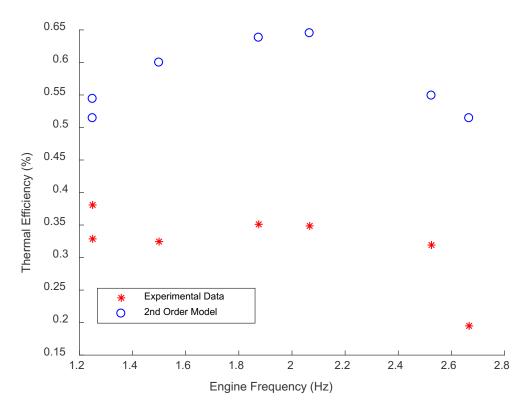


Figure 5.20: Measured Thermal Efficiency with Overlaid Second Order Model for a Heating Cap Temperature of 300 °C and a Mean Pressure of 430 kPa

Figure 5.21 plots measured shaft power overlaid with corresponding results from the second order model. Data for the plot was recorded with the heating cap temperature at 200 °C. Data and model follow similar trends and indicate similar maximum power frequencies. The model overestimates the experimental results under all conditions tested. Causes of shaft power overestimation include neglect of losses such as seal leakage, heat transfer hysteresis, and flow friction in the connecting pipe and power cylinder head, as well as inaccurate calculation of losses such as mechanical friction and flow friction, due to unrealistic reference cycle results and simplifying assumptions.

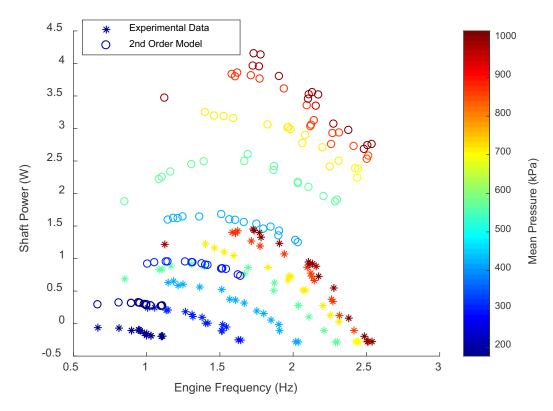


Figure 5.21: Measured Shaft Power as a Function of Engine Frequency and Mean Pressure with Overlaid Second Order Model. Data was collected at a heating cap temperature of 200 °C.

The measured total heat rejection rate is compared with results from the second order model in Figure 5.22. The plot shows that the total heat rejection rate is overestimated by the model for all conditions tested. The trends followed differ between the data and the model. The experimental data shows a clear increase in heat rejection rate with increasing mean pressure. Mean pressure dependence is not exhibited by the second order model results. A pressure dependent loss mechanism may be missing from the heat rejection rate calculation, or the pressure dependence in one of the included loss mechanisms may be underrepresented due to the assumptions made. The experimental data also shows a decrease in the heat rejection rate above a threshold engine frequency which depends on the mean pressure. This is indicative of a change in flow phenomena on the gas side of the heat exchanger. The model uses Reynolds analogy with a turbulent steady flow friction factor correlation for all engine frequencies; hence, changes in flow regime are not represented.

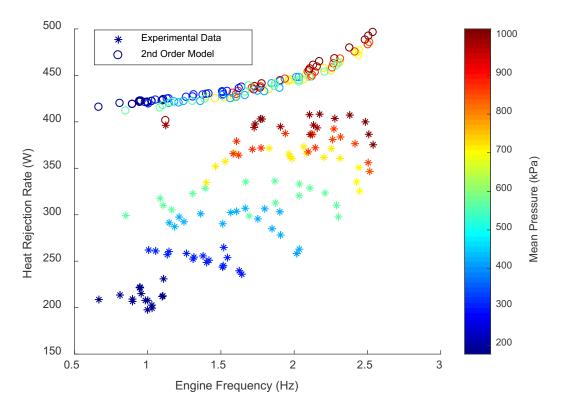


Figure 5.22: Measured Heat Rejection Rate as a Function of Engine Frequency and Mean Pressure with Overlaid Second Order Model. Data was collected at a heating cap temperature of 200 °C.

5.12 Conclusions

Experimental results have been compared to model predictions to assess agreement. Effort was focused on evaluating individual components of the model, in addition to overall results. Significant discrepancies between measured and modeled results were discovered in several areas. Of these, indicator diagram prediction was the most influential, since most other calculations are based on its results. Indicator diagram prediction accuracy was observed to decline with thermal source temperature, due to the greater influence of neglected decoupled losses at lower temperature difference operating points.

To further improve the low thermal source temperature performance of the engine, it is recommended that the heater head be replaced with something similar to the cooler. The aims of the modification would be to reduce temperature drop from the thermal source to the heater gas, and decrease conduction loss and heat loss through the insulation. Resulting changes in dead volume and flow geometry will have unknown effects.

Chapter 6. Conclusions and Future Work

This research was conducted with the intent of addressing two main issues. The first was the applicability of commonly used second order models to Stirling engines with thermal source temperatures less than 150 °C. The second was the identification of modifications necessary to improve the low thermal source temperature performance of the ST05G-CNC Stirling engine. The problems were investigated experimentally.

It was shown that the assumption of decoupled losses, fundamental to the second order modeling approach, breaks down at low thermal source temperatures. Under these conditions, both the ideal adiabatic and the ideal isothermal reference cycles significantly overestimate the measured indicated work of the cycle. The discrepancy was attributed to the absence of losses in the reference cycle calculation. The influence of these losses on the reference cycle results becomes greater as the thermal source temperature declines. Since nearly all the decoupled losses rely on the reference cycle for their input parameters, inaccuracies are far-reaching. Further model validation awaits improvement of the reference cycle simulation.

Experiments proved that the minimum thermal source temperature of the engine could be reduced by reducing the piston diameter and increasing the crankcase volume. These modifications were shown to reduce the amount of forced work and crankcase gas spring hysteresis, leading to a performance improvement at low thermal source temperatures. The measured shaft power was unaffected by the addition of dead volume reduction components in the connecting pipe, displacer mount, and power cylinder head. A suggested further modification is to replace the heater head with something resembling the cooler, with the aim of reducing temperature drop between the thermal source and the heater gas, the conduction loss, and the heat lost through the insulation. The significance of these loss mechanisms was shown using experimental results. The change would also facilitate a liquid thermal source.

Future work on these topics could include:

- 1. Measurements of wall temperatures, and faster response gas temperatures inside the engine for characterization of convective heat transfer processes.
- 2. Experiments and modeling to study the effects of seal leakage, heat transfer hysteresis, and changes in thermal sink temperature.
- 3. Optimization of the regenerator properties for low thermal source temperatures.

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Appendix A: Analysis of Experimental Uncertainty

Introduction

The following uncertainty analysis follows the procedure documented by Wheeler and Ganji [1]. The propagation of uncertainty may be quantified using the root sum of squares error given by

$$w_{Z} = \left(\sum_{i=1}^{n} \left[w_{x_{i}} \frac{\partial Z}{\partial x_{i}}\right]^{2}\right)^{\frac{1}{2}}$$
(A.1)

where Z is the result calculated from n measured variables, x_i , and w is the uncertainty associated with the variable indicated by the subscript.

If Z is calculated by multiplying measured variables only, i.e.

$$Z = C x_1^{\ a} x_2^{\ b} \dots x_n^{\ N} \tag{A.2}$$

then Eq. (A.1) reduces to

$$\frac{w_{Z}}{Z} = \left\{ \left(a \frac{w_{1}}{x_{1}} \right)^{2} + \left(b \frac{w_{2}}{x_{2}} \right)^{2} + \dots + \left(N \frac{w_{n}}{x_{n}} \right)^{2} \right\}^{\frac{1}{2}}$$
(A.3)

The following sections give the error propagation equation for each calculated result. They also list potential error sources and their potential contributions to the uncertainty for each type of base measurement. Data is presented in tables for simplicity.

Temperature Drop

Definition of Functional Relationship

Temperature drops are calculated using equations of the form

$$\Delta T = T_1 - T_2 \tag{A.4}$$

where T_1 and T_2 are the measured working fluid or coolant temperatures.

Estimation of Uncertainties in Measured Variables

Table A.1 Estimated Uncertain		Uncertainty	
Sources of Error	Error Type	Contribution	Comments
		(°C)	
standard deviation/noise	random	0.03	Calculated using calibration
standard deviation/horse	Tandom	0.05	data
spatial variation	systematic	_	Most significant for heating
spatial valiation	systematic		cap thermocouple.
			Only significant for heater
conduction	systematic	-	Only significant for heater head thermocouples. More significant at higher heating cap temperatures. Mitigated by taking the
conduction			
			cap temperatures.
quantization rand	random	dom -	Mitigated by taking the
1			average at steady state.
time constant	systematic	_	Mitigated by taking the
			average at steady state.
radiation	systematic	-	Only significant for heater
	<i>.</i>		head thermocouples.
differences between			Mitigated by applying
thermocouples	systematic -	-	calibration terms to the raw
-			data
Standard Accuracy from	random	4	Greater of ± 2.2 °C or ± 0.75
Manufacturer [2]			%[2]

Table A.1 Estimated Uncertainties for Thermocouple Measurements

Total Uncertainty	5 °C (10 °C for heating cap temperature due to	
rotar Uncertainty	increased spatial variation)	

Table A.2 Estimated Uncertain		Uncertainty	
Sources of Error	Error Type	Contribution	Comments
		(°C)	
standard deviation/noise	random	0.03 Calculated using calibrati	Calculated using calibration
standard deviation/horse	Tandom	0.03	data
			Not significant since cross-
spatial variation	systematic	-	sectional area of stream is
			small
conduction	systematic	_	Not significant since water is
Conduction	Systematic		near ambient temperature
quantization	random	_	Mitigated by taking the
			average at steady state.
time constant	time constant systematic	_	Mitigated by taking the
			average at steady state.
radiation	systematic	-	Not significant since water is
	-		near ambient temperature
differences between			Mitigated by applying
RTDs	systematic -	-	calibration terms to the raw
			data
Accuracy stated by	random	0.8	Class B Accuracy [3]
manufacturer [3]			
Total Uncerta	ainty		1 °C

Table A.2 Estimated Uncertainties for RTD Measurements

Propagation of Uncertainty

Applying Eq. (A.1) to Eq. (A.4) yields

$$w_{\Delta T} = \left\{ \left(w_{T_1} \right)^2 + \left(-w_{T_2} \right)^2 \right\}^{\frac{1}{2}}$$
(B.5)

Since the same instruments and procedures are used to measure temperatures T_1 and T_2 , it will be assumed that they have the same uncertainty, i.e.

$$w_{T_1} = w_{T_2} = w_T$$

 W_{T_1} This allows simplification of Eq. (A.5)

$$w_{\Delta T} = \{(w_T)^2 + (-w_T)^2\}^{\frac{1}{2}} = \{2(w_T)^2\}^{\frac{1}{2}} = \sqrt{2}w_T$$
(A.6)

Table A.3: Inputs and Results for Uncertainty Propagation in Temperature Difference

W_T (gas temperatures)	0.01 °C
w_T (water temperatures)	0.01 °C
Propagated Uncertainty, $W_{\Delta T}$	0.014 °C

Pressure

The pressure measurements are not used for further calculations, so no uncertainty propagation calculations are shown in this section.

Estimation of Uncertainties in Measured Variables

Table A.4 Estimated Uncert	ain	ties for Validyne Pressu	ire Measurements	\$
				· · · ·

		Uncertainty				
Sources of Error	Error Type	Contribution	Comments			
		(kPa)				
noise	random	_	Mitigated by taking the			
noise	Tandom	_	average at steady state.			
			Assumed to be negligible			
spatial variation	systematic	_	since pressure drops are small			
spatial variation	systematic		in regions characterized by a			
			single pressure measurement.			
connection tube losses	systematic	_	Mitigated by taking the			
	systematic		average at steady state.			
			0.07 kPa = 0.01 PSI, which is			
calibration machine	random 0.	0.07	the resolution of the machine			
			display.			
quantization	random	- Mitigated by taking the	Mitigated by taking the			
quantization	Tandom	0.07 the resolution of the machine display. - Mitigated by taking the average at steady state. - Mitigated by taking the average at steady state. - Mitigated by taking the average at steady state.				
time constant	systematic	_	Mitigated by taking the			
time constant	systematic	nauc -	average at steady state.			
		\pm 0.25 % Full				
		Scale	Calculated using 10 bar as			
Accuracy stated by manufacturer [4]		= 2.5 kPa for	full scale value for absolute			
	random	absolute	transducers and 5 psi for			
		= 0.0862 kPa	differential transducer			
		for				
		differential				

Total Uncertainty	5 kPa for absolute measurement, 0.01 kPa for
rotar Uncertainty	differential measurement

Uncertainty **Sources of Error Error Type** Contribution Comments (kPa) standard deviation/noise random Assumed negligible. -Assumed to be negligible since pressure drops are spatial variation small in regions systematic characterized by a single pressure measurement. Mitigated by taking leak down time measurements with engine at random _ steady state. Assumed negligible. quantization random _ mean pressure determined 5 random from Validyne transducers Resolution stated by the ± 0.007 random manufacturer [5] **Total Uncertainty** 5.01 kPa

Table A.5: Estimated Uncertainties for PCB Pressure Measurements

Engine Frequency

Definition of Functional Relationship

$$f = \frac{\Delta\theta}{t} \tag{A.7}$$

Estimation of Uncertainties in Measured Variables

Table A.6 Estimated Uncertainties for Crankshaft Position Measurement

Sources of Error	Error Type	Uncertainty Contribution (°)	Comments
noise	random	-	not significant since only counting pulses of 5 V.
belt stretch/alignment	random	<u>+</u> 5	Alignment is done by looking at the crankshaft with thecrankcase cover removed.
quantization	random	-	not significant since only counting pulses of 5 V.
Total Uncertainty			5 °

Table A.7 Estimated Uncertainties for Time Measurement

Sources of Error	Error Type	Uncertainty Contribution (s)	Comments
electrical/software lag	systematic	0.001	
Total Uncertainty			0.001 s

Propagation of Uncertainty

$$w_{\omega} = \left\{ \left(w_{\Delta\theta} \frac{\partial f}{\partial \Delta\theta} \right)^2 + \left(w_t \frac{\partial f}{\partial t} \right)^2 \right\}^{\frac{1}{2}} = \left\{ \left(w_{\Delta\theta} \frac{1}{t} \right)^2 + \left(-w_t \frac{1}{t^2} \right)^2 \right\}^{\frac{1}{2}}$$
(A.8)

 Table A.8: Inputs and Results for Uncertainty Propagation in Angular Frequency

$w_{\Delta\theta}$ (uncertainty in crank angle increment)	0.0873 rad (5 °)
w_t (uncertainty in time)	0.001 s
t (maximum measured time)	10 s
Propagated Uncertainty , w_{ω}	0.0087 rad/s

Power Measurement

Definition of Functional Relationship

$$\dot{W} = \tau \omega \tag{A.9}$$

Estimation of Uncertainties in Measured Variables

Table A.9 Estimated Uncertainties for Torque Measurement

Sources of Error	Error Type	Uncertainty Contribution (Nm)	Comments
quantization	random		Mitigated by taking the average at steady state.
response time	systematic		Mitigated by taking the average at steady state.
Inconsistent speed during power measurement	random		Inertia of the engine and output shaft can affect torque measurement during changes in speed
Manufacturer Data Sheet [6]	random	0.05 Nm	Nonlinearity \pm 0.2% of RO Hysteresis \pm 0.1% of RO Nonrepeatability \pm 0.2% of RO [6] added together to get full uncertainty
Total Uncertai	nty		0.05 Nm

Propagation of Uncertainty

$$w_{\dot{W}} = \dot{W} \left\{ \left(\frac{w_{\tau}}{\tau}\right)^2 + \left(\frac{w_{\omega}}{\omega}\right)^2 \right\}^{\frac{1}{2}}$$
(A.10)

w_{τ} (uncertainty in torque)	0.05 Nm
τ (maximum measured torque)	2 Nm
w_{ω} (uncertainty in angular frequency)	0.0087 rad/s
ω (maximum measured angular frequency)	31.4 rad/s (10 Hz)
Propagated Uncertainty , <i>w</i> _W	0.25 W

Table A.10: Inputs and Results for Uncertainty Propagation in Shaft Power

Heat Input Rate

Definition of Functional Relationship

$$\dot{Q}_{in} = I^2 R \left(\frac{time \ on}{total \ time} \right) = I^2 R t_{frac} \tag{A.11}$$

Estimation of Uncertainties in Measured Variables

Sources of Error	Error Type	Uncertainty Contribution (A)	Comments
Manufacturer Specified Accuracy [7]	random	0.33	2 %
Total Uncertainty			0.4 A

Table A.11 Estimated Uncertainties for Current Measurements

Sources of Error	Error Type	Uncertainty Contribution (Ω)	Comments
temperature dependent resistance	systematic	-	Resistance depends on temperature. Heater wire material is unknown and high temperature measurements were deemed too dangerous.
Manufacturer data sheet [8]	random	0.058	0.05 Ohms + 8 digits [8]
Total Uncert	tainty		0.1 Ω

Propagation of Uncertainty

$$w_{t_{frac}} = \left\{ \left(\frac{w_t}{t_{eff}} \right)^2 + \left(w_t \frac{t_{on}}{t_{eff}^2} \right)^2 \right\}^{\frac{1}{2}}$$
(A.12)

$$w_{P_{heater}} = \{(2w_I I R)^2 + (w_R I^2)^2\}^{\frac{1}{2}}$$
(A.13)

$$w_{\dot{Q}_{in}} = \dot{Q}_{in} \left\{ \left(\frac{w_{P_{heater}}}{P_{heater}} \right)^2 + \left(\frac{w_{t_{frac}}}{t_{frac}} \right)^2 \right\}^{\frac{1}{2}}$$
(A.14)

 w_t (uncertainty in time) 0.001 s t_{eff} (total time for heat input measurement) 1 800 s t_{on} (maximum time heater is on during heat 280 s input measurement) $w_{t_{frac}}$ (uncertainty in fraction of time heater is 5.62e-7 s on) w_I (uncertainty in current) 0.4 A *I* (maximum measured current) 16.5 A *R* (maximum measured resistance) 12.088 Ω w_R (uncertainty in resistance) 1Ω $W_{P_{heater}}$ (uncertainty in heater power 316 W consumption) t_{frac} (maximum fraction of time heater is on) 0.156 **Propagated Uncertainty**, *w*_{*Qin*} 48.5 W

Table A.13: Inputs and Results for Uncertainty Propagation in Heat Input Rate

Heat Rejection Rate

Definition of Functional Relationship

$$\dot{Q}_{out} = \dot{V}\rho c\Delta T \tag{A.15}$$

Estimation of Uncertainties in Measured Variables

Table A.14 Estimated Uncertainties for Volume Flowrate Measurements

Sources of Error	Error Type	Uncertainty Contribution (L/min)	Comments
Calibration, air bubbles, tubing alignment, etc.	random	0.01	Estimate based on calibration
Total Uncertainty			0.01 L/min.

Table A.15 Estimated Uncertainties for Coolant Density, ρ

Sources of Error	Error Type	Uncertainty Contribution (kg/m ³)	Comments
temperature			
impurities			
air bubbles			
pressure			
Total Uncer	tainty		5 kg/m ³

Table A.16 Estimated Uncertainties for Coolant Specific Heat Capacity

Sources of Error	Error Type	Uncertainty Contribution (J/kgK)	Comments
temperature			
impurities			

air bubbles		
pressure		
Total Uncer	tainty	5 J/kgK

Propagation of Uncertainty

$$w_{\dot{Q}_{out}} = \dot{Q}_{out} \left\{ \left(\frac{w_{\dot{V}}}{\dot{V}} \right)^2 + \left(\frac{w_{\rho}}{\rho} \right)^2 + \left(\frac{w_c}{c} \right)^2 + \left(\frac{w_{\Delta T}}{\Delta T} \right)^2 \right\}^{\frac{1}{2}}$$
(A.16)

Table A.17: Inputs and Results for Uncertainty Propagation in Heat Rejection Rate

$w_{\dot{V}}$ (uncertainty in volume flow rate)	$1.67e-8 \text{ m}^3/\text{s}$
\dot{V} (maximum measured volume flow rate)	1.33e-5 m ³ /s
w_{ρ} (uncertainty in coolant density)	5 kg/m ³
ρ (maximum coolant density)	1000 kg/m ³
w_c (uncertainty in coolant specific heat capacity)	5 J/kgK
<i>c</i> (maximum coolant specific heat capacity)	4184 J/kgK
$w_{\Delta T}$ (uncertainty in coolant temperature rise)	0.014 °C
ΔT (maximum measured coolant temperature rise)	5 °C
Propagated Uncertainty, <i>w</i> _{<i>Q</i>_{out}}	2.40 W

Thermal Efficiency

Definition of Functional Relationship

$$\eta_{th} = \frac{\dot{W}}{\dot{Q}_{in}} \tag{A.17}$$

Propagation of Uncertainty

$$w_{\eta_{th}} = \left\{ \left(w_{\dot{W}} \frac{\partial \eta_{th}}{\partial \dot{W}} \right)^2 + \left(w_{\dot{Q}_{in}} \frac{\partial \eta_{th}}{\partial \dot{Q}_{in}} \right)^2 \right\}^{\frac{1}{2}} = \left\{ \left(\frac{w_{\dot{W}}}{\dot{Q}_{in}} \right)^2 + \left(w_{\dot{Q}_{in}} \frac{-\dot{W}}{\dot{Q}_{in}^2} \right)^2 \right\}^{\frac{1}{2}}$$
(A.18)

Table A.18: Inputs and Results for Uncertainty Propagation in Thermal Efficiency

$w_{\dot{W}}$ (uncertainty in shaft power)	0.25 W
\dot{W} (maximum measured shaft power)	10 W
$W_{Q_{in}}$ (uncertainty in heat input)	48.5 W
\dot{Q}_{in} (maximum measured heat input)	500 W
Propagated Uncertainty, $w_{\eta_{th}}$	0.002

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Appendix B: Optimum Swept Volume Ratio Based on Equal Pressure Swings

The swept volume ratio has been estimated on the assumption that the displacer and piston should each be able to change the pressure by the same amount. The formulae of West [6] were repurposed to determine the pressure swing of each reciprocating component individually. The displacer pressure swing is calculated assuming the piston is at midstroke, and vise versa.

Assumptions

- 1. The pressure swing induced by the displacer should be equal to that induced by the piston.
- 2. The ideal gas law is applicable.
- 3. Piston and displacer move individually.
- 4. No leakage.
- 5. Pressure throughout the engine is constant.

Displacer Induced Pressure Swing:

From West page 29 [6], the displacer induced pressure swing ΔP_D is given by

$$\Delta P_D \approx P_m \frac{V_D}{V_m} \frac{(T_H - T_C)}{T_m} \tag{B.1}$$

where

 P_m is the mean pressure (displacer at midstroke)

 V_D is the displacer swept volume

 V_m is the total engine volume with the piston at midstroke

 T_H is the hot space gas temperature

 T_C is the cold space gas temperature

 T_m is the effective average gas temperature with the displacer at midstroke

Piston Induced Pressure Swing:

From the ideal gas law we have

$$P_{min} = \frac{mRT_m}{V_{max}} \qquad \qquad P_{max} = \frac{mRT_m}{V_{min}} \qquad \qquad P_m = \frac{mRT_m}{V_m}$$

where

m is the mass of the working fluidR is the ideal gas constant V_{max} is the maximum total engine volume(piston at bottom dead center) V_{min} is the minimum total engine volume(piston at top dead center) P_{min} is the minimum engine pressure (pistonat BDC displacer at midstroke) P_{max} is the maximum engine pressure(piston at TDC displacer at midstroke)

Considering the piston induced pressure swing we have

$$\frac{\Delta P_P}{P_m} = \frac{P_{max} - P_{min}}{P_m} = \frac{\frac{mRT_m}{V_{min}} - \frac{mRT_m}{V_{max}}}{\frac{mRT_m}{V_m}} = \frac{\frac{1}{V_{min}} - \frac{1}{V_{max}}}{\frac{1}{V_m}}$$
$$\frac{\Delta P_P}{P_m} = V_m \left(\frac{1}{V_{min}} - \frac{1}{V_{max}}\right) = V_m \left(\frac{V_{max} - V_{min}}{V_{max}V_{min}}\right) = V_m \left(\frac{V_P}{V_{max}V_{min}}\right)$$
$$\Delta P_P = P_m V_m \left(\frac{V_P}{V_{max}V_{min}}\right) \tag{B.2}$$

where

 V_P is the piston swept volume

Equating the two pressure swings we have

$$\Delta P_D = \Delta P_P$$

$$P_m \frac{V_D}{V_m} \frac{(T_H - T_C)}{T_m} = P_m V_m \left(\frac{V_P}{V_{max} V_{min}}\right)$$

$$\frac{(T_H - T_C)}{T_m} = \frac{V_m^2}{V_D} \left(\frac{V_P}{V_{max}V_{min}}\right)$$
(B.3)

The volumes V_{max} , V_{min} , and V_m can be rewritten in terms of the piston swept volume and the constant volume V_c , which is the sum of the displacer swept volume and the dead volume.

$$V_m = (V_D + V_{dead}) + \frac{1}{2}V_P = V_C + \frac{1}{2}V_P$$
(B.4)

$$V_{min} = (V_D + V_{dead}) = V_C \tag{B.5}$$

$$V_{max} = (V_D + V_{dead} + V_P) = V_C + V_P$$
 (B.6)

Substituting (B.4), (B.5), and (B.6) into (B.3) yields

$$\frac{(T_H - T_C)}{T_m} = \frac{V_P}{V_D V_C} \frac{\left(V_C + \frac{1}{2}V_P\right)^2}{V_C + V_P}$$
(B.7)

To facilitate a numerical solution, equation (B.7) may be written as a third order polynomial as follows.

$$\frac{(T_H - T_C)}{T_m} = \frac{V_P}{V_D V_C} \frac{\left(V_C + \frac{1}{2}V_P\right) \left(V_C + \frac{1}{2}V_P\right)}{V_C + V_P} = \frac{V_P}{V_D V_C} \frac{\left(V_C^2 + V_C V_P + \frac{1}{4}V_P^2\right)}{V_C + V_P}$$
$$\frac{(T_H - T_C)}{T_m} = \frac{\left(V_P V_C^2 + V_C V_P^2 + \frac{1}{4}V_P^3\right)}{V_D V_C^2 + V_D V_C V_P}$$
$$T_{factor} V_D V_C^2 + T_{factor} V_D V_C V_P = V_P V_C^2 + V_C V_P^2 + \frac{1}{4}V_P^3$$
$$\left(\frac{1}{4}\right) V_P^3 + (V_C) V_P^2 + \left(V_C^2 - T_{factor} V_D V_C\right) V_P + \left(-T_{factor} V_D V_C^2\right) = 0$$
(B.8)
where
$$T_{factor} = \frac{(T_H - T_C)}{T_m}$$

Lastly, an expression for T_m is needed. Assume the isothermal model temperature profile, as shown below.

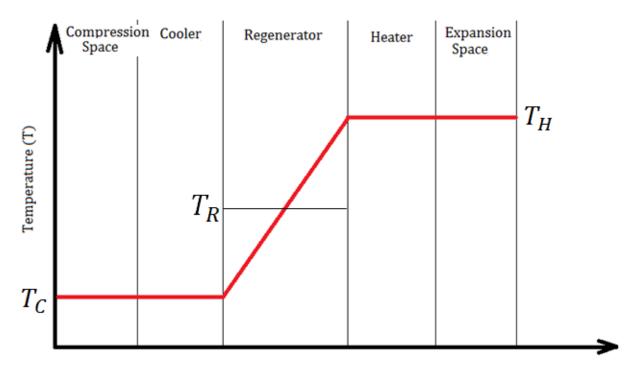


Figure A3.1.1: Isothermal Model Assumed Temperature Profile

Now consider an average temperature weighted by mass.

$$T_m = \frac{\frac{1}{2}m_D T_C + m_{cooler} T_C + m_{regen} T_R + m_{heater} T_H + \frac{1}{2}m_D T_H}{m_D + m_{cooler} + m_{regen} + m_{heater}}$$
(B.9)

where

 m_D is the mass of gas in the displacer cylinder m_{cooler} is the mass of gas in the cooler

 m_{regen} is the mass of gas in the regenerator

 m_{heater} is the mass of gas in the heater

Note that the mass of gas in the piston cylinder has not been considered here.

Using the ideal gas law to substitute for mass, reduces equation (B.9) to

$$T_{m} = \frac{\left(\frac{P\frac{1}{2}V_{D}}{RT_{C}}\right) + \left(\frac{PV_{cooler}}{RT_{C}}\right)T_{C} + \left(\frac{PV_{regen}}{RT_{R}}\right)T_{R} + \left(\frac{PV_{heater}}{RT_{H}}\right)T_{H} + \left(\frac{P\frac{1}{2}V_{D}}{RT_{H}}\right)T_{H}}{\left(\frac{P\frac{1}{2}V_{D}}{RT_{C}}\right) + \left(\frac{PV_{cooler}}{RT_{C}}\right) + \left(\frac{PV_{regen}}{RT_{R}}\right) + \left(\frac{PV_{heater}}{RT_{H}}\right) + \left(\frac{P\frac{1}{2}V_{D}}{RT_{H}}\right)}$$

$$T_m = \frac{V_D + V_{cooler} + V_{regen} + V_{heater}}{\left(\frac{\frac{1}{2}V_D}{T_C}\right) + \left(\frac{V_{cooler}}{T_C}\right) + \left(\frac{V_{regen}}{T_R}\right) + \left(\frac{V_{heater}}{T_H}\right) + \left(\frac{\frac{1}{2}V_D}{T_H}\right)}$$
(B.10)

For the regenerator temperature, the log-mean temperature will be used as recommended by Urieli and Berchowitz [10].

$$T_R = \frac{(T_H - T_C)}{\ln\left(\frac{T_H}{T_C}\right)} \tag{B.11}$$

References

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Appendix C: MATLAB Source Code for Mathematical Models

sea.m

```
function [REF CYCLE DATA, LOSSES DATA, PARTICLE TRAJECTORY DATA, ENGINE DATA]
= ...
    sea (ENGINE DATA, crank inc, Model Code, Losses Code, part traj on off)
% Israel Urieli 7/20/02 - Modified by Connor Speer April 2017
% To allow automatic iteration of the SEA code, this script has been
% converted to a function that may be called by the iteration script.
% Modified October 2017 by Connor Speer to use structures throughout and
% allow easy choice of models
%% Inputs:
% ENGINE DATA --> Structure specifying engine geometry and operating point.
% crank inc --> Crank angle step size for numerical integration in [degrees]
% Model Code --> Code specifying which model to run.
% 1 = Ideal Isothermal Model
% 2 = Ideal Adiabatic Model
% 3 = Simple Model
% Losses Code --> Code specifying which losses subfunction to run
% 0 = no loss calculations
% 1 = parasitic losses GEN.m
% 2 = parasitic losses HTG A.m
% 3 = parasitic_losses_OPA.m
% 4 = parasitic losses TER.m
% 5 = parasitic losses LTG.m
% 6 = parasitic losses FSE.m
% 7 = parasitic losses CC.m
% 8 = parasitic losses HTG B.m
\% part traj on off --> 1 if you want to run the particle trajectory
% function, 0 if you don't.
%% Outputs
% ISOTHERMAL DATA --> Structure containing results from the ideal
% isothermal model
% ADIABATIC DATA --> Structure containing results from the ideal adiabatic
% model
% SIMPLE DATA --> Structure containing results from the simple model
% LOSSES DATA --> Structure containing results from decoupled loss
% calculations
%% Set Default Output Structures to Zero
LOSSES DATA = [];
PARTICLE_TRAJECTORY_DATA = [];
```

```
%% Do preliminary calculations, define all engine parameters.
ENGINE DATA = define (ENGINE DATA);
%% Correct working fluid mass according to Paul 2015
ENGINE DATA = mass correction (ENGINE DATA, crank inc, Model Code);
switch Model Code
    case 1
    % Solve the ideal isothermal model
    REF CYCLE DATA = isothermal(ENGINE DATA, crank inc);
    case 2
    % Solve the ideal adiabatic model
   REF CYCLE DATA = adiabatic (ENGINE DATA, crank inc);
    case 3
    % Solve the simple model with regenerator enthalpy loss only
    REF CYCLE DATA = simple(ENGINE DATA, crank inc);
    otherwise
    disp('ERROR: Invalid model code.')
end
%% Calculate parasitic losses and add them to the reference cycle results
switch Losses Code
    case 0
        % Do NOTHING
    case 1
        % Use the general losses subfunction to calculate decoupled losses
       LOSSES DATA
parasitic losses GEN (ENGINE DATA, REF CYCLE DATA, crank inc);
    case 2
       % Use the unvalidated HTG engine specific losses subfunction to
calculate decoupled losses
        LOSSES DATA
                                                                              =
parasitic losses HTG(ENGINE DATA, REF CYCLE DATA, crank inc);
    case 3
        % Use the OPA engine specific losses subfunction to calculate
decoupled losses
       LOSSES DATA
                                                                              =
parasitic losses OPA(ENGINE DATA, REF CYCLE DATA, crank inc);
    case 4
       % Use the Terrapin engine specific losses subfunction to calculate
decoupled losses
       LOSSES DATA
                                                                              =
parasitic losses TER (ENGINE DATA, REF CYCLE DATA, crank inc);
    case 5
        % Use the low temperature gamma engine specific losses subfunction to
calculate decoupled losses
        LOSSES DATA
                                                                              =
parasitic losses LTG(ENGINE DATA, REF CYCLE DATA, crank inc);
    case 6
        % Use the Franchot engine specific losses subfunction to calculate
decoupled losses
```

```
LOSSES DATA
                                                                              =
parasitic losses FSE (ENGINE DATA, REF CYCLE DATA, crank inc);
    case 7
        % Use the coffee cup engine specific losses subfunction to calculate
decoupled losses
       LOSSES DATA
                                                                              =
parasitic losses CC(ENGINE DATA, REF CYCLE DATA, crank inc);
    case 8
        % Use the "validated" HTG engine specific losses subfunction to
calculate decoupled losses
       LOSSES DATA
                                                                              =
parasitic losses HTG B(ENGINE DATA, REF CYCLE DATA, crank inc);
    otherwise
        disp('ERROR: Invalid losses code')
end
%% Calculate 1-D particle trajectories and flush ratios
Num Mass Inc = 10;
```

```
if part_traj_on_off == 1
    PARTICLE_TRAJECTORY_DATA = ...
    Gen_Part_Traj(ENGINE_DATA, REF_CYCLE_DATA, Num_Mass_Inc);
end
```

The Define Function Set

define.m

```
function ENGINE DATA = define(ENGINE DATA)
% define the stirling engine geometric
% and operational parameters
% Israel Urieli 4/1/02 (April Fool's Day)
% Modified 2/12/2010 to include no-matrix regenerator awgr0
% Modified by Connor Speer April 2017. This function has been changed to
% accept an engine data structure as an input.
% Modified by Connor Speer October 2017. No more global variables.
% Calculate and display drive mechanism information
ENGINE DATA = engine (ENGINE DATA);
% Calculate and display heat exchanger and regenerator information
ENGINE DATA = heatex(ENGINE DATA);
% Calculate and display working fluid information
ENGINE DATA = gas(ENGINE DATA);
% Calculate mas of working fluid and display Schmidt analysis results
ENGINE DATA = operat(ENGINE DATA);
```

```
function ENGINE DATA = engine(ENGINE DATA)
% Define engine configuration and drive geometric parameters.
% Israel Urieli 4/14/02
% Modified by Connor Speer May 2017, October 2017
engine type = ENGINE DATA.engine type; % Engine layout and drive mechanism,
see below.
if(strncmp(engine type,'s',1)) % Sinusoidal alpha
   ENGINE DATA = sindrive(ENGINE DATA);
elseif(strncmp(engine type, 'y', 1)) % Ross yoke mechanism alpha
   ENGINE DATA = yokedrive(ENGINE DATA);
elseif(strncmp(engine type, 'r', 1)) % Ross rocker V-drive alpha
   ENGINE DATA = rockerVdrive(ENGINE DATA);
elseif(strncmp(engine type, 'g', 1)) % Sinusoidal gamma
   ENGINE DATA = gammasindrive(ENGINE DATA);
elseif(strncmp(engine type,'x',1)) % Slider-crank mechanism gamma
   ENGINE DATA = gammacrankdrive(ENGINE DATA);
elseif(strncmp(engine type, 'a', 1)) % Slider-crank mechanism alpha
    ENGINE DATA = alphacrankdrive(ENGINE DATA);
else
   fprintf('engine type is undefined\n')
end
%_____
function ENGINE DATA = sindrive(ENGINE DATA)
% Sinusoidal drive engine configuration
% Israel Urieli 4/14/02
% Connor Speer, October 2017
% SET ENGINE VOLUME AND PHASE ANGLE PARAMETERS;
Vclc = ENGINE DATA.Vclc;
Vcle = ENGINE DATA.Vcle;
Vswe = ENGINE DATA.Vswe;
Vswc = ENGINE DATA.Vswc;
alpha deg = ENGINE DATA.alpha deg;
fprintf('Sinusoidal alpha engine configuration\n')
fprintf('\nsinusoidal drive engine data summary:\n');
           comp clearence, swept vols %.1f, %.1f [cm^3]\n',
fprintf('\t
Vclc*1e6,Vswc*1e6);
                   clearence,swept vols %.1f, %.1f
fprintf('\t exp
                                                              [cm^3]\n',
Vcle*1e6,Vswe*1e6);
fprintf('\t expansion phase angle advance %.lf[degrees]\n', alpha deg);
%_____
function ENGINE DATA = yokedrive(ENGINE DATA)
% Ross yoke drive engine configuration
% Israel Urieli 4/14/02
% Connor Speer, October 2017
fprintf('Ross yoke drive engine configuration\n');
% Compression, expansion swept volumes [m^3]
```

```
Vclc = ENGINE DATA.Vclc;
```

```
Vcle = ENGINE DATA.Vcle;
b1 = ENGINE DATA.b1; % Ross yoke length (1/2 yoke base) [m]
b2 = ENGINE DATA.b2; % Ross yoke height [m]
crank = ENGINE DATA.crank; % crank radius [m]
% Diameter of compression/expansion pistons [m]
dcomp = ENGINE DATA.dcomp;
dexp = ENGINE DATA.dexp;
% Area of compression/expansion pistons [m^2]
acomp = pi*dcomp^2/4.0;
aexp = pi*dexp^2/4.0;
% Minimum yoke vertical displacement [m]
yoke = sqrt(b1^{2} + b2^{2});
ymax = sqrt((yoke + crank)^2 - b2^2);
ymin = sqrt((yoke - crank)^2 - b2^2);
% Compression, expansion swept volumes [m^3]
Vswc = acomp*(ymax - ymin);
Vswe = aexp*(ymax - ymin);
% Phase angle advance of expansion space [radians]
thmaxe = asin(ymax/(yoke + crank));
thmaxc = pi - thmaxe;
thmine = pi + asin(ymin/(yoke - crank));
thminc = 3*pi - thmine;
alpha = 0.5*(thmaxc - thmaxe) + 0.5*(thminc - thmine);
alpha deg = alpha*180/pi;
fprintf('\nRoss yoke drive engine data summary:\n');
fprintf(' yoke length b1 (1/2 yoke base) %.lf [mm]\n', b1*1e3);
fprintf(' yoke height b2 %.1f [mm]\n', b2*1e3);
fprintf(' crank radius %.1f [mm]\n', crank*1e3);
fprintf(' compression piston diameter %.1f [mm]\n', dcomp*1e3);
fprintf(' expansion piston diameter %.1f [mm]\n', dexp*1e3);
fprintf(' comp clearence,swept vols %.1f, %.1f [cm^3]\n', Vclc*1e6,Vswc*1e6);
fprintf(' exp clearence,swept vols %.1f, %.1f [cm^3]\n', Vcle*1e6,Vswe*1e6);
fprintf('ymin = \%.1f(cm), ymax = \%.1f(cm) \n', ymin*1e2, ymax*1e2)
fprintf(' alpha = %.1f(degrees) \n', alpha deg);
%_____
function ENGINE DATA = rockerVdrive(ENGINE DATA)
% Ross rocker-V drive engine configuration
% Israel Urieli 4/14/02 & Martine Long 2/14/05
% Connor Speer, October 2017
fprintf('Ross rocker-V drive engine configuration\n');
% Compression, expansion clearence vols [m^3]
Vclc = ENGINE DATA.Vclc;
Vcle = ENGINE DATA.Vcle;
crank = ENGINE DATA.crank; % crank radius [m]
```

```
% Length of comp/exp piston connecting rods [m]
conrodc = ENGINE DATA.conrodc;
conrode = ENGINE DATA.conrode;
% Diameter of compression/expansion pistons [m]
dcomp = ENGINE DATA.dcomp;
dexp = ENGINE DATA.dexp;
% Phase angle advance of expansion space [radians]
alpha deg = ENGINE DATA.alpha deg;
% Area of compression/expansion pistons [m^2]
acomp = pi*dcomp^2/4.0;
aexp = pi*dexp^2/4.0;
% Maximum comp/exp piston vertical displacement [m]
ycmax = conrodc + crank;
ycmin = conrodc - crank;
yemax = conrode + crank;
yemin = conrode - crank;
% Compression, expansion swept volumes [m^3]
Vswc = acomp*(ycmax - ycmin);
Vswe = aexp*(yemax - yemin);
fprintf('\nRoss rocker-V drive engine data summary:\n');
fprintf(' crank radius %.1f [mm]\n', crank*1e3);
fprintf(' compression piston connecting rod length %.1f [mm]\n',
conrodc*1e3);
fprintf(' expansion piston connecting rod length %.1f [mm]\n', conrode*1e3);
fprintf(' compression piston diameter %.lf [mm]\n', dcomp*1e3);
fprintf(' expansion piston diameter %.1f [mm]\n', dexp*1e3);
fprintf(' comp clearence, swept vols %.1f, %.1f [cm^3]\n', Vclc*1e6,Vswc*1e6);
fprintf(' exp clearence, swept vols %.1f, %.1f [cm^3]\n', Vcle*1e6, Vswe*1e6);
fprintf('
                                                %.1f(cm),
              COMPRESSION
                               ymin
                                        =
                                                               vmax
%.lf(cm)\n',ycmin*1e2,ycmax*1e2)
fprintf(' EXPANSION ymin = %.lf(cm), ymax = %.lf(cm) \n', yemin*le2, yemax*le2)
fprintf(' expansion phase angle advance %.1f[degrees]\n', alpha deg);
°._____
%_____
function ENGINE DATA = gammasindrive(ENGINE DATA)
% Gamma sinusoidal drive engine configuration
% Added by Connor Speer 01/06/17
% Connor Speer, October 2017
fprintf('gamma sinusoidal drive engine configuration\n')
% Piston, displacer clearence vols [m^3]
Vcld = ENGINE DATA.Vcld;
Vclp = ENGINE DATA.Vclp;
% Piston, displacer swept volumes [m^3]
Vswp = ENGINE DATA.Vswp;
```

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```

```
Vswd = ENGINE DATA.Vswd;
% Displacer Phase Angle Advance for Gamma
beta deg = ENGINE DATA.beta deg; %[deg]
fprintf('\n gamma sinusoidal drive engine data summary:\n');
fprintf(' piston clearence, swept vols %.1f, %.1f [cm^3]\n',
Vclp*1e6,Vswp*1e6);
fprintf(' displacer clearence, swept vols %.1f, %.1f [cm^3]\n',
Vcld*1e6,Vswd*1e6);
fprintf(' displacer phase angle advance %.1f[degrees]\n', beta deg);
%_____
function ENGINE DATA = gammacrankdrive(ENGINE DATA)
% Gamma crankshaft drive engine configuration
% Added by Connor Speer 02/14/17
% Connor Speer, October 2017
% Piston, displacer clearence vols [m^3]
Vclp = ENGINE DATA.Vclp;
Vcld = ENGINE DATA.Vcld;
% Piston, displacer bores [m]
Pbore = ENGINE DATA.Pbore;
Dbore = ENGINE DATA.Dbore;
% Piston, displacer desaxe offset in [m]
Pr1 = ENGINE DATA.Pr1;
Dr1 = ENGINE DATA.Dr1;
% Piston, displacer crank radius in [m]
Pr2 = ENGINE DATA.Pr2;
Dr2 = ENGINE DATA.Dr2;
% Piston, displacer connecting rod lengths [m]
Pr3 = ENGINE DATA.Pr3;
Dr3 = ENGINE DATA.Dr3;
% Displacer Phase Angle Advance for Gamma
beta deg = ENGINE DATA.beta deg; %[deg]
fprintf('gamma crankshaft drive engine configuration\n')
\% Calculate the swept volumes (NEED TO FIX THESE TO WORK FOR CASES WHERE
% THERE IS A DESAXE OFFSET!!!!)
Vswp = (pi/4) * (Pbore^{2}) * (2*Pr2);
Vswd = (pi/4) * (Dbore^{2}) * (2*Dr2);
fprintf('\n Gamma crankshaft drive engine data summary:\n');
fprintf(' piston clearence,swept vols %.1f, %.1f [cm^3]\n',
Vclp*1e6,Vswp*1e6);
fprintf(' displacer clearence, swept vols %.1f, %.1f [cm^3]\n',
Vcld*1e6,Vswd*1e6);
fprintf(' displacer phase angle advance %.lf[degrees]\n', beta deg);
```

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```

```
function ENGINE DATA = alphacrankdrive(ENGINE DATA)
% Alpha crankshaft drive engine configuration
% Added by Connor Speer 02/15/17
% Connor Speer, October 2017
% Expansion Space Phase Angle Advance [deg]
alpha deg = ENGINE DATA.alpha deg;
% Compression, expansion clearence vols [m^3]
Vclc = ENGINE DATA.Vclc;
Vcle = ENGINE DATA.Vcle;
% Compression, expansion piston bores [m]
Cbore = ENGINE DATA.Cbore;
Ebore = ENGINE DATA.Ebore;
% Compression, expansion desaxe offset in [m]
Cr1 = ENGINE DATA.Cr1;
Er1 = ENGINE DATA.Er1;
% Compression, expansion crank radius in [m]
Cr2 = ENGINE DATA.Cr2;
Er2 = ENGINE DATA.Er2;
% Compression, expansion connecting rod lengths [m]
Cr3 = ENGINE DATA.Cr3;
Er3 = ENGINE DATA.Er3;
% Calculate the swept volumes (NEED TO FIX THESE TO WORK FOR CASES WHERE
% THERE IS A DESAXE OFFSET!!!!)
V_{SWC} = (pi/4) * (Cbore^{2}) * (2*Cr2);
Vswe = (pi/4) * (Ebore^{2}) * (2*Er2);
ENGINE DATA.Vswc = Vswc;
ENGINE DATA.Vswe = Vswe;
% %% DATA PRINTING
% fprintf('\nAlpha crankshaft drive engine data summary:\n');
% fprintf('\t compression space clearence,swept vols %.1f, %.1f [cm^3]\n',
Vclc*1e6,Vswc*1e6);
% fprintf('\t expansion space clearence,swept vols %.1f, %.1f [cm^3]\n',
Vcle*1e6,Vswe*1e6);
  fprintf('\t expansion space phase angle advance %.1f[degrees]\n',
alpha deg);
```

gas.m

```
function ENGINE_DATA = gas(ENGINE_DATA)
% specifies the working gas properties (he, h2, air)
% Israel Urieli 4/20/02
```

```
gas type = ENGINE DATA.gas type;
if(strncmp(gas type, 'hy', 2))
    fprintf('gas type is hydrogen\n')
  ENGINE DATA.gamma = 1.4; % Specific heat ratio: cp/cv
   ENGINE DATA.R = 4157.2; % Specific gas constant in [J/kgK]
   ENGINE DATA.kgas = 0.2843; % Thermal conductivity in [W/mK]
   ENGINE DATA.mu0 = 8.35e-6; % Dynamic viscosity at reference temp t0
[kg.m/s]
  ENGINE DATA.t suth = 84.4; % Sutherland constant [K]
elseif(strncmp(gas type, 'he', 2))
     fprintf('gas type is helium\n')
    ENGINE DATA.gamma = 1.67; % Specific heat ratio: cp/cv
    ENGINE DATA.R = 2078.6; % Specific gas constant in [J/kgK]
    ENGINE DATA.kgas = 0.142; % Thermal conductivity in [W/mK]
    ENGINE DATA.mu0 = 18.85e-6; % Dynamic viscosity at reference temp t0
[kq.m/s]
    ENGINE DATA.t suth = 80.0; % Sutherland constant [K]
elseif(strncmp(gas_type, 'ai', 2))
2
    fprintf('gas type is air\n')
    ENGINE DATA.gamma = 1.4; % Specific heat ratio: cp/cv
    ENGINE DATA.R = 287.0; % Specific gas constant in [J/kgK]
    ENGINE DATA.kgas = 0.04418; % Thermal conductivity in [W/mK]
    ENGINE DATA.mu0 = 17.08e-6; % Dynamic viscosity at reference temp t0
[kq.m/s]
    ENGINE DATA.t suth = 112.0; % Sutherland constant [K]
else
8
     fprintf('gas type is undefined\n')
end
```

heatex.m

```
ENGINE DATA.dk = ENGINE DATA.cooler pipe diameter; % cooler hydraulic
diameter [m]
   ENGINE DATA.lk = ENGINE DATA.cooler pipe length; % cooler effective
length [m]
   ENGINE DATA.ak
                                                                           =
ENGINE DATA.cooler num pipes*pi*ENGINE DATA.dk*ENGINE DATA.dk/4; % cooler
internal free flow area [m^2]
   ENGINE DATA.Vk = ENGINE DATA.ak*ENGINE DATA.lk; % cooler void volume
[m^3]
   ENGINE DATA.awgk
                                                                           =
ENGINE_DATA.cooler_num_pipes*pi*ENGINE_DATA.dk*ENGINE_DATA.lk; % cooler
internal wetted area [m^2]
elseif(strncmp(cooler type, 'a', 1)) % Annulus
    % Inner and outer diameters of the annular heater [m]
   dout = ENGINE DATA.cooler outer diameter;
   din = ENGINE DATA.cooler inner diameter;
   ENGINE DATA.dk = dout - din; % cooler hydraulic diameter [m]
   ENGINE DATA.lk = ENGINE DATA.cooler length; % cooler effective length [m]
   ENGINE DATA.ak = pi*(dout*dout - din*din)/4; % cooler internal free flow
area [m^2]
   ENGINE DATA.Vk = ENGINE DATA.ak*ENGINE DATA.cooler length; % cooler void
volume [m^3]
   ENGINE DATA.awgk = pi*dout*ENGINE DATA.cooler length; % cooler internal
wetted area [m^2]
elseif(strncmp(cooler type,'s',1)) % Slots
   % cooler internal free flow area [m^2]
   ENGINE DATA.ak
ENGINE DATA.cooler num slots*ENGINE DATA.cooler slot width*ENGINE DATA.cooler
slot height;
    % cooler void volume [m^3]
   ENGINE DATA.Vk = ENGINE DATA.ak*ENGINE DATA.cooler length;
   % cooler internal wetted area [m^2]
   ENGINE DATA.awgk
                                                                           =
ENGINE DATA.cooler num slots* (ENGINE DATA.cooler slot width
                                                                           +
2*ENGINE DATA.cooler slot height)*ENGINE DATA.cooler length;
   ENGINE DATA.dk = 4*ENGINE DATA.Vk/ENGINE DATA.awgk; % cooler hydraulic
diameter [m]
   ENGINE DATA.lk = ENGINE DATA.cooler length; % cooler effective length [m]
elseif(strncmp(cooler_type,'c',1)) % Custom
   ENGINE DATA.ak = ENGINE DATA.cooler free flow area; % cooler internal
free flow area [m^2]
   ENGINE DATA.Vk = ENGINE DATA.ak*ENGINE DATA.cooler length; % cooler void
volume [m^3]
   ENGINE DATA.awgk = ENGINE DATA.cooler wetted surface area; % cooler
internal wetted area [m^2]
   ENGINE DATA.dk = 4*ENGINE DATA.Vk/ENGINE DATA.awgk; % cooler hydraulic
diameter [m]
   ENGINE DATA.lk = ENGINE DATA.cooler length; % cooler effective length [m]
```

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```

```
else
    fprintf('ERROR: Cooler type is undefined.\n')
end
%% PRINTING
% fprintf('Cooler data summary:\n');
% fprintf('\t void volume(cc) %.2f\n', ENGINE DATA.Vk*1e6)
% fprintf('\t free flow area (cm^2) %.2f\n', ENGINE DATA.ak*1e4)
% fprintf('\t wetted area (cm^2) %.2f\n', ENGINE DATA.awgk*1e4)
% fprintf('\t hydraulic diameter(mm) %.2f\n', ENGINE DATA.dk*1e3)
% fprintf('\t cooler length (cm) %.2f\n', ENGINE DATA.lk*1e2)
<u>%______</u>
function ENGINE DATA = heater(ENGINE DATA)
% Specify heater geometric parameters
% Israel Urieli 4/15/02
% Modified by Connor Speer, October 2017. No globals.
heater type = ENGINE DATA.heater type;
if(strncmp(heater type, 'p', 1)) % Pipes
   ENGINE DATA.dh = ENGINE DATA.heater pipe diameter; % heater hydraulic
diameter [m]
   ENGINE DATA.lh = ENGINE DATA.heater pipe length; % heater effective
length [m]
   ENGINE DATA.ah
ENGINE DATA.heater num pipes*pi*ENGINE DATA.dh*ENGINE DATA.dh/4; % heater
internal free flow area [m^2]
   ENGINE DATA.Vh = ENGINE DATA.ah*ENGINE DATA.lh; % heater void volume
[m^3]
   ENGINE DATA.awgh
                                                                           =
ENGINE DATA.heater num pipes*pi*ENGINE DATA.dh*ENGINE DATA.lh; %
                                                                      heater
internal wetted area [m^2]
elseif(strncmp(heater type, 'a', 1)) % Annulus
    % Inner and outer diameters of the annular heater [m]
   dout = ENGINE DATA.heater outer diameter;
   din = ENGINE DATA.heater inner diameter;
   ENGINE DATA.dh = dout - din; % heater hydraulic diameter [m]
   ENGINE_DATA.lh = ENGINE_DATA.heater_length; % heater effective length [m]
   ENGINE DATA.ah = pi*(dout*dout - din*din)/4; % heater internal free flow
area [m^2]
   ENGINE DATA.Vh = ENGINE DATA.ah*ENGINE DATA.heater length; % heater void
volume [m^3]
   ENGINE DATA.awgh = pi*dout*ENGINE DATA.heater length; % heater internal
wetted area [m^2]
elseif(strncmp(heater type,'s',1)) % Slots
    % heater internal free flow area [m^2]
   ENGINE DATA.ah
ENGINE DATA.heater num slots*ENGINE DATA.heater slot width*ENGINE DATA.heater
slot height;
   % heater void volume [m^3]
```

```
ENGINE DATA.Vh = ENGINE DATA.ah*ENGINE DATA.heater length;
    % heater internal wetted area [m^2]
    ENGINE DATA.awqh
                                                                             =
ENGINE DATA.heater num slots* (ENGINE DATA.heater slot width
                                                                             +
2*ENGINE DATA.heater slot height)*ENGINE DATA.heater length;
    ENGINE DATA.dh = 4*ENGINE DATA.Vh/ENGINE DATA.awgh; % heater hydraulic
diameter [m]
    ENGINE DATA.lh = ENGINE DATA.heater length; % heater effective length [m]
elseif(strncmp(heater_type,'c',1)) % Custom
   ENGINE DATA.ah = ENGINE DATA.heater free flow area; % heater internal
free flow area [m^2]
   ENGINE DATA.Vh = ENGINE DATA.ah*ENGINE DATA.heater length; % heater void
volume [m^3]
   ENGINE DATA.awgh = ENGINE DATA.heater wetted surface area;
                                                                  % heater
internal wetted area [m^2]
   ENGINE DATA.dh = 4*ENGINE DATA.Vh/ENGINE DATA.awgh; % heater hydraulic
diameter [m]
   ENGINE DATA.lh = ENGINE DATA.heater length; % heater effective length [m]
else
    fprintf('ERROR: Heater type is undefined.\n')
end
% %% PRINTING
% fprintf('Heater data summary:\n');
% fprintf('\t void volume(cc) %.2f\n', ENGINE_DATA.Vh*1e6)
% fprintf('\t free flow area (cm^2) %.2f\n', ENGINE DATA.ah*1e4)
% fprintf('\t wetted area (cm^2) %.2f\n', ENGINE DATA.awgh*1e4)
% fprintf('\t hydraulic diameter(mm) %.2f\n', ENGINE DATA.dh*1e3)
% fprintf('\t heater length (cm) %.2f\n', ENGINE DATA.lh*1e2)
operat.m
function ENGINE DATA = operat(ENGINE DATA)
% Determine operating parameters and do Schmidt anlysis
% Israel Urieli 4/20/02
% Modified by Connor Speer, October 2017. No globals.
% Calculate regenerator mean effective temperature
ENGINE DATA.Tqr
                                              (ENGINE DATA.Tqh
                             =
ENGINE DATA.Tgk)/log(ENGINE DATA.Tgh/ENGINE DATA.Tgk);
ENGINE DATA.omega = 2*pi*ENGINE DATA.freq; % Engine angular frequency (rad/s)
% fprintf('Operating parameters:\n');
% fprintf('\t mean pressure (kPa): %.3f\n',ENGINE_DATA.Pmean*1e-3);
% fprintf('\t cold sink temperature (K): %.lf\n',ENGINE DATA.TC);
% fprintf('\t hot source temperature (K): %.lf\n',ENGINE DATA.TH);
```

```
% fprintf('\t effective regenerator temperature (K): %.1f\n',ENGINE DATA.TR);
```

```
% fprintf('\t operating frequency (hertz): %.lf\n',ENGINE DATA.freq);
ENGINE DATA = Schmidt (ENGINE DATA); % Do Schmidt analysis
%_____
function ENGINE DATA = Schmidt(ENGINE DATA)
% Schmidt anlysis
% Israel Urieli 3/31/02 - Extended by Connor Speer January 2017
% Modified by Connor Speer, October 2017. No globals.
engine type = ENGINE DATA.engine type;
if strcmp(engine type,'g') || strcmp(engine type,'x')
   % Gamma Schmidt analysis
   % Constant Calculations
   Vdead = ENGINE DATA.Vh + ENGINE DATA.Vr + ENGINE DATA.Vk; % Dead Volume
   tao = ENGINE DATA.Tgk/ENGINE DATA.Tgh; % Temperature ratio
    kappa = ENGINE DATA.Vswp/ENGINE DATA.Vswd; % Ratio of piston swept volume
to displacer swept volume
   chi = Vdead/ENGINE DATA.Vswd; % Dead volume ratio
    freq = ENGINE DATA.freq; % Engine Frequency [Hz]
   ENGINE DATA.beta = ENGINE DATA.beta deg*(pi/180); %(rad)
    % Senft Pressure calculations
   Y = 1 + tao + kappa + ((4*chi*tao)/(1+tao));
   A = kappa - ((1-tao)*cosd(ENGINE DATA.beta deg));
   B = (1-tao) * sind (ENGINE DATA.beta deg);
   X = sqrt((A^2) + (B^2));
   angle = acos(A/(sqrt((A^2) + (B^2)))); % Is this the same as pressure
phase below?
   % Here the mass of gas in the engine is calculated as the mean of the
   % mass calculated at each crank angle degree.
    theta = 0:(pi/180):2*pi; %(rad)
   Ve = (0.5*ENGINE DATA.Vcld)+(ENGINE DATA.Vswd*0.5)*...
        (1+cos(theta+ENGINE DATA.beta)); % Expansion space volume in [m^3].
   Vc = (0.5*ENGINE DATA.Vcld)+ENGINE DATA.Vclp+ENGINE DATA.Vswd-Ve+...
        (ENGINE DATA.Vswp*0.5*(1+cos(theta))); % Compression space volume in
[m^3].
    % Mass of gas in the engine [kg].
    ENGINE DATA.mgas
                                                                           =
ENGINE DATA.pmean/(mean(ENGINE DATA.R*((Vc./ENGINE DATA.Tgk)...
+ (ENGINE DATA.Vk/ENGINE DATA.Tqk) + ((ENGINE DATA.Vr*log(ENGINE DATA.Tqh/ENGINE
DATA.Tgk))/...
        (ENGINE DATA.Tqh-
ENGINE DATA.Tqk))+(ENGINE DATA.Vh/ENGINE DATA.Tqh)+(Ve./ENGINE DATA.Tqh)).^-
1));
    % Calculation of heat and work.
   W Schmidt = (pi*(1-tao)*(ENGINE DATA.Vswd+ENGINE DATA.Vswp)...
*ENGINE DATA.pmean*kappa*sin(ENGINE DATA.beta))/((kappa+1)*(sqrt((Y^2)-
(X^2) + Y) ;
```

```
Power Schmidt = W Schmidt*freq;
   eff Schmidt = 1-tao; % Carnot efficency
else
   ENGINE DATA.alpha = ENGINE DATA.alpha deg*(pi/180); %(rad)
   % Alpha Schmidt analysis
   C =
                         (((ENGINE DATA.Vswe/ENGINE DATA.Tgh)^2
                                                                    +
(ENGINE DATA.Vswc/ENGINE DATA.Tgk)^2 +...
2*(ENGINE DATA.Vswe/ENGINE DATA.Tgh)*(ENGINE DATA.Vswc/ENGINE DATA.Tgk)*cos(E
NGINE DATA.alpha))^0.5)/2;
       = (ENGINE_DATA.Vswc/2 + ENGINE_DATA.Vclc
   S
                                                                     +
ENGINE DATA.Vk)/ENGINE DATA.Tqk +...
      ENGINE DATA.Vr/ENGINE DATA.Tgr + (ENGINE DATA.Vswe/2 +
ENGINE DATA.Vcle + ENGINE DATA.Vh)/ENGINE DATA.Tqh;
   b = c/s;
   sqrtb = (1 - b^2)^{0.5};
   bf = (1 - 1/sqrtb);
   pressure phase
atan (ENGINE DATA.Vswe*sin (ENGINE DATA.alpha) / ENGINE DATA.Tgh/...
       (ENGINE DATA.Vswe*cos(ENGINE DATA.alpha)/ENGINE DATA.Tqh
                                                                      +
ENGINE DATA.Vswc/ENGINE DATA.Tqk));
                        fprintf(' pressure phase angle beta
2
%.1f(degrees)\n',pressure phase*180/pi)
   % total mass of working gas in engine
   ENGINE DATA.mgas = ENGINE DATA.pmean*s*sqrtb/ENGINE DATA.R;
    fprintf(' total mass of gas: %.3f(gm)\n',ENGINE DATA.mgas*1e3)
8
   % work output
   WC
(pi*ENGINE DATA.Vswc*ENGINE DATA.mqas*ENGINE DATA.R*sin(pressure phase)*bf/c)
;
   We
(pi*ENGINE DATA.Vswe*ENGINE DATA.mgas*ENGINE DATA.R*sin(pressure phase
ENGINE DATA.alpha) *bf/c);
   W Schmidt = (Wc + We);
   Power Schmidt = W Schmidt*ENGINE DATA.freq;
   eff Schmidt = W Schmidt/We; % qe = we (Carnot efficiency)
end
% Printout Schmidt analysis results
fprintf('========= Schmidt analysis =======\n')
fprintf(' Work(joules) %.3f \n Power(watts) %.3f\n',
W Schmidt, Power Schmidt);
% fprintf(' Qexp(joules) %.3e, Qcom(joules) %.3e\n', we,wc);
fprintf(' Indicated efficiency (Carnot efficiency) %.3f\n %%',
eff Schmidt*100);
fprintf('----->\n')
```

regen.m

```
function ENGINE DATA = regen(ENGINE DATA)
% Specifies regenerator geometric and thermal properties
% Israel Urieli 04/20/02 (modified 12/01/03)
% modified 2/12/2010 to include awgr0 (wetted area)
% modified 11/27/2010 to include 'no regenerator matrix'
% modified 10/5/2017 by Connor Speer and Jason Michaud
% modified 10/15/2017 by Connor Speer, no globals.
regen type = ENGINE DATA.regen config;
% Available regenerator configurations are:
% t for tubular regenerator housing
% a for annular regenerator housing
% r for rectangular regenerator housing
if(strncmp(regen_type,'t',1))
      fprintf('Tubular regenerator housing\n')
    ENGINE DATA.lr = ENGINE DATA.regen length; % regenerator effective length
[m]
    domat = ENGINE DATA.regen housing ID;
    dimat = 0;
    % no matrix regenerator wetted area [m^2]
    ENGINE DATA.awgr0 = ENGINE DATA.regen num tubes*pi*domat*ENGINE DATA.lr;
                            ENGINE DATA.regen num tubes*pi*(domat*domat
    ENGINE DATA.amat =
dimat*dimat)/4; % regen matrix area
elseif(strncmp(regen type, 'a', 1))
      fprintf('Annular regenerator housing\n')
    ENGINE DATA.lr = ENGINE DATA.regen length; % regenerator effective length
[m]
    domat = ENGINE DATA.regen housing ID;
    dimat = ENGINE DATA.regen matrix ID;
    % no matrix regenerator wetted area [m^2]
    ENGINE DATA.awgr0
ENGINE DATA.regen num tubes*pi*(domat+dimat)*ENGINE DATA.lr;
                            ENGINE DATA.regen num tubes*pi*(domat*domat
    ENGINE DATA.amat =
dimat*dimat)/4; % regen matrix area
 elseif(strncmp(regen type, 'r', 1))
      fprintf('Rectangular regenerator housing\n')
    ENGINE DATA.lr = ENGINE DATA.regen length; % regenerator effective length
[m]
    % no matrix regenerator wetted area [m^2]
```

```
ENGINE DATA.awgr0
((2*ENGINE DATA.regen height)+(2*ENGINE DATA.regen width))*ENGINE DATA.lr*ENG
INE DATA.regen num;
   ENGINE DATA.amat
ENGINE DATA.regen num*ENGINE DATA.regen height*ENGINE DATA.regen width;
                                                                           8
regen matrix area
else
% fprintf('regenerator configuration is undefined\n')
end
% Call regenerator matrix subfunction
% Available regenerator materials are:
% m for mesh regenerator material
% f for foil regenerator material
% n for regenerator material
ENGINE DATA = matrix (ENGINE DATA);
%_____
function ENGINE DATA = matrix(ENGINE DATA)
% Specifies regenerator matrix geometric and thermal properties
% Israel Urieli 03/31/02
% modified 11/27/10 for no regenerator matrix
% Modified 10/5/2017 by Connor Speer
% Modified 10/15/2017 by Connor Speer, no globals
matrix type = ENGINE DATA.regen matrix type;
if(strncmp(matrix_type, 'm', 1)) % Mesh regenerator
   ENGINE DATA.ar = ENGINE DATA.amat*ENGINE DATA.regen matrix porosity;
   ENGINE DATA.lr = ENGINE DATA.regen length;
   ENGINE DATA.Vr = ENGINE DATA.ar*ENGINE DATA.lr;
    ENGINE DATA.dr
ENGINE DATA.regen wire diameter*ENGINE DATA.regen matrix porosity/(1
ENGINE DATA.regen matrix porosity);
    ENGINE DATA.awgr = 4*ENGINE DATA.Vr/ENGINE DATA.dr + ENGINE DATA.awgr0;
8
                          fprintf('\t matrix porosity:
                                                                   %.3f\n',
ENGINE DATA.regen matrix porosity)
                                     matrix wire diam %.2f(mm)\n',
                      fprintf('\t
ENGINE DATA.regen wire diameter*1e3)
8
     fprintf('\t hydraulic diam %.3f(mm)\n', ENGINE DATA.dr*1e3)
8
     fprintf('\t total wetted area %.3e(sq.m)\n', ENGINE DATA.awgr)
     fprintf('\t regenerator length %.1f(mm)\n', ENGINE DATA.lr*1e3)
2
     fprintf('\t void volume %.2f(cc)\n', ENGINE DATA.Vr*1e6)
2
elseif(strncmp(matrix type, 'f', 1))
    fprintf('Wrapped foil matrix\n')
   ENGINE DATA.am
ENGINE DATA.foil thickness*ENGINE DATA.unrolled foil length;
   ENGINE DATA.ar = ENGINE DATA.amat - ENGINE DATA.am;
   ENGINE DATA.Vr = ENGINE DATA.ar*ENGINE DATA.lr;
```

```
ENGINE DATA.awgr = 2*ENGINE DATA.lr*ENGINE DATA.unrolled foil length +
awgr0;
    ENGINE DATA.dr = 4*ENGINE DATA.Vr/ENGINE DATA.awgr;
    porosity = ENGINE DATA.ar/ENGINE DATA.amat;
8
8
      fprintf('\t unrolled foil length: %.3f(m)\n', fl)
8
     fprintf('\t foil thickness %.3f(mm)\n',ENGINE DATA.foil thickness*1e3)
      fprintf('\t hydraulic diam %.3f(mm)\n', ENGINE DATA.dr*1e3)
2
     fprintf('\t total wetted area %f(sq.m)\n', ENGINE DATA.awgr)
8
8
      fprintf('\t void volume %.2f(cc)\n', ENGINE_DATA.Vr*1e6)
8
     fprintf('\t porosity %.3f\n', porosity)
elseif(strncmp(matrix type, 'n', 1))
      fprintf('No regenerator matrix\n')
8
    ENGINE DATA.ar = ENGINE DATA.amat;
    ENGINE DATA.Vr = ENGINE DATA.ar*ENGINE DATA.lr;
    ENGINE DATA.awgr = ENGINE DATA.awgr0;
    ENGINE DATA.dr = 4*ENGINE DATA.Vr/ENGINE DATA.awgr;
90
00
      fprintf('\t hydraulic diam %.3f(mm)\n', ENGINE DATA.dr*1e3)
      fprintf('\t total wetted area %f(sq.m)\n', ENGINE DATA.awgr)
8
      fprintf('\t void volume %.2f(cc)\n', ENGINE DATA.Vr*1e6)
9
else
8
      fprintf('matrix configuration is undefined\n')
end
```

The Isothermal Function Set

derivative.m

```
function dx = derivative(x,dy)
%derivative Take derivative of one variable 'x' with respect to dy
% Developed Oct 2016 - Shahzeb Mirza
% Takes 'derivative' assuming the array x is one cycle of a periodic
% function with respect to y. Uses FORWARD FINITE DIFFERENCE METHOD.
dx = diff(x);
dx (end+1) = x(1) - x(end);
dx = dx/dy;
end
```

isothermal.m

```
function ISOTHERMAL DATA = isothermal (ENGINE DATA, crank inc)
% Isothermal Function that when given an ENGINE DATA data structure returns
% performance results based on the Ideal Isothermal Model
% Developed by Shahzeb Mirza, October 2017
% Edited by Connor Speer, October 2017
8{
VARIABLE NAMES AND MEANINGS
theta - Array of sequential crank angles in [rad]
Vc - Compression Space Volume (function of angle) [m^3]
Ve - Expansion Space Volume (function of angle) [m^3]
Vk - Cold Space Volume (const.) [m^3]
Vh - Hot Space Volume (const.) [m^3]
Vr - Regenerator Volume (const.) [m^3]
Tgk - Hot-side GAS Temperature (const.) [K]
Tgh - Cold-side GAS Temperature (const.) [K]
Tr - Regenerator Temperature (const.) [K]
pmean - Initial Fill Pressure (const.) [Pa]
p - Engine Pressure (function of angle) [Pa]
R - Gas Specific Constant [J/kgK]
M - mass of gas
8}
%% Create array of crank increments in RADIANS
theta = linspace(0,2*pi, 360/crank inc + 1);
dtheta = theta(2) - theta(1);
nEl = length(theta);
%% Call on separate 'volume' function to get volume variations
% dVc, dVe returned here are derivatives with respect to theta
[Vc, Ve, dVc, dVe] = volume(theta, ENGINE DATA);
```

```
% % dVc and dVe returned here are just the differences between adjacent
% % entries
% dVc = diff(Vc);
% dVc(end+1) = Vc(1) - Vc(end);
% dVe = diff(Ve);
% dVe(end+1) = Ve(1) - Ve(end);
%% Find or Calculate engine CONSTANTS
Vk = ENGINE DATA.Vk;
Vh = ENGINE_DATA.Vh;
Vr = ENGINE DATA.Vr;
Tgk = ENGINE DATA.Tgk;
Tqh = ENGINE DATA.Tqh;
% pmean = ENGINE DATA.pmean;
R = ENGINE DATA.R;
tau = Tqh/Tqk;
deltaT = Tgh - Tgk;
Tr = deltaT/log(tau);
M = ENGINE DATA.mgas;
% Engine pressure as a function of crank angle
p = M * R . / (Vc/Tgk + Vk/Tgk + Vr/Tr + Vh/Tgh + Ve/Tgh);
% Pressure Derivative
dp = derivative(p,dtheta);
% Mass functions
mc = (p .* Vc)./(R .* Tgk);
mk = (p .* Vk)./(R .* Tgk);
mr = (p .* Vr) . / (R .* Tr);
mh = (p .* Vh) . / (R .* Tgh);
me = (p .* Ve)./(R .* Tgh);
% Mass Derivatives
dmc = derivative(mc,dtheta);
dmk = derivative(mk,dtheta);
dmr = derivative(mr,dtheta);
dmh = derivative(mh, dtheta);
dme = derivative(me, dtheta);
% Mass flows
m dot ck = -dmc;
m dot kr = -dmc - dmk;
m dot rh = dmh + dme;
m dot he = dme;
%% Find Work Done by Expansion and Compression Spaces
% Differential Method: Produces accurate results if crank angle increment
% is extremely fine (~0.01 degrees). Otherwise error is significant.
% Advantage is that it is sensitive to the 'orientation' of the Indicator
% Diagram
dWc = (p \cdot * dVc * dtheta);
```

```
dWe = (p .* dVe * dtheta);
dW = dWc + dWe;
Wc = cumsum(dWc);
We = cumsum(dWe);
W = Wc + We;
% Polyarea Method: Accurate Results at almost any crank angle increment,
% but slower than differential method. Is not sensitive to orientation of
% the indicator diagrams
% We = repmat(polyarea(Ve, p),1,nEl);
% Wc = repmat(-polyarea(Vc, p),1,nEl);
% % dWe = derivative(We, dtheta);
% % dWc = derivative(Wc, dtheta);
% % dW = dWe + dWc;
% % Wc = cumsum(dWc);
% % We = cumsum(dWe);
% W = Wc + We;
%% PREALLOCATE ISOTHERMAL DATA STRUCTURE;
ISOTHERMAL DATA(nEl).theta = []; % Crank angle (radians)
ISOTHERMAL DATA(nEl).p = []; % Pressure (Pa)
ISOTHERMAL DATA(nEl).Vc = []; % Compression space volume (m^3)
ISOTHERMAL DATA(nEl).Ve = []; % Expansion space volume (m^3)
ISOTHERMAL DATA(nEl).mc = []; % Mass of gas in the compression space (kg)
ISOTHERMAL DATA(nEl).mk = []; % Mass of gas in the cooler (kg)
ISOTHERMAL DATA(nEl).mr = []; % Mass of gas in the regenerator (kg)
ISOTHERMAL DATA(nEl).mh = []; % Mass of gas in the heater (kg)
ISOTHERMAL DATA(nEl).me = []; % Mass of gas in the expansion space (kg)
ISOTHERMAL DATA(nEl).m dot ck = []; % Conditional mass flow compression space
/ cooler (kg/rad)
ISOTHERMAL DATA(nEl).m dot kr = []; % Conditional mass flow cooler

regenerator (kg/rad)
ISOTHERMAL DATA(nEl).m dot rh = []; % Conditional mass flow regenerator /
heater (kq/rad)
ISOTHERMAL DATA(nEl).m dot he = []; % Conditional mass flow heater /
expansion space (kg/rad)
ISOTHERMAL_DATA(nEl).Tgc = []; % Compression space gas temperature (K)
ISOTHERMAL DATA(nEl).Tge = []; % Expansion space gas temperature (K)
ISOTHERMAL DATA(nEl).Qk = []; % Heat transferred to the cooler (J)
ISOTHERMAL DATA(nEl).Qr = []; % Heat transferred to the regenerator (J)
ISOTHERMAL DATA(nEl).Qh = []; % Heat transferred to the heater (J)
ISOTHERMAL DATA(nEl).Wc = []; % Work done by the compression space (J)
ISOTHERMAL DATA(nEl).We = []; % Work done by the expansion space (J)
ISOTHERMAL_DATA(nEl).W = []; % Total work done (WC + WE) (J)
ISOTHERMAL DATA(nEl).Tgck = []; % Conditional gas temperature compression
space / cooler (K)
ISOTHERMAL DATA(nEl).Tghe = []; % Conditional gas temperature heater /
expansion space (K)
ISOTHERMAL DATA(nEl).dTqc = []; % Derivative of compression space
                                                                         qas
temperature (K/rad)
ISOTHERMAL DATA(nEl).dTge = []; % Derivative of expansion space
                                                                         qas
temperature (K/rad)
```

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```

ISOTHERMAL DATA(nEl).dQk = []; % Derivative of heat transferred to the cooler (J/rad)ISOTHERMAL DATA(nEl).dQr = []; % Derivative of heat transferred to the regenerator (J/rad) ISOTHERMAL DATA(nEl).dQh = []; % Derivative of heat transferred to the heater (J/rad)ISOTHERMAL DATA(nEl).dWc = []; % Derivative of work done by the compression space (J/rad) ISOTHERMAL DATA(nEl).dWe = []; % Derivative of work done by the expansion space (J/rad)ISOTHERMAL DATA(nEl).dW = []; % Derivative of total work done (WC + WE) (J/rad) ISOTHERMAL DATA(nEl).dp = []; % Derivative of Pressure (Pa/rad) ISOTHERMAL DATA(nEl).dVc = []; % Derivative of compression space volume (m^3/rad) ISOTHERMAL DATA(nEl).dVe = []; % Derivative of expansion space volume (m³/rad) ISOTHERMAL DATA(nEl).dmc = []; % Derivative of mass of gas in the compression space (kg/rad) ISOTHERMAL DATA(nEl).dmk = []; % Derivative of mass of gas in the cooler (kg/rad) ISOTHERMAL DATA(nEl).dmr = []; % Derivative of mass of gas in the regenerator (kg/rad) ISOTHERMAL DATA(nEl).dmh = []; % Derivative of mass of gas in the heater (kg/rad) ISOTHERMAL DATA(nEl).dme = []; % Derivative of mass of gas in the expansion space (kq/rad)

%% OUTPUT TO ISOTHERMAL DATA STRUCTURE: for i = 1:nEl ISOTHERMAL_DATA(i).p = p(i); % Pressure (Pa) ISOTHERMAL DATA(i).Vc = Vc(i); % Compression space volume (m^3) ISOTHERMAL DATA(i).Ve = Ve(i); % Expansion space volume (m^3) ISOTHERMAL DATA(i).mc = mc(i); % Mass of gas in the compression space (kq) ISOTHERMAL DATA(i).mk = mk(i); % Mass of gas in the cooler (kg) ISOTHERMAL DATA(i).mr = mr(i); % Mass of gas in the regenerator (kg) ISOTHERMAL DATA(i).mh = mh(i); % Mass of gas in the heater (kg) ISOTHERMAL_DATA(i).me = me(i); % Mass of gas in the expansion space (kg) ISOTHERMAL DATA(i).m dot ck = m dot ck(i); % Conditional mass flow compression space / cooler (kg/rad) ISOTHERMAL DATA(i).m dot kr = m dot kr(i); % Conditional mass flow cooler / regenerator (kg/rad) ISOTHERMAL DATA(i).m dot rh = m dot rh(i); % Conditional mass flow regenerator / heater (kg/rad) ISOTHERMAL DATA(i).m dot he = m dot he(i); % Conditional mass flow heater / expansion space (kg/rad) ISOTHERMAL DATA(i).Tgc = Tgk; % Compression space gas temperature (K) ISOTHERMAL DATA(i).Tge = Tgh; % Expansion space gas temperature (K) ISOTHERMAL DATA(i).Qk = 0; % Heat transferred to the cooler (J) ISOTHERMAL_DATA(i).Qr = 0; % Heat transferred to the regenerator (J) ISOTHERMAL DATA(i).Qh = 0; % Heat transferred to the heater (J) ISOTHERMAL DATA(i).Wc = Wc(i); % Work done by the compression space (J) ISOTHERMAL DATA(i).We = We(i); % Work done by the expansion space (J) ISOTHERMAL DATA(i).W = W(i); % Total work done (WC + WE) (J)

ISOTHERMAL DATA(i).Tgck = Tgk; % Conditional gas temperature compression space / cooler (K) ISOTHERMAL DATA(i).Tghe = Tgh; % Conditional gas temperature heater / expansion space (K) ISOTHERMAL DATA(i).dTgc = 0; % Derivative of compression space gas temperature (K/rad) ISOTHERMAL DATA(i).dTge = 0; % Derivative of expansion space gas temperature (K/rad) ISOTHERMAL DATA(i).dQk = 0; % Derivative of heat transferred to the cooler (J/rad) ISOTHERMAL DATA(i).dQr = 0; % Derivative of heat transferred to the regenerator (J/rad) ISOTHERMAL DATA(i).dQh = 0; % Derivative of heat transferred to the heater (J/rad)ISOTHERMAL DATA(i).dWc = dWc(i); % Derivative of work done by the compression space (J/rad) ISOTHERMAL DATA(i).dWe = dWe(i); % Derivative of work done by the expansion space (J/rad) ISOTHERMAL DATA(i).dW = dW(i); % Derivative of total work done (WC + WE) (J/rad) ISOTHERMAL DATA(i).dp = dp(i); % Derivative of Pressure (Pa/rad) ISOTHERMAL DATA(i).dVc = dVc(i); % Derivative of compression space volume (m^3/rad) ISOTHERMAL DATA(i).dVe = dVe(i); % Derivative of expansion space volume (m^3/rad) ISOTHERMAL DATA(i).dmc = dmc(i); % Derivative of mass of gas in the compression space (kg/rad) ISOTHERMAL DATA(i).dmk = dmk(i); % Derivative of mass of gas in the cooler (kg/rad) ISOTHERMAL DATA(i).dmr = dmr(i); % Derivative of mass of qas in the regenerator (kg/rad) ISOTHERMAL DATA(i).dmh = dmh(i); % Derivative of mass of gas in the heater (kq/rad)ISOTHERMAL DATA(i).dme = dme(i); % Derivative of mass of gas in the expansion space (kg/rad) end ENGINE DATA.mqas = M; % Total Mass of gas in the engine (kg) %% PLOT % theta = theta*180/pi; % hold on; % plot(theta,mc); % plot(theta,mk); % plot(theta,mr); % plot(theta,mh); % plot(theta,me); % hold off; % legend('mc','mk','mr','mh','me'); % xlabel('Crank Angle (deg)') % ylabel('Mass (kg)') % title('Engine Space Mass') 8 % figure; hold on; % plot(theta, W); % plot(theta, We); % plot(theta, Wc); % legend('W','We','Wc');

```
% xlabel('Crank Angle (deg)')
% ylabel('Work (J)')
% title('Cumulative Work in Cycle')
%
% figure; hold on;
% plot(theta, dW);
% plot(theta, dWe);
% plot(theta, dWc);
% legend('dW','dWe','dWc');
% xlabel('Crank Angle (deg)')
% ylabel('"POWER" (J/rad)')
% title('Power in Cycle')
end
```

The Adiabatic Function Set

adiabatic.m

```
function ADIABATIC DATA = adiabatic (ENGINE DATA, crank inc)
% ideal adiabatic model simulation
% Israel Urieli, 7/6/2002
% Modified by Connor Speer October 2017 to use structures.
% Inputs:
% ENGINE DATA --> Structure containing engine geometry and operating point
% crank inc --> crank angle step size [degrees]
% Output:
% ADIABATIC DATA --> Structure containing ideal adiabatic model results
% Preallocate space in a structure array for ideal adiabatic model
% results. All derivatives are with respect to crank angle.
ADIABATIC DATA((360/crank inc)+1).theta = []; % Crank angle (radians)
ADIABATIC DATA((360/crank inc)+1).p = []; % Pressure (Pa)
ADIABATIC_DATA((360/crank_inc)+1).Vc = []; % Compression space volume (m^3)
ADIABATIC DATA((360/crank inc)+1).Ve = []; % Expansion space volume (m^3)
ADIABATIC DATA((360/crank inc)+1).mc = []; % Mass of gas in the compression
space (kg)
ADIABATIC DATA((360/crank inc)+1).mk = []; % Mass of gas in the cooler (kg)
ADIABATIC DATA((360/crank inc)+1).mr = []; % Mass of gas in the regenerator
(kq)
ADIABATIC DATA((360/crank inc)+1).mh = []; % Mass of gas in the heater (kg)
ADIABATIC DATA((360/crank inc)+1).me = []; % Mass of gas in the expansion
space (kg)
ADIABATIC DATA((360/crank inc)+1).m dot ck = []; % Conditional mass flow
compression space / cooler (kg/rad)
ADIABATIC DATA((360/crank inc)+1).m dot kr = []; % Conditional mass flow
cooler / regenerator (kg/rad)
ADIABATIC DATA((360/crank inc)+1).m dot rh = []; % Conditional mass flow
regenerator / heater (kg/rad)
ADIABATIC DATA((360/crank inc)+1).m dot he = []; % Conditional mass flow
heater / expansion space (kg/rad)
ADIABATIC DATA((360/crank inc)+1).Tgc = []; % Compression space
                                                                        gas
temperature (K)
ADIABATIC DATA((360/crank inc)+1).Tge = [];
                                              % Expansion space
                                                                         gas
temperature (K)
ADIABATIC DATA((360/crank inc)+1).Qk = []; % Heat transferred to the cooler
(J)
ADIABATIC DATA((360/crank inc)+1).Qr = []; % Heat transferred to the
regenerator (J)
ADIABATIC DATA((360/crank inc)+1).Qh = []; % Heat transferred to the heater
(J)
ADIABATIC DATA((360/crank inc)+1).Wc = []; % Work done by the compression
space (J)
ADIABATIC DATA((360/crank inc)+1).We = []; % Work done by the expansion
space (J)
```

ADIABATIC DATA((360/crank inc)+1).W = []; % Total work done (WC + WE) (J) ADIABATIC DATA((360/crank inc)+1).Tqck = []; % Conditional gas temperature compression space / cooler (K) ADIABATIC DATA((360/crank inc)+1).Tghe = []; % Conditional gas temperature heater / expansion space (K) ADIABATIC DATA((360/crank inc)+1).dTgc = []; % Derivative of compression space gas temperature (K/rad) ADIABATIC DATA((360/crank inc)+1).dTge = []; % Derivative of expansion space gas temperature (K/rad) ADIABATIC DATA((360/crank inc)+1).dQk = []; % Derivative of heat transferred to the cooler (J/rad)ADIABATIC DATA((360/crank inc)+1).dQr = []; % Derivative of heat transferred to the regenerator (J/rad)ADIABATIC DATA((360/crank inc)+1).dQh = []; % Derivative of heat transferred to the heater (J/rad)ADIABATIC DATA((360/crank inc)+1).dWc = []; % Derivative of work done by the compression space (J/rad) ADIABATIC DATA((360/crank inc)+1).dWe = []; % Derivative of work done by the expansion space (J/rad) ADIABATIC DATA((360/crank inc)+1).dW = []; % Derivative of total work done (WC + WE) (J/rad) ADIABATIC DATA((360/crank inc)+1).dp = []; % Derivative of Pressure (Pa/rad) ADIABATIC DATA((360/crank inc)+1).dVc = []; % Derivative of compression space volume (m^3/rad) ADIABATIC DATA((360/crank inc)+1).dVe = []; % Derivative of expansion space volume (m^{3}/rad) ADIABATIC DATA((360/crank inc)+1).dmc = []; % Derivative of mass of gas in the compression space (kg/rad) ADIABATIC DATA((360/crank inc)+1).dmk = []; % Derivative of mass of gas in the cooler (kg/rad) ADIABATIC DATA((360/crank inc)+1).dmr = []; % Derivative of mass of gas in the regenerator (kg/rad) ADIABATIC DATA((360/crank inc)+1).dmh = []; % Derivative of mass of gas in the heater (kg/rad) ADIABATIC DATA((360/crank inc)+1).dme = []; % Derivative of mass of gas in the expansion space (kg/rad) % Set values of the variables in ADIABATIC DATA at crank angle zero equal % to zero. ADIABATIC DATA(1).theta = 0; % Crank angle (radians) ADIABATIC_DATA(1).p = 0; % Pressure (Pa) ADIABATIC DATA(1).Vc = 0; % Compression space volume (m^3) ADIABATIC DATA(1).Ve = 0; % Expansion space volume (m^3) ADIABATIC DATA(1).mc = 0; % Mass of gas in the compression space (kg) ADIABATIC DATA(1).mk = 0; % Mass of gas in the cooler (kg) ADIABATIC DATA(1).mr = 0; % Mass of gas in the regenerator (kg) ADIABATIC DATA(1).mh = 0; % Mass of gas in the heater (kg) ADIABATIC DATA(1).me = 0; % Mass of gas in the expansion space (kg) ADIABATIC DATA(1).m dot ck = 0; % Conditional mass flow compression space / cooler (kg/rad) ADIABATIC DATA(1).m dot kr = 0; % Conditional mass flow cooler / regenerator (kg/rad) ADIABATIC DATA(1).m dot rh = 0; % Conditional mass flow regenerator / heater (kg/rad)

ADIABATIC DATA(1).m dot he = 0; % Conditional mass flow heater / expansion space (kg/rad) ADIABATIC DATA(1).Tgc = 0; % Compression space gas temperature (K) ADIABATIC DATA(1).Tge = 0; % Expansion space gas temperature (K) ADIABATIC DATA(1).Qk = 0; % Heat transferred to the cooler (J) ADIABATIC DATA(1).Qr = 0; % Heat transferred to the regenerator (J) ADIABATIC DATA(1).Qh = 0; % Heat transferred to the heater (J) ADIABATIC DATA(1).Wc = 0; % Work done by the compression space (J) ADIABATIC_DATA(1).We = 0; % Work done by the expansion space (J) ADIABATIC_DATA(1).W = 0; % Total work done (WC + WE) (J) ADIABATIC DATA(1).Tgck = 0; % Conditional gas temperature compression space / cooler (K) ADIABATIC DATA(1).Tqhe = 0; % Conditional gas temperature heater / expansion space (K) ADIABATIC DATA(1).dTgc = 0; % Derivative of compression space gas temperature (K/rad) ADIABATIC DATA(1).dTge = 0; % Derivative of expansion space gas temperature (K/rad) ADIABATIC DATA(1).dQk = 0; % Derivative of heat transferred to the cooler (J/rad) ADIABATIC DATA(1).dQr = 0; % Derivative of heat transferred to the regenerator (J/rad) ADIABATIC DATA(1).dQh = 0; % Derivative of heat transferred to the heater (J/rad)ADIABATIC DATA(1).dWc = 0; % Derivative of work done by the compression space (J/rad)ADIABATIC DATA(1).dWe = 0; % Derivative of work done by the expansion space (J/rad) ADIABATIC DATA(1).dW = 0; % Derivative of total work done (WC + WE) (J/rad) ADIABATIC DATA(1).dp = 0; % Derivative of Pressure (Pa/rad) ADIABATIC DATA(1).dVc = 0; % Derivative of compression space volume (m^3/rad) ADIABATIC DATA(1).dVe = 0; % Derivative of expansion space volume (m^3/rad) ADIABATIC DATA(1).dmc = 0; % Derivative of mass of gas in the compression space (kq/rad) ADIABATIC DATA(1).dmk = 0; % Derivative of mass of gas in the cooler (kg/rad) ADIABATIC DATA(1).dmr = 0; % Derivative of mass of gas in the regenerator (kq/rad)ADIABATIC DATA(1).dmh = 0; % Derivative of mass of gas in the heater (kg/rad) ADIABATIC DATA(1).dme = 0; % Derivative of mass of gas in the expansion space (kg/rad)

```
%% Convergence Criteria
%%%%%%% CHANGING
epsilon = .0001; % Allowable error in temperature (K)
```

```
% epsilon = .01; % Allowable error in temperature (K)
max_iteration = 10000; % Maximum number of iterations to convergence
ninc = 360/crank_inc; % number if integration increments (every degree)
dtheta = 2.0*pi/ninc; % integration increment (radians)
```

```
%% Initial conditions:
% Preallocate space for the variable "y" which contains the 22 variable
% values for one crank angle increment.
y = zeros(1, 22);
% Initial temperature at interface between heater and expansion space is
% assumed to be equal to the heater gas temperature.
ADIABATIC DATA(1).Tghe = ENGINE DATA.Tgh;
y(18) = ENGINE DATA.Tgh;
% Initial temperature at interface between compression space and cooler is
% assumed to be equal to the cooler gas temperature.
ADIABATIC DATA(1).Tgck = ENGINE DATA.Tgk;
y(17) = ENGINE DATA.Tgk;
% Initial expansion space temperature is assumed to be equal to the heater
% gas temperature.
ADIABATIC DATA(1).Tge = ENGINE DATA.Tgh;
y(2) = ENGINE DATA.Tge;
% Initial compression space temperature is assumed to be equal to the
% cooler gas temperature.
ADIABATIC DATA(1).Tqc = ENGINE DATA.Tqk;
y(1) = ENGINE DATA.Tgk;
iter = 0; % Initialize iteration counter.
Terror = 10*epsilon; % Initial error to enter the loop
% Iteration loop to cyclic convergence
while ((Terror >= epsilon)&&(iter < max iteration))</pre>
% cyclic initial conditions
    theta = 0;
    y(3) = 0; \% 3 = QK
    y(4) = 0; % 4 = QR
    y(5) = 0; % 5 = QH
    y(6) = 0; \% 6 = WC
    y(7) = 0; \% 7 = WE
    y(8) = 0; 8 = W
    fprintf('iteration %d: Tc(@360 dq) = %.1f[K], Te(@360 dq) =
%.lf[K]\n',iter,y(1),y(2))
    % Initialize crank increment counter variable (counter = 1 are the intial
conditions)
    counter = 2;
    for i = 1:1:ninc % For each crank angle degree
        % Make variables for most recently calculated crank angle
        % increment into the vector "y".
        ADIABATIC DATA(counter-1).Tgc = y(1);
        ADIABATIC DATA (counter-1). Tge = y(2);
        ADIABATIC DATA(counter-1).Qk = y(3);
        ADIABATIC DATA(counter-1).Qr = y(4);
        ADIABATIC DATA (counter-1).Qh = y(5);
```

```
ADIABATIC DATA(counter-1).Wc = y(6);
        ADIABATIC DATA (counter-1). We = y(7);
        ADIABATIC DATA(counter-1).W = y(8);
        ADIABATIC DATA(counter-1).p = y(9);
        ADIABATIC DATA (counter-1). Vc = y(10);
        ADIABATIC DATA (counter-1). Ve = y(11);
        ADIABATIC DATA(counter-1).mc = y(12);
        ADIABATIC DATA(counter-1).mk = y(13);
        ADIABATIC DATA (counter-1).mr = y(14);
        ADIABATIC DATA(counter-1).mh = y(15);
        ADIABATIC DATA(counter-1).me = y(16);
        ADIABATIC DATA(counter-1).Tgck = y(17);
        ADIABATIC DATA (counter-1). Type = y(18);
        ADIABATIC DATA (counter-1).m dot ck = y(19);
        ADIABATIC DATA (counter-1).m dot kr = y(20);
        ADIABATIC DATA (counter-1).m dot rh = y(21);
        ADIABATIC DATA(counter-1).m dot he = y(22);
        % Use 4th order Runge-Kutta algorithm to calculate variable values
        % for the next crank angle increment.
       [theta,y,dy] = rk4(7,theta,dtheta,y,ENGINE_DATA); % Calculate the
variable values for the next crank angle increment
       % Store the newly calculated values in the ADIABATIC DATA solution
       % structure
       ADIABATIC DATA (counter).theta = theta;
       ADIABATIC DATA(counter).Tgc = y(1);
       ADIABATIC DATA(counter).Tge = y(2);
       ADIABATIC DATA (counter) .Qk = y(3);
      ADIABATIC DATA (counter) Qr = y(4);
      ADIABATIC DATA (counter).Qh = y(5);
      ADIABATIC DATA(counter).Wc = y(6);
      ADIABATIC DATA (counter). We = y(7);
       ADIABATIC DATA (counter) .W = y(8);
       ADIABATIC DATA(counter).p = y(9);
       ADIABATIC DATA(counter).Vc = y(10);
      ADIABATIC DATA (counter). Ve = y(11);
       ADIABATIC DATA (counter).mc = y(12);
       ADIABATIC DATA (counter).mk = y(13);
       ADIABATIC DATA (counter) .mr = y(14);
       ADIABATIC DATA (counter).mh = y(15);
       ADIABATIC_DATA(counter).me = y(16);
       ADIABATIC DATA(counter).Tgck = y(17);
       ADIABATIC DATA(counter).Tghe = y(18);
       ADIABATIC DATA(counter).m dot ck = y(19);
      ADIABATIC DATA (counter).m dot kr = y(20);
      ADIABATIC DATA (counter).m dot rh = y(21);
       ADIABATIC DATA (counter).m dot he = y(22);
       ADIABATIC DATA(counter).dTgc = dy(1);
       ADIABATIC DATA (counter).dTge = dy(2);
       ADIABATIC DATA(counter).dQk = dy(3);
       ADIABATIC DATA(counter).dQr = dy(4);
      ADIABATIC DATA(counter).dQh = dy(5);
       ADIABATIC DATA(counter).dWc = dy(6);
```

```
ADIABATIC DATA(counter).dWe = dy(7);
      ADIABATIC DATA (counter). dW = dy(8);
      ADIABATIC DATA (counter).dp = dy(9);
      ADIABATIC DATA(counter).dVc = dy(10);
      ADIABATIC DATA(counter).dVe = dy(11);
      ADIABATIC DATA (counter).dmc = dy(12);
      ADIABATIC DATA (counter).dmk = dy(13);
      ADIABATIC DATA(counter).dmr = dy(14);
      ADIABATIC DATA (counter).dmh = dy(15);
      ADIABATIC DATA(counter).dme = dy(16);
      % Increment the crank increment counter variable
      counter = counter + 1;
   end
   % Check if the expansion and compression space temperatures at crank
   % angle 360 match the ones at crank angle 0.
   Terror
                                               abs([ADIABATIC DATA(1).Tgc]-
[ADIABATIC DATA((360/crank inc)+1).Tgc])...
                                               abs([ADIABATIC DATA(1).Tge]-
[ADIABATIC DATA((360/crank inc)+1).Tge]);
   epsilon
                                abs(max([ADIABATIC DATA.Tqc])
                     =
min([ADIABATIC DATA.Tqc]))*0.001;
   iter = iter + 1; % Increment iteration counter variable
 end
if (iter >= max iteration)
    fprintf('No convergence within %d iteration\n', max iteration)
end
%% Print Out Ideal Adiabatic Analysis Results
% The heat and work quantities are cumulative, so the values at 360 degrees
% represent the total energy transferred in one complete cycle.
eff = ADIABATIC DATA(end).W / ADIABATIC DATA(end).Qh;
Qkpower = ADIABATIC DATA(end).Qk * ENGINE DATA.freq;
Qrpower = ADIABATIC DATA(end).Qr * ENGINE DATA.freq;
Qhpower = ADIABATIC DATA(end).Qh * ENGINE DATA.freq;
Wpower = ADIABATIC DATA(end).W * ENGINE DATA.freq;
ADIABATIC DATA(1).eff = eff;
ADIABATIC DATA(1).Qkpower = Qkpower;
ADIABATIC DATA(1).Qrpower = Qrpower;
ADIABATIC_DATA(1).Qhpower = Qhpower;
ADIABATIC DATA(1).Wpower = Wpower;
fprintf(' Heat transferred to the cooler: %.2f[W]\n', Qkpower);
fprintf(' Net heat transferred to the regenerator: %.2f[W]\n', Qrpower);
fprintf(' Heat transferred to the heater: %.2f[W]\n', Qhpower);
fprintf(' Indicated power output: %.2f[W]\n', Wpower);
fprintf(' Thermal efficiency : %.1f[%%]\n', eff*100);
fprintf('========\n')
```

dadiab.m

```
function [y, dy] = dadiab(theta, y, ENGINE DATA)
% Evaluate ideal adiabatic model derivatives
% Israel Urieli, 7/6/2002
% Arguments: theta - current cycle angle [radians]
             y(22) - vector of current variable values
% Returned values:
             y(22) - updated vector of current variables
2
8
              dy(16) vector of current derivatives
% Function invoked : volume.m
% Modified by Connor Speer October 2017 to use structures.
Vk = ENGINE DATA.Vk; % cooler void volume [m^3]
Vr = ENGINE DATA.Vr; % regen void volume [m^3]
Vh = ENGINE DATA.Vh; % heater void volume [m^3]
R = ENGINE DATA.R; % gas constant [J/kg.K]
cp = ENGINE DATA.cp; % specific heat capacity at constant pressure [J/kg.K]
cv = ENGINE DATA.cv; % specific heat capacity at constant volume [J/kq.K]
gamma = ENGINE DATA.gamma; % ratio: cp/cv
mgas = ENGINE DATA.mgas; % total mass of gas in engine [kg]
Tgk = ENGINE DATA.Tgk; % cooler gas temperature [K]
Tgr = ENGINE DATA.Tgr; % regenerator gas temperature [K]
Tgh = ENGINE DATA.Tgh; % heater gas temperature [K]
% Indices of the y, dy vectors:
TC = 1; % Compression space temperature (K)
TE = 2; % Expansion space temperature (K)
 QK = 3; % Heat transferred to the cooler (J)
QR = 4; % Heat transferred to the regenerator (J) QH = 5; % Heat transferred to the heater (J)
 WC = 6; % Work done by the compression space (J)
 WE = 7; % Work done by the expansion space (J)
 W = 8; % Total work done (WC + WE) (J)
 P = 9; % Pressure (Pa)
VC = 10; % Compression space volume (m^3)
VE = 11; % Expansion space volume (m^3)
MC = 12; % Mass of gas in the compression space (kg)
 MK = 13; % Mass of gas in the cooler (kg)
MR = 14; % Mass of gas in the regenerator (kg)
MH = 15; % Mass of gas in the heater (kg)
ME = 16; % Mass of gas in the expansion space (kg)
 TCK = 17; % Conditional temperature compression space / cooler (K)
 THE = 18; % Conditional temeprature heater / expansion space (K)
 GACK = 19; % Conditional mass flow compression space / cooler (kg/rad)
 GAKR = 20; % Conditional mass flow cooler / regenerator (kg/rad)
GARH = 21; % Conditional mass flow regenerator / heater (kg/rad)
 GAHE = 22; % Conditional mass flow heater / expansion space (kg/rad)
8_____
```

% Volume and volume derivatives:

```
[y(VC),y(VE),dy(VC),dy(VE)] = volume(theta, ENGINE DATA);
% Pressure and pressure derivatives:
vot = Vk/Tqk + Vr/Tqr + Vh/Tqh;
 y(P) = (mgas*R/(y(VC)/y(TC) + vot + y(VE)/y(TE)));
 top = -y(P) * (dy(VC) / y(TCK) + dy(VE) / y(THE));
bottom = (y(VC) / (y(TCK) * gamma) + vot + y(VE) / (y(THE) * gamma));
dy(P) = top/bottom;
% Mass accumulations and derivatives:
 y(MC) = y(P) * y(VC) / (R*y(TC));
y(MK) = y(P) * Vk / (R*Tgk);
y(MR) = y(P) * Vr / (R*Tgr);
y(MH) = y(P) * Vh/(R*Tqh);
 y(ME) = y(P) * y(VE) / (R*y(TE));
dy(MC) = (y(P) * dy(VC) + y(VC) * dy(P) / gamma) / (R*y(TCK));
dy(ME) = (y(P) * dy(VE) + y(VE) * dy(P) / gamma) / (R*y(THE));
dpop = dy(P)/y(P);
 dy(MK) = y(MK) * dpop;
 dy(MR) = y(MR) * dpop;
dy(MH) = y(MH) * dpop;
% Mass flow between cells:
y(GACK) = -dy(MC);
y(GAKR) = y(GACK) - dy(MK);
y(GAHE) = dy(ME);
y(GARH) = y(GAHE) + dy(MH);
% Conditional temperatures between cells:
y(TCK) = Tgk;
 if(y(GACK) > 0)
    y(TCK) = y(TC);
 end
 y(THE) = y(TE);
 if(y(GAHE)>0)
    y(THE) = Tgh;
 end
% 7 derivatives to be integrated by rk4:
% Working space temperatures:
dy(TC) = y(TC) * (dpop + dy(VC) / y(VC) - dy(MC) / y(MC));
dy(TE) = y(TE) * (dpop + dy(VE) / y(VE) - dy(ME) / y(ME));
% Energy:
 dy (QK) = Vk*dy (P) * cv/R - cp* (y (TCK) * y (GACK) - Tgk*y (GAKR));
 dy(QR) = Vr*dy(P)*cv/R - cp*(Tgk*y(GAKR) - Tgh*y(GARH));
dy(QH) = Vh^*dy(P)^*cv/R - cp^*(Tgh^*y(GARH) - y(THE)^*y(GAHE));
dy(WC) = y(P) * dy(VC);
dy(WE) = y(P) * dy(VE);
% Net work done:
dy(W) = dy(WC) + dy(WE);
y(W) = y(WC) + y(WE);
```

volume.m

```
function [Vc,Ve,dVc,dVe] = volume(theta, ENGINE DATA)
% determine working space volume variations and derivatives
% Israel Urieli, 7/6/2002
% Modified 2/14/2010 to include rockerV (rockdrive)
% Modified by Connor Speer October 2017
% Argument: theta - current cycle angle [radians]
% Returned values:
% vc, ve - compression, expansion space volumes [m^3]
% dvc, dve - compression, expansion space volume derivatives
% *** Note: For gamma engines, the total workspace volume is maximum at
% crank angle 0. For alpha engines, the compression space volume is maximum
% at crank angle zero.
engine_type = ENGINE_DATA.engine_type; % Letter indicationg engine layout and
drive mechanism
if (strncmp(engine type, 's', 1)) % Sinusoidal alpha
    [Vc,Ve,dVc,dVe] = sinevol(theta, ENGINE DATA);
elseif(strncmp(engine type,'y',1)) % Ross yoke mechanism alpha
    [Vc,Ve,dVc,dVe] = yokevol(theta, ENGINE DATA);
elseif(strncmp(engine_type,'r',1)) % Ross rocker V-drive alpha
    [Vc,Ve,dVc,dVe] = rockvol(theta, ENGINE DATA);
elseif(strncmp(engine type, 'g', 1)) % Sinusoidal gamma
    [Vc,Ve,dVc,dVe] = gammasinvol(theta, ENGINE_DATA);
elseif(strncmp(engine type,'x',1)) % Slider-crank mechanism gamma
    [Vc,Ve,dVc,dVe] = gammacrankvol(theta, ENGINE DATA);
elseif(strncmp(engine type, 'a', 1)) % Slider-crank mechanism alpha
    [Vc,Ve,dVc,dVe] = alphacrankvol(theta, ENGINE DATA);
end
function [Vc,Ve,dVc,dVe] = sinevol(theta, ENGINE DATA)
% sinusoidal drive volume variations and derivatives
% Israel Urieli, 7/6/2002
% Argument: theta - current cycle angle [radians]
% Returned values:
% vc, ve - compression, expansion space volumes [m^3]
% dvc, dve - compression, expansion space volume derivatives
Vclc = ENGINE DATA.Vclc;
Vcle = ENGINE DATA.Vcle;
Vswc = ENGINE DATA.Vswc;
Vswe = ENGINE DATA.Vswe;
alpha = ENGINE DATA.alpha;
% Vclc Vcle % compression, expansion clearence vols [m^3]
% Vswc Vswe % compression, expansion swept volumes [m^3]
% alpha % phase angle advance of expansion space [radians]
```

```
Vc = Vclc + 0.5*Vswc*(1 + cos(theta));
Ve = Vcle + 0.5*Vswe*(1 + cos(theta + alpha));
dVc = -0.5*Vswc*sin(theta);
dVe = -0.5*Vswe*sin(theta + alpha);
<u>&_____</u>
function [Vc,Ve,dVc,dVe] = yokevol(theta, ENGINE DATA)
% Ross yoke drive volume variations and derivatives
% Israel Urieli, 7/6/2002
% Modified by Connor Speer, October 2017.
% Argument: theta - current cycle angle [radians]
% Returned values:
% Vc, Ve - compression, expansion space volumes [m^3]
   dVc, dVe - compression, expansion space volume derivatives
% compression, expansion clearence vols [m^3]
Vclc = ENGINE DATA.Vclc;
Vcle = ENGINE DATA.Vcle;
b1 = ENGINE DATA.b1; % Ross yoke length (1/2 yoke base) [m]
b2 = ENGINE DATA.b2; % Ross yoke height [m]
crank = ENGINE DATA.crank; % crank radius [m]
% area of compression/expansion pistons [m^2]
acomp = ENGINE DATA.acomp;
aexp = ENGINE DATA.aexp;
ymin = ENGINE DATA.ymin; % minimum yoke vertical displacement [m]
sinth = sin(theta);
costh = cos(theta);
bth = (b1^2 - (crank*costh)^2)^{0.5};
ye = crank*(sinth + (b2/b1)*costh) + bth;
yc = crank*(sinth - (b2/b1)*costh) + bth;
Ve = vcle + aexp*(ye - ymin);
Vc = vclc + acomp*(yc - ymin);
dVc = acomp*crank*(costh + (b2/b1)*sinth + crank*sinth*costh/bth);
dVe = aexp*crank*(costh - (b2/b1)*sinth + crank*sinth*costh/bth);
%------
function [vc,ve,dvc,dve] = rockvol(theta, ENGINE_DATA)
% Ross Rocker-V drive volume variations and derivatives
% Israel Urieli, 7/6/2002 & Martine Long 2/25/2005
% Argument: theta - current cycle angle [radians]
% Returned values:
% vc, ve - compression, expansion space volumes [m^3]
   dvc, dve - compression, expansion space volume derivatives
global vclc vcle % compression, expansion clearence vols [m^3]
global crank % crank radius [m]
global acomp aexp % area of compression/expansion pistons [m^2]
global conrodc conrode % length of comp/exp piston connecting rods [m]
global ycmax yemax % maximum comp/exp piston vertical displacement [m]
```

```
sinth = sin(theta);
costh = cos(theta);
beth = (conrode^2 - (crank*costh)^2)^{0.5};
bcth = (conrodc^2 - (crank*sinth)^2)^{0.5};
ye = beth - crank*sinth;
yc = bcth + crank*costh;
ve = vcle + aexp*(yemax - ye);
vc = vclc + acomp*(ycmax - yc);
dvc = acomp*crank*sinth*(crank*costh/bcth + 1);
dve = -aexp*crank*costh*(crank*sinth/beth - 1);
function [vc,ve,dvc,dve] = gammasinvol(theta, ENGINE DATA);
% gamma sinusoidal drive volume variations and derivatives
% Added by Connor Speer - January 2017
% Argument: theta - current cycle angle [radians]
% Returned values:
% vc, ve - compression, expansion space volumes [m^3]
  dvc, dve - compression, expansion space volume derivatives
8
global vclp vcld % piston, displacer clearence vols [m^3]
global vswp vswd % compression, expansion swept volumes [m^3]
global beta % phase angle advance of displacer motion over piston [radians]
%*** Total volume is maximum at theta = 0 for gammas.
vc = vcld + vclp + (vswd*0.5)*(1 + ((vswp/vswd)*(1+cos(theta)) -
cos(theta+beta)));
ve = vcld + (vswd*0.5)*(1 + cos(theta+beta));
dvc = -(vswd*0.5)*(((vswp/vswd)*sin(theta)) - sin(theta+beta));
dve = -(vswd*0.5)*sin(theta+beta);
<u>۹_____</u>
function [vc,ve,dvc,dve] = gammacrankvol(theta, ENGINE DATA)
% gamma crankshaft drive volume variations and derivatives
% Added by Connor Speer - February 2017
% Argument: theta - current cycle angle [radians]
% Returned values:
% vc, ve - compression, expansion space volumes [m^3]
8
   dvc, dve - compression, expansion space volume derivatives
vclp = ENGINE DATA.Vclp;
vcld = ENGINE DATA.Vclp;
Dbore = ENGINE DATA.Dbore;
Pbore = ENGINE DATA.Pbore;
Dr1 = ENGINE DATA.Dr1;
Dr2 = ENGINE DATA.Dr2;
Dr3 = ENGINE DATA.Dr3;
Pr1 = ENGINE DATA.Pr1;
Pr2 = ENGINE DATA.Pr2;
Pr3 = ENGINE DATA.Pr3;
beta = ENGINE DATA.beta deg*(pi/180);
% vclp vcld % piston, displacer clearence vols [m^3]
% Dbore Pbore % displacer, piston bores [m]
```

```
% Dr1 Pr1 % displacer, piston desaxe offset in [m]
% Dr2 Pr2 % displacer, piston crank length (half stroke) in [m]
% Dr3 Pr3 % displacer, piston connecting rod lengths [m]
% beta % phase angle advance of displacer motion over piston [radians]
%*** Total volume is maximum at theta = 0 for gammas.
Ptheta2 = pi - theta;
Dtheta2 = Ptheta2 - beta;
Dtheta3 = pi - asin((-Dr1+(Dr2*sin(Dtheta2)))/Dr3);
Dr4 = Dr2*cos(Dtheta2) - Dr3*cos(Dtheta3);
Dr4max = sqrt(((Dr2+Dr3)^2) - (Dr1^2));
Dr4min = sqrt(((Dr3-Dr2)^2)-(Dr1^2));
ve = (vcld*0.5) + ((pi/4)*(Dbore^{2}))*(Dr4max-Dr4);
DVc = (((pi/4)*(Dbore^2))*(Dr4max-Dr4min)) - ve;
Ptheta3 = pi - asin((-Pr1+(Pr2*sin(Ptheta2)))/Pr3);
Pr4 = Pr2*cos(Ptheta2) - Pr3*cos(Ptheta3);
Pr4max = sqrt(((Pr2+Pr3)^2) - (Pr1^2));
PVc = (((pi/4) * (Pbore^{2})) * (Pr4max-Pr4));
vc = (vcld*0.5) + vclp + DVc + PVc;
dDtheta3
                                        (Dr2.*cos(Dtheta2))./(Dr3.*sqrt(1-(((-
Dr1+(Dr2.*sin(Dtheta2)))./Dr3).^2)));
dDr4 = Dr2.*sin(Dtheta2) + Dr3.*sin(Dtheta3).*dDtheta3;
dve = -(pi/4) * (Dbore^{2}) . * (dDr4);
dPtheta3
                                        (Pr2.*cos(Ptheta2))./(Pr3.*sqrt(1-(((-
Pr1+(Pr2.*sin(Ptheta2)))./Pr3).^2)));
dPr4 = Pr2.*sin(Ptheta2) + Pr3.*sin(Ptheta3).*dPtheta3;
dPVc = -(pi/4) * (Pbore^2) .* dPr4;
dDVc = -dve;
dvc = dDVc + dPVc;
<u>&_____</u>
function [vc,ve,dvc,dve] = alphacrankvol(theta, ENGINE DATA)
% alpha crankshaft drive volume variations and derivatives
% Added by Connor Speer - February 2017
% Argument: theta - current cycle angle [radians]
% Returned values:
% vc, ve - compression, expansion space volumes [m^3]
% dvc, dve - compression, expansion space volume derivatives
vclc = ENGINE DATA.Vclc;
vcle = ENGINE DATA.Vcle;
Cbore = ENGINE DATA.Cbore;
Ebore = ENGINE DATA.Ebore;
Cr1 = ENGINE DATA.Cr1;
Cr2 = ENGINE DATA.Cr2;
Cr3 = ENGINE DATA.Cr3;
Er1 = ENGINE DATA.Er1;
Er2 = ENGINE DATA.Er2;
Er3 = ENGINE DATA.Er3;
alpha = ENGINE DATA.alpha;
```

```
% vclc vcle % compression, expansion clearence vols [m^3]
% Cbore Ebore % compression, expansion piston bores [m]
% Cr1 Er1 % compression, expansion desaxe offset in [m]
% Cr2 Er2 % compression, expansion crank length (half stroke) in [m]
% Cr3 Er3 % compression, expansion connecting rod lengths [m]
% alpha % phase angle advance of expansion space [radians]
%*** Compression space volume is maximum at theta = 0 for alphas. Be
% careful defining crank angle 0 if using a desaxe offset.
Ctheta2 = theta - pi;
Etheta2 = Ctheta2 + alpha;
Ctheta3 = pi - asin((-Cr1+(Cr2*sin(Ctheta2)))/Cr3);
Cr4 = Cr2*cos(Ctheta2) - Cr3*cos(Ctheta3);
Cr4max = sqrt(((Cr2+Cr3)^2)-(Cr1^2));
vc = vclc + ((pi/4) * (Cbore^2)) * (Cr4max-Cr4);
Etheta3 = pi - asin((-Er1+(Er2*sin(Etheta2)))/Er3);
Er4 = Er2*cos(Etheta2) - Er3*cos(Etheta3);
Er4max = sqrt(((Er2+Er3)^2) - (Er1^2));
ve = vcle + ((pi/4) * (Ebore^{2})) * (Er4max-Er4);
                                         (-Cr2*cos(Ctheta2))/(Cr3*sqrt(1-(((-
dCtheta3
Cr1+(Cr2*sin(Ctheta2)))/Cr3).^2)));
dCr4 = -Cr2*sin(Ctheta2) + Cr3*sin(Ctheta3)*dCtheta3;
dvc = -(pi/4) * (Cbore^{2}) * (dCr4);
dEtheta3
                                         (-Er2*cos(Etheta2))/(Er3*sqrt(1-(((-
Er1+(Er2*sin(Etheta2)))/Er3).^2)));
dEr4 = -Er2*sin(Etheta2) + Er3*sin(Etheta3)*dEtheta3;
dve = -(pi/4) * (Ebore^{2}) * (dEr4);
<u>%_____</u>
```

The Simple Heat Exchanger Model Function Set

simple.m

```
function [SIMPLE DATA] = simple(ENGINE DATA, crank inc)
% simple analysis - including heat transfer and pressure drop effects
% Israel Urieli, 7/22/2002 (modified 12/3/2003 for temp plots)
% Modified 2/7/2010 to include grloss in hotsim & kolsim
% Modified 2/15/2010 logical reorganization
% Modified by Connor Speer, 2017 to include parasitic losses
% Modified by Connor Speer, October 2017, to use structure system.
%% Inputs:
% ENGINE DATA --> Structure containing engine geometry and operating point
% crank inc --> crank angle step size [degrees]
%% Outputs:
% SIMPLE DATA --> Structure containing results from the simple model
% Initialize variables
Tqk old = ENGINE DATA.Twk; % Initial cooler gas temp = cooler wall temp
Tqh old = ENGINE DATA.Twh; % Initial heater gas temp = heater wall temp
epsilon = 0.1; % allowable temperature error bound for cyclic convergence
(originally 1)
Terror = 10*epsilon; % Initial temperature error (to enter loop)
% Store original reference cycle results (no heat exchanger losses)
REF CYCLE DATA = adiabatic (ENGINE DATA, crank inc); % Perform an ideal
adiabatic simulation
while (Terror>epsilon)
   ADIABATIC DATA = adiabatic (ENGINE DATA, crank inc); % Perform an ideal
adiabatic simulation
   qrloss = regsim(ENGINE DATA, ADIABATIC DATA, crank inc);
                                                               % Calculate
regenerator enthalpy loss using results from ideal adiabatic simulation.
   Tqh new
                                                                              =
hotsim (ENGINE DATA, ADIABATIC DATA, ENGINE DATA. Twh, grloss, crank inc);
                                                                              8
Calculate new heater mean gas temperature
   Tgk new
                                                                              =
kolsim(ENGINE DATA, ADIABATIC DATA, ENGINE DATA.Twk, grloss, crank inc);
                                                                              9
Calculate new cooler mean gas temperature
  Terror = abs(Tgh old - Tgh new) + abs(Tgk old - Tgk new);
  Tqh old = Tqh new;
  Tqk old = Tqk new;
  Tgr = (Tgh old-Tgk old)/log(Tgh old/Tgk old);
  ENGINE DATA.Tgh = \overline{T}gh new;
  ENGINE DATA.Tgk = Tgk new;
  ENGINE DATA.Tgr = Tgr;
end
%% Store converged solution in SIMPLE DATA structure
SIMPLE DATA = ADIABATIC DATA;
```

```
SIMPLE DATA(1).grloss = grloss; % Regenerator enthalpy loss per cycle in (J)
SIMPLE DATA(1).Tgh = Tgh new; % Converged heater gas temperature (K)
SIMPLE DATA(1).Tgk = Tgk new; % Converged cooler gas temperature (K)
SIMPLE DATA(1).Tgr = Tgr; % Converged regenerator mean effective gas
temperature (K)
SIMPLE DATA(1).W dot ref = REF CYCLE DATA(end).W*ENGINE DATA.freq;
%% Print Out Simple Analysis Results
fprintf(' Regenerator net enthalpy
                                                  loss:
                                                            %.1f[W]\n',
SIMPLE DATA(1).qrloss*ENGINE DATA.freq);
fprintf('heater wall/gas temperatures:
                                           Twh
                                                 = %.1f[K],
                                                                 Тh
%.lf[K]\n',ENGINE DATA.Twh,SIMPLE DATA(1).Tgh);
                                         Twk
fprintf('cooler wall/gas temperatures:
                                                  =
                                                      %.1f[K],
                                                                 Τk
                                                                      =
%.lf[K]\n',ENGINE DATA.Twk,SIMPLE DATA(1).Tgk);
                        due to
fprintf('Power lost
                                         imperfect
                                                     heat
                                                             exchange:
%.1f[W]\n',SIMPLE DATA(1).W dot ref-(SIMPLE DATA(end).W*ENGINE DATA.freq));
% Print out ideal adiabatic analysis results
eff = SIMPLE DATA(end).W/SIMPLE DATA(end).Qh; % Thermal efficency
Qkpower = SIMPLE DATA(end).Qk*ENGINE DATA.freq; % Heat transferred to the
cooler (W)
Qrpower = SIMPLE DATA(end).Qr*ENGINE DATA.freq;
                                              % Heat transferred to the
regenerator (W)
                                              % Heat transferred to the
Qhpower = SIMPLE DATA(end).Qh*ENGINE DATA.freq;
heater (W)
Wpower = SIMPLE DATA(end).W*ENGINE DATA.freq; % Total power output for
ideal adiabatic model (W)
fprintf('====== Converged Ideal Adiabatic Analysis ======\n');
fprintf(' Heat transferred to the cooler: %.2f[W]\n', Qkpower);
fprintf(' Net heat transferred to the regenerator: %.2f[W]\n', Qrpower);
fprintf(' Heat transferred to the heater: %.2f[W]\n', Qhpower);
fprintf(' Total power output: %.2f[W]\n', Wpower);
fprintf(' Ideal adiabatic thermal efficiency: %.1f[%%]\n', eff*100);
```

foilfr.m

```
function [st,ht,fr] = foilfr(ENGINE DATAmu,N Re)
% evaluate regenerator wrapped foil stanton number, friction factor
% Israel Urieli, 7/22/2002
% Arguments:
   mu - gas dynamic viscosity [kq.m/s]
00
  N Re - Reynolds number
8
8
   ENGINE DATA - structure defining engine geometry and operating point
% Returned values:
% st - Stanton number
% ht - heat transfer coefficient [W/m^2.K]
% fr - Reynolds friction factor ( = re*fanning friction factor)
cp = ENGINE DATA.cp; % specific heat capacity at constant pressure [J/kg.K]
prandtl = ENGINE DATA.prandtl; % Prandtl number
```

```
dr = ENGINE_DATA.dr; % regenerator hydraulic diameter [m]
if (N_Re < 2000) % normally laminar flow
    fr = 24;
else
    fr = 0.0791*N_Re^0.75;
end
% From Reynolds simple analogy:
st=fr/(2*N_Re*prandtl);
ht=st*N Re*cp*mu/dr;</pre>
```

hotsim.m

```
function Tgh = hotsim(ENGINE DATA, ADIABATIC DATA, Twh, grloss, crank inc)
% evaluate heater average heat transfer performance
% Israel Urieli, 7/22/2002
% Modified 2/6/2010 to include regenerator qrloss
% Modified by Connor Speer 2017, October 2017. No globals.
%% Inputs:
% ENGINE DATA --> Structure containing engine geometry and operating point
% ADIABATIC DATA --> structure of adiabatic reference cycle results
% Twh --> heater wall temperature [K]
% grloss --> heat loss due to imperfect regenerator [J]
% crank inc --> crank angle step size for numerical integration (degrees)
%% Output:
% Tgh --> heater average gas temperature [K]
% Preallocate space for loop variables
gah = zeros(1,360/crank inc);
N Re = zeros(1,360/crank inc);
% Calculating the Reynolds number over the cycle
for i = 1:1:(360/crank inc)+1
                                    (ADIABATIC DATA(i).m dot rh
  gah(i)
                                                                         +
ADIABATIC DATA(i).m dot he) * ENGINE DATA.omega/2;
  gh = gah(i)/ENGINE DATA.ah;
   [mu,kgas,N Re(i)] = reynum(ENGINE DATA,ENGINE DATA.Tgh,gh,ENGINE DATA.dh);
end
% Average and maximum Reynolds number
N_Re_avg = mean(N Re(1:(360/crank inc)));
N Re max = max(N Re(1:(360/crank inc)));
[ht,fr] = pipefr(ENGINE DATA,ENGINE DATA.dh,mu,N Re avg); % Heat transfer
coefficient
% Calculate the average gas temperature in the heater
Tgh = Twh - (ADIABATIC DATA((360/crank inc)+1).Qh + qrloss)*...
   ENGINE DATA.freq/(ht*ENGINE DATA.awgh); % Heater gas temperature [K]
```

```
fprintf(' Average Reynolds number : %.lf\n',N_Re_avg)
fprintf(' Maximum Reynolds number : %.lf\n',N_Re_max)
fprintf(' Convective heat transfer coefficient [W/m^2*K] : %.2f\n',ht)
fprintf('heater wall/gas temperatures: Twh = %.lf[K], Tgh =
%.lf[K]\n',Twh,Tgh);
```

kolsim.m

```
function Tgk = kolsim(ENGINE DATA, ADIABATIC DATA, Twk, grloss, crank inc)
% evaluate cooler average heat transfer performance
% Israel Urieli, 7/22/2002
% Modified 2/6/2010 to include regenerator qrloss
% Modified by Connor Speer 2017, October 2017. No globals.
%% Inputs:
% ENGINE DATA --> Structure containing engine geometry and operating point
% ADIABATIC DATA --> structure of adiabatic reference cycle
% Twk --> cooler wall temperature [K]
% qrloss --> heat loss due to imperfect regenerator [J]
% crank inc --> crank angle step size for numerical integration (degrees)
%% Output:
% Tgk --> cooler average gas temperature [K]
% Preallocate space for loop variables
gak = zeros(1,360/crank inc);
N Re = zeros(1,360/crank inc);
% Calculating the Reynolds number over the cycle
for i = 1:1:(360/crank inc)+1
                                    (ADIABATIC DATA(i).m dot ck
   gak(i)
                                                                           +
ADIABATIC DATA(i).m dot kr)*ENGINE DATA.omega/2;
   gk = gak(i)/ENGINE DATA.ak;
   [mu,kgas,N Re(i)] = reynum(ENGINE DATA,ENGINE DATA.Tgk,gk,ENGINE DATA.dk);
end
% Average and maximum Reynolds number
N Re avg = mean(N Re(1:(360/crank inc)));
N Re max = max(N Re(1:(360/crank inc)));
[ht,fr] = pipefr(ENGINE DATA, ENGINE DATA.dk, mu, N Re avg); % Heat transfer
coefficient
                                  (ADIABATIC DATA(360/crank inc+1).Qk
Tak
        =
                 Twk
grloss) * ENGINE DATA.freg/...
    (ht*ENGINE DATA.awgk); % Cooler gas temperature [K]
fprintf(' Average Reynolds number : %.1f\n', N Re avg)
fprintf(' Maximum Reynolds number : %.lf\n',N Re max)
fprintf(' Heat transfer coefficient [W/m^2*K] : %.2f\n',ht)
fprintf('cooler wall/gas temperatures: Twk = %.1f[K],
                                                                    Tqk
                                                                         =
.1f[K] \setminus n', Twk, Tgk);
```

matrixfr.m

```
function [st,fr] = matrixfr(ENGINE_DATA,N_Re)
% evaluate regenerator mesh matrix stanton number, friction factor
% Israel Urieli, 7/22/2002
% Modified by Connor Speer, October 2017. No globals.
% Arguments:
% N_Re - Reynolds number
% ENGINE_DATA - structure defining engine geometry and operating point
% Returned values:
% st - Stanton number
% fr - Reynolds friction factor ( = re*fanning friction factor)
prandtl = ENGINE_DATA.prandtl; % Prandtl number
% equations taken from Kays & London (1955 edition)
st = 0.46*N_Re^(-0.4)/prandtl; % Stanton Number
fr = 54 + 1.43*N_Re^0.78; % Reynolds friction factor
```

pipefr.m

```
function [ht,fr] = pipefr(ENGINE DATA,d,mu,N Re)
% evaluate heat transfer coefficient, Reynolds friction factor
% Israel Urieli, 7/22/2002 (corrected header 2/20/2011)
% Connor Speer, October 2017. No globals.
% Arguments:
% d - hydraulic diameter [m]
% mu - gas dynamic viscosity [kg.m/s]
% re - Reynolds number
% Returned values:
 ht - heat transfer coefficient [W/m^2.K]
% fr - Reynolds friction factor ( = re*fanning friction factor)
cp = ENGINE DATA.cp; % specific heat capacity at constant pressure [J/kg.K]
prandtl = ENGINE DATA.prandtl; % Prandtl number
% Personal communication with Alan Organ, because of oscillating
% flow, we assume that flow is always turbulent. Use the Blasius
% relation for all Reynolds numbers:
fr = 0.0791*N Re^0.75;
% Modified by Jason Michaud, 6/9/2017
% If the flow is laminar, use the circular pipe laminar friction factor
% equation. If the Reynolds number is between 5*10^3 and 1*10^5 use Blasius
% friction factor equation for fully developed turbulent flow in pipe.
% if re <= 2300
    fr = 64/re;
2
```

```
% elseif (3000 <= re) && (re <=200000)
% fr = 0.0791*re^(-0.25);
% else
% return
% end
% From Reynolds simple analogy:
ht = fr*mu*cp/(2*d*prandtl);
```

regsim.m

```
function qrloss = regsim(ENGINE DATA, ADIABATIC DATA, crank inc)
% Evaluate the effectiveness and performance of the regenerator
% Israel Urieli, 7/23/2002 - Modified 2/15/2010
% modified 11/27/2010 to include 'no regenerator matrix'
% Modified by Connor Speer, October 2017. No globals.
%% Inputs:
% ENGINE DATA --> Structure containing engine geometry and operating point
% ADIABATIC DATA --> Structure containing ideal adiabatic model results
% crank inc --> crank angle step size for simulation in [degrees]
%% Output:
% qrloss --> regenerator net enthalpy loss [J]
% Preallocate space for loop variables
N Re = zeros(1, 360/crank inc);
gar = zeros(1,360/crank inc);
qreg = zeros(1,360/crank inc);
% Reynolds number over the cycle
for i = 1:1:(360/crank inc)+1
                                      (ADIABATIC DATA(i).m dot kr
    gar(i)
                       =
                                                                               +
ADIABATIC DATA(i).m dot rh) * ENGINE DATA.omega/2;
    gr = gar(i)/ENGINE DATA.ar;
    [mu,kgas,N Re(i)]
                                                                               =
reynum (ENGINE DATA, ENGINE DATA.Tgr, gr, ENGINE DATA.dr);
end
% Average and maximum Reynolds number
N Re avg = mean(N Re(1:(360/crank inc)));
N Re max = max(N Re(1:(360/crank inc)));
% Stanton number, number of transfer units, regenerator effectiveness
if (strncmp(ENGINE DATA.regen matrix type, 'm', 1))
    [N St, fr] = matrixfr(ENGINE DATA, N Re avg);
elseif (strncmp(ENGINE DATA.regen matrix type, 'f', 1))
    [N St, ht, fr] = foilfr (ENGINE DATA, ENGINE DATA.dr, mu, N Re avg);
elseif (strncmp(ENGINE DATA.regen matrix type, 'n', 1))
    [N St, ht, fr] = foilfr(ENGINE DATA, ENGINE DATA.dr, mu, N Re avg);
end
NTU = N_St*ENGINE_DATA.awgr/(2*ENGINE_DATA.ar);
effect = NTU/(NTU + 1);
```

```
%% Calculate qrloss
% Find the amount of heat transferred unidirectionally to the working gas
% from the regenerator in a complete cycle. Use the effectiveness to
% calculate the regenerator enthalpy loss.
qrmin = min([ADIABATIC_DATA.Qr]);
qrmax = max([ADIABATIC_DATA.Qr]);
qrloss = (1 - effect)*(qrmax - qrmin); %[W]
% Regenerator simple analysis results:
```

reynum.m

```
function [mu,kgas,re] = reynum(ENGINE DATA,t,g,d)
% evaluate dynamic viscosity, thermal conductivity, Reynolds number
% Israel Urieli, 7/22/2002 (mu units correction 2/13/2011)
% Modified by Connor Speer, October 2017. No globals.
% Arguments:
% t - gas temperature [K]
8
   q - mass flux [kg/m^2.s]
8
   d - hydraulic diameter [m]
8
   ENGINE DATA - structure defining engine geometry and operating point
% Returned values:
% mu - gas dynamic viscosity [kg/m.s]
% kgas - gas thermal conductivity [W/m.K]
% re - Reynolds number
cp = ENGINE DATA.cp; % specific heat capacity at constant pressure [J/kg.K]
mu0 = ENGINE DATA.mu0; % dynamic viscosity at reference temp t0 [kg.m/s]
t0 = ENGINE DATA.t0; % reference temperature [K]
t suth = ENGINE DATA.t suth; % Sutherland constant [K]
prandtl = ENGINE DATA.prandtl; % Prandtl number
mu = mu0*(t0 + t suth)/(t + t suth)*(t/t0)^{1.5};
kgas = cp*mu/prandtl;
re = abs(q) * d/mu;
if(re < 1)
   re = 1;
end
```

The Parasitic Losses Function Set

worksim.m

```
function
                  [dwork h, dwork r, dwork k, pdropk, pdroph, pdropr]
worksim(ENGINE DATA, REF CYCLE_DATA, crank_inc)
% Evaluate the pressure drop available work loss [J]
% Israel Urieli, 7/23/2002, Modified by Connor Speer - June 2017
% Modified by Connor Speer, October 2017. No globals.
% Inputs:
% crank inc --> crank angle step size for simulation in [degrees]
% Outputs:
% dwork --> pressure drop available work loss [J]
% pdropk --> pressure drop across the cooler [Pa]
% pdroph --> pressure drop across the heater [Pa]
% pdropr --> pressure drop across the regenerator [Pa]
dtheta = 2*pi/(360/crank inc);
dwork h = 0; % initialize pumping work loss
dwork r = 0; % initialize pumping work loss
dwork k = 0; % initialize pumping work loss
% Preallocate space for loop variables
pdropk = zeros(1,360/crank inc);
pdroph = zeros(1,360/crank inc);
pdropr = zeros(1,360/crank inc);
dp = zeros(1,360/crank inc);
pc = zeros(1,360/crank inc);
pe = zeros(1,360/crank inc);
N Re = zeros(1,360/crank inc);
for i = 1:1:(360/crank inc)
    % Cooler
                              ([REF CYCLE DATA(i).m dot ck]
   m dot k
                                                                           +
[REF CYCLE DATA(i).m dot kr])*ENGINE DATA.omega/(2*ENGINE DATA.ak); % mass
flux in [kq/s*m^2]
    [mu,kqas,N Re(i)]
reynum (ENGINE DATA, ENGINE DATA.Tqk, m dot k, ENGINE DATA.dk); % Reynolds number
for crank angle increment
    [ht,fr] = pipefr(ENGINE DATA,ENGINE DATA.dk,mu,N Re(i)); % Reynolds
friction factor for each crank angle increment
   pdropk(i)
2*fr*mu*ENGINE DATA.Vk*m dot k*ENGINE DATA.lk/(REF CYCLE DATA(i).mk*ENGINE DA
TA.dk^2); % Pressure drop across cooler in [Pa].
    % Work Lost due to pressure drop in the cooler
    dwork k = dwork k + dtheta*pdropk(i)*REF CYCLE DATA(i).dVe; % pumping
work [J]
    % Regenerator
                    =
                                    (REF CYCLE DATA(i).m dot kr
   m dot r
                                                                            +
```

```
REF CYCLE DATA(i).m dot rh)*ENGINE DATA.omega/(2*ENGINE DATA.ar);
```

```
[mu,kgas,N Re(i)]
reynum (ENGINE DATA, ENGINE DATA.Tgr, m dot r, ENGINE DATA.dr);
    if(strncmp(ENGINE DATA.regen matrix type, 'm', 1))
         [st,fr] = matrixfr(ENGINE DATA, N Re(i));
    elseif (strncmp(ENGINE DATA.regen matrix type,'f',1))
         [st,ht,fr] = foilfr(ENGINE DATA.dr,mu,N Re(i));
    end
   pdropr(i)
2*fr*mu*ENGINE DATA.Vr*m dot r*ENGINE DATA.lr/(REF CYCLE DATA(i).mr*ENGINE DA
TA.dr^2;
    % Work Lost due to pressure drop in the regenerator
    dwork r = dwork r + dtheta*pdropr(i)*REF CYCLE DATA(i).dVe; % pumping
work [J]
    % Heater
   m dot h
                                     (REF CYCLE DATA(i).m dot rh
                                                                             +
                       =
REF CYCLE DATA(i).m dot he)*ENGINE DATA.omega/(2*ENGINE DATA.ah);
    [mu,kgas,N Re(i)]
                                                                             =
reynum (ENGINE DATA, ENGINE DATA.Tgh, m dot h, ENGINE DATA.dh);
    [ht,fr] = pipefr(ENGINE DATA,ENGINE DATA.dh,mu,N Re(i));
    pdroph(i)
2*fr*mu*ENGINE DATA.Vh*m dot h*ENGINE DATA.lh./(REF CYCLE DATA(i).mh*ENGINE D
ATA.dh^2);
    % Work Lost due to pressure drop in the heater
    dwork h = dwork h + dtheta*pdroph(i)*[REF CYCLE DATA(i).dVe]; % pumping
work [J]
    % Overall Pressure Drop
    dp(i) = pdropk(i) + pdropr(i) + pdroph(i);
   pc(i) = REF CYCLE DATA(i).p; % Baseline pressure is defined to be the
compression space pressure.
   pe(i) = pc(i) + dp(i); % Expansion space pressure is the compression
space pressure plus the total pressure drop.
end
%% Add one last value to the results so the length matches the other
variables
pdropk((360/crank inc)+1) = pdropk(1);
pdropr((360/crank inc)+1) = pdropr(1);
pdroph((360/crank inc)+1) = pdroph(1);
dp((360/crank inc)+1) = dp(1);
pc((360/crank inc)+1) = pc(1);
pe((360/crank inc)+1) = pe(1);
```

FW_Subfunction_v3.m

function [W_ind, FW, W_shaft]
FW_Subfunction_v3(theta,P_engine,P_buffer,V_engine,effect, wantPlot)

% Forced Work subfunction updated to run faster without plotting

=

```
% functionality
% Forced Work 2 - Written by Connor Speer, November 2016
% *** Forced Work modificiations - April 2017 - Calynn Stumpf
% *** Modified in June 2017 to work as a subfunction.
% Modified August 2017 by Steven Middleton and Shahzeb Mirza
% See Senft Pg 17 for a definition of forced work.
% Inputs:
% theta --> Vector of engine crank angles, Vmax = 0 deg, [deg]
% P engine --> Vector of engine pressures corresponding to theta vector [Pa]
% P buffer --> Vector of buffer pressures corresponding to theta vector [Pa]
% V engine --> Vector of engine volumes corresponding to theta vector [m^3]
% effect --> Constant mechanism effectiveness
% wantPlot --> True or False
% Outputs:
% W ind --> Indicated work in [J]
\% FW --> Forced work in [J]
% W shaft --> Shaft work out in [J]
% Notes:
% Orientation of Pressure and Volume arrays must be correct (Indicator
% diagram must 'turn' the desired way
E = effect; % Mechanism effectiveness
P cycle = P engine; % Engine Pressure = Cycle Pressure
Vtotal = V engine; % Engine Volume = Total Volume
W ind = polyarea(Vtotal, P cycle); % Calculate Indicated Work by Integrating
the Indicator Diagram
%% Plot Set-Up
set(0, 'defaultfigurecolor', [1 1 1])
% % Location of Figures
% x = 500;
% y = 500;
2
% % Size of Figures
% width = 550;
% height = 400;
2
% % Font For Figures
% font = 'Times New Roman';
% font size = 8;
```

```
% % Location of Figures
% x = 500;
% y = 500;
8
% % Size of Figures
% width = 326;
% height = 275;
8
% % Font For Figures
% font = 'Times New Roman';
% font size = 10;
% % Location of Figures
% x = 500;
% y = 500;
2
% % Size of Figures
% width = 550;
% height = 400;
2
% % Font For Figures
% font = 'Times New Roman';
% font size = 16;
% Location of Figures
x = 500;
y = 500;
% Size of Figures
width = 326;
height = 275;
% Font For Figures
font = 'Arial';
font size = 11;
% To change line width for plots, say "'LineWidth',2"
%% Forced Work Calculations
% Calculate the difference b/w cycle and buffer pressure at each point
P diff = P cycle - P buffer;
dV = delta(V_engine);
FW = 0;
if wantPlot
  figure('Position', [x y width height]);
  hold on;
end
```

```
nLines = 350;
spacing = floor(length(dV)/nLines);
% Use DEFINITION of Forced work and Riemann Sums to find final FW
for i = 1:length(dV)
    if (sign(dV(i)) ~= sign(P diff(i))) % If they are of opposite sign
        FW = FW + abs(P diff(i) * dV(i));
        if (wantPlot) && (mod(i, spacing) == 0)
            plot([V_engine(i)
                                                V engine(i)], [P engine(i)./1000
P buffer(i)./1000], 'r', 'LineWidth',3);
        end
    end
end
W shaft = (E*W \text{ ind}) - (((1/E) - E)*FW);  Shaft Work
if wantPlot
    P1 = plot(V engine, P engine./1000, 'b', 'LineWidth',2);
    P2 = plot(V engine, P buffer./1000, 'k', 'LineWidth', 2);
    xlabel('Engine Volume (m^3)', 'FontName', font, 'FontSize', font size)
    ylabel('Pressure (kPa)', 'FontName', font, 'FontSize', font_size)
    legend([P1 P2], {'Engine Pressure', 'Buffer Pressure'})
    set(gca, 'fontsize', font size);
    set(gca, 'FontName', font)
     xlim([1.34e-3 1.8e-3])
8
    ylim([800 1250])
    hold off
end
% Display Indicated Work
Text1 = ['Indicated Cycle Work: ',num2str(W ind),' J'];
disp(Text1);
% Total Forced Work
Text2 = ['Total Forced Work: ',num2str(FW),' J'];
disp(Text2);
% Display Shaft Work (See Senft pg 106)
Text3 = ['Shaft Work:
                                ',num2str(W shaft),' J'];
disp(Text3);
end
delta.m
```

```
function [ DELTA ] = delta( Vector)
% This function calculates the wrapping derivative of each element in the
% Array (assumes cyclic)
% Takes an vector, Outputs an vector of the same size
if (isvector(Vector))
    DELTA = Vector*0;
    DELTA(2:end-1) = (Vector(3:end)-Vector(1:end-2));
    DELTA(1) = (Vector(2)-Vector(end));
    DELTA(end) = (Vector(1)-Vector(end-1));
```

```
DELTA = DELTA/2;
else
    % Array is not a vector
    fprintf('Provided number to delta function is not a vector');
end
```

end

Engine Specific Functions

Chapter_3_Plots.m

```
% Chapter 3 Plots.m - Written by Connor Speer - October 2017
clear,clc,close all;
%% Plot Aesthetics
set(0,'defaultfigurecolor',[1 1 1])
% Location of Figures
x = 500;
y = 500;
% Size of Figures
width = 550;
height = 400;
% Font For Figures
font = 'Arial';
font size = 11;
%% FIGURE 3.X Isothermal Model vs. Adiabatic Model
% % Thermal Source Temperature Variation
% Min TH = 273 + 25; % Minimum thermal source temp to be simulated in [K].
% Max TH = 273 + 500; % Maximum thermal source temp to be simulated in [K].
% TH inc = 10; % Thermal source temp increment in [K].
8
% Vdead = 874.35*1e-6;
00
% % Isothermal Model Set-Up
% crank inc = 1;
% Model Code = 1; % Code specifying which model to run.
% Losses Code = 0; % Code specifying which losses subfunction to run
% part traj on off = 0; % No particle trajectory calculation
% ENGINE DATA = HTG ENGINE DATA; % Structure defining engine geometry and
operating conditions.
8
\% counter = 1;
% % counter max = length (Min TH:TH inc:Max TH);
00
% for TH = Min TH:TH inc:Max TH
   ENGINE DATA.Tsource = TH;
8
8
     ENGINE DATA.Tgh = TH;
8
    ENGINE DATA.Twh = TH;
8
     ENGINE DATA. Tge = TH;
00
00
     [ISOTHERMAL DATA, LOSSES DATA, PARTICLE TRAJECTORY DATA, ENGINE DATA] =
. . .
00
     sea(ENGINE DATA, crank inc, Model Code, Losses Code, part traj on off);
8
```

```
8
      ISOTHERMAL SOL(counter).W ind = ISOTHERMAL DATA(end).W;
8
                                     ISOTHERMAL SOL(counter).efficiency
ISOTHERMAL DATA(end).W/ISOTHERMAL DATA(end).We;
8
      ISOTHERMAL SOL(counter).p = [ISOTHERMAL DATA.p];
8
                ISOTHERMAL SOL(counter).Vtotal = [ISOTHERMAL DATA.Ve] +
[ISOTHERMAL DATA.Vc] + ...
8
          repelem(Vdead,length([ISOTHERMAL DATA.Ve]));
8
8
      counter = counter + 1;
% end
2
% % Adiabatic Model Set-Up
% crank inc = 1;
% Model Code = 2; % Code specifying which model to run.
% Losses Code = 0; % Code specifying which losses subfunction to run
% part traj on off = 0; % No particle trajectory calculation
% ENGINE DATA = HTG ENGINE DATA; % Structure defining engine geometry and
operating conditions.
8
\% counter = 1;
% % counter max = length (Min TH:TH inc:Max TH);
00
% for TH = Min TH:TH inc:Max TH
      ENGINE DATA.Tsource = TH;
00
8
      ENGINE DATA.Tgh = TH;
8
      ENGINE DATA. Twh = TH;
8
      ENGINE DATA. Tge = TH;
2
8
      [ADIABATIC DATA, LOSSES DATA, PARTICLE TRAJECTORY DATA, ENGINE DATA] =
. . .
8
      sea(ENGINE DATA, crank inc, Model Code, Losses Code, part traj on off);
00
00
      ADIABATIC SOL(counter).W ind = ADIABATIC DATA(end).W;
8
                                     ADIABATIC SOL(counter).efficiency
                                                                              =
ADIABATIC DATA(end).W/ADIABATIC DATA(end).Qh;
      ADIABATIC SOL(counter).p = [ADIABATIC DATA.p];
8
8
                  ADIABATIC SOL(counter).Vtotal = [ADIABATIC DATA.Ve]
[ADIABATIC DATA.Vc] + ...
8
         repelem(Vdead,length([ADIABATIC DATA.Ve]));
8
      counter = counter + 1;
8
% end
% % Indicated Work vs TH
% figure('Position', [x y 326 275])
% TH_Range = Min_TH:TH inc:Max TH;
% TH Range Celcius = TH Range - 273.15;
% hold on
% plot(TH Range Celcius, [ISOTHERMAL SOL.W ind],'b','LineWidth',2);
% plot(TH Range Celcius, [ADIABATIC SOL.W ind],'r','LineWidth',2);
% xlabel('Heater Gas Temperature (°C)', 'FontName', font, 'FontSize', font size);
% ylabel('Indicated Work (J)','FontName',font,'FontSize',font size);
% ylim([0 inf])
% legend('Isothermal Model','Adiabatic Model','Location','SouthEast')
% set(gca,'fontsize',font size);
% set(gca, 'FontName', font)
% hold off
2
```

```
% % Efficiency vs TH
% figure('Position', [x y 326 275])
% TH_Range = Min_TH:TH_inc:Max TH;
% TH Range Celcius = TH Range - 273.15;
% hold on
% plot(TH Range Celcius, [ISOTHERMAL SOL.efficiency].*100,'b','LineWidth',2);
% plot(TH Range Celcius, [ADIABATIC SOL.efficiency].*100,'r','LineWidth',2);
% xlabel('Heater Gas Temperature (°C)', 'FontName', font, 'FontSize', font size);
% ylabel('Thermal Efficiency (%)','FontName',font,'FontSize',font size);
% ylim([0 inf])
% legend('Isothermal Model','Adiabatic Model','Location','SouthEast')
% set(gca,'fontsize',font size);
% set(gca, 'FontName', font)
% hold off
0
% % High Temperature Indicator Diagram Comparison
% figure('Position', [x y 326 275])
% hold on
8
                                             plot([ISOTHERMAL SOL(end).Vtotal],
[ISOTHERMAL SOL(end).p]./1000, 'b', 'LineWidth',2);
                                              plot([ADIABATIC SOL(end).Vtotal],
00
[ADIABATIC SOL(end).p]./1000,'r','LineWidth',2);
% xlabel('Engine Volume (m^3)','FontName',font,'FontSize',font_size);
% ylabel('Pressure (kPa)','FontName',font,'FontSize',font size);
% ylim([700 1400])
% legend('Isothermal Model','Adiabatic Model','Location','NorthEast')
% set(gca,'fontsize',font size);
% set(gca, 'FontName', font)
% hold off
2
% % Low Temperature Indicator Diagram Comparison
% figure('Position', [x y 326 275])
% hold on
8
                                               plot([ISOTHERMAL SOL(1).Vtotal],
[ISOTHERMAL SOL(1).p]./1000, 'b', 'LineWidth',2);
                                                plot([ADIABATIC SOL(1).Vtotal],
2
[ADIABATIC SOL(1).p]./1000, 'r', 'LineWidth', 2);
% xlabel('Engine Volume (m^3)','FontName',font,'FontSize',font size);
% ylabel('Pressure (kPa)','FontName',font,'FontSize',font size);
% legend('Isothermal Model','Adiabatic Model','Location','NorthEast')
% set(gca,'fontsize',font size);
% set(gca, 'FontName', font)
% hold off
% % Mean Pressure Variation
% Min pmean = 100000; % Minimum mean pressure to be simulated in [Pa].
% Max pmean = 1000000; % Maximum mean pressure to be simulated in [Pa].
% pmean inc = 100000; % mean pressure increment in [Pa].
2
% % Isothermal Model Set-Up
% crank inc = 1;
% Model Code = 1; % Code specifying which model to run.
% Losses Code = 0; % Code specifying which losses subfunction to run
% part traj on off = 0; % No particle trajectory calculation
% ENGINE DATA = HTG ENGINE DATA; % Structure defining engine geometry and
operating conditions.
8
```

```
% counter = 1;
% % counter max = length (Min TH:TH inc:Max TH);
8
% for pmean = Min pmean:pmean inc:Max pmean
00
      ENGINE DATA.pmean = pmean;
8
8
      [ISOTHERMAL DATA, LOSSES DATA, PARTICLE TRAJECTORY DATA, ENGINE DATA] =
. . .
8
      sea(ENGINE DATA, crank inc, Model Code, Losses Code, part traj on off);
8
8
      ISOTHERMAL SOL(counter).W ind = ISOTHERMAL DATA(end).W;
00
                                     ISOTHERMAL SOL(counter).efficiency
                                                                               =
ISOTHERMAL DATA (end) .W/ISOTHERMAL DATA (end) .We;
0
8
      counter = counter + 1;
% end
8
% % Adiabatic Model Set-Up
% crank inc = 1;
% Model Code = 2; % Code specifying which model to run.
% Losses Code = 0; % Code specifying which losses subfunction to run
% part traj on off = 0; % No particle trajectory calculation
% ENGINE DATA = HTG ENGINE DATA; % Structure defining engine geometry and
operating conditions.
8
% counter = 1;
% % counter max = length (Min TH:TH inc:Max TH);
2
% for pmean = Min pmean:pmean inc:Max pmean
8
      ENGINE DATA.pmean = pmean;
00
00
       [ADIABATIC DATA, LOSSES DATA, PARTICLE TRAJECTORY DATA, ENGINE DATA] =
. . .
8
      sea(ENGINE DATA, crank inc, Model Code, Losses Code, part traj on off);
8
%
      ADIABATIC SOL(counter).W ind = ADIABATIC DATA(end).W;
                                      ADIABATIC SOL(counter).efficiency
00
ADIABATIC DATA(end).W/ADIABATIC DATA(end).Qh;
00
8
      counter = counter + 1;
% end
00
% figure('Position', [x y width height])
% pmean Range kPa = Min pmean:pmean inc:Max pmean;
% hold on
% plot(pmean Range kPa, [ISOTHERMAL SOL.W ind],'LineWidth',2);
% plot(pmean Range kPa, [ADIABATIC SOL.W ind], 'LineWidth',2);
% xlabel('Mean Pressure (kPa)','FontName',font,'FontSize',font size);
% ylabel('Indicated Work (J)', 'FontName', font, 'FontSize', font size);
% legend('Isothermal Model','Adiabatic Model','Location','Northwest')
0
% figure('Position', [x y width height])
% pmean Range kPa = Min pmean:pmean inc:Max pmean;
% hold on
% plot(pmean Range kPa, [ISOTHERMAL SOL.efficiency].*100,'LineWidth',2);
% plot(pmean Range kPa, [ADIABATIC SOL.efficiency].*100,'LineWidth',2);
% xlabel('Mean Pressure (kPa)', 'FontName', font, 'FontSize', font size);
```

```
% ylabel('Thermal Efficiency (%)','FontName',font,'FontSize',font size);
% legend('Isothermal Model','Adiabatic Model','Location','Northwest')
%% FIGURE 3.X Regenerator Enthalpy Loss
% % crank inc = 1; % Crank angle step size for model output [degrees].
8 8
% % % Regenerator Porosity Variation
% % Min porosity = 0.8; % Minimum porosity to be simulated.
% % Max porosity = 0.99; % Maximum porosity to be simulated.
% % porosity inc = 0.005; % Porosity increment.
000
% % Model Code = 3; % Code specifying which model to run (3 = Simple Model).
% % Losses Code = 2; % Code specifying which losses subfunction to run
\% % part traj on off = 0; % No particle trajectory calculation
8 8
% % ENGINE DATA = HTG ENGINE DATA; % Structure defining engine geometry and
operating conditions.
8 8
% % % Vary Porosity in 2nd Order Model:
                     2
                                           POROSITY DATA
HTG 2nd Order Vary('regen matrix porosity', Min porosity, Max porosity, porosity
inc,ENGINE DATA);
00
% % % Find porosity at maximum power
% [Max Power,max power index] = max([POROSITY DATA.W dot]);
% % porosity at Max Power = Min porosity + (max power index-1)*porosity inc;
8 8
% % % Find porosity at maximum efficiency
% % [Max Efficiency,max efficiency index] = max([POROSITY DATA.eff thermal]);
% % porosity at Max Efficiency = Min porosity + (max efficiency index-
1) *porosity_inc;
8 8
% % % Find porosity at stall
% [Min Power, free run index] = min(abs([POROSITY DATA.W dot]));
% % porosity at Free Run = Min porosity + (free run index-1)*porosity inc;
8 8
% % % Power and Efficiency vs. Regenerator Porosity
% % figure('Position', [x y 326 275])
% % porosity Range = Min porosity:porosity inc:Max porosity;
% % porosity Range percent = porosity Range.*100;
8 8
% % porosity Power Range = [POROSITY DATA.W dot];
% % porosity Efficiency Range = [POROSITY DATA.eff thermal].*100;
% % % % Plot Power on the left axis
% % % yyaxis left
% % plot(porosity Range percent,porosity Power Range,'r','LineWidth',2)
% % % vlim([0 inf])
% % ylabel('Power Output (W)','FontName',font,'FontSize',font size)
% % % set(gca,'ycolor','r')
% % % % Plot efficiency on the right axis
% % % yyaxis right
                                      2
                                                                             2
plot (porosity Range percent, porosity Efficiency Range, 'b', 'LineWidth', 2)
% % ylim([0 inf])
% % % ylabel('Thermal Efficiency (%)','FontName',font,'FontSize',font size)
% % % set(gca,'ycolor','b')
```

```
% % % xlabel('Renerator Porosity (%)','FontName',font,'FontSize',font size)
% % % legend('Power','Efficiency','Location','South')
% % % set(gca,'fontsize',font size);
% % % set(gca, 'FontName', font)
e e
% % % Regen flow friction and enthalpy Losses vs Porosity
% % figure('Position', [x y 326 275])
% % plot(porosity Range percent, [POROSITY DATA.Q grloss], 'k', 'LineWidth',2)
% % ylim([0 inf])
% ylabel('Enthalpy Loss (W)', 'FontName', font, 'FontSize', font size)
% % xlabel('Regenerator Porosity (%)','FontName',font,'FontSize',font size)
% % set(gca,'fontsize',font size);
% % set(gca, 'FontName', font)
2
% crank inc = 1; % Crank angle step size for model output [degrees].
8
% % Regenerator Wire Diameter Variation
% Min regen wire = 2e-05; % Minimum regenerator wire diameter to be simulated
in [m].
% Max regen wire = 15e-05; % Maximum regenerator wire diameter to be
simulated in [m].
% regen wire inc = 0.5e-05; % Regenerator wire diameter increment in [m].
% Model Code = 3; % Code specifying which model to run (3 = Simple Model).
% Losses Code = 2; % Code specifying which losses subfunction to run
% part traj on off = 0; % No particle trajectory calculation
2
% ENGINE DATA = HTG ENGINE DATA; % Structure defining engine geometry and
operating conditions.
00
% % Vary Porosity in 2nd Order Model:
2
                              REGEN WIRE DATA
HTG 2nd Order Vary('regen wire diameter', Min regen wire, Max regen wire, regen
wire_inc,ENGINE DATA);
2
% % % Power and Efficiency vs. Regenerator Wire Diameter
% % figure('Position', [x y 326 275])
% % regen wire Range = Min regen wire:regen wire inc:Max regen wire;
% % regen wire Range mm = regen wire Range.*1000;
8 8
% % regen wire Power Range = [REGEN WIRE DATA.W dot];
% % regen wire Efficiency Range = [REGEN WIRE DATA.eff thermal].*100;
8 8
% % % Plot Power on the left axis
% % yyaxis left
% % plot(regen wire Range mm, regen wire Power Range, 'r', 'LineWidth', 2)
% % ylim([0 inf])
% ylabel('Power Output (W)','FontName',font,'FontSize',font size)
% % set(gca,'ycolor','r')
% % % Plot efficiency on the right axis
% % yyaxis right
% % plot(regen wire Range mm, regen wire Efficiency Range, 'b', 'LineWidth',2)
% % ylim([0 inf])
% ylabel('Thermal Efficiency (%)', 'FontName', font, 'FontSize', font size)
% % set(gca, 'ycolor', 'b')
```

```
xlabel('Renerator
                                                       Wire
0
             2
                                                                       Diameter
(mm)', 'FontName', font, 'FontSize', font size)
% % legend('Power','Efficiency','Location','South')
% % set(gca,'fontsize',font size);
% % set(gca, 'FontName', font)
8
% % Regen enthalpy Losses vs Porosity
% figure('Position', [x y 326 275])
% plot(regen wire Range mm, [REGEN WIRE DATA.Q qrloss], 'k', 'LineWidth', 2)
% ylim([0 inf])
% ylabel('Enthalpy Loss (W)', 'FontName', font, 'FontSize', font size)
2
                xlabel('Regenerator
                                                                        Diameter
                                                   Wire
(mm)', 'FontName', font, 'FontSize', font size)
% set(gca,'fontsize',font size);
% set(gca, 'FontName', font)
%% Figure 3.X: Power and Efficiency vs. Frequency Using 2nd Order Model
% crank inc = 1; % Crank angle step size for model output [degrees].
00
% % Mean Pressure Variation
% Min freq = 0.5; % Minimum frequency to be simulated in [Hz].
% Max freq = 12; % Maximum frequency to be simulated in [Hz].
% freq inc = 0.5; % Frequency increment in [Hz].
8
% Model Code = 3; % Code specifying which model to run (3 = Simple Model).
% Losses Code = 2; % Code specifying which losses subfunction to run
% part traj on off = 0; % No particle trajectory calculation
8
% ENGINE DATA = HTG ENGINE DATA; % Structure defining engine geometry and
operating conditions.
% ENGINE DATA.Pbore = 0.085;
% ENGINE DATA.V buffer max = 0.0032;
% ENGINE DATA.Vclp = 1.733e-04;
% ENGINE DATA.GSH config = 1;
% % Vary Frequency with 85 mm Piston:
8
                                   FREQ DATA
HTG_2nd_Order_Vary('freq',Min freq,Max freq,freq inc,ENGINE DATA);
% % Find mean pressure at maximum power
% [Max Power,max power index] = max([FREQ DATA.W dot]);
% freq at Max Power = Min freq + (max power index-1)*freq inc;
00
% % Find mean pressure at maximum efficiency
% [Max Efficiency,max efficiency index] = max([FREQ DATA.eff thermal]);
% freq at Max Efficiency = Min freq + (max efficiency index-1)*freq inc;
8
% % Find mean pressure at stall
% [Min Power, free run index] = min(abs([FREQ DATA.W dot]));
% freq at Free Run = Min freq + (free run index-1)*freq inc;
2
% % Power and Efficiency vs. Frequency
% figure('Position', [x y 326 275])
% freq Range = Min freq:freq inc:Max freq;
8
% freq Power Range = [FREQ DATA.W dot];
```

```
% freq Efficiency Range = [FREQ DATA.eff thermal].*100;
8
% % Plot Power on the left axis
% yyaxis left
% plot(freq Range, freq Power Range, 'r', 'LineWidth', 2)
% ylim([0 inf])
% ylabel('Power Output (W)','FontName',font,'FontSize',font size)
% set(gca,'ycolor','r')
% % Plot efficiency on the right axis
% yyaxis right
% plot(freq Range, freq Efficiency Range, 'b', 'LineWidth', 2)
% ylim([0 inf])
% ylabel('Thermal Efficiency (%)','FontName',font,'FontSize',font size)
% set(gca,'ycolor','b')
% xlabel('Engine Frequency (Hz)', 'FontName', font, 'FontSize', font size)
% legend('Power','Efficiency','Location','South')
% set(gca,'fontsize',font size);
% set(gca, 'FontName', font)
%
% % Normalized Power Losses vs Frequency
% figure('Position', [x y 326 275])
% P HEX rel = [FREQ DATA.P HEX]./[FREQ_DATA.ref_cycle_power];
% P_mech_rel = [FREQ_DATA.P_mech]./[FREQ_DATA.ref cycle power];
% P
   _flow_h_rel = [FREQ_DATA.P_flow_h]./[FREQ_DATA.ref_cycle_power];
% P flow r rel = [FREQ DATA.P flow r]./[FREQ DATA.ref cycle power];
% P flow k rel = [FREQ DATA.P flow k]./[FREQ DATA.ref cycle power];
% % P GSH rel = [FREQ DATA.P GSH]./[FREQ DATA.ref cycle power];
% hold on
% plot(freq Range, P HEX rel.*100, 'LineWidth', 2)
% plot(freq_Range,P mech rel.*100,'LineWidth',2)
% plot(freq_Range,P_flow_h_rel.*100,'LineWidth',2)
% plot(freq_Range,P_flow_r_rel.*100,'LineWidth',2)
% plot(freq Range, P flow k rel.*100, 'LineWidth', 2)
% % plot(freq Range, P GSH rel.*100, 'LineWidth', 2)
% hold off
% xlabel('Engine Frequency (Hz)','FontName',font,'FontSize',font size)
% ylabel('Normalized Power Losses (%)','FontName',font,'FontSize',font size)
   legend('Imperfect Heat Transfer','Mechanical Friction','Heater
8
                                                                            Flow
Friction', 'Regenerator Flow Friction',...
      'Cooler Flow Friction', 'Gas Spring Hysteresis', 'Location', 'North')
8
% set(gca,'fontsize',font size);
% set(gca, 'FontName', font)
% ylim([0 100])
% xlim([0 12])
8
% % Flow Friction losses vs Frequency
% figure('Position', [x y 326 275])
% hold on
% plot(freq_Range,[FREQ_DATA.P_flow_h],'r','LineWidth',2)
% plot(freq Range, [FREQ DATA.P flow r], 'g', 'LineWidth', 2)
% plot(freq Range,[FREQ DATA.P flow k],'b','LineWidth',2)
% hold off
% xlabel('Engine Frequency (Hz)','FontName',font,'FontSize',font size)
% ylabel('Flow Friction Losses (W)', 'FontName', font, 'FontSize', font size)
% legend('Heater', 'Regenerator', 'Cooler', 'Location', 'NorthWest')
% set(gca,'fontsize',font size);
% set(gca, 'FontName', font)
```

```
0
% % Pressure Drops vs Frequency
% figure('Position', [x y 326 275])
% hold on
% plot([FREQ DATA(end).pdroph]./1000,'r','LineWidth',2)
% plot([FREQ_DATA(end).pdropr]./1000,'g','LineWidth',2)
% plot([FREQ DATA(end).pdropk]./1000, 'b', 'LineWidth',2)
% hold off
% xlabel('Crank Angle (\circ)', 'FontName', font, 'FontSize', font size)
% ylabel('Pressure Drop (kPa)','FontName',font,'FontSize',font_size)
% legend('Heater','Regenerator','Cooler','Location','NorthEast')
% set(gca,'fontsize',font size);
% set(gca, 'FontName', font)
%% Figure 3.X: Power and Efficiency vs. Mean Pressure Using 2nd Order Model
crank inc = 1; % Crank angle step size for model output [degrees].
% Mean Pressure Variation
Min pmean = 100000; % Minimum mean pressure to be simulated in [Pa].
Max pmean = 100000000; % Maximum mean pressure to be simulated in [Pa].
pmean inc = 1000000; % Mean pressure increment in [Pa].
Model Code = 3; % Code specifying which model to run (3 = Simple Model).
Losses Code = 2; % Code specifying which losses subfunction to run
part traj on off = 0; % No particle trajectory calculation
ENGINE DATA = HTG ENGINE DATA; % Structure defining engine geometry and
operating conditions.
ENGINE DATA.Pbore = 0.085;
ENGINE DATA.V buffer max = 0.0032;
ENGINE DATA.Vclp = 1.733e-04;
ENGINE DATA.GSH config = 1;
% Vary Frequency with 85 mm Piston:
PMEAN DATA
                                                                              =
HTG 2nd Order Vary('pmean', Min pmean, Max pmean, pmean inc, ENGINE DATA);
% Find mean pressure at maximum power
[Max Power,max power index] = max([PMEAN DATA.W dot]);
pmean at Max Power = Min pmean + (max power index-1)*pmean inc;
% Find mean pressure at maximum efficiency
[Max Efficiency,max efficiency index] = max([PMEAN DATA.eff thermal]);
pmean at Max Efficiency = Min pmean + (max efficiency index-1)*pmean inc;
% Find mean pressure at stall
[Min Power, free run index] = min(abs([PMEAN DATA.W dot]));
pmean at Free Run = Min pmean + (free run index-1)*pmean inc;
% Power and Efficiency vs. Mean Pressure
figure('Position', [x y 326 275])
pmean Range = Min pmean:pmean inc:Max pmean;
pmean Range kPa = pmean Range./1000;
pmean Power Range = [PMEAN DATA.W dot];
```

```
pmean Efficiency Range = [PMEAN DATA.eff thermal].*100;
% Plot Power on the left axis
yyaxis left
plot(pmean Range kPa,pmean Power Range,'r','LineWidth',2)
ylim([0 inf])
ylabel('Power Output (W)', 'FontName', font, 'FontSize', font size)
set(gca, 'ycolor', 'r')
% Plot efficiency on the right axis
yyaxis right
plot (pmean Range kPa, pmean Efficiency Range, 'b', 'LineWidth', 2)
ylim([0 inf])
ylabel('Thermal Efficiency (%)', 'FontName', font, 'FontSize', font size)
set(gca, 'ycolor', 'b')
xlabel('Mean Pressure (kPa)', 'FontName', font, 'FontSize', font size)
legend('Power','Efficiency','Location','South')
set(gca, 'fontsize', font size);
set(gca, 'FontName', font)
% Normalized Power Losses vs Mean Pressure
figure('Position', [x y 326 275])
P HEX rel = [PMEAN_DATA.P_HEX]./[PMEAN_DATA.ref_cycle_power];
P mech rel = [PMEAN DATA.P mech]./[PMEAN DATA.ref cycle power];
P_flow_h_rel = [PMEAN_DATA.P_flow_h]./[PMEAN_DATA.ref_cycle_power];
P flow r rel = [PMEAN DATA.P flow r]./[PMEAN DATA.ref cycle power];
P flow k rel = [PMEAN DATA.P flow k]./[PMEAN DATA.ref cycle power];
% P GSH rel = [PMEAN DATA.P GSH]./[PMEAN DATA.ref cycle power];
hold on
plot(pmean Range kPa, P HEX rel.*100, 'LineWidth', 2)
plot(pmean Range kPa, P mech rel.*100, 'LineWidth', 2)
plot(pmean_Range_kPa,P_flow_h_rel.*100,'LineWidth',2)
plot(pmean_Range_kPa,P_flow_r_rel.*100,'LineWidth',2)
plot(pmean Range kPa,P_flow_k_rel.*100,'LineWidth',2)
% plot(pmean Range kPa,P GSH rel.*100,'LineWidth',2)
hold off
xlabel('Mean Pressure (kPa)', 'FontName', font, 'FontSize', font size)
ylabel('Normalized Power Losses (%)', 'FontName', font, 'FontSize', font size)
                   Heat Transfer', 'Mechanical Friction', 'Heater Flow
legend('Imperfect
Friction', 'Regenerator Flow Friction',...
    'Cooler Flow Friction','Gas Spring Hysteresis','Location','North')
set(gca, 'fontsize', font size);
set(gca, 'FontName', font)
ylim([0 100])
%% Figure 3.X: Power and Efficiency vs. Thermal Source Temperature Using 2nd
Order Model
% % Thermal Source Temperature Variation
% Min TH = 273 + 50; % Minimum thermal source temperature to be simulated in
[K].
% Max TH = 273 + 1000; % Maximum thermal source temperature to be simulated
in [K].
% TH inc = 50; % Thermal source temperature increment in [K].
% % Plot 1 - Power and Efficiency vs. Hot Source Temperature, As-Built
% ENGINE DATA = HTG ENGINE DATA;
% ENGINE DATA.Pbore = 0.085;
```

```
% ENGINE DATA.V buffer max = 0.0032;
% ENGINE DATA.Vclp = 1.733e-04;
% ENGINE DATA.GSH config = 1;
8
% counter = 1;
% for TH = Min TH:TH inc:Max TH
00
      ENGINE DATA.Tsource = TH;
      ENGINE DATA.Tge = TH;
8
8
      ENGINE DATA.Tgh = TH;
8
      ENGINE DATA.Twh = TH;
00
8
      [SECOND ORDER DATA, REF CYCLE DATA, LOSSES DATA] ...
8
          = HTG 2nd Order (ENGINE DATA);
00
8
      SOL(counter).second order power = SECOND ORDER DATA.W dot;
%
      SOL(counter).second order efficiency = SECOND ORDER DATA.eff thermal;
                                          SOL(counter).ref cycle power
8
[REF CYCLE DATA(end).W].*[ENGINE DATA.freq];
                                                   REF CYCLE DATA(1).W dot ref-
8
                       SOL(counter).P HEX
(REF CYCLE DATA(end).W*ENGINE DATA.freq);
00
      SOL(counter).P mech = LOSSES DATA.P mech;
      SOL(counter).P flow h = LOSSES DATA.P flow h;
8
      SOL(counter).P_flow_r = LOSSES_DATA.P flow r;
8
8
      SOL(counter).P_flow_k = LOSSES_DATA.P_flow_k;
      SOL(counter).P GSH = LOSSES DATA.P GSH;
8
8
      counter = counter + 1;
% end
2
% figure('Position', [x y 326 275])
00
% TH Range = Min TH:TH inc:Max TH;
% TH Range Celcius = TH Range - 273.15;
8
% % Plot Power on the left axis
% yyaxis left
% plot(TH Range Celcius,[SOL.second order power],'r','LineWidth',2)
% ylim([0 inf])
% ylabel('Power Output (W)','FontName',font,'FontSize',font size)
% set(gca,'ycolor','r')
% % Plot efficiency on the right axis
% yyaxis right
% plot(TH Range Celcius,[SOL.second order efficiency]*100,'b','LineWidth',2)
% ylim([0 inf])
% ylabel('Thermal Efficiency (%)','FontName',font,'FontSize',font size)
% set(gca,'ycolor','b')
8
8
                 xlabel('Heater
                                                Wall
                                                                     Temperature
(\circC)', 'FontName', font, 'FontSize', font size)
% legend('Power','Efficiency','Location','SouthEast')
% set(gca,'fontsize',font size);
% set(gca, 'FontName', font)
8
% % Plot 2 - Relative Power Losses As-Built
% P HEX rel = [SOL.P HEX]./[SOL.ref cycle power];
% P mech rel = [SOL.P mech]./[SOL.ref cycle power];
% P flow h rel = [SOL.P flow h]./[SOL.ref cycle power];
% P flow r rel = [SOL.P flow r]./[SOL.ref cycle power];
```

```
% P flow k rel = [SOL.P flow k]./[SOL.ref cycle power];
% % P GSH rel = [SOL.P GSH]./[SOL.ref cycle power];
0
% figure('Position', [x y 326 275])
% hold on
% plot(TH Range Celcius, P HEX rel.*100, 'LineWidth', 2)
% plot(TH Range Celcius, P mech rel.*100, 'LineWidth',2)
% plot(TH Range Celcius, P flow h rel.*100, 'LineWidth', 2)
% plot(TH Range Celcius, P flow r rel.*100, 'LineWidth', 2)
% plot(TH_Range_Celcius,P_flow_k_rel.*100,'LineWidth',2)
% % plot(TH Range Celcius, P GSH rel.*100, 'LineWidth', 2)
% ylim([0 100])
% xlim([200 1000])
% hold off
0
                 xlabel('Heater
                                                Wall
                                                                     Temperature
(\circC)', 'FontName', font, 'FontSize', font size)
% ylabel({'Relative Power Losses (%)'},'FontName',font,'FontSize',font size)
% legend('Imperfect Heat Transfer','Mechanical Friction','Heater
                                                                          Flow
Friction', 'Regenerator Flow Friction',...
      'Cooler Flow Friction', 'Gas Spring Hysteresis', 'Location', 'NorthEast')
% set(gca,'fontsize',font size);
% set(gca, 'FontName', font)
```

Chapter_4_Model_Plots.m

% Chapter 4 Plots.m - Written by Connor Speer - October 2017 clear,clc,close all; %% Input Parameters % crank inc = 1; % Crank angle step size for model output [degrees]. % Engine Hot Source Temperature Variation Min TH = 373.15; % Minimum hot source temperature to be simulated in [K]. Max TH = 773.15; % Maximum hot source temperature to be simulated in [K]. TH Increment = 100; % Hot source temperature increment in [K]. %% Plot Aesthetics set(0, 'defaultfigurecolor', [1 1 1]) % Location of Figures x = 500;y = 500;% Size of Figures width = 550;height = 400;% Font For Figures font = 'Arial';

```
font size = 11;
% % Location of Figures
% x = 500;
% y = 500;
2
% % Size of Figures
% width = 326;
% height = 275;
2
% % Font For Figures
% font = 'Times New Roman';
% font size = 10;
% % Location of Figures
% x = 500;
% y = 500;
2
% % Size of Figures
% width = 550;
% height = 400;
8
% % Font For Figures
% font = 'Times New Roman';
% font size = 16;
% To change line width for plots, say "'LineWidth',2".
% To include math symbols with their own font size and font type in the
% axes labels, do this:
% xlabel({'\fontsize{11} Engine Speed \fontsize{11} \fontname{Cambria Math}
\omega \fontsize{11} \fontname{Times New Roman} [RPM]'});
% Here is the degree symbol in case you need it °C. Alternatively, use
% \circ.
%% Plot 1 - Power and Efficiency vs. Hot Source Temperature, As-Built
ENGINE DATA = HTG ENGINE DATA;
ENGINE DATA.Pbore = 0.085;
ENGINE DATA.V buffer max = 0.0032;
ENGINE DATA.Vclp = 1.733e-04;
ENGINE DATA.GSH config = 1;
counter = 1;
for TH = Min TH:TH Increment:Max TH
  ENGINE DATA.Tsource = TH;
  ENGINE DATA.Tge = TH;
  ENGINE DATA.Tgh = TH;
  ENGINE DATA.Twh = TH;
```

```
[SECOND ORDER DATA, REF CYCLE DATA, LOSSES DATA] ...
        = HTG 2nd Order (ENGINE DATA);
    SOL(counter).second order power = SECOND ORDER DATA.W dot;
    SOL(counter).second order efficiency = SECOND ORDER DATA.eff thermal;
    SOL(counter).ref cycle power
[REF CYCLE DATA(end).W].*[ENGINE DATA.freq];
    SOL(counter).P HEX
                                                   REF CYCLE DATA(1).W dot ref-
                                    =
(REF CYCLE DATA(end).W*ENGINE DATA.freq);
    SOL(counter).P_mech = LOSSES_DATA.P_mech;
    SOL(counter).P flow h = LOSSES DATA.P flow h;
    SOL(counter).P flow r = LOSSES DATA.P flow r;
    SOL(counter).P flow k = LOSSES DATA.P flow k;
    SOL(counter).P GSH = LOSSES DATA.P GSH;
    counter = counter + 1;
end
figure('Position', [x y width height])
TH Range = Min TH:TH Increment:Max TH;
TH Range Celcius = TH Range - 273.15;
% Plot Power on the left axis
yyaxis left
plot(TH Range Celcius, [SOL.second order power], 'LineWidth', 2)
ylim([0 inf])
ylabel('Power Output, (W)', 'FontName', font, 'FontSize', font size)
% Plot efficiency on the right axis
yyaxis right
plot(TH Range Celcius, [SOL.second order efficiency] *100, 'LineWidth', 2)
ylim([0 inf])
ylabel('Thermal Efficiency, (%)', 'FontName', font, 'FontSize', font size)
xlabel('Thermal
                                      Source
                                                                    Temperature,
(^\circC)', 'FontName', font, 'FontSize', font size)
legend('Power','Efficiency','Location','NorthWest')
set(gca, 'fontsize', font size);
set(gca, 'FontName', font)
%% Plot 2 - Relative Power Losses As-Built
P mech rel = [SOL.P mech]./[SOL.ref cycle power];
P flow h rel = [SOL.P flow h]./[SOL.ref cycle power];
P_flow_r_rel = [SOL.P_flow_r]./[SOL.ref_cycle_power];
P flow k rel = [SOL.P flow k]./[SOL.ref cycle power];
P GSH rel = [SOL.P GSH]./[SOL.ref cycle power];
P HEX rel = [SOL.P HEX]./[SOL.ref cycle power];
figure('Position', [x y width height])
hold on
plot(TH Range Celcius, P mech rel.*100, 'LineWidth', 2, 'Color', 'm')
plot(TH Range Celcius,P flow h rel.*100, 'LineWidth',2, 'Color', 'r')
plot(TH Range Celcius,P flow r rel.*100, 'LineWidth',2, 'Color', 'g')
plot(TH Range Celcius, P flow k rel.*100, 'LineWidth', 2, 'Color', 'b')
plot(TH Range Celcius,P GSH rel.*100, 'LineWidth',2, 'Color', 'k')
```

```
plot(TH Range Celcius, P HEX rel.*100, 'LineWidth', 2, 'Color', 'c')
% xlim([100 500])
% ylim([0 350])
hold off
xlabel('Thermal
                                                                   Temperature,
                                      Source
(^\circC)', 'FontName', font, 'FontSize', font size)
ylabel({'Relative Power
                                 Losses';'(%
                                                           Reference
                                                                          Cycle
                                                  of
Power)'},'FontName',font,'FontSize',font size)
legend('Mechanical Friction','Heater
                                         Flow
                                                Friction', 'Regenerator
                                                                           Flow
Friction'...
    ,'Cooler Flow Friction','Crankcase Gas Spring Hysteresis','Imperfect Heat
Transfer', 'Position', [0.1 50 550 400])
set(gca, 'fontsize', font size);
set(gca, 'FontName', font)
%% Plot 3 - Power and Efficiency vs. Hot Source Temperature, All Mods
ENGINE DATA = HTG ENGINE DATA;
ENGINE DATA.Pbore = 0.044;
ENGINE DATA.V buffer max = 0.0032 + 0.004633333;
ENGINE DATA.Vclp = 1.733e-04 - 0.000132;
ENGINE DATA.GSH config = 4;
counter = 1;
for TH = Min TH:TH Increment:Max TH
    ENGINE DATA.Tsource = TH;
    ENGINE DATA.Tge = TH;
    ENGINE DATA.Tgh = TH;
    ENGINE DATA.Twh = TH;
    [SECOND ORDER DATA, REF CYCLE DATA, LOSSES DATA] ...
        = HTG 2nd Order (ENGINE DATA);
    SOL(counter).second order power = SECOND ORDER DATA.W dot;
    SOL(counter).second order efficiency = SECOND ORDER DATA.eff thermal;
    SOL(counter).ref cycle power
[REF CYCLE DATA(end).W].*[ENGINE DATA.freq];
    SOL(counter).P HEX
                                   =
                                                   REF CYCLE DATA(1).W dot ref-
(REF CYCLE DATA(end).W*ENGINE DATA.freq);
    SOL(counter).P mech = LOSSES DATA.P mech;
    SOL(counter).P flow h = LOSSES DATA.P flow h;
    SOL(counter).P flow r = LOSSES DATA.P flow r;
    SOL(counter).P_flow_k = LOSSES_DATA.P_flow_k;
    SOL(counter).P GSH = LOSSES DATA.P GSH;
    counter = counter + 1;
end
figure('Position', [x y width height])
TH Range = Min TH:TH Increment:Max TH;
TH Range Celcius = TH Range - 273.15;
% Plot Power on the left axis
yyaxis left
plot(TH Range Celcius, [SOL.second order power], 'LineWidth', 2)
```

```
ylim([0 inf])
ylabel('Power Output, (W)', 'FontName', font, 'FontSize', font size)
% Plot efficiency on the right axis
yyaxis right
plot(TH Range Celcius, [SOL.second order efficiency] *100, 'LineWidth', 2)
ylim([0 inf])
ylabel('Thermal Efficiency, (%)', 'FontName', font, 'FontSize', font size)
xlabel('Thermal
                                      Source
                                                                    Temperature,
(^\circC)', 'FontName', font, 'FontSize', font size)
legend('Power', 'Efficiency', 'Location', 'NorthWest')
set(gca, 'fontsize', font size);
set(gca, 'FontName', font)
%% Plot 2 - Relative Power Losses All Mods
P mech rel = [SOL.P mech]./[SOL.ref cycle power];
P flow h rel = [SOL.P flow h]./[SOL.ref cycle power];
P_flow_r_rel = [SOL.P_flow_r]./[SOL.ref_cycle_power];
P flow k rel = [SOL.P flow k]./[SOL.ref cycle power];
P GSH rel = [SOL.P GSH]./[SOL.ref cycle power];
P HEX rel = [SOL.P HEX]./[SOL.ref cycle power];
figure('Position', [x y width height])
hold on
plot(TH Range Celcius, P mech rel.*100, 'LineWidth', 2, 'Color', 'm')
plot(TH Range Celcius,P flow h rel.*100, 'LineWidth',2, 'Color', 'r')
plot(TH Range Celcius, P flow r rel.*100, 'LineWidth', 2, 'Color', 'g')
plot(TH Range Celcius, P flow k rel.*100, 'LineWidth', 2, 'Color', 'b')
plot(TH Range Celcius,P GSH rel.*100, 'LineWidth',2, 'Color', 'k')
plot(TH Range Celcius, P HEX rel.*100, 'LineWidth', 2, 'Color', 'c')
% xlim([100 500])
% ylim([0 350])
hold off
xlabel('Thermal
                                                                    Temperature,
                                      Source
(^\circC)', 'FontName', font, 'FontSize', font size)
                                 Losses';'(%
ylabel({'Relative Power
                                                  of
                                                            Reference
                                                                           Cycle
Power)'},'FontName',font,'FontSize',font size)
legend('Mechanical Friction','Heater Flow Friction', 'Regenerator
                                                                            Flow
Friction'...
    ,'Cooler Flow Friction','Crankcase Gas Spring Hysteresis','Imperfect Heat
Transfer', 'Position', [0.1 50 550 400])
set(gca, 'fontsize', font_size);
set(gca, 'FontName', font)
%% Optimum Piston Size for 95/5 Temperature Difference
% Input Parameters
Tgh = 273 + 95; %(K)
Tgk = 273 + 5; %(K)
Vmin = (874.35 + 542.87) *1e-6; %(m^3)
Vswd = 542.87*1e-6; %(m^3)
Sp = 0.075; \%(m)
% Kolin's Formula
Vswp Kolin = (Vmin*(Tgh-Tgk))/1100; %(m^3)
Pbore Kolin = sqrt((4/pi)*Vswp Kolin); %(m)
```

```
% Connor's Equal Pressure Swings Method
Tgr = (Tgh-Tgk) / log (Tgh/Tgk);
% Mean temperature (displacer at mid-stroke)
Tmean = (Vmin) / (((0.5*Vswd) / Tgh) + ((Vh) / Tgh) + ...
     ((Vr)/Tqr) + ((Vk)/Tqk) + ((0.5*Vswd)/Tqk));
Tfactor = (Tgh-Tgk)/Tmean; % Temperature difference factor [dimensionless].
C1 = 0.25; % Polynomial coefficient 1.
C2 = Vmin; % Polynomial coefficient 2.
C3 = (Vmin^2) - (Tfactor*Vswd*Vmin); % Polynomial coefficient 3.
C4 = -Tfactor*Vswd*(Vmin^2); % Polynomial coefficient 4.
p = [C1 \ C2 \ C3 \ C4];
                    % Find roots of the polynomial.
r = roots(p);
Sort roots = sort(r); % Order roots from smallest to largest.
Vswp = Sort roots(3); % Choose the largest root to be the piston swept vol.
Pbore Connor = sqrt((4*Vswp)/(pi*Sp)); % Piston diameter in [mm].
% Second Order Model Optimization
ENGINE DATA = HTG ENGINE DATA;
ENGINE DATA.freq = 2;
ENGINE_DATA.V_buffer_max = 0.0032 + 0.004633333;
ENGINE DATA.Vclp = 1.733e-04 - 0.000132;
ENGINE DATA.GSH config = 4;
ENGINE DATA.Tsource = 273 + 95;
ENGINE DATA.Tge = 273 + 95;
ENGINE DATA.Tgh = 273 + 95;
ENGINE DATA.Twh = 273 + 95;
ENGINE DATA.Tsink = 273 + 5;
ENGINE DATA.Tqc = 273 + 5;
ENGINE DATA.Tqk = 273 + 5;
ENGINE DATA.Twk = 273 + 5;
counter = 1;
Pbore = 0.01:0.001:0.09;
for Dp = Pbore
    ENGINE DATA.Pbore = Dp;
    [SECOND ORDER DATA, REF CYCLE DATA, LOSSES DATA] ...
        = HTG 2nd Order (ENGINE DATA);
    SOL(counter).Power 2nd order = SECOND ORDER DATA.W dot;
    SOL(counter).Efficiency 2nd order = SECOND ORDER DATA.eff thermal;
    SOL(counter).ref cycle power
[REF CYCLE DATA(end).W].*[ENGINE DATA.freq];
```

```
SOL(counter).REF CYCLE DATA = REF CYCLE DATA;
    SOL(counter).P HEX
                                    =
                                                   REF CYCLE DATA(1).W dot ref-
(REF CYCLE DATA(end).W*ENGINE DATA.freq);
    SOL(counter).P mech = LOSSES DATA.P mech;
    SOL(counter).P flow h = LOSSES DATA.P flow h;
    SOL(counter).P flow r = LOSSES DATA.P flow r;
    SOL(counter).P flow k = LOSSES DATA.P flow k;
    SOL(counter).P GSH = LOSSES DATA.P GSH;
    counter = counter + 1;
end
figure('Position', [x y width height])
% Plot Power on the left axis
yyaxis left
plot(Pbore,[SOL.Power 2nd order],'LineWidth',2)
ylabel('Power Output, (W)', 'FontName', font, 'FontSize', font size)
% Plot efficiency on the right axis
yyaxis right
plot(Pbore,[SOL.Efficiency 2nd order]*100,'LineWidth',2)
ylabel('Thermal Efficiency, (%)', 'FontName', font, 'FontSize', font size)
                            (m)', 'FontName', font, 'FontSize', font size)
xlabel('Piston Diameter,
legend('Power', 'Efficiency', 'Location', 'NorthWest')
set(gca,'fontsize',font size);
set(gca, 'FontName', font)
[Max power, Max power index] = max([SOL.Power 2nd order]);
Pbore 2nd order power = Pbore (Max power index);
[Max efficiency, Max efficiency index] = max([SOL.Efficiency 2nd order]);
Pbore 2nd order eff = Pbore(Max efficiency index);
figure('Position', [x y width height])
hold on
plot(Pbore,[SOL.ref cycle power])
plot(Pbore, [SOL.P HEX])
plot(Pbore,[SOL.P_mech])
plot(Pbore, [SOL.P flow h])
plot(Pbore, [SOL.P flow r])
plot(Pbore,[SOL.P flow k])
plot(Pbore,[SOL.P GSH])
hold off
xlabel('Piston Diameter,
                             (m) ', 'FontName', font, 'FontSize', font size)
ylabel('Power Losses', 'FontName', font, 'FontSize', font size)
legend('Reference Cycle
                             Power','Imperfect Heat
                                                         Transfer', 'Mechanical
Friction', 'Heater Flow Friction', 'Regenerator Flow Friction'...
    , 'Cooler Flow Friction', 'Crankcase Gas Spring Hysteresis', 'Position', [0.1
50 550 400])
set(gca,'fontsize',font size);
set(gca, 'FontName', font)
```

HTG_2nd_Order.m

function [SECOND ORDER DATA, REF CYCLE DATA, LOSSES DATA] HTG 2nd Order (ENGINE DATA) % Written by Connor Speer, October 2017. % This function contains a scheme for adding decoupled losses to the % reference cycle results. %% Input: % ENGINE DATA --> Engine geometry and operating point. %% Preamble % A heat engine communicates with its environment in three ways: Heat % transfer between the thermal source and sink, and work transfer through % the output shaft. Decoupled losses can affect any of these three energy % transfer mechanisms. %% Call SEA code to calculate reference cycle and decoupled losses crank inc = 1; % Crank angle step size for numerical integration in [deg] Model Code = 3; % Code specifying which model to run (3 = Simple Model). Losses Code = 8; % Code specifying which losses subfunction to run part traj on off = 0; % 0 = no particle trajectory calculation. [REF CYCLE DATA, LOSSES_DATA, ... PARTICLE TRAJECTORY DATA] = sea(ENGINE DATA, crank inc, Model Code,... Losses Code, part traj on off); %% Heat Transfer Between the Engine and the Thermal Source SECOND ORDER DATA.Qh dot = REF CYCLE DATA(end).Qh*ENGINE DATA.freq + ... % Reference cycle heat input rate (-LOSSES_DATA.P_flow_h) + ... % Flow friction in the heater (-0.5*LOSSES DATA.P flow r) + ... % Half of flow friction in the regenerator LOSSES DATA.Q cond + ... % Conduction loss LOSSES DATA.Q seals + ... % Seal leakage LOSSES DATA.Q app + ... % Appendix gap loss LOSSES DATA.Q insulation + ... % Heat lost through the insulation LOSSES DATA.Q qrloss; % Regenerator enthalpy loss %% Work Transfer Between the Engine and the Load SECOND ORDER DATA.W dot = REF CYCLE DATA(end).W*ENGINE_DATA.freq - ... % Reference cycle power output LOSSES DATA.P mech - ... % Mechanical friction LOSSES DATA.P flow h - ... % Flow friction in the heater LOSSES DATA.P flow r - ... % Flow friction in the regenerator LOSSES DATA.P flow k - ... % Flow friction in the cooler LOSSES DATA.P GSH - ... % Gas spring hysteresis LOSSES DATA.P seals - ... % Seal leakage LOSSES_DATA.P_HTH - ... % Heat transfer hysteresis LOSSES DATA.P FPS - ... % Finite piston speed LOSSES DATA.P pump cool - ... % Coolant pump LOSSES DATA.P pump hot; % Heating system pump

%% Heat Transfer Between the Engine and the Thermal Sink

```
SECOND ORDER DATA.Qk dot = -REF CYCLE DATA(end).Qk*ENGINE DATA.freq + ... %
Reference cycle heat rejection rate
   LOSSES DATA.P mech + ... % Mechanical friction
   0.5*LOSSES DATA.P flow r + ... % Half of flow friction in the regenerator
   LOSSES DATA.P flow k + ... % Flow friction in the cooler
   LOSSES DATA.Q cond + ... % Conduction loss
   LOSSES DATA.Q seals + ... % Seal leakage
   LOSSES DATA.Q app + ... % Appendix gap loss
   LOSSES DATA.Q qrloss; % Regenerator enthalpy loss
%% Thermal Efficiency
SECOND ORDER DATA.eff thermal
                                                                      =
SECOND ORDER DATA.W dot/SECOND ORDER DATA.Qh dot;
%% Overall Energy Balance
SECOND ORDER DATA.Energy Imbalance = SECOND ORDER DATA.Qh dot - ...
   SECOND ORDER DATA.W_dot - SECOND_ORDER_DATA.Qk_dot;
%% Display Results
fprintf('======= 2nd Order Model Results ========\n')
fprintf(' Heat input rate: %.2f[W]\n', SECOND_ORDER_DATA.Qh_dot);
fprintf(' Heat rejection rate: %.2f[W]\n', SECOND ORDER DATA.Qk dot);
fprintf(' Power output: %.2f[W]\n', SECOND ORDER DATA.W dot);
fprintf('
           Thermal
                                   efficiency:
                                                           %.1f[%%]\n',
SECOND ORDER DATA.eff thermal*100);
fprintf(' Energy Imbalance: %.1f[W]\n', SECOND_ORDER_DATA.Energy_Imbalance);
% fprintf(' Exergy destruction at thermal source: %.lf[W]\n',
LOSSES DATA.X dest_source);
% fprintf(' Exergy destruction at thermal sink: %.lf[W]\n',
LOSSES DATA.X dest sink);
fprintf('=======Summary of Losses ========\n')
fprintf(' Mechanical friction: %.2f[W]\n', LOSSES DATA.P mech);
fprintf(' Flow friction in the heater: %.2f[W]\n', LOSSES DATA.P flow h);
fprintf(' Flow
                   friction in the
                                            regenerator: %.2f[W]\n',
LOSSES_DATA.P_flow r);
fprintf(' Flow friction in the cooler: %.2f[W]\n', LOSSES DATA.P flow k);
fprintf(' Gas spring hysteresis: %.2f[W]\n', LOSSES DATA.P GSH);
fprintf(' Seal leakage: %.1f[W]\n', LOSSES DATA.P seals);
fprintf(' Heat transfer hysteresis: %.lf[W]\n', LOSSES DATA.P HTH);
fprintf(' Finite piston speed: %.lf[W]\n', LOSSES DATA.P FPS);
fprintf(' Coolant pump: %.lf[W]\n', LOSSES DATA.P pump cool);
fprintf(' Heating system pump: %.1f[W]\n', LOSSES DATA.P pump hot);
fprintf(' Regenerator enthalpy loss: %.1f[W]\n', LOSSES DATA.Q qrloss);
fprintf(' Conduction loss: %.1f[W]\n', LOSSES_DATA.Q_cond);
fprintf(' Appendix gap loss: %.1f[W]\n', LOSSES DATA.Q app);
fprintf(' Heat lost through
                                            insulation:
                                                           %.1f[W]\n',
LOSSES DATA.Q insulation);
fprintf('========\n')
```

HTG_2nd_Order_Vary.m

```
function
                                    DATA STRUCTURE
                                                                              =
HTG 2nd Order Vary (varName, Min, Max, Increment, ENGINE DATA)
% Written by Connor Speer - April 2017
% Editted by Shahzeb Mirza - October 2017
% The purpose of this script is to run the SEA code repeatedly for a
% variety of any given variable, and return results.
% Inputs:
% varName --> String with the exact variable name
% Min --> Lower bound of the variable range being considered [any unit]
% Max --> Upper bound of the variable range being considered [any unit]
% Increment --> Increment size for variable range [any unit
% ENGINE DATA --> Structure which defines engine geometry and operating
conditions
% Crank Angle Increment --> Crank angle step size for numerical integration
in [degrees]
% Model Code --> Code specifying which model to run.
% 1 = Ideal Isothermal Model
% 2 = Ideal Adiabatic Model
% 3 = Simple Model
% Losses Code --> Code specifying which losses subfunction to run
% 1 = parasitic losses GEN.m
% 2 = parasitic losses HTG.m
range = Min:Increment:Max;
% Preallocate space
DATA STRUCTURE(length(range)).Qh dot = [];
DATA STRUCTURE(length(range)).Qk_dot = [];
DATA STRUCTURE(length(range)).W dot = [];
DATA STRUCTURE(length(range)).eff thermal = [];
counter = 1; % Initialize counter variable
counter max = length(range);
h = waitbar(0, 'Running 2nd order model...');
for i = range
    command = strcat('ENGINE DATA.', varName, ' = i;');
    eval(command);
    % Call the second order model subfunction
    [SECOND ORDER DATA, REF CYCLE DATA, LOSSES DATA]
                                                                              =
HTG 2nd Order (ENGINE DATA);
    % Store outputs from the model
    DATA STRUCTURE (counter).Qh dot = SECOND ORDER DATA.Qh dot;
    DATA STRUCTURE (counter).Qk dot = SECOND ORDER DATA.Qk dot;
```

```
DATA STRUCTURE (counter) .W dot = SECOND ORDER DATA.W dot;
    DATA STRUCTURE (counter).eff thermal = SECOND ORDER DATA.eff thermal;
    DATA STRUCTURE (counter).ref cycle power = REF CYCLE DATA(1).W dot ref;
    DATA STRUCTURE (counter) .ref cycle heat in
REF CYCLE DATA(end).Qh*ENGINE DATA.freq;
    DATA STRUCTURE (counter) .ref cycle heat out
REF CYCLE DATA(end).Qk*ENGINE DATA.freq;
    DATA STRUCTURE (counter) .FW = LOSSES DATA.FW;
    DATA STRUCTURE (counter) . P HEX
                                      =
                                                  REF CYCLE DATA(1).W dot ref-
(REF CYCLE DATA(end).W*ENGINE DATA.freq);
    DATA STRUCTURE (counter).P mech = LOSSES_DATA.P_mech;
    DATA STRUCTURE (counter).pdroph = LOSSES DATA.pdroph;
    DATA STRUCTURE (counter).pdropr = LOSSES DATA.pdropr;
    DATA STRUCTURE (counter).pdropk = LOSSES DATA.pdropk;
    DATA_STRUCTURE(counter).P_flow_h = LOSSES_DATA.P_flow_h;
    DATA_STRUCTURE(counter).P_flow_r = LOSSES_DATA.P_flow_r;
    DATA STRUCTURE(counter).P flow k = LOSSES DATA.P flow k;
    DATA STRUCTURE (counter).P GSH = LOSSES DATA.P GSH;
    DATA STRUCTURE (counter).Q qrloss = LOSSES DATA.Q qrloss;
    DATA STRUCTURE (counter).Q cond = LOSSES DATA.Q cond;
    DATA STRUCTURE (counter).Q app = LOSSES DATA.Q app;
    DATA STRUCTURE(counter).P seals = LOSSES DATA.P seals;
    DATA_STRUCTURE(counter).Q_seals = LOSSES_DATA.Q_seals;
    DATA STRUCTURE (counter).P HTH = LOSSES DATA.P HTH;
    DATA STRUCTURE (counter). P FPS = LOSSES DATA. P FPS;
    DATA STRUCTURE(counter).P pump cool = LOSSES DATA.P pump cool;
    DATA_STRUCTURE(counter).P_pump_hot = LOSSES_DATA.P_pump_hot;
    DATA STRUCTURE(counter).X dest source = LOSSES DATA.X dest source;
    DATA_STRUCTURE(counter).X_dest_sink = LOSSES_DATA.X_dest_sink;
    DATA STRUCTURE(counter).Q insulation = LOSSES DATA.Q insulation;
    % Close the temporary data file to prevent Matlab errors
    fclose('all');
    counter = counter + 1;
    waitbar(counter/ counter max)
end
close(h)
HTG ENGINE DATA.m
function ENGINE DATA = HTG ENGINE DATA
% This function will define a structure that describes the geometric data,
% operating conditions, and working fluid properties for the HTG engine.
```

% Default values are for the fully modified version of the HTG engine.

%% Drive Mechanism:

```
% Engine Type
% s --> Alpha sinusoidal
% a --> Alpha slider crank
% y --> Alpha Ross yoke drive
% r --> Alpha Ross rocker-V drive
% q --> Gamma sinusoidal
% x --> Gamma slider crank
ENGINE DATA.engine type = 'x';
% Slider Crank Mechanism Dimensions
ENGINE DATA.Pbore = 0.044; %[m]
ENGINE DATA.Pr1 = 0; %[m]
ENGINE DATA.Pr2 = 0.0375; %[m]
ENGINE DATA.Pr3 = 0.156; %[m]
ENGINE DATA.Dbore = 0.096; %[m]
ENGINE DATA.Dr1 = 0; %[m]
ENGINE DATA.Dr2 = 0.0375; \& [m]
ENGINE DATA.Dr3 = 0.130; %[m]
%% Volumes: WHAT ABOUT THE APPENDIX GAP????!
% Power Piston Clearance Volume for Gamma Engines
% --> Includes the Cylinder Head and Connecting Pipe in this case.
% Dead volume reduction parts are subtracted
ENGINE DATA.Vclp = 1.733e-04 - 0.000132; %[m^3]
% Power Piston Swept Volume for Gammas
ENGINE DATA.Vswp = 4.256e-04; %[m^3]
% Total Displacer Clearance Volume (above and below) for Gammas
ENGINE DATA.Vcld = 1.448e-05; %[m^3]
% Displacer Swept Volume for Gammas
ENGINE DATA.Vswd = 5.429e-04; %[m^3]
% Displacer Phase Angle Advance for Gamma
ENGINE DATA.beta deg = 90.0; %[deg]
%% Cooler:
% Cooler Type
% p --> smooth pipes
% a --> smooth annulus
% s --> slots
ENGINE DATA.cooler type = 's';
% Cooler Slot Width for Slot Cooler
ENGINE DATA.cooler slot width = 1.00e-03; %[m]
% Cooler Slot Height for Slot Cooler
ENGINE DATA.cooler slot height = 1.00e-02; %[m]
% Cooler Heat Exchanger Length
ENGINE DATA.cooler length = 8.400e-02; %[m]
```

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```
% Cooler Number of Slots
ENGINE DATA.cooler num slots = 144; %[m]
%% Regenerator:
% Regenerator Configuration
% t --> tubular regenerator
% a --> annular regenerator
ENGINE DATA.regen config = 'a';
% Regen Housing O.D. for Annular Regenerator (May not be needed since
% conduction loss calc was redone)
ENGINE DATA.regen housing OD = 1.465e-01; %[m]
% Regen Housing I.D. for Annular Regenerator (May not be needed since
% conduction loss calc was redone)
ENGINE DATA.regen housing ID = 1.355e-01; %[m]
% Matrix I.D. for Annular Regenerator
ENGINE DATA.regen matrix ID = 1.030e-01;
% Regenerator Length
ENGINE DATA.regen length = 5.481e-02; %[m]
% Regenerator Number of Tubes
ENGINE DATA.regen num tubes = 1;
% Regenerator Matrix Type
% m --> mesh
% f --> foil
% n --> no matrix
ENGINE DATA.regen matrix type = 'm';
% Matrix Porosity for Mesh Matrix
ENGINE DATA.regen matrix porosity = 0.893;
% Matrix Wire Diameter for Mesh Matrix
ENGINE DATA.regen wire diameter = 5.08e-05; %[m]
%% Heater:
% Heater Type
% p --> smooth pipes
% a --> smooth annulus
% s --> slots
ENGINE DATA.heater type = 's';
% Pipe I.D. for Smooth Pipe Heater
% ENGINE DATA.heater pipe ID = ; %[m]
% Heater Slot Width for Slot Heater
ENGINE DATA.heater slot width = 3.180e-03; %[m]
% Heater Slot Height for Slot Heater
ENGINE DATA.heater slot height = 5.170e-03; %[m]
```

```
% Heater Heat Exchanger Length
ENGINE DATA.heater length = 1.233e-01; %[m]
% Heater Number of Slots for Slot Heater
ENGINE DATA.heater num slots = 64;
%% Operating Conditions:
% Working Fluid
% hy --> hydrogen
% he --> helium
% ai --> air
ENGINE DATA.gas type = 'ai';
% Mean Pressure
ENGINE DATA.pmean = 1000000.0; %[Pa] (= 10 bar)
% Cold Sink Temperature
ENGINE DATA.Tsink = 294.0; %[K]
% Cooler Gas Temperature
ENGINE DATA.Tgk = 294.0; %[K]
% Cooler Wall Temperature
ENGINE DATA.Twk = 294.0; %[K]
% Compression Space Temperature
ENGINE DATA.Tgc = 294.0; %[K]
% Hot Source Temperature
ENGINE DATA.Tsource = 273 + 200; %[K]
% Heater Gas Temperature
ENGINE DATA.Tgh = 273 + 200; %[K]
% Heater Wall Temperature
ENGINE DATA.Twh = 273 + 200; %[K]
% Expansion Space Temperature
ENGINE DATA.Tge = 273 + 200; %[K]
% Operating Frequency
ENGINE DATA.freq = 4.2; %[Hz]
%% Data for Engine Specific Loss Calculations:
% Maximum volume of the buffer space
% Volume of crankcase extension has been added
ENGINE DATA.V buffer max = 0.0032 + 0.004633333; %[m^3]
% Constant mechanism effectiveness
ENGINE DATA.effect = 0.7; % [unitless]
% Configuration code for GSH calculation
ENGINE DATA.GSH config = 4; % All mods
```

HTG_GSH.m

```
function P hys = HTG GSH(RPM, pmean, tk)
% Inputs:
% RPM --> engine speed in [rev/min]
% pmean --> engine mean pressure in [Pa]
% tk --> cooler temperature in [K]
omega = RPM*(1/60)*(2*pi); %[rad/s]
% Gas Spring Hysteresis Losses (Subtract from work output)
% Input parameters needed:
% omega --> angular frequency of the engine [rad/s]
% gama --> specific heat ratio of the spring gas
% Tw --> gas spring wall temperature [K]
% pmean --> mean pressure in the gas spring [Pa] (assumed to be the mean
% cycle pressure)
% kgas --> thermal conductivity of the spring gas [W/mK] (assumed to be the
% working fluid)
% delV --> volume amplitude of the spring cavity [m^3]
% VB --> mean volume of the gas spring cavity [m^3]
% Aw --> mean wetted area of the gas spring [m^2]
% delA --> wetted area amplitude [m^2]
% Inputs for Original ST05G-CNC Stirling Engine
Tw = tk; %[K] (assumed to be equal to the cooler temperature)
delV = 0.25*pi*(0.085^2)*0.075; %[m^3]
VB = 0.5 \pm delV + 0.002488647 + 0.000091248 + 0.000419874 + 0.000186558 + \dots
   0.000182367 - 0.000229935 - 0.000061378 - 0.000059277 - ...
   0.000007376 - 0.000021882 - 0.000013195 - 0.000009817 - ...
   0.000009173 - 0.000231607; %[m^3]
delA = pi*0.085*0.075; %[m^2]
Aw = 0.5*delA + 0.05853681 + 0.00804849 + 0.01866106 + 0.01030158 + ...
   0.02145481 + 0.03279471 + 0.01778246 + 0.02301812 + 0.00211262 + \ldots
   0.007294024 + 0.00026389 + 0.00045239 + 0.02173007; % [m^2]
% Calculation of the gas spring hysteresis loss
F1 = sqrt(0.125*omega*gama*(gama-1)*Tw*pmean*kgas);
F2 = (delV/VB)*((0.5*gama*(delV/VB)*Aw) - delA);
P hys = F1*F2*freq; % Power lost to gas spring hysteresis in [W].
```

HTG_GSH_Empirical.m

function P_hys = HTG_GSH_Empirical(Hz,pmean,Config_code)
% Written by Connor Speer - August 2017

% Calculates the gas spring hysteresis loss for the the high temperature

```
% gamma engine with the 85mm piston.
% Based on a surface fit that is a second degree polynomial in the x and y
% directions. 'poly22'.
% Inputs:
% Hz --> engine speed in [Hz]
% pmean --> engine mean pressure in [Pa]
% Config code --> code specifying the buffer space configuration
% 1 --> 85 mm piston, original crankcase volume
% 2 --> 85 mm piston, extended crankcase volume
% 3 --> 44 mm piston, original crankcase volume
% 4 --> 44 mm piston, extended crankcase volume
x = Hz;
y = pmean;
switch Config code
    case 1 % 85 mm piston, original crankcase volume
    p00 = -2.855;
    p10 = 4.902;
    p01 = -1.239e - 05;
    p20 = -0.4064;
    p11 = 2.327e - 05;
    p02 = 7.373e - 12;
    case 2 % 85 mm piston, extended crankcase volume
    p00 = 0;
    p10 = 0;
    p01 = 0;
    p20 = 0;
    p11 = 0;
    p02 = 0;
    case 3 % 44 mm piston, original crankcase volume
    p00 = 0.2473;
    p10 = -0.1534;
    p01 = 2.311e-07;
    p20 = 0.07564;
    p11 = 2.076e - 06;
    p02 = 1.975e - 13;
    case 4 % 44 mm piston, extended crankcase volume
    p00 = 0.1611;
    p10 = -0.2116;
    p01 = 2.969e - 07;
    p20 = 0.09854;
    p11 = 5.766e - 07;
    p02 = 1.987e - 13;
end
```

parasitic_losses_HTG.m

P hys = p00 + p10.*x + p01.*y + p20.*x.^2 + p11.*x.*y + p02.*y.^2; %[W]

function LOSSES DATA parasitic losses HTG (ENGINE DATA, REF CYCLE DATA, crank inc) % Written by Connor Speer - January 2017 % Calculates the parasitic losses. % Modified by Connor Speer, October 2017. No globals. % Losses already accounted for by the "Simple" simulation: % - Regenerator Enthalpy Loss % Inputs: % ENGINE DATA --> Structure containing engine geometry and operating point % REF CYCLE DATA --> Structure containing data from the reference cycle % crank inc --> crank angle step size in [degrees] % Output: % LOSSES DATA --> Structure containing parasitic loss information %% Mechanical Friction (Forced Work Method, See Senft's Book) vtot = ([REF CYCLE DATA.Vc] + ENGINE DATA.Vk + ENGINE DATA.Vr + ... ENGINE DATA.Vh + [REF CYCLE DATA.Ve]); % cubic meters p engine = [REF CYCLE DATA.p]; % Pascals Pbore = ENGINE DATA.Pbore; % piston bore [m] Pr1 = ENGINE DATA.Pr1; % piston desaxe offset in [m] Pr2 = ENGINE DATA.Pr2; % piston crank length (half stroke) in [m] Pr3 = ENGINE DATA.Pr3; % piston connecting rod lengths [m] theta = 0:crank inc*(pi/180):2*pi; Ptheta2 = pi - theta;Ptheta3 = pi - asin((-Pr1+(Pr2*sin(Ptheta2)))/Pr3); Pr4 = Pr2*cos(Ptheta2) - Pr3*cos(Ptheta3); $Pr4max = sqrt(((Pr2+Pr3)^2) - (Pr1^2));$ Pr4min = sqrt(((Pr3-Pr2)^2)-(Pr1^2)); Pstroke = Pr4max - Pr4min; % Crankcase Volume Variations in (m^3) V buffer = ENGINE DATA.V buffer max - ((Pr4max-Pr4)*(((pi/4)*(Pbore^2)))); p0 = mean([REF CYCLE DATA.p]); % Mean crankcase pressure in (Pa). % Mean crankcase volume in (m^3). V0 = ENGINE DATA.V buffer max - 0.5*Pstroke*(((pi/4)*(Pbore^2))); % % Constant Buffer Pressure Equal to the Mean Pressure % p buff const = mean([REF CYCLE DATA.p]); % Pascals % p buffer = repelem(p buff const, length(vtot)); % % Buffer Pressure Assuming Isothermal Compression and Expansion % T crankcase = ENGINE DATA.Tgc; % Mean crankcase temperature in [K]. % % Mass of gas in the crankcase in [kg].

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```
% m crankcase = (p0*V0)/(ENGINE DATA.rgas*T crankcase);
% p buffer = (m crankcase*R*T crankcase)./V buffer;
% Buffer Pressure Assuming Adiabatic Compression and Expansion in (Pa).
p buffer = p0.*((V0./V buffer).^ENGINE DATA.gamma);
[W ind, FW, W shaft] = \dots
   FW Subfunction v3(1,p engine,p buffer,vtot,ENGINE DATA.effect,0);
% Store forced work in LOSSES DATA structure
LOSSES DATA.FW = FW; %(J)
% Net output shaft power (W) (Senft's formula)
P shaft = W shaft*ENGINE DATA.freq;
% Power lost to mechanical friction in [W]
LOSSES DATA.P mech = (W ind*ENGINE DATA.freq) - P shaft;
%% Flow Friction
% Calculate pressure drops
[dwork h,dwork r,dwork k,pdropk,pdroph,pdropr] = ...
   worksim(ENGINE DATA, REF CYCLE DATA, crank inc);
LOSSES DATA.pdropk = pdropk; % Pressure drop across the cooler in (Pa)
LOSSES DATA.pdroph = pdroph; % Pressure drop across the heater in (Pa)
LOSSES DATA.pdropr = pdropr; % Pressure drop across the regenerator in (Pa)
% Pressure drop power loss in the heater
LOSSES_DATA.P_flow_h = dwork h*ENGINE DATA.freq; %(W)
% Pressure drop power loss in the regenerator
LOSSES DATA.P flow r = dwork r*ENGINE DATA.freq; %(W)
% Pressure drop power loss in the cooler
LOSSES DATA.P flow k = dwork k*ENGINE DATA.freq; %(W)
%% Regenerator Enthalpy Loss
A = isfield(REF CYCLE DATA, 'qrloss');
if A == 1
   % Convert regenerator enthalpy loss per cycle in (J) to a rate in (W)
   LOSSES DATA.Q qrloss = REF CYCLE DATA(1).qrloss*ENGINE DATA.freq; %(W)
else
   LOSSES DATA.Q qrloss = 0;
end
%% Conduction Loss (1-D Fourier Law)
% Input parameters needed:
% A wall --> Average cross-sectional area of the wall conduction path [m^2]
% k wall --> Average thermal conductivity of the wall conduction material
% [W/mK]
```

```
% L wall --> Length of the wall conduction path [m]
% A regen --> Regenerator free flow area [m^2]
% kgas --> Thermal conductivity of the working gas [W/mK]
\ L regen --> Length of the regenerator [m]
% A displacer --> Cross-sectional area of the displacer [m^2]
% k displacer --> Effective thermal conductivity of the displacer [W/m^2]
% L displacer --> Length of the displacer [m]
% % Inputs for Original ST05G-CNC Stirling Engine
% A wall = 0.25*pi*((0.1397^2)-(0.134^2)+(0.0976^2)-(0.096^2)); % [m^2]
% k wall = 25; % Stainless steel [W/m^2K] (Temperature dependent)
% L wall = 0.05651; %[m] Length of regenerator cavity in this case
% A regen = 0.1*0.25*pi*((0.134^2)-(0.0976^2)); %[m^2] Area x porosity
% L regen = 0.05651; %[m]
% A displacer = 0.25*pi*(0.094^2); %[m^2]
% k displacer = (0.25*pi)*(1/A displacer)*(((0.0924^2)*(kgas))+(((0.094^2)-
(0.0924^2))*k wall)); %[W/mK]
% L displacer = 0.15405; %[m]
% Inputs for As Built HTG Stirling Engine
A wall = 0.25*pi*((0.1465^2)-(0.1355^2)+(0.103^2)-(0.0956^2)); % [m^2]
k wall = 47; % AISI 1020 steel [W/m^2K] (From Solidworks)
L wall = 0.055; %[m] Length of regenerator cavity in this case
A regen = 0.25*pi*((0.1355^2)-(0.103^2)); %[m^2] Area or regenerator
k regen = 0.9*ENGINE DATA.kgas + 0.1*(19); % Porosity weighted working gas +
316 stainless steel.
L regen = 0.055; %[m]
A displacer = 0.25*pi*(0.094^2); %[m^2]
k displacer
                                                                              =
(0.25*pi)*(1/A_displacer)*(((0.0924^2)*(ENGINE DATA.kgas))+(((0.094^2)-
(0.0924<sup>2</sup>))*19)); %[W/mK]
L displacer = (0.15613 + 0.14513)/2; %[m]
% Conduction through the engine walls
Q wall = (A wall*k wall*(ENGINE DATA.Twh-ENGINE DATA.Twk))/L wall; %[W]
% Conduction through the regenerator
Q fluid = (A regen*k regen*(ENGINE DATA.Tgh-ENGINE DATA.Tgk))/L regen; %[W]
% Conduction through the displacer
Q displacer = (A displacer*k displacer*(mean([REF CYCLE DATA.Tge])...
    -mean([REF CYCLE DATA.Tgc])))/L displacer; %[W]
% Total Conduction Loss [W]
LOSSES DATA.Q cond = Q wall + Q fluid + Q displacer;
%% Gas Spring Hysteresis Losses
% Input parameters needed:
% Tw --> gas spring wall temperature [K]
% delV --> volume amplitude of the spring cavity [m^3]
% VB --> mean volume of the gas spring cavity [m^3]
% Aw --> mean wetted area of the gas spring [m^2]
% delA --> wetted area amplitude [m^2]
```

```
% Inputs for Original ST05G-CNC Stirling Engine
% Tw = ENGINE DATA.Tqk; %[K] (assumed to be equal to the cooler temperature)
% delV = 0.25*pi*(0.085^2)*0.075; %[m^3]
% VB = 0.5*delV + 0.002488647 + 0.000091248 + 0.000419874 + 0.000186558 + ...
8
      0.000182367 - 0.000229935 - 0.000061378 - 0.000059277 - ...
8
      0.000007376 - 0.000021882 - 0.000013195 - 0.000009817 - ...
8
      0.000009173 - 0.000231607; %[m^3]
% delA = pi*0.085*0.075; %[m^2]
% Aw = 0.5*delA + 0.05853681 + 0.00804849 + 0.01866106 + 0.01030158 + ...
2
     0.02145481 + 0.03279471 + 0.01778246 + 0.02301812 + 0.00211262 + \ldots
8
      0.007294024 + 0.00026389 + 0.00045239 + 0.02173007; % [m^2]
00
% % Calculation of the gas spring hysteresis loss
% F1 = sqrt(0.125*ENGINE DATA.omega*ENGINE DATA.gamma*...
% (ENGINE DATA.gamma-1)*Tw*ENGINE DATA.pmean*ENGINE DATA.kgas);
% F2 = (delV/VB)*((0.5*ENGINE DATA.gamma*(delV/VB)*Aw) - delA);
8
% LOSSES DATA.P GSH = F1*F2*ENGINE DATA.freq; % Power lost to gas spring
hysteresis in [W].
LOSSES DATA.P GSH = 0;
%% Seal Leakage Losses
% Input parameters needed:
% mloss outside --> Working fluid loss rate due to leakage to the outside
[Pa/s]
% isentropic eff comp --> Isentropic efficiency of the compressor
\% h ambient --> Enthalpy of the air entering the compressor in [J/kg]
\% h2 isentropic --> Discharge enthalpy of the compressor in [J/kg]
% Inputs for HTG Stirling Engine
mloss outside = 0; % [kg/s]
isentropic_eff_comp = 0.75; % [unitless]
h ambient = 298180; % [J/kg]
h2 isentropic = 575590; % [J/kg]
% Piston Leakage
% Displacer Leakage
% Leakage to the outside (adds compressor work for a pressurized engine)
% *** This will not affect the measured engine output if the engine is not
% driving the compressor.
% Power consumed by the compressor to maintain engine pressure
P compressor = (mloss outside*(h2 isentropic-h ambient))/isentropic eff comp;
8[W]
% Total leakage loss effects
LOSSES DATA.P seals = P compressor; % Power lost due to seal leakage in [W].
LOSSES DATA.Q seals = 0; % Heat lost due to seal leakage in [W].
%% Appendix Gap Losses (Pg 140 of Urieli and Berchowitz)
% Input parameters needed:
\% D --> diameter of the displacer cylinder \ref{eq:D} [m]
% kgas --> thermal conductivity of the working fluid [W/mK]
```

```
% Xd --> displacer motion amplitude (displacer stroke) [m]
% upsilon --> linear axial temperature gradient (bad assumption in this case
since cooler is a different material) [K/m]
% h --> appendix gap width(distance b/w displacer wall and cylinder wall) [m]
% omega --> engine angular frequency [rad/s]
% phi --> phase angle b/w displacer motion and pressure variation [rad]
% alpha solid --> thermal diffusivity of the displacer and cylinder material
in [m^2/s]
% k solid --> thermal conductivity of the displacer and cylinder material in
[W/m.K]
% Inputs for HTG Stirling Engine
D = 0.096; \%[m]
Xd = 0.075; %[m]
upsilon = (ENGINE DATA.Tqh-ENGINE DATA.Tqk)/0.220; %[K/m] (Divided by length
of displacer cylinder)
h = 0.001; %[m]
alpha solid = 1.172e-05; % [m^2/s] (Steel from Wikipedia)
k solid = 47; %[W/m.K] (AISI 1020 Steel from Solidworks - Displacer is
Stainless so this should be refined)
% Crank angle at which minimum workspace pressure occurs
[~,pmax index] = max([REF CYCLE DATA.p]);
pmaxAngle = pmax index*crank inc - crank inc; %[degrees]
% Crank angle at which expansion space volume is minimum
[~,Vemin index] = min([REF CYCLE DATA.Ve]);
DispTDCAngle = Vemin index*crank inc - crank inc; %[degrees]
% Crank angle by which pressure variation leads the displacer motion
phi = (pmaxAngle-DispTDCAngle); %[degrees]
pressure = [REF CYCLE DATA.p];
delp = max(pressure) - min(pressure); %[Pa]
w = sqrt(ENGINE DATA.omega/(2*alpha solid));
A1 = -pi*0.5*D*ENGINE DATA.kgas*(Xd^2)*(upsilon/h);
A2 = pi*D*delp*h*Xd*ENGINE DATA.omega*sin(phi);
AЗ
                                        (ENGINE DATA.gamma/(ENGINE DATA.gamma-
1)) *log(ENGINE DATA.Tgh/ENGINE DATA.Tgk)*...
    (0.5-(ENGINE DATA.kgas/(w*h*k solid))-0.5);
LOSSES DATA.Q app = abs(A1 + (A2*A3)); % Heat lost due to appendix gap in
[W].
%% Heat Transfer Hysteresis
LOSSES DATA.P HTH = 0; % Power lost to heat transfer hysteresis in [W].
%% Finite Piston Speed Loss
% % Equations come from Petrescu 2002 and quasi-steady approach was inspired
% % by Hosseinzade 2015
```

```
0
% % Calculate the constant quantity "a"
% a = sqrt(3*ENGINE DATA.gamma);
8
% % Calculate vectors of average molecular speeds corresponding to the
% % vector of crank angle increments in (m/s)
% cc = sqrt(3*ENGINE DATA.R.*[REF CYCLE DATA.Tqc]); % Compression space
% ce = sqrt(3*ENGINE DATA.R.*[REF CYCLE DATA.Tge]); % Expansion space
8
% % Calculate vectors of piston speeds in (m/s)
% Dr1 = ENGINE DATA.Dr1;
% Dr2 = ENGINE DATA.Dr2;
% Dr3 = ENGINE DATA.Dr3;
% Dbore = ENGINE DATA.Dbore;
2
% Pr1 = ENGINE DATA.Pr1;
% Pr2 = ENGINE DATA.Pr2;
% Pr3 = ENGINE DATA.Pr3;
% Pbore = ENGINE DATA.Pbore;
% Ptheta2 = pi - [REF CYCLE DATA.theta]; %(rad)
% Dtheta2 = Ptheta2 - ENGINE DATA.beta; %(rad)
8
% Ptheta2 dot = -ENGINE DATA.omega; %(rad/s)
% Dtheta2 dot = -ENGINE DATA.omega; %(rad/s)
8
% Ptheta3 = pi - asin((-Pr1+(Pr2.*sin(Ptheta2)))./Pr3); %(rad)
% Dtheta3 = pi - asin((-Dr1+(Dr2.*sin(Dtheta2)))./Dr3); %(rad)
0
% wp = (Pr2*Ptheta2 dot.*sin(Ptheta3-Ptheta2))./cos(Ptheta3); %(m/s)
% wd = (Dr2*Dtheta2 dot.*sin(Dtheta3-Dtheta2))./cos(Dtheta3); %(m/s)
2
% % Calculate incremental volume changes caused by the piston and displacer
          dPtheta3
                                        (Pr2.*cos(Ptheta2))./(Pr3.*sqrt(1-(((-
8
                     =
Pr1+(Pr2.*sin(Ptheta2)))./Pr3).^2)));
% dPr4 = Pr2.*sin(Ptheta2) + Pr3.*sin(Ptheta3).*dPtheta3;
% dVp = -(pi/4) * (Pbore^{2}) .* dPr4;
8
        dDtheta3
                                        (Dr2.*cos(Dtheta2))./(Dr3.*sqrt(1-(((-
00
                        =
Dr1+(Dr2.*sin(Dtheta2)))./Dr3).^2)));
% dDr4 = Dr2.*sin(Dtheta2) + Dr3.*sin(Dtheta3).*dDtheta3;
% dVe = -(pi/4) * (Dbore^{2}) . * (dDr4);
2
% % Calculate vectors of lost work
% dWp = [REF CYCLE DATA.p].*(-a*wp./cc).*dVp;
8
% % Calculate total work lost to finite piston speed
% W FPS = sum(dWp);
0
% % Calculate total power lost to finite piston speed
% LOSSES DATA.P FPS = W FPS*ENGINE DATA.freq; %(W)
LOSSES DATA.P FPS = 0; % Power loss due to relative motion between piston and
gas molecules in [W].
```

```
%% Cooling/Heating System Pumping Power
```

% Some of the power produced by the engine must be used to drive the % coolant pump (unless a heat pipe or other passive cooling method is used). % A fuel pump or hot side water pump may also be needed. % Inputs: % rho cool --> density of coolant in (kg/m^3) $g \rightarrow g$ g \rightarrow gravitational acceleration in (m/s²) % V dot cool --> volume flow rate of coolant in (m^3/s) % H cool --> coolant pump net head in (m) % eff pump cool --> coolant pump efficiency % P pump cool = (rho cool*g*V dot cool*H cool)/eff pump; %(W) LOSSES DATA.P pump cool = 0; % Power required to drive the coolant pump in (W). LOSSES DATA.P pump hot = 0; % Power required to drive fuel pump or hot water pump in [W]. %% Exergy Destruction due to Heat Conduction at the Thermal Source/Sink Interfaces % The temperature drop between the heater/cooler gas temperature and the % thermal source/sink causes exergy destruction. % Calculations follow an example on Pg 446 of Cengel Thermodynamics % Assumptions: % 1. Steady state conduction process. % 2. 1-dimensional heat conduction. % 3. The exergy of the wall itself is constant, since it does not change % state. % Average heat transfer rates in the heater and cooler in (W) Qh dot avg = mean([REF CYCLE DATA.Qh]*ENGINE DATA.freq); Qk dot avg = mean([REF CYCLE DATA.Qk]*ENGINE DATA.freq); % Average gas temperatures in the heater and cooler in (K) Tgh avg = mean([ENGINE DATA.Tgh]); Tgk avg = mean([ENGINE DATA.Tgk]); % Temperatures of the thermal source and sink in (K) Tsource = ENGINE DATA.Tsource; Tsink = ENGINE DATA.Tsink; T0 = ENGINE DATA.Tsink; % Temperature of the environment in (K) % Calculate exergy destruction in the heater and cooler in (W) LOSSES DATA.X dest source = Qh dot avg*(1-(T0/Tsource)) - Qh dot avg*(1-(TO/Tgh avg)); LOSSES DATA.X dest sink = Qk dot avg*(1-(T0/Tsink)) - Qk dot avg*(1-(TO/Tgk avg));

%% Heat lost through the heating cap insulation LOSSES DATA.Q insulation = 0;

parasitic_losses_HTG_B.m

function LOSSES DATA parasitic losses HTG B(ENGINE DATA, REF CYCLE DATA, crank inc) % Written by Connor Speer - January 2017 % Calculates the parasitic losses. % Modified by Connor Speer, October 2017. No globals. % Losses already accounted for by the "Simple" simulation: % - Regenerator Enthalpy Loss % Inputs: % ENGINE DATA --> Structure containing engine geometry and operating point % REF CYCLE DATA --> Structure containing data from the reference cycle % crank inc --> crank angle step size in [degrees] % Output: % LOSSES DATA --> Structure containing parasitic loss information %% Mechanical Friction (Forced Work Method, See Senft's Book) vtot = ([REF CYCLE DATA.Vc] + ENGINE DATA.Vk + ENGINE DATA.Vr + ... ENGINE DATA.Vh + [REF CYCLE DATA.Ve]); % cubic meters p engine = [REF CYCLE DATA.p]; % Pascals Pbore = ENGINE DATA.Pbore; % piston bore [m] Pr1 = ENGINE DATA.Pr1; % piston desaxe offset in [m] Pr2 = ENGINE DATA.Pr2; % piston crank length (half stroke) in [m] Pr3 = ENGINE DATA.Pr3;% piston connecting rod lengths [m] theta = 0:crank inc*(pi/180):2*pi; Ptheta2 = pi - theta;Ptheta3 = pi - asin((-Pr1+(Pr2*sin(Ptheta2)))/Pr3); Pr4 = Pr2*cos(Ptheta2) - Pr3*cos(Ptheta3); $Pr4max = sqrt(((Pr2+Pr3)^2) - (Pr1^2));$ $Pr4min = sqrt(((Pr3-Pr2)^{2})-(Pr1^{2}));$ Pstroke = Pr4max - Pr4min; % Crankcase Volume Variations in (m^3) V buffer = ENGINE DATA.V buffer max - ((Pr4max-Pr4)*(((pi/4)*(Pbore^2)))); p0 = mean([REF CYCLE DATA.p]); % Mean crankcase pressure in (Pa). % Mean crankcase volume in (m^3). V0 = ENGINE DATA.V buffer max - 0.5*Pstroke*(((pi/4)*(Pbore^2))); % % Constant Buffer Pressure Equal to the Mean Pressure

=

```
% p buff const = mean([REF CYCLE DATA.p]); % Pascals
% p buffer = repelem(p buff const, length(vtot));
% % Buffer Pressure Assuming Isothermal Compression and Expansion
% T crankcase = ENGINE DATA.Tgc; % Mean crankcase temperature in [K].
% % Mass of gas in the crankcase in [kg].
% m crankcase = (p0*V0)/(ENGINE DATA.rgas*T crankcase);
% p buffer = (m crankcase*R*T crankcase)./V buffer;
% Buffer Pressure Assuming Adiabatic Compression and Expansion in (Pa).
p buffer = p0.*((V0./V buffer).^ENGINE DATA.gamma);
% % Buffer Pressure Determined By Shazeb's Empirical Ellipse Function
% p buffer = getBufferPressure(ENGINE DATA.pmean,crank inc);
[W ind, FW, W shaft] = \dots
    FW Subfunction v3(1,p engine,p buffer,vtot,ENGINE DATA.effect,0);
% Store forced work in LOSSES DATA structure
LOSSES DATA.FW = FW; %(J)
% Net output shaft power (W) (Senft's formula)
P shaft = W shaft*ENGINE DATA.freq;
% Power lost to mechanical friction in [W]
LOSSES DATA.P mech = (W ind*ENGINE DATA.freq) - P shaft;
%% Flow Friction
regen corr factor = 1;
% Calculate pressure drops
[~,~,~,pdropk,pdroph,pdropr] = ...
   worksim(ENGINE DATA, REF CYCLE DATA, crank inc);
LOSSES DATA.pdropk = pdropk; % Pressure drop across the cooler in (Pa)
LOSSES DATA.pdroph = pdroph; % Pressure drop across the heater in (Pa)
LOSSES DATA.pdropr = pdropr; % Pressure drop across the regenerator in (Pa)
dwork h
                                                                           =
sum(crank inc*(pi/180).*pdropr(1:360).*[REF CYCLE DATA(1:360).dVe]);
                                                                           8
pumping work [J]
dwork r
sum(crank inc*(pi/180).*regen corr factor.*pdropr(1:360).*[REF CYCLE DATA(1:3
60).dVe]); % pumping work [J]
dwork k
                                                                           =
sum(crank inc*(pi/180).*pdropr(1:360).*[REF CYCLE DATA(1:360).dVe]);
                                                                           00
pumping work [J]
% Pressure drop power loss in the heater
LOSSES DATA.P flow h = dwork h*ENGINE DATA.freq; %(W)
% Pressure drop power loss in the regenerator
```

```
LOSSES DATA.P flow r = dwork r*ENGINE DATA.freq; %(W)
% Pressure drop power loss in the cooler
LOSSES DATA.P flow k = dwork k*ENGINE DATA.freq; %(W)
%% Regenerator Enthalpy Loss
A = isfield(REF CYCLE DATA, 'qrloss');
if A == 1
    \% Convert regenerator enthalpy loss per cycle in (J) to a rate in (W)
    LOSSES DATA.Q qrloss = REF CYCLE DATA(1).qrloss*ENGINE DATA.freq; %(W)
else
    LOSSES DATA.Q qrloss = 0;
end
%% Conduction Loss (1-D Fourier Law)
% Input parameters needed:
% A wall --> Average cross-sectional area of the wall conduction path [m^2]
% k wall --> Average thermal conductivity of the wall conduction material
% [W/mK]
% L wall --> Length of the wall conduction path [m]
% A regen --> Regenerator free flow area [m^2]
% kgas --> Thermal conductivity of the working gas [W/mK]
% L regen --> Length of the regenerator [m]
% A displacer --> Cross-sectional area of the displacer [m^2]
% k displacer --> Effective thermal conductivity of the displacer [W/m^2]
% L displacer --> Length of the displacer [m]
% % Inputs for Original ST05G-CNC Stirling Engine
% A wall = 0.25*pi*((0.1397^2)-(0.134^2)+(0.0976^2)-(0.096^2)); % [m^2]
% k_wall = 25; % Stainless steel [W/m^2K] (Temperature dependent)
% L wall = 0.05651; %[m] Length of regenerator cavity in this case
% A regen = 0.1*0.25*pi*((0.134^2)-(0.0976^2)); %[m^2] Area x porosity
% L regen = 0.05651; %[m]
% A displacer = 0.25*pi*(0.094^2); %[m^2]
% k displacer = (0.25*pi)*(1/A displacer)*(((0.0924^2)*(kgas))+(((0.094^2)-
(0.0924^2))*k wall)); %[W/mK]
% L displacer = 0.15405; %[m]
% % Inputs for As Built HTG Stirling Engine
A wall = 0.25*pi*((0.1465^2)-(0.1355^2)+(0.103^2)-(0.0956^2)); % [m^2]
k wall = 47; % AISI 1020 steel [W/m^2K] (From Solidworks)
L wall = 0.055; %[m] Length of regenerator cavity in this case
A regen = 0.25*pi*((0.1355^2)-(0.103^2)); %[m^2] Area or regenerator
k regen = 0.9*ENGINE DATA.kgas + 0.1*(19); % Porosity weighted working gas +
316 stainless steel.
L regen = 0.055; %[m]
A displacer = 0.25*pi*(0.094^2); %[m^2]
k displacer
                                                                              =
(0.25*pi)*(1/A displacer)*(((0.0924^2)*(ENGINE DATA.kgas))+(((0.094^2)-
(0.0924<sup>2</sup>))*19)); %[W/mK]
L displacer = (0.15613 + 0.14513)/2; %[m]
% Conduction through the engine walls
```

```
Q_wall = (A_wall*k_wall*(ENGINE_DATA.Tgh-ENGINE_DATA.Tgk))/L_wall; %[W]
```

```
% Conduction through the regenerator
Q fluid = (A regen*k regen*(ENGINE DATA.Tqh-ENGINE DATA.Tqk))/L regen; %[W]
% Conduction through the displacer
Q displacer = (A displacer*k displacer*(mean([REF CYCLE DATA.Tge])...
    -mean([REF CYCLE DATA.Tgc])))/L displacer; %[W]
% Conduction through the regenerator material
% Total Conduction Loss [W]
LOSSES DATA.Q cond = Q wall + Q fluid + Q displacer;
%% Gas Spring Hysteresis Losses
% Input parameters needed:
% Tw --> gas spring wall temperature [K]
% delV --> volume amplitude of the spring cavity [m^3]
% VB --> mean volume of the gas spring cavity [m^3]
% Aw --> mean wetted area of the gas spring [m<sup>2</sup>]
% delA --> wetted area amplitude [m^2]
% % Inputs for Original ST05G-CNC Stirling Engine
% Tw = ENGINE DATA.Tqk; %[K] (assumed to be equal to the cooler temperature)
% delV = 0.25*pi*(0.085^2)*0.075; %[m^3]
% VB = 0.5*delV + 0.002488647 + 0.000091248 + 0.000419874 + 0.000186558 + ...
      0.000182367 - 0.000229935 - 0.000061378 - 0.000059277 - ...
8
8
      0.000007376 - 0.000021882 - 0.000013195 - 0.000009817 - ...
2
      0.000009173 - 0.000231607; %[m^3]
% delA = pi*0.085*0.075; %[m^2]
% Aw = 0.5*delA + 0.05853681 + 0.00804849 + 0.01866106 + 0.01030158 + ...
     0.02145481 + 0.03279471 + 0.01778246 + 0.02301812 + 0.00211262 + ...
      0.007294024 + 0.00026389 + 0.00045239 + 0.02173007; %[m^2]
8
8
% % Calculation of the gas spring hysteresis loss
% F1 = sqrt(0.125*ENGINE DATA.omega*ENGINE DATA.gamma*...
% (ENGINE DATA.gamma-1)*Tw*ENGINE DATA.pmean*ENGINE DATA.kgas);
% F2 = (delV/VB)*((0.5*ENGINE DATA.gamma*(delV/VB)*Aw) - delA);
2
% P hys = F1*F2*ENGINE DATA.freq; % Power lost to gas spring hysteresis in
[W].
% Empirical Formula Based on Experimental Data
LOSSES DATA.P GSH
HTG GSH Empirical (ENGINE DATA.freq, ENGINE DATA.pmean, ENGINE DATA.GSH config);
8[W]
%% Seal Leakage Losses
% Input parameters needed:
% mloss outside --> Working fluid loss rate due to leakage to the outside
[Pa/s]
% isentropic eff comp --> Isentropic efficiency of the compressor
\% h ambient \overline{-->} Enthalpy of the air entering the compressor in [J/kg]
\frac{1}{2} h2 isentropic --> Discharge enthalpy of the compressor in [J/kg]
```

```
% Inputs for HTG Stirling Engine
mloss outside = 0; % [kg/s]
isentropic eff comp = 0.75; % [unitless]
h ambient = 298180; % [J/kg]
h2 isentropic = 575590; % [J/kg]
% Piston Leakage
% Displacer Leakage
% Leakage to the outside (adds compressor work for a pressurized engine)
% *** This will not affect the measured engine output if the engine is not
% driving the compressor.
% Power consumed by the compressor to maintain engine pressure
P compressor = (mloss outside*(h2 isentropic-h ambient))/isentropic eff comp;
8[W]
% Total leakage loss effects
LOSSES DATA.P seals = 0; % Power lost due to seal leakage in [W].
LOSSES DATA.Q seals = 0; % Heat lost due to seal leakage in [W].
%% Appendix Gap Losses (Pg 140 of Urieli and Berchowitz)
% Input parameters needed:
% D --> diameter of the displacer cylinder ??? [m]
% kgas --> thermal conductivity of the working fluid [W/mK]
% Xd --> displacer motion amplitude (displacer stroke) [m]
% upsilon --> linear axial temperature gradient (bad assumption in this case
since cooler is a different material) [K/m]
% h --> appendix gap width(distance b/w displacer wall and cylinder wall) [m]
% omega --> engine angular frequency [rad/s]
% phi --> phase angle b/w displacer motion and pressure variation [rad]
% alpha solid --> thermal diffusivity of the displacer and cylinder material
in [m^2/s]
% k solid --> thermal conductivity of the displacer and cylinder material in
[W/m.K]
% Inputs for HTG Stirling Engine
D = 0.096; \%[m]
Xd = 0.075; %[m]
upsilon = (ENGINE DATA.Tqh-ENGINE DATA.Tqk)/0.220; %[K/m] (Divided by length
of displacer cylinder)
h = 0.001; %[m]
alpha solid = 1.172e-05; %[m^2/s] (Steel from Wikipedia)
k solid = 47; %[W/m.K] (AISI 1020 Steel from Solidworks - Displacer is
Stainless so this should be refined)
% Crank angle at which minimum workspace pressure occurs
[~,pmax index] = max([REF CYCLE DATA.p]);
pmaxAngle = pmax index*crank inc - crank inc; %[degrees]
% Crank angle at which expansion space volume is minimum
[~,Vemin index] = min([REF CYCLE DATA.Ve]);
DispTDCAngle = Vemin index*crank inc - crank inc; %[degrees]
```

```
% Crank angle by which pressure variation leads the displacer motion
phi = (pmaxAngle-DispTDCAngle); %[degrees]
pressure = [REF CYCLE DATA.p];
delp = max(pressure) - min(pressure); %[Pa]
w = sqrt(ENGINE DATA.omega/(2*alpha solid));
A1 = -pi*0.5*D*ENGINE DATA.kgas*(Xd^2)*(upsilon/h);
A2 = pi*D*delp*h*Xd*ENGINE DATA.omega*sin(phi);
AЗ
                                        (ENGINE DATA.gamma/(ENGINE DATA.gamma-
1)) *log(ENGINE DATA.Tgh/ENGINE DATA.Tgk) *...
    (0.5-(ENGINE DATA.kgas/(w*h*k solid))-0.5);
LOSSES DATA.Q app = abs(A1 + (A2*A3)); % Heat lost due to appendix gap in
[W].
%% Heat Transfer Hysteresis
LOSSES DATA.P HTH = 0; % Power lost to heat transfer hysteresis in [W].
%% Finite Piston Speed Loss
% % Equations come from Petrescu 2002 and quasi-steady approach was inspired
% % by Hosseinzade 2015
2
% % Calculate the constant quantity "a"
% a = sqrt(3*ENGINE DATA.gamma);
00
% % Calculate vectors of average molecular speeds corresponding to the
% % vector of crank angle increments in (m/s)
% cc = sqrt(3*ENGINE_DATA.R.*[REF CYCLE DATA.Tgc]); % Compression space
% ce = sqrt(3*ENGINE DATA.R.*[REF CYCLE DATA.Tqe]); % Expansion space
8
% % Calculate vectors of piston speeds in (m/s)
% Dr1 = ENGINE DATA.Dr1;
% Dr2 = ENGINE DATA.Dr2;
% Dr3 = ENGINE DATA.Dr3;
% Dbore = ENGINE DATA.Dbore;
2
% Pr1 = ENGINE DATA.Pr1;
% Pr2 = ENGINE DATA.Pr2;
% Pr3 = ENGINE DATA.Pr3;
% Pbore = ENGINE DATA.Pbore;
00
% Ptheta2 = pi - [REF CYCLE DATA.theta]; %(rad)
% Dtheta2 = Ptheta2 - ENGINE DATA.beta; %(rad)
% Ptheta2 dot = -ENGINE DATA.omega; %(rad/s)
% Dtheta2 dot = -ENGINE DATA.omega; %(rad/s)
8
% Ptheta3 = pi - asin((-Pr1+(Pr2.*sin(Ptheta2)))./Pr3); %(rad)
% Dtheta3 = pi - asin((-Dr1+(Dr2.*sin(Dtheta2)))./Dr3); %(rad)
0
% wp = (Pr2*Ptheta2 dot.*sin(Ptheta3-Ptheta2))./cos(Ptheta3); %(m/s)
```

```
% wd = (Dr2*Dtheta2 dot.*sin(Dtheta3-Dtheta2))./cos(Dtheta3); %(m/s)
2
% % Calculate incremental volume changes caused by the piston and displacer
                    =
                                        (Pr2.*cos(Ptheta2))./(Pr3.*sqrt(1-(((-
8
          dPtheta3
Pr1+(Pr2.*sin(Ptheta2)))./Pr3).^2)));
% dPr4 = Pr2.*sin(Ptheta2) + Pr3.*sin(Ptheta3).*dPtheta3;
% dVp = -(pi/4) * (Pbore^{2}) .* dPr4;
00
8
        dDtheta3
                                        (Dr2.*cos(Dtheta2))./(Dr3.*sqrt(1-(((-
Dr1+(Dr2.*sin(Dtheta2)))./Dr3).^2)));
% dDr4 = Dr2.*sin(Dtheta2) + Dr3.*sin(Dtheta3).*dDtheta3;
% dVe = -(pi/4) * (Dbore^2) .* (dDr4);
2
% % Calculate vectors of lost work
% dWp = [REF CYCLE DATA.p].*(-a*wp./cc).*dVp;
% % Calculate total work lost to finite piston speed
% W FPS = sum(dWp);
00
% % Calculate total power lost to finite piston speed
% LOSSES DATA.P FPS = W FPS*ENGINE DATA.freq; %(W)
LOSSES DATA.P FPS = 0; % Power loss due to relative motion between piston and
gas molecules in [W].
%% Cooling/Heating System Pumping Power
\% Some of the power produced by the engine must be used to drive the
% coolant pump (unless a heat pipe or other passive cooling method is used).
% A fuel pump or hot side water pump may also be needed.
% Inputs:
% rho cool --> density of coolant in (kg/m^3)
g \rightarrow q avoitational acceleration in (m/s<sup>2</sup>)
% V dot cool --> volume flow rate of coolant in (m^3/s)
% H cool --> coolant pump net head in (m)
% eff pump cool --> coolant pump efficiency
% P pump cool = (rho cool*g*V dot cool*H cool)/eff pump; %(W)
LOSSES DATA.P pump cool = 0; % Power required to drive the coolant pump in
(W).
LOSSES DATA.P pump hot = 0; % Power required to drive fuel pump or hot water
pump in [W].
%% Exergy Destruction due to Heat Conduction at the Thermal Source/Sink
Interfaces
% The temperature drop between the heater/cooler gas temperature and the
% thermal source/sink causes exergy destruction.
% Calculations follow an example on Pq 446 of Cengel Thermodynamics
% Assumptions:
% 1. Steady state conduction process.
% 2. 1-dimensional heat conduction.
```

```
% 3. The exergy of the wall itself is constant, since it does not change
% state.
% Average heat transfer rates in the heater and cooler in (W)
Qh dot avg = mean([REF CYCLE DATA.Qh]*ENGINE DATA.freq);
Qk dot avg = mean([REF CYCLE DATA.Qk]*ENGINE DATA.freq);
% Average gas temperatures in the heater and cooler in (K)
Tgh avg = mean([ENGINE DATA.Tgh]);
Tqk avg = mean([ENGINE DATA.Tqk]);
% Temperatures of the thermal source and sink in (K)
Tsource = ENGINE DATA.Tsource;
Tsink = ENGINE DATA.Tsink;
T0 = ENGINE DATA.Tsink; % Temperature of the environment in (K)
% Calculate exergy destruction in the heater and cooler in (W)
LOSSES DATA.X dest source = Qh dot avq^{(1-(T0/Tsource))} -
                                                               Qh dot avg*(1-
(T0/Tgh avg));
LOSSES DATA.X dest sink = Qk dot avg*(1-(T0/Tsink)) - Qk dot avg*(1-
(TO/Tgk avg));
%% Heat lost through the heating cap insulation
```

% LOSSES_DATA.Q_insulation = 135; % Measured at 300 deg C Cap Temperature (W) LOSSES DATA.Q insulation = 90; % Measured at 200 deg C Cap Temperature (W)

Vary.m

```
function DATA_STRUCTURE = Vary(varName,Min,Max,Increment,ENGINE_DATA,...
crank_inc,Model_Code,Losses_Code,part_traj_on_off)
% Written by Connor Speer - April 2017
% Editted by Shahzeb Mirza - October 2017
% The purpose of this script is to run the SEA code repeatedly for a
% variety of any given variable, and return results.
% Inputs:
% varName --> String with the exact variable name
% Min --> Lower bound of the variable range being considered [any unit]
% Max --> Upper bound of the variable range being considered [any unit]
% Increment --> Increment size for variable range [any unit
% ENGINE_DATA --> Structure which defines engine geometry and operating
conditions
% Crank_Angle_Increment --> Crank angle step size for numerical integration
in [degrees]
```

```
% Model Code --> Code specifying which model to run.
% 1 = Ideal Isothermal Model
% 2 = Ideal Adiabatic Model
% 3 = Simple Model
% Losses Code --> Code specifying which losses subfunction to run
% 1 = parasitic_losses_GEN.m
% 2 = parasitic losses HTG.m
range = Min:Increment:Max;
% Preallocate space
DATA STRUCTURE(length(range)).REF CYCLE DATA = [];
DATA STRUCTURE(length(range)).LOSSES DATA = [];
counter = 1; % Initialize counter variable
for i = range
    command = strcat('ENGINE DATA.', varName,' = i;');
    eval(command);
    % Call the SEA code as a subfunction
    [REF CYCLE DATA, LOSSES DATA, PARTICLE TRAJECTORY DATA, ENGINE DATA] =
. . .
    sea(ENGINE DATA,crank inc,Model Code, Losses Code,part traj on off);
    % Store outputs from the SEA code
    DATA STRUCTURE (counter).REF CYCLE DATA = REF CYCLE DATA;
    DATA STRUCTURE (counter) . LOSSES DATA = LOSSES DATA;
    % Close the temporary data file to prevent Matlab errors
    fclose('all');
    counter = counter + 1;
end
```

Miscellaneous Functions

rk4.m

```
function [x, y, dy] = rk4(n,x,dx,y,ENGINE DATA)
% Classical fourth order Runge-Kutta method
% Integrates n first order differential equations
% dy(x,y) over interval x to x+dx
% Israel Urieli - Jan 21, 2002
x0 = x;
y0 = y;
% Modifications made by Steven Middleton
% (1) eliminated for loops in favor of matrix operations (faster)
% ... previous code maintained in comments
% Comments: Is it necassary to pass y variable through deriv? It is
% unused. Also, if one has the function handle feval is unnecessary.
% Modifications made by Connor Speer, October 2017:
% Got rid of feval in favour of calling dadiab directly.
% Now uses the ENGINE DATA structure.
[y,dy1] = dadiab(x0,y,ENGINE DATA);
y(1:n) = y0(1:n) + 0.5*dx*dy1(1:n);
xm = x0 + 0.5*dx;
[y,dy2] = dadiab(xm,y,ENGINE DATA);
y(1:n) = y0(1:n) + 0.5*dx*dy2(1:n);
[y,dy3] = dadiab(xm,y,ENGINE DATA);
y(1:n) = y0(1:n) + dx*dy3(1:n);
x = x0 + dx;
[y,dy] = dadiab(x,y,ENGINE DATA);
dy = (dy1 + 2*(dy2 + dy3) + dy)/6;
y(1:n) = y0(1:n) + dx*dy(1:n);
% function [x, y, dy] = rk4(deriv,n,x,dx,y)
% % Classical fourth order Runge-Kutta method
% % Integrates n first order differential equations
% % dy(x,y) over interval x to x+dx
% % Israel Urieli - Jan 21, 2002
% x0 = x;
% V0 = V;
% [y,dy1] = feval(deriv,x0,y);
% for i = 1:n
% y(i) = y0(i) + 0.5*dx*dy1(i);
% end
% xm = x0 + 0.5 * dx;
% [y,dy2] = feval(deriv,xm,y);
% for i = 1:n
```

```
% y(i) = y0(i) + 0.5*dx*dy2(i);
% end
% [y,dy3] = feval(deriv,xm,y);
% for i = 1:n
% y(i) = y0(i) + dx*dy3(i);
% end
% x = x0 + dx;
% [y,dy] = feval(deriv,x,y);
% for i = 1:n
% dy(i) = (dy1(i) + 2*(dy2(i) + dy3(i)) + dy(i))/6;
% y(i) = y0(i) + dx*dy(i);
% end
```

mass_correction.m

```
function ENGINE DATA = mass correction (ENGINE DATA, crank inc, Model Code)
% Written by Connor Speer and Shahzeb Mirza, October 2017.
% This function uses the iterative scheme proposed by "2015(Paul) Modeling a
% complete Stirling engine", to correct the mass of working fluid so that
% the reference cycle simulation has the same mean pressure as the one
% specified by the user in ENGINE DATA.
% Find pressure as a function of crank angle using the initial mass value
% in the ENGINE DATA structure, which is calculated in define.m using the
% Schmidt analysis.
if Model Code == 1
    % Solve the ideal isothermal model
    ISOTHERMAL DATA = isothermal(ENGINE DATA, crank inc);
   REF CYCLE DATA = ISOTHERMAL DATA;
elseif Model Code == 2
    % Solve the ideal adiabatic model
    ADIABATIC DATA = adiabatic (ENGINE DATA, crank inc);
   REF CYCLE DATA = ADIABATIC DATA;
elseif Model Code == 3
    % Solve the simple model (no flow friction)
    SIMPLE DATA = simple(ENGINE DATA, crank inc);
    REF CYCLE DATA = SIMPLE DATA;
else
    disp('ERROR: Invalid model code.')
end
% Find the mean pressure of the reference cycle
pbar = mean([REF CYCLE DATA.p]); %(Pa)
% Recall the mean pressure specified in the ENGINE DATA structure.
pmean = ENGINE DATA.pmean; %(Pa)
% If this 'found' mean pressure is significantly different from the
% 'desired' mean pressure specified in the ENGINE DATA structure, then
% iteratively loop through an algorithm that changes the mass value until
% the mean pressure calculated by the reference cycle matches the desired
```

% value.

```
Mold = ENGINE DATA.mgas; % (kg)
while( abs((pmean - pbar)/pmean) > 0.001 )
    Mnew = (1 + (pmean - pbar)/pmean) * Mold;
    Mold = Mnew;
    ENGINE DATA.mgas = Mnew;
    if Model Code == 1
        % Solve the ideal isothermal model
        ISOTHERMAL DATA = isothermal(ENGINE DATA, crank inc);
        disp(abs((pmean - pbar)/pmean));
        REF CYCLE DATA = ISOTHERMAL DATA;
    elseif Model Code == 2
        % Solve the ideal adiabatic model
        ADIABATIC DATA = adiabatic (ENGINE DATA, crank inc);
        REF CYCLE DATA = ADIABATIC DATA;
    elseif Model Code == 3
        % Solve the simple model (no flow friction)
        SIMPLE DATA = simple(ENGINE DATA, crank inc);
        REF CYCLE DATA = SIMPLE DATA;
    else
        disp('ERROR: Invalid model code.')
    end
    % Find the mean pressure of the reference cycle
    pbar = mean([REF CYCLE DATA.p]);
end
```

Revised_Crank_Vol.m

```
% Crank Vol.m - Written by Connor Speer - February 2017
% This script calculates the volume variations for engines which use slider
% crank mechanisms.
% See page 162 in Cleghorn's second edition of "Mechanics of Machines".
% Edited by Connor Speer - September 2017
% Changed angle definitions in the gamma part to make them more clear for
thesis
% paper.
clear, clc, close all;
% Gamma Engines
% Gamma Engine Input Parameters
% Dr1 --> Displacer desaxe offset in [m]
% Dr2 --> Displacer crank length in [m]
% Dr3 --> Displacer connecting rod length in [m]
% Dbore --> Displacer bore in [m]
% Pr1 --> Piston desaxe offset in [m]369
% Pr2 --> Piston crank length in [m]
% Pr3 --> Piston connecting rod length in [m]
```

```
% Pbore --> Piston bore in [m]
% Vdead --> Total dead volume in [m^3]
% V crankcase max --> Maximum crankcase volume in [m^3]
\% beta deg --> Phase angle advance of displacer motion over piston motion
[degrees]
% Input Parameters for HTG Engine
Dr1 = 0; %[m]
Dr2 = 0.0375; %[m]
Dr3 = 0.130; %[m]
Dbore = 0.096; %[m]
Pr1 = 0; %[m]
Pr2 = 0.0375; %[m]
Pr3 = 0.156; %[m]
Pbore = 0.085; %[m]
Vdead = 579.09*1e-6; %[m^3]
V crankcase max = 0.0032; %[m^3]
beta deg = 90; %[degrees]
% Specify the crank angle range and increment
%*** Crank angle is zero when total volume is maximum for gamma engines
theta_deg = 0:5:360; %[degrees]
Ptheta2 = pi - theta deg*(pi/180); %[rad]
Dtheta2 = Ptheta2 - beta deg*(pi/180); %[rad]
% Working Space Volume Variations
Dr4max = sqrt(((Dr2+Dr3)^2) - (Dr1^2));
Dr4min = sqrt(((Dr3-Dr2)^{2})-(Dr1^{2}));
Dstroke = Dr4max - Dr4min;
Vswd = ((pi/4)*(Dbore^2))*Dstroke;
Pr4max = sqrt(((Pr2+Pr3)^2) - (Pr1^2));
Pr4min = sqrt(((Pr3-Pr2)^2)-(Pr1^2));
Pstroke = Pr4max - Pr4min;
Vswp = ((pi/4)*(Pbore^2))*Pstroke;
Dtheta3 = pi - asin((-Dr1+(Dr2*sin(Dtheta2)))/Dr3);
Dr4 = Dr2*cos(Dtheta2) - Dr3*cos(Dtheta3);
Ve = ((pi/4) * (Dbore^{2})) * (Dr4max-Dr4);
DVc = (((pi/4) * (Dbore^2)) * Dstroke) - Ve;
Ptheta3 = pi - asin((-Pr1+(Pr2*sin(Ptheta2)))/Pr3);
Pr4 = Pr2*cos(Ptheta2) - Pr3*cos(Ptheta3);
PVc = (((pi/4) * (Pbore^{2})) * (Pr4max-Pr4));
Vc = DVc + PVc;
Vtotal = Vdead + (((pi/4)*(Dbore^2))*2*Dr2) + PVc;
% Crankcase Volume Variations
V_crankcase = V_crankcase max - PVc;
% Sinusoidal Volume Variations for Comparison
theta = theta deg*(pi/180);
Ve sine = Vswd*0.5*(1+cos(theta+(beta deg*(pi/180))));
```

```
Vc sine = (Vswd-Ve sine) + Vswp*0.5*(1+cos(theta));
Vtotal sine = Vdead + Ve sine + Vc sine;
% % Crankcase Pressure Models
% SHR = 1.4; % Specific heat ratio of air.
% PO = 1000000; % Engine fill pressure in [Pa].
% T crankcase = 298; % Mean crankcase temperature in [K].
% R = 287; % Gas constant for air in [J/kgK].
% % Mean crankcase volume in [m^3].
% V0 = V crankcase max - 0.5*Pstroke*(((pi/4)*(Pbore^2)));
% % Mass of gas in the crankcase in [kg].
% m crankcase = (P0*V0)/(R*T crankcase);
8
% % Crankcase Pressure Assuming Adiabatic Compression and Expansion
% P crankcase adiabatic = P0.*((V0./V crankcase).^SHR); % Crankcase pressure
in [Pa].
% % Crankcase Pressure Assuming Isothermal Compression and Expansion
% P crankcase isothermal = (m crankcase*R*T crankcase)./V crankcase;
% figure
% hold on
% plot(theta deg, P crankcase adiabatic*1e-5)
% plot(theta deg, P crankcase isothermal*1e-5)
% hold off
% xlabel('Crank Angle [degrees]')
% ylabel('Crankcase Pressure [Pa]')
% legend('Adiabatic Crankcase', 'Isothermal Crankcase')
% % Alpha Engines
% % Alpha Engine Input Parameters
% % Cr1 --> Compression piston desaxe offset in [m]
% % Cr2 --> Compression piston crank length in [m]
% % Cr3 --> Compression piston connecting rod length in [m]
% % Cbore --> Compression piston bore in [m]
% % Er1 --> Expansion piston desaxe offset in [m]
% % Er2 --> Expansion piston crank length in [m]
\%~\%~{\rm Er3} --> Expansion piston connecting rod length in [m]
% % Ebore --> Expansion piston bore in [m]
% % Vdead --> Total dead volume in [m^3]
\% % V crankcase max --> Maximum crankcase volume in [m^3] (i.e. both pistons
% % at TDC. This may not be possible when assembled)
% % alpha deg --> Phase angle advance of expansion space over compression
space [degrees]
00
% % Made up numbers for testing
% Cr1 = 0; %[m]
% Cr2 = 0.0375; %[m]
% Cr3 = 0.156; %[m]
% Cbore = 0.085; %[m]
```

```
% Er1 = 0; %[m]
% Er2 = 0.0375; %[m]
% Er3 = 0.156; %[m]
% Ebore = 0.096; %[m]
% Vdead = 579.09*1e-6; %[m^3]
% V crankcase max = 0.0032; %[m^3]
% alpha deg = 90; %[degrees]
8
% % Specify the crank angle range and increment
% % *** Crank angle is zero when Vc is maximum for alpha engines
% % *** Be careful defining crank angle 0 for desaxe offset alphas
% theta deg = 0:5:360;
% theta = theta deg*(pi/180); %[rad]
2
% Ctheta2 = theta - pi;
% Etheta2 = Ctheta2 + alpha deg*(pi/180);
8
% % Working Space Volume Variations
% Cr4max = sqrt(((Cr2+Cr3)^2)-(Cr1^2));
% Cr4min = sqrt(((Cr3-Cr2)^2)-(Cr1^2));
% Cstroke = Cr4max - Cr4min;
% CVswept = ((pi/4)*(Cbore^2))*Cstroke;
2
% Er4max = sqrt(((Er2+Er3)^2)-(Er1^2));
% Er4min = sqrt(((Er3-Er2)^2)-(Er1^2));
% Estroke = Er4max - Er4min;
% EVswept = ((pi/4)*(Ebore^2))*Estroke;
2
% Ctheta3 = pi - asin((-Cr1+(Cr2*sin(Ctheta2)))/Cr3);
% Cr4 = Cr2*cos(Ctheta2) - Cr3*cos(Ctheta3);
% Vc = (((pi/4)*(Cbore^2))*(Cr4max-Cr4));
8
% Etheta3 = pi - asin((-Er1+(Er2*sin(Etheta2)))/Er3);
% Er4 = Er2*cos(Etheta2) - Er3*cos(Etheta3);
% Ve = (((pi/4)*(Ebore^2))*(Er4max-Er4));
2
% Vtotal = Vdead + Ve + Vc;
8
% % Crankcase Volume Variations
% V crankcase = V crankcase max - Vc - Ve;
00
% % Sinusoidal Volume Variations for Comparison
% Vc sine = CVswept*0.5*(1+cos(theta));
% Ve sine = EVswept*0.5*(1+cos(theta+(alpha deg*(pi/180))));
% Vtotal sine = Vdead + Ve sine + Vc sine;
% Plots
set(0, 'defaultfigurecolor', [1 1 1])
% % For Connor's Thesis Paper
% % Location of Figures
% x = 500;
% y = 500;
```

```
8
% % Size of Figures
% width = 550;
% height = 400;
8
% % Font For Figures
% font = 'Arial';
% font size = 11;
% Location of Figures
x = 500;
y = 500;
% Size of Figures
width = 326;
height = 275;
% Font For Figures
font = 'Arial';
font size = 11;
% % Location of Figures
% x = 500;
% y = 500;
8
% % Size of Figures
% width = 550;
% height = 400;
8
% % Font For Figures
% font = 'Times New Roman';
% font size = 16;
% To change line width for plots, say "'LineWidth',2".
% To include math symbols with their own font size and font type in the
% axes labels, do this:
% xlabel({'\fontsize{11} Engine Speed \fontsize{11} \fontname{Cambria Math}
\omega \fontsize{11} \fontname{Times New Roman} [RPM]'});
% Here is the degree symbol in case you need it °C. Alternatively, use
% \circ.
% Plot 1 - Total Working Space Volume as a Function of Crank Angle
figure('Position', [x y width height])
hold on
plot(theta deg, Vtotal, 'r', 'linewidth', 2)
plot(theta deg,Vtotal sine,'k','linewidth',2)
xlim([0 360])
hold off
```

```
xlabel('Crank Angle (\circ)', 'FontName', font, 'FontSize', font size)
ylabel('Total Workspace Volume (m^3)', 'FontName', font, 'FontSize', font size)
legend('Slider-Crank', 'Sinusoidal', 'Location', 'Southeast')
set(gca, 'fontsize', font size);
set(gca, 'FontName', font)
% Plot 2 - Piston Position as a Function of Crank Angle
figure('Position', [x y width height])
hold on
plot(theta deg, max(Vtotal)/((pi/4)*(Pbore^2)) -
Vtotal/((pi/4)*(Pbore^2)), 'r', 'linewidth', 2)
plot(theta deg,max(Vtotal sine)/((pi/4)*(Pbore^2)) -
Vtotal sine/((pi/4)*(Pbore^2)),'k','linewidth',2)
xlim([0 360])
hold off
xlabel('Crank Angle (\circ)', 'FontName', font, 'FontSize', font size)
ylabel('Piston Position (m)', 'FontName', font, 'FontSize', font size)
legend('Slider-Crank', 'Sinusoidal', 'Location', 'Northeast')
set(gca, 'fontsize', font size);
set(gca, 'FontName', font)
% Plot 3 - Displacer Position as a Function of Crank Angle
figure('Position', [x y width height])
hold on
plot(theta deg,max(Ve)/((pi/4)*(Dbore^2)) -
(Ve/((pi/4)*(Dbore^2))), 'r', 'linewidth', 2)
plot(theta deg,max(Ve sine)/((pi/4)*(Dbore^2)) -
(Ve sine/((pi/4)*(Dbore^2))), 'k', 'linewidth', 2)
xlim([0 360])
hold off
xlabel('Crank Angle (\circ)', 'FontName', font, 'FontSize', font size)
ylabel('Displacer Position (m)', 'FontName', font, 'FontSize', font size)
legend('Slider-Crank', 'Sinusoidal', 'Location', 'Northeast')
set(gca, 'fontsize', font size);
set(gca, 'FontName', font)
% figure('Position', [x y width height])
% plot(theta deg, V crankcase*1000)
% xlabel('Crank Angle [degrees]', 'FontName', font, 'FontSize', font size)
% ylabel('Crankcase Volume [L]','FontName',font,'FontSize',font size)
% % Plot 1 - Total Working Space Volume as a Function of Crank Angle
% figure('Position', [x y width height])
% hold on
% plot(theta deg, Vtotal*1000,'r','linewidth',2)
% plot(theta deg,Vtotal sine*1000,'k','linewidth',2)
% xlim([0 360])
% hold off
% xlabel('Crank Angle [\circ]', 'FontName', font, 'FontSize', font_size)
% ylabel('Total Workspace Volume [L]', 'FontName', font, 'FontSize', font_size)
% legend('Slider-Crank', 'Sinusoidal', 'Location', 'Southeast')
% set(gca, 'fontsize', font size);
% set(gca, 'FontName', font)
2
% % Plot 2 - Compression Piston Position as a Function of Crank Angle
% figure('Position', [x y width height])
```

```
% hold on
% plot(theta deg, max(Vc)/((pi/4)*(Cbore^2)) -
Vc/((pi/4)*(Cbore^2)), 'r', 'linewidth', 2)
% plot(theta deg,max(Vc sine)/((pi/4)*(Cbore^2)) -
Vc sine/((pi/4)*(Cbore<sup>2</sup>)),'k','linewidth',2)
% xlim([0 360])
% hold off
% xlabel('Crank Angle [\circ]', 'FontName', font, 'FontSize', font size)
% ylabel('Compression Piston Position
[m]', 'FontName', font, 'FontSize', font size)
% legend('Slider-Crank', 'Sinusoidal', 'Location', 'Northeast')
% set(gca,'fontsize',font size);
% set(gca, 'FontName', font)
0
% % Plot 3 - Expansion Piston Position as a Function of Crank Angle
% figure('Position', [x y width height])
% hold on
% plot(theta deg,max(Ve)/((pi/4)*(Ebore^2)) -
(Ve/((pi/4)*(Ebore^2))), 'r', 'linewidth', 2)
% plot(theta deg,max(Ve sine)/((pi/4)*(Ebore^2)) -
(Ve sine/((pi/4)*(Ebore^2))), 'k', 'linewidth', 2)
% xlim([0 360])
% hold off
% xlabel('Crank Angle [\circ]', 'FontName', font, 'FontSize', font size)
% ylabel('Expansion Piston Position
[m]', 'FontName', font, 'FontSize', font size)
% legend('Slider-Crank','Sinusoidal','Location','Northeast')
% set(gca,'fontsize',font size);
% set(gca, 'FontName', font)
00
% figure('Position', [x y width height])
% plot(theta deg, V crankcase*1000)
% xlabel('Crank Angle [degrees]', 'FontName', font, 'FontSize', font size)
% ylabel('Crankcase Volume [L]','FontName',font,'FontSize',font size)
```

Appendix D: MATLAB Source Code for Data Processing

General Data Processing Functions

Process_Data.m

```
function DATA STRUCTURE = Process Data(log file folder)
% Written by Connor Speer - October 2017
% Process experimental data and return it in a structure for plotting
% elsewhere.
% Calculate Correction Terms Using Calibration Data
Abs Val Cal Folder = 'X:\01 Current Students\Connor Speer\00 Thesis and
Journal Papers\00 Thesis\00 Data and Plots\Calibration Codes\Validyne
Calibration Oct. 22';
[ABS VAL FIT COEFFICIENTS]...
   = ABS VAL Correction Terms(Abs Val Cal Folder, 0);
Diff Val Cal Folder = 'X:\01 Current Students\Connor Speer\00 Thesis and
Journal Papers\00 Thesis\00 Data and Plots\Calibration Codes\Differential
Validyne Calibration Oct. 22';
[DIFF VAL FIT COEFFICIENTS]...
   = DIFF VAL Correction Terms (Diff Val Cal Folder, 0);
TC Cal Folder = 'X:\01 Current Students\Connor Speer\00 Thesis and Journal
Papers\00 Thesis\00 Data and Plots\Calibration Codes\Thermocouple Calibration
Oct. 22';
[TC FIT COEFFICIENTS]...
   = TC Correction Terms(TC Cal Folder, 0);
RTD Cal Folder = 'X:\01 Current Students\Connor Speer\00 Thesis and Journal
Papers\00 Thesis\00 Data and Plots\Calibration Codes\RTD Calibration Oct.
22';
[RTD FIT COEFFICIENTS]...
   - RTD Correction Terms(RTD_Cal_Folder, 0);
% Cooling System Input Parameters
V dot Cooler = 0.800*1.66667e-5; % Cooler water volume flow rate [m^3/s]
V dot ConPipePowCyl = 0.200*1.66667e-5; % Connecting Pipe and Power Cylinder
water volume flow rate [m^3/s]
c water = 4184; % Specific heat capacity of water in [J/kqK]
dens water = 1000; % Water density [kg/m^3]
```

```
% Calculations
m dot Cooler = V dot Cooler*dens water; % Cooler water mass flow rate [kg/s]
m dot ConPipePowCyl = V dot ConPipePowCyl*dens water; % Connecting Pipe water
mass flow rate [kg/s]
% Collect all the log file names from the test data folder
log files info = dir(fullfile(log file folder, '*.log'));
%% Preallocate space for the structure array
DATA_STRUCTURE(length(log_files_info)/3).filename = [];
DATA_STRUCTURE(length(log_files_info)/3).Filename_Hz = [];
DATA STRUCTURE(length(log files info)/3).Filename P shaft = [];
DATA STRUCTURE(length(log files info)/3).time TC = [];
DATA STRUCTURE(length(log files info)/3).time RTD = [];
DATA STRUCTURE(length(log files info)/3).time Volt = [];
DATA STRUCTURE (length (log files info) / 3).theta deg = [];
DATA_STRUCTURE(length(log_files_info)/3).T_0 = [];
DATA_STRUCTURE(length(log_files_info)/3).T 1 = [];
DATA STRUCTURE(length(log files info)/3).T 2 = [];
DATA STRUCTURE(length(log files info)/3).T 3 = [];
DATA STRUCTURE(length(log files info)/3).T 4 = [];
DATA STRUCTURE(length(log files info)/3).T 5 = [];
DATA STRUCTURE(length(log files info)/3).T 6 = [];
DATA STRUCTURE(length(log files info)/3).RTD 0 = [];
DATA STRUCTURE(length(log files info)/3).RTD 1 = [];
DATA STRUCTURE (length (log files info) / 3) .RTD 2 = [];
DATA STRUCTURE(length(log files info)/3).RTD 3 = [];
DATA STRUCTURE(length(log files info)/3).P1 Pa = [];
DATA STRUCTURE(length(log files info)/3).P2 Pa = [];
DATA_STRUCTURE(length(log_files_info)/3).P3_Pa = [];
DATA_STRUCTURE(length(log_files_info)/3).P4_Pa = [];
DATA STRUCTURE(length(log files info)/3).P5 Pa = [];
DATA STRUCTURE(length(log files info)/3).A = [];
DATA STRUCTURE(length(log files info)/3).Z = [];
DATA STRUCTURE(length(log files info)/3).TOR = [];
DATA STRUCTURE(length(log files info)/3).pmean = [];
DATA STRUCTURE (length (log files info) /3).Cap Setpoint = [];
DATA STRUCTURE (length (log files info) /3).Bath Setpoint = [];
DATA STRUCTURE(length(log files info)/3).Tge = [];
DATA STRUCTURE (length (log files info) / 3).Tgc = [];
DATA_STRUCTURE(length(log files info)/3).Tgk = [];
DATA STRUCTURE(length(log files info)/3).Tgh = [];
DATA STRUCTURE (length (log files info)/3).T cooler inlet = [];
DATA_STRUCTURE(length(log_files_info)/3).T_cooler_outlet = [];
DATA STRUCTURE(length(log files info)/3).Torque avg = [];
DATA STRUCTURE(length(log files info)/3).Engine RPM = [];
DATA STRUCTURE (length (log files info) / 3) . Engine Hz = [];
DATA STRUCTURE(length(log files info)/3).P shaft = [];
DATA STRUCTURE (length (log files info) / 3). P ind Validyne = [];
DATA STRUCTURE(length(log files info)/3).P ind PCB = [];
DATA_STRUCTURE(length(log_files_info)/3).N_Beale = [];
DATA STRUCTURE(length(log files info)/3).N West = [];
DATA STRUCTURE (length (log files info) / 3) .N T = [];
DATA STRUCTURE (length (log files info) /3).Qdot Cooler = [];
DATA STRUCTURE (length (log files info) /3).Qdot ConPipePowCyl = [];
```

```
DATA STRUCTURE(length(log files info)/3).Error isothermal = [];
DATA STRUCTURE (length (log files info)/3).Loss Factor isothermal = [];
DATA_STRUCTURE(length(log_files_info)/3).Error_adiabatic = [];
DATA STRUCTURE (length (log files info) /3). Power adiabatic = [];
DATA STRUCTURE(length(log files info)/3).P GSH Loss Validyne = [];
DATA STRUCTURE (length (log files info) / 3).P GSH Loss PCB = [];
DATA STRUCTURE(length(log files info)/3).Exp FW = [];
DATA STRUCTURE (length (log files info) /3). Tdrop Cap to Expansion Space = [];
DATA STRUCTURE (length (log files info) / 3).P 2nd order = [];
DATA_STRUCTURE(length(log_files_info)/3).Q_dot_in_2nd_order = [];
DATA_STRUCTURE(length(log_files_info)/3).Q_dot_rej_2nd_order = [];
DATA STRUCTURE (length (log files info) /3).eff thermal 2nd order = [];
DATA STRUCTURE (length (log files info)/3).Vtotal rounded = [];
DATA STRUCTURE(length(log files info)/3).Vtotal = [];
DATA STRUCTURE(length(log files info)/3).p engine experimental = [];
DATA STRUCTURE(length(log files info)/3).p engine isothermal = [];
DATA_STRUCTURE(length(log_files_info)/3).p_engine_adiabatic = [];
DATA STRUCTURE(length(log files info)/3).p buffer experimental = [];
DATA STRUCTURE (length (log files info)/3).p buffer isothermal = [];
DATA STRUCTURE(length(log files info)/3).p buffer adiabatic = [];
DATA STRUCTURE (length (log files info)/3).pdrop regen experimental = [];
DATA STRUCTURE (length (log files info)/3).pdrop regen model = [];
DATA STRUCTURE(length(log_files_info)/3).T_crankcase = [];
DATA_STRUCTURE(length(log_files_info)/3).Q_dot_in = [];
DATA_STRUCTURE(length(log_files_info)/3).eff thermal = [];
DATA STRUCTURE (length (log files info)/3).Conduction Loss Model = [];
DATA STRUCTURE (length (log files info) /3).P lost regen FF = [];
DATA STRUCTURE (length (log files info) /3).P lost regen FF model = [];
% Initialize counter variable
counter = 1;
counter max = (1/3) *length(log files info);
WaitBar = waitbar(0, 'Processing experimental data ...');
%% Open triplets of log files
for i = 1:3:length(log files info)
    % Open the RTD log file.
    filename RTD = strcat(log file folder,'\',log files info(i).name);
    [RTD 0,RTD 1,RTD 2,RTD 3] = importfile RTD(filename RTD);
00
      RTD 0 --> Cooler water inlet
8
      RTD 1 --> Cooler water outlet
8
      RTD 2 --> Con Pipe/Pow Cyl inlet
8
      RTD 3 --> Con Pipe/Pow Cyl outlet
    % Open the thermocouple log file.
    filename TC = strcat(log file folder,'\',log files info(i+1).name);
    [T 0,T 1,T 2,T 3,T 4,T 5,T 6,T 7,T 8,T 9,T 10,T 11,T 12,T 13] = ...
    importfile TC(filename TC);
8
     T 0 --> Expansion Space
%
     T 1 --> HH-Regen
9
     T 2 --> HH Flange - Bypass Side
8
     T 3 --> HH Flange - Power Piston Side
8
     T 4 --> Displacer Mount
     T 5 --> Crankcase
8
```

```
% T 6 --> Power Piston
```

```
% Open the voltage log file.
    filename Volt = strcat(log file folder, '\', log files info(i+2).name);
    [A,Z,TOR,P1,P2,P3,P4,P5] = importfile P(filename Volt);
     A --> 500 PPR Rotary Encoder Output
9
8
      Z --> 1 PPR Rotary Encoder Output
8
      TOR --> Torque Transducer Output
8
     P1 --> Validyne Regenerator Differential Pressure
8
     P2 --> Validyne Power Cylinder
8
    P3 --> Validyne Crankcase
8
    P4 --> PCB Power Cylinder
00
     P5 --> PCB Crankcase
    %% Apply Calibration
    RTD 0 = calibrate RTD(0,RTD 0,RTD FIT COEFFICIENTS); %(deg C)
    RTD 1 = calibrate RTD(1,RTD 1,RTD FIT COEFFICIENTS); % (deg C)
    RTD_2 = calibrate_RTD(2,RTD_2,RTD_FIT_COEFFICIENTS); %(deg C)
    RTD 3 = calibrate RTD(3,RTD 3,RTD FIT COEFFICIENTS); % (deg C)
    % Don't adjust first two thermocouples because calibration data range
    % is too low, and extrpolating it will lead to more error.
      T_0 = calibrate_TC(0,T_0_raw,TC_FIT_COEFFICIENTS); %(deg C)
00
2
    T 1 = calibrate TC(1,T 1 raw,TC FIT COEFFICIENTS); %(deg C)
    T 2 = calibrate TC(2,T 2,TC FIT COEFFICIENTS); %(deg C)
    T 3 = calibrate TC(3,T 3,TC FIT COEFFICIENTS); %(deg C)
    T_4 = calibrate_TC(4,T_4,TC_FIT_COEFFICIENTS); %(deg C)
T_5 = calibrate_TC(5,T_5,TC_FIT_COEFFICIENTS); %(deg C)
    T 6 = calibrate TC(6,T 6,TC FIT COEFFICIENTS); %(deg C)
    P1 Pa raw = P1*0.5*6894.76; %(Pa)
    P1 Pa = calibrate diff VAL(1,P1 Pa raw, DIFF VAL FIT COEFFICIENTS); %(Pa)
    P2 Pa raw = P2*20*6894.76; %(Pa)
    P3 Pa raw = P3*20*6894.76;  %(Pa)
    P2 Pa = calibrate abs VAL(2, P2 Pa raw, ABS VAL FIT COEFFICIENTS);
    P3 Pa = calibrate abs VAL(3,P3 Pa raw,ABS VAL FIT COEFFICIENTS);
    % Calculate mean pressure from the Validyne transducers
    pmean = mean(P2_Pa); %[Pa]
    [P4, P5] = PCB Pressure Calibration(P4.*0.5, P5.*0.5);
    P4 Pa = mean(P\overline{2} Pa) + P\overline{4}; % PCB Power Cylinder
    P5 Pa = mean(P3 Pa) + P5; % PCB Crankcase
    TOR = Futek Torque Calibration(TOR);
    Torque avg = mean(TOR); %[Nm]
    %% Collect the Start and End Times of the voltage log file
    volt log file = fileread(filename Volt);
    start index = regexp(volt log file, 'Start');
    end_index = regexp(volt_log_file,'End');
    start line = volt log file(start index:end index-1);
    end line = volt log file(end index:end index+14);
    [token start, remain start] = strtok(start line);
```

```
[token end, remain end] = strtok(end line);
    start time = str2double(strip(remain start));
    end time = str2double(strip(remain end));
    % Time for voltages
    time inc Volt = (end time-start time)/length(A);
    N Volt = length(A);
    time Volt = (0:N Volt-1)*time inc Volt;
    time Volt = time Volt(:);
    % Time for thermocouples
    time inc TC = (end time-start time)/length(T 0);
    N TC = length(T 0);
    time TC = (0:N TC-1)*time inc TC;
    time TC = time TC(:);
    % Time for RTDs
    time inc RTD = (end time-start time)/length(RTD 0);
    N RTD = length(RTD 0);
    time RTD = (0:N RTD-1)*time inc RTD;
    time RTD = time RTD(:);
    %% Record Data from the name
    % Heater Cap Temperature Setpoint
    [token1, remain1] = strtok(log files info(i).name, 'TH ');
    Cap Setpoint = str2double(token1); \frac{1}{8}[deq C]
    % Coolant Water Bath Setpoint
    [token3,remain3] = strtok(log files_info(i).name,'TC');
    [token4, remain4] = strtok(remain3, ' ');
    token5 = strtok(remain4, ' ');
    Bath Setpoint = str2double(token5); %[deg C]
    % Engine Speed
    [token6, remain6] = strtok(log files info(i).name, 'D');
    [token7, remain7] = strtok(remain6, 'D');
    [token8, remain8] = strtok(remain7, ' ');
    [token9,remain9] = strtok(remain8, '');
    Filename_RPM = str2double(token9); %[RPM]
    Filename Hz = Filename RPM/60; %[Hz]
    %% Calculate Data from the file
8
     % Convert pressures and average pressures into units of Pa
8
     p scale1 = 0.5*0.0689476*100000; % (1V = 0.5 PSI)
8
     p scale2 = 20*0.0689476*100000; % (1V = 20 PSI)
8
     p scale3 = (1/0.024)*0.0689476*100000*0.5; % 24 mV/PSI, Gain = 2
8
00
     P1 Pa = P1.*p scale1; % Regenerator Differential Validyne
00
00
      P2 Pa = P2.*p scale2; % Validyne Power Cylinder
00
      P3 Pa = P3.*p scale2; % Validyne Crankcase
8
8
      % Calculate mean pressure from Validyne transducers
8
      pmean = mean(P2 Pa); %[Pa]
8
```

```
327
```

```
P4_Pa = mean(P2_Pa) + P4.*p scale3; % PCB Power Cylinder
0
8
      P5 Pa = mean(P3 Pa) + P5.*p scale3; % PCB Crankcase
    % Calculate average expansion space gas temperature
    Tge = mean(T 0); %[deg C]
    % Calculate average compression space gas temperature
    Tgc = (mean(T 6) + mean(T 4))/2; % [deg C]
    % Calculate average Cooler Inlet Water Temperature
    T cooler inlet = mean(RTD 0); %[deg C]
    % Calculate average Cooler Outlet Water Temperature
    T cooler outlet = mean(RTD 1); %[deg C]
      % Calculate average torque
8
2
     Torque avg = mean(TOR) *2; %[Nm]
    % Calculate crank angles
    [theta_deg] = Encoder_2_Angle(A,Z); %[deg]
    theta = theta deg*(pi/180); % [rad]
    % Calculate Average Crankshaft Speed
    refs = find(A < 0.5);
    % Initialize variables
   pulse count = 0;
    for inc = 1:(length(refs)-1)
        if refs(inc+1) ~= (refs(inc) + 1)
            pulse count = pulse count + 1;
        end
    end
    Engine Ang Freq = ((pulse count/(end time-start time))/500)*(2*pi); %
[rad/sec]
    Engine Hz = Engine Ang Freq/(2*pi); %[Hz]
    Engine RPM = Engine Ang Freq*(60/(2*pi)); % [rev/min]
    % Calculate the engine power output
    P shaft = Torque avg*Engine Ang Freq; %[W]
    % Calculate the engine power output using the speed in the filename
    % (for efficiency data files)
    Filename P shaft = Torque avg*Filename Hz*2*pi; %[W]
    % Calculate the heat input
   Num Samples On = sum(P1 > 6.99);
    Num Samples Total = length(P1);
    OnFraction = Num Samples On/Num Samples Total;
    Q dot in = OnFraction*3290.958; %(W)
    % Calculate the engine thermal efficiency
    eff thermal = Filename P shaft/Q dot in;
```

```
% Calculate the Beale number
    VsweptPP = (426)*1e-6; % Power Piston swept volume in [m^3]
    N Beale = P shaft/((pmean)*(Engine Ang Freq/(2*pi))*VsweptPP);
    % Calculate the West Number
    T \text{ factor} = (Tge+Tgc) / (Tge-Tgc);
    N West = N Beale*T factor;
    % Calculate the Characteristic Temperature Ratio
    N T = Cap Setpoint/Bath Setpoint;
    % Average the Crank Angles and Pressures
    [P1 avg Pa] = PV data avg(theta, P1 Pa);
    [P2 avg Pa] = PV data avg(theta, P2 Pa);
    [P3 avg Pa] = PV data avg(theta, P3 Pa);
    [P4 avg Pa] = PV data avg(theta, P4 Pa);
    [P5 avg Pa] = PV data avg(theta,P5 Pa);
    % Calculate volumes at rounded crank angles to go with average pressures
    %% Use crank angles to calculate volumes
    % Input Parameters for HTG Engine
    Vdead = 876.79*1e-6 - 132*1e-6; %[m^3] (With DV Reduction Parts)
    ENGINE DATA = HTG ENGINE DATA;
    ENGINE DATA.Pbore = 0.044; %[m]
    theta deg rounded = 0:1:359;
    theta rounded = theta deg rounded* (pi/180);
    theta rounded = theta rounded(:);
    [Vc rounded, Ve rounded, dVc rounded, dVe rounded] = volume(theta rounded,
ENGINE DATA);
    [Vc, Ve, dVc, dVe] = volume (theta, ENGINE DATA);
    % Calculate Volumes
    Vtotal rounded = Vdead + Vc rounded + Ve rounded;
    Vtotal rounded = Vtotal rounded(:);
    Vtotal = Vdead + Vc + Ve;
    Vtotal = Vtotal(:);
    % Crankcase Volume Variations
    Pbore = ENGINE DATA.Pbore; % piston bore [m]
    Pr1 = ENGINE DATA.Pr1; % piston desaxe offset in [m]
    Pr2 = ENGINE DATA.Pr2; % piston crank radius in [m]
    Pr3 = ENGINE DATA.Pr3; % piston connecting rod length [m]
    Ptheta2 = pi - theta_rounded;
    Ptheta3 = pi - asin((-Pr1+(Pr2*sin(Ptheta2)))/Pr3);
    Pr4 = Pr2*cos(Ptheta2) - Pr3*cos(Ptheta3);
    Pr4max = sqrt(((Pr2+Pr3)^2)-(Pr1^2));
    % Crankcase Volume Variations in (m^3)
```

```
V crankcase rounded = ENGINE DATA.V buffer max - ((Pr4max-
Pr4)*(((pi/4)*(Pbore^2)))); %(m^3)
   V crankcase rounded = V crankcase rounded(:);
    % Buffer Pressure Models
    R = 287; % Ideal gas constant for air in (J/kgK)
    gamma = 1.4; % Specific heat ratio for air.
    p0 = mean(P3 Pa); % Mean crankcase pressure in (Pa).
    V0 = mean(V crankcase rounded); % Mean crankcase volume in (m^3).
    T crankcase = mean(T 5) + 273.15; % Mean crankcase temperature in [K].
   m crankcase = (p0*V0)/(R*T crankcase); % Mass of gas in the crankcase in
[kg].
   p buffer isothermal = (m crankcase*R*T crankcase)./V crankcase rounded;
%(Pa)
   p_buffer_isothermal = p_buffer_isothermal(1:360);
   p buffer adiabatic = p0.*((V0./V crankcase rounded).^qamma); %(Pa)
   p buffer adiabatic = p buffer adiabatic(1:360);
    % Calculate the work lost to regenerator flow friction
    dW regen FF = P1 avg Pa.*(pi/4).*(0.096.^2).*dVe rounded; %[J]
    W lost regen FF = sum(dW regen FF); %[J]
    P lost regen FF = W lost regen FF*Engine Hz; %[W]
    % Calculate Experimental Indicated Work and Power in the Compression
    % Space according to Validynes
    W ind Validyne = polyarea(Vtotal rounded, P2 avg Pa); %[J]
    P ind Validyne = W ind Validyne*Engine Hz; %[W]
    % Calculate Experimental Indicated Work and Power in the Compression
    % Space according to PCB
    W ind PCB = polyarea(Vtotal rounded, P4 avg Pa); %[J]
    P ind PCB = W ind PCB*Engine Hz; %[W]
    % Calculate Crankcase Gas Spring Hysteresis Loss according to Validyne
    W GSH Loss Validyne = polyarea(Vtotal rounded,P3 avq Pa); %[J]
    P GSH Loss Validyne = W GSH Loss Validyne*Engine Hz; %[W]
    % Calculate Crankcase Gas Spring Hysteresis Loss according to PCB
    W GSH Loss PCB = polyarea(Vtotal rounded, P5 avg Pa); %[J]
    P GSH Loss PCB = W GSH Loss PCB*Engine Hz; %[W]
    % Calculate the rate of heat removed by the cooling system
    Qdot Cooler = m dot Cooler*c water*(mean(RTD 1)-mean(RTD 0)); %[W]
    Qdot ConPipePowCyl = m dot ConPipePowCyl*c water*(mean(RTD 3)-
mean(RTD 2)); %[W]
    %% Calculate the Ideal Isothermal Model Indicated power
    ENGINE DATA = HTG ENGINE DATA;
    crank inc = 1; %[deg]
   Model Code = 1; % Ideal isothermal model
    Losses Code = 0; % No loss calculations
```

part traj on off = 0; % No particle trajectory calculations

```
\% Change operating conditions of the engine data structure to match the
% current data set
ENGINE DATA.Tgk = (((mean(T 2)+mean(T 3))/2)+mean(T 4))/2 + 273.15; %[K]
ENGINE DATA.Tgh = (mean(T 0)+mean(T 1))/2 + 273.15; %[K]
ENGINE DATA.Twk = Bath Setpoint + 273.15; %[K]
ENGINE DATA.Twh = Cap Setpoint + 273.15; %[K]
ENGINE DATA.Tgc = (mean(T 6)+mean(T 4))/2 + 273.15; %[K]
ENGINE DATA.Tge = mean(T 0) + 273.15; %[K]
ENGINE DATA.pmean = pmean; %[Pa]
[ISOTHERMAL DATA, \sim, \sim] = ...
    sea(ENGINE DATA, crank inc, Model Code, Losses Code, part traj on off);
p engine isothermal = [ISOTHERMAL DATA.p]; %(Pa)
p_engine_isothermal = p_engine_isothermal(1:360);
W ind isothermal = ISOTHERMAL DATA(end).W; %(J)
P ind isothermal = W ind isothermal*Engine Hz; %(W)
% Calculate the ideal isothermal model Error in Predicting Indicated
% Work
Error isothermal = ((W ind isothermal-W ind PCB)/W ind PCB) *100;  (
% Calculate the ideal isothermal model loss factor
Loss Factor isothermal = P shaft/P ind isothermal;
%% Calculate the Ideal Adiabatic Model Indicated Power
ENGINE DATA = HTG ENGINE DATA;
crank inc = 1; %[deg]
Model Code = 2; % Ideal adiabatic model
Losses Code = 0; % HTG specific loss calculations
part traj on off = 0; % No particle trajectory calculations
% Change operating conditions of the engine data structure to match the
% current data set
ENGINE_DATA.Tgk = (((mean(T_2)+mean(T_3))/2)+mean(T_4))/2 + 273.15; %[K]
ENGINE DATA.Tgh = (mean(T 0)+mean(T 1))/2 + 273.15; %[K]
ENGINE DATA.Twk = Bath Setpoint + 273.15; %[K]
ENGINE DATA.Twh = Cap Setpoint + 273.15; %[K]
ENGINE DATA.Tgc = (mean(T 6)+mean(T 4))/2 + 273.15; %[K]
ENGINE DATA.Tge = mean(T 0) + 273.15; %[K]
ENGINE DATA.pmean = pmean; %[Pa]
[ADIABATIC DATA, \sim, \sim] = ...
    sea(ENGINE DATA, crank inc, Model Code, Losses Code, part traj on off);
p engine adiabatic = [ADIABATIC DATA.p]; %(Pa)
```

```
p engine adiabatic = p engine adiabatic(1:360);
    W ind adiabatic = ADIABATIC DATA(end).W; %(J)
    Power adiabatic = ADIABATIC DATA(end).W*Engine Hz; % (W)
    % Calculate the ideal adiabatic Model Error in Predicting Indicated
    % Work
   Error adiabatic = ((W ind adiabatic-W ind PCB)/W ind PCB)*100;
    %% Calculate the Second Order Model Results
    ENGINE DATA = HTG ENGINE DATA;
    % Change operating conditions of the engine data structure to match the
    % current data set
    ENGINE DATA.Tqk = (((mean(T 2)+mean(T 3))/2)+mean(T 4))/2 + 273.15; %[K]
    ENGINE DATA.Tgh = (mean(T 0)+mean(T 1))/2 + 273.15; %[K]
8
     ENGINE DATA.Twk = Bath Setpoint + 273.15; %[K]
8
     ENGINE DATA.Twh = Cap Setpoint + 273.15; %[K]
    ENGINE_DATA.Twk = ((mean(T_2)+mean(T_3))/2) + 273.15; %[K]
    ENGINE DATA.Twh = mean(T 1) + 273.15; %[K]
    ENGINE DATA.Tgc = mean(T 4) + 273.15; %[K]
    ENGINE DATA.Tge = mean(T 0) + 273.15; %[K]
    ENGINE DATA.Pbore = 0.044; %[m]
    ENGINE DATA.Vclp = 1.733e-04 - 0.000132; %[m^3]
    ENGINE DATA.pmean = pmean; %[Pa]
    ENGINE DATA.V buffer max = 0.0032 + 0.004633333; %[m^3]
    ENGINE DATA.GSH config = 4; % All mods
   ENGINE DATA.freq = Engine Hz; %[Hz] for power data
8
     ENGINE DATA.freq = Filename Hz; %[Hz] for efficiency data
    [SECOND ORDER DATA,~,LOSSES DATA] = HTG 2nd Order (ENGINE DATA);
    Conduction Loss Model = LOSSES DATA.Q cond; %[W]
    pdrop regen model = LOSSES DATA.pdropr; %[Pa]
   pdrop regen model = pdrop regen model(1:360)';
    %% Calculate Experimental Forced Work according to Validynes
    P engine exp = P2 avg Pa; %[Pa]
    P buffer exp = P3 avg Pa; %[Pa]
    % Call forced work subfunction
    [FW W ind, Exp FW, FW W shaft] =
FW Subfunction v3(theta rounded, P engine exp, P buffer exp, Vtotal rounded, 0.7,
0);
```

```
% Temperature Drop Between Heating Cap and Expansion Space Gas
Tdrop Cap to Expansion Space = Cap Setpoint - Tge; %[degC]
```

```
%% Store the data in a structure
    DATA STRUCTURE (counter).filename = log files info(i).name;
    DATA STRUCTURE (counter). Filename Hz = Filename Hz;
    DATA STRUCTURE (counter). Filename P shaft = Filename P shaft;
    DATA STRUCTURE (counter).time TC = time TC;
    DATA_STRUCTURE (counter).time RTD = time RTD;
    DATA STRUCTURE (counter).time Volt = time Volt;
    DATA STRUCTURE (counter).theta deg = theta deg;
    DATA STRUCTURE (counter). T = T = 0;
    DATA STRUCTURE (counter).T 1 = T 1;
    DATA STRUCTURE (counter) .T^2 = T^2;
    DATA_STRUCTURE (counter).T_3 = T_
                                     3;
    DATA_STRUCTURE (counter).T_4 = T_4;
    DATA STRUCTURE (counter).T 5 = T 5;
    DATA STRUCTURE (counter).T 6 = T 6;
    DATA STRUCTURE (counter). RTD 0 = RTD 0;
    DATA STRUCTURE (counter).RTD 1 = RTD 1;
    DATA STRUCTURE (counter).RTD 2 = RTD 2;
    DATA STRUCTURE (counter).RTD 3 = RTD 3;
    DATA_STRUCTURE (counter) .P1_Pa = P1_Pa;
    DATA STRUCTURE (counter).P2 Pa = P2 Pa;
    DATA STRUCTURE (counter).P3 Pa = P3 Pa;
    DATA STRUCTURE (counter). P4 Pa = P4 Pa;
    DATA STRUCTURE (counter).P5 Pa = P5 Pa;
    DATA STRUCTURE (counter) .A = A;
    DATA STRUCTURE (counter).Z = Z;
    DATA STRUCTURE (counter).TOR = TOR.*2;
    DATA STRUCTURE (counter).pmean = pmean;
    DATA STRUCTURE (counter). Cap Setpoint = Cap Setpoint;
    DATA STRUCTURE (counter).Bath Setpoint = Bath Setpoint;
    DATA STRUCTURE (counter). Tge = Tge;
    DATA STRUCTURE (counter).Tgc = Tgc;
    DATA STRUCTURE (counter). Tgk = (((mean(T 2)+mean(T 3))/2)+mean(T 4))/2;
    DATA STRUCTURE (counter).Tgh = (mean(T 0)+mean(T 1))/2;
    DATA STRUCTURE (counter).T cooler inlet = T cooler inlet;
    DATA STRUCTURE (counter). T cooler outlet = T cooler outlet;
    DATA STRUCTURE (counter).Torque avg = Torque avg;
    DATA STRUCTURE (counter) . Engine RPM = Engine RPM;
    DATA STRUCTURE (counter). Engine Hz = Engine Hz;
    DATA_STRUCTURE(counter).P_shaft = P_shaft;
    DATA_STRUCTURE(counter).P_ind_Validyne = P_ind_Validyne;
    DATA STRUCTURE (counter). P ind PCB = P ind PCB;
    DATA STRUCTURE (counter) . N Beale = N Beale;
    DATA STRUCTURE (counter) .N West = N West;
    DATA STRUCTURE (counter) .N T = N T;
    DATA STRUCTURE (counter).Qdot Cooler = Qdot Cooler;
    DATA STRUCTURE(counter).Qdot ConPipePowCyl = Qdot ConPipePowCyl;
    DATA STRUCTURE (counter).Error isothermal = Error isothermal;
    DATA STRUCTURE(counter).Loss Factor isothermal = Loss Factor isothermal;
    DATA STRUCTURE (counter). Error adiabatic = Error adiabatic;
    DATA_STRUCTURE(counter).Power_adiabatic = Power adiabatic;
    DATA STRUCTURE(counter).P GSH Loss Validyne = P GSH Loss Validyne;
    DATA STRUCTURE (counter).P GSH Loss PCB = P GSH Loss PCB;
    DATA STRUCTURE (counter). Exp FW = Exp FW;
    DATA STRUCTURE (counter). Tdrop Cap to Expansion Space =
Tdrop Cap to Expansion Space;
```

```
DATA STRUCTURE (counter).P 2nd order = SECOND ORDER DATA.W dot;
    DATA STRUCTURE (counter).Q dot in 2nd order = SECOND ORDER DATA.Qh dot;
    DATA_STRUCTURE (counter).Q_dot rej 2nd order = SECOND ORDER DATA.Qk dot;
    DATA STRUCTURE (counter).eff thermal 2nd order =
SECOND ORDER DATA.eff thermal;
    DATA STRUCTURE (counter).Vtotal rounded = Vtotal rounded;
    DATA STRUCTURE (counter).Vtotal = Vtotal;
    DATA STRUCTURE (counter).p engine experimental = P4 avg Pa;
    DATA STRUCTURE (counter).p engine isothermal = p engine isothermal';
    DATA_STRUCTURE(counter).p_engine_adiabatic = p_engine_adiabatic';
    DATA STRUCTURE (counter).p buffer experimental = P5 avg Pa;
    DATA STRUCTURE(counter).p buffer isothermal = p buffer isothermal;
    DATA STRUCTURE(counter).p buffer adiabatic = p buffer adiabatic;
    DATA STRUCTURE (counter).pdrop regen experimental = P1 avg Pa;
    DATA STRUCTURE (counter).pdrop regen model = pdrop regen model;
    DATA STRUCTURE (counter).T crankcase = mean (T 5);
    DATA STRUCTURE (counter).Q dot in = Q dot in;
    DATA STRUCTURE (counter).eff thermal = eff thermal;
    DATA STRUCTURE (counter).Conduction Loss Model = Conduction Loss Model;
    DATA STRUCTURE (counter). P lost regen FF = P lost regen FF;
    DATA STRUCTURE (counter).P lost regen FF model = LOSSES_DATA.P_flow_r;
8[W]
    counter = counter + 1;
    % Update Wait Bar
    waitbar(counter / counter max)
```

```
end
```

```
close(WaitBar)
```

importfile_P.m

```
function [A1,Z1,TOR1,P1,P2,P3,P4,P5] = importfile P(filename, startRow,
endRow)
%IMPORTFILE Import numeric data from a text file as column vectors.
2
    [A1,Z1,TOR1,P6,P7,P8,P9,P10] = IMPORTFILE(FILENAME) Reads data from
0
    text file FILENAME for the default selection.
0
8
   [A1,Z1,TOR1,P6,P7,P8,P9,P10] = IMPORTFILE (FILENAME, STARTROW, ENDROW)
8
  Reads data from rows STARTROW through ENDROW of text file FILENAME.
0
% Example:
% [A1,Z1,TOR1,P6,P7,P8,P9,P10] =
importfile('TH 250 TC 21 P 60 44mm 0 Volt.log', 6, 300005);
00
8
     See also TEXTSCAN.
% Auto-generated by MATLAB on 2017/10/24 14:52:10
%% Initialize variables.
delimiter = ' \ t';
if nargin<=2</pre>
    startRow = 6;
```

```
endRow = inf;
end
%% Format for each line of text:
% column1: double (%f)
8
   column2: double (%f)
8
   column3: double (%f)
  column4: double (%f)
2
% column5: double (%f)
% column6: double (%f)
  column7: double (%f)
2
% column8: double (%f)
% For more information, see the TEXTSCAN documentation.
%% Open the text file.
fileID = fopen(filename, 'r');
%% Read columns of data according to the format.
% This call is based on the structure of the file used to generate this
% code. If an error occurs for a different file, try regenerating the code
% from the Import Tool.
dataArray = textscan(fileID, formatSpec, endRow(1)-startRow(1)+1,
'Delimiter', delimiter, 'TextType', 'string', 'EmptyValue', NaN,
'HeaderLines', startRow(1)-1, 'ReturnOnError', false, 'EndOfLine', '\r\n');
for block=2:length(startRow)
    frewind(fileID);
    dataArrayBlock = textscan(fileID, formatSpec, endRow(block) -
startRow(block)+1, 'Delimiter', delimiter, 'TextType', 'string',
'EmptyValue', NaN, 'HeaderLines', startRow(block)-1, 'ReturnOnError', false,
'EndOfLine', '\r\n');
    for col=1:length(dataArray)
        dataArray{col} = [dataArray{col};dataArrayBlock{col}];
    end
end
%% Close the text file.
fclose(fileID);
%% Post processing for unimportable data.
% No unimportable data rules were applied during the import, so no post
% processing code is included. To generate code which works for
% unimportable data, select unimportable cells in a file and regenerate the
% script.
%% Allocate imported array to column variable names
A1 = dataArray{:, 1};
Z1 = dataArray{:, 2};
TOR1 = dataArray{:, 3};
P1 = dataArray{:, 4};
P2 = dataArray{:, 5};
P3 = dataArray{:, 6};
P4 = dataArray{:, 7};
P5 = dataArray{:, 8};
```

importfile_RTD.m

```
function [RTD 0,RTD 1,RTD 2,RTD 3] = importfile RTD(filename, startRow,
endRow)
%IMPORTFILE Import numeric data from a text file as column vectors.
   [RTD 0,RTD 1,RTD 2,RTD 3] = IMPORTFILE(FILENAME) Reads data from text
    file FILENAME for the default selection.
8
8
8
   [RTD 0, RTD 1, RTD 2, RTD 3] = IMPORTFILE (FILENAME, STARTROW, ENDROW)
0
   Reads data from rows STARTROW through ENDROW of text file FILENAME.
00
% Example:
8
    [RTD 0,RTD 1,RTD 2,RTD 3] =
importfile('TH 250 TC 21 P 60 44mm 0 RTD.log', 6, 1005);
8
8
     See also TEXTSCAN.
% Auto-generated by MATLAB on 2017/10/24 14:46:26
%% Initialize variables.
delimiter = ' \setminus t';
if nargin<=2</pre>
    startRow = 6;
    endRow = inf;
end
%% Format for each line of text:
% column1: double (%f)
% column2: double (%f)
2
   column3: double (%f)
2
   column4: double (%f)
% For more information, see the TEXTSCAN documentation.
formatSpec = '%f%f%f%f%[^\n\r]';
%% Open the text file.
fileID = fopen(filename, 'r');
%% Read columns of data according to the format.
% This call is based on the structure of the file used to generate this
% code. If an error occurs for a different file, try regenerating the code
% from the Import Tool.
dataArray = textscan(fileID, formatSpec, endRow(1)-startRow(1)+1,
'Delimiter', delimiter, 'TextType', 'string', 'HeaderLines', startRow(1)-1,
'ReturnOnError', false, 'EndOfLine', '\r\n');
for block=2:length(startRow)
    frewind(fileID);
    dataArrayBlock = textscan(fileID, formatSpec, endRow(block)-
startRow(block)+1, 'Delimiter', delimiter, 'TextType', 'string',
'HeaderLines', startRow(block)-1, 'ReturnOnError', false, 'EndOfLine',
' r n');
    for col=1:length(dataArray)
        dataArray{col} = [dataArray{col};dataArrayBlock{col}];
    end
end
```

```
%% Close the text file.
fclose(fileID);
%% Post processing for unimportable data.
% No unimportable data rules were applied during the import, so no post
% processing code is included. To generate code which works for
% unimportable data, select unimportable cells in a file and regenerate the
% script.
%% Allocate imported array to column variable names
RTD_0 = dataArray{:, 1};
RTD_1 = dataArray{:, 2};
RTD_2 = dataArray{:, 3};
RTD_3 = dataArray{:, 4};
```

importfile_TC.m

```
function [T 0,T 1,T 2,T 3,T 4,T 5,T 6,T 7,T 8,T 9,T 10,T 11,T 12,T 13] =
importfile TC(filename, startRow, endRow)
%IMPORTFILE Import numeric data from a text file as column vectors.
    [T 0,T 1,T 2,T 3,T 4,T 5,T 6,T 7,T 8,T 9,T 10,T 11,T 12,T 13] =
8
    IMPORTFILE (FILENAME) Reads data from text file FILENAME for the default
8
8
    selection.
8
00
   [T 0,T 1,T 2,T 3,T 4,T 5,T 6,T 7,T 8,T 9,T 10,T 11,T 12,T 13] =
00
    IMPORTFILE (FILENAME, STARTROW, ENDROW) Reads data from rows STARTROW
2
   through ENDROW of text file FILENAME.
0
% Example:
    [T_0, T_1, T_2, T_3, T_4, T_5, T_6, T_7, T_8, T_9, T_{10}, T_{11}, T_{12}, T_{13}] =
8
importfile('TH 250 TC 21 P 60 44mm 0 Temp.log', 6, 50005);
8
     See also TEXTSCAN.
0
% Auto-generated by MATLAB on 2017/10/24 14:51:24
%% Initialize variables.
delimiter = ' \setminus t';
if nargin<=2</pre>
    startRow = 6;
    endRow = inf;
end
%% Format for each line of text:
   column1: double (%f)
2
   column2: double (%f)
2
   column3: double (%f)
8
   column4: double (%f)
8
   column5: double (%f)
8
  column6: double (%f)
8
% column7: double (%f)
% column8: double (%f)
% column9: double (%f)
   column10: double (%f)
00
```

```
column11: double (%f)
2
   column12: double (%f)
2
   column13: double (%f)
2
2
   column14: double (%f)
% For more information, see the TEXTSCAN documentation.
%% Open the text file.
fileID = fopen(filename, 'r');
%% Read columns of data according to the format.
% This call is based on the structure of the file used to generate this
% code. If an error occurs for a different file, try regenerating the code
% from the Import Tool.
dataArray = textscan(fileID, formatSpec, endRow(1)-startRow(1)+1,
'Delimiter', delimiter, 'TextType', 'string', 'EmptyValue', NaN,
'HeaderLines', startRow(1)-1, 'ReturnOnError', false, 'EndOfLine', '\r\n');
for block=2:length(startRow)
    frewind(fileID);
    dataArrayBlock = textscan(fileID, formatSpec, endRow(block)-
startRow(block)+1, 'Delimiter', delimiter, 'TextType', 'string',
'EmptyValue', NaN, 'HeaderLines', startRow(block)-1, 'ReturnOnError', false,
'EndOfLine', '\r\n');
    for col=1:length(dataArray)
        dataArray{col} = [dataArray{col};dataArrayBlock{col}];
    end
end
%% Close the text file.
fclose(fileID);
%% Post processing for unimportable data.
% No unimportable data rules were applied during the import, so no post
% processing code is included. To generate code which works for
% unimportable data, select unimportable cells in a file and regenerate the
% script.
%% Allocate imported array to column variable names
T = dataArray\{:, 1\};
T = dataArray{:, 2};
T = dataArray{:, 3};
T^{-}3 = dataArray{:, 4};
T 4 = dataArray{:, 5};
T = dataArray{:, 6};
T 6 = dataArray{:, 7};
T 7 = dataArray{:, 8};
T 8 = dataArray{:, 9};
T = dataArray{:, 10};
T = dataArray{:, 11};
T 11 = dataArray{:, 12};
T 12 = dataArray{:, 13};
T 13 = dataArray{:, 14};
```

Encoder_2_Angle.m

```
function [theta deg] = Encoder 2 Angle(A,Z)
% Written by Connor Speer, October 2017. Subfunction to convert rotary
% encoder voltage data into crank angles.
%% Inputs:
% A --> column vector of A-output voltages from the rotary encoder
% Z --> column vector of Z-output voltages from the rotary encoder
\% *** A and Z must be the same length
%% Outputs
% theta deg --> column vector of angles corresponding to rotary encoder
% outputs in (deg)
% freq --> frequency of rotary encoder in (Hz)
% RPM --> speed of rotary encoder in (RPM)
%% Find reference pulse in Z output
threshold = 3;
ref_pulse = find(Z > threshold, 1);
%% Work backwards from reference pulse to find pulse counts
if A(ref pulse) > 2.5
    pulse_flag = 1;
else
    pulse flag = 0;
end
A count = zeros(size(A));
bwd counter = 500;
row = ref pulse - 1;
while row ~= 0
    if pulse flag == 0 && A(row) < 2.5
        bwd counter = bwd counter - 1;
    end
    if bwd counter == -1
    bwd counter = 500;
    end
    A count(row) = bwd counter;
    if A(row) < 2.5
       pulse flag = 1;
    else
       pulse flag = 0;
    end
    row = row - 1;
end
%% Work forwards from reference pulse to find pulse counts
if A(ref pulse) > 2.5
   pulse flag = 1;
```

```
else
    pulse flag = 0;
end
fwd counter = 0;
for row = ref pulse:length(A)
    if pulse flag == 0 && A(row) > 2.5
        fwd counter = fwd counter + 1;
    end
    if fwd_counter == 501
    fwd counter = 0;
    end
    A count(row) = fwd counter;
    if A(row) > 2.5
        pulse flag = 1;
    else
        pulse flag = 0;
    end
end
%% Use pulse count to calculate crank angles
theta deg = A count*(360/500); % [deg]
%% Calculate Crankshaft Speed
refs = find (A < 0.5);
% Initialize variables
pulse count = 0;
for inc = 1:(length(refs)-1)
    if refs(inc+1) ~= (refs(inc) + 1)
        pulse count = pulse count + 1;
    end
end
```

PV_data_avg.m

```
function [avg_pressures] = PV_data_avg(angles,pressures)
% Written by Connor Speer, March 2017
% Inputs:
% angles --> angles corresponding to pressures in [radians].
% Round angles to the nearest whole number and convert to degrees
rounded_angles = round(angles*180/pi);
% Average all pressures which share the same angle
% Initialize vectors
```

```
avg_pressures = zeros(360,1);
for current_angle = 0:1:359
indices = rounded_angles == current_angle;
avg_press = mean(pressures(indices));
avg_pressures(current_angle+1) = avg_press;
end
```

Calibration Functions

Calibration_Function_Call.m

```
% Calibration Function Call.m
% Written by Connor Speer, November 2017
clear,clc,close all;
%% Plot Set-Up
set(0, 'defaultfigurecolor', [1 1 1])
% Location of Figures
x = 500;
y = 500;
% Size of Figures
width = 550;
height = 400;
% Font For Figures
font = 'Arial';
font size = 11;
%% Thermocouples
TC Cal Folder = 'X:\01 Current Students\Connor Speer\00 Thesis and Journal
Papers\00 Thesis\00 Data and Plots\Calibration Codes\Thermocouple Calibration
Oct. 22';
[TC FIT COEFFICIENTS]...
   = TC Correction Terms(TC Cal Folder, 0);
% Collect all the log file names from the test data folder
log files info = dir(fullfile(TC Cal Folder, '*.log'));
counter = 1;
for i = 1:length(log_files_info)
   filename TC = strcat(TC Cal Folder,'\',log files info(i).name);
   [TC 0,TC 1,TC 2,TC 3,TC 4,TC 5,TC 6,T 7,T 8,T 9,T 10,T 11,T 12,T 13] =
. . .
   importfile TC(filename TC);
8
    T 0 --> Expansion Space
```

```
T 1 --> HH-Regen
00
      T^2 --> HH Flange - Bypass Side
8
8
      T 3 --> HH Flange - Power Piston Side
8
      T 4 --> Displacer Mount
8
      T 5 --> Crankcase
8
      T 6 --> Power Piston
TC true(:,counter) = mean([mean(TC 0) mean(TC 1) mean(TC 2) mean(TC 3)
mean(TC 4) mean(TC 5) mean(TC 6)]); %(deg C)
% TC 0 raw(:,counter) = TC 0; %(deg C)
% TC 1 raw(:,counter) = TC 1; %(deg C)
TC 2 raw(:,counter) = TC 2; \%(\text{deg C})
TC 3 raw(:, counter) = TC 3; %(\deg C)
TC_4raw(:,counter) = TC_4; %(deg C)
TC_5_raw(:, counter) = TC_5; % (deg C)
TC_6 raw(:, counter) = TC_6; % (deg C)
% TC 0 calibrated(:,counter) =
calibrate TC(0,TC 0 raw(:,counter),TC FIT COEFFICIENTS); %(deg C)
% TC 1 calibrated(:,counter) =
calibrate_TC(1,TC_1_raw(:,counter),TC_FIT_COEFFICIENTS); %(deg C)
TC 2 calibrated(:,counter) =
calibrate TC(2,TC 2 raw(:,counter),TC FIT COEFFICIENTS); %(deg C)
TC 3 calibrated(:,counter) =
calibrate_TC(3,TC_3_raw(:,counter),TC_FIT COEFFICIENTS); %(deg C)
TC 4 calibrated(:,counter) =
calibrate TC(4,TC 4 raw(:,counter),TC FIT COEFFICIENTS); %(deg C)
TC 5 calibrated(:,counter) =
calibrate TC(5,TC 5 raw(:,counter),TC FIT COEFFICIENTS); %(deg C)
TC 6 calibrated(:,counter) =
calibrate TC(6,TC 6 raw(:,counter),TC FIT COEFFICIENTS); % (deg C)
counter = counter + 1;
end
% Plot 5a - Measured Temperature vs. "True" Temperature before adjustment
% figure('Position', [x y 326 275])
% hold on
% % plot(mean(TC 0 raw),TC true,'*k')
% % plot(mean(TC 1 raw),TC true, '*g')
% plot(mean(TC 2 raw),TC_true,'*b')
% plot(mean(TC_3_raw),TC_true,'*m')
% plot(mean(TC 4 raw),TC true,'*c')
% plot(mean(TC 5 raw),TC true,'*r')
% plot(mean(TC 6 raw),TC true,'*y')
% plot(TC true,TC true,'-r')
% hold off
% xlabel('"True" Temperature (\circC)')
% ylabel('Measured Temperature (\circC)')
% legend('TC 2','TC 3','TC 4','TC 5','TC 6','"True"
Temperature', 'Location', 'NorthWest')
% Plot 5b - Measured Temperature Error before adjustment
figure('Position', [x y 326 275])
hold on
```

```
% plot(TC true,mean(TC 0 raw)-TC true,'*k')
% plot(TC true, mean(TC 1 raw) - TC true, '*g')
plot(TC_true, mean(TC_2_raw)-TC_true, '*b')
plot(TC_true, mean(TC_3_raw)-TC_true, '*m')
plot(TC true, mean(TC 4 raw) -TC true, '*c')
plot(TC true, mean(TC 5 raw)-TC true, '*r')
plot(TC true, mean(TC 6 raw)-TC true, '*y')
hold off
xlabel('"True" Temperature (\circC)')
ylabel('Measured Temperature Error (\circC)')
% Plot 6a - Measured Temperature vs. "True" Temperature before adjustment
% figure('Position', [x y 326 275])
% hold on
% % plot(mean(TC 0 raw),TC true,'*k')
% % plot(mean(TC 1 raw),TC true,'*g')
% plot(mean(TC 2 raw),TC true, '*b')
% plot(mean(TC 3 raw),TC true,'*m')
% plot(mean(TC_4_raw),TC_true,'*c')
% plot(mean(TC_5_raw),TC_true,'*r')
% plot(mean(TC_6_raw),TC_true,'*y')
% plot(TC true,TC true,'-r')
% hold off
% xlabel('"True" Temperature (\circC)')
% ylabel('Measured Temperature (\circC)')
% legend('TC 2','TC 3','TC 4','TC 5','TC 6','"True"
Temperature', 'Location', 'NorthWest')
% Plot 6b - Measured Temperature Error after adjustment
figure('Position', [x y 326 275])
hold on
% plot(TC_true,mean(TC_0_calibrated)-TC_true,'*k')
% plot(TC true,mean(TC 1 calibrated)-TC true,'*g')
plot(TC true, mean(TC 2 calibrated) -TC true, '*b')
plot(TC true, mean(TC 3 calibrated) -TC true, '*m')
plot(TC true, mean(TC 4 calibrated) -TC true, '*c')
plot(TC true, mean(TC 5 calibrated) -TC true, '*r')
plot(TC true,mean(TC 6 calibrated)-TC true, '*y')
hold off
xlabel('"True" Temperature (\circC)')
ylabel('Measured Temperature Error (\circC)')
%% Validyne Absolute Pressure
Abs Val Cal Folder = 'X:\01 Current Students\Connor Speer\00 Thesis and
Journal Papers\00 Thesis\00 Data and Plots\Calibration Codes\Validyne
Calibration Oct. 22';
[ABS VAL FIT COEFFICIENTS]...
    = ABS VAL Correction Terms (Abs Val Cal Folder, 0);
% Collect all the log file names from the test data folder
log files info = dir(fullfile(Abs Val Cal Folder, '*.log'));
```

```
counter = 1;
```

```
for i = 1:length(log files info)
filename Volt = strcat(Abs Val Cal Folder,'\',log files info(i).name);
[A,Z,TOR,P1,P2,P3,P4,P5] = importfile P(filename Volt);
      P1 --> Validyne Regenerator Differential Pressure
8
8
      P2 --> Validyne Power Cylinder
8
     P3 --> Validyne Crankcase
P cal machine(:,counter) = str2double(extractBetween(log files info(i).name,
'E ', 'PSI')); %(PSI)
P cal machine(:,counter) = P cal machine(:,counter)*6894.76; %(Pa)
P2 Pa raw(:,counter) = P2*20*6894.76; %(Pa)
P3 Pa raw(:,counter) = P3*20*6894.76; %(Pa)
P2 Pa calibrated(:,counter) =
calibrate abs VAL(2,P2 Pa raw(:,counter),ABS VAL FIT COEFFICIENTS); %(Pa)
P3 Pa calibrated(:,counter) =
calibrate abs VAL(3,P3 Pa raw(:,counter),ABS VAL FIT COEFFICIENTS); %(Pa)
counter = counter + 1;
end
% Plot 5a - Measured Pressure vs. "True" Pressure before adjustment
% figure('Position', [x y 326 275])
% hold on
% plot(mean(P2 Pa raw)./1000,P cal machine./1000,'*r')
% plot(mean(P3 Pa raw)./1000, P cal machine./1000, 'ok')
% plot(P cal machine./1000,P cal machine./1000,'-r')
% hold off
% xlabel('Calibration Machine Pressure (kPa)');
% ylabel('Measured Pressure (kPa)')
% legend('Power Cylinder','Crankcase','Cal Machine','Location','NorthWest')
% Plot 5b - Measured Pressure Error before adjustment
figure('Position', [x y 326 275])
hold on
plot(P cal machine./1000,mean(P2 Pa raw)./1000-P cal machine./1000,'*r')
plot(P cal machine./1000, mean(P3 Pa raw)./1000-P cal machine./1000, 'ok')
hold off
xlabel('Calibration Machine Pressure (kPa)');
ylabel('Measured Pressure Error (kPa)')
legend('Power Cylinder', 'Crankcase', 'Location', 'NorthWest')
% Plot 6a - Measured Pressure vs. "True" Pressure before adjustment
% figure('Position', [x y 326 275])
% hold on
% plot(mean(P2 Pa calibrated)./1000,P cal machine./1000,'*r')
% plot(mean(P3 Pa calibrated)./1000,P cal machine./1000,'ok')
% plot(P cal machine./1000,P cal machine./1000,'-r')
% hold off
% xlabel('Calibration Machine Pressure (kPa)');
% ylabel('Measured Pressure (kPa)')
% legend('Power Cylinder','Crankcase','Cal Machine','Location','NorthWest')
% Plot 6b - Measured Pressure Error before adjustment
figure('Position', [x y 326 275])
```

```
hold on
plot(P cal machine./1000, mean(P2 Pa calibrated)./1000-
P cal machine./1000, '*r')
plot (P cal machine./1000, mean (P3 Pa calibrated)./1000-
P cal machine./1000, 'ok')
hold off
xlabel('Calibration Machine Pressure (kPa)');
ylabel('Measured Pressure Error (kPa)')
legend('Power Cylinder', 'Crankcase', 'Location', 'NorthWest')
%% Validyne Differential Pressure
Diff Val Cal Folder = 'X:\01 Current Students\Connor Speer\00 Thesis and
Journal Papers\00 Thesis\00 Data and Plots\Calibration Codes\Differential
Validvne Calibration Oct. 22';
[DIFF VAL FIT COEFFICIENTS]...
    = DIFF VAL Correction Terms (Diff Val Cal Folder, 0);
% Collect all the log file names from the test data folder
log files info = dir(fullfile(Diff Val Cal Folder, '*.log'));
counter = 1;
for i = 1:length(log files info)
filename Volt = strcat(Diff Val Cal Folder, '\', log files info(i).name);
[A,Z,TOR,P1,P2,P3,P4,P5] = importfile P(filename Volt);
      P1 --> Validyne Regenerator Differential Pressure
8
2
      P2 --> Validyne Power Cylinder
2
      P3 --> Validyne Crankcase
P cal machine(:,counter) = str2double(extractBetween(log files info(i).name,
'E ', 'PSI')); %(PSI)
P cal machine(:,counter) = P cal machine(:,counter)*6894.76; %(Pa)
P1 Pa raw(:,counter) = P1*0.5*6894.76; %(Pa)
P1 Pa calibrated(:,counter) =
calibrate diff VAL(1,P1 Pa raw(:,counter),DIFF VAL FIT COEFFICIENTS); %(Pa)
counter = counter + 1;
end
% Plot 5a - Measured Pressure vs. "True" Pressure before adjustment
% figure('Position', [x y 326 275])
% hold on
% plot(mean(P1 Pa raw)./1000,P cal machine./1000,'*k')
% plot(P cal machine./1000,P cal machine./1000,'-r')
% hold off
% xlabel('Calibration Machine Pressure (kPa)')
% ylabel('Measured Pressure (kPa)')
% legend('Regenerator Differential','Cal Machine','Location','NorthWest')
% Plot 5b - Measured Pressure Error before adjustment
figure('Position', [x y 326 275])
plot(P cal machine./1000,mean(P1 Pa raw)./1000-P cal machine./1000,'*k')
xlabel('Calibration Machine Pressure (kPa)')
ylabel('Measured Pressure Error (kPa)')
```

```
% Plot 6a - Measured Pressure vs. "True" Pressure before adjustment
% figure('Position', [x y 326 275])
% hold on
% plot(mean(P1 Pa calibrated)./1000,P cal machine./1000,'*k')
% plot(P cal machine./1000,P cal machine./1000,'-r')
% hold off
% xlabel('Calibration Machine Pressure (kPa)')
% ylabel('Measured Pressure (kPa)')
% legend('Regenerator Differential','Cal Machine','Location','NorthWest')
% Plot 6b - Measured Pressure Error before adjustment
figure('Position', [x y 326 275])
plot(P cal machine./1000, mean(P1 Pa calibrated)./1000-
P cal machine./1000, '*k')
xlabel('Calibration Machine Pressure (kPa)')
ylabel('Measured Pressure Error (kPa)')
%% RTDs
RTD Cal Folder = 'X:\01 Current Students\Connor Speer\00 Thesis and Journal
Papers\00 Thesis\00 Data and Plots\Calibration Codes\RTD Calibration Oct.
22';
[RTD FIT COEFFICIENTS]...
    = RTD Correction Terms(RTD Cal Folder, 0);
% Collect all the log file names from the test data folder
log files info = dir(fullfile(RTD Cal Folder, '*.log'));
counter = 1;
for i = 1:length(log files info)
    filename RTD = strcat(RTD Cal Folder,'\',log files info(i).name);
    [RTD 0,RTD 1,RTD 2,RTD 3] = importfile RTD(filename RTD);
00
      RTD 0 --> Cooler water inlet
00
     RTD 1 --> Cooler water outlet
2
      RTD 2 --> Con Pipe/Pow Cyl inlet
2
      RTD 3 --> Con Pipe/Pow Cyl outlet
RTD true(:,counter) = mean([mean(RTD 0) mean(RTD 1) mean(RTD 2)
mean(RTD 3)]); %(deg C)
RTD 0 raw(:,counter) = RTD 0; %(deg C)
RTD_1_raw(:,counter) = RTD_1; %(deg C)
RTD 2 raw(:,counter) = RTD 2; %(deg C)
RTD 3 raw(:,counter) = RTD 3; % (deg C)
RTD 0 calibrated(:,counter) =
calibrate RTD(0,RTD 0 raw(:,counter),RTD FIT COEFFICIENTS); % (deg C)
RTD 1 calibrated(:,counter) =
calibrate RTD(1,RTD 1 raw(:,counter),RTD FIT COEFFICIENTS); % (deg C)
RTD 2 calibrated(:,counter) =
calibrate RTD(2,RTD 2 raw(:,counter),RTD FIT COEFFICIENTS); % (deg C)
RTD 3 calibrated(:,counter) =
calibrate RTD(3,RTD 3 raw(:,counter),RTD FIT COEFFICIENTS); %(deg C)
counter = counter + 1;
end
```

```
% Plot 5a - Measured Temperature vs. "True" Temperature before adjustment
% figure('Position', [x y 326 275])
% hold on
% plot(mean(RTD 0 raw),RTD true,'*k')
% plot(mean(RTD 1 raw),RTD true,'*g')
% plot(mean(RTD_2_raw),RTD_true,'*b')
% plot(mean(RTD 3 raw), RTD true, '*m')
% plot(RTD true,RTD true,'-r')
% hold off
% xlabel('"True" Temperature (\circC)')
% ylabel('Measured Temperature (\circC)')
% legend('RTD 0','RTD 1','RTD 2','RTD 3','"True"
Temperature', 'Location', 'NorthWest')
% Plot 5b - Measured Temperature Error before adjustment
figure('Position', [x y 326 275])
hold on
plot(RTD true, mean(RTD 0 raw)-RTD true, '*k')
plot(RTD true, mean(RTD 1 raw) - RTD true, '*g')
plot(RTD true, mean(RTD 2 raw) - RTD true, '*b')
plot(RTD true, mean(RTD 3 raw) - RTD true, '*m')
hold off
xlabel('"True" Temperature (\circC)')
vlabel('Measured Temperature Error (\circC)')
% Plot 6a - Measured Temperature vs. "True" Temperature before adjustment
% figure('Position', [x y 326 275])
% hold on
% plot(mean(RTD 0 raw),RTD true,'*k')
% plot(mean(RTD 1 raw),RTD true, '*g')
% plot(mean(RTD 2 raw),RTD true, '*b')
% plot(mean(RTD 3 raw), RTD true, '*m')
% plot(RTD true,RTD true,'-r')
% hold off
% xlabel('"True" Temperature (\circC)')
% ylabel('Measured Temperature (\circC)')
% legend('RTD 0','RTD 1','RTD 2','RTD 3','"True"
Temperature', 'Location', 'NorthWest')
% Plot 6b - Measured Temperature Error after adjustment
figure('Position', [x y 326 275])
hold on
plot(RTD true, mean(RTD 0 calibrated)-RTD true, '*k')
plot(RTD true, mean(RTD 1 calibrated) - RTD true, '*g')
plot(RTD true, mean(RTD 2 calibrated) - RTD true, '*b')
plot(RTD true, mean(RTD 3 calibrated)-RTD true, '*m')
hold off
xlabel('"True" Temperature (\circC)')
ylabel('Measured Temperature Error (\circC)')
```

ABS_VAL_Correction_Terms.m

```
function [ABS_VAL_FIT_COEFFICIENTS]...
```

```
= ABS VAL Correction Terms (P Cal Folder, Cal Stats On Off)
% Written by Connor Speer - October '17
% Modified by Shahzeb Mirza Oct 2017
% Modified by Connor Speer - December '17
% The goal of this function is to collect calibration data from a specified
% folder and determine the correction terms and raw data statistics.
% Calibration correction factors are then used to adjust the raw data.
% Collect all the log file names from the thermocouple test data folder
P log files info = dir(fullfile(P Cal Folder, '*.log'));
% Preallocate space for the structure array
P DATA(length(P log files info)).P 2 raw = [];
P DATA(length(P log files info)).P 2 avg = [];
P DATA(length(P log files info)).P 2 stdev = [];
P DATA(length(P log files info)).P 2 corr = [];
P_DATA(length(P_log_files_info)).P_3_raw = [];
P DATA(length(P log files info)).P 3 avg = [];
P DATA(length(P log files info)).P 3 stdev = [];
P DATA(length(P log files info)).P 3 corr = [];
P DATA(length(P log files info)).P 4 raw = [];
P DATA(length(P log files info)).P 4 avg = [];
P DATA(length(P log files info)).P 4 stdev = [];
P DATA(length(P log files info)).P 4 corr = [];
P DATA(length(P log files info)).P overall avg = [];
P DATA(length(P log files info)).P single = [];
% Initialize counter variable
counter = 1;
counter max = 0.5*length(P log files info);
WaitBar = waitbar(0, 'Analyzing calibration data...');
% Open Calibration Log Files
for i = 1:1:length(P log files info)
   filename Volt = strcat(P Cal Folder, '\', P log files info(i).name);
   [A,Z,TOR,P 1,P 2,P 3,P 4,P 5] = importfile P(filename Volt);
     A --> 500 PPR Rotary Encoder Output
8
00
     Z --> 1 PPR Rotary Encoder Output
8
     TOR --> Torque Transducer Output
8
     P1 --> Validyne Regenerator Differential Pressure
00
     P2 --> Validyne Power Cylinder
    P3 --> Validyne Crankcase
00
00
    P4 --> PCB Power Cylinder
8
    P5 --> PCB Crankcase
   % Calculate Data from the file
```

```
% Calculate the average reading for each pressure transducer
```

```
P 2 avg = mean(P 2)*20*6894.76; %(Pa)
   P_3_avg = mean(P_3)*20*6894.76; %(Pa)
   P 4 avg = mean(P 4)*20*6894.76; %(Pa)
   % Collect the "true" pressure from the name of the log file
   try
   P cal machine = str2double(extractBetween(P log files info(i).name,
'E ', 'PSI')); %(PSI)
   catch
   end
   P cal machine = P cal machine*6894.76; %(Pa)
   % Calculate the correction term for each pressure transducer
    P 2 corr = P cal machine - P 2 avg; %(Pa)
   P 3 corr = P cal machine - P 3 avg; %(Pa)
   P 4 corr = P cal machine - P 4 avg; % (Pa)
   % Calculate the sample standard deviation for each pressure transducer
    P 2 stdev = std(P 2);
    P^{3} stdev = std(P^{3});
   P 4 stdev = std(P 4);
    % Find the maximum standard deviation of all the thermocouples
    stdev max = max([P 2 stdev P 3 stdev P 4 stdev]);
    % Calculate the worst case random uncertainty for a single measurement
    P single = 2*stdev max; % t = 2, See example 7.3 in Wheeler and Ganji
    % Store the values from the log file in a structure
    P DATA(counter).P 2 raw = P 2;
   P_DATA(counter).P_2_avg = P_2_avg;
P_DATA(counter).P_2_stdev = P_2_stdev;
    P DATA(counter).P 2 corr = P 2 corr;
    P_DATA(counter).P_3_raw = P_3;
   P_DATA(counter).P_3_avg = P_3_avg;
P_DATA(counter).P_3_stdev = P_3_stdev;
   P DATA(counter).P 3 corr = P 3 corr;
    P_DATA(counter).P_4_raw = P_4;
    P DATA(counter).P 4 avg = P 4 avg;
    P DATA(counter).P 4 stdev = P 4 stdev;
    P DATA(counter).P 4 corr = P 4 corr;
   P DATA(counter).P cal machine = P cal machine;
    P DATA(counter).P single = P single;
    % Increment the counter variable
   counter = counter + 1;
    % Update Wait Bar
   waitbar(counter / counter max)
```

end
close(WaitBar);

```
%% Fit Curves to Correction Terms
% Fit a curve to the correction terms. Each thermocouple gets its own
% curve. Could potentially use the R^2 value to quantify the systematic
% error.
P_2_fit = fit([P_DATA.P_2_avg]',[P_DATA.P_2_corr]','poly3');
P_3_fit = fit([P_DATA.P_3_avg]',[P_DATA.P_3_corr]','poly3');
P_4_fit = fit([P_DATA.P_4_avg]',[P_DATA.P_4_corr]','poly3');
% Store the coefficients of the fitted curve equations in a structure
ABS_VAL_FIT_COEFFICIENTS.P_2 = coeffvalues(P_2_fit);
ABS_VAL_FIT_COEFFICIENTS.P_3 = coeffvalues(P_3_fit);
ABS_VAL_FIT_COEFFICIENTS.P_4 = coeffvalues(P_4_fit);
```

```
Display the worst case random uncertainty for a single measurement
D1 = ['Worst case random uncertainty for a single
measurement:',num2str(P_single),' V'];
disp(D1);
```

calibrate_abs_VAL.m

function P calibrated = calibrate abs VAL(Ch num, P raw, ABS VAL FIT COEFFICIENTS) % Written by Connor Speer, December 2017 % This function adds correction terms, calculated via the fit coefficients, % to a vector of input raw data and returns a vector of calibrated data. %% Inputs % Ch num --> Channel number of the transducer. Must be the same as in the % calibration data. % P raw --> raw pressure data in Pa. % ABS VAL FIT COEFFICIENTS --> 3rd order polynomial fit coefficients for % correction terms %% Outputs % P calibrated --> Calibrated pressure in Pa. %% Calculate correction terms if Ch num == 2p1 = ABS VAL FIT COEFFICIENTS.P 2(1); p2 = ABS VAL FIT COEFFICIENTS.P 2(2); p3 = ABS VAL FIT COEFFICIENTS.P 2(3); p4 = ABS VAL FIT COEFFICIENTS.P 2(4); elseif Ch num == 3 p1 = ABS_VAL_FIT_COEFFICIENTS.P_3(1); p2 = ABS VAL FIT COEFFICIENTS.P 3(2); p3 = ABS VAL FIT COEFFICIENTS.P 3(3); p4 = ABS VAL FIT COEFFICIENTS.P 3(4);

correction_terms = p1.*P_raw.^3 + p2.*P_raw.^2 + p3.*P_raw + p4; %% Apply correction terms P_calibrated = P_raw + correction_terms;

DIFF_VAL_Correction_Terms.m

```
function [DIFF VAL FIT COEFFICIENTS]...
   = DIFF VAL Correction Terms (P Cal Folder, Cal Stats On Off)
% Written by Connor Speer - October '17
% Modified by Shahzeb Mirza Oct 2017
% Modified by Connor Speer - December '17
% The goal of this function is to collect calibration data from a specified
% folder and determine the correction terms and raw data statistics.
% Calibration correction factors are then used to adjust the raw data.
% Collect all the log file names from the thermocouple test data folder
P log files info = dir(fullfile(P Cal Folder, '*.log'));
% Preallocate space for the structure array
P DATA(length(P log files info)).P 1 raw = [];
P_DATA(length(P_log_files_info)).P_1_avg = [];
P DATA(length(P log files info)).P 1 stdev = [];
P DATA(length(P log files info)).P 1 corr = [];
P DATA(length(P log files info)).P overall avg = [];
P DATA(length(P log files info)).P single = [];
% Initialize counter variable
counter = 1;
counter max = 0.5*length(P log files info);
WaitBar = waitbar(0, 'Analyzing calibration data...');
% Open Calibration Log Files
for i = 1:1:length(P log files info)
   filename Volt = strcat(P Cal Folder, '\', P_log_files_info(i).name);
   [A,Z,TOR,P_1,P_2,P_3,P_4,P_5] = importfile_P(filename_Volt);
8
    A --> 500 PPR Rotary Encoder Output
8
     Z --> 1 PPR Rotary Encoder Output
8
     TOR --> Torque Transducer Output
8
     P1 --> Validyne Regenerator Differential Pressure
8
    P2 --> Validyne Power Cylinder
8
    P3 --> Validyne Crankcase
     P4 --> PCB Power Cylinder
8
00
     P5 --> PCB Crankcase
```

```
% Calculate Data from the file
```

351

end

```
% Calculate the average reading for each pressure transducer
    P 1 avg = mean(P 1)*0.5*6894.76; %(Pa)
    % Collect the "true" pressure from the name of the log file
    try
    P cal machine = str2double(extractBetween(P log files info(i).name,
'E ', 'PSI')); %(PSI)
   catch
    end
    P cal machine = P cal machine*6894.76; %(Pa)
    % Calculate the correction term for each pressure transducer
    P 1 corr = P cal machine - P 1 avg; %(Pa)
    % Calculate the sample standard deviation for each pressure transducer
    P 1 stdev = std(P 1);
    % Find the maximum standard deviation of all the thermocouples
    stdev max = P 1 stdev;
    % Calculate the worst case random uncertainty for a single measurement
    P single = 2*stdev max; % t = 2, See example 7.3 in Wheeler and Ganji
    % Store the values from the log file in a structure
    P DATA(counter).P 1 raw = P 1;
    P DATA(counter).P 1 avg = P 1 avg;
    P DATA(counter).P 1 stdev = P 1 stdev;
    P DATA(counter).P 1 corr = P 1 corr;
    P DATA(counter).P cal machine = P cal machine;
    P DATA(counter).P single = P single;
    % Increment the counter variable
    counter = counter + 1;
    % Update Wait Bar
   waitbar(counter / counter max)
end
close(WaitBar);
%% Fit Curves to Correction Terms
% Fit a curve to the correction terms. Each thermocouple gets its own
% curve. Could potentially use the R^2 value to quantify the systematic
% error.
P 1 fit = fit([P DATA.P_1_avg]', [P_DATA.P_1_corr]', 'poly3');
% Store the coefficients of the fitted curve equations in a structure
DIFF VAL FIT COEFFICIENTS.P 1 = coeffvalues(P 1 fit);
```

```
% Display the worst case random uncertainty for a single measurement
D1 = ['Worst case random uncertainty for a single
measurement:',num2str(P_single),' V'];
disp(D1);
```

calibrate_diff_VAL.m

```
function P calibrated =
calibrate diff VAL(Ch num, P raw, ABS VAL FIT COEFFICIENTS)
% Written by Connor Speer, December 2017
% This function adds correction terms, calculated via the fit coefficients,
% to a vector of input raw data and returns a vector of calibrated data.
%% Inputs
\% Ch num --> Channel number of the transducer. Must be the same as in the
% calibration data.
% P raw --> raw pressure data in Pa.
% ABS VAL FIT COEFFICIENTS --> 3rd order polynomial fit coefficients for
% correction terms
%% Outputs
% P calibrated --> Calibrated pressure in Pa.
%% Calculate correction terms
if Ch num == 1
    p1 = ABS VAL FIT COEFFICIENTS.P 1(1);
    p2 = ABS VAL FIT COEFFICIENTS.P 1(2);
    p3 = ABS VAL FIT COEFFICIENTS.P 1(3);
    p4 = ABS VAL FIT COEFFICIENTS.P 1(4);
end
correction terms = p1.*P raw.<sup>3</sup> + p2.*P raw.<sup>2</sup> + p3.*P raw + p4;
%% Apply correction terms
P calibrated = P raw + correction terms;
```

RTD_Correction_Terms.m

```
% Preallocate space for the structure array
RTD DATA(length(RTD log files info)).RTD 0 raw = [];
RTD DATA(length(RTD log files info)).RTD 0 avg = [];
RTD DATA(length(RTD log files info)).RTD 0 stdev = [];
RTD DATA(length(RTD log files info)).RTD 0 corr = [];
RTD DATA(length(RTD log files info)).RTD 1 raw = [];
RTD DATA(length(RTD log files info)).RTD 1 avg = [];
RTD DATA(length(RTD log files info)).RTD 1 stdev = [];
RTD DATA(length(RTD log files info)).RTD 1 corr = [];
RTD DATA(length(RTD log files info)).RTD 2 raw = [];
RTD DATA(length(RTD log files info)).RTD 2 avg = [];
RTD DATA(length(RTD log files info)).RTD 2 stdev = [];
RTD DATA(length(RTD log files info)).RTD 2 corr = [];
RTD DATA(length(RTD log files info)).RTD 3 raw = [];
RTD_DATA(length(RTD_log_files_info)).RTD_3_avg = [];
RTD_DATA(length(RTD_log_files_info)).RTD_3 stdev = [];
RTD DATA(length(RTD log files info)).RTD 3 corr = [];
RTD DATA(length(RTD log files info)).RTD true = [];
RTD DATA(length(RTD log files info)).P single = [];
% Initialize counter variable
counter = 1;
counter max = 0.5*length(RTD log files info);
WaitBar = waitbar(0, 'Analyzing calibration data...');
% Open Calibration Log Files
for i = 1:1:length(RTD log files info)
   filename RTD = strcat(RTD Cal Folder, '\', RTD log files info(i).name);
   [RTD 0,RTD 1,RTD 2,RTD 3] = importfile RTD(filename RTD);
     RTD 0 --> Cooler water inlet
00
8
     RTD 1 --> Cooler water outlet
8
     RTD 2 --> Con Pipe/Pow Cyl inlet
8
     RTD 3 --> Con Pipe/Pow Cyl outlet
   % Calculate Data from the file
   % Calculate the average reading for each RTD
   RTD 0 avg = mean(RTD 0); %(deg C)
   RTD 1 avg = mean(RTD 1); % (deg C)
   RTD 2 avg = mean(RTD 2); %(\deg C)
   RTD 3 avg = mean(RTD 3); %(deg C)
   % Calculate the "true" temperature as the average of all RTDs
   RTD true = mean([RTD 0 avg RTD 1 avg RTD 2 avg RTD 3 avg]);
   % Calculate the correction term for each RTD
   RTD 0 corr = RTD true - RTD 0 avg; % (deg C)
   RTD 1 corr = RTD true - RTD 1 avg; % (deg C)
```

```
RTD 2 corr = RTD true - RTD 2 avg; %(deg C)
    RTD 3 corr = RTD true - RTD_3_avg; %(deg C)
    % Calculate the sample standard deviation for each RTD
    RTD 0 stdev = std(RTD 0);
    RTD 1 stdev = std(RTD 1);
    RTD 2 stdev = std(RTD 2);
    RTD 3 stdev = std(RTD 3);
    % Find the maximum standard deviation of all the thermocouples
    stdev max = max([RTD 0 stdev RTD 1 stdev RTD 2 stdev RTD 3 stdev]);
    % Calculate the worst case random uncertainty for a single measurement
    P single = 2*stdev max; % t = 2, See example 7.3 in Wheeler and Ganji
    % Store the values from the log file in a structure
    RTD DATA(counter).RTD 0 raw = RTD 0;
    RTD DATA(counter).RTD 0 avg = RTD 0 avg;
    RTD_DATA(counter).RTD_0_stdev = RTD_0_stdev;
    RTD_DATA(counter).RTD_0_corr = RTD_0_corr;
    RTD DATA(counter).RTD 1 raw = RTD 1;
    RTD_DATA(counter).RTD_1_avg = RTD_1_avg;
    RTD DATA(counter).RTD 1 stdev = RTD 1 stdev;
    RTD DATA(counter).RTD 1 corr = RTD 1 corr;
    RTD DATA(counter).RTD 2 raw = RTD 2;
    RTD DATA(counter).RTD 2 avg = RTD 2 avg;
    RTD DATA(counter).RTD 2 stdev = RTD 2 stdev;
    RTD DATA(counter).RTD 2 corr = RTD 2 corr;
    RTD DATA(counter).RTD 3 raw = RTD 3;
    RTD DATA(counter).RTD 3 avg = RTD 3 avg;
    RTD DATA(counter).RTD 3 stdev = RTD 3 stdev;
    RTD DATA(counter).RTD 3 corr = RTD 3 corr;
    RTD DATA(counter).RTD true = RTD true;
    RTD DATA(counter).P single = P single;
    % Increment the counter variable
    counter = counter + 1;
    % Update Wait Bar
    waitbar(counter / counter max)
end
close(WaitBar);
%% Fit Curves to Correction Terms
% Fit a curve to the correction terms. Each thermocouple gets its own
% curve. Could potentially use the R^2 value to quantify the systematic
% error.
RTD 0 fit = fit([RTD DATA.RTD 0 avg]',[RTD DATA.RTD 0 corr]','poly3');
RTD 1 fit = fit([RTD DATA.RTD 1 avg]',[RTD DATA.RTD 1 corr]','poly3');
```

```
RTD 2 fit = fit([RTD DATA.RTD 2 avg]',[RTD DATA.RTD 2 corr]','poly3');
RTD_3_fit = fit([RTD_DATA.RTD_3 avg]', [RTD_DATA.RTD_3 corr]', 'poly3');
% Store the coefficients of the fitted curve equations in a structure
RTD FIT COEFFICIENTS.RTD 0 = coeffvalues(RTD 0 fit);
RTD FIT COEFFICIENTS.RTD 1 = coeffvalues(RTD 1 fit);
RTD_FIT_COEFFICIENTS.RTD_2 = coeffvalues(RTD_2_fit);
RTD FIT COEFFICIENTS.RTD 3 = coeffvalues(RTD 3 fit);
% Display the worst case random uncertainty for a single measurement
D1 = ['Worst case random uncertainty for a single
measurement:',num2str(P single),' \circC'];
disp(D1);
calibrate_RTD.m
function RTD calibrated = calibrate RTD(Ch num,RTD raw,RTD FIT COEFFICIENTS)
% Written by Connor Speer, December 2017
% This function adds correction terms, calculated via the fit coefficients,
% to a vector of input raw data and returns a vector of calibrated data.
%% Inputs
% Ch num --> Channel number of the transducer. Must be the same as in the
% calibration data.
% P raw --> raw pressure data in Pa.
% ABS VAL FIT COEFFICIENTS --> 3rd order polynomial fit coefficients for
% correction terms
%% Outputs
% P calibrated --> Calibrated pressure in Pa.
%% Calculate correction terms
if Ch num == 0
    p1 = RTD FIT COEFFICIENTS.RTD 0(1);
   p2 = RTD FIT COEFFICIENTS.RTD 0(2);
   p3 = RTD FIT COEFFICIENTS.RTD 0(3);
   p4 = RTD FIT COEFFICIENTS.RTD 0(4);
elseif Ch num == 1
   p1 = RTD FIT COEFFICIENTS.RTD 1(1);
   p2 = RTD FIT COEFFICIENTS.RTD 1(2);
   p3 = RTD FIT COEFFICIENTS.RTD 1(3);
    p4 = RTD FIT COEFFICIENTS.RTD 1(4);
elseif Ch num == 2
    p1 = RTD FIT COEFFICIENTS.RTD 2(1);
    p2 = RTD FIT COEFFICIENTS.RTD 2(2);
   p3 = RTD FIT COEFFICIENTS.RTD 2(3);
   p4 = RTD FIT COEFFICIENTS.RTD 2(4);
elseif Ch num == 3
    p1 = RTD FIT COEFFICIENTS.RTD 3(1);
    p2 = RTD_FIT_COEFFICIENTS.RTD_3(2);
   p3 = RTD_FIT_COEFFICIENTS.RTD_3(3);
```

```
p4 = RTD_FIT_COEFFICIENTS.RTD_3(4);
```

end

correction_terms = p1.*RTD_raw.^3 + p2.*RTD_raw.^2 + p3.*RTD_raw + p4;
%% Apply correction terms
RTD_calibrated = RTD_raw + correction_terms;

TC_Correction_Terms.m

```
function [TC FIT COEFFICIENTS]...
    = TC Correction Terms (TC Cal Folder, Cal Stats On Off)
% Written by Connor Speer - October '17
% Modified by Shahzeb Mirza Oct 2017
% Modified by Connor Speer - December '17
% The goal of this function is to collect calibration data from a specified
% folder and determine the correction terms and raw data statistics.
% Calibration correction factors are then used to adjust the raw data.
% Collect all the log file names from the thermocouple test data folder
TC log files info = dir(fullfile(TC Cal Folder, '*.log'));
% Preallocate space for the structure array
TC DATA(length(TC log files info)).TC 0 raw = [];
TC DATA(length(TC log files info)).TC 0 avg = [];
TC_DATA(length(TC_log_files_info)).TC_0_stdev = [];
TC DATA(length(TC log files info)).TC 0 corr = [];
TC DATA(length(TC log files info)).TC 1 raw = [];
TC DATA(length(TC log files info)).TC 1 avg = [];
TC_DATA(length(TC_log_files_info)).TC_1_stdev = [];
TC DATA(length(TC log files info)).TC 1 corr = [];
TC DATA(length(TC log files info)).TC 2 raw = [];
TC_DATA(length(TC_log_files_info)).TC_2_avg = [];
TC DATA(length(TC log files info)).TC 2 stdev = [];
TC DATA(length(TC log files info)).TC 2 corr = [];
TC DATA(length(TC log files info)).TC 3 raw = [];
TC_DATA(length(TC_log_files_info)).TC_3_avg = [];
TC DATA(length(TC log files info)).TC 3 stdev = [];
TC DATA(length(TC log files info)).TC 3 corr = [];
TC DATA(length(TC log files info)).TC 4 raw = [];
TC DATA(length(TC log files info)).TC 4 avg = [];
TC DATA(length(TC log files info)).TC 4 stdev = [];
TC DATA(length(TC log files info)).TC 4 corr = [];
TC DATA(length(TC log files info)).TC 5 raw = [];
TC DATA(length(TC log files info)).TC 5 avg = [];
TC DATA(length(TC log files info)).TC 5_stdev = [];
TC DATA(length(TC log files info)).TC 5 corr = [];
```

```
TC DATA(length(TC log files info)).TC 6 raw = [];
TC_DATA(length(TC_log_files_info)).TC_6_avg = [];
TC_DATA(length(TC_log_files_info)).TC_6_stdev = [];
TC DATA(length(TC log files info)).TC 6 corr = [];
TC DATA(length(TC log files info)).TC true = [];
TC DATA(length(TC log files info)).P single = [];
% Initialize counter variable
counter = 1;
counter max = 0.5*length(TC log files info);
WaitBar = waitbar(0, 'Analyzing calibration data...');
% Open Calibration Log Files
for i = 1:1:length(TC log files info)
    filename TC = strcat(TC Cal Folder,'\',TC log files info(i).name);
[TC_0,TC_1,TC_2,TC_3,TC_4,TC_5,TC_6,TC_7,TC_8,TC_9,TC_10,TC_11,TC_12,TC_13] =
    importfile TC(filename TC);
8
     T 0 --> Expansion Space
     T<sup>1</sup> --> HH-Regen
8
90
     T 2 --> HH Flange - Bypass Side
     T^{-3} \rightarrow HH Flange - Power Piston Side
00
8
     T 4 --> Displacer Mount
8
     T 5 --> Crankcase
8
     T 6 --> Power Piston
    % Calculate Data from the file
    % Calculate the average reading for each RTD
   TC 0 avg = mean(TC 0); %(deg C)
    TC_1 avg = mean(TC_1); % (deg C)
      _2_avg = mean(TC_2); %(deg C)
    ТC
   TC_3_avg = mean(TC_3); % (deg C)
   TC 4 avg = mean(TC 4); %(\deg C)
    TC 5 avg = mean(TC 5); %(deg C)
    TC 6 avg = mean(TC 6); %(\deg C)
    % Calculate the "true" temperature as the average of all RTDs
    TC true = mean([TC 0 avg TC 1 avg TC 2 avg TC 3 avg TC 4 avg TC 5 avg
TC 6 avg]);
    % Calculate the correction term for each RTD
    TC 0 corr = TC true - TC 0 avg; %(deg C)
    TC 1 corr = TC true - TC 1 avg; % (deg C)
    TC 2 corr = TC true - TC 2 avg; % (deg C)
   TC_3_corr = TC_true - TC_3_avg; %(deg C)
TC_4_corr = TC_true - TC_4_avg; %(deg C)
    TC 5 corr = TC true - TC 5 avg; % (deg C)
    TC 6 corr = TC true - TC 6 avg; %(deg C)
    % Calculate the sample standard deviation for each RTD
```

```
TC 0 stdev = std(TC_0);
    ТC
      1 \text{ stdev} = \text{std}(\text{TC } 1);
    TC 2 stdev = std(TC 2);
    TC 3 stdev = std(TC 3);
    TC 4 stdev = std(TC 4);
    TC 5 stdev = std(TC 5);
    TC 6 stdev = std(TC 6);
    % Find the maximum standard deviation of all the thermocouples
    stdev max = max([TC 0 stdev TC 1 stdev TC 2 stdev TC 3 stdev TC 4 stdev
TC 5 stdev TC 6 stdev]);
    % Calculate the worst case random uncertainty for a single measurement
    P single = 2*stdev max; % t = 2, See example 7.3 in Wheeler and Ganji
    % Store the values from the log file in a structure
    TC DATA(counter).TC 0 raw = TC 0;
    TC DATA(counter).TC 0 avg = TC 0 avg;
    TC DATA(counter).TC 0 stdev = TC 0 stdev;
    TC DATA(counter).TC 0 corr = TC 0 corr;
    TC DATA(counter).TC 1 raw = TC 1;
    TC_DATA(counter).TC_1_avg = TC 1 avg;
    TC DATA(counter).TC 1 stdev = TC 1 stdev;
    TC DATA (counter).TC 1 corr = TC 1 corr;
    TC DATA(counter).TC 2 raw = TC 2;
    TC DATA(counter).TC 2 avg = TC 2 avg;
    TC_DATA(counter).TC_2_stdev = TC_2_stdev;
    TC_DATA(counter).TC_2_corr = TC_2_corr;
    TC DATA(counter).TC 3 raw = TC 3;
    TC_DATA(counter).TC_3_avg = TC_3_avg;
    TC_DATA(counter).TC_3_stdev = TC_3_stdev;
    TC DATA(counter).TC 3 corr = TC 3 corr;
    TC_DATA(counter).TC_4_raw = TC_4;
    TC_DATA(counter).TC_4_avg = TC_4_avg;
    TC DATA(counter).TC 4 stdev = TC 4 stdev;
    TC DATA(counter).TC 4 corr = TC 4 corr;
    TC_DATA(counter).TC_5_raw = TC_5;
    TC DATA(counter).TC 5 avg = TC 5 avg;
    TC DATA(counter).TC 5 stdev = TC 5 stdev;
    TC DATA(counter).TC 5 corr = TC 5 corr;
    TC DATA(counter).TC 6 raw = TC 6;
    TC DATA(counter).TC 6 avg = TC 6 avg;
    TC DATA(counter).TC 6 stdev = TC 6 stdev;
    TC_DATA(counter).TC_6_corr = TC_6_corr;
    TC DATA(counter).TC true = TC true;
    TC DATA(counter).P single = P single;
```

% Increment the counter variable

```
counter = counter + 1;
    % Update Wait Bar
    waitbar(counter / counter max)
end
close(WaitBar);
%% Fit Curves to Correction Terms
% Fit a curve to the correction terms. Each thermocouple gets its own
% curve. Could potentially use the R^2 value to quantify the systematic
% error.
TC 0 fit = fit([TC DATA.TC 0 avg]',[TC DATA.TC 0 corr]','poly3');
TC_1_fit = fit([TC_DATA.TC_1_avg]',[TC_DATA.TC_1_corr]','poly3');
TC_2_fit = fit([TC_DATA.TC_2_avg]',[TC_DATA.TC_2_corr]','poly3');
TC 3 fit = fit([TC DATA.TC 3 avg]',[TC DATA.TC 3 corr]','poly3');
TC 4 fit = fit([TC DATA.TC 4 avg]',[TC DATA.TC 4 corr]','poly3');
TC 5 fit = fit([TC DATA.TC 5 avg]',[TC DATA.TC 5 corr]','poly3');
TC 6 fit = fit([TC DATA.TC 6 avg]',[TC DATA.TC 6 corr]','poly3');
% Store the coefficients of the fitted curve equations in a structure
TC FIT COEFFICIENTS.TC 0 = coeffvalues(TC 0 fit);
TC FIT COEFFICIENTS.TC 1 = coeffvalues(TC 1 fit);
TC_FIT_COEFFICIENTS.TC_2 = coeffvalues(TC_2_fit);
TC_FIT_COEFFICIENTS.TC_3 = coeffvalues(TC_3_fit);
TC_FIT_COEFFICIENTS.TC_4 = coeffvalues(TC_4_fit);
TC FIT COEFFICIENTS.TC 5 = coeffvalues(TC 5 fit);
TC FIT COEFFICIENTS.TC 6 = coeffvalues(TC 6 fit);
% Display the worst case random uncertainty for a single measurement
D1 = ['Worst case random uncertainty for a single
measurement:',num2str(P single),' \circC'];
```

calibrate_TC.m

disp(D1);

function TC_calibrated = calibrate_TC(Ch_num,TC_raw,TC_FIT_COEFFICIENTS)
% Written by Connor Speer, December 2017
% This function adds correction terms, calculated via the fit coefficients,
% to a vector of input raw data and returns a vector of calibrated data.
%% Inputs
% Ch_num --> Channel number of the transducer. Must be the same as in the
% calibration data.
% P_raw --> raw temperature data in deg C.
% ABS_VAL_FIT_COEFFICIENTS --> 3rd order polynomial fit coefficients for
% correction terms
%% Outputs
% P_calibrated --> Calibrated temperature in deg C.
%% Calculate correction terms

```
if Ch num == 0
    p1 = TC FIT COEFFICIENTS.TC_0(1);
    p2 = TC_FIT_COEFFICIENTS.TC_0(2);
   p3 = TC FIT COEFFICIENTS.TC 0(3);
   p4 = TC FIT COEFFICIENTS.TC 0(4);
elseif Ch num == 1
   p1 = TC FIT COEFFICIENTS.TC 1(1);
   p2 = TC FIT COEFFICIENTS.TC 1(2);
    p3 = TC FIT COEFFICIENTS.TC 1(3);
    p4 = TC FIT COEFFICIENTS.TC 1(4);
elseif Ch num == 2
   p1 = TC FIT COEFFICIENTS.TC 2(1);
   p2 = TC FIT COEFFICIENTS.TC 2(2);
   p3 = TC FIT COEFFICIENTS.TC 2(3);
   p4 = TC FIT COEFFICIENTS.TC 2(4);
elseif Ch num == 3
    p1 = TC FIT COEFFICIENTS.TC 3(1);
    p2 = TC FIT COEFFICIENTS.TC 3(2);
    p3 = TC FIT COEFFICIENTS.TC 3(3);
   p4 = TC FIT COEFFICIENTS.TC 3(4);
elseif Ch num == 4
    p1 = TC FIT COEFFICIENTS.TC 4(1);
    p2 = TC FIT COEFFICIENTS.TC_4(2);
    p3 = TC_FIT_COEFFICIENTS.TC_4(3);
   p4 = TC FIT COEFFICIENTS.TC 4(4);
elseif Ch num == 5
   p1 = TC FIT COEFFICIENTS.TC 5(1);
   p2 = TC FIT COEFFICIENTS.TC 5(2);
   p3 = TC FIT COEFFICIENTS.TC 5(3);
    p4 = TC FIT COEFFICIENTS.TC 5(4);
elseif Ch num == 6
    p1 = TC FIT COEFFICIENTS.TC 6(1);
    p2 = TC FIT COEFFICIENTS.TC_6(2);
   p3 = TC FIT COEFFICIENTS.TC 6(3);
   p4 = TC FIT COEFFICIENTS.TC 6(4);
end
correction terms = p1.*TC raw.^3 + p2.*TC raw.^2 + p3.*TC raw + p4;
%% Apply correction terms
TC calibrated = TC raw + correction terms;
```

Futek_Torque_Calibration.m

```
function [Torque_Nm]...
 = Futek_Torque_Calibration(Torque_Voltage)
% Written by Connor Speer - October '17
% The Futek torque transducer was shipped with calibration documents from
% the factory. This function corrects raw data using the calibration
% information provided by Futek.
%% Inputs:
% Torque Voltage --> Column vector of voltages collected from the torque
```

```
% transducer in (V)
%% Outputs:
% Torque Nm --> Column vector of torques in (Nm) corresponding to the
% input voltages from the torque transducer.
%% Convert from voltage to torque
% Test data from the calibration certificate:
Cal Input Nm = [0.000; 1.695; 3.389; 5.084; 6.779; 8.474; 9.999; 0.000;
0.000; -1.695; -3.389; -5.084; -6.779; -8.474; -9.999; 0.000];
Cal Output V = [0.000; 0.846; 1.698; 2.543; 3.391; 4.238; 5.001; 0.013;
0.000; -0.846; -1.691; -2.536; -3.383; -4.231; -4.994; 0.001];
% Fit a linear polynomial to the calibration data.
Cal Data Fit = fit(Cal Output V,Cal Input Nm, 'poly1');
% Extract the coefficients of the linear fit
Cal Data Fit coeffs = coeffvalues(Cal Data Fit);
% Apply equation of fitted polynomial to calculate torque in (Nm)
Torque Nm = Torque Voltage*Cal Data Fit coeffs(1) + Cal Data Fit coeffs(2);
```

PCB_Pressure_Calibration.m

% (Nm)

```
function [Pa LW35041, Pa LW35042]...
    = PCB Pressure Calibration (Voltage LW35041, Voltage LW35042)
% Written by Connor Speer - October '17
% The PCB pressure transducers were shipped with calibration documents from
% the factory. This function corrects raw data using the calibration
% information provided by PCB.
%% Inputs:
% Voltage LW35041 --> Column vector of voltages collected from the
% transducer with LW35041 serial number in (V)
% Voltage LW35042 --> Column vector of voltages collected from the
% transducer with LW35042 serial number in (V)
%% Outputs:
% Pa LW35041 --> Column vector of pressures in (Pa) corresponding to the
% input voltages from the LW35041 transducer.
% Pa LW35042 --> Column vector of pressures in (Pa) corresponding to the
% input voltages from the LW35042 transducer.
% Use test data provided by PCB to convert raw voltages into pressure in
% (Pa).
%% LW35041 Transducer
% Preallocate space for the pressure column vector
Pa LW35041 = zeros(length(Voltage LW35041),1);
```

```
for i = 1:1:length(Voltage LW35041)
    % See what range of voltage it's in and use the corresponding
    % sensitivity to convert to pressure in (Pa).
    if Voltage LW35041(i) < 0.9
        Pa LW35041(i) = Voltage LW35041(i)*(1000000/3.602); %(Pa)
    elseif Voltage LW35041(i) >= 0.90001
        Pa LW35041(i) = Voltage LW35041(i)*(1000000/3.589); %(Pa)
    end
end
%% LW35042 Transducer
% Preallocate space for the pressure column vector
Pa LW35042 = zeros(length(Voltage LW35042),1);
for i = 1:1:length(Voltage LW35042)
    % See what range of voltage it's in and use the corresponding
    % sensitivity to convert to pressure in (Pa).
    if Voltage LW35042(i) < 0.9
        Pa LW35042(i) = Voltage LW35042(i)*(1000000/3.519); %(Pa)
    elseif Voltage LW35042(i) >= 0.90001
        Pa LW35042(i) = Voltage LW35042(i)*(1000000/3.512); %(Pa)
    end
end
```

Chapter 2

Chapter_2_Plots.m

```
% Chapter 2 Plots.m - Written by Connor Speer - October 2017
% Plot examples of raw data.
clear,clc,close all;
%% Cooling System Input Parameters
V dot Cooler = 0.800*1.66667e-5; % Cooler water volume flow rate [m^3/s]
V dot ConPipePowCyl = 0.200*1.66667e-5; % Connecting Pipe and Power Cylinder
water volume flow rate [m^3/s]
c water = 4184; % Specific heat capacity of water in [J/kgK]
dens water = 1000; % Water density [kg/m^3]
% Calculations
m dot Cooler = V dot Cooler*dens water; % Cooler water mass flow rate [kg/s]
m dot ConPipePowCyl = V dot ConPipePowCyl*dens water; % Connecting Pipe water
mass flow rate [kg/s]
%% Process Experimental Data
% 44 mm piston mod only
example data folder = 'X:\01 Current Students\Connor Speer\00 Thesis and
Journal Papers\00 Thesis\00 Data and Plots\Chapter 2 Plots\44mmCCDV Power
Tests';
EXAMPLE DATA = Process Data(example data folder);
```

```
%% Plot Set-Up
set(0, 'defaultfigurecolor', [1 1 1])
% Location of Figures
x = 500;
y = 500;
% Size of Figures
width = 550;
height = 400;
% Font For Figures
font = 'Arial';
font size = 11;
% % Location of Figures
% x = 500;
% y = 500;
8
% % Size of Figures
% width = 326;
% height = 275;
8
% % Font For Figures
% font = 'Times New Roman';
\% font size = 10;
% % Location of Figures
% x = 500;
% y = 500;
00
% % Size of Figures
% width = 550;
% height = 400;
00
% % Font For Figures
% font = 'Times New Roman';
% font size = 16;
% To change line width for plots, say "'LineWidth',2".
% To include math symbols with their own font size and font type in the
% axes labels, do this:
% xlabel({'\fontsize{11} Engine Speed \fontsize{11} \fontname{Cambria Math}
\omega \fontsize{11} \fontname{Times New Roman} [RPM]'});
% Here is the degree symbol in case you need it °C. Alternatively, use
% \circ.
```

```
%% Preliminary Data Plots
% Gas Temperatures vs. Time
figure('Position', [x y width height])
hold on
plot([EXAMPLE DATA(1).time TC],[EXAMPLE DATA(1).T 0],'.')
plot([EXAMPLE_DATA(1).time_TC],[EXAMPLE_DATA(1).T_1],'.')
plot([EXAMPLE DATA(1).time TC], [EXAMPLE DATA(1).T 2], '.')
plot([EXAMPLE DATA(1).time TC], [EXAMPLE DATA(1).T 3], '.')
plot([EXAMPLE DATA(1).time TC],[EXAMPLE DATA(1).T 4],'.')
plot([EXAMPLE DATA(1).time TC],[EXAMPLE DATA(1).T 5],'.')
plot([EXAMPLE_DATA(1).time_TC], [EXAMPLE_DATA(1).T_6],'.')
xlabel('Time (s)', 'FontName', font, 'FontSize', font size);
ylabel('Gas Temperatures (\circC)', 'FontName', font, 'FontSize', font size);
legend('Expansion Space', 'Regenerator Hot', 'Regenerator Cold Left',...
    'Regenerator Cold Right', 'Displacer Mount', 'Crankcase', 'Power
Cylinder', 'Location', 'East')
set(gca, 'fontsize', font size);
set(gca, 'FontName', font)
hold off
% Expansion Space Gas Temperature vs. Crank Angle
figure('Position', [x y width height])
hold on
theta deg TC = EXAMPLE DATA(1).theta deg(6:6:end);
plot(theta deg TC, [EXAMPLE DATA(1).T 0], '.')
xlabel('Crank Angle (\circ)', 'FontName', font, 'FontSize', font size);
ylabel('Expansion Space Gas Temperature
(\circC)', 'FontName', font, 'FontSize', font size);
set(gca, 'fontsize', font size);
set(gca, 'FontName', font)
% Water Temperatures vs. Time
figure('Position', [x y width height])
hold on
plot([EXAMPLE DATA(1).time RTD],[EXAMPLE DATA(1).RTD 0],'r.')
plot([EXAMPLE DATA(1).time RTD], [EXAMPLE DATA(1).RTD 1], 'b.')
plot([EXAMPLE DATA(1).time RTD], [EXAMPLE DATA(1).RTD 2], 'k.')
plot([EXAMPLE DATA(1).time RTD], [EXAMPLE DATA(1).RTD 3], 'q.')
xlabel('Time (s)', 'FontName', font, 'FontSize', font size);
ylabel('Water Temperatures (\circC)', 'FontName', font, 'FontSize', font_size);
legend('Cooler Inlet', 'Cooler Outlet', 'Con Pipe/Pow Cyl Inlet',...
    'Con Pipe/Pow Cyl Outlet', 'Location', 'East')
set(gca, 'fontsize', font size);
set(gca, 'FontName', font)
hold off
% Water Temperatures vs. Crank Angle
figure('Position', [x y width height])
theta deg RTD = EXAMPLE DATA(1).theta deg(300:300:end);
hold on
plot(theta deg RTD,[EXAMPLE DATA(1).RTD 0],'r.')
plot(theta deg RTD,[EXAMPLE DATA(1).RTD 1], 'b.')
plot(theta deg RTD,[EXAMPLE DATA(1).RTD 2],'k.')
plot(theta deg RTD,[EXAMPLE DATA(1).RTD 3],'g.')
xlabel('Crank Angle (\circ)', 'FontName', font, 'FontSize', font size);
```

```
ylabel('Water Temperatures (\circC)', 'FontName', font, 'FontSize', font size);
legend('Cooler Inlet', 'Cooler Outlet', 'Con Pipe/Pow Cyl Inlet',...
    'Con Pipe/Pow Cyl Outlet', 'Location', 'East')
set(gca, 'fontsize', font size);
set(gca, 'FontName', font)
hold off
% Rotary Encoder Outputs vs. Time
figure('Position', [x y width height])
hold on
plot([EXAMPLE DATA(1).time Volt],[EXAMPLE DATA(1).A],'r')
plot([EXAMPLE DATA(1).time Volt], [EXAMPLE DATA(1).Z], 'b')
xlabel('Time (s)', 'FontName', font, 'FontSize', font size);
ylabel('Voltage (V)', 'FontName', font, 'FontSize', font size);
xlim([0.23 0.26])
legend('A-Output', 'Z-Output')
set(gca, 'fontsize', font size);
set(gca, 'FontName', font)
hold off
% Pressure vs. Time for PCB and Validynes
figure('Position', [x y width height])
hold on
plot([EXAMPLE DATA(1).time Volt], [EXAMPLE DATA(1).P2 Pa], 'r.')
plot([EXAMPLE DATA(1).time Volt],[EXAMPLE DATA(1).P3 Pa],'g.')
plot([EXAMPLE DATA(1).time Volt],[EXAMPLE DATA(1).P4 Pa],'b.')
plot([EXAMPLE DATA(1).time Volt],[EXAMPLE DATA(1).P5 Pa],'k.')
xlabel('Time (s)','FontName',font,'FontSize',font size);
ylabel('Pressure (Pa)', 'FontName', font, 'FontSize', font size);
legend('Validyne Power Cylinder', 'Validyne Crankcase', PCB Power
Cylinder',...
    'PCB Crankcase', 'Location', 'East')
set(gca, 'fontsize', font size);
set(gca, 'FontName', font)
hold off
xlim([0 1])
% Pressure vs. Crank Angle for PCB and Validynes
figure('Position', [x y width height])
hold on
plot([EXAMPLE DATA(1).theta deg],[EXAMPLE DATA(1).P2 Pa],'r.')
plot([EXAMPLE DATA(1).theta deg],[EXAMPLE DATA(1).P3 Pa],'b.')
plot([EXAMPLE_DATA(1).theta_deg],[EXAMPLE_DATA(1).P4_Pa],'g.')
plot([EXAMPLE DATA(1).theta deg], [EXAMPLE DATA(1).P5 Pa], 'k.')
xlabel('Crank Angle (\circ)', 'FontName', font, 'FontSize', font size);
ylabel('Pressure (Pa)', 'FontName', font, 'FontSize', font size);
legend('Validyne Power Cylinder', 'Validyne Crankcase', PCB Power
Cylinder',...
    'PCB Crankcase', 'Location', 'East')
set(gca, 'fontsize', font size);
set(gca, 'FontName', font)
hold off
% Pressure vs. Crank Angle for Regenerator Differential Validyne
figure('Position', [x y width height])
plot([EXAMPLE DATA(1).time Volt],[EXAMPLE DATA(1).P1 Pa],'k.')
```

```
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```

```
xlabel('Time (s)', 'FontName', font, 'FontSize', font size);
ylabel('Regenerator Differential Pressure
(Pa)', 'FontName', font, 'FontSize', font size);
set(gca, 'fontsize', font size);
set(gca, 'FontName', font)
% Heater Control Signal vs. Time
% Torque vs. Time
figure('Position', [x y width height])
plot([EXAMPLE_DATA(1).time_Volt],[EXAMPLE_DATA(1).TOR],'.')
xlabel('Time (s)', 'FontName', font, 'FontSize', font size);
ylabel('Torque (Nm)', 'FontName', font, 'FontSize', font size);
set(gca, 'fontsize', font size);
set(gca, 'FontName', font)
xlim([0 2])
% Torque vs. Crank Angle
figure('Position', [x y width height])
plot([EXAMPLE DATA(1).theta deg],[EXAMPLE_DATA(1).TOR],'r.')
xlabel('Crank Angle (\circ)', 'FontName', font, 'FontSize', font_size);
ylabel('Torque (Nm)', 'FontName', font, 'FontSize', font size);
set(gca, 'fontsize', font size);
set(gca, 'FontName', font)
```

TC_Time_Constant.m

```
% TC Time Constant.m - Written by Connor Speer, November 2016
% Calculations based on example 4-1 in Cengel Heat and Mass Transfer pg 222
clear, clc, close all
%% Input Parameters
% Working gas properties (for air at 100 degC and 1 atm)
rho air = 0.9458; %(kg/m^3)
k air = 0.03095; % (W/mK)
Pr air = 0.7111; % No units.
mu inf = 2.181e-05; %(kg/ms)
mu s = 1.729e-05; %(kg/ms)
% Type K Thermocouple junction properties
% Chromel: http://www.matweb.com/search/datasheet.aspx?matguid=e14ca9c83c5
% f45dd945e655fa4edff8b
rho chromel = 8730; %(kg/m^3)
k chromel = 19.2; %(W/mK)
c chromel = 448; %(J/kgK)
% Alumel: http://www.matweb.com/search/DataSheet.aspx?MatGUID=c8c0b158524a
% 446bb953b781dee28efb
rho_alumel = 8610; %(kg/m^3)
k alumel = 29.7; %(W/mK)
c_alumel = 523; %(J/kgK)
```

```
% Diameter of thermocouple junction
D = 0.00077; \% (m)
% Average working gas velocity
v = 10:0.1:100; % (m/s)
%% Calculate Average Thermocouple Junction Properties
rho TC = (rho chromel+rho alumel)/2; %(kg/m^3)
k TC = (k chromel+k alumel)/2; %(W/mK)
c TC = (c chromel+c alumel)/2; %(J/kgK)
%% Calculate Reynolds Number
Re = rho air.*v.*D./mu inf;
%% Calculate Nusselt Number
% Whitaker correlation from page 413.
\% Valid for 3.5 < Re < 80 000 and 0.7 < Pr < 380.
Nu = 2 + (0.4.*(Re.^{0.5}) +
0.06.*(Re.^(2/3)))*(Pr air^0.4)*((mu inf/mu s)^0.25);
%% Calculate Convective Heat Transfer Coefficient
h = Nu.*k air./D; %(W/m^2K)
%% Calculate The Characteristic Length
Lc = (1/6) * D; % (m)
%% Calculate Biot Number
Bi = (h.*Lc)./k TC; % No units
%% Calculate The Exponent b
b = h./(rho TC*c TC*Lc); %(s^{-1})
%% Calculate Time Constant
% This is the time for the thermocouple junction to reach 99 % of the
% initial temperature difference for a step change in temperature.
t = -log(0.01)./b; %(s)
% % Display the time constant
% D1 = ['Thermocouple time constant for step change in temperature:
',num2str(t),' s'];
% disp(D1);
```

```
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```

%% Plots

```
set(0,'defaultfigurecolor',[1 1 1])
% Location of Figures
x = 500;
y = 500;
% Size of Figures
width = 550;
height = 400;
% Font For Figures
font = 'Arial';
font size = 11;
% % Location of Figures
% x = 500;
% y = 500;
0
% % Size of Figures
% width = 326;
% height = 275;
8
% % Font For Figures
% font = 'Times New Roman';
% font size = 10;
% % Location of Figures
% x = 500;
% y = 500;
0
% % Size of Figures
% width = 550;
% height = 400;
00
% % Font For Figures
% font = 'Times New Roman';
% font size = 16;
% To change line width for plots, say "'LineWidth',2".
% To include math symbols with their own font size and font type in the
% axes labels, do this:
% xlabel({'\fontsize{11} Engine Speed \fontsize{11} \fontname{Cambria Math}
\omega \fontsize{11} \fontname{Times New Roman} [RPM]'});
% Here is the degree symbol in case you need it °C. Alternatively, use
% \circ.
```

```
figure('Position', [x y width height])
hold on
plot(v,t,'LineWidth',2)
plot(v,repelem(0.6,length(t)),'LineWidth',2);
xlabel('Working Gas Velocity,
  (m/s)','FontName',font,'FontSize',font_size)
ylabel('Time, (s)','FontName',font,'FontSize',font_size)
legend('Thermocouple Response Time','Cycle time at 100 RPM')
hold off
```

Uncertainty_Propagation.m

```
% Uncertainty Propagation.m - Written by Connor Speer, October 2017
% Calculate uncertainty propagation for calculated quantities.
clear, clc, close all;
%% Input Parameters
w TOR = 0.1; % Uncertainty in torque (Nm)
TOR = 2; % Maximum measured value of torque (Nm)
w theta = 5*(pi/180); % Uncertainty in crank position (rad)
w t = 0.001; % Uncertainty in time elapsed (sec)
t pow = 10; % Maximum time elapsed for power measurement (s)
W dot shaft = 10; % Maximum measured shaft power in (W)
ang freq = 31.4; % Maximum measured angular frequency (rad/s)
w V dot = 1.6666667e-8; % Uncertainty in water volume flow rate (m^3/s)
V dot = 1.3333e-5; % Maximum coolant volume flow rate in (m^3/s)
w rho water = 5; % Uncertainty in water density (kg/m^3)
rho water = 1000; % Maximum water density (kg/m^3)
w c water = 5; % Uncertainty in water specific heat capacity (J/kgK)
c water = 4184; % Maximum water specific heat capacity (J/kgK)
Tdrop water = 5; % Maximum water temperature drop (K)
Q dot in = 500; % Maximum measured heat input rate (W)
t eff = 1800; % Maximum time elapsed for power measurement (s)
Q dot rej = 400; % Maximum measured heat rejection rate (W)
w I heater = 0.4; % Uncertainty in heater current (Amps)
I heater = 16.5; % Maximum measured heater current (Amps)
w R heater = 1; % Uncertainty in heater resistance (Ohms)
R heater = 12.088; % Uncertainty in heater resistance (Ohms)
t on = 280; % Maximum amount of time heater is on (s)
P heater = 3250; % Maximum power consumption of heater (W)
OnFrac = 0.156; % Maximum fraction of time heater is on (unitless)
w TC = 0.01; % Uncertainty in gas temperatures, differential measurement (K)
w RTD = 0.01; % Uncertainty in water temperatures, differential measurement
(K)
```

```
w p Val = 270; % Uncertainty in Validyne absolute pressure (Pa)
w p Diff = 170; % Uncertainty in Validyne differential pressure (Pa)
w p PCB = 5010; % Uncertainty in PCB absolute pressure (Pa)
% w delta theta = 5*(pi/180); % Uncertainty in crank angle difference (rad)
%% Relative Uncertainties in Calculated Quantities
% Gas Temperature Drop
w_Tdrop_gas = sqrt(2) *w TC; %(deg C)
% Water Temperature Drop
w Tdrop water = sqrt(2) *w RTD; %(deg C)
% Engine Frequency
w ang freq = sqrt((w theta/t pow)^2 + (w t/(t pow^2))^2); (rad/s)
% Shaft Power
w W dot shaft = W dot shaft*sqrt((w TOR/TOR)^2 + (w ang freq/ang freq)^2);
8(W)
% Heat Rejection Rate
w Q dot rej = Q dot rej*sqrt((w V dot/V dot)^2 + (w rho water/rho water)^2 +
    (w c water/c water)^2 + (w Tdrop water/Tdrop water)^2); % (unitless)
% Heater Power Consumption
w Pheater = sqrt((w I heater*2*I heater*R heater)^2 +
(\overline{W} \ R \ heater*(I \ heater^2))^2); \& (\overline{W})
% Fraction of time heater is on
w OnFrac = sqrt((w t/t eff)^2 + (w t*(t on/(t eff^2)))^2); %(unitless)
% Heat Input Rate
w Q dot in = Q dot in*sqrt((w Pheater/P heater)^2 + (w OnFrac/OnFrac)^2);
%(W)
% Efficiency
w eff thermal = sqrt((w W dot shaft/Q dot in)^2 + ...
    (w Q dot in*(W dot shaft/(Q dot in^2)))^2); %(unitless)
% Gas Temperature Drop
Unc Tdrop gas = sqrt(2) *w TC; % (deg C)
% Water Temperature Drop
Unc Tdrop water = sqrt(2) *w RTD; % (deg C)
% Engine frequency (Hz)
RelUnc freq = sqrt((w delta theta*(1/(360*t pow)))^2 + \dots
    ((w t*delta theta)/(360*t pow^2))^2); %(unitless)
```

Chapter 4

Chapter_4_Plots.m

% Compare the effect of the 3 modifications on the engine performance.

% Chapter 4 Plots.m - Written by Connor Speer - October 2017

clear,clc,close all;

%% Cooling System Input Parameters V_dot_Cooler = 0.800*1.66667e-5; % Cooler water volume flow rate [m^3/s] V_dot_ConPipePowCyl = 0.200*1.66667e-5; % Connecting Pipe and Power Cylinder water volume flow rate [m^3/s] c_water = 4184; % Specific heat capacity of water in [J/kgK] dens water = 1000; % Water density [kg/m^3]

% Calculations m_dot_Cooler = V_dot_Cooler*dens_water; % Cooler water mass flow rate [kg/s] m_dot_ConPipePowCyl = V_dot_ConPipePowCyl*dens_water; % Connecting Pipe water mass flow rate [kg/s]

```
%% Process Experimental Data
% 44 mm piston mod only
prelim_log_file_folder_44mm = 'X:\01_Current_Students\Connor Speer\00_Thesis
and Journal Papers\00_Thesis\00_Data and Plots\Chapter 4 Plots (Mod
Comparison)\Power Tests\Prelim Mod Comparison\44mm';
PRELIM_DATA_44mm = Process_Data(prelim_log_file_folder_44mm);
```

% 44 mm piston mod and crankcase extension prelim_log_file_folder_44mmCC = 'X:\01_Current_Students\Connor Speer\00_Thesis and Journal Papers\00_Thesis\00_Data and Plots\Chapter 4 Plots (Mod Comparison)\Power Tests\Prelim Mod Comparison\44mmCC'; PRELIM_DATA_44mmCC = Process_Data(prelim_log_file_folder_44mmCC);

% 44 mm piston mod, crankcase extension, and dead volume reduction prelim_log_file_folder_44mmCCDV = 'X:\01_Current_Students\Connor Speer\00_Thesis and Journal Papers\00_Thesis\00_Data and Plots\Chapter 4 Plots (Mod Comparison)\Power Tests\Prelim Mod Comparison\44mmCCDV'; PRELIM DATA 44mmCCDV = Process Data(prelim log file folder 44mmCCDV);

```
% All three mods
log_file_folder_44mmCCDV = 'X:\01_Current_Students\Connor Speer\00_Thesis and
Journal Papers\00_Thesis\00_Data and Plots\Chapter 4 Plots (Mod
Comparison)\Power Tests\44mmCCDV Power Tests';
DATA_44mmCCDV = Process_Data(log_file_folder_44mmCCDV);
```

```
% No dead volume mod
log_file_folder_44mmCC = 'X:\01_Current_Students\Connor Speer\00_Thesis and
Journal Papers\00_Thesis\00_Data and Plots\Chapter 4 Plots (Mod
Comparison)\Power Tests\44mmCC Power Tests';
DATA 44mmCC = Process Data(log file folder 44mmCC);
```

```
% Loaded cool down, all mods
loaded cool folder 44mmCCDV = 'X:\01 Current Students\Connor Speer\00 Thesis
and Journal Papers\00 Thesis\00 Data and Plots\Chapter 4 Plots (Mod
Comparison) \Cool Down Tests \Cool Down with Load (All Mods) ';
LOADED COOL 44mmCCDV = Process Data(loaded cool folder 44mmCCDV);
%% Plot Set-Up
set(0, 'defaultfigurecolor', [1 1 1])
% Location of Figures
x = 500;
y = 500;
% Size of Figures
width = 550;
height = 400;
% Font For Figures
font = 'Arial';
font size = 11;
$$$$$$
% % Location of Figures
% x = 500;
% y = 500;
0
% % Size of Figures
% width = 326;
% height = 275;
8
% % Font For Figures
% font = 'Times New Roman';
% font size = 10;
% % Location of Figures
% x = 500;
% y = 500;
8
% % Size of Figures
% width = 550;
% height = 400;
% % Font For Figures
% font = 'Times New Roman';
% font size = 16;
% To change line width for plots, say "'LineWidth',2".
```

```
% To include math symbols with their own font size and font type in the
% axes labels, do this:
% xlabel({'\fontsize{11} Engine Speed \fontsize{11} \fontname{Cambria Math}
\omega \fontsize{11} \fontname{Times New Roman} [RPM]'});
% Here is the degree symbol in case you need it °C. Alternatively, use
% \circ.
save Calibrated Data for Chapter 4 Plots.mat
%% As Built Data Plots
% % Import data from text file.
% % Script for importing data from the following text file:
8 8
8 8
      X:\04 Stirling Engine\04 Experiments\03 High Temp Gamma\004 HTG Test
Data April 3 - 2017\019 P150 TH500 TL5 0 Temp.log
8 8
% % To extend the code to different selected data or a different text file,
% % generate a function instead of a script.
2
% % Auto-generated by MATLAB on 2017/04/04 17:05:54
2
% % Initialize variables.
% filename = 'X:\01 Current Students\Connor Speer\00 Thesis and Journal
Papers\00 Thesis\00 Data and Plots\Chapter 4 Plots (Mod Comparison)\As-Built
Cool Down Run\P60 THCOOL TL21 14 Temp.log';
% delimiter = '\t';
\% startRow = 6;
2
% % Format for each line of text:
% % column1: double (%f)
% % column2: double (%f)
% % column3: double (%f)
% % column4: double (%f)
% % column5: double (%f)
% % column6: double (%f)
% % column7: double (%f)
% % column8: double (%f)
% % column9: double (%f)
% % column10: double (%f)
% % column11: double (%f)
% % column12: double (%f)
% % column13: double (%f)
% % column14: double (%f)
% % For more information, see the TEXTSCAN documentation.
0
% % Open the text file.
% fileID = fopen(filename, 'r');
0
% % Read columns of data according to the format.
% % This call is based on the structure of the file used to generate this
% % code. If an error occurs for a different file, try regenerating the code
% % from the Import Tool.
```

```
% dataArray = textscan(fileID, formatSpec, 'Delimiter', delimiter,
'TextType', 'string', 'EmptyValue', NaN, 'HeaderLines', startRow-1,
'ReturnOnError', false, 'EndOfLine', '\r\n');
8
% % Close the text file.
% fclose(fileID);
% % Post processing for unimportable data.
% % No unimportable data rules were applied during the import, so no post
% % processing code is included. To generate code which works for
% % unimportable data, select unimportable cells in a file and regenerate the
% % script.
00
% % Allocate imported array to column variable names
% T 0 = dataArray{:, 1};
% T 1 = dataArray{:, 2};
% T_2 = dataArray{:, 3};
% T_3 = dataArray{:, 4};
% T 4 = dataArray{:, 5};
% T 5 = dataArray{:, 6};
% T 6 = dataArray{:, 7};
% T 7 = dataArray{:, 8};
% T 8 = dataArray{:, 9};
% T 9 = dataArray{:, 10};
% T 10 = dataArray{:, 11};
% T 11 = dataArray{:, 12};
% T 12 = dataArray{:, 13};
% T<sup>13</sup> = dataArray{:, 14};
0
8
% % Clear temporary variables
% clearvars filename delimiter startRow formatSpec fileID dataArray ans;
00
% % Import data from text file.
% % Script for importing data from the following text file:
e e
       X:\04 Stirling Engine\04 Experiments\03 High Temp Gamma\004 HTG Test
Data April 3 - 2017\020 P150 TH500 TL5 0 Volt.log
000
% % To extend the code to different selected data or a different text file,
% % generate a function instead of a script.
8
% % Auto-generated by MATLAB on 2017/04/04 17:06:42
2
% % Initialize variables.
% filenameP = 'X:\01 Current Students\Connor Speer\00 Thesis and Journal
Papers\00 Thesis\00 Data and Plots\Chapter 4 Plots (Mod Comparison)\As-Built
Cool Down Run\P60 THCOOL TL21 14 Volt.log';
% delimiter = '\t';
% startRow = 6;
0
% % Format for each line of text:
% % column1: double (%f)
% % column2: double (%f)
% % column3: double (%f)
% % column4: double (%f)
% % column5: double (%f)
```

```
% % column6: double (%f)
% % column7: double (%f)
% % column8: double (%f)
% % For more information, see the TEXTSCAN documentation.
% formatSpec = '%f%f%f%f%f%f%f%f%f%f%f%[^\n\r]';
8
% % Open the text file.
% fileID = fopen(filenameP,'r');
0
% % Read columns of data according to the format.
\% % This call is based on the structure of the file used to generate this
% % code. If an error occurs for a different file, try regenerating the code
% % from the Import Tool.
% dataArray = textscan(fileID, formatSpec, 'Delimiter', delimiter,
'TextType', 'string', 'EmptyValue', NaN, 'HeaderLines', startRow-1,
'ReturnOnError', false, 'EndOfLine', '\r\n');
8
% % Close the text file.
% fclose(fileID);
00
% % Post processing for unimportable data.
% % No unimportable data rules were applied during the import, so no post
% % processing code is included. To generate code which works for
% % unimportable data, select unimportable cells in a file and regenerate the
% % script.
90
% % Allocate imported array to column variable names
% A = dataArray{:, 1};
% Z = dataArray{:, 2};
% TOR = dataArray{:, 3};
% P1 = dataArray{:, 4}; % Regenerator Differential Pressure
% P2 = dataArray{:, 5}; % Displacer Mount
% P3 = dataArray{:, 6}; % Power Piston
% P4 = dataArray{:, 7}; % Crankcase
% P5 = dataArray{:, 8}; % Expansion Space
2
% % Collect the Start and End Times of the log file
% volt log file = fileread(filenameP);
% start index = regexp(volt log file, 'Start');
% end index = regexp(volt log file, 'End');
% start line = volt log file(start index:end index-1);
% end line = volt log file(end index:end index+14);
% [token start, remain start] = strtok(start line);
% [token end, remain end] = strtok(end line);
% start time = str2double(strip(remain start));
% end time = str2double(strip(remain end));
00
% % Clear temporary variables
% clearvars filenameP delimiter startRow formatSpec fileID dataArray ans;
2
% % Find reference pulse in Z output
% threshold = 3;
% ref pulse = find(Z > threshold, 1);
0
```

```
% % Work backwards from reference pulse to find pulse counts
% if A(ref pulse) > 2.5
    pulse flag = 1;
00
% else
00
    pulse flag = 0;
% end
2
% A count = zeros(size(A));
00
% bwd counter = 500;
% row = ref pulse - 1;
8
% while row ~= 0
00
    if pulse flag == 0 && A(row) < 2.5
%
       bwd counter = bwd counter - 1;
8
    end
8
8
    if bwd counter == -1
00
   bwd counter = 500;
00
   end
00
00
    A count(row) = bwd counter;
00
8
    if A(row) < 2.5
8
       pulse flag = 1;
8
    else
8
        pulse flag = 0;
8
    end
00
    row = row - 1;
% end
8
% % Work forwards from reference pulse to find pulse counts
% if A(ref pulse) > 2.5
8
    pulse flag = 1;
% else
8
    pulse flag = 0;
% end
00
% fwd counter = 0;
00
% for row = ref pulse:length(A)
8
     if pulse flag == 0 && A(row) > 2.5
        fwd counter = fwd counter + 1;
8
8
    end
00
00
    if fwd counter == 501
00
    fwd counter = 0;
00
    end
00
%
    A count(row) = fwd counter;
9
8
    if A(row) > 2.5
       pulse flag = 1;
8
8
    else
```

```
2
      pulse flag = 0;
00
   end
% end
0
% % Use pulse count to calculate crank angles
% crank angle = A count*(360/500); % [deg]
0
% % Calculate Crankshaft Speed
2
\% refs = find(A < 0.5);
0
% % Initialize variables
% pulse count = 0;
2
% for inc = 1:(length(refs)-1)
8
   if refs(inc+1) ~= (refs(inc) + 1)
2
      pulse count = pulse count + 1;
8
   end
% end
00
% Engine Freq = ((pulse count/(end time-start time))/500)*(2*pi); % [rad/sec]
% Engine RPM = Engine Freq*(60/(2*pi)); % [rev/min]
00
% % Average the Crank Angles and Pressures
% [avg_P1] = PV_data_avg(crank_angle*(pi/180),P1);
% [avg P2] = PV data avg(crank angle*(pi/180),P2);
% [avg P3] = PV data avg(crank angle*(pi/180),P3);
% [avg P4] = PV data avg(crank angle*(pi/180),P4);
% [avg P5] = PV data avg(crank angle*(pi/180),P5);
2
% % Convert pressures and average pressures into units of bar
% p scale = 20*0.0689476;
% P1 bar = P1.*p scale;
% P2 bar = P2.*p scale;
% P3 bar = P3.*p scale;
% P4 bar = P4.*p scale;
% P5 bar = P5.*p scale;
2
% P1 avg bar = avg P1.*p scale;
% P2 avg bar = avg P2.*p scale;
% P3 avg bar = avg P3.*p scale;
% P4 avg bar = avg P4.*p scale;
% P5 avg bar = avg P5.*p scale;
0
% % Use crank angles to calculate volumes
% % Gamma Engine Input Parameters
% % Dr1 --> Displacer desaxe offset in [m]
```

```
% % Dr2 --> Displacer crank length in [m]
% % Dr3 --> Displacer connecting rod length in [m]
% % Dbore --> Displacer bore in [m]
% % Pr1 --> Piston desaxe offset in [m]
% % Pr2 --> Piston crank length in [m]
% % Pr3 --> Piston connecting rod length in [m]
% % Pbore --> Piston bore in [m]
% % Vdead --> Total dead volume in [m^3]
% % beta deg --> Phase angle advance of displacer motion over piston motion
[degrees]
2
% % Input Parameters for HTG Engine
% Dr1 = 0; %[m]
% Dr2 = 0.0375; %[m]
% Dr3 = 0.130; %[m]
% Dbore = 0.096; %[m]
% Pr1 = 0; %[m]
% Pr2 = 0.0375; %[m]
% Pr3 = 0.156; %[m]
% Pbore = 0.085; %[m]
% Vdead = 876.79*1e-6; %[m^3]
% V crankcase max = 0.0032; %[m^3]
% beta deg = 90; %[degrees]
8
% % We use the equations from Cleghorn's "Mechanics of Machines" to determine
% % the volume variations here. Cleghorn defines his angle differently, so
% % here we switch to theta Cleghorn
% theta Cleghorn = pi - crank angle*(pi/180); % [rad]
0
% % Calculate Volumes
% beta = beta deg*(pi/180);
2
% Dtheta3 = pi - asin((-Dr1+(Dr2*sin(theta Cleghorn+beta)))/Dr3);
% Dr4 = Dr2*cos(theta Cleghorn+beta) - Dr3*cos(Dtheta3);
% Dr4max = sqrt(((Dr2+Dr3)^2)-(Dr1^2));
% Ve = ((pi/4)*(Dbore^2))*(Dr4max-Dr4);
% DVc = (((pi/4)*(Dbore^2))*2*Dr2) - Ve;
8
% Ptheta3 = pi - asin((-Pr1+(Pr2*sin(theta Cleqhorn)))/Pr3);
% Pr4 = Pr2*cos(theta Cleqhorn) - Pr3*cos(Ptheta3);
% Pr4max = sqrt(((Pr2+Pr3)^2)-(Pr1^2));
% PVc = (((pi/4)*(Pbore^2))*(Pr4max-Pr4));
% Vc = DVc + PVc;
% Pr4min = sqrt(((Pr3-Pr2)^2)-(Pr1^2));
% Pstroke = Pr4max - Pr4min;
8
% Vtotal = Vdead + (((pi/4)*(Dbore^2))*2*Dr2) + PVc;
2
% % Crankcase Volume Variations
% V crankcase = V crankcase max - ((Pr4max-Pr4)*(((pi/4)*(Pbore^2))));
00
% % Calculate volumes at rounded crank angles to go with average pressures
% crank angle rounded deg = 0:1:359; %[deg]
% theta Cleqhorn rounded = pi - crank angle rounded deg.*(pi/180); %[rad]
% Dtheta3 rounded = pi - asin((-
Dr1+(Dr2*sin(theta Cleghorn rounded+beta)))/Dr3);
```

```
% Dr4 rounded = Dr2*cos(theta Cleghorn rounded+beta) -
Dr3*cos(Dtheta3 rounded);
% Ve rounded = ((pi/4)*(Dbore^2))*(Dr4max-Dr4 rounded);
% DVc rounded = (((pi/4)*(Dbore^2))*2*Dr2) - Ve rounded;
00
% Ptheta3 rounded = pi - asin((-Pr1+(Pr2*sin(theta Cleghorn rounded)))/Pr3);
% Pr4 rounded = Pr2*cos(theta Cleghorn rounded) - Pr3*cos(Ptheta3 rounded);
% PVc rounded = (((pi/4)*(Pbore^2))*(Pr4max-Pr4 rounded));
% Vc rounded = DVc rounded + PVc rounded;
0
% Vtotal rounded = Vdead + (((pi/4)*(Dbore^2))*2*Dr2) + PVc rounded;
% Vtotal rounded = Vtotal rounded(:);
8
% % Calculate Experimental Indicated Work and Power
% W ind = polyarea(Vtotal rounded, P3 avg bar*100000);
% P ind = W ind*(Engine RPM/60);
8
8
% % Make Experimental Forced Work Plot
% [W ind, FW, W shaft] = ...
% FW Subfunction v3(1,P3 avg_bar.*100000, ...
% flipud(P4 avg bar.*100000),Vtotal_rounded,0.7, 1);
%% Modeling of Modifications
% % Forced Work Plot Comparison for Reduced Piston Diameter
% % 85 mm piston
% ENGINE DATA = HTG ENGINE DATA;
% ENGINE DATA.Pbore = 0.085;
% ENGINE DATA.V buffer max = 0.0032;
% ENGINE DATA.Vclp = 1.733e-04;
% ENGINE DATA.GSH config = 1;
% ENGINE DATA.Tsource = 273 + 200;
% ENGINE DATA.Tge = 273 + 200;
% ENGINE DATA.Tgh = 273 + 200;
% ENGINE DATA.Twh = 273 + 200;
2
% [SECOND ORDER DATA, REF CYCLE DATA, LOSSES DATA] ...
         = HTG 2nd Order (ENGINE_DATA);
2
8
% % 44 mm piston
% ENGINE DATA = HTG ENGINE DATA;
% ENGINE DATA.Pbore = 0.044;
% ENGINE DATA.V buffer max = 0.0032;
% ENGINE DATA.Vclp = 1.733e-04;
% ENGINE DATA.GSH config = 1;
% ENGINE DATA.Tsource = 273 + 200;
% ENGINE DATA.Tge = 273 + 200;
% ENGINE DATA.Tqh = 273 + 200;
% ENGINE DATA.Twh = 273 + 200;
8
% [SECOND ORDER DATA, REF CYCLE DATA, LOSSES DATA] ...
2
         = HTG 2nd Order (ENGINE DATA);
8
% % Effect of DV Reduction Components
% % 44 mm piston, extended crankcase, no DV reduction
```

```
% ENGINE DATA = HTG ENGINE DATA;
% ENGINE DATA.Pbore = 0.044;
% ENGINE DATA.V buffer max = 0.0032 + 0.004633333;
% ENGINE DATA.Vclp = 1.733e-04;
% ENGINE DATA.GSH config = 1;
% ENGINE DATA.Tsource = 273 + 200;
% ENGINE DATA.Tge = 273 + 200;
% ENGINE DATA.Tgh = 273 + 200;
% ENGINE DATA.Twh = 273 + 200;
2
% [SECOND ORDER DATA, REF CYCLE DATA, LOSSES DATA] ...
2
          = HTG 2nd Order (ENGINE DATA);
8
% Pswing NoDV = max([REF_CYCLE_DATA.p]) - min([REF_CYCLE_DATA.p]);
% TswingExp NoDV = max([REF CYCLE DATA.Tge]) - min([REF CYCLE DATA.Tge]);
% deltaTeffective NoDV = mean([REF CYCLE DATA.Tge]) -
mean([REF CYCLE DATA.Tgc]);
8
8
% % 44 mm piston, extended crankcase, DV reduction
% ENGINE DATA = HTG ENGINE DATA;
% ENGINE DATA.Pbore = 0.044;
% ENGINE DATA.V buffer max = 0.0032 + 0.004633333;
% ENGINE DATA.Vclp = 1.733e-04 - 0.000132;
% ENGINE DATA.GSH config = 1;
% ENGINE DATA.Tsource = 273 + 200;
% ENGINE DATA.Tge = 273 + 200;
% ENGINE DATA.Tqh = 273 + 200;
% ENGINE DATA.Twh = 273 + 200;
8
% [SECOND ORDER DATA DV, REF CYCLE DATA DV, LOSSES DATA DV] ...
8
          = HTG 2nd Order (ENGINE DATA);
8
% Pswing DV = max([REF CYCLE DATA DV.p]) - min([REF CYCLE DATA DV.p]);
% TswingExp DV = max([REF CYCLE DATA DV.Tge]) - min([REF CYCLE DATA DV.Tge]);
% deltaTeffective DV = mean([REF CYCLE DATA DV.Tge]) -
mean([REF CYCLE DATA DV.Tqc]);
%% Preliminary Modification Data Plots
% Torque vs. Frequency for Several Mean Pressures
figure('Position', [x y width height])
hold on
pointsize = 30;
scatter([PRELIM DATA 44mm.Engine Hz], [PRELIM DATA 44mm.Torque avg],
pointsize, [PRELIM DATA 44mm.pmean]./1000, 'o')
scatter([PRELIM DATA 44mmCC.Engine Hz], [PRELIM DATA 44mmCC.Torque avg],
pointsize, [PRELIM DATA 44mmCC.pmean]./1000,'*')
scatter([PRELIM DATA 44mmCCDV.Engine Hz], [PRELIM DATA 44mmCCDV.Torque avg],
pointsize, [PRELIM DATA 44mmCCDV.pmean]./1000,'x')
ylim([0 inf])
xlabel('Engine Frequency (Hz)', 'FontName', font, 'FontSize', font size);
ylabel('Torque (Nm)', 'FontName', font, 'FontSize', font size);
c = colorbar;
ylabel(c,'Mean Pressure (kPa)','FontName',font,'FontSize',font size)
colormap(jet)
legend('44 mm Piston', 'Crankcase Extension', 'Dead Volume Reduction')
set(gca, 'fontsize', font size);
```

```
set(gca, 'FontName', font)
hold off
% Power vs. Frequency for Several Mean Pressures
figure('Position', [x y width height])
hold on
pointsize = 30;
scatter([PRELIM DATA 44mm.Engine Hz], [PRELIM DATA 44mm.P shaft], pointsize,
[PRELIM DATA 44mm.pmean]./1000, 'o')
scatter([PRELIM DATA 44mmCC.Engine Hz],[PRELIM DATA 44mmCC.P shaft],
pointsize, [PRELIM DATA 44mmCC.pmean]./1000, '*')
scatter([PRELIM DATA 44mmCCDV.Engine Hz], [PRELIM DATA 44mmCCDV.P shaft],
pointsize, [PRELIM DATA 44mmCCDV.pmean]./1000, 'x')
ylim([0 3.5])
xlabel('Engine Frequency (Hz)', 'FontName', font, 'FontSize', font size);
ylabel('Shaft Power (W)', 'FontName', font, 'FontSize', font size);
c = colorbar;
ylabel(c,'Mean Pressure (kPa)','FontName',font,'FontSize',font size)
colormap(jet)
legend('44 mm Piston', 'Crankcase Extension', 'Dead Volume Reduction')
set(gca, 'fontsize', font size);
set(gca, 'FontName', font)
hold off
% Speed vs. Pressure
figure('Position', [x y width height])
hold on
plot([PRELIM DATA 44mm.pmean]./1000, [PRELIM DATA 44mm.Engine Hz], 'o')
plot([PRELIM DATA 44mmCC.pmean]./1000, [PRELIM DATA 44mmCC.Engine Hz], '*')
plot([PRELIM DATA 44mmCCDV.pmean]./1000,[PRELIM DATA 44mmCCDV.Engine Hz],'x')
xlabel('Mean Pressure (kPa)', 'FontName', font, 'FontSize', font size)
ylabel('Engine Frequency (Hz)', 'FontName', font, 'FontSize', font_size)
legend('44 mm Piston','Crankcase Extension','Dead Volume
Reduction', 'Location', 'NorthWest')
set(gca, 'fontsize', font size);
set(gca, 'FontName', font)
hold off
% Indicated Power vs. Speed for Several Mean Pressures
figure('Position', [x y width height])
pointsize = 30;
hold on
scatter([PRELIM DATA 44mm.Engine Hz],[PRELIM DATA 44mm.P ind PCB], pointsize,
[PRELIM DATA 44mm.pmean]./1000, 'o')
scatter([PRELIM DATA 44mmCC.Engine Hz], [PRELIM DATA 44mmCC.P ind PCB],
pointsize, [PRELIM DATA 44mmCC.pmean]./1000, '*')
scatter([PRELIM DATA 44mmCCDV.Engine Hz], [PRELIM DATA 44mmCCDV.P ind PCB],
pointsize, [PRELIM DATA 44mmCCDV.pmean]./1000,'x')
ylim([0 inf])
xlabel('Engine Frequency (Hz)', 'FontName', font, 'FontSize', font size)
ylabel('Indicated Power (W)', 'FontName', font, 'FontSize', font size);
c = colorbar;
ylabel(c,'Mean Pressure (kPa)','FontName',font,'FontSize',font size)
colormap(jet)
legend('44 mm Piston', 'Crankcase Extension', 'Dead Volume
Reduction', 'Location', 'SouthEast')
```

```
set(gca,'fontsize',font size);
set(gca, 'FontName', font)
hold off
% Crankcase Gas Spring Hysteresis Loss vs. Speed for Several Mean Pressures
figure('Position', [x y width height])
pointsize = 30;
hold on
scatter([PRELIM DATA 44mm.Engine Hz], [PRELIM DATA 44mm.P GSH Loss PCB],
pointsize, [PRELIM DATA 44mm.pmean]./1000, 'o')
scatter([PRELIM DATA 44mmCC.Engine Hz], [PRELIM DATA 44mmCC.P GSH Loss PCB],
pointsize, [PRELIM DATA 44mmCC.pmean]./1000, '*')
scatter([PRELIM DATA 44mmCCDV.Engine Hz], [PRELIM DATA 44mmCCDV.P GSH Loss PCB
], pointsize, [PRELIM DATA 44mmCCDV.pmean]./1000,'x')
xlabel('Engine Frequency (Hz)', 'FontName', font, 'FontSize', font size)
ylabel('Crankcase Gas Spring Hysteresis Loss
(W) ', 'FontName', font, 'FontSize', font size);
c = colorbar;
ylabel(c,'Mean Pressure (kPa)','FontName',font,'FontSize',font size)
colormap(jet)
legend('44 mm Piston','Crankcase Extension','Dead Volume
Reduction', 'Location', 'NorthWest')
set(gca, 'fontsize', font size);
set(gca, 'FontName', font)
hold off
% Experimental Forced Work vs. Speed for Several Mean Pressures
figure('Position', [x y width height])
pointsize = 30;
hold on
scatter([PRELIM DATA 44mm.Engine Hz], [PRELIM DATA 44mm.Exp FW], pointsize,
[PRELIM DATA 44mm.pmean]./1000, 'o')
scatter([PRELIM DATA 44mmCC.Engine Hz], [PRELIM DATA 44mmCC.Exp FW],
pointsize, [PRELIM DATA 44mmCC.pmean]./1000, '*')
scatter([PRELIM DATA 44mmCCDV.Engine Hz], [PRELIM DATA 44mmCCDV.Exp FW],
pointsize, [PRELIM DATA 44mmCCDV.pmean]./1000,'x')
xlabel('Engine Frequency (Hz)', 'FontName', font, 'FontSize', font size)
ylabel('Experimental Forced Work (J)', 'FontName', font, 'FontSize', font size);
c = colorbar;
ylabel(c,'Mean Pressure (kPa)','FontName',font,'FontSize',font size)
colormap(jet)
legend('44 mm Piston', 'Crankcase Extension', 'Dead Volume
Reduction', 'Location', 'NorthWest')
set(qca, 'fontsize', font size);
set(gca, 'FontName', font)
hold off
% Indicator Diagrams Before and After Crankcase Extension
figure('Position', [x y width height])
hold on
plot([PRELIM DATA 44mm(33).Vtotal rounded], [PRELIM DATA 44mm(33).p engine exp
erimental]./1000,'.r')
plot([PRELIM DATA 44mmCC(41).Vtotal rounded], [PRELIM DATA 44mmCC(41).p engine
experimental]./1000,'.k')
plot([PRELIM DATA 44mm(33).Vtotal rounded], [PRELIM DATA 44mm(33).p buffer exp
erimental]./1000,'.r')
```

```
plot([PRELIM DATA 44mmCC(41).Vtotal rounded], [PRELIM DATA 44mmCC(41).p buffer
experimental]./1000,'.k')
xlabel('Engine Volume (m^3)', 'FontName', font, 'FontSize', font size)
ylabel('Pressure (kPa)', 'FontName', font, 'FontSize', font size);
legend('44 mm Piston', 'Crankcase Extension', 'Location', 'NorthEast')
set(gca, 'fontsize', font size);
set(gca, 'FontName', font)
hold off
%% Further Testing on Dead Volume Reduction Parts Plots
% Power vs. Frequency
figure('Position', [x y 326 275])
hold on
pointsize = 30;
scatter([DATA 44mmCC.Engine Hz],[DATA 44mmCC.P shaft], pointsize,'b*')
scatter([DATA 44mmCCDV.Engine Hz],[DATA 44mmCCDV.P shaft], pointsize,'rx')
ylim([0 inf])
xlabel('Engine Frequency (Hz)', 'FontName', font, 'FontSize', font size);
ylabel('Shaft Power (W)', 'FontName', font, 'FontSize', font size);
legend ('No DV Reduction', 'DV Reduction', 'Location', 'SouthWest')
set(gca, 'fontsize', font size);
set(gca, 'FontName', font)
hold off
% Indicated Power vs. Speed for Several Mean Pressures
figure('Position', [x y 326 275])
pointsize = 30;
hold on
scatter([DATA 44mmCC.Engine Hz],[DATA 44mmCC.P ind PCB], pointsize,'b*')
scatter([DATA_44mmCCDV.Engine Hz],[DATA 44mmCCDV.P ind PCB], pointsize,'rx')
ylim([0 inf])
xlabel('Engine Frequency (Hz)', 'FontName', font, 'FontSize', font size)
ylabel('Indicated Power (W)', 'FontName', font, 'FontSize', font size);
legend('No DV Reduction', 'DV Reduction', 'Location', 'SouthEast')
set(gca, 'fontsize', font size);
set(gca, 'FontName', font)
hold off
% Cooler Heat Removal vs. Speed for Several Mean Pressures
figure('Position', [x y 326 275])
pointsize = 30;
hold on
Q_dot_rej_44mmCC = [DATA_44mmCC.Qdot Cooler];
Q dot rej 44mmCCDV = [DATA 44mmCCDV.Qdot Cooler];
scatter([DATA 44mmCC.Engine Hz],Q dot rej 44mmCC, pointsize,
[DATA 44mmCC.pmean]./1000, 'b*')
scatter([DATA 44mmCCDV.Engine Hz],Q dot_rej_44mmCCDV, pointsize,
[DATA 44mmCCDV.pmean]./1000, 'rx')
xlabel('Engine Frequency (Hz)', 'FontName', font, 'FontSize', font size)
ylabel('Heat Rejection Rate (W)', 'FontName', font, 'FontSize', font size);
legend('No DV Reduction', 'DV Reduction', 'Location', 'SouthEast')
set(gca, 'fontsize', font size);
set(gca, 'FontName', font)
hold off
```

% Con Pipe/Pow Cyl Heat Removal vs. Speed for Several Mean Pressures

```
figure('Position', [x y 326 275])
pointsize = 30;
hold on
Q dot rej 44mmCC = [DATA 44mmCC.Qdot ConPipePowCyl];
Q dot rej 44mmCCDV = [DATA 44mmCCDV.Qdot ConPipePowCyl];
scatter([DATA 44mmCC.Engine Hz],Q dot rej 44mmCC, pointsize, 'b*')
scatter([DATA 44mmCCDV.Engine Hz],Q dot rej 44mmCCDV, pointsize,'rx')
xlabel('Engine Frequency (Hz)', 'FontName', font, 'FontSize', font size)
ylabel('Heat Rejection Rate (W)', 'FontName', font, 'FontSize', font size);
legend('No DV Reduction', 'DV Reduction', 'Location', 'SouthWest')
set(gca, 'fontsize', font size);
set(gca, 'FontName', font)
hold off
%% Loaded Cool Down Plots for All Mods
% Torque vs. Expansion Space Temperature
figure('Position', [x y 326 275])
pointsize = 30;
hold on
scatter([LOADED COOL 44mmCCDV.Tge], [LOADED COOL 44mmCCDV.Torque avq],
pointsize, [LOADED COOL 44mmCCDV.Engine Hz], 'o')
ylim([0.1 inf])
xlabel('Expansion Space Temperature
(\circC)', 'FontName', font, 'FontSize', font size);
ylabel('Torque (Nm)', 'FontName', font, 'FontSize', font size);
c = colorbar;
ylabel(c,'Engine Frequency (Hz)','FontName',font,'FontSize',font size)
colormap(jet)
hold off
% Power vs. Expansion Space Temperature
figure('Position', [x y 326 275])
pointsize = 30;
hold on
scatter([LOADED COOL 44mmCCDV.Tge],[LOADED COOL 44mmCCDV.P shaft], pointsize,
[LOADED COOL 44mmCCDV.Engine Hz], 'o')
ylim([0 inf])
xlabel('Expansion Space Temperature
(\circC)', 'FontName', font, 'FontSize', font size);
ylabel('Shaft Power (W)', 'FontName', font, 'FontSize', font size);
c = colorbar;
ylabel(c, 'Engine Frequency (Hz)', 'FontName', font, 'FontSize', font size)
colormap(jet)
hold off
% Shaft Work vs. Expansion Space Temperature
figure('Position', [x y 326 275])
pointsize = 30;
hold on
scatter([LOADED COOL 44mmCCDV.Tge],[LOADED COOL 44mmCCDV.P shaft]./[LOADED CO
OL 44mmCCDV.Engine Hz], pointsize, [LOADED COOL 44mmCCDV.Engine Hz], 'o')
% ylim([0 inf])
xlabel('Expansion Space Temperature
(\circC)', 'FontName', font, 'FontSize', font size);
ylabel('Shaft Work (J)', 'FontName', font, 'FontSize', font size);
c = colorbar;
```

```
ylabel(c,'Engine Frequency (Hz)','FontName',font,'FontSize',font size)
colormap(jet)
hold off
% Speed vs. Expansion Space Temperature
figure('Position', [x y width height])
hold on
plot([LOADED COOL 44mmCCDV.Tge], [LOADED COOL 44mmCCDV.Engine Hz], 'ko')
xlabel('Expansion Space Temperature
(\circC)', 'FontName', font, 'FontSize', font size)
ylabel('Engine Frequency (Hz)', 'FontName', font, 'FontSize', font size)
set(gca, 'fontsize', font size);
set(gca, 'FontName', font)
hold off
% Indicated Work vs. Expansion Space Temperature
figure('Position', [x y width height])
hold on
plot([LOADED COOL 44mmCCDV.Tge],[LOADED COOL 44mmCCDV.P ind PCB]./[LOADED COO
L 44mmCCDV.Engine Hz], 'o')
ylim([0 inf])
xlabel('Expansion Space Temperature
(\circC)', 'FontName', font, 'FontSize', font size)
ylabel('Indicated Work (J)', 'FontName', font, 'FontSize', font size);
hold off
% Series of Indicator Diagrams for Dead Volume Reduction
figure('Position', [x v width height])
pointsize = 1;
hold on
for i = 1:length(LOADED COOL 44mmCCDV)
    if LOADED COOL 44mmCCDV(i).Tge > 180
scatter([LOADED COOL 44mmCCDV(i).Vtotal rounded],[LOADED COOL 44mmCCDV(i).p e
ngine experimental]./1000,pointsize,repelem([LOADED COOL 44mmCCDV(i).Tge],360
))
    end
end
xlabel('Engine Volume (m^3)', 'FontName', font, 'FontSize', font size)
ylabel({'Engine Pressure (kPa)'},'FontName',font,'FontSize',font size);
c = colorbar;
ylabel(c, 'Expansion Space Temperature
(\circC)', 'FontName', font, 'FontSize', font size)
colormap(jet)
% Series of Buffer Pressure Diagrams for Dead Volume Reduction
figure('Position', [x y width height])
pointsize = 1;
hold on
for i = 1:length(LOADED COOL 44mmCCDV)
    if LOADED COOL 44mmCCDV(i).Tge > 180
scatter([LOADED COOL 44mmCCDV(i).Vtotal rounded],[LOADED COOL 44mmCCDV(i).p b
```

```
uffer experimental]./1000,pointsize,repelem([LOADED COOL 44mmCCDV(i).Tge],360
))
    end
end
xlabel('Engine Volume (m^3)', 'FontName', font, 'FontSize', font size)
ylabel({'Buffer Pressure (kPa)'},'FontName',font,'FontSize',font size);
c = colorbar;
ylabel(c, 'Expansion Space Temperature
(\circC)', 'FontName', font, 'FontSize', font size)
colormap(jet)
% Crankcase and Power Cylinder Mean Pressures vs. Expansion space
% temperature for Dead Volume Reduction
figure('Position', [x y width height])
hold on
for i = 1:length(LOADED COOL 44mmCCDV)
plot([LOADED COOL 44mmCCDV(i).Tge],mean([LOADED COOL 44mmCCDV(i).p engine exp
erimental]./1000),'or')
plot([LOADED COOL 44mmCCDV(i).Tge],mean([LOADED COOL 44mmCCDV(i).p buffer exp
erimental]./1000), '*k')
end
hold off
xlabel('Expansion Space Temperature
(\circC)', 'FontName', font, 'FontSize', font size)
ylabel('Pressure (kPa)', 'FontName', font, 'FontSize', font size)
legend ('Mean Power Cylinder Pressure', 'Mean Crankcase Pressure')
set(gca, 'fontsize', font size);
set(gca, 'FontName', font)
% Experimental Forced Work vs. Expansion Space Temperature, All Mods
figure('Position', [x y 326 275])
hold on
plot([LOADED COOL 44mmCCDV.Tge],[LOADED COOL 44mmCCDV.Exp FW],'r*')
xlabel('Expansion Space Temperature
(\circC)', 'FontName', font, 'FontSize', font size)
ylabel('Forced Work (J)', 'FontName', font, 'FontSize', font size);
set(gca,'fontsize',font size);
set(gca, 'FontName', font)
hold off
% Experimental Indicated Work vs. Expansion Space Temperature, All Mods
figure('Position', [x y 326 275])
hold on
plot([LOADED COOL 44mmCCDV.Tge],[LOADED COOL 44mmCCDV.P ind PCB]./[LOADED COO
L 44mmCCDV.Engine Hz], 'ko')
xlabel('Expansion Space Temperature
(\circC)', 'FontName', font, 'FontSize', font size)
ylabel('Indicated Work (J)', 'FontName', font, 'FontSize', font size);
set(gca, 'fontsize', font size);
set(gca, 'FontName', font)
hold off
% Forced Work Ratio vs. Expansion Space Temperature
figure('Position', [x y width height])
hold on
```

```
plot([LOADED COOL 44mmCCDV.Tge],[LOADED COOL 44mmCCDV.Exp FW]./([LOADED COOL
44mmCCDV.P ind PCB]./[LOADED COOL 44mmCCDV.Engine Hz]), 'ko')
xlabel('Expansion Space Temperature
(\circC)', 'FontName', font, 'FontSize', font size)
ylabel('Forced Work Ratio', 'FontName', font, 'FontSize', font size);
set(gca, 'fontsize', font size);
set(gca, 'FontName', font)
hold off
% GSH Loss vs. Expansion Space Temperature
figure('Position', [x y width height])
pointsize = 30;
scatter([LOADED COOL 44mmCCDV.Tge],([LOADED COOL 44mmCCDV.P GSH Loss PCB]./[L
OADED COOL 44mmCCDV.Engine Hz]),
pointsize, [LOADED COOL 44mmCCDV.Engine Hz], 'o')
xlabel('Expansion Space Temperature
(\circC)', 'FontName', font, 'FontSize', font size)
ylabel('Gas Spring Hysteresis (J)', 'FontName', font, 'FontSize', font size);
c = colorbar;
ylabel(c, 'Engine Frequency (Hz)', 'FontName', font, 'FontSize', font size)
colormap(jet)
```

Chapter 5

Chapter_5_Plots.m

```
% Compare model to experimental data.
clear,clc,close all;
%% Cooling System Input Parameters
V dot Cooler = 0.800*1.66667e-5; % Cooler water volume flow rate [m^3/s]
V dot ConPipePowCyl = 0.200*1.66667e-5; % Connecting Pipe and Power Cylinder
water volume flow rate [m^3/s]
c water = 4184; % Specific heat capacity of water in [J/kgK]
dens water = 1000; % Water density [kg/m^3]
% Calculations
m dot Cooler = V dot Cooler*dens water; % Cooler water mass flow rate [kg/s]
m dot ConPipePowCyl = V dot ConPipePowCyl*dens water; % Connecting Pipe water
mass flow rate [kg/s]
%% Process Experimental Data
% % Efficiency data, TH = 300, TC = 21, P = 60
% efficiency file folder = 'X:\01 Current Students\Connor Speer\00 Thesis and
Journal Papers\00 Thesis\00 Data and Plots\Chapter 5 Plots (Model
Validation) \Efficiency';
% EFFICIENCY DATA = Process Data(efficiency file folder);
8
```

% Chapter 5 Plots.m - Written by Connor Speer - October 2017

```
% % Conduction Loss Data
% conduction loss file folder = 'X:\01 Current Students\Connor
Speer\00 Thesis and Journal Papers\00 Thesis\00 Data and Plots\Chapter 5
Plots (Model Validation) \Conduction Loss';
% COND LOSS DATA = Process Data(conduction loss file folder);
% Fully Modified Tests
full mods 200deg file folder = 'X:\01 Current Students\Connor Speer\00 Thesis
and Journal Papers\00 Thesis\00 Data and Plots\Chapter 5 Plots (Model
Validation) \Fully Modified Tests \TH 200';
TH200 DATA = Process Data(full mods 200deg file folder);
% Indicator Diagram Plots
full mods PV file folder = 'X:\01 Current Students\Connor Speer\00 Thesis and
Journal Papers\00 Thesis\00 Data and Plots\Chapter 5 Plots (Model
Validation)\Fully Modified Tests\P 60 TH 200 and 300';
PV DATA = Process Data(full mods PV file folder);
%% Plot Set-Up
set(0, 'defaultfigurecolor', [1 1 1])
% Location of Figures
x = 500;
y = 500;
% Size of Figures
width = 550;
height = 400;
% Font For Figures
font = 'Arial';
font size = 11;
% % Location of Figures
% x = 500;
% y = 500;
8
% % Size of Figures
% width = 326;
% height = 275;
% % Font For Figures
% font = 'Times New Roman';
\% font size = 10;
% % Location of Figures
% x = 500;
% y = 500;
```

```
0
% % Size of Figures
% width = 550;
% height = 400;
20
% % Font For Figures
% font = 'Times New Roman';
% font size = 16;
% To change line width for plots, say "'LineWidth',2".
% To include math symbols with their own font size and font type in the
% axes labels, do this:
% xlabel({'\fontsize{11} Engine Speed \fontsize{11} \fontname{Cambria Math}
\omega \fontsize{11} \fontname{Times New Roman} [RPM]'});
% Here is the degree symbol in case you need it °C. Alternatively, use
% \circ.
%% Efficiency Plots
% % Thermal Efficiency vs. Speed for Several Mean Pressures
% figure('Position', [x y width height])
% Sorted efficiencies = [EFFICIENCY DATA(5:7).eff thermal
EFFICIENCY DATA(1:4).eff thermal];
% Sorted frequencies = [EFFICIENCY DATA(5:7).Filename Hz
EFFICIENCY DATA(1:4).Filename Hz];
% plot(Sorted frequencies,Sorted efficiencies.*100,'--o','LineWidth',2)
% xlabel('Engine Frequency (Hz)','FontName',font,'FontSize',font size);
% ylabel('Thermal Efficiency (%)','FontName',font,'FontSize',font size);
% set(gca,'fontsize',font size)
% set(gca, 'FontName', font)
00
% % Thermal Efficiency vs. Speed for Several Mean Pressures with Overlayed
2nd Order Model
% figure('Position', [x y width height])
% hold on
% plot([EFFICIENCY DATA.Filename Hz],[EFFICIENCY DATA.eff thermal].*100,'r*')
plot([EFFICIENCY DATA.Filename Hz], [EFFICIENCY DATA.eff thermal 2nd order].*1
00, 'bo')
% xlabel('Engine Frequency (Hz)','FontName',font,'FontSize',font size);
% ylabel('Thermal Efficiency (%)','FontName',font,'FontSize',font size);
% legend('Experimental Data','2nd Order Model','Location','NorthWest')
% set(gca,'fontsize',font size)
% set(gca, 'FontName', font)
% hold off
2
% % Heat Input with Overlaid Model
% figure('Position', [x y width height])
% hold on
% plot([EFFICIENCY DATA.Filename Hz],[EFFICIENCY DATA.Q dot in],'r*')
plot([EFFICIENCY DATA.Filename Hz], [EFFICIENCY DATA.Q dot in 2nd order], 'bo')
% xlabel('Engine Frequency (Hz)', 'FontName', font, 'FontSize', font size)
```

```
% ylabel('Heat Input Rate (W)','FontName',font,'FontSize',font size);
% legend('Experimental Data','2nd Order Model','Location','NorthWest')
% set(gca,'fontsize',font_size)
% set(gca, 'FontName', font)
% hold off
00
% % Shaft Power with Overlaid Model
% figure('Position', [x y width height])
% pointsize = 30;
% hold on
% scatter([EFFICIENCY DATA.Filename Hz], [EFFICIENCY DATA.Filename P shaft],
pointsize, [EFFICIENCY DATA.pmean], '*')
% scatter([EFFICIENCY DATA.Filename Hz], [EFFICIENCY DATA.P 2nd order],
pointsize, [EFFICIENCY DATA.pmean], 'o')
% xlabel('Engine Frequency (Hz)', 'FontName', font, 'FontSize', font size)
% ylabel('Shaft Power (W)', 'FontName', font, 'FontSize', font size);
% c = colorbar;
% ylabel(c,'Mean Pressure (Pa)','FontName',font,'FontSize',font size)
% colormap(jet)
% legend('Experimental Data','2nd Order Model')
% set(gca,'fontsize',font size)
% set(gca, 'FontName', font)
% hold off
%% Conduction Loss Plots
% % Heat Rejection Rates vs. Heating Cap Setpoint with Overlaid Conduction
% % Loss Model
% figure('Position', [x y 326 275])
% Q dot rej = [COND LOSS DATA.Qdot Cooler] +
[COND LOSS DATA.Qdot ConPipePowCyl];
% hold on
% plot([COND LOSS DATA.Cap Setpoint],Q dot rej,'--ob','LineWidth',2)
8
plot([COND LOSS DATA.Cap Setpoint], [COND LOSS DATA.Conduction Loss Model], '-
k','LineWidth',2)
% xlabel('Heating Cap Setpoint (°C)', 'FontName', font, 'FontSize', font size)
% ylabel('Conduction Loss (W)','FontName',font,'FontSize',font size);
% legend('Measured Heat Rejection Rate','Conduction Loss
Model', 'Location', 'NorthWest')
% set(gca,'fontsize',font size)
% set(gca, 'FontName', font)
% hold off
0
% % Measured Conduction Loss as a Fraction of the Measured Heat Input Rate
% figure('Position', [x y 326 275])
% Q dot rej percent = (Q dot rej./[COND LOSS DATA.Q dot in]).*100;
% hold on
% plot([COND_LOSS_DATA.Cap_Setpoint],Q_dot_rej_percent,'--ob','LineWidth',2)
% xlabel('Heating Cap Setpoint (°C)','FontName',font,'FontSize',font size)
% ylabel({'Conduction Loss as a';'Fraction of Heat Input
(%)'},'FontName',font,'FontSize',font size);
% set(gca,'fontsize',font size)
% set(gca, 'FontName', font)
% hold off
00
```

```
% % Heat Loss Through Insulation
% figure('Position', [x y 326 275])
% Q dot rej = [COND LOSS DATA.Qdot Cooler] +
[COND LOSS DATA.Qdot ConPipePowCyl];
% Q loss insulation = [COND LOSS DATA.Q dot in] - Q dot rej;
% plot([COND LOSS DATA.Cap Setpoint],Q loss insulation, '--ok', 'LineWidth',2)
% xlabel('Heating Cap Setpoint (°C)', 'FontName', font, 'FontSize', font size)
% ylabel('Heat Lost Through Insulation
(W)', 'FontName', font, 'FontSize', font size);
% set(gca,'fontsize',font size)
% set(gca, 'FontName', font)
2
% % Fraction of Heat Input Lost Through the Insulation
% figure('Position', [x y 326 275])
% Q loss insulation percent =
(Q loss insulation./[COND LOSS DATA.Q dot in]).*100;
% plot([COND LOSS DATA.Cap Setpoint], Q loss insulation percent,'--
ok', 'LineWidth', 2)
% xlabel('Heating Cap Setpoint (°C)', 'FontName', font, 'FontSize', font size)
% ylabel({'Heat Lost Through Insulation';'as a Fraction of Heat Input
(%)'},'FontName',font,'FontSize',font size);
% set(gca,'fontsize',font size)
% set(gca, 'FontName', font)
%% Gas Spring Hysteresis Plots
% Crankcase Gas Spring Hysteresis Loss vs. Speed for Several Mean Pressures
figure('Position', [x y width height])
pointsize = 30;
scatter([TH200 DATA.Engine Hz],[TH200 DATA.P GSH Loss PCB]./[TH200 DATA.Engin
e Hz], pointsize, [TH200 DATA.pmean]./1000)
xlabel('Engine Frequency (Hz)', 'FontName', font, 'FontSize', font_size)
ylabel({'Crankcase Gas Spring';'Hysteresis Loss Per Cycle
(J)'},'FontName',font,'FontSize',font size);
c = colorbar;
ylabel(c,'Mean Pressure (kPa)','FontName',font,'FontSize',font size)
colormap(jet)
set(gca, 'fontsize', font size)
set(gca, 'FontName', font)
% Crankcase Gas Spring Hysteresis Loss vs. Speed for Several Mean Pressures
figure('Position', [x y width height])
pointsize = 30;
scatter([TH200 DATA.Engine Hz], [TH200 DATA.P GSH Loss PCB], pointsize,
[TH200 DATA.pmean]./1000)
xlabel('Engine Frequency (Hz)', 'FontName', font, 'FontSize', font size)
ylabel('Crankcase Gas Spring Hysteresis Loss
(W)', 'FontName', font, 'FontSize', font size);
c = colorbar;
ylabel(c,'Mean Pressure (kPa)','FontName',font,'FontSize',font size)
colormap(jet)
set(gca, 'fontsize', font size)
set(gca, 'FontName', font)
% 3D Plot of Crankcase Gas Spring Hysteresis Loss vs. Speed and Mean Pressure
```

```
figure('Position', [x y width height])
```

```
X = [TH200 DATA.Engine Hz]';
Y = [TH200 DATA.pmean]./1000;
Y = Y';
Z = [TH200_DATA.P GSH Loss PCB]';
[sf, gof] = fit([X, Y], Z, 'poly22');
plot(sf,[X,Y],Z)
xlabel('Engine Frequency (Hz)', 'FontName', font, 'FontSize', font size)
ylabel('Mean Pressure (kPa)', 'FontName', font, 'FontSize', font size)
zlabel({'Crankcase Gas Spring';'Hysteresis Loss
(W) '}, 'FontName', font, 'FontSize', font size)
set(gca, 'fontsize', font size)
set(gca, 'FontName', font)
% Crankcase Gas Spring Hysteresis Loss vs. Speed for Several Mean Pressures
% with Overlayed Empirical Model
figure('Position', [x y width height])
hold on
plot([TH200 DATA.Engine Hz],[TH200 DATA.P GSH Loss PCB],'ok')
P hys Empirical =
HTG GSH Empirical([TH200 DATA.Engine Hz], [TH200 DATA.pmean], 4);
plot([TH200_DATA.Engine_Hz],P_hys_Empirical,'*r')
xlabel('Engine Frequency (Hz)', 'FontName', font, 'FontSize', font_size)
ylabel({'Crankcase Gas Spring';' Hysteresis Loss
(W) ' }, 'FontName', font, 'FontSize', font size)
legend('Experimental Data','Empirical Model','Location', 'northwest')
set(gca, 'fontsize', font size);
set(gca, 'FontName', font)
hold off
%% Indicated Work Plots
% Ideal Isothermal Model and Ideal Adiabatic Model Error in Indicated
% Work vs. Speed for Two Heating Cap Temperatures
figure('Position', [x y width height])
pointsize = 30;
hold on
scatter([PV DATA.Engine Hz], [PV DATA.Error isothermal], pointsize,
[PV DATA.Cap Setpoint], 'o')
scatter([PV DATA.Engine Hz],[PV DATA.Error adiabatic], pointsize,
[PV DATA.Cap Setpoint], '*')
xlabel('Engine Frequency (Hz)', 'FontName', font, 'FontSize', font size)
ylabel({'Indicated Work Error (%)'},'FontName',font,'FontSize',font size);
c = colorbar;
ylabel(c, 'Heating Cap Temperature
(\circC)', 'FontName', font, 'FontSize', font size)
mycolors = [0 \ 0 \ 1; \ 1 \ 0 \ 0];
colormap(mycolors)
c.Ticks = [200 300];
legend('Ideal Isothermal Model','Ideal Adiabatic
Model', 'Location', 'NorthWest')
set(gca, 'fontsize', font size)
set(gca, 'FontName', font)
hold off
% Experimental Indicator Diagram with Overlaid isothermal and adiabatic
% models
```

```
393
```

```
% for i = 1:length([PV DATA.filename])-1
      figure('Position', [x y width height])
2
8
      hold on
0
plot([PV DATA(i).Vtotal rounded], [PV DATA(i).p engine experimental]./1000,'*k
1)
8
plot([PV DATA(i).Vtotal rounded], [PV DATA(i).p engine isothermal]./1000,'r','
LineWidth',2)
plot([PV DATA(i).Vtotal rounded], [PV DATA(i).p engine adiabatic]./1000, b', 'L
ineWidth',2)
2
     hold off
2
      xlabel('Engine Volume (m^3)','FontName',font,'FontSize',font size)
8
      ylabel('Pressure (kPa)','FontName',font,'FontSize',font size)
8
      legend ('Experimental Data', 'Ideal Isothermal Model', 'Ideal Adiabatic
Model')
8
      title(PV DATA(i).filename)
2
      set(gca, 'fontsize', font size)
8
      set(gca, 'FontName', font)
% end
% Example Indicator Diagram
figure('Position', [x y 326 275])
hold on
plot([PV DATA(28).Vtotal rounded], [PV DATA(28).p engine experimental]./1000, '
ok', 'MarkerSize',2)
plot([PV DATA(28).Vtotal rounded], [PV DATA(28).p engine isothermal]./1000, 'r'
,'LineWidth',2)
plot([PV DATA(28).Vtotal rounded], [PV DATA(28).p engine adiabatic]./1000, 'b',
'LineWidth',2)
hold off
xlabel('Engine Volume (m^3)', 'FontName', font, 'FontSize', font size)
ylabel('Pressure (kPa)', 'FontName', font, 'FontSize', font size)
xlim([0.00134 0.00148])
ylim([300 550])
legend('Exp Data','Isothermal','Adiabatic')
set(gca, 'fontsize', font size)
set(gca, 'FontName', font)
%% Teknic Spin Test Plots
% % Friction Plots.m - Written by Connor Speer - July 2017
8
% % Calls the overall plots subfunction for several data folders and produces
% % plots.
00
% % Fully Assembled
% log file folder 1 = 'X:\01 Current Students\Connor Speer\00 Thesis and
Journal Papers\00 Thesis\00 Data and Plots\Chapter 5 Plots (Model
Validation) \Tecknic Spin Tests \01 Fully Assembled';
% DATA STRUCTURE 1 =
Subfunction Overall Plots Tecknic Spin(log file folder 1);
% % Crankcase Cover Removed
```

```
% log file folder 2 = 'X:\01 Current Students\Connor Speer\00 Thesis and
Journal Papers\00 Thesis\00 Data and Plots\Chapter 5 Plots (Model
Validation) \Tecknic Spin Tests \02 Crankcase Cover Removed';
\% DATA STRUCTURE 2 =
Subfunction Overall Plots Tecknic Spin(log file folder 2);
00
% % Crankcase Cover and Heater Head Removed
% log file folder 3 = 'X:\01 Current Students\Connor Speer\00 Thesis and
Journal Papers\00 Thesis\00 Data and Plots\Chapter 5 Plots (Model
Validation) \Tecknic Spin Tests \03 Crankcase Cover & Heater Head Removed';
\% DATA STRUCTURE 3 =
Subfunction Overall_Plots_Tecknic_Spin(log_file_folder_3);
00
% % CC Cover, HH, and Power Cylinder Head Removed
% log file folder 4 = 'X:\01 Current Students\Connor Speer\00 Thesis and
Journal Papers\00 Thesis\00 Data and Plots\Chapter 5 Plots (Model
Validation)\Tecknic Spin Tests\04 CC Cover & HH & Power Cyl Head Removed';
\% DATA STRUCTURE 4 =
Subfunction Overall Plots Tecknic Spin(log file folder 4);
% % CC Cover, HH, P Cyl Head, and Cooler Removed
% log file folder 5 = 'X:\01 Current Students\Connor Speer\00 Thesis and
Journal Papers\00 Thesis\00 Data and Plots\Chapter 5 Plots (Model
Validation)\Tecknic Spin Tests\05 CC Cover & HH & Power Cyl Head & Cooler
Removed';
% DATA STRUCTURE 5 =
Subfunction Overall Plots Tecknic Spin(log file folder 5);
2
% % Plot 1 - Total Friction vs. Speed Showing Relative Contributions
% figure('Position', [x y width height])
% hold on
% speed = [50 100 200 300 400 500 600];
% frequency = speed./60;
00
% plot(frequency,-[DATA STRUCTURE 1.P shaft],'ob')
% plot(frequency, - [DATA STRUCTURE 2.P shaft], '*r')
% plot(frequency,-[DATA STRUCTURE_3.P_shaft],'^k')
% plot(frequency,-[DATA STRUCTURE 4.P shaft],'xm')
% plot(frequency,-[DATA STRUCTURE 5.P shaft],'.q')
% xlabel('Engine Frequency (Hz)', 'FontName', font, 'FontSize', font size)
% ylabel('Power Consumption (W)', 'FontName', font, 'FontSize', font size)
% legend('Fully Assembled','No CC Cover','No CC Cover or HH','No CC Cover,
HH, or P Cyl Head', 'No CC Cover, HH, P Cyl Head, or
Cooler', 'Location', 'NorthWest')
% hold off
% set(gca,'fontsize',font size)
% set(gca, 'FontName', font)
% % Plot 2 - Indicated Power Consumption, Measured Shaft Power Consumption,
% % Mechanism Effectiveness
% figure('Position', [x y width height])
% hold on
% yyaxis left
% plot(frequency, [DATA STRUCTURE 1.P ind], 'ob')
% plot(frequency,-[DATA STRUCTURE 1.P shaft],'*b')
```

```
% ylabel('Indicated Power Consumption
(W) ', 'FontName', font, 'FontSize', font size)
% set(gca,'ycolor','b')
0
% yyaxis right
% plot(frequency,-[DATA STRUCTURE 1.P ind]./[DATA STRUCTURE 1.P shaft],'or')
% ylabel('Mechanism Effectiveness','FontName',font,'FontSize',font size)
% set(gca,'ycolor','r')
% xlabel('Engine Frequency (Hz)','FontName',font,'FontSize',font size)
% xlim([0 7])
% legend('Indicated Power Consumption', 'Power Supplied by Electric
Motor', 'Mechanism Effectiveness', 'Location', 'North')
% set(gca,'fontsize',font size)
% set(gca, 'FontName', font)
%% Buffer Pressure, Forced Work, and Mechanism Effectiveness Plots
% Series of Buffer Pressure Indicator Diagrams with Overlaid Isothermal and
% Adiabatic Buffer Pressure Models
% for i = 1:length([TH200 DATA.filename])-1
      figure('Position', [x y width height])
2
2
      hold on
8
plot([TH200 DATA(i).Vtotal rounded], [TH200 DATA(i).p buffer experimental]./10
00, 'ok')
0
plot([TH200 DATA(i).Vtotal rounded], [TH200 DATA(i).p buffer isothermal]./1000
,'r','LineWidth',2)
plot([TH200 DATA(i).Vtotal rounded], [TH200 DATA(i).p buffer adiabatic]./1000,
'b','LineWidth',2)
8
     hold off
8
      xlabel('Engine Volume (m^3)', 'FontName', font, 'FontSize', font size)
      ylabel('Pressure (kPa)', 'FontName', font, 'FontSize', font size)
8
8
      legend('Experimental Data','Isothermal Model','Adiabatic
Model', 'Location', 'NorthWest')
      title(TH200 DATA(i).filename)
8
      set(gca, 'fontsize', font size)
00
      set(gca, 'FontName', font)
2
% end
% Example buffer pressure diagram with overlaid isothermal and adiabatic
% models
figure('Position', [x y width height])
hold on
plot([TH200 DATA(44).Vtotal rounded], [TH200 DATA(44).p buffer experimental]./
1000, 'ok')
plot([TH200 DATA(44).Vtotal rounded],[TH200 DATA(44).p buffer isothermal]./10
00, 'r', 'LineWidth', 2)
plot([TH200 DATA(44).Vtotal rounded],[TH200 DATA(44).p buffer adiabatic]./100
0, 'b', 'LineWidth', 2)
hold off
xlabel('Engine Volume (m^3)','FontName',font,'FontSize',font size)
ylabel('Crankcase Pressure (kPa)', 'FontName', font, 'FontSize', font size)
```

```
legend('Experimental Data','Isothermal Assumption','Adiabatic
Assumption', 'Location', 'NorthWest')
set(gca, 'fontsize', font size)
set(gca, 'FontName', font)
%% Overall Torque and Power Plots
% Torque vs. Frequency for Several Mean Pressures
figure('Position', [x y width height])
pointsize = 30;
scatter([TH200 DATA.Engine Hz],[TH200 DATA.Torque avg], pointsize,
[TH200 DATA.pmean]./1000)
xlabel('Engine Frequency (Hz)', 'FontName', font, 'FontSize', font size);
ylabel('Torque (Nm)', 'FontName', font, 'FontSize', font size);
c = colorbar;
ylabel(c,'Mean Pressure (kPa)','FontName',font,'FontSize',font size)
ylim([0 inf])
colormap(jet)
set(qca,'fontsize',font size)
set(gca, 'FontName', font)
% Power vs. Frequency for Several Mean Pressures
figure('Position', [x y width height])
pointsize = 30;
scatter([TH200 DATA.Engine Hz], [TH200 DATA.P shaft], pointsize,
[TH200 DATA.pmean]./1000)
xlabel('Engine Frequency (Hz)', 'FontName', font, 'FontSize', font size);
ylabel('Shaft Power (W)', 'FontName', font, 'FontSize', font size);
vlim([0 inf])
c = colorbar;
ylabel(c,'Mean Pressure (kPa)','FontName',font,'FontSize',font size)
colormap(jet)
set(gca, 'fontsize', font size)
set(gca, 'FontName', font)
% Power vs. Speed for Several Mean Pressures with Overlayed 2nd Order Model
figure('Position', [x y width height])
hold on
pointsize = 30;
scatter([TH200 DATA.Engine Hz],[TH200 DATA.P shaft], pointsize,
[TH200 DATA.pmean]./1000, '*')
scatter([TH200 DATA.Engine Hz], [TH200 DATA.P 2nd order], pointsize,
[TH200 DATA.pmean]./1000, 'o')
xlabel('Engine Frequency (Hz)', 'FontName', font, 'FontSize', font_size);
ylabel('Shaft Power (W)', 'FontName', font, 'FontSize', font size);
% ylim([0 inf])
c = colorbar;
ylabel(c,'Mean Pressure (kPa)','FontName',font,'FontSize',font size)
colormap(jet)
legend('Experimental Data','2nd Order Model','Location','NorthWest')
set(gca, 'fontsize', font size);
set(gca, 'FontName', font)
hold off
```

```
%% Relative Cooling Zone Plots
% Heat Rejection rate with overlaid model
```

```
figure('Position', [x y width height])
pointsize = 30;
hold on
scatter([TH200 DATA.Engine Hz],
[TH200 DATA.Qdot Cooler]+[TH200 DATA.Qdot ConPipePowCyl], pointsize,
[TH200 DATA.pmean]./1000, '*')
scatter([TH200 DATA.Engine Hz], [TH200 DATA.Q dot rej 2nd order], pointsize,
[TH200 DATA.pmean]./1000, 'o')
xlabel ('Engine Frequency (Hz)', 'FontName', font, 'FontSize', font size)
ylabel({'Heat Rejection Rate (W)'}, 'FontName', font, 'FontSize', font size);
c = colorbar;
ylabel(c,'Mean Pressure (kPa)','FontName',font,'FontSize',font size)
colormap(jet)
legend('Experimental Data', '2nd Order Model')
set(gca, 'fontsize', font size)
set(gca, 'FontName', font)
% Heat Rejected in both zones
figure('Position', [x y width height])
pointsize = 30;
hold on
scatter([TH200 DATA.Engine Hz], [TH200 DATA.Qdot Cooler], pointsize,
[TH200 DATA.pmean]./1000, 'o')
scatter([TH200 DATA.Engine Hz], [TH200 DATA.Qdot ConPipePowCyl], pointsize,
[TH200 DATA.pmean]./1000, '*')
xlabel('Engine Frequency (Hz)', 'FontName', font, 'FontSize', font size)
ylabel({'Heat Rejection Rate (W)'}, 'FontName', font, 'FontSize', font size);
c = colorbar;
ylabel(c,'Mean Pressure (kPa)','FontName',font,'FontSize',font size)
colormap(jet)
legend('Cooler','Con Pipe and Pow Cyl')
set(gca, 'fontsize', font size)
set(gca, 'FontName', font)
% Relative Heat Rejection of Con Pipe/Pow Cyl Zone
figure('Position', [x y width height])
pointsize = 30;
RelQrejCPPC = ([TH200 DATA.Qdot ConPipePowCyl]./ ...
    ([TH200 DATA.Qdot ConPipePowCyl] + [TH200 DATA.Qdot Cooler]))*100;
scatter([TH200 DATA.Engine Hz], RelQrejCPPC, pointsize,
[TH200 DATA.pmean]./1000)
xlabel('Engine Frequency (Hz)', 'FontName', font, 'FontSize', font size)
ylabel({'Portion of Heat Rejected in'; 'Connecting Pipe and Power Cylinder
(%)'},'FontName',font,'FontSize',font size);
c = colorbar;
ylabel(c,'Mean Pressure (kPa)','FontName',font,'FontSize',font size)
colormap(jet)
set(gca, 'fontsize', font size)
set(gca, 'FontName', font)
%% Heat Exchanger and Regenerator Performance Plots
% Temperature Drop Between Cap Setpoint and Gas in Heater vs. Speed for
```

```
Several Mean Pressures
figure('Position', [x y 326 275])
pointsize = 30;
```

```
HeaterTdrop = [TH200 DATA.Cap Setpoint] - [TH200 DATA.Tgh];
scatter([TH200 DATA.Engine Hz],HeaterTdrop, pointsize,
[TH200 DATA.pmean]./1000)
xlabel('Engine Frequency (Hz)', 'FontName', font, 'FontSize', font size)
ylabel({'Heater Temperature Drop
(°C)'}, 'FontName', font, 'FontSize', font size);
c = colorbar;
ylabel(c,'Mean Pressure (kPa)','FontName',font,'FontSize',font size)
colormap(jet)
set(gca, 'fontsize', font size)
set(gca, 'FontName', font)
% Temperature Drop Between Gas in Cooler and Bath Setpoint for Several Mean
Pressures
figure('Position', [x y 326 275])
pointsize = 30;
CoolerTdrop = [TH200 DATA.Tqk] - [TH200 DATA.Bath Setpoint];
scatter([TH200 DATA.Engine Hz], CoolerTdrop, pointsize,
[TH200 DATA.pmean]./1000)
xlabel('Engine Frequency (Hz)', 'FontName', font, 'FontSize', font size)
ylabel({'Cooler Temperature Drop
(°C)'}, 'FontName', font, 'FontSize', font size);
c = colorbar;
ylabel(c,'Mean Pressure (kPa)','FontName',font,'FontSize',font size)
colormap(jet)
set(gca, 'fontsize', font size)
set(gca, 'FontName', font)
% Regenerator Pressure Drop vs. Crank Angle for Several Mean Pressures
% Overlaid Model
figure('Position', [x y 326 275])
theta deg = 0:1:359;
hold on
plot(theta deg, [TH200 DATA(97).pdrop regen experimental]./1000, '--
k', 'LineWidth',2)
plot(theta deg, [TH200 DATA(100).pdrop regen experimental]./1000, '--
q', 'LineWidth',2)
plot(theta deg, [TH200 DATA(109).pdrop regen experimental]./1000, '--
r', 'LineWidth',2)
plot(theta deg,[TH200 DATA(97).pdrop regen model]./1000,'k','LineWidth',2)
plot(theta deg, [TH200 DATA(100).pdrop regen model]./1000,'g','LineWidth',2)
plot(theta_deg,[TH200_DATA(109).pdrop_regen_model]./1000,'r','LineWidth',2)
xlabel('Crank Angle (\circ)', 'FontName', font, 'FontSize', font size)
ylabel('Regenerator Pressure Drop
(kPa)', 'FontName', font, 'FontSize', font size)
xlim([0 360])
legend('freq = 2.3 Hz', 'freq = 0.85 Hz', 'freq = 1.7 Hz', 'Location', 'South')
set(gca, 'fontsize', font size)
set(gca, 'FontName', font)
% Regenerator Pressure Drop vs. Crank Angle for Several Rotational Speeds
% Overlaid Model
figure('Position', [x y 326 275])
theta deg = 0:1:359;
hold on
```

```
plot(theta deg,[TH200 DATA(5).pdrop regen experimental]./1000,'--
k', 'LineWidth', 2)
plot(theta deg, [TH200 DATA(73).pdrop regen experimental]./1000, '--
g', 'LineWidth', 2)
plot(theta deg,[TH200 DATA(87).pdrop regen experimental]./1000,'--
r', 'LineWidth',2)
plot(theta deg,[TH200 DATA(5).pdrop regen model]./1000,'k','LineWidth',2)
plot(theta deg,[TH200 DATA(73).pdrop regen model]./1000,'g', 'LineWidth',2)
plot(theta_deg,[TH200_DATA(87).pdrop_regen_model]./1000,'r','LineWidth',2)
xlabel('Crank Angle (\circ)', 'FontName', font, 'FontSize', font size)
ylabel('Regenerator Pressure Drop
(kPa)', 'FontName', font, 'FontSize', font size)
xlim([0 360])
legend('pmean = 707 kPa', 'pmean = 293 kPa', 'pmean = 421
kPa', 'Location', 'South')
set(gca, 'fontsize', font size)
set(gca, 'FontName', font)
% % Regenerator Pressure Drop vs. Crank Angle for Several Mean Pressures
% % Overlaid "Validated" Model
% figure('Position', [x y 326 275])
\% theta deg = 0:1:359;
% hold on
% plot(theta deg,[TH200 DATA(97).pdrop regen experimental]./1000,'--
k','LineWidth',2)
% plot(theta deg,[TH200 DATA(100).pdrop regen experimental]./1000,'--
g', 'LineWidth', 2)
% plot(theta deg,[TH200 DATA(109).pdrop regen experimental]./1000,'--
r','LineWidth',2)
0
plot(theta deq,[TH200 DATA(97).pdrop regen model]./1000.*8,'k','LineWidth',2)
plot(theta deg,[TH200 DATA(100).pdrop regen model]./1000.*8,'g','LineWidth',2
plot(theta deg,[TH200 DATA(109).pdrop regen model]./1000.*8,'r','LineWidth',2
)
% xlabel('Crank Angle (\circ)', 'FontName', font, 'FontSize', font size)
% ylabel('Regenerator Pressure Drop
(kPa)', 'FontName', font, 'FontSize', font size)
% xlim([0 360])
% legend('freq = 2.3 Hz','freq = 0.85 Hz','freq = 1.7 Hz','Location','South')
% set(gca,'fontsize',font size)
% set(gca, 'FontName', font)
8
% % Regenerator Pressure Drop vs. Crank Angle for Several Rotational Speeds
% % Overlaid "Validated" Model
% figure('Position', [x y 326 275])
\% theta deg = 0:1:359;
% hold on
% plot(theta deg,[TH200 DATA(5).pdrop regen experimental]./1000,'--
k', 'LineWidth', 2)
% plot(theta deg,[TH200 DATA(73).pdrop regen experimental]./1000,'--
q','LineWidth',2)
% plot(theta deg,[TH200 DATA(87).pdrop regen experimental]./1000,'--
r','LineWidth',2)
```

```
0
plot(theta deg,[TH200 DATA(5).pdrop regen model]./1000.*8,'k','LineWidth',2)
plot(theta deg,[TH200 DATA(73).pdrop regen model]./1000.*8,'g','LineWidth',2)
plot(theta deg, [TH200 DATA(87).pdrop regen model]./1000.*8, 'r', 'LineWidth', 2)
% xlabel('Crank Angle (\circ)', 'FontName', font, 'FontSize', font size)
% ylabel('Regenerator Pressure Drop
(kPa)', 'FontName', font, 'FontSize', font size)
% xlim([0 360])
% legend('pmean = 707 kPa', 'pmean = 293 kPa', 'pmean = 421
kPa', 'Location', 'South')
% set(gca,'fontsize',font size)
% set(gca, 'FontName', font)
% % Regenerator Pressure Drop Amplitude vs. Speed and Pressure
% figure('Position', [x y width height])
% pointsize = 30;
% maxes = max([TH200 DATA.P1 Pa]./1000);
% mins = min([TH200 DATA.P1 Pa]./1000);
% scatter([TH200 DATA.Engine Hz], (maxes-mins), pointsize,
[TH200 DATA.pmean]./1000)
% ylabel('Regenerator Pressure Drop Amplitude
(kPa)', 'FontName', font, 'FontSize', font size);
% xlabel('Engine Frequency (Hz)', 'FontName', font, 'FontSize', font size)
% c = colorbar;
% ylabel(c,'Mean Pressure (kPa)','FontName',font,'FontSize',font size)
% colormap(jet)
% set(gca,'fontsize',font size)
% set(gca, 'FontName', font)
% % Power Lost to Regenerator Flow Friction (Power consumed by displacer)
% figure('Position', [x y width height])
% pointsize = 30;
% scatter([TH200 DATA.Engine Hz],[TH200 DATA.P lost regen FF], pointsize,
[TH200 DATA.pmean]./1000)
% ylabel('Power Lost to Regenerator Flow Friction
(W) ', 'FontName', font, 'FontSize', font size);
% xlabel('Engine Frequency (Hz)','FontName',font,'FontSize',font size)
% c = colorbar;
% ylabel(c,'Mean Pressure (kPa)','FontName',font,'FontSize',font size)
% colormap(jet)
% set(gca,'fontsize',font size)
% set(gca, 'FontName', font)
00
% % Power Lost to Regenerator Flow Friction with overlaid model
% figure('Position', [x y width height])
% pointsize = 30;
% hold on
% scatter([TH200 DATA.Engine Hz],[TH200 DATA.P lost regen FF], pointsize,
[TH200 DATA.pmean]./1000, '*')
% scatter([TH200 DATA.Engine Hz],[TH200 DATA.P lost regen FF model],
pointsize, [TH200 DATA.pmean]./1000,'o')
% ylabel('Power Lost to Regenerator Flow Friction
(W)', 'FontName', font, 'FontSize', font size);
% xlabel('Engine Frequency (Hz)','FontName',font,'FontSize',font size)
% c = colorbar;
```

```
% ylabel(c,'Mean Pressure (kPa)','FontName',font,'FontSize',font size)
% colormap(jet)
% legend('Experimental Data','Quasi-Steady Model','Location','NorthWest')
% set(gca,'fontsize',font size)
% set(gca, 'FontName', font)
8
% % Error in Regenerator Pressure Drop Amplitude vs. Speed and Pressure
% figure('Position', [x y width height])
% pointsize = 30;
% exp maxes = max([TH200 DATA.pdrop regen experimental]./1000);
% exp mins = min([TH200 DATA.pdrop regen experimental]./1000);
% exp_amps = (exp maxes-exp mins);
% model maxes = max([TH200 DATA.pdrop regen model]./1000);
% model mins = min([TH200 DATA.pdrop regen model]./1000);
% model amps = (model maxes-model mins);
% val model maxes = max([TH200 DATA.pdrop regen model]./1000.*8);
% val model mins = min([TH200 DATA.pdrop regen model]./1000.*8);
% val model amps = (val model maxes-val model mins);
% pdropr error = ((model amps-exp amps)./exp amps).*100;
% val pdropr error = ((val model amps-exp amps)./exp amps).*100;
% hold on
% scatter([TH200 DATA.Engine Hz],pdropr error, pointsize,
[TH200 DATA.pmean]./1000, 'o')
% scatter([TH200 DATA.Engine Hz],val pdropr error, pointsize,
[TH200 DATA.pmean]./1000, '*')
% ylabel({'Regenerator Pressure Drop';'Amplitude Error
(%)'}, 'FontName', font, 'FontSize', font size);
% ylim([-91 25])
% xlabel('Engine Frequency (Hz)', 'FontName', font, 'FontSize', font size)
% c = colorbar;
% ylabel(c,'Mean Pressure (kPa)','FontName',font,'FontSize',font size)
% colormap(jet)
% legend('Original Model','Model x8')
% set(gca,'fontsize',font size)
% set(gca, 'FontName', font)
% Preferential Flow Evidence
% Data for Plot 3 (60 PSI, 600 RPM)
filenameT_0 = 'X:\01_Current_Students\Connor Speer\00_Thesis and Journal
Papers\00 Thesis\00 Data and Plots\Chapter 5 Plots (Model Validation)\Tecknic
Spin Tests\06 HH Rotation Tests\P 60 RPM 600 0 Temp.log';
filenameP 0 = 'X:\01 Current Students\Connor Speer\00 Thesis and Journal
Papers\00 Thesis\00 Data and Plots\Chapter 5 Plots (Model Validation)\Tecknic
Spin Tests\06 HH Rotation Tests\P 60 RPM 600 0 Volt.log';
[theta rounded deg 0, P5 avg bar 0] =
Averaged Data Plots Tecknic Spin(filenameT 0, filenameP 0);
filenameT 1 = 'X:\01 Current Students\Connor Speer\00 Thesis and Journal
Papers\00 Thesis\00 Data and Plots\Chapter 5 Plots (Model Validation)\Tecknic
Spin Tests\06_HH Rotation Tests\P_60_RPM_600_1_Temp.log';
filenameP 1 = 'X:\01 Current Students\Connor Speer\00 Thesis and Journal
Papers\00 Thesis\00 Data and Plots\Chapter 5 Plots (Model Validation)\Tecknic
```

```
Spin Tests\06 HH Rotation Tests\P 60 RPM 600 1 Volt.log';
```

```
[theta_rounded_deg_1,P5_avg_bar_1] =
Averaged_Data_Plots_Tecknic_Spin(filenameT_1,filenameP_1);
```

filenameT_2 = 'X:\01_Current_Students\Connor Speer\00_Thesis and Journal
Papers\00_Thesis\00_Data and Plots\Chapter 5 Plots (Model Validation)\Tecknic
Spin Tests\06_HH Rotation Tests\P_60_RPM_600_2_Temp.log';
filenameP_2 = 'X:\01_Current_Students\Connor Speer\00_Thesis and Journal
Papers\00_Thesis\00_Data and Plots\Chapter 5 Plots (Model Validation)\Tecknic
Spin Tests\06_HH Rotation Tests\P_60_RPM_600_2_Volt.log';
[theta_rounded_deg_2,P5_avg_bar_2] =
Averaged Data Plots Tecknic Spin(filenameT 2,filenameP 2);

filenameT_3 = 'X:\01_Current_Students\Connor Speer\00_Thesis and Journal
Papers\00_Thesis\00_Data and Plots\Chapter 5 Plots (Model Validation)\Tecknic
Spin Tests\06_HH Rotation Tests\P_60_RPM_600_3_Temp.log';
filenameP_3 = 'X:\01_Current_Students\Connor Speer\00_Thesis and Journal
Papers\00_Thesis\00_Data and Plots\Chapter 5 Plots (Model Validation)\Tecknic
Spin Tests\06_HH Rotation Tests\P_60_RPM_600_3_Volt.log';
[theta_rounded_deg_3,P5_avg_bar_3] =
Averaged_Data_Plots_Tecknic_Spin(filenameT_3,filenameP_3);

filenameT_4 = 'X:\01_Current_Students\Connor Speer\00_Thesis and Journal
Papers\00_Thesis\00_Data and Plots\Chapter 5 Plots (Model Validation)\Tecknic
Spin Tests\06_HH Rotation Tests\P_60_RPM_600_4_Temp.log';
filenameP_4 = 'X:\01_Current_Students\Connor Speer\00_Thesis and Journal
Papers\00_Thesis\00_Data and Plots\Chapter 5 Plots (Model Validation)\Tecknic
Spin Tests\06_HH Rotation Tests\P_60_RPM_600_4_Volt.log';
[theta_rounded_deg_4,P5_avg_bar_4] =
Averaged Data Plots Tecknic Spin(filenameT 4,filenameP 4);

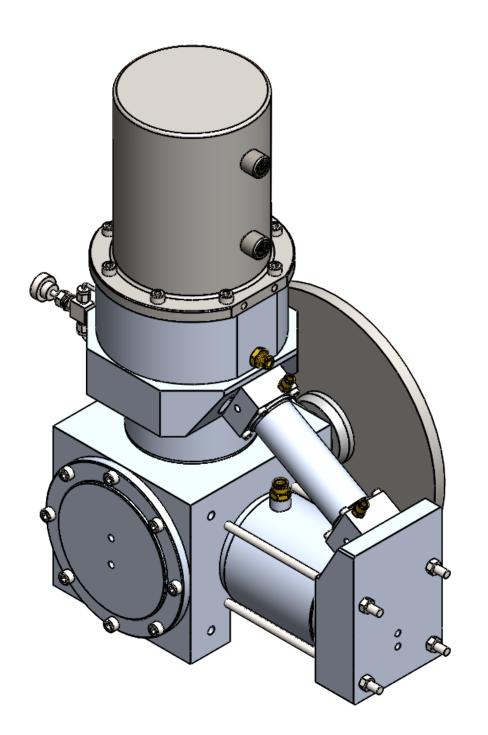
```
filenameT_5 = 'X:\01_Current_Students\Connor Speer\00_Thesis and Journal
Papers\00_Thesis\00_Data and Plots\Chapter 5 Plots (Model Validation)\Tecknic
Spin Tests\06_HH Rotation Tests\P_60_RPM_600_5_Temp.log';
filenameP_5 = 'X:\01_Current_Students\Connor Speer\00_Thesis and Journal
Papers\00_Thesis\00_Data and Plots\Chapter 5 Plots (Model Validation)\Tecknic
Spin Tests\06_HH Rotation Tests\P_60_RPM_600_5_Volt.log';
[theta_rounded_deg_5,P5_avg_bar_5] =
Averaged_Data_Plots_Tecknic_Spin(filenameT_5,filenameP_5);
```

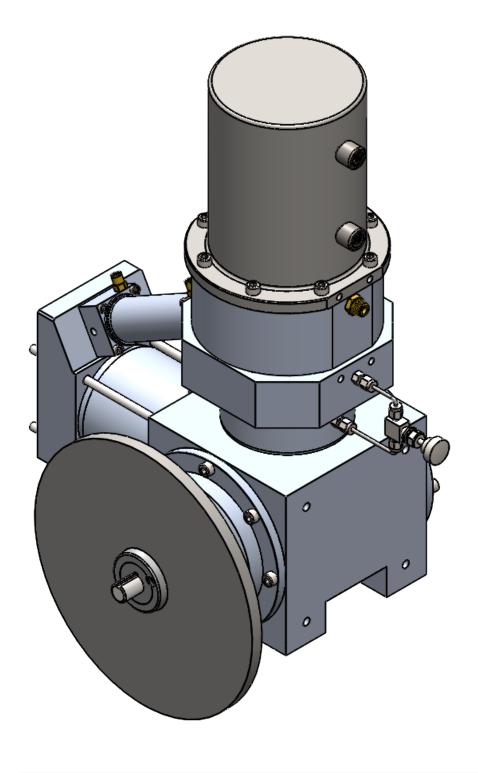
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filenameT_6 = 'X:\01_Current_Students\Connor Speer\00_Thesis and Journal
Papers\00_Thesis\00_Data and Plots\Chapter 5 Plots (Model Validation)\Tecknic
Spin Tests\06_HH Rotation Tests\P_60_RPM_600_6_Temp.log';
filenameP_6 = 'X:\01_Current_Students\Connor Speer\00_Thesis and Journal
Papers\00_Thesis\00_Data and Plots\Chapter 5 Plots (Model Validation)\Tecknic
Spin Tests\06_HH Rotation Tests\P_60_RPM_600_6_Volt.log';
[theta_rounded_deg_6,P5_avg_bar_6] =
Averaged_Data_Plots_Tecknic_Spin(filenameT_6,filenameP_6);
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filenameT_7 = 'X:\01_Current_Students\Connor Speer\00_Thesis and Journal
Papers\00_Thesis\00_Data and Plots\Chapter 5 Plots (Model Validation)\Tecknic
Spin Tests\06_HH Rotation Tests\P_60_RPM_600_7_Temp.log';
filenameP_7 = 'X:\01_Current_Students\Connor Speer\00_Thesis and Journal
Papers\00_Thesis\00_Data and Plots\Chapter 5 Plots (Model Validation)\Tecknic
Spin Tests\06_HH Rotation Tests\P_60_RPM_600_7_Volt.log';
[theta_rounded_deg_7,P5_avg_bar_7] =
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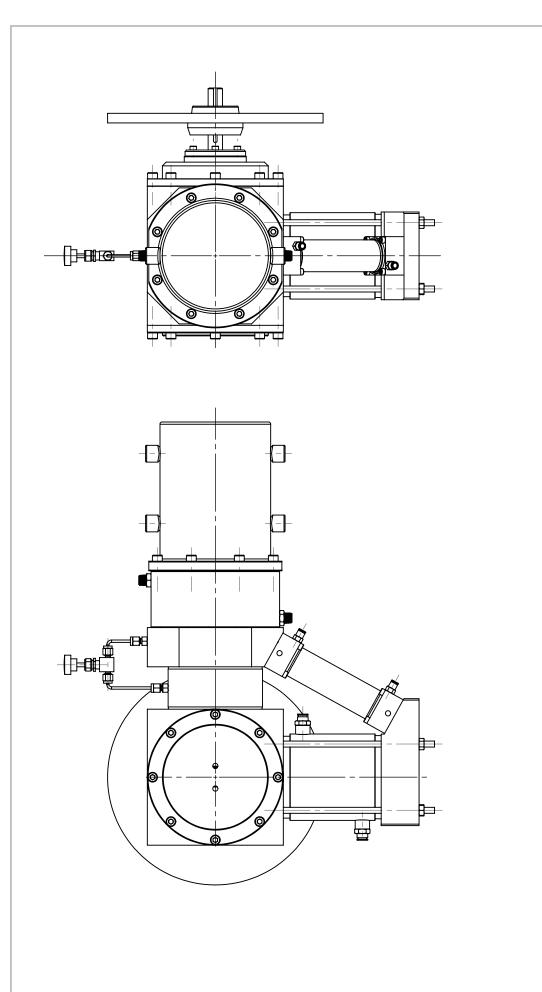
```
% Polar Plot of Heater Pressure Drop Amplitude
figure('Position', [x y width height])
amp \ Odeg = (max(P5 \ avg \ bar \ 0)) - min(P5 \ avg \ bar \ 0))*100;
amp 45deg = (max(P5 avg bar 1) - min(P5 avg bar 1))*100;
amp 90deg = (max(P5 avg bar 2) - min(P5 avg bar 2))*100;
amp_135deg = (max(P5_avg_bar_3) - min(P5_avg_bar_3))*100;
amp 180deg = (max(P5 avg bar 4) - min(P5 avg bar 4))*100;
amp 225deg = (max(P5 avg bar 5) - min(P5 avg bar 5))*100;
amp 270deg = (max(P5 avg bar 6) - min(P5 avg bar 6))*100;
amp 315deg = (max(P5 avg bar 7) - min(P5 avg bar 7))*100;
HHangles = [0 \ 45 \ 90 \ 135 \ 180 \ 225 \ 270 \ 315 \ 0];
HHangles = HHangles*(pi/180);
amps = [amp 0deg amp 45deg amp 90deg amp 135deg amp 180deg amp 225deg
amp 270deg amp 315deg amp 0deg];
polarplot(HHangles, amps, '-o', 'LineWidth', 2)
ax = qca;
ax.ThetaTickLabel = {'Power Cylinder',' ',' ',' ',' Bypass Line',' ',' '};
ax.ThetaTick = [0 45 90 135 180 225 270 315];
figure('Position', [x y width height])
hold on
plot([TH200 DATA.pmean]./1000,mean([TH200 DATA.T 2]),'ob')
plot([TH200 DATA.pmean]./1000,mean([TH200 DATA.T 3]), '*r')
ylabel({'Temperature (\circC)'}, 'FontName', font, 'FontSize', font size);
xlabel('Mean Pressure (kPa)', 'FontName', font, 'FontSize', font size)
legend('Regenerator Cold Left (Bypass Side)', 'Regenerator Cold Right (Power
Cylinder Side)', 'Location', 'NorthWest')
set(gca, 'fontsize', font size)
set(gca, 'FontName', font)
hold off
```

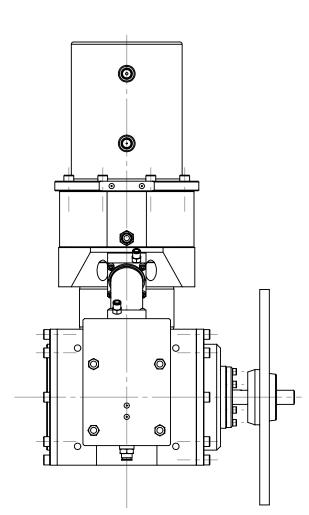
Appendix E: Drawing Package for Modified Stirling Engine



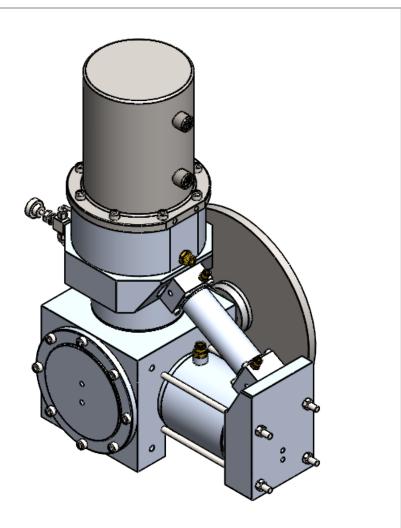


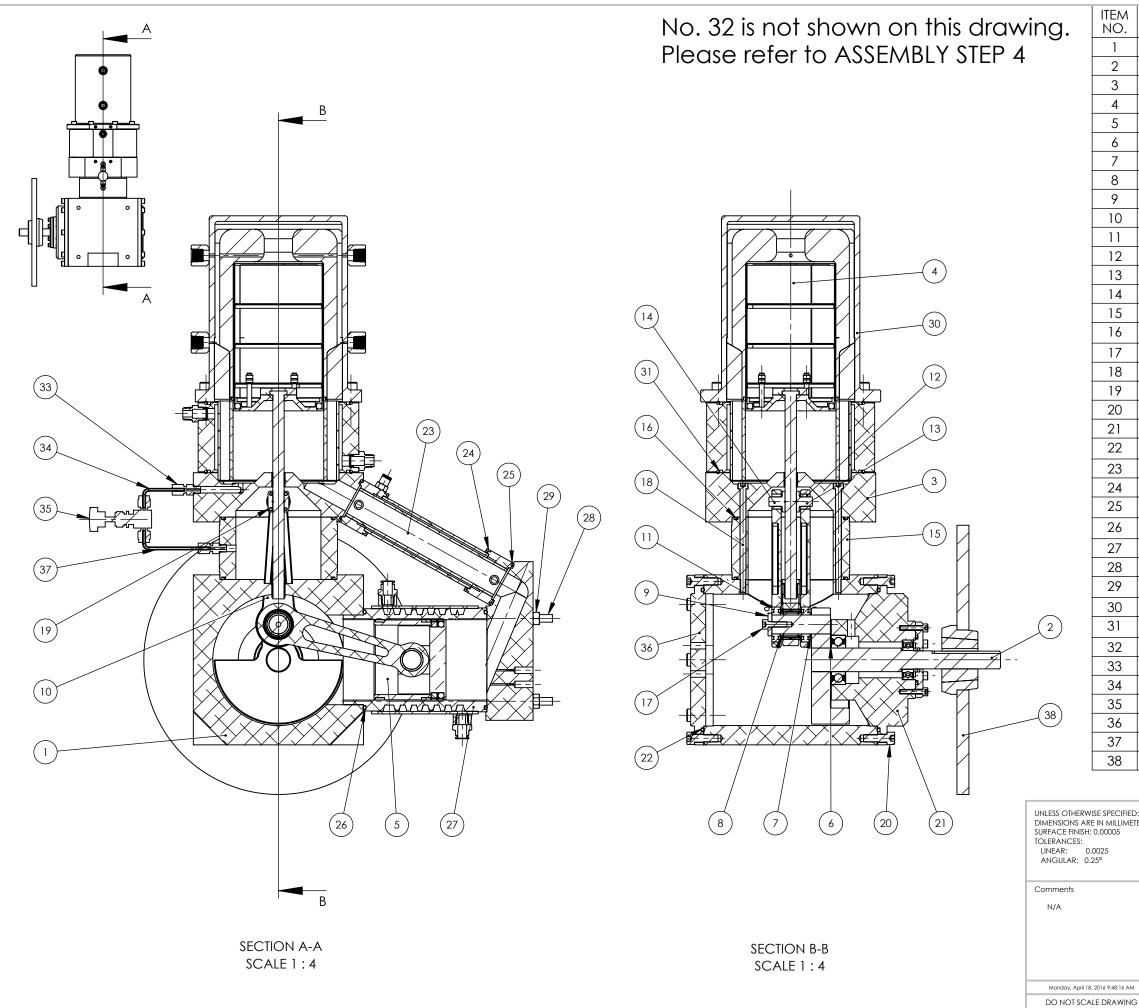
UNLESS OTHERWISE SPECIFIED: DIMENSIONS ARE IN MILLIMETERS SURFACE FINISH: 0.00005 TOLERANCES: LINEAR: 0.0025 ANGUI AR: 0.25°	NOBES RESEARCH GROUP				UASolve TEC Edmonton Department of Mechanical Engineering UNIVERSITY OF ALBERTA				
74400B44. 0.20	DRAWN	Jiacheng Yao	TITLE:						
Comments									
N/A	SOLID by	Jiacheng Yao	CSE 1 Owwall Accomply						
	CHK'D	Connor Speer	GSE - 1 Overall Assembly						
	APPV'D	NOT APPROVED							
	Material:				DWG NO.			REVISION	
	N/A				STIRLING_ENGINE_RESEARCH_VERSION				
Monday, April 18, 2016 9:48:16 AM									
DO NOT SCALE DRAWING	DRW File: 000_STIRLING_ENGINE_RESEARCH_VERSION			Projec	et: GSE-1	Mass:	SCALE:1:3.5 SHEET	1 OF 8	





UNLESS OTHERWISE SPECIFIED: DIMENSIONS ARE IN MILLIMETERS SURFACE FINISH: 0.00005 TOLERANCES: LINEAR: 0.0025 ANGULAR: 0.25°	NOBES RESEARCH GROUP				UASolve TEC Edmonton Department of Mechanical Engineering UNIVERSITY OF ALBERTA				
ANGULAR. 0.25	DRAWN	Jiacheng Yao	TITLE:						
Comments N/A	SOLID by	Jiacheng Yao	GSE - 1 Overall Assembly						
	CHK'D	Connor Speer							
	APPV'D	NOT APPROVED							
	Material:			[DWG NO.				REVISION
		N/A			STIRLING_ENGINE_RESEARCH_VERSION				
Monday, April 18, 2016 9:48:16 AM						-	-	_	<i>·</i> · ·
DO NOT SCALE DRAWING	DRW File: 000_STIRLING_ENGINE_RESEARCH_VERSION PI			Project:	GSE-1	Mass:	SCALE:1:5	SHEET	2 OF 8



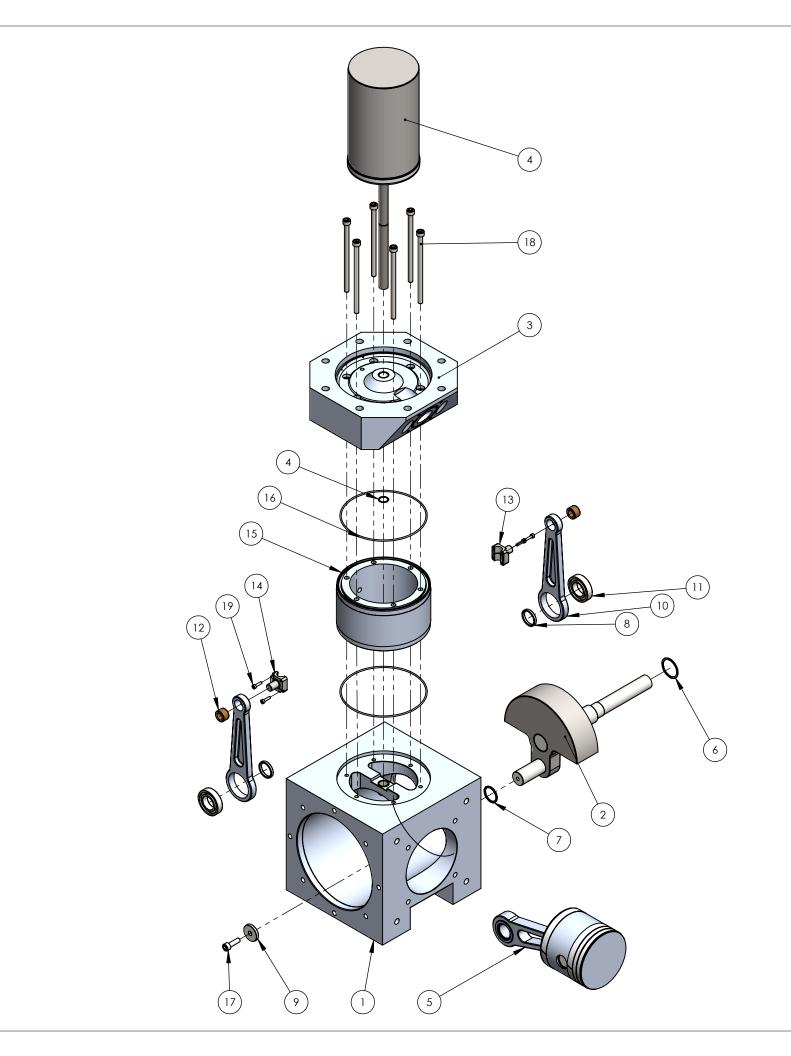


C-CS-Z-0 A-DM-Z-0 A-DP-F B-PP-Z-00	DO-CRANKCASE_ASM O-CRANKSHAFT_ASM DO-DISP_MOUNT_ASM -00-DISP_FULL_ASM	1							
A-DM-Z-0 A-DP-F B-PP-Z-00	DO-DISP_MOUNT_ASM	1							
A-DP-F B-PP-Z-00									
B-PP-Z-00-	-00-DISP FULL ASM	1							
C-ZZ-	POWER_PISTON_ASM	1							
C-72-7-02-SPACER_115									
C-ZZ-	Z-03-SPACER_116	1							
C-ZZ-	Z-04-SPACER_117	2							
C-ZZ-	Z-05-SPACER_118	1							
A-ZZ-Z-04-DISP_PISTON_ROD									
AFBMA 20.1	- 19-20 - 14,SI,NC,14_68	2							
A-ZZ-Z-05-BI	RONZE_BUSHING_10MM	2							
A-ZZ-Z-	-02-R_CROSSHEAD	1							
A-ZZ-Z	-03-L_CROSSHEAD	1							
A	-ZZ-Z-01-FOOT	1							
O-ring 1	12x1.8-A-ISO 3601-1	2							
B18.3.1M - 6 x	1.0 x 20 Hex SHCS 20NHX	1							
B18.3.1M - 6 x 1	.0 x 110 Hex SHCS 24NHX	6							
B18.3.1M - 3 x	0.5 x 12 Hex SHCS 12NHX	4							
B18.3.1M - 8 x 1	.25 x 25 Hex SHCS 25NHX	16							
C-BC-Z-00-BE	ARING CARTRIDGE ASM	1							
		2							
		1							
		8							
		1							
		1							
		4							
		-							
	•	4							
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B18.3.1M - 8 x 1	.25 x 30 Hex SHCS 30NHX	8							
		2							
A-ZZ-Z-	10-BYPASS_TUBE_2	1							
A-ZZ-Z-	-06-0.125IN_VALVE	1							
C-	ZZ-Z-01-COVER	1							
		1							
	00-FLYWHEEL ASM	1							
	C-ZZ- A-ZZ-Z-0 AFBMA 20.1 A-ZZ-Z-05-BF A-ZZ-Z A-ZZ-Z A-ZZ-Z A B18.3.1M - 6 x B18.3.1M - 8 x C-BC-Z-00-BE O-ring D B-CP-Z- B18.3.1M - 5 x O-ring D B-CP-Z- B18.3.1M - 5 x O-ring D B-PC-Z-C C-ZZ-Z- B18.2.4.1M - Hex A-DC-Z D-ring 13 B18.3.1M - 8 x 1 A-ZZ-Z-07-C A-ZZ-Z- A-ZZ-Z-	C-ZZ-Z-05-SPACER_118							

STIRLING	ENGINE	RESEARCH	VERSION

REVISION

DO NOT SCALE DRAWING DRW File: 000_STIRLING_ENGINE_RESEARCH_VERSION Project: GSE-1 SCALE:1:5 SHEET 3 OF 8



ITEM NO.	DRW NUMBER	Assembly Step 1/QTY.
1	C-CC-Z-00-CRANKCASE_ASM	1
2	C-CS-Z-00-CRANKSHAFT_ASM	1
3	A-DM-Z-00-DISP_MOUNT_ASM	1
4	A-DP-F-00-DISP_FULL_ASM	1
5	B-PP-Z-00-POWER_PISTON_ASM	1
6	C-ZZ-Z-02-SPACER_115	1
7	C-ZZ-Z-03-SPACER_116	1
8	C-ZZ-Z-04-SPACER_117	2
9	C-ZZ-Z-05-SPACER_118	1
10	A-ZZ-Z-04-DISP_PISTON_ROD	2
11	AFBMA 20.1 - 19-20 - 14,SI,NC,14_68	2
12	A-ZZ-Z-05-BRONZE_BUSHING_10MM	2
13	A-ZZ-Z-02-R_CROSSHEAD	1
14	A-ZZ-Z-03-L_CROSSHEAD	1
15	A-ZZ-Z-01-FOOT	1
16	O-ring 112x1.8-A-ISO 3601-1	2
17	B18.3.1M - 6 x 1.0 x 20 Hex SHCS 20NHX	1
18	B18.3.1M - 6 x 1.0 x 110 Hex SHCS 24NHX	6
19	B18.3.1M - 3 x 0.5 x 12 Hex SHCS 12NHX	4

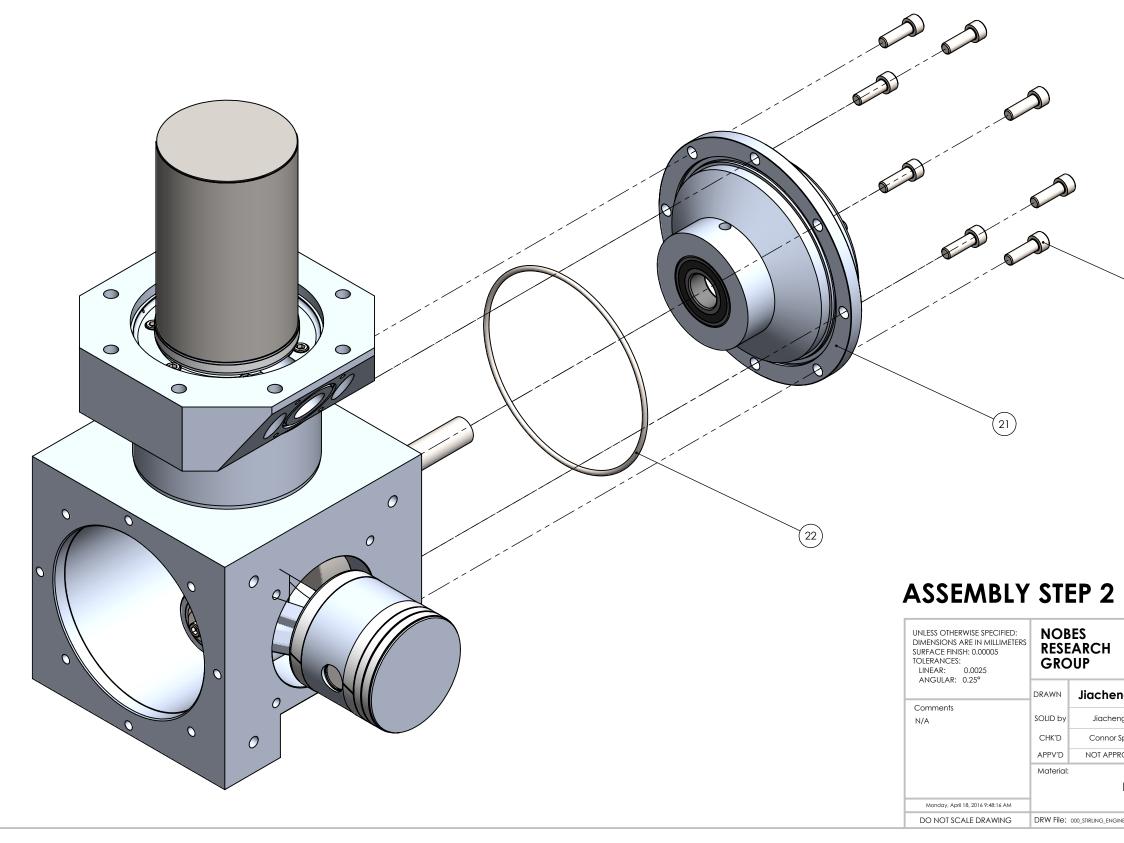
ASSEMBLY STEP 1

UNLESS OTHERWISE SPECIFIED: DIMENSIONS ARE IN MILLIMETERS SURFACE FINISH: 0.00005 TOLERANCES: LINEAR: 0.0025 ANGULAR: 0.25°	NOBES RESEARCH GROUP		
ANOULAR. 0.25	DRAWN	Jiachen	
Comments N/A	SOLID by	Jiacheng	
	CHK'D	Connor Sp	
	APPV'D	NOT APPRC	
	Material		
		1	
Monday, April 18, 2016 9:48:16 AM			
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UNIVERSITY OF ALBERTA

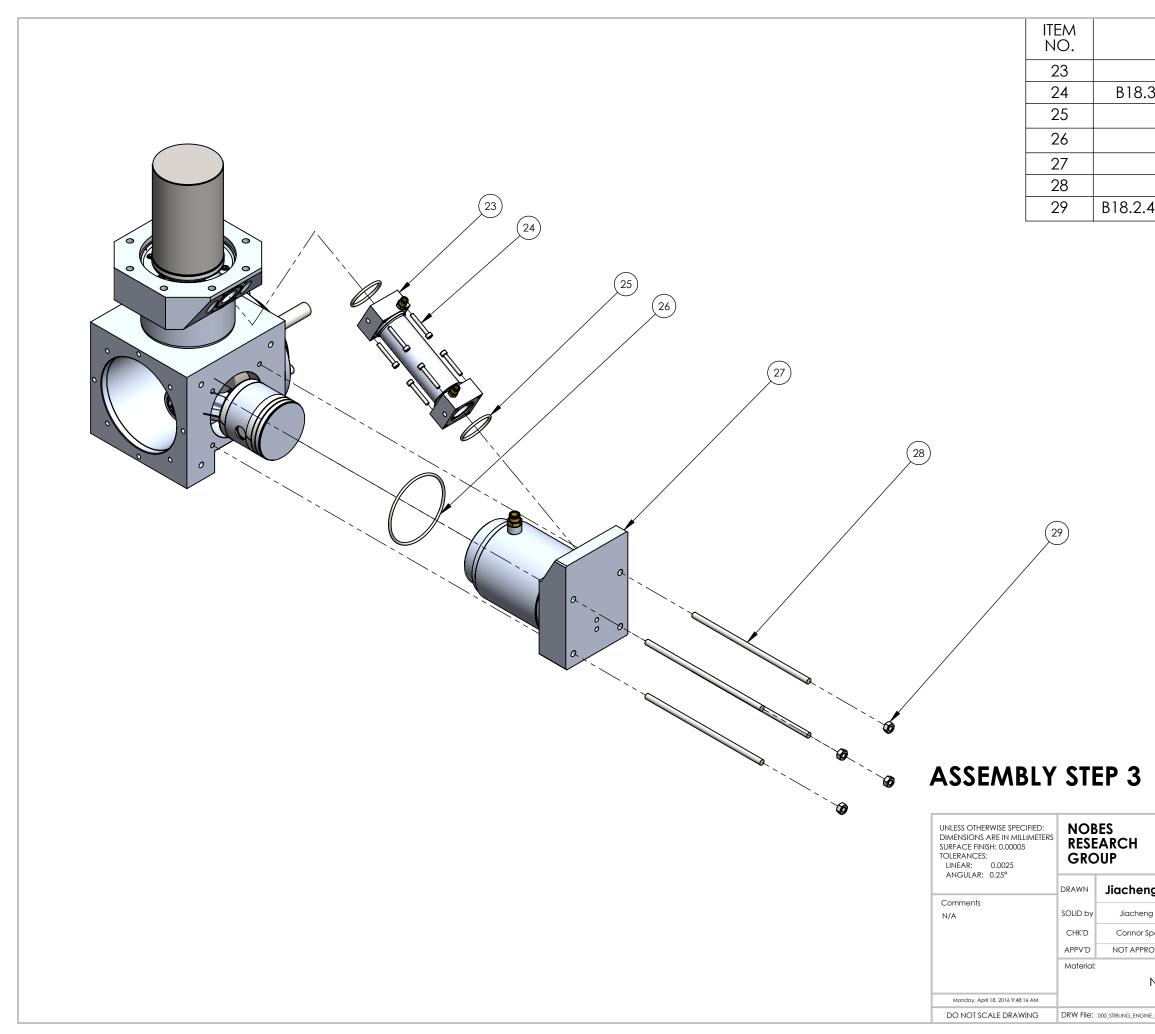
g Yao	TITLE:						
g Yao			CSF 10	Quarall A	ssamhl	X 7	
peer		•	GSE - 1 (Jver all A		y	
OVED							
N/A			DWG NO. STIRLING	_ENGINE_RESE	EARCH_VERS	SION	REVISION A
e_research_ver	REARCH_VERSION Project: GSE-1 Mass: SCALE:1:5 SHEET 4 C				4 OF 8		

ITEM NO.	DRW NUMBER	Assembly Step 2/QTY.
20	B18.3.1M - 8 x 1.25 x 25 Hex SHCS 25NHX	8
21	C-BC-Z-00-BEARING_CARTRIDGE_ASM	1
22	O-ring DIN 3771 - 145x3.55	1



20

g Yao	TITLE:						
g Yao			CSF 1	Overell A	ssamhl	T 7	
beer			USE - I	Overall A	Issembl	y	
OVED							
N/A			DWG NO. STIRLING	G_ENGINE_RESH	EARCH_VERS	SION	REVISION
E_RESEARCH_VER	SION	Projec	t: GSE-1	Mass:	SCALE:2:5	SHEET	5 OF 8

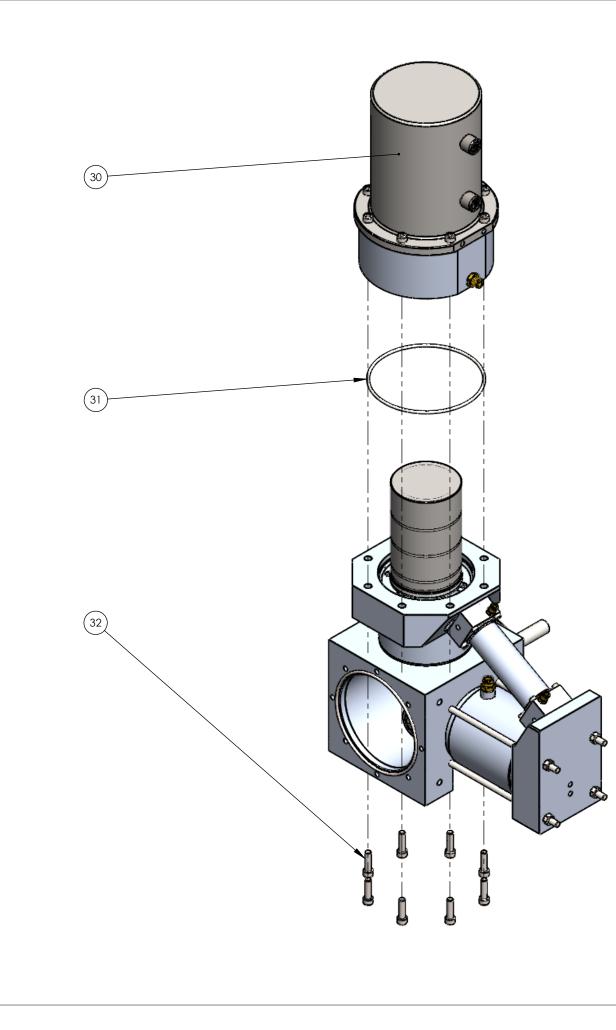


DRW NUMBER	Assembly Step 3/QTY.
B-CP-Z-00-CNCT_PIPE_ASM	1
3.1M - 5 x 0.8 x 35 Hex SHCS 22NHX	8
O-ring DIN 3771 - 43.7x3.55	2
O-ring DIN 3771 - 97.5x3.55	1
B-PC-Z-00-POWER_CYL_ASM	1
C-ZZ-Z-06-THREADED_ROD	4
4.1M - Hex nut, Style 1, M8 x 1.25D-N	4

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UNIVERSITY OF ALBERTA

g Yao	TITLE:						
g Yao			CSF 1	Ovorall A	ssomh	X 7	
peer			U2F - I	Overall A	Issembl	y	
OVED							
			DWG NO.	G ENGINE RESI	TADCH VED	SION	REVISION
N/A			STIKLIW	J_ENGINE_KESI	LAKCH_VER		A
E_RESEARCH_VE	rsion	Projec	et: GSE-1	Mass:	SCALE:1:5	SHEET	6 OF 8

ITEM NO.	PART NUMBER	Assembly Step 4/QTY.
30	A-DC-Z-00-DISP-CYL_ASM	1
31	O-ring 150x3.55-A-ISO 3601-1	1
32	B18.3.1M - 8 x 1.25 x 30 Hex SHCS 30NHX	8

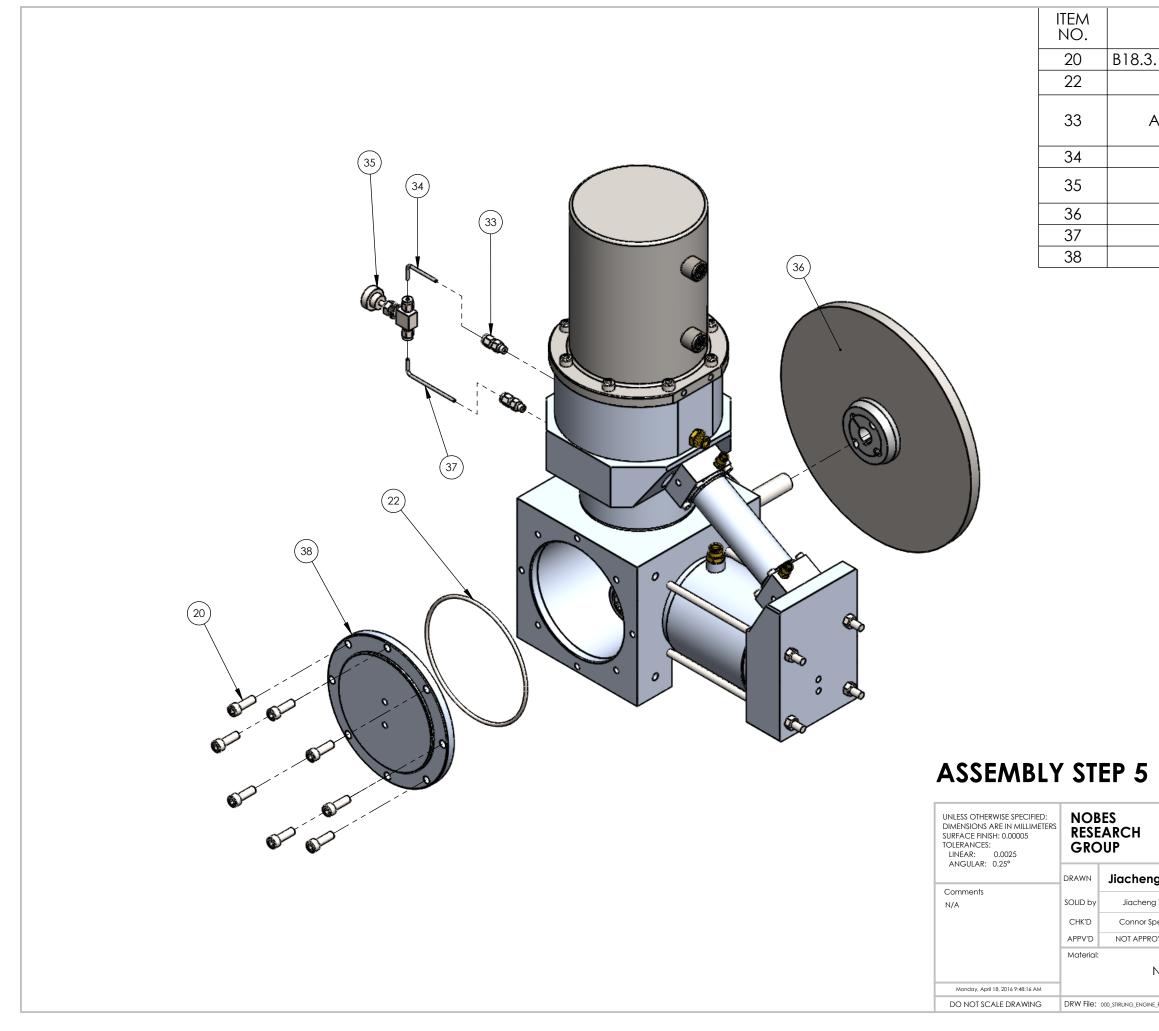


ASSEMBLY STEP 4

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74400E44. 0.25	DRAWN	Jiachen
Comments N/A	SOLID by	Jiacheng
	CHK'D	Connor Sp
	APPV'D	NOT APPRC
	Material:	
		1
Monday, April 18, 2016 9:48:16 AM		
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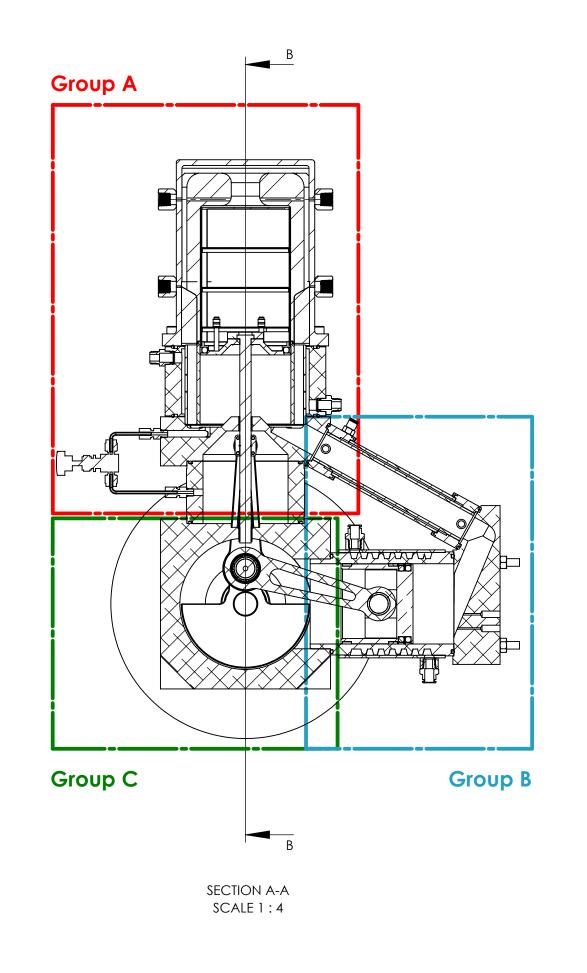
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g Yao			CSF 1	Overell A	ssombl	T 7	
peer			GSE - I	Overall A	Issembl	y	
OVED							
N/A			DWG NO. STIRLING	G_ENGINE_RESH	EARCH_VERS	SION	REVISION
e_research_ver	RSION	Projec	rt: GSE-1	Mass:	SCALE:1:5	SHEET	7 OF 8

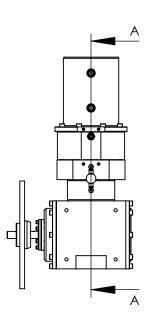


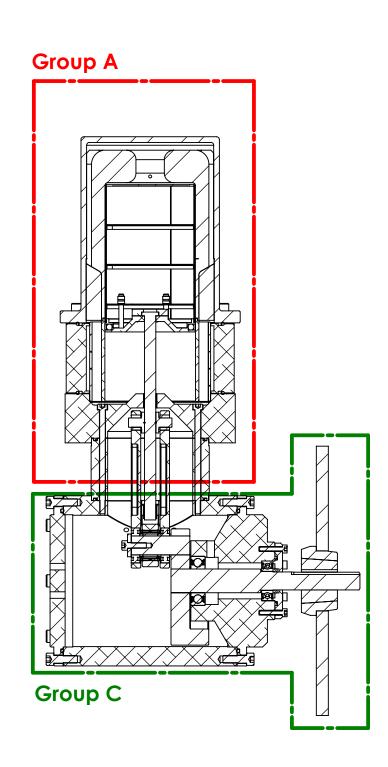
PART NUMBER	Assembly Step 5/QTY.
3.1M - 8 x 1.25 x 25 Hex SHCS 25NHX	16
O-ring DIN 3771 - 145x3.55	2
A-ZZ-Z-07-0.125IN_ST_SWAGELOK	2
A-ZZ-Z-10-BYPASS_TUBE_2	1
A-ZZ-Z-06-0.125IN_VALVE	1
C-ZZ-F-00-FLYWHEEL_ASM	1
A-ZZ-Z-09-BYPASS_TUBE_1	1
C-ZZ-Z-01-COVER	1

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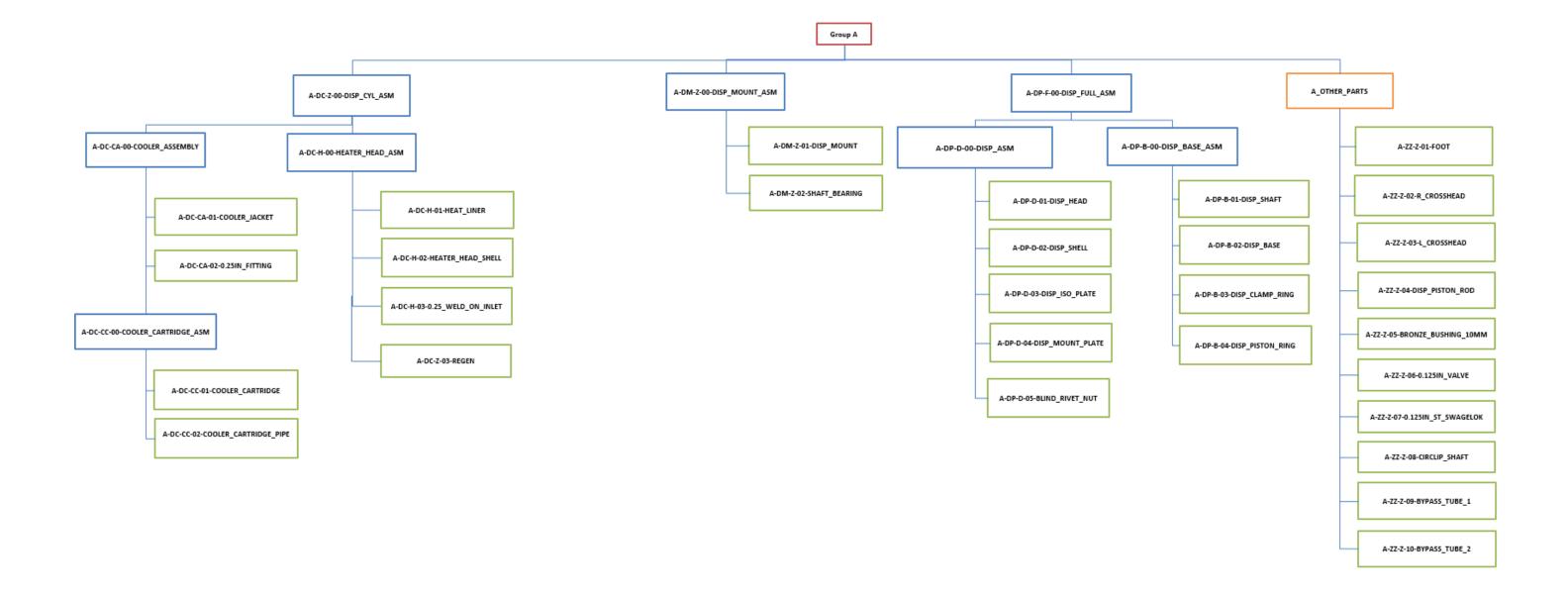
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g Yao			CSF 1	Ovoroll A	ssombl	X 7	
peer			GSE - I	Overall A	Issembl	y	
OVED							
N/A			DWG NO. STIRLING	G_ENGINE_RESI	EARCH_VERS	SION	REVISION
E_RESEARCH_VE	rsion	Projec	t: GSE-1	Mass:	SCALE:1:4	SHEET	8 OF 8

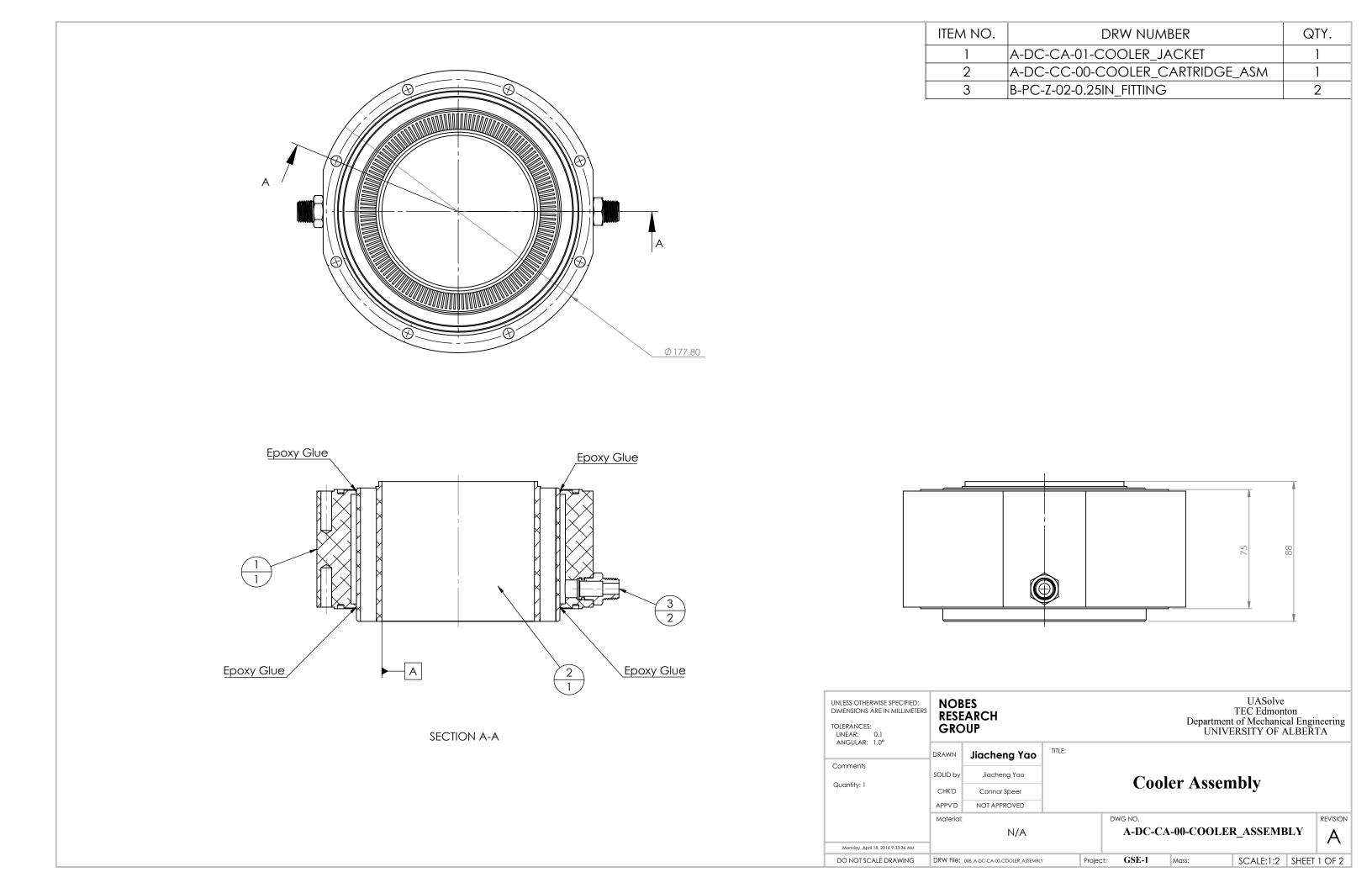


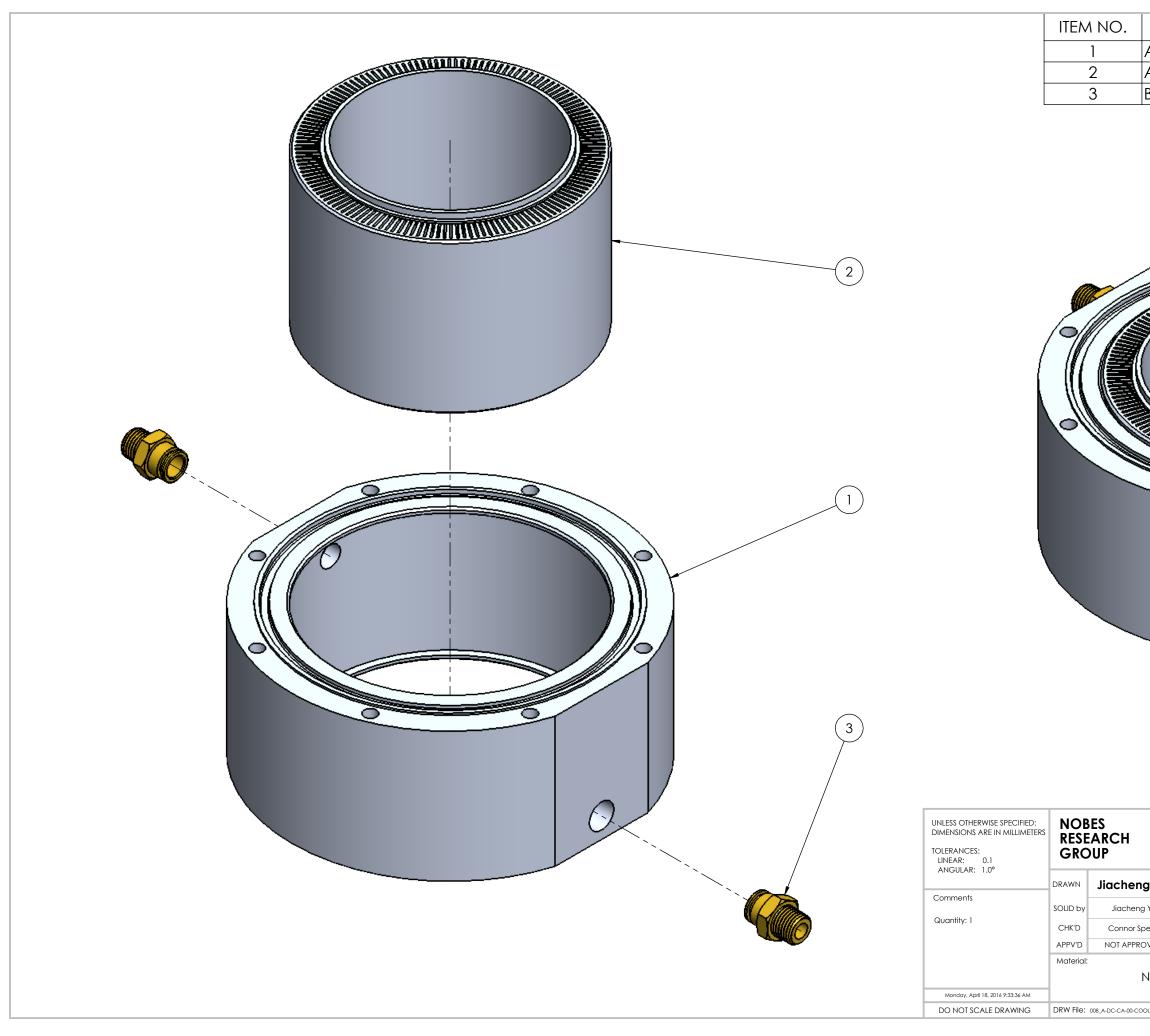




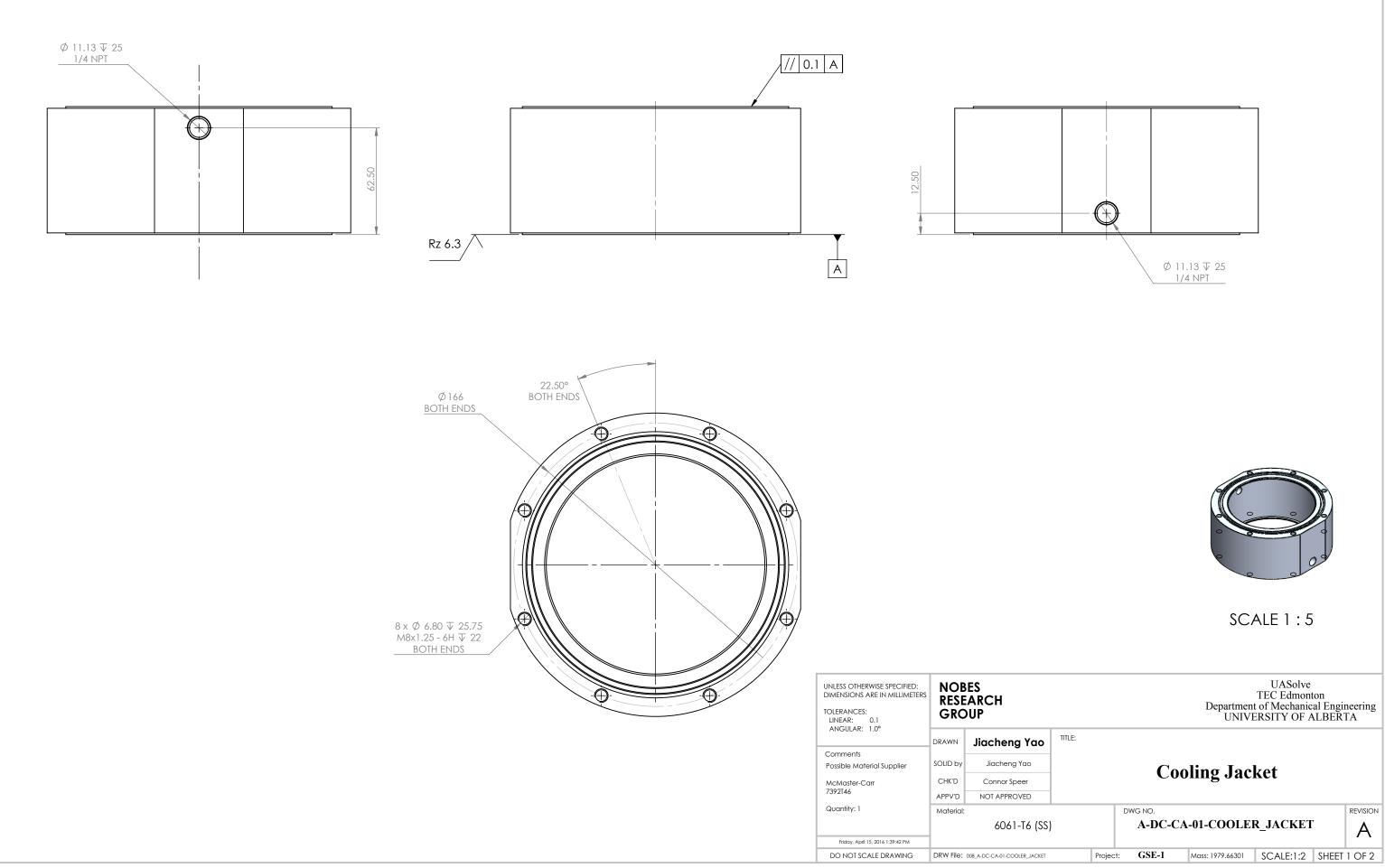
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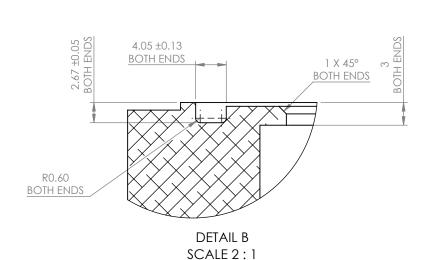


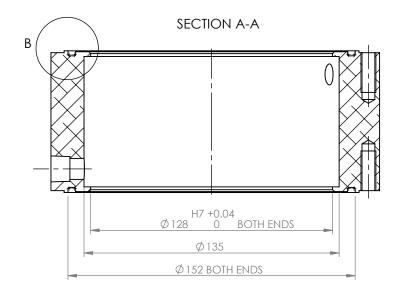


	C		√BER		QTY.
A-DC-C	A-01-C	DOLER .	JACKET		1
				DGE_ASM	1
-	02-0.25				2
			Depa	UASolva TEC Edmoi artment of Mechani UNIVERSITY OF	nton
ng Yao 🗧	ſLE:				
ng Yao		\mathbf{C}	1. 4		
Speer		Coo	oler As	ssembly	
ROVED					
N/A		DWG NO. A-DC-C	СА-00-СО	OLER_ASSEM	BLY A
COOLER_ASSEMBLY	Project:	GSE-1	Mass:	SCALE:2:3	SHEET 2 OF 2

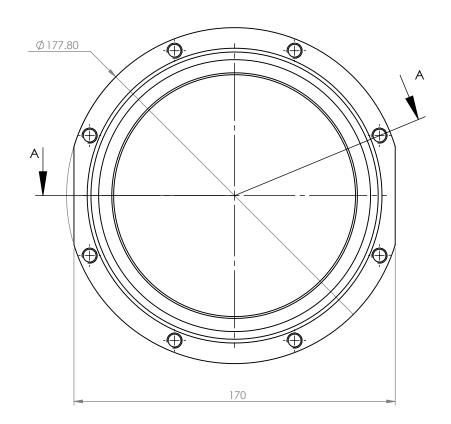


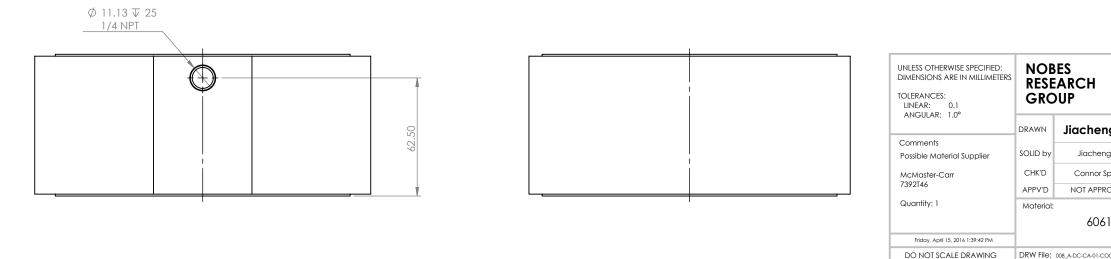
OLER_JACKET	Project:	GSE-1	Mass: 1979.66301	SCALE:1:2	SHEET 1 OF 2





O-Ring Information Size: 145 x 3.5mm Supplier: Hi-Tech Seals Part #: 35145 Material: 1, Viton and 1, Nitrile





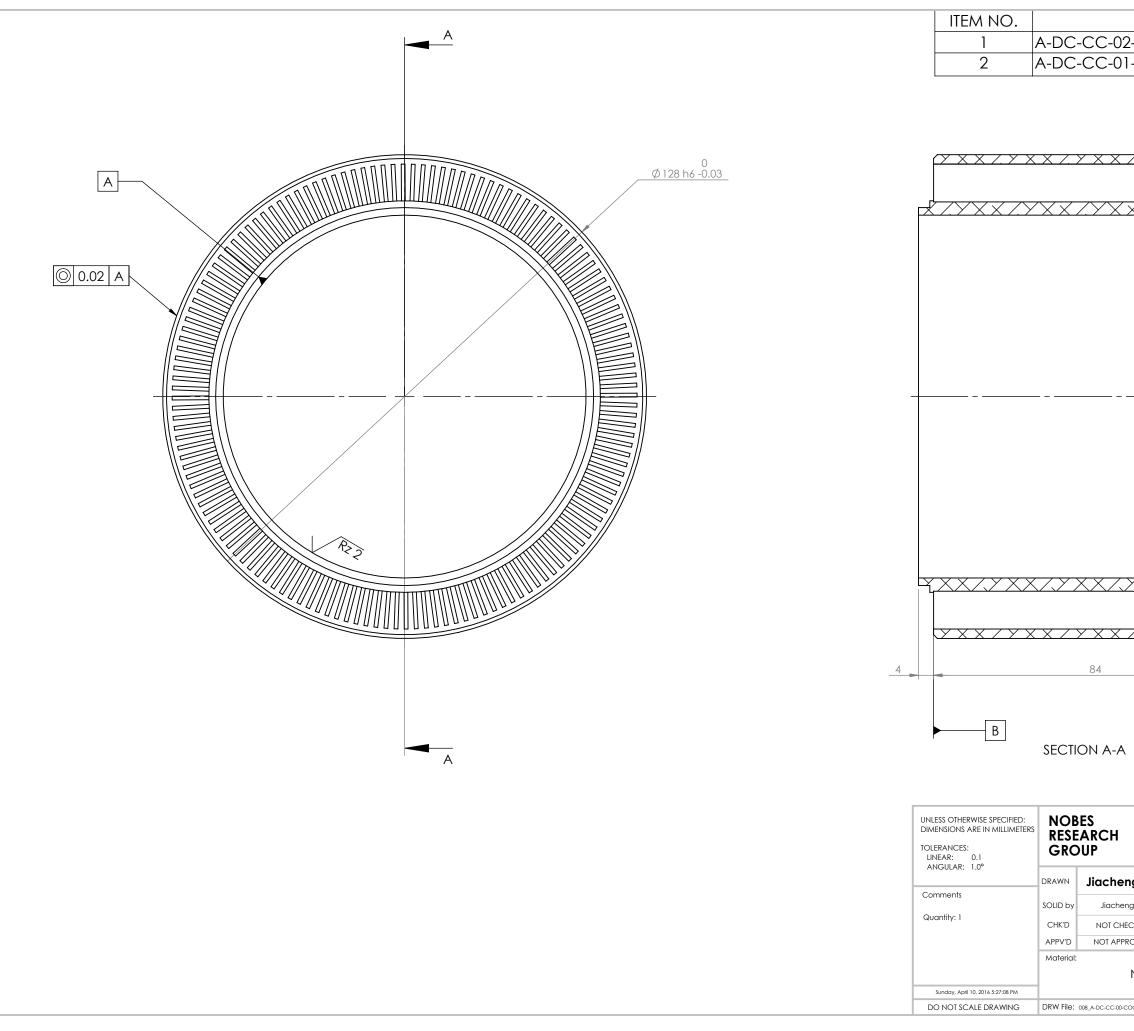


SCALE 1 : 5

Please fillet/chamfer all edges to R0.3

General surface finish: VRz 10

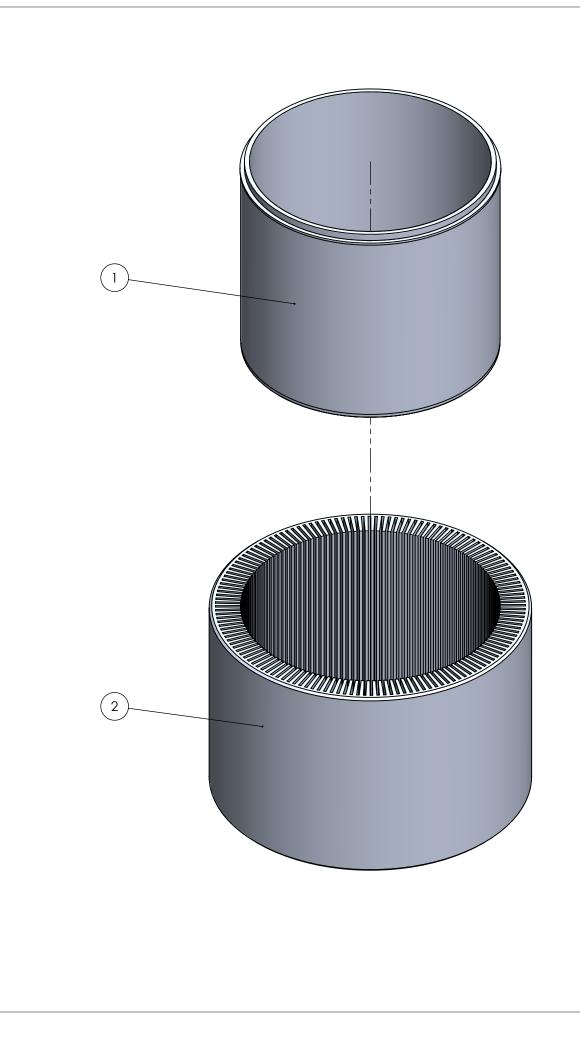
g Yao	TITLE:						
g Yao			Co	oling Jac	lzot		
beer			CU	uning Jac	KEL		
OVED							
			DWG NO.				REVISION
I-T6 (SS)			A-DC-C	A-01-COOLE	R_JACKET	- -	А
OLER_JACKET		Projec	et: GSE-1	Mass: 1979.66301	SCALE:1:2	SHEET	2 OF 2

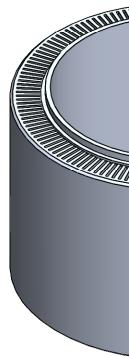


DRW NUMBER		Material	QTY.
2-COOLER_CAI		6061-T6 (SS)	1
1-COOLER_CA	RTRIDGE	6061 Alloy	1
		1 2	
	Ι	UASolve TEC Edmon Department of Mechanic UNIVERSITY OF	iton
ng Yao IIILE: Ang Yao ECKED ROVED		idge Assemb	
N/A	DWG NO. A-DC-CC-00-CO	OLER_CARTRIDGE_A	SM REVISION

0-COOLER CARTRIDGE ASM Project: GSE-1 Mass: SCALE-1-1 SHEET 1 OF 2	N/A		А-ДС-СС	-00-COOLER_CA	.KTKIDGE_A	
	0-COOLER_CARTRIDGE_ASM	Project:	GSE-1	Mass:	SCALE:1:1	SHEET 1 OF

	Material QTY.
	5061-T6 (SS) 1
	6061 Alloy 1
LERANCES: INEAR: 0.1	UASolve TEC Edmonton artment of Mechanical Engineer UNIVERSITY OF ALBERTA
DRAWN Jiacheng Yao	
solid by Jiacheng Yao Cooler Cartrid	

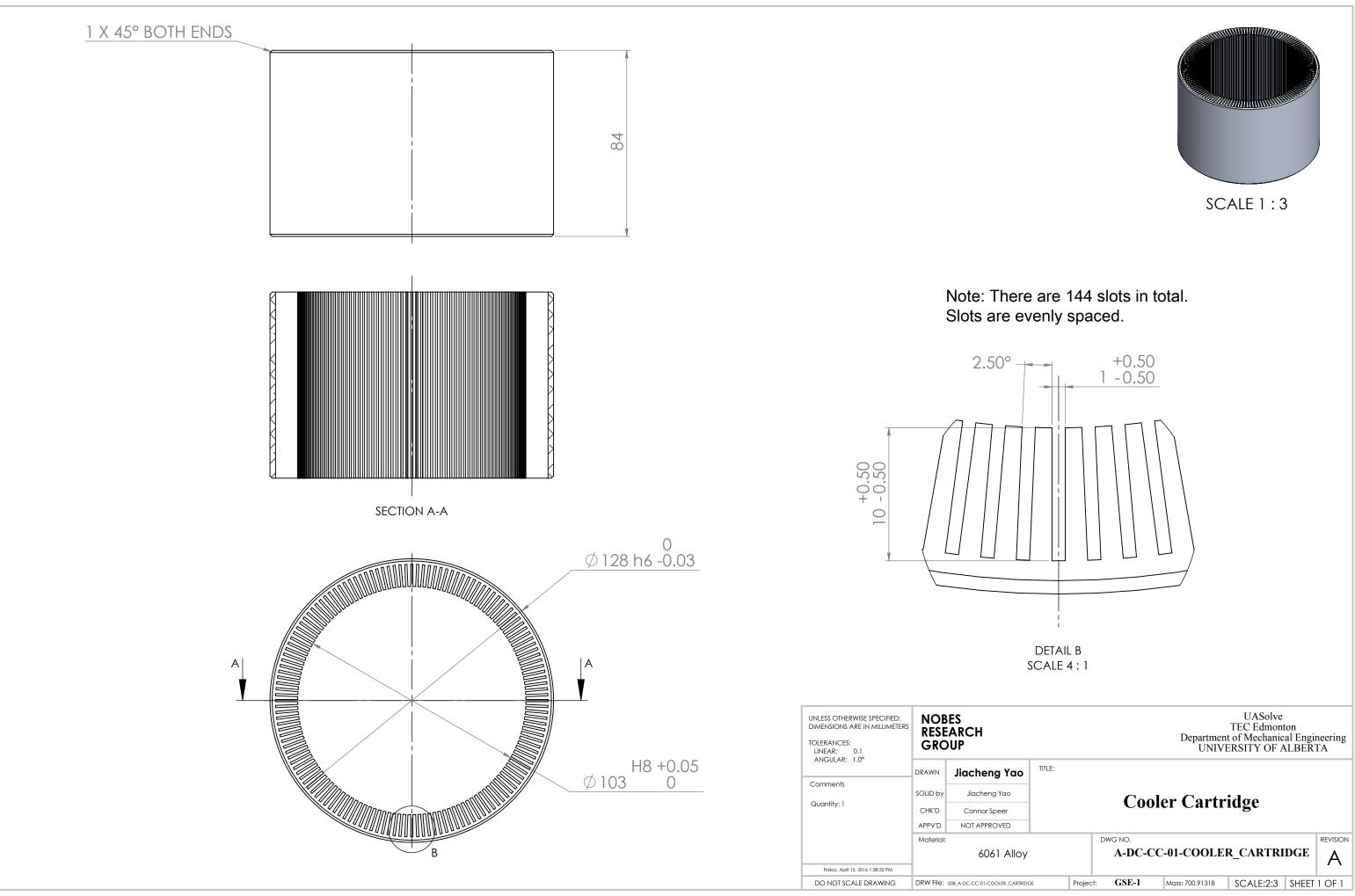




UNLESS OTHERWISE SPECIFIED: DIMENSIONS ARE IN MILLIMETERS TOLERANCES: LINEAR: 0.1 ANGULAR: 1.0°	NOB RESE GRC	ARCH
ANOULAR. 1.0	DRAWN	Jiacheng Yo
Comments	SOLID by	Jiacheng Yao
Quantity: 1	CHK'D	NOT CHECKED
	APPV'D	NOT APPROVED
	Material:	
		N/A
Sunday, April 10, 2016 5:27:08 PM		
DO NOT SCALE DRAWING	DRW File:	008_A-DC-CC-00-COOLER_C

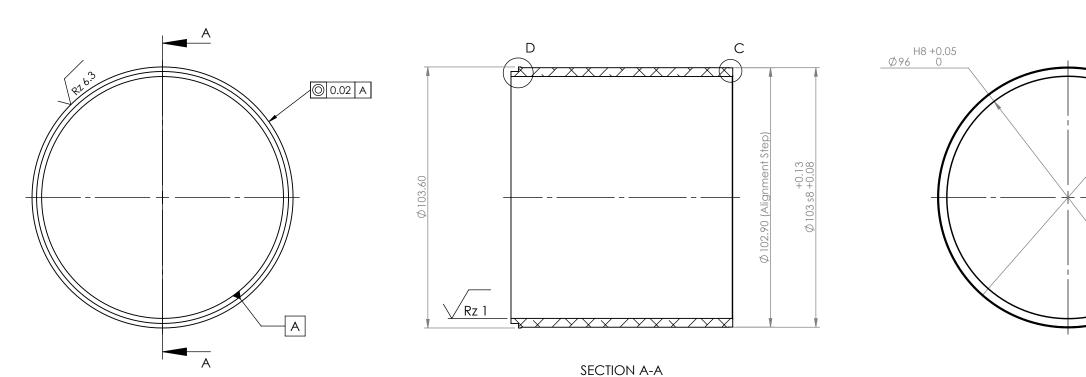
Cooler Cartridge Assembly

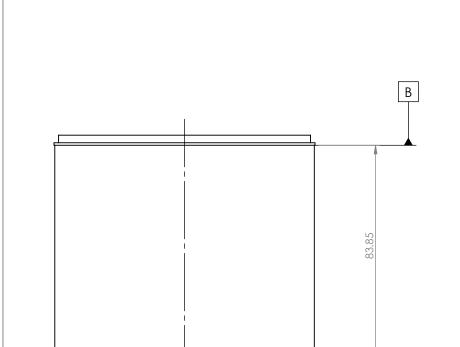
ROVED								
			DWG NO.					
N/A A-DC-CC-00-COOLER_CARTRIDGE_ASM						А		
OOLER_CARTRIDGE_A	.sm P	Project	GSE-1	Mass:	SCALE:1:1	SHEET	2 OF 2	

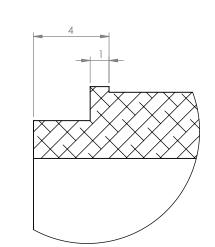




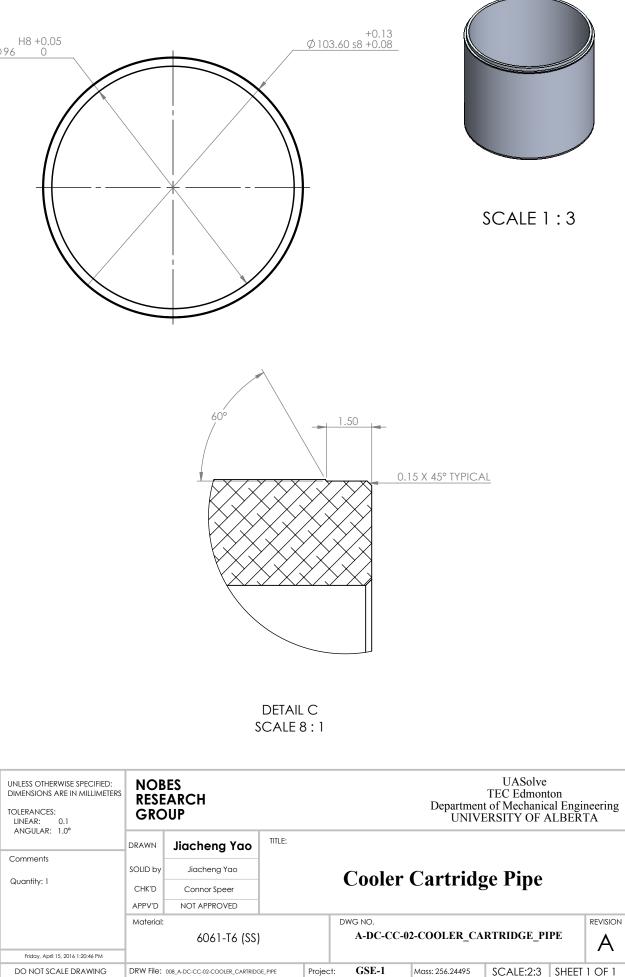
RTRIDGE	Project:	GSE-1	Mass: 700.91318	SCALE:2:3

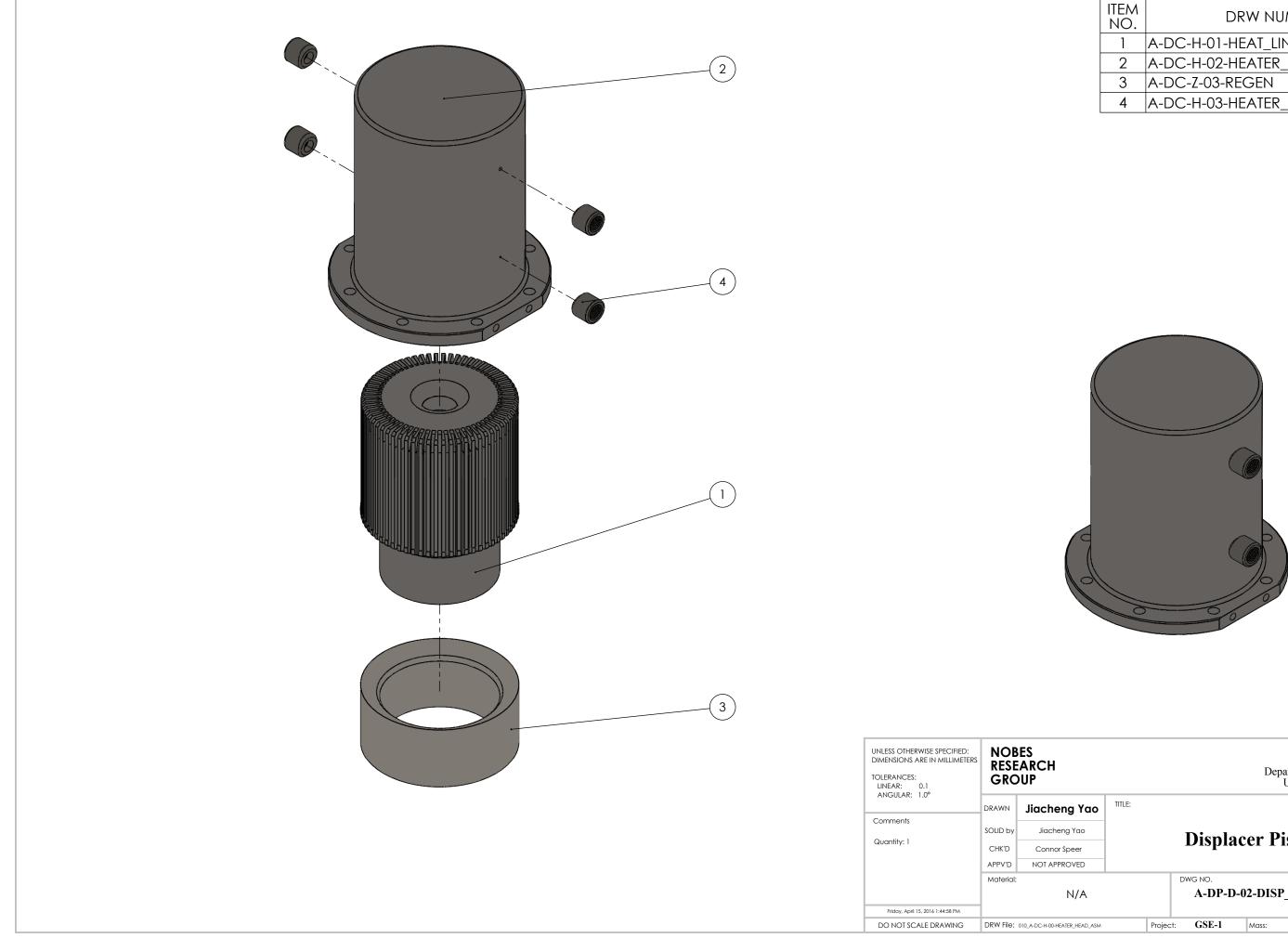






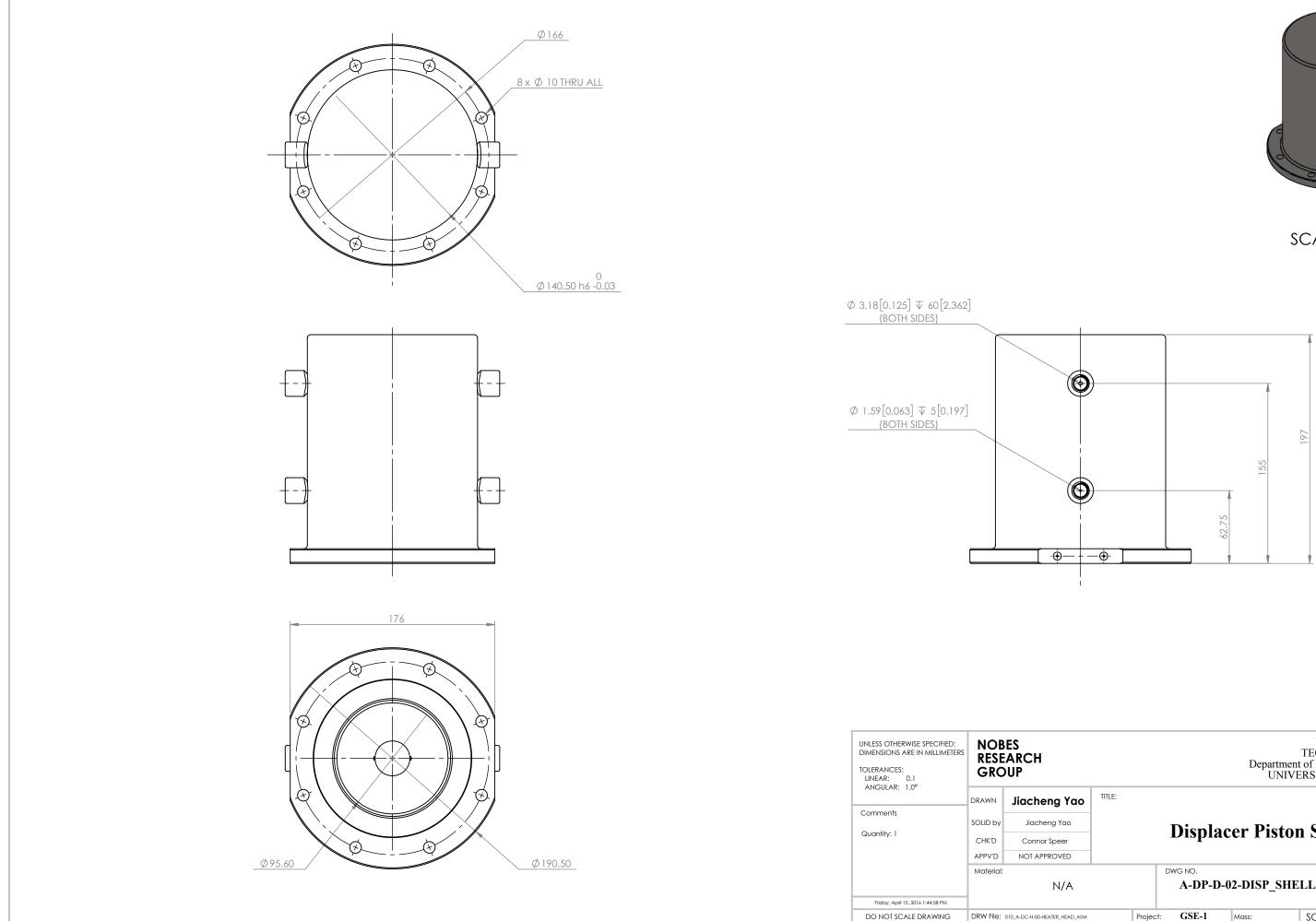
DETAIL D SCALE 5 : 1

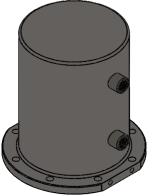




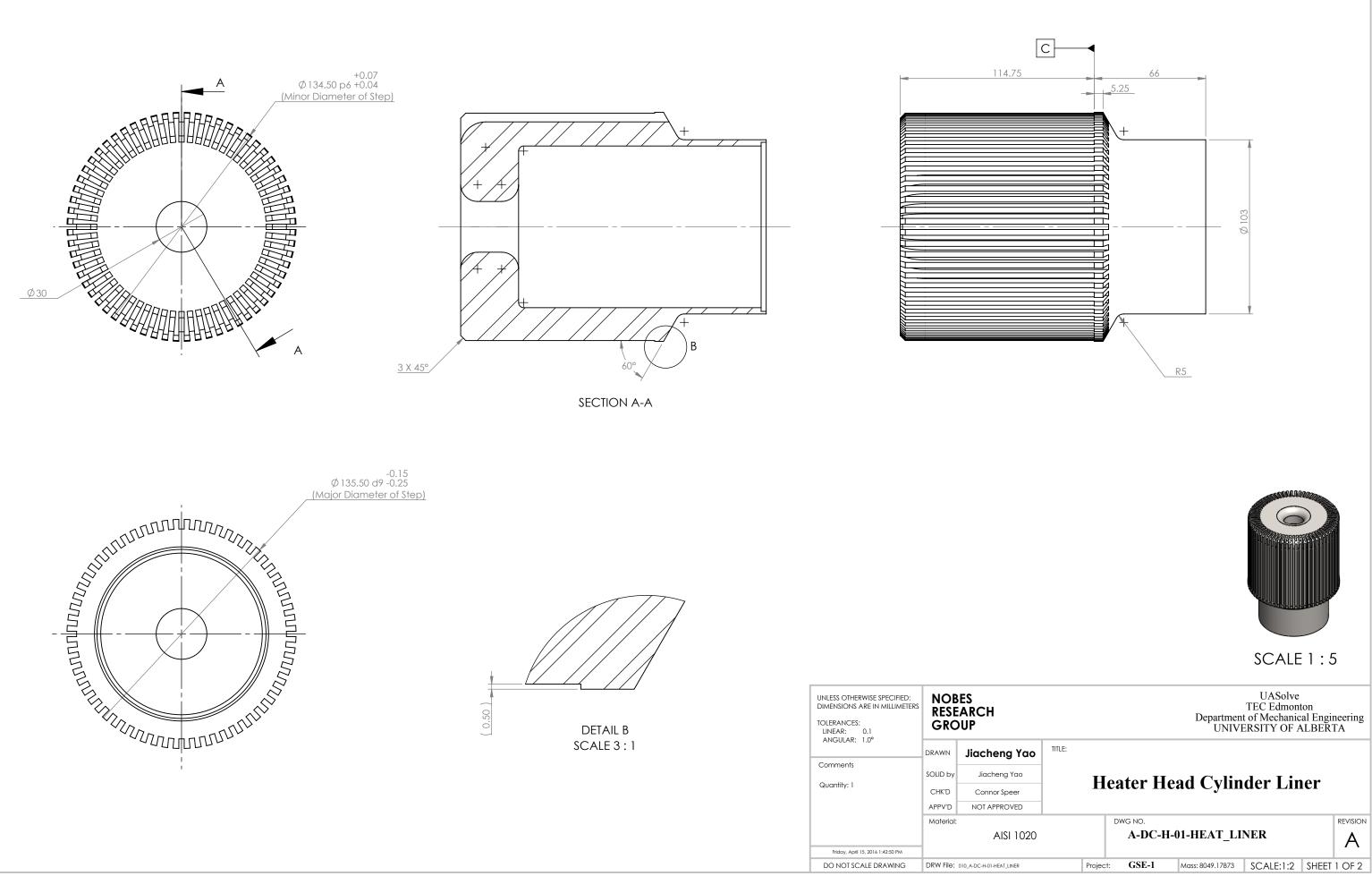
ITEM NO.	DRW NUMBER	QTY.
1	A-DC-H-01-HEAT_LINER	1
2	A-DC-H-02-HEATER_HEAD_SHELL	1
3	A-DC-Z-03-REGEN	1
4	A-DC-H-03-HEATER_HEAD_INLET	4

g Yao	TITLE:						
g Yao			Dicolo	cer Pisto	n Shall		
peer			Dispia		II SHEII		
OVED							
			DWG NO.				REVISION
N/A	A-DP-D-02-DISP_SHELL						A
ER_HEAD_ASM		Projec	t: GSE-1	Mass:	SCALE:1:3	SHEET	1 OF 2

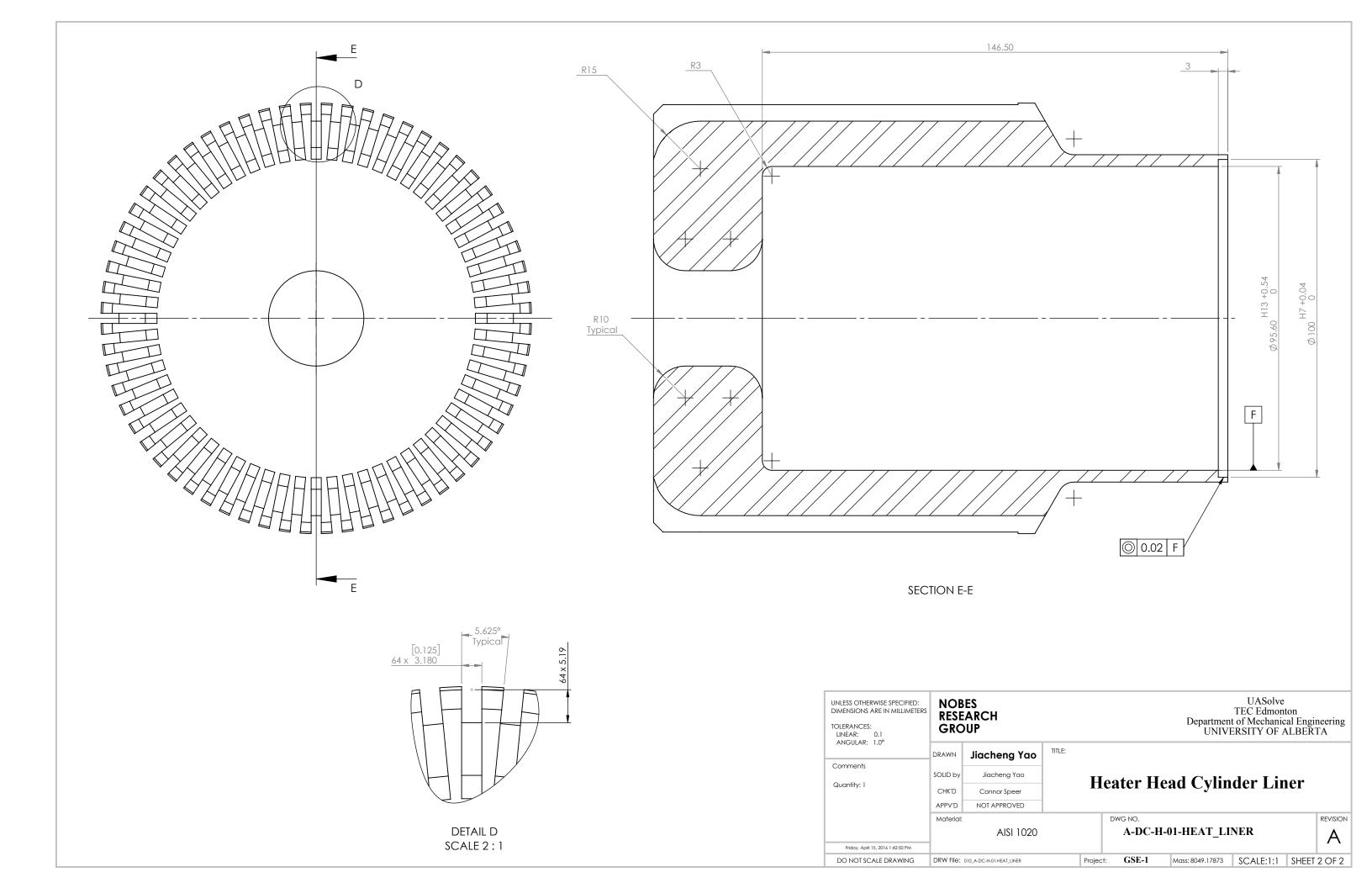


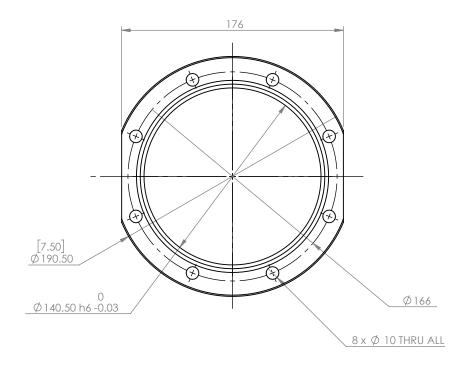


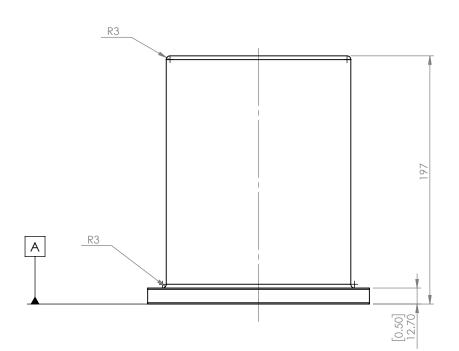
g Yao	TITLE:							
g Yao			Displ	acor	Dista	n Shall		
beer			Dishi	acer	1 15101	n Shell		
OVED								
			DWG NO.					REVISION
N/A A-I			A-DP-	-D-02-DI	SP_SHE	LL		Α
		Durte	t: GSE-1			CO 41 5-1-2	CUEFT	0.05.0
R_HEAD_ASM		Projec	T: GSE-I	Mass:		SCALE:1:3	SHEEL	2 OF 2

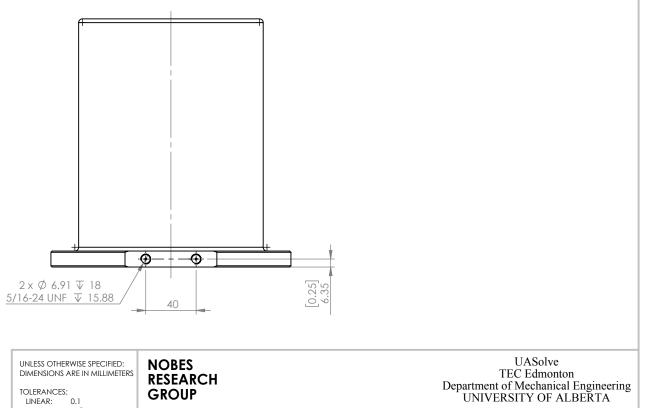


g Yao	TITLE:						
g Yao		Ц	ootor Ho	ad Cylin	dor I in	OF	
peer				ad Cylin		ICI	
OVED							
			DWG NO.				REVISION
SI 1020 A-DC-H-01-HEAT_LINER						А	
LINER	Project: GSE-1 Mass: 8049.17873 SCALE:1:2 SHEET 1 C				1 OF 2		

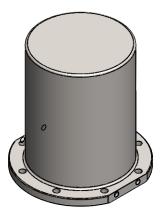




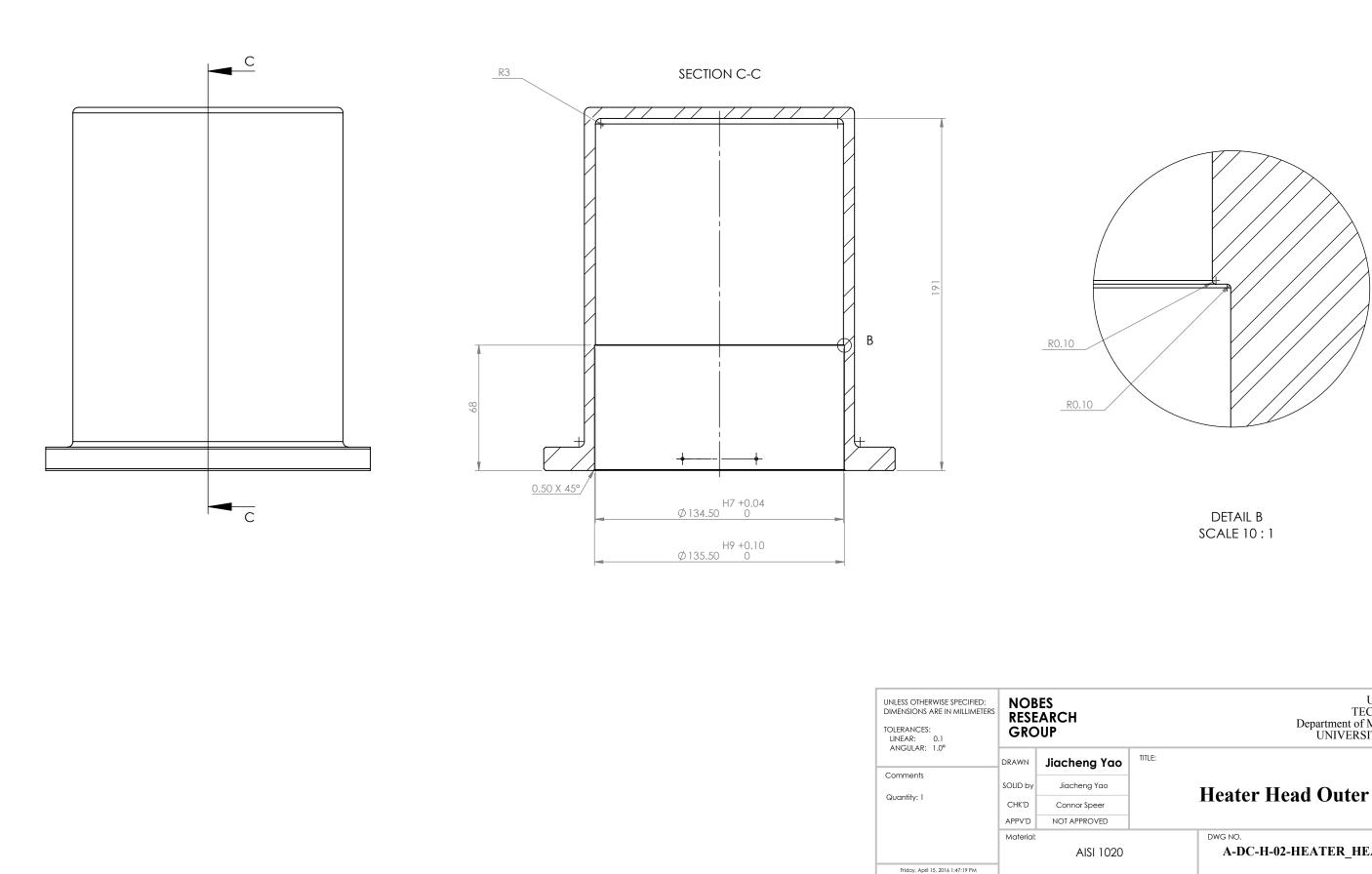




UNLESS OTHERWISE SPECIFIED: DIMENSIONS ARE IN MILLIMETERS TOLERANCES: LINEAR: 0.1	NOE RESE GRC	ARCH
ANGULAR: 1.0°	DRAWN	Jiacheng
Comments	SOLID by	Jiacheng '
Quantity: 1	CHK'D	Connor Spe
	APPV'D	NOT APPRO
	Material:	AISI
Friday, April 15, 2016 1:47:19 PM		
DO NOT SCALE DRAWING	DRW File:	010_A-DC-H-02-HEATER

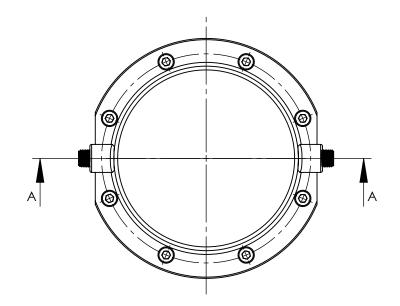


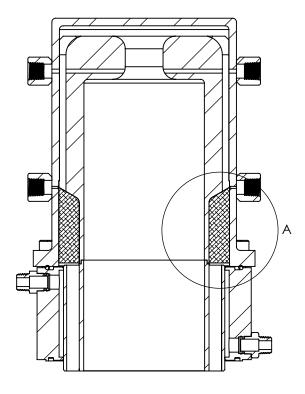
g Yao	TITLE:							
g Yao			Hoot	or H	lead Out	or Shal	1	
oeer			IIcai		icau Oui		1	
OVED								
			DWG NO.					REVISION
SI 1020	A-DC-H-02-HEATER_HEAD_SHELL A						А	
ER_HEAD_SHELL		Projec	t: GSE	2-1	Mass: 5695.49312	SCALE:1:3	SHEET	1 OF 2



do not scale drawing

DRAWN	Jiacheng Yao	TITLE:	
SOLID by	Jiacheng Yao	Heater Head Outer Shell	
CHK'D	Connor Speer	meater meau Outer Snen	
APPV'D	NOT APPROVED		
Material:	AISI 1020	DWG NO. A-DC-H-02-HEATER_HEAD_SHELL	REVISION
DRW File:	010_A-DC-H-02-HEATER_HEAD_SHELL	Project: GSE-1 Mass: 5695.49312 SCALE:1:2 SHEET	2 OF 2





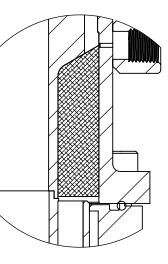
SECTION A-A

Stuff Regenerator space with 250 g of Knitted Stainless Steel Wire Mesh dia. 0.05 - 0.06 mm. This will yield a filling factor of 0.1.

Before stuffing, remove oil residues from the wire by heating it to 330 deg C. Then, blow off any particles using compressed air.

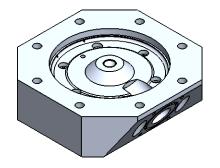
Take care to stuff the mesh equally into the regenerator space and to keep the Heater Head free from impurities and/or wire particles.

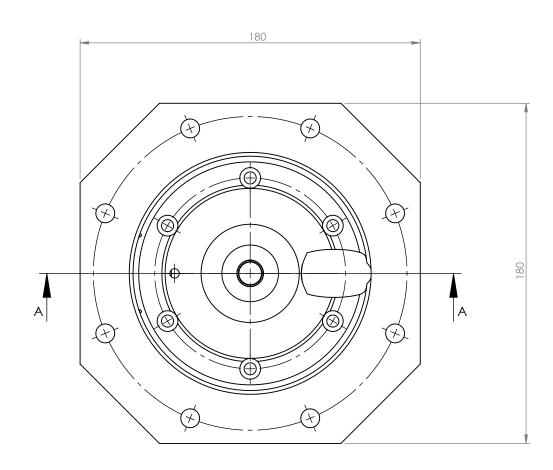
UNLESS OTHERWISE SPECIFIED: DIMENSIONS ARE IN MILLIMETERS TOLERANCES: LINEAR: 0.1 ANGULAR: 1.0°	NOE RESE GRC	ARCH
	DRAWN	Jiacheng
Comments	SOLID by	Jiacheng
Quantity: 1	CHK'D	Connor Sp
	APPV'D	NOT APPRO
	Material	
		SS Wir
Friday, April 15, 2016 1:48:32 PM		
DO NOT SCALE DRAWING	DRW File:	012_A-DC-Z-03-REGEN

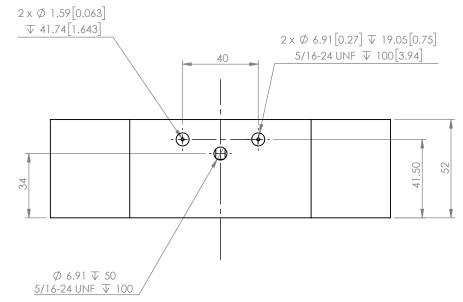


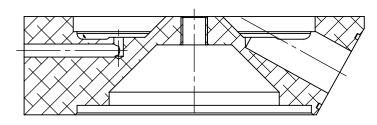
DETAIL A SCALE 2 : 3

UASolve TEC Edmonton Department of Mechanical Engin UNIVERSITY OF ALBERT							neering ΓΑ	
g Yao	TITLE:							
g Yao				D	aganarat			
beer				N	egenerate	JI		
OVED								
				G NO.				REVISION
ire Mesh				A-DC-Z-	00-DISP_CYI	L_ASM		А
4	Project: GSE-1 Mass: SCALE:1:3 SHEET					1 OF 1		

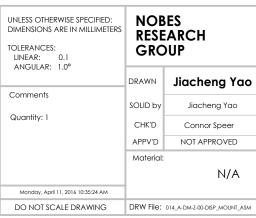




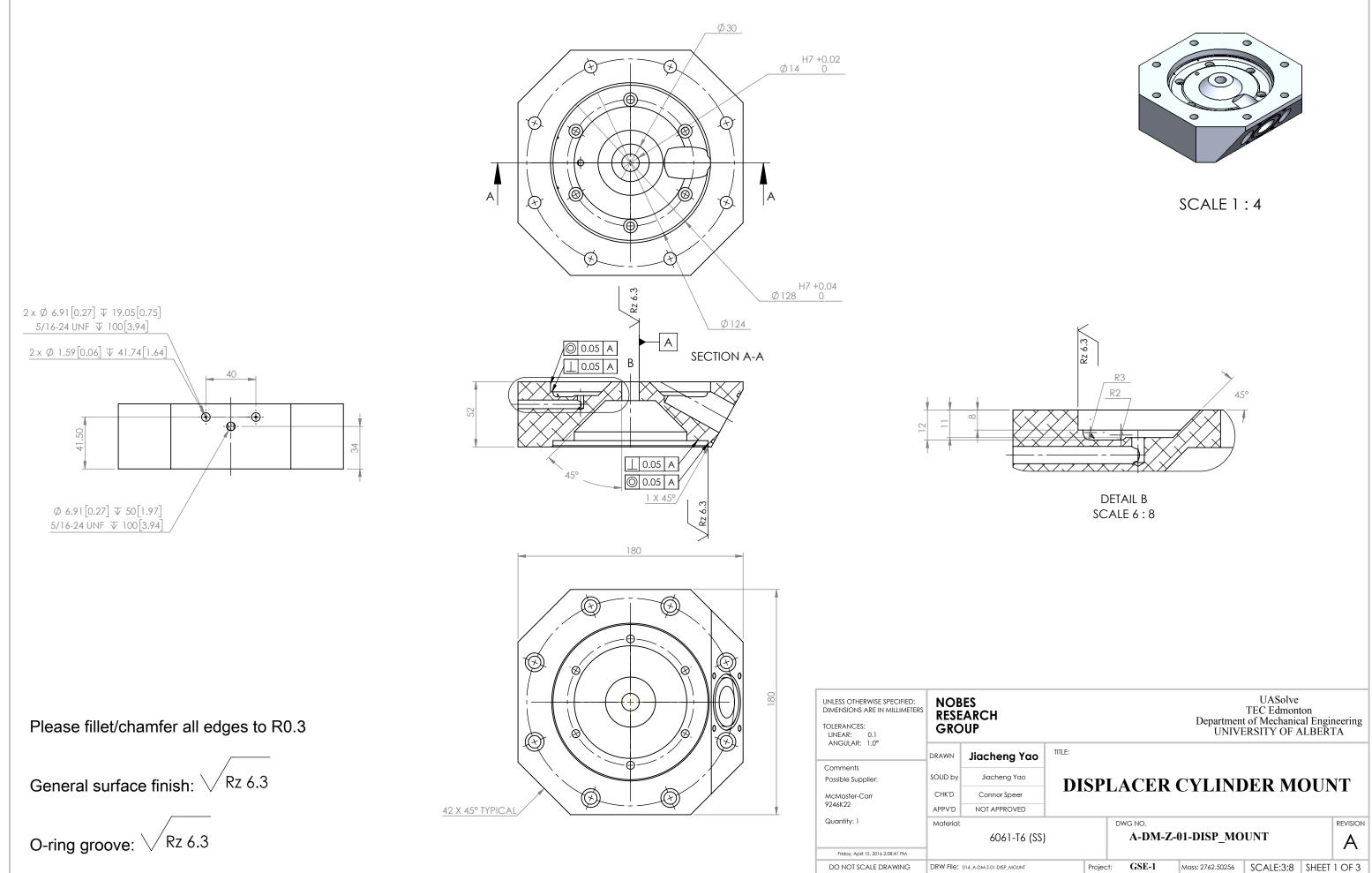


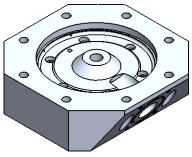


SECTION A-A

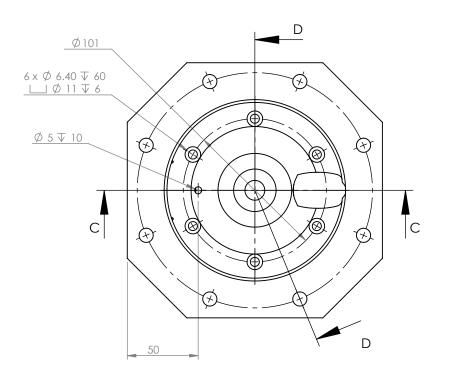


_								
	ITEM I	۷O.		PART	NUMBER		Q	TY.
	1		A-D	M-Z-01-DIS	SP_MOUN	IT		1
	2		A-D	M-Z-02-SH	AFT_BEAR	RING		1
						UASolve		
RCH P	1				Departme UNI	TEC Edmon ent of Mechanic VERSITY OF	ton cal Engin ALBER	neering ΓA
liach	ieng Yao	TITLE:						
Jiac	heng Yao		Г	Jisnlaaar	Mount	Assamb	1.7	
	nor Speer		L	Displacer	IVIUUII	A99CIIID	'I Y	
NOT A	PPROVED			DWG NO.				REVISION
	N/A				00-DISP_M	OUNT_ASM	[A
A-DM-Z-00	D-DISP_MOUNT_ASM		Projec	t: GSE-1	Mass:	SCALE:1:2	SHEET	1 OF 1

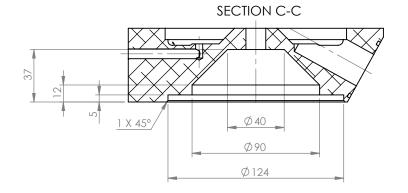


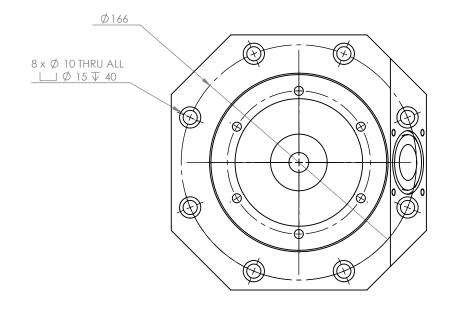


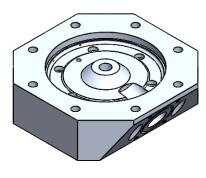
g Yao	TITLE:		
g Yao	DISDI ACI	ER CYLINDER MOUN	JT
beer	DISI LACI	ER CILINDER MOUP	11
OVED			
	DWG NO.		REVISION
I-T6 (SS)	A-D	M-Z-01-DISP_MOUNT	А











UNLESS OTHERWISE SPECIFIED: DIMENSIONS ARE IN MILLIMETERS TOLERANCES: LINEAR: 0.1 ANGULAR: 1.0°	NOBES RESEARCH GROUP		
ANOULAR. 1.0	DRAWN	Jiacheng	
Comments Possible Supplier:	SOLID by	Jiacheng '	
McMaster-Carr	CHK'D	Connor Spe	
9246K22	APPV'D	NOT APPRO	
Quantity: 1	Material:		
		6061-	
Friday, April 15, 2016 2:08:41 PM	1		
DO NOT SCALE DRAWING	DRW File:	014_A-DM-Z-01-DISP_M	

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SECTION D-D

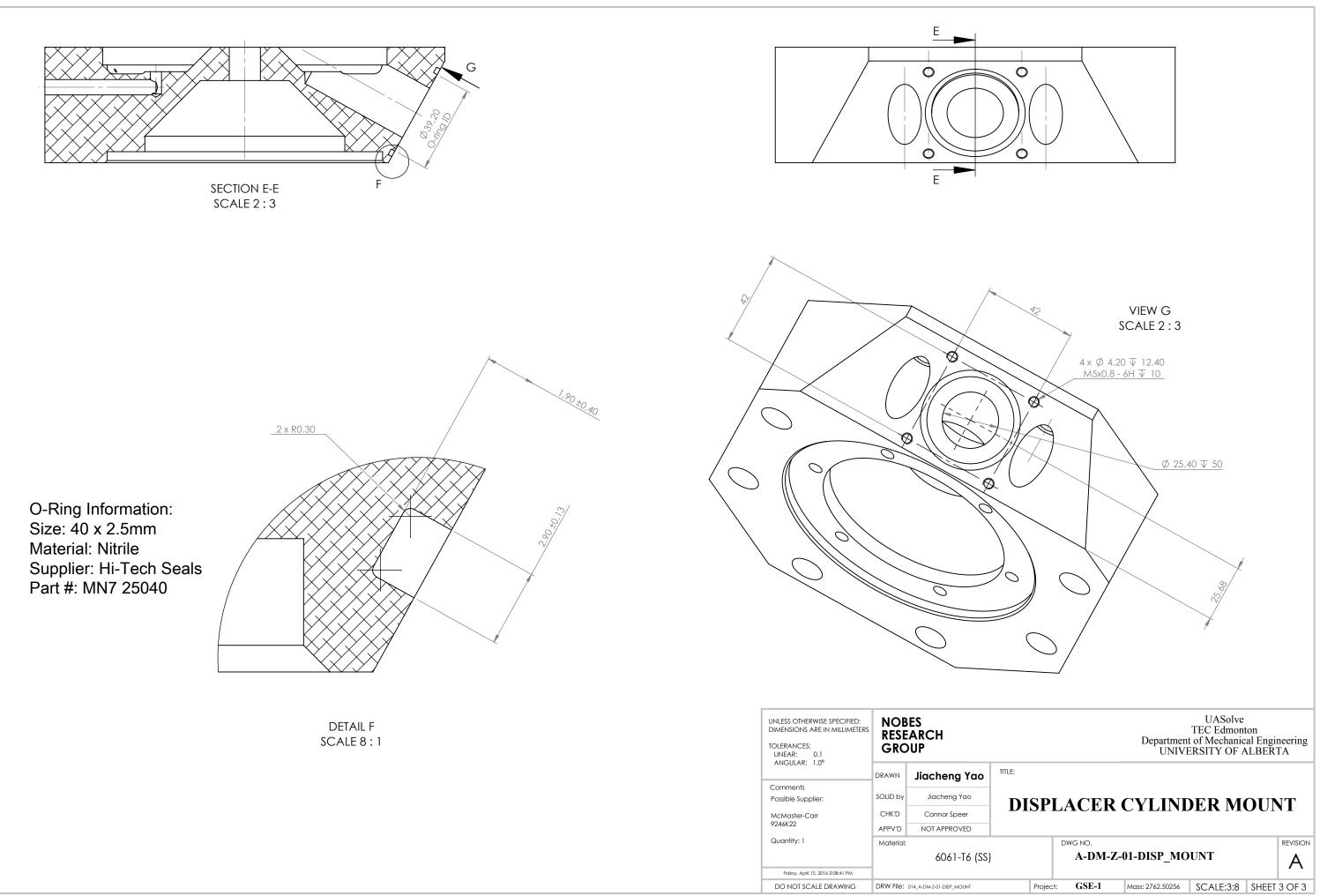
UASolve TEC Edmonton Department of Mechanical Engineering UNIVERSITY OF ALBERTA

g Yao	TITLE:		
g Yao	ыср	LACER CYLINDER MOUN	JT
beer	DISL	LACER CILINDER MOUN	۱۱
OVED			
		DWG NO.	REVISION
I-T6 (SS)		A-DM-Z-01-DISP_MOUNT	Α

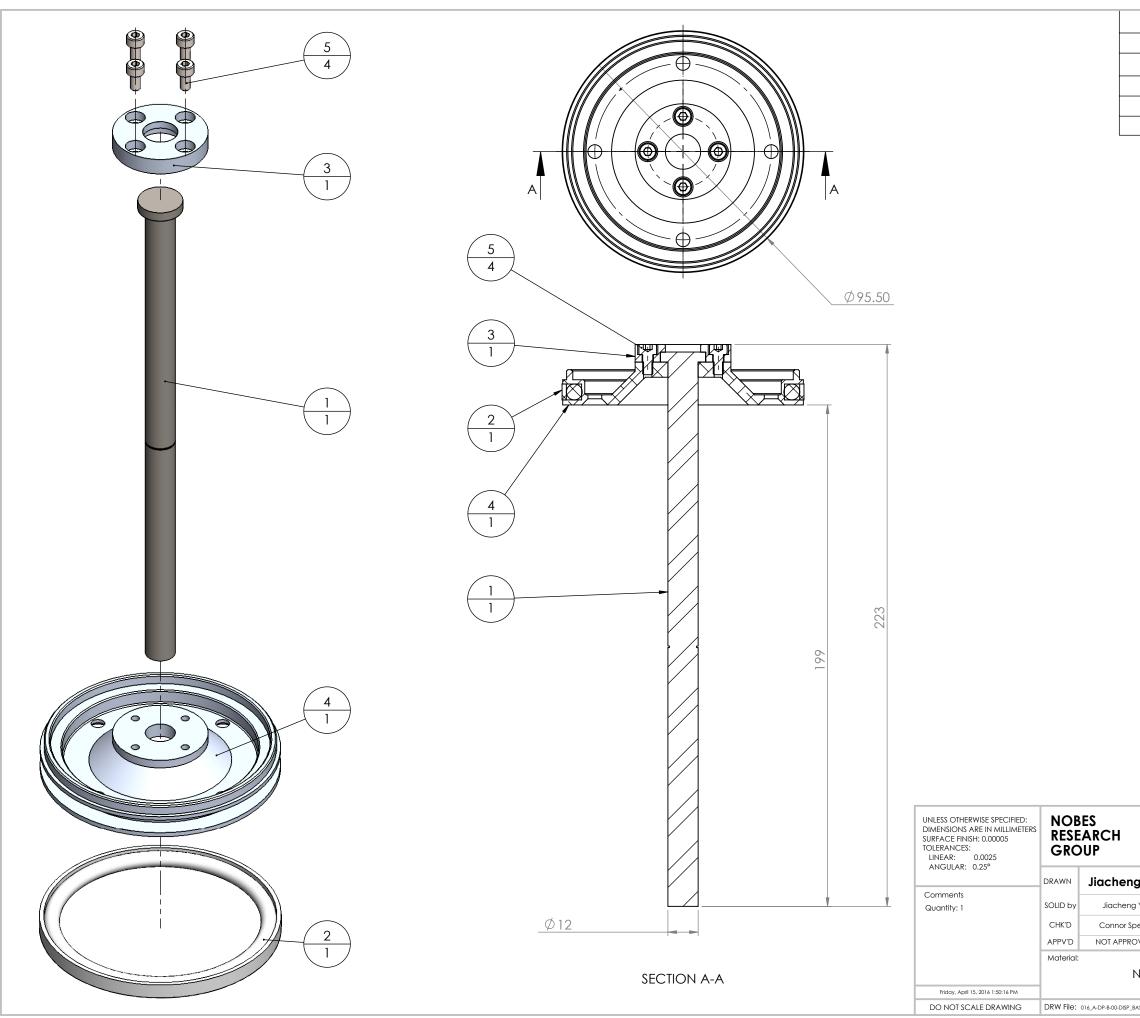
MOUNT

Project: GSE-1

Mass: 2762.50256 SCALE:3:8 SHEET 2 OF 3



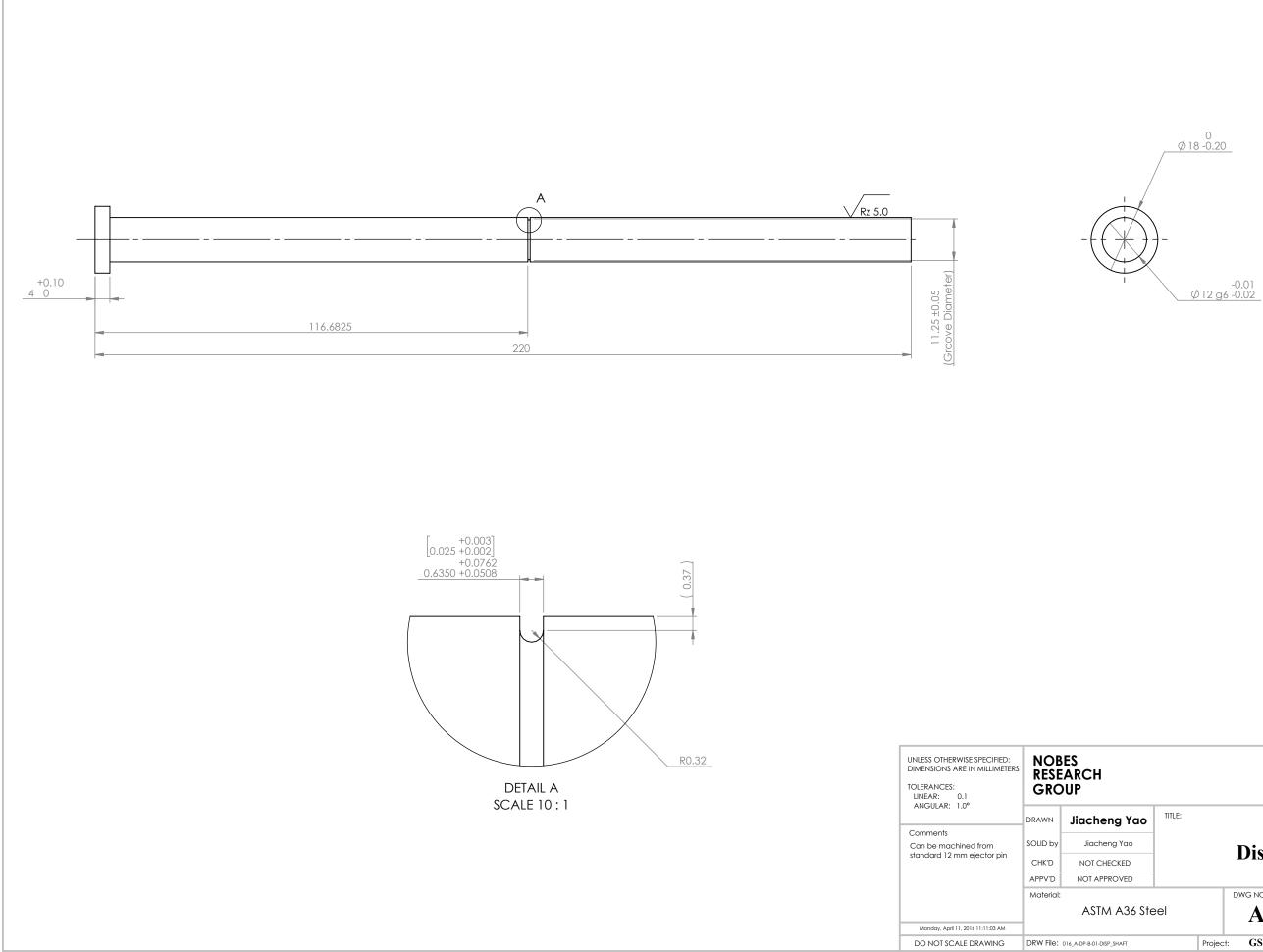
DO NOT SCALE DRAWING	DRW File: 014_A-DM-Z-01-DISP_



ITEM NO.	DRW NUMBER	QTY.
1	A-DP-B-01-DISP_SHAFT	1
2	A-DP-B-04-DISP_RING	1
3	A-DP-B-03-DISP_CLAMP_RING	1
4	A-DP-B-02-DISP_BASE	1
5	B18.3.1M - 4 x 0.7 x 8 Hex SHCS 8NHX	4



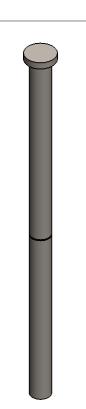
g Yao	TITLE:						
g Yao			Disnlad	er Pistor	n Base		
peer	Displacer Piston Base						
OVED							
N/A			dwg no. A-DP-B	-00-DISP_H	BASE_AS	Μ	REVISION A
BASE_ASM Proj			t: ST05G	Mass:	SCALE:2:3	SHEET	1 OF 1

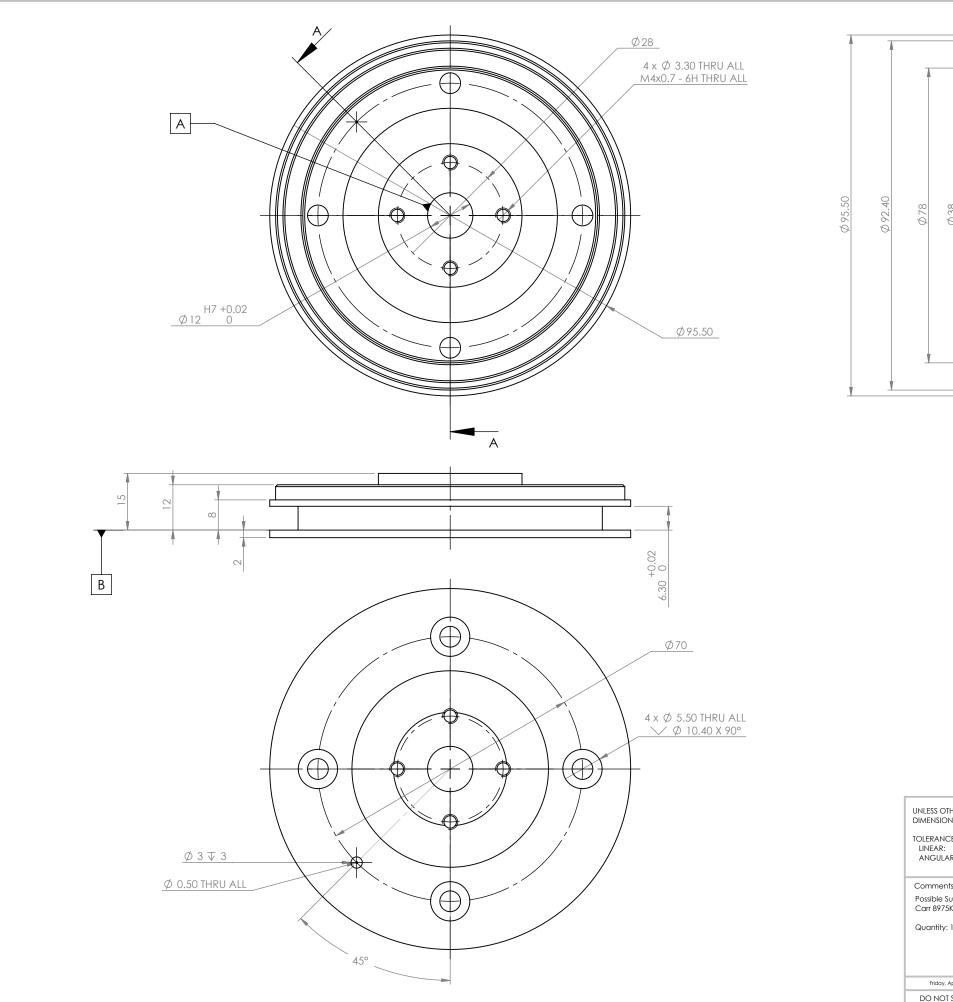


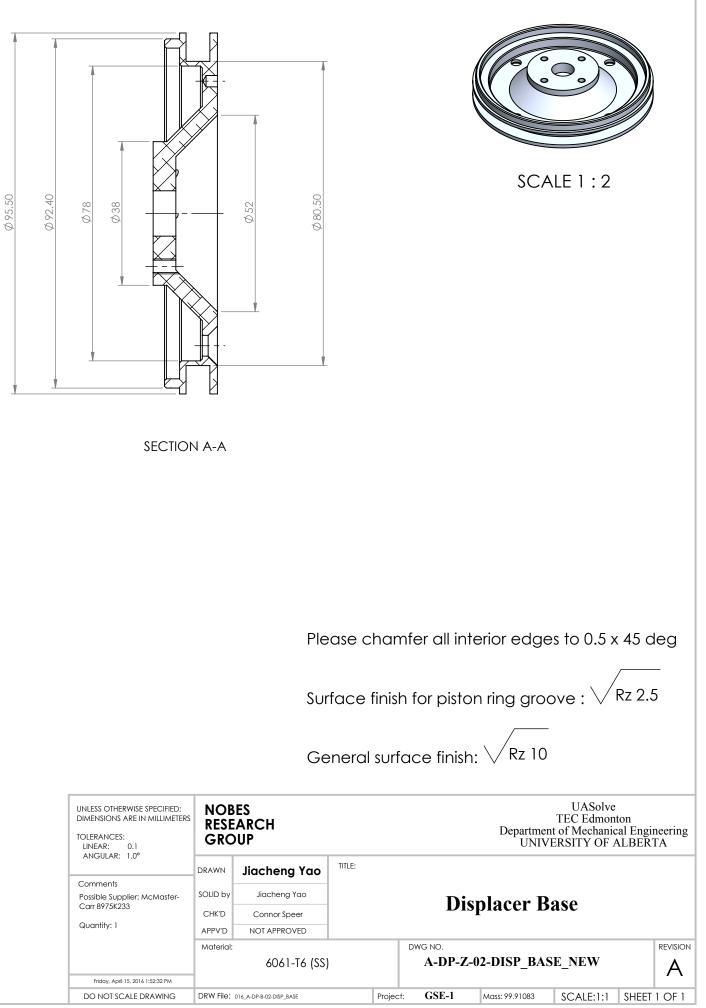
Displacar Distan Shaft						
Displacer Fiston Shalt						
	D'	WG NO.			REVISION	
el		A-D	P-B-01-I	DISP_S	SHAFA	
shaft Project		GSE-1	Mass: 199.64721	SCALE:1:1	SHEET 1 OF 1	
	el	D	el dwg no. A-D	el dwg No. A-DP-B-01-I	A-DP-B-01-DISP_S	

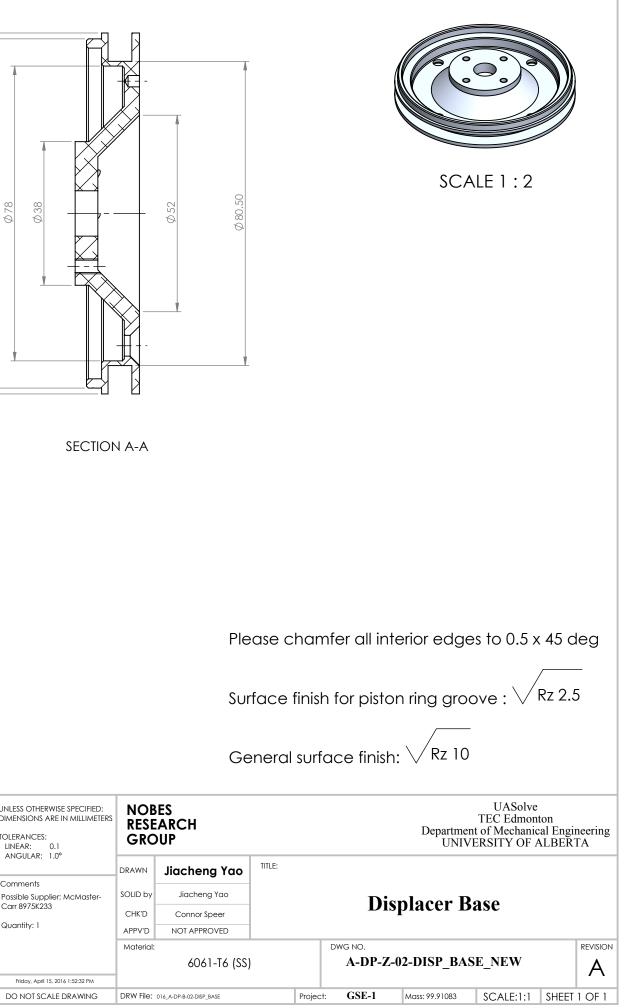


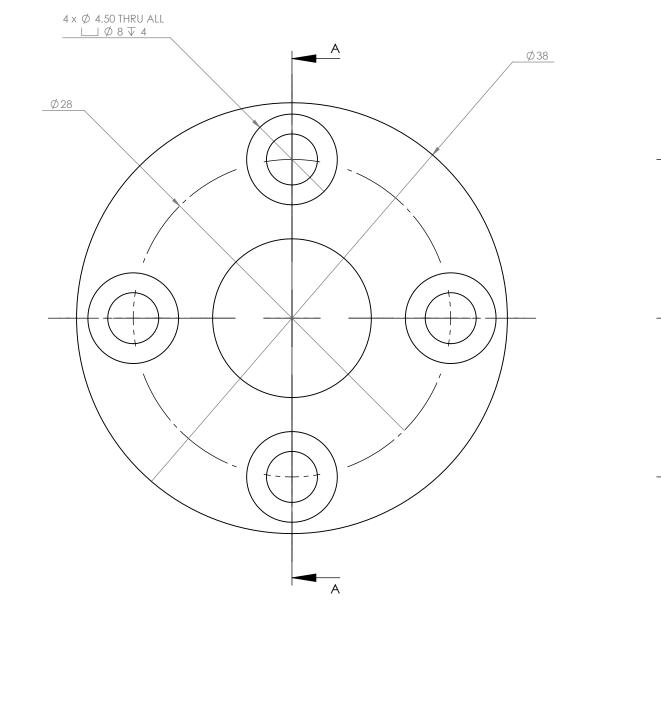


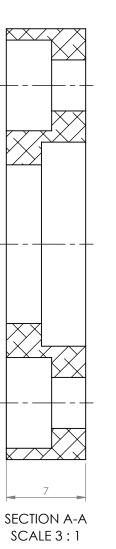










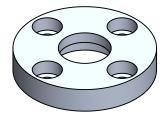


Ø 14 THRU ALL Ø 18 ₹ 3.90

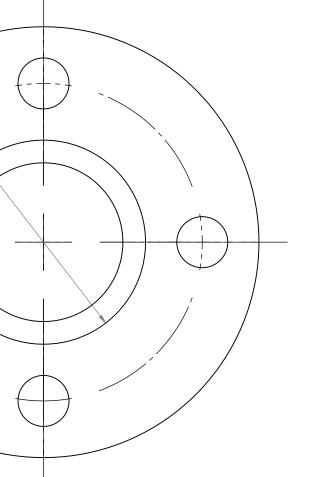
> NOBES RESEARCH GROUP UNLESS OTHERWISE SPECIFIED: DIMENSIONS ARE IN MILLIMETERS TOLERANCES: LINEAR: 0.1 ANGULAR: 1.0° DRAWN Jiacheng Comments Possible Supplier: McMaster-Carr 8975K74 SOLID by Jiacheng CHK'D Connor Sp APPV'D NOT APPRO Quantity: 1 Material: 606 Monday, April 11, 2016 12:12:34 PM DO NOT SCALE DRAWING DRW File: 016_A-DP-B-03-DISP_CLAMP_RING

Please fillet/chamfer all edges to R0.3

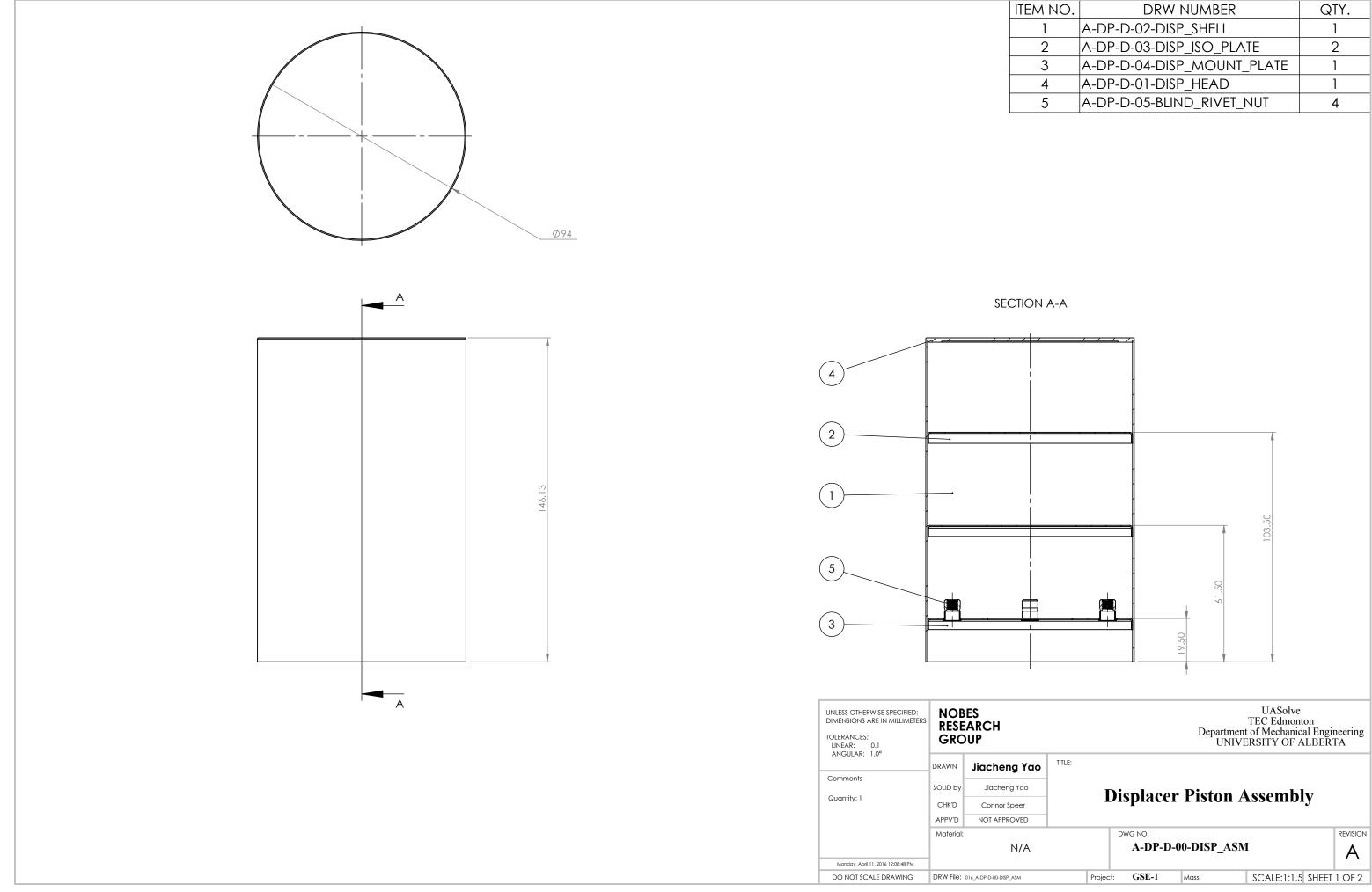
General surface finish \sqrt{Rz} 6.3





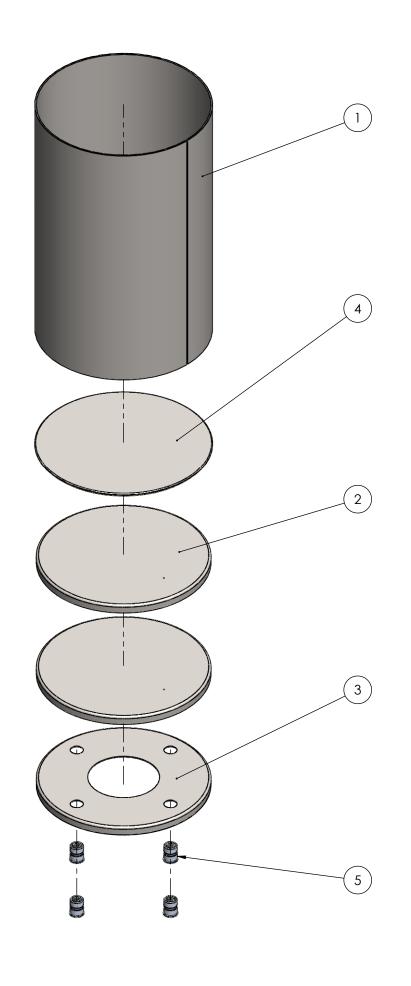


g Yao	TITLE:	TTLE: Clamp Ring					
g Yao							
beer							
OVED							
			DWG NO.				REVISION
I-T6 (SS)			A-DP-B-	03-DISP_CLA	MP_RING		А
			t: GSE-1	Mass: 14.77998	SCALE:1:10	SHEET	1 OF 1



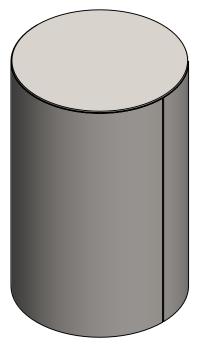
ITEM NO.	DRW NUMBER	QTY.
1	A-DP-D-02-DISP_SHELL	1
2	A-DP-D-03-DISP_ISO_PLATE	2
3	A-DP-D-04-DISP_MOUNT_PLATE	1
4	A-DP-D-01-DISP_HEAD	1
5	A-DP-D-05-BLIND_RIVET_NUT	4

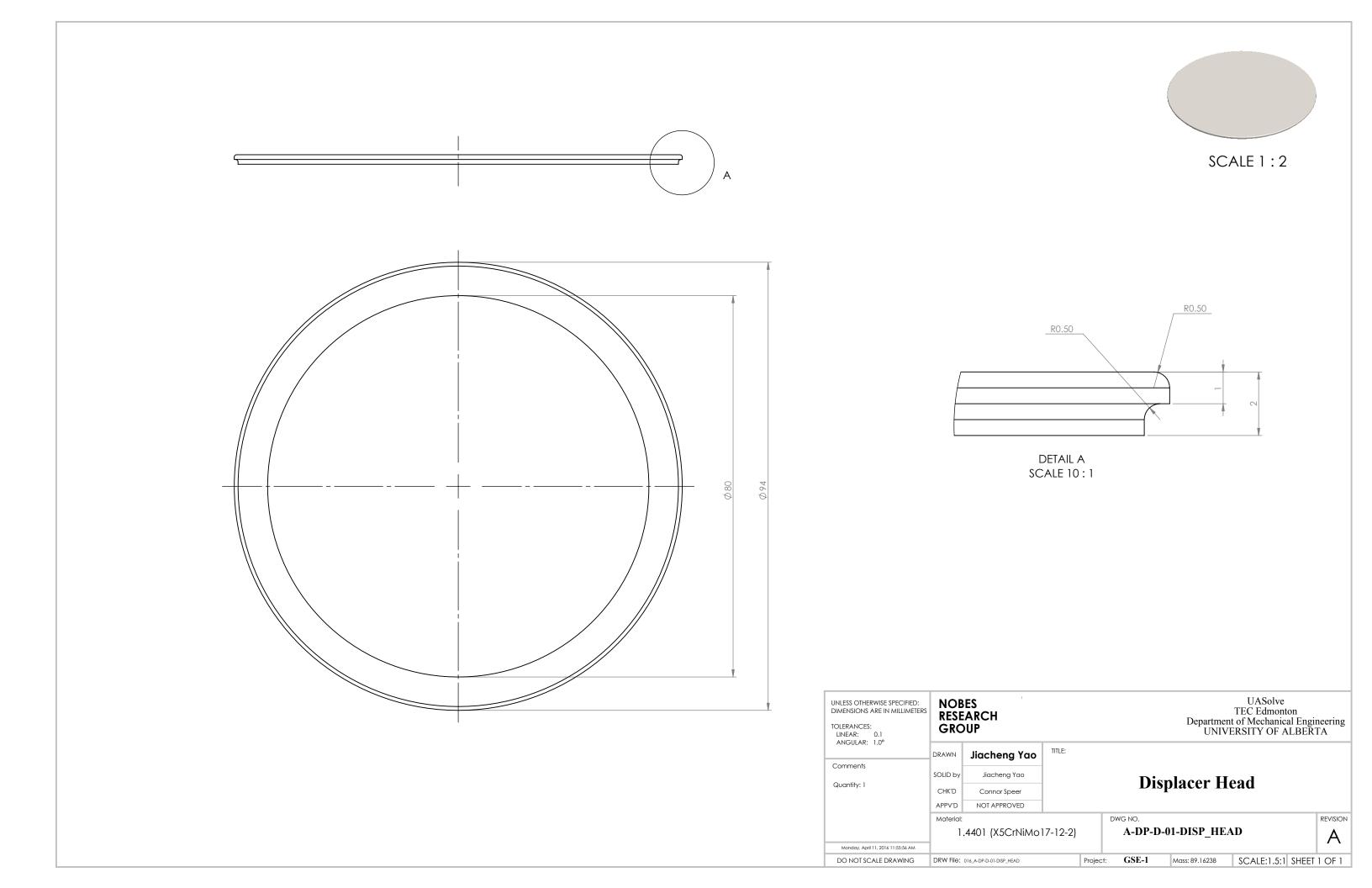
g Yao	TITLE:					
g Yao	Displacer Piston Assembly					
beer		I	Jispiace		Assembly	
DVED						
N/A				-00-DISP_ASM	М	REVISION
ASM		Projec	t: GSE-1	Mass:	SCALE:1:1.5 SHEE	T 1 OF 2

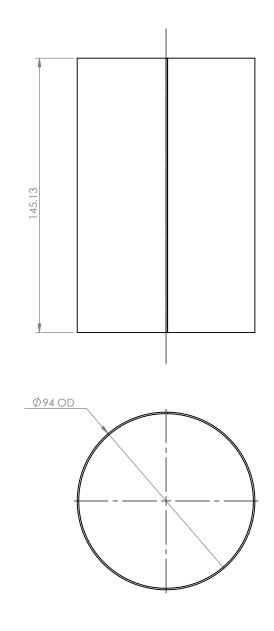


UNLESS OTHERWISE SPECIFIED: DIMENSIONS ARE IN MILLIMETERS TOLERANCES: LINEAR: 0.1 ANGULAR: 1.0°	NOBES RESEARCH GROUP				UASolve TEC Edmonton Department of Mechanical Engineering UNIVERSITY OF ALBERTA				
ANGULAR. T.U	DRAWN	Jiacheng Yao	TITLE:						
Comments	SOLID by	Jiacheng Yao	Displacer Piston Assembly						
Quantity: 1	CHK'D	Connor Speer							
	APPV'D	NOT APPROVED							
	Material:				DWG NO.				REVISION
	N/A				A-DP-D-00-DISP_ASM				A
Monday, April 11, 2016 12:08:48 PM								_	<i>,</i> ,
DO NOT SCALE DRAWING	DRW File:	016_A-DP-D-00-DISP_ASM		Project	GSE-1	Mass:	SCALE:1:2	SHEET	2 OF 2

ITEM NO.	DRW NUMBER	QTY.
1	A-DP-D-02-DISP_SHELL	1
2	A-DP-D-03-DISP_ISO_PLATE	2
3	A-DP-D-04-DISP_MOUNT_PLATE	1
4	A-DP-D-01-DISP_HEAD	1
5	A-DP-D-05-BLIND_RIVET_NUT	4







As Bent

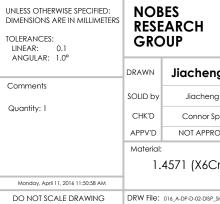
UP 359° R 46.2 Depends on Joining Process

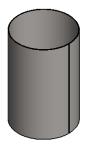
Flat Pattern

Sheet metal thickness: 0.8 mm Bend sheet metal and TIG-weld joints.

Alternatively, scarf joint 3 mm from both ends and spot weld without gaps.

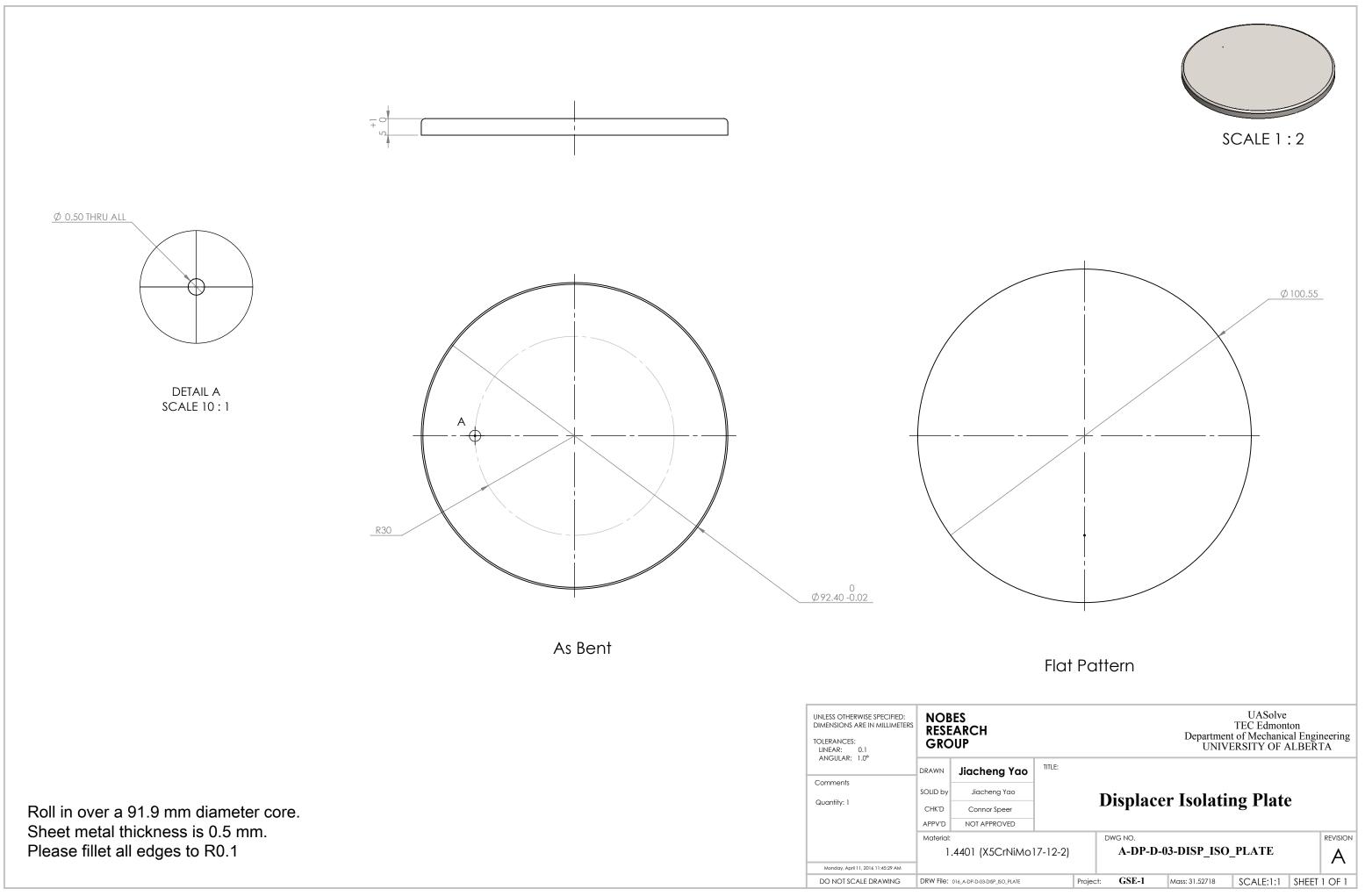
Please fillet all edges to R0.1

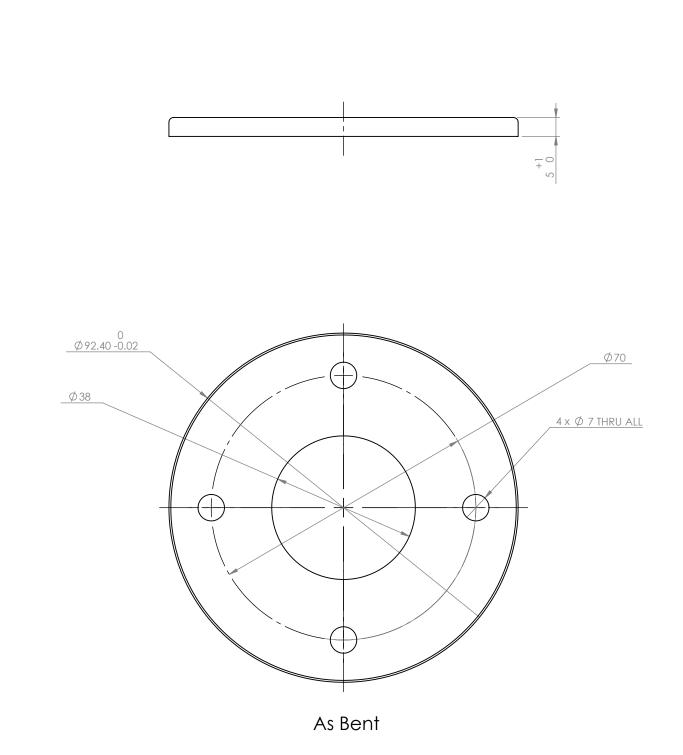


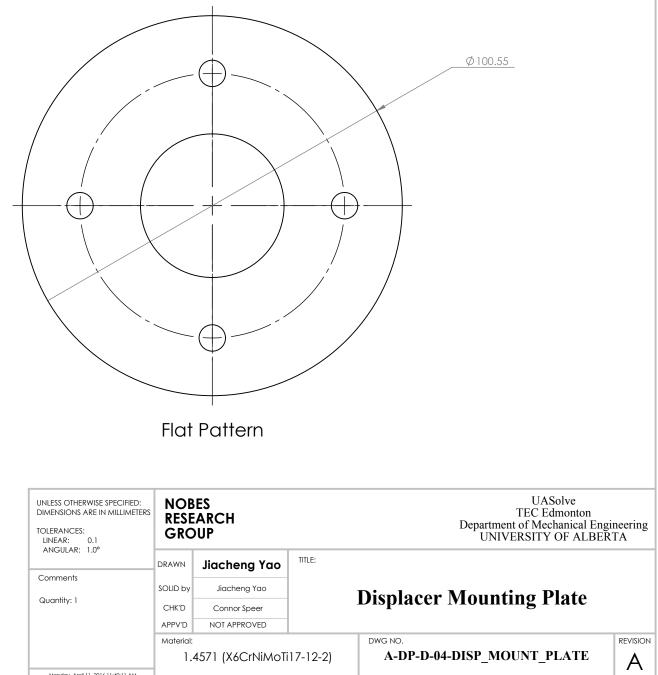


SCALE 1:5

g Yao	TITLE:								
g Yao	Displacer Piston Shell								
beer									
DVED									
rNiMoTi17-12-2)				DWG NO. A-DP-D-02-DISP_SHELL					
SHELL	Project:		t: GS	GSE-1 Mass: 271.20326 SCALE:1:2 SHE		SHEET	1 OF 1		

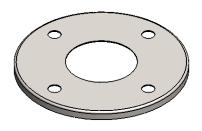






Monday, April 11, 2016 11:40:11 AM DO NOT SCALE DRAWING DRW File: 016_A-DP-D-04-DISP_

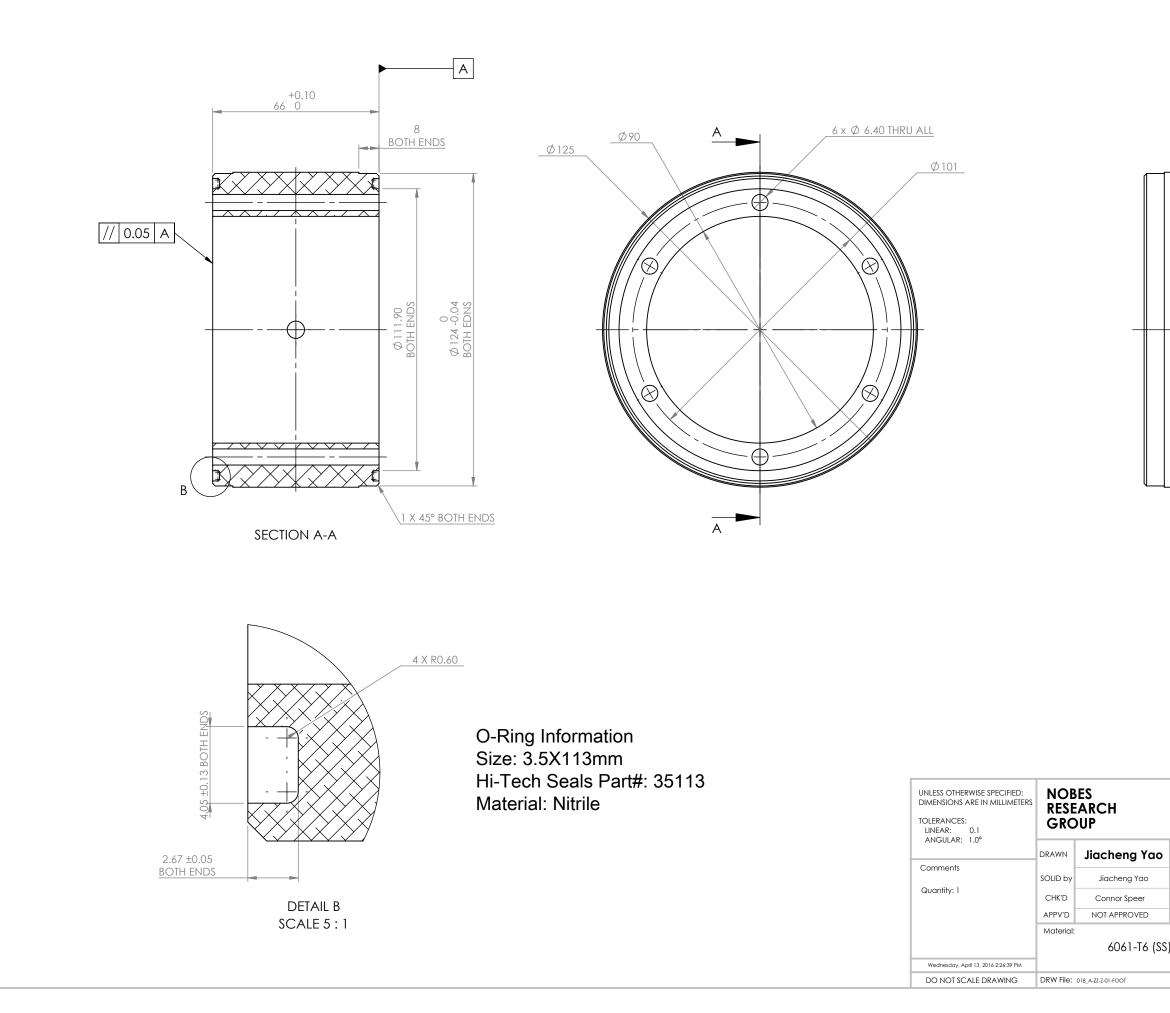
Sheet metal thickness: 0.8 mm Roll in over a 90.8 mm diameter core. Please fillet all edges to R0.1

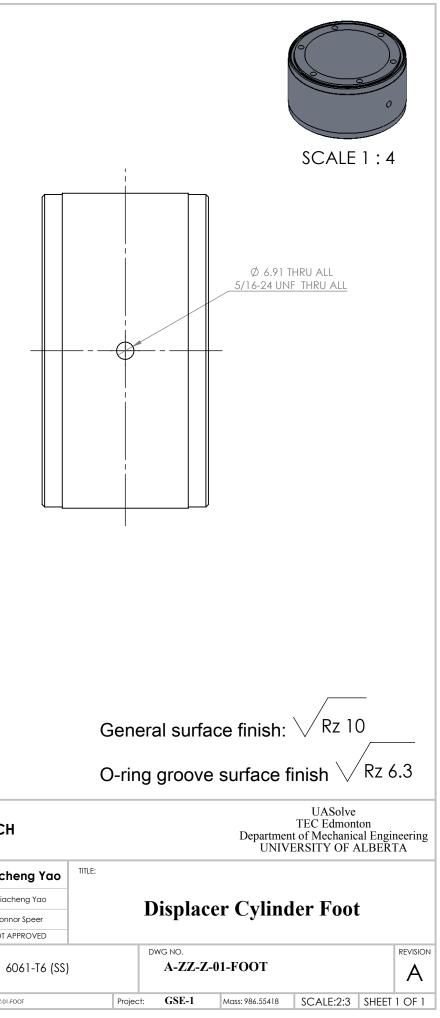


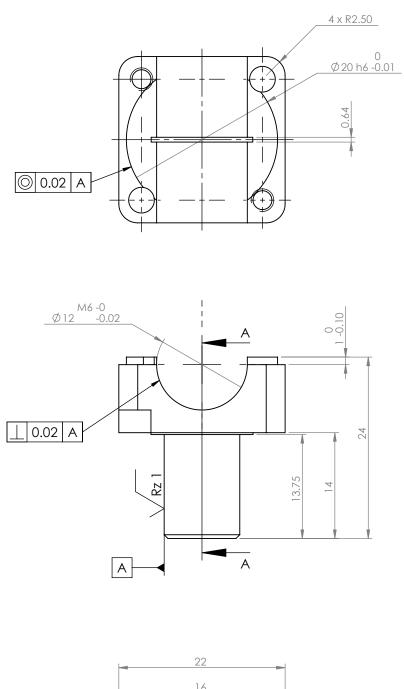
SCALE 1:2

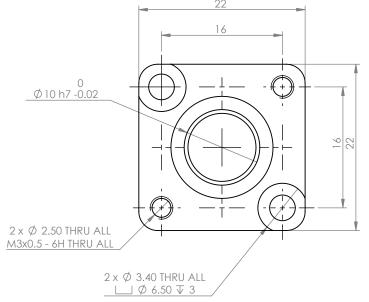
			-	-	
_MOUNT_PLATE	Project:	GSE-1	Mass: 26.37576	SCALE:1:1	SHEET 1 OF 1

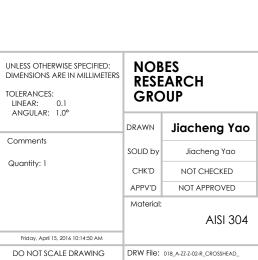
A Other Parts





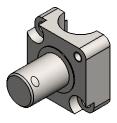




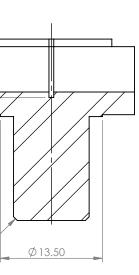


0.72

<u>0.50 X 45°</u>

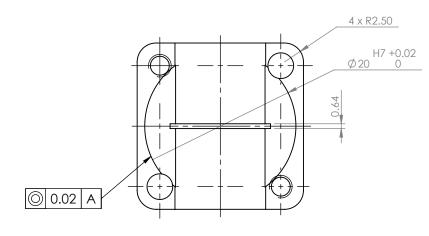


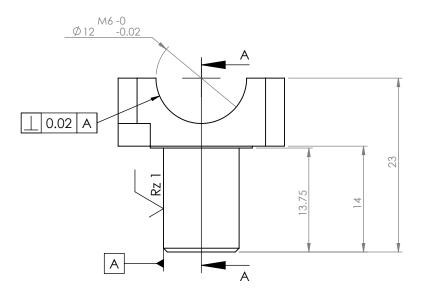
SCALE 1:1

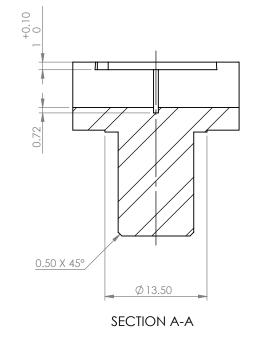


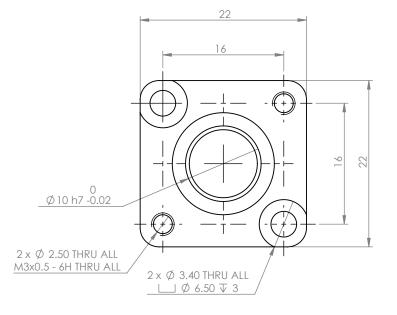
SECTION A-A

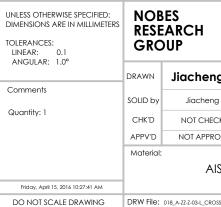
Please fillet/chamfer all edges to R0.1 General surface finish: Rz 10 UASolve TEC Edmonton Department of Mechanical Engineering UNIVERSITY OF ALBERTA Yao TITLE: Crosshead Right DWG NO. A-ZZ-Z-02-R_CROSSHEAD A Project: GSE-1 Mass: 30.91090 SCALE:2:1 SHEET 1 OF 1

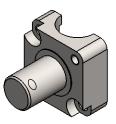










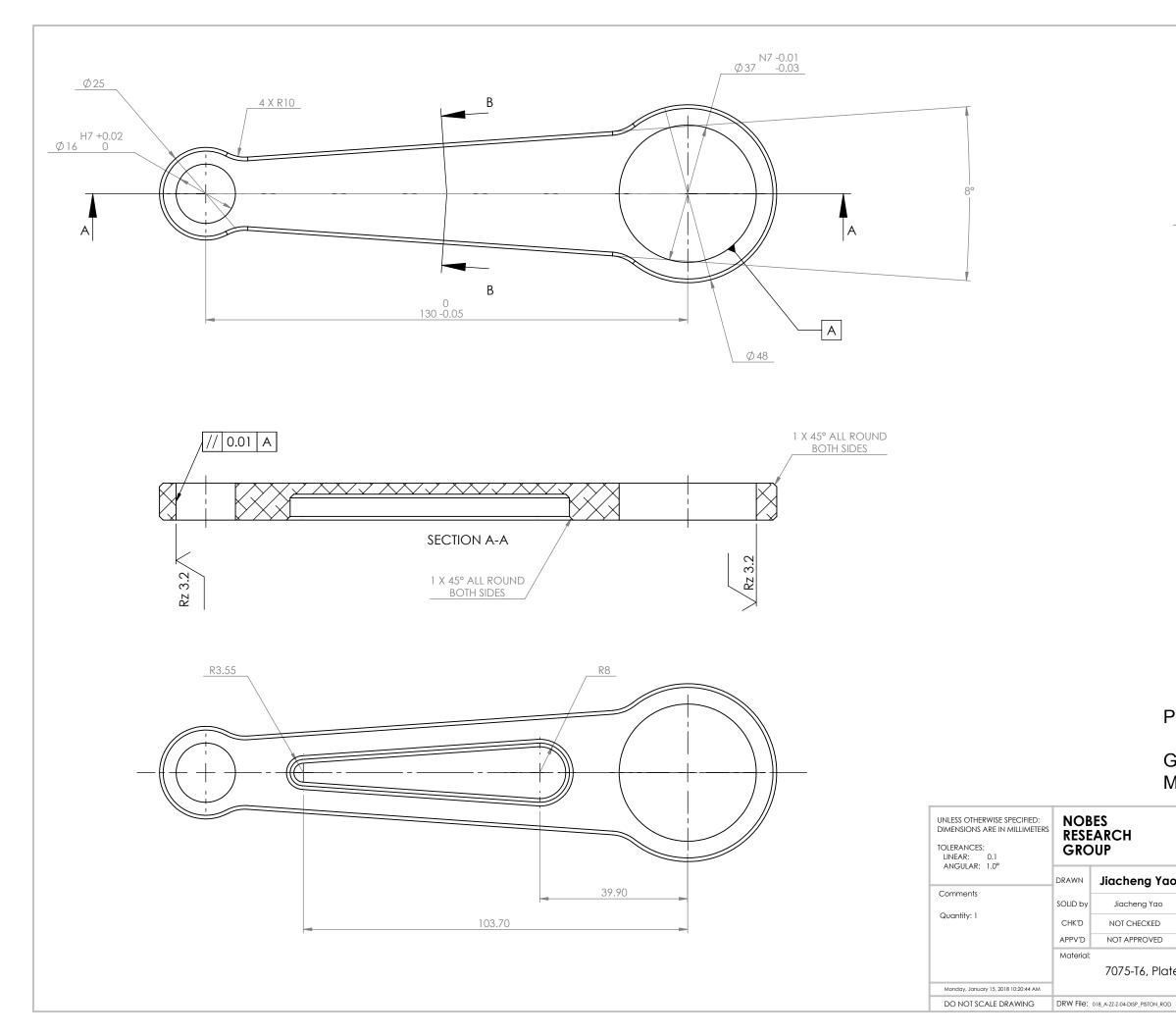


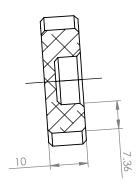
SCALE 1:1

Please fillet/chamfer All Edges R0.1mm

General surface finish: \bigvee Rz 10

g Yao	TITLE:						
y Yao			Cr	osshead I	oft		
CKED			CI	USSIICAU I			
DVED							
			DWG NO.				REVISION
SI 304			A-ZZ-Z	-03-L_CROSS	HEAD		Α
SSHEAD	F	Project	: GSE-1	Mass: 29.50406	SCALE:2:1	SHEET	1 OF 1





SCALE 1:3

SECTION B-B

Please fillet/chamfer all edges to R1

General surface finish: \sqrt{Rz} 10 Maximum deviation between pair is 0.01 mm.

UASolve TEC Edmonton Department of Mechanical Engineering UNIVERSITY OF ALBERTA

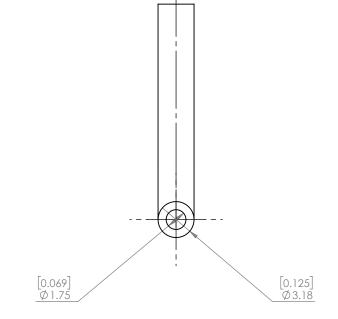
SCALE:1:1 SHEET 1 OF 1

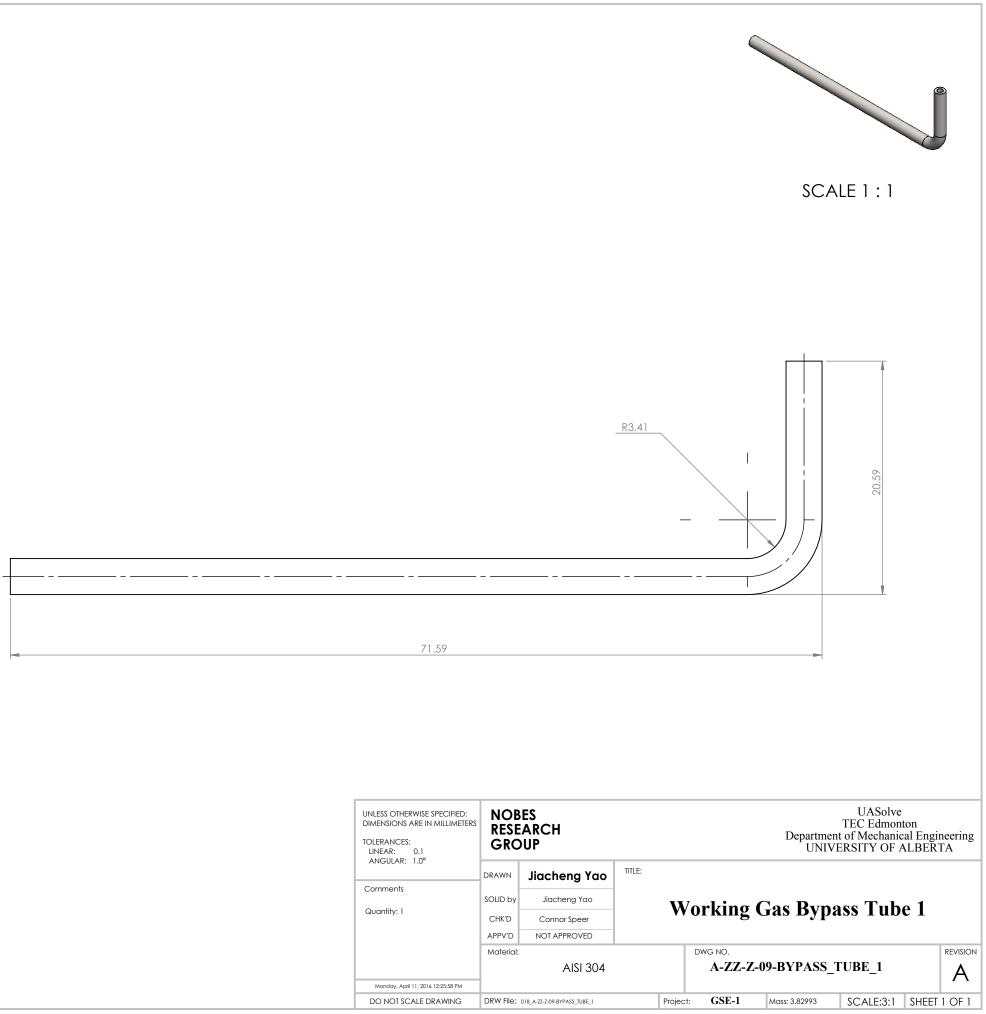
g Yao	TITLE:		
g Yao		DISPLACER PISTON	
CKED		CONNECTING ROD	
OVED			
		DWG NO.	REVISION
5, Plate ((SS)	A-ZZ-Z-04-DISP_PISTON_ROD	Α

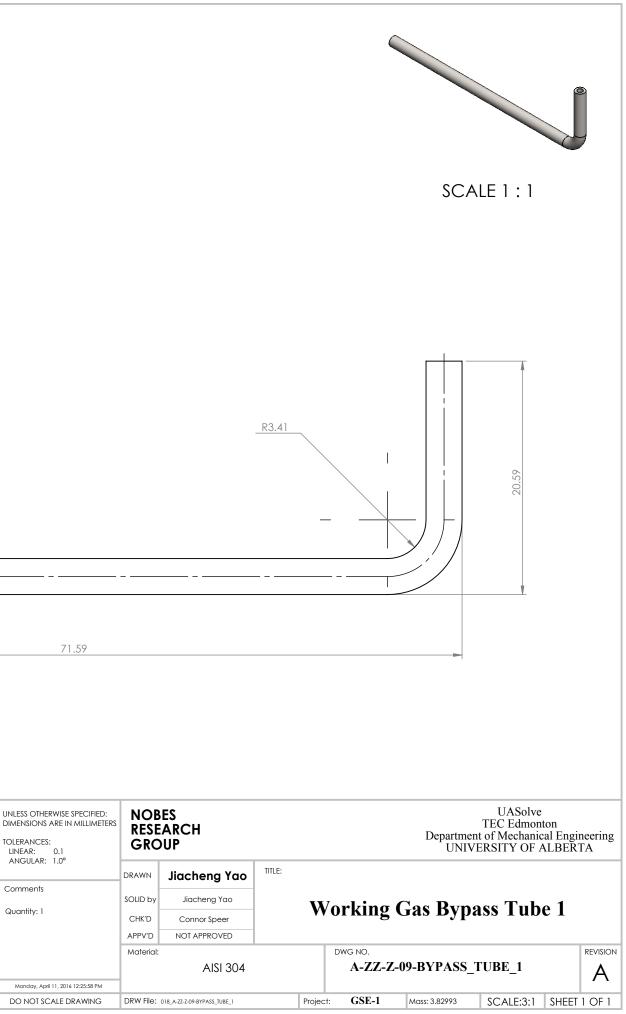
Mass: 83.28454

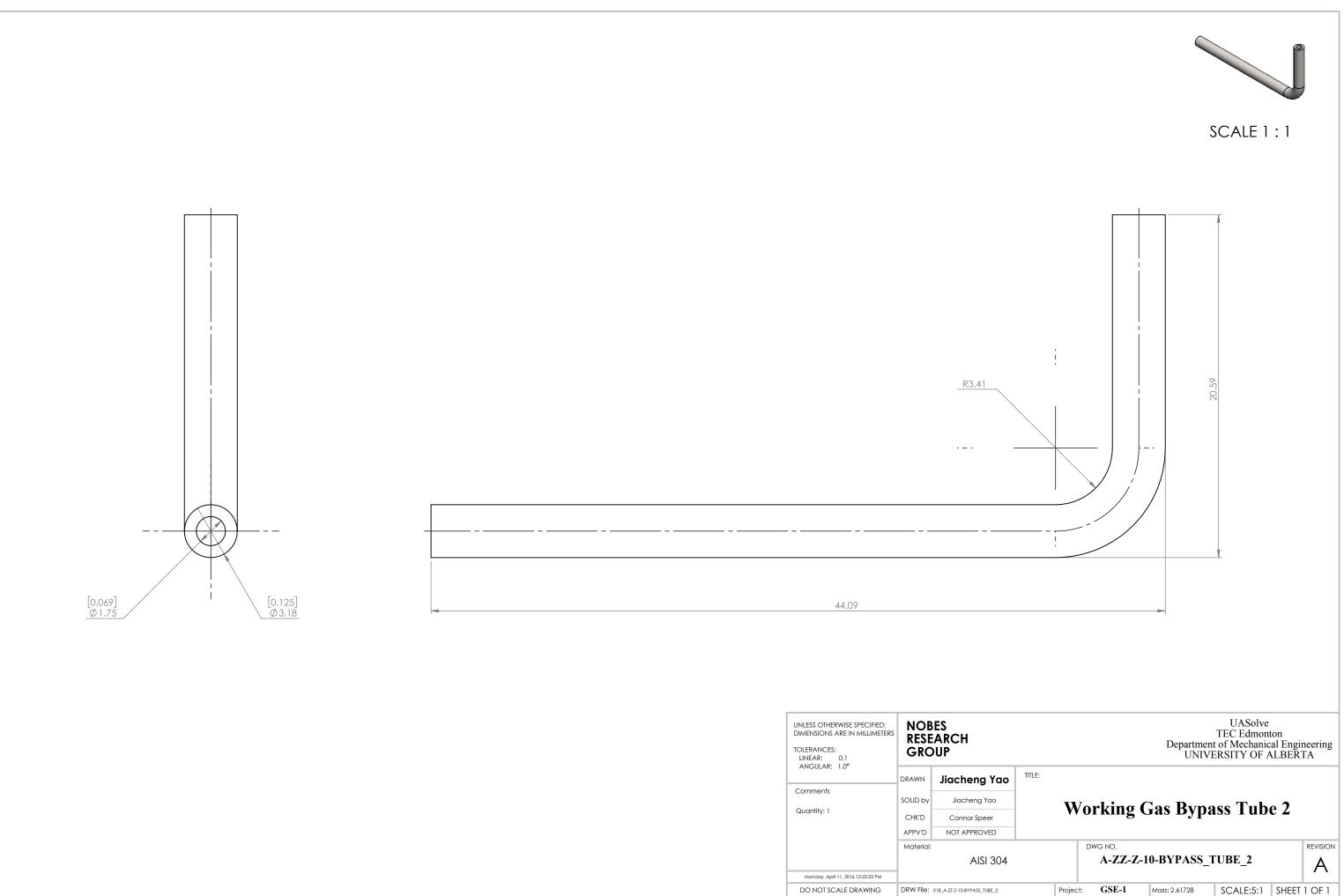
GSE-1

Project:

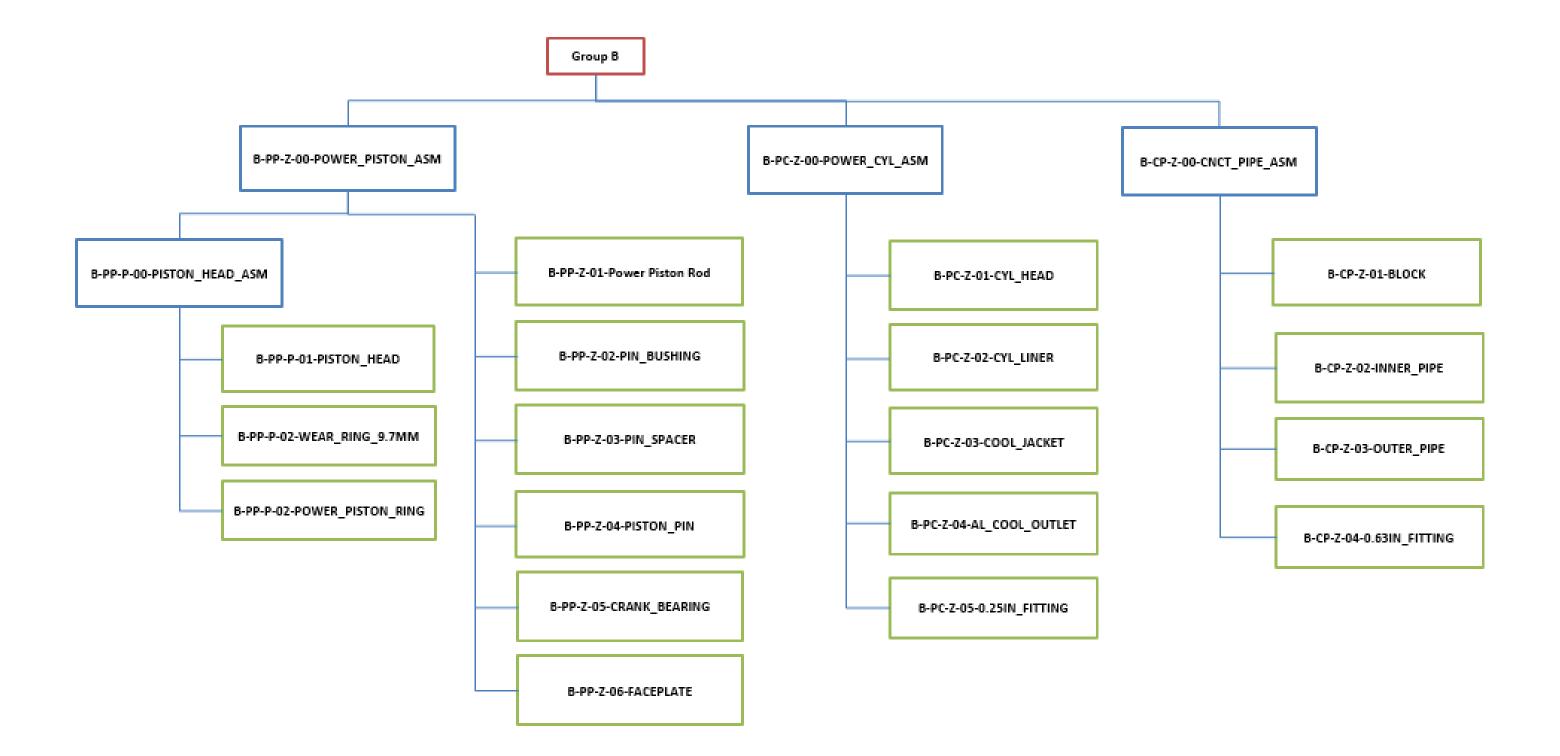




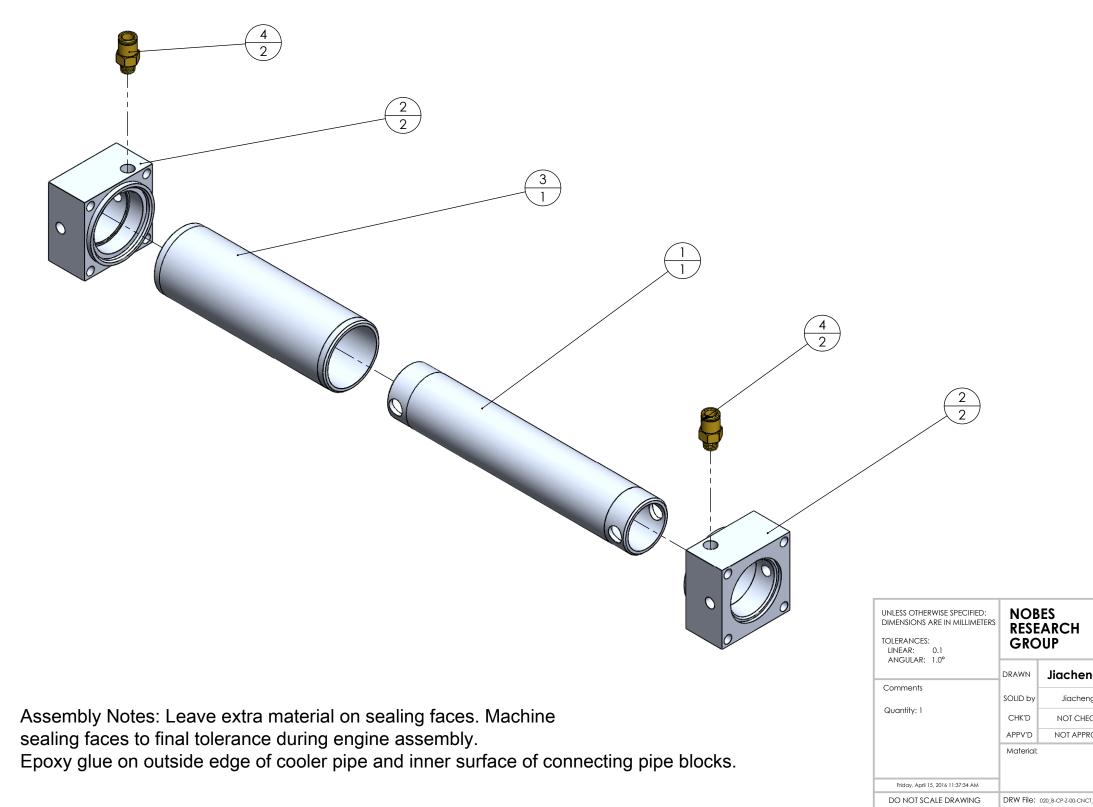


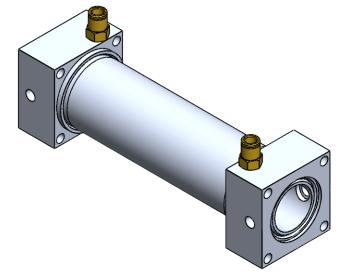


VLESS OTHERWISE SPECIFIED: IMENSIONS ARE IN MILLIMETERS DLERANCES: LINEAR: 0,1 ANGULAR: 1,0°	RESE GRC	ARCH
	DRAWN	Jiacheng
Comments	SOLID by	Jiacheng Y
Quantity: 1	CHK'D	Connor Spe
	APPV'D	NOT APPROV
	Material:	AISI
Monday, April 11, 2016 12:22:22 PM		
do not scale drawing	DRW File:	018_A-ZZ-Z-10-BYPASS_TU

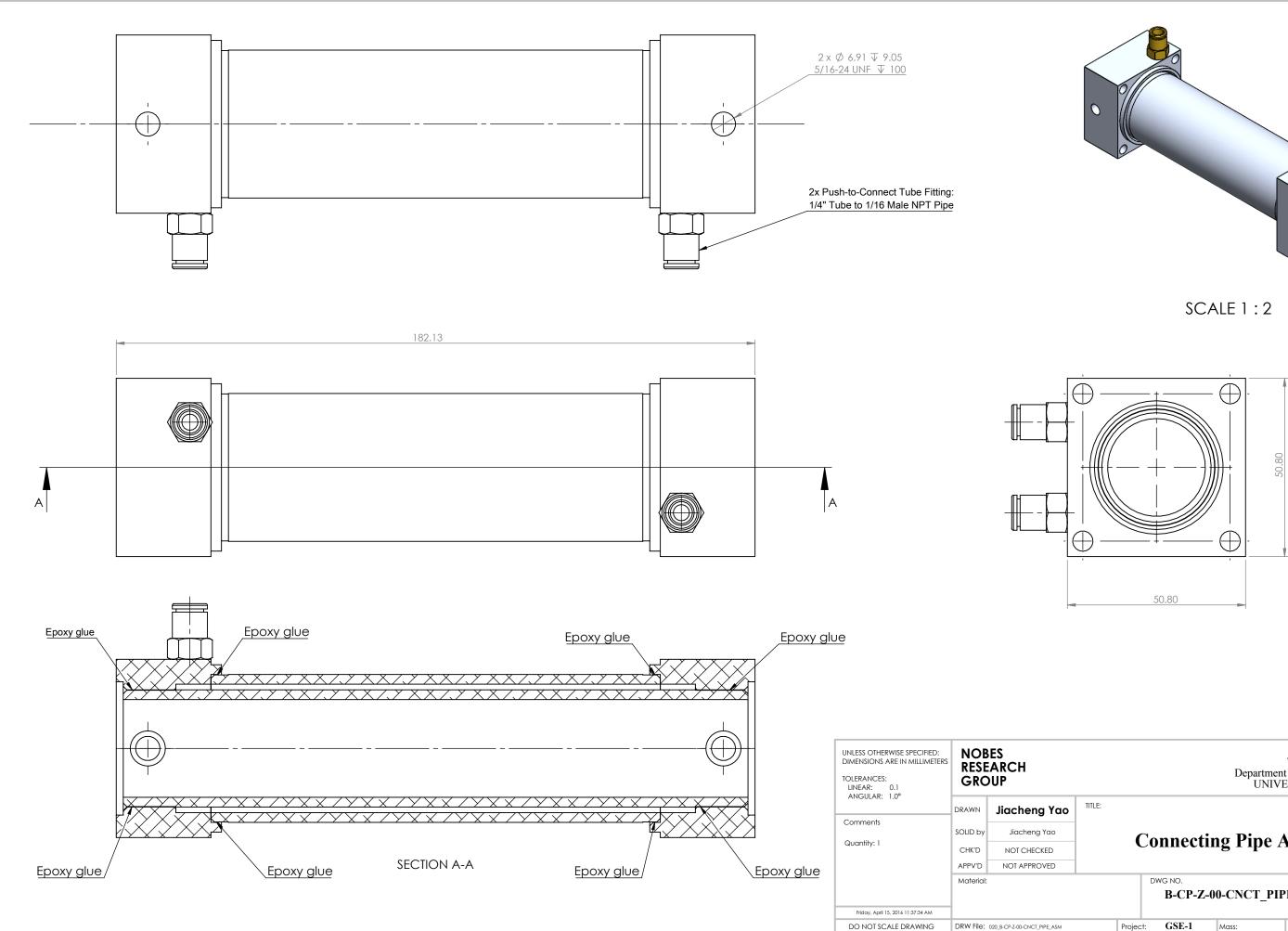


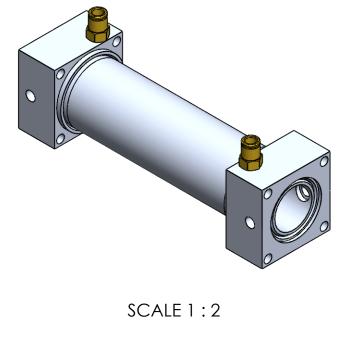
ITEM NO.	DRW NUMBER	Material	QTY.
1	B-CP-Z-02-INNER_PIPE	6061-O (SS)	1
2	B-CP-Z-01-BLOCK	6061-O (SS)	2
3	B-CP-Z-03-OUTER_PIPE	6061-O (SS)	1
4	B-CP-Z-04-0.63IN_FITTING		2



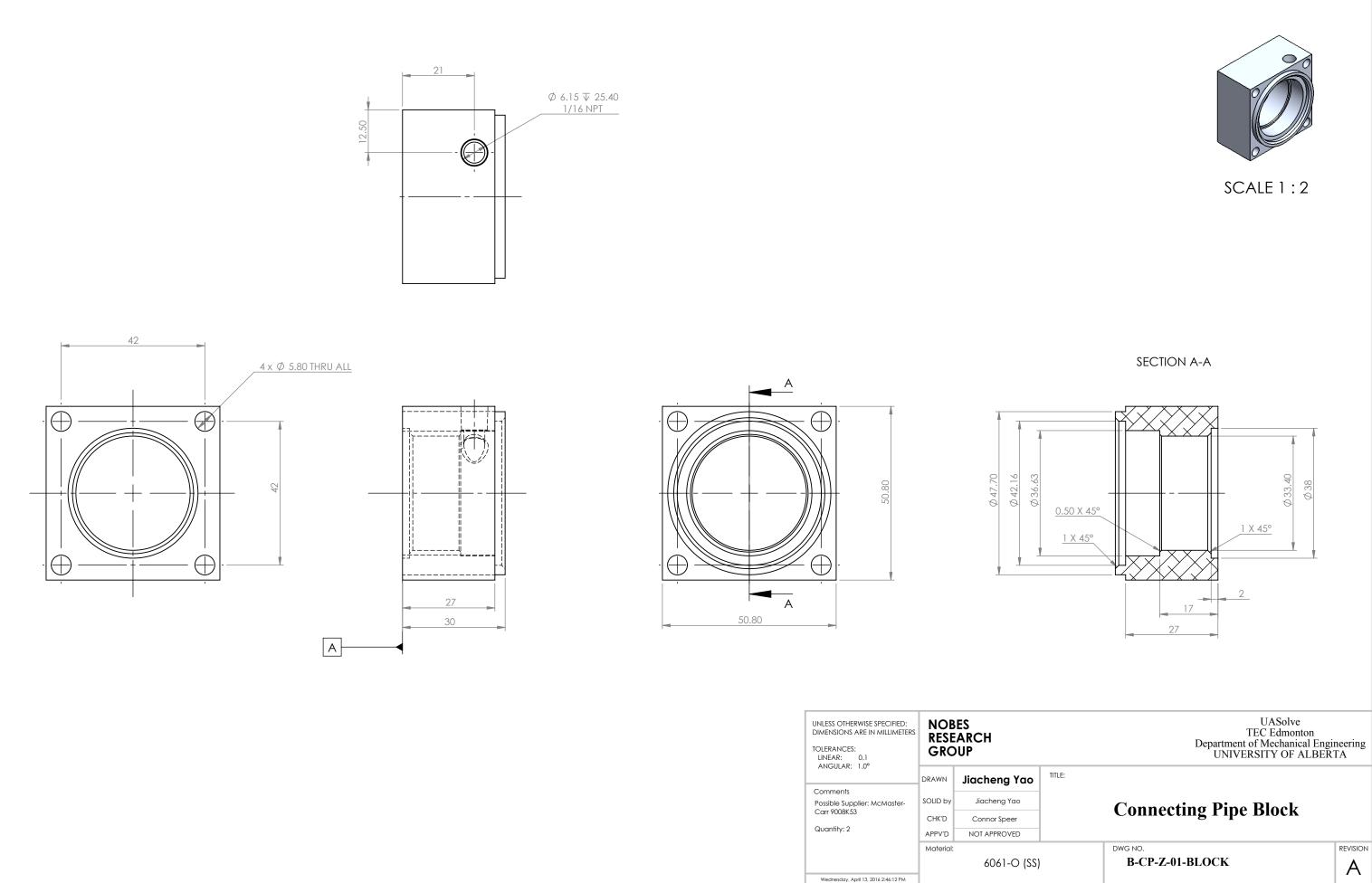


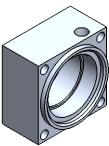
g Yao	TITLE:						
g Yao		(onnati	ng Ding /	ssomb	x 7	
CKED		ľ		ng Pipe A	72261110	l y	
OVED							
			DWG NO.				REVISION
			B-CP-Z-	00-CNCT_PIP	'E_ASM		А
_PIPE_ASM		Projec	t: GSE-1	Mass:	SCALE:1:2	SHEET	1 OF 2





g Yao	TITLE:						
g Yao		(onnacti	ng Ding /	scomb	x 7	
CKED		ľ	Connecti	ig ripe A	7226111D	l y	
OVED							
			DWG NO.				REVISION
			B-CP-Z-0	00-CNCT_PIP	'E_ASM		А
PIPE_ASM		Projec	t: GSE-1	Mass:	SCALE:1:1	SHEET	2 OF 2



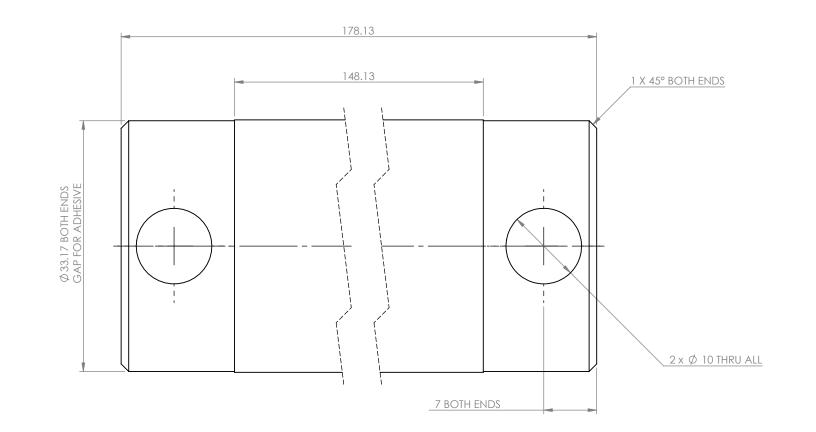




GSE-1

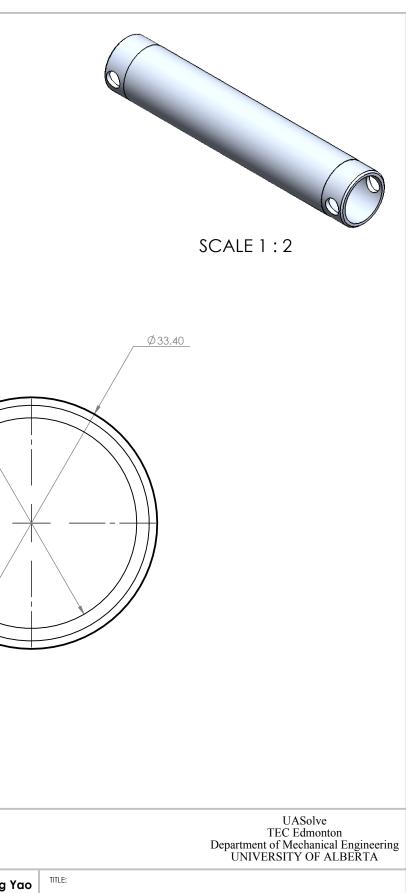
Project:

Mass: 111.82140 SCALE:1:1 SHEET 1 OF 1



NOBES RESEARCH GROUP UNLESS OTHERWISE SPECIFIED: DIMENSIONS ARE IN MILLIMETERS TOLERANCES: LINEAR: 0.1 ANGULAR: 1.0° Jiacheng DRAWN Comments 1" SCH 10 Pipe Possible Supplier: McMaster-Carr 4561T311 SOLID by Jiacheng CHK'D Connor Sp APPV'D NOT APPRO Quantity: 1 Material: 606 Wednesday, April 13, 2016 2:33:47 PM do not scale drawing DRW File: 020_B-CP-Z-02-INNER_P

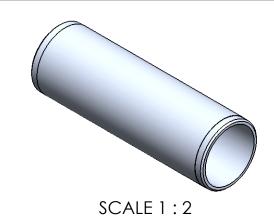
Ø27.86



g Yao	TITLE:							
g Yao			Inn	or C	onnootir	ng Dina		
beer			11111		onnectir	ig r ipe		
DVED								
			DWG NO.					REVISION
I-O (SS)			B-C	P-Z-0	2-INNER_PI	PE		Α
PIPE		Projec	t: GSE	-1	Mass: 124.65968	SCALE:2:1	SHEET	1 OF 1

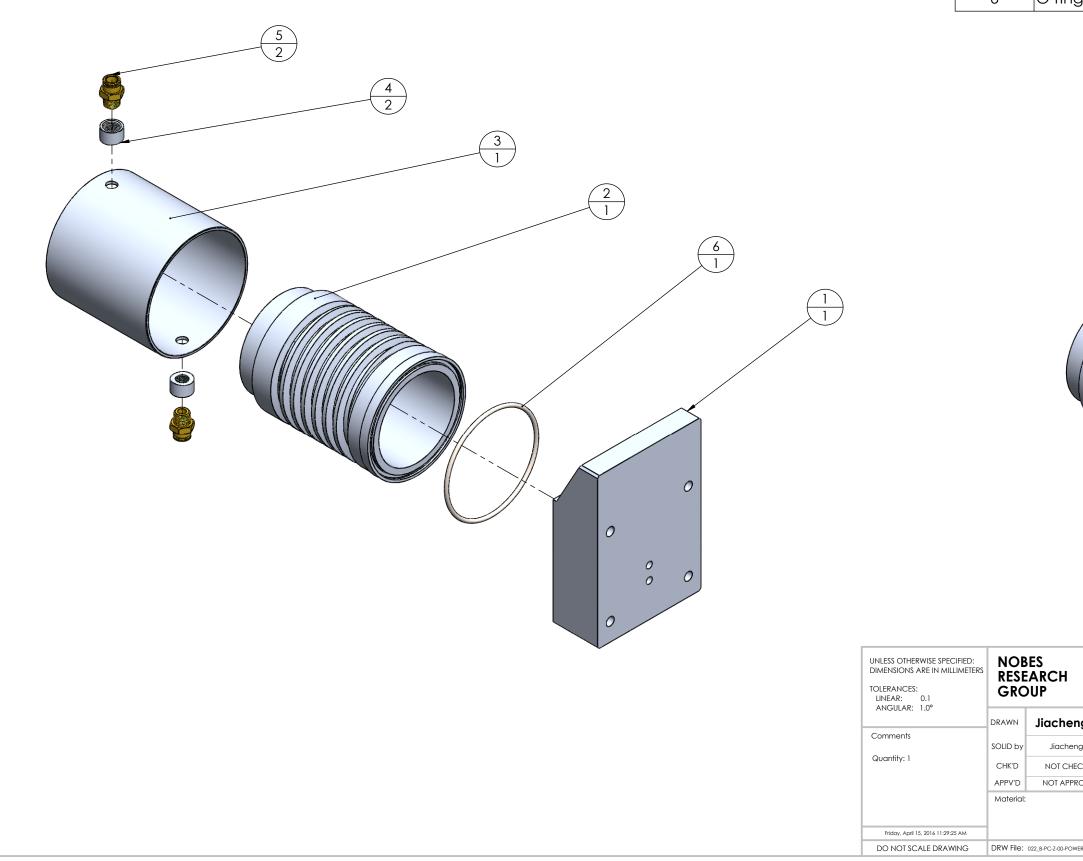
128.13	1 X 45° BOTH ENDS
	Ø 41.90 BOTH ENDS 3AP FOR ADHESIVE)
	(GAP FOI

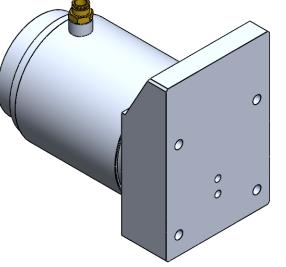
UNLESS OTHERWISE SPECIFIED: DIMENSIONS ARE IN MILLIMETERS TOLERANCES: LINEAR: 0.1 ANGULAR: 1.0°				UASolve TEC Edmonton Department of Mechanical Engineerii UNIVERSITY OF ALBERTA				neering ΓΑ	
ANGULAR. 1.0	DRAWN	Jiacheng Yao	TITLE:						
Comments									
1 1/4" SCH 10 pipe	SOLID by	Jiacheng Yao	Outer Connecting Pipe						
Possible Supplier: McMaster- Carr 4561T411	CHK'D	Connor Speer			Outer	Jonnecui	ig ripe		
Quantity: 1	APPV'D	NOT APPROVED							
	Material:				DWG NO.				REVISION
		6061-O (SS)			B-CP-Z-	03-OUTER_P	IPE		Α
Wednesday, April 13, 2016 2:30:30 PM									
DO NOT SCALE DRAWING	DRW File:	020_B-CP-Z-03-OUTER_PIPE		Project:	GSE-1	Mass: 117.57288	SCALE:1.5:1	SHEET	1 OF 1



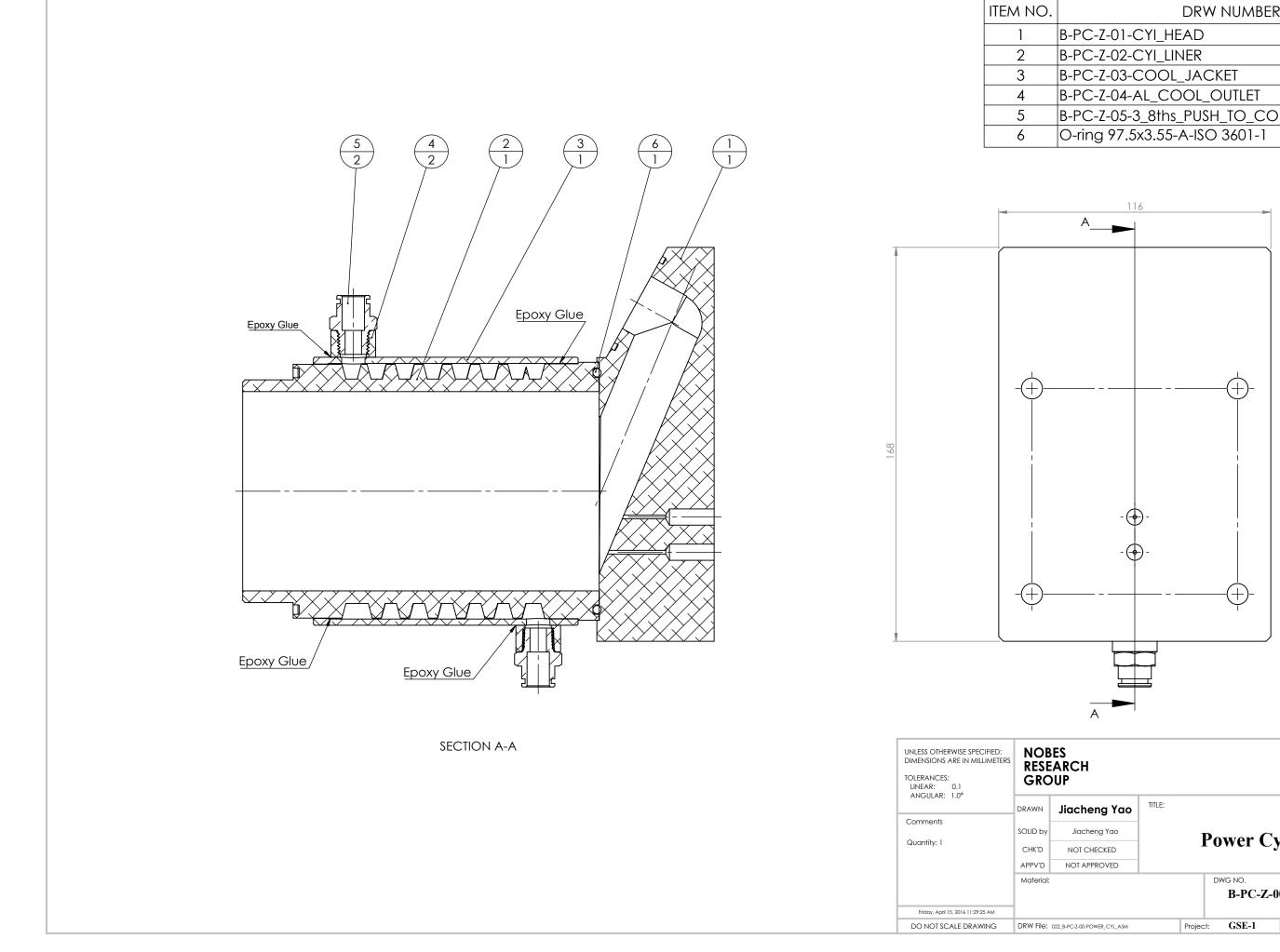
Ø36.63 Ø42.16

ITEM NO.	DRW NUMBER	QTY.
1	B-PC-Z-01-CYI_HEAD	1
2	B-PC-Z-02-CYI_LINER	1
3	B-PC-Z-03-COOL_JACKET	1
4	B-PC-Z-04-AL_COOL_OUTLET	2
5	B-PC-Z-05-3_8ths_PUSH_TO_CONNECT_FITTING2	2
6	O-ring 97.5x3.55-A-ISO 3601-1	1



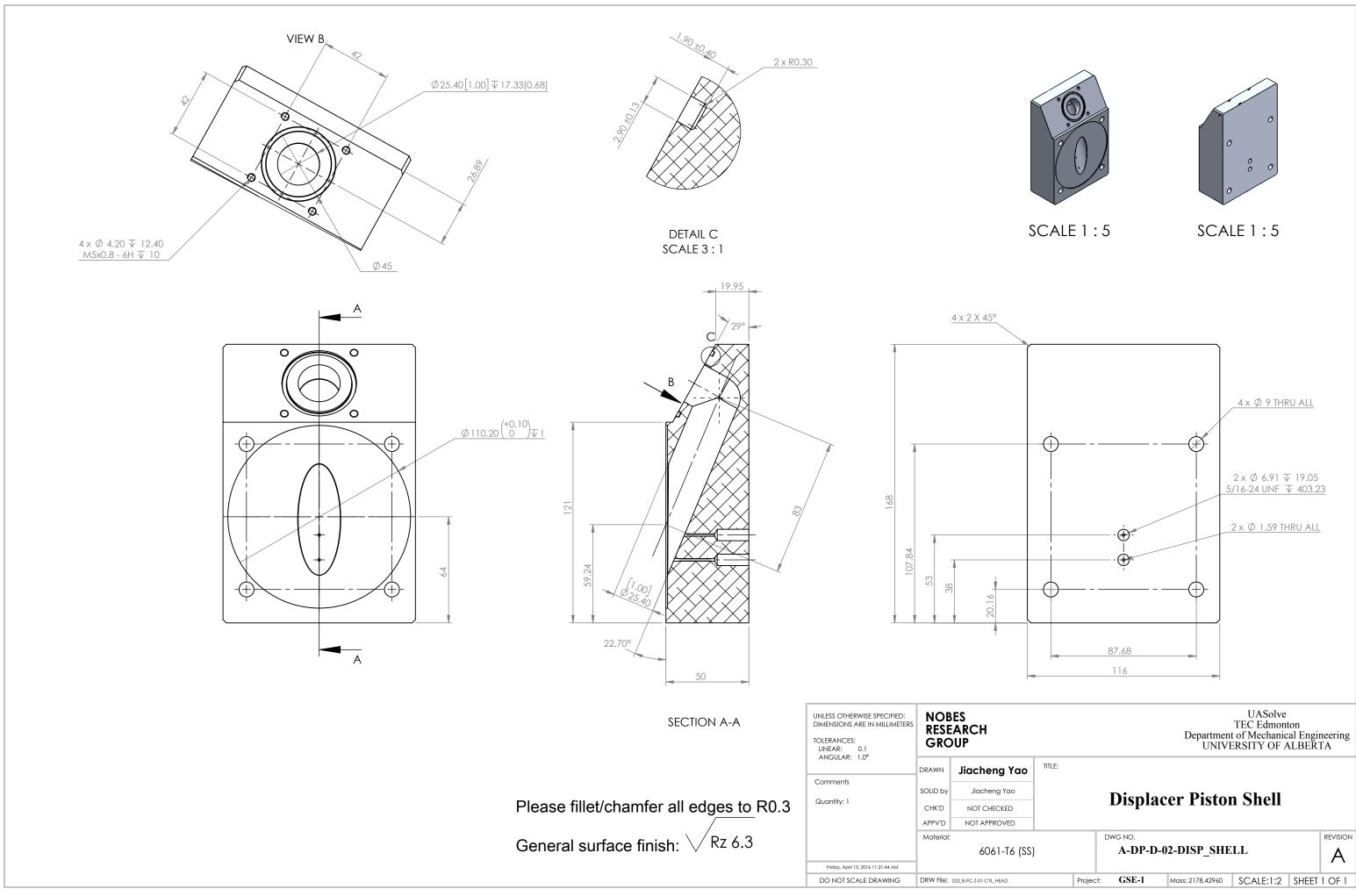


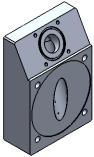
Jiacheng Yao	TITLE:					
Jiacheng Yao		Do	wor C	vlindor	Assambl	x 7
NOT CHECKED		F U	wer C	ylinder A	Assembl	l y
NOT APPROVED						
		D	WG NO. B-PC-Z-	00-POWER_	CYL_ASM	REVISION
022_B-PC-Z-00-POWER_CYL_ASM		Project:	GSE-1	Mass:	SCALE:1:3	SHEET 1 OF 2

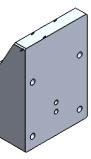


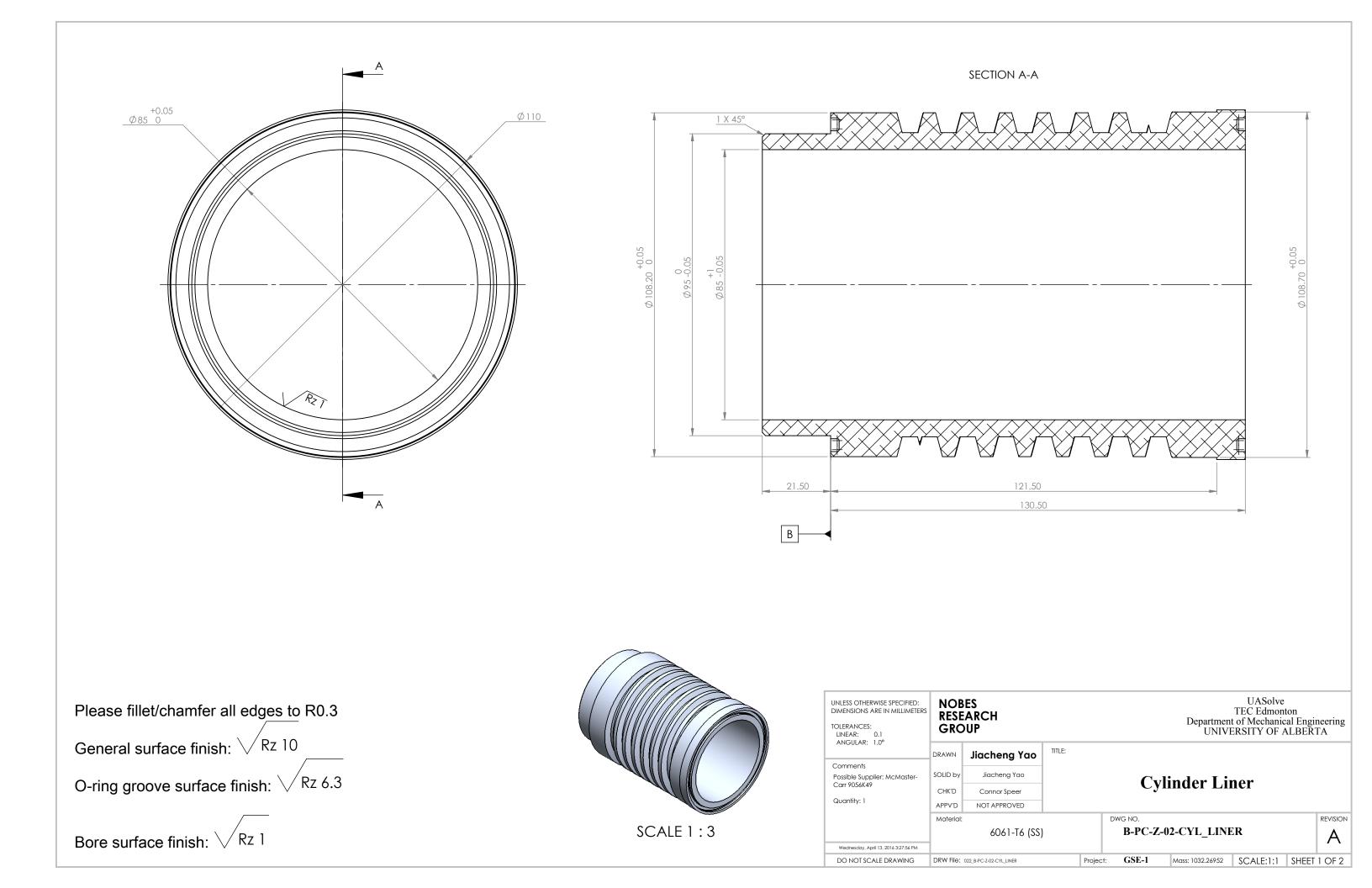
DRW NUMBER	QTY.
-Z-01-CYI_HEAD	1
-Z-02-CYI_LINER	1
-Z-03-COOL_JACKET	1
-Z-04-AL_COOL_OUTLET	2
-Z-05-3_8ths_PUSH_TO_CONNECT_FITTING2	2
g 97.5x3.55-A-ISO 3601-1	1

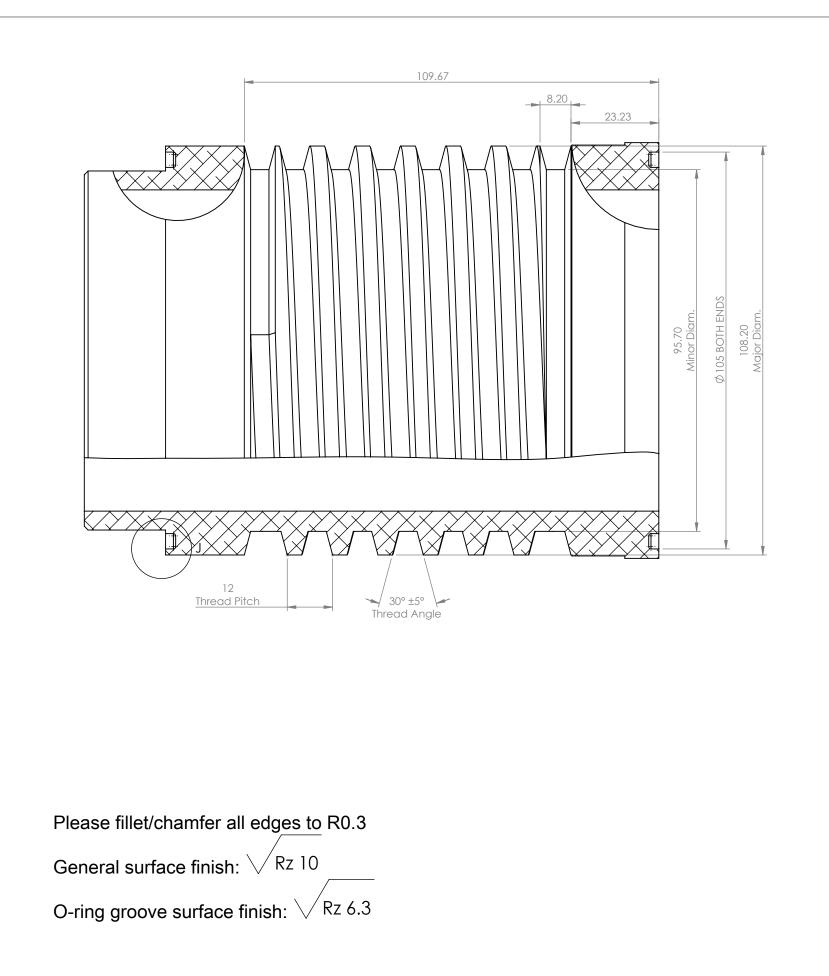
ng Yao	TITLE:									
ng Yao		1	Dowon C	ulindan A	ssamhl	T 7				
ECKED		Power Cylinder Assembly								
ROVED										
	-		DWG NO.				REVISION			
			B-PC-Z-	00-POWER_C	CYL_ASM		A			
VER_CYL_ASM Pro			t: GSE-1	Mass:	SCALE:2:3	SHEET	2 OF 2			



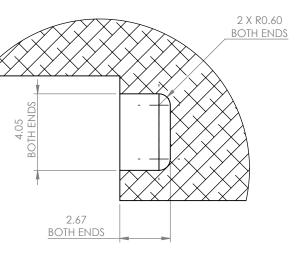






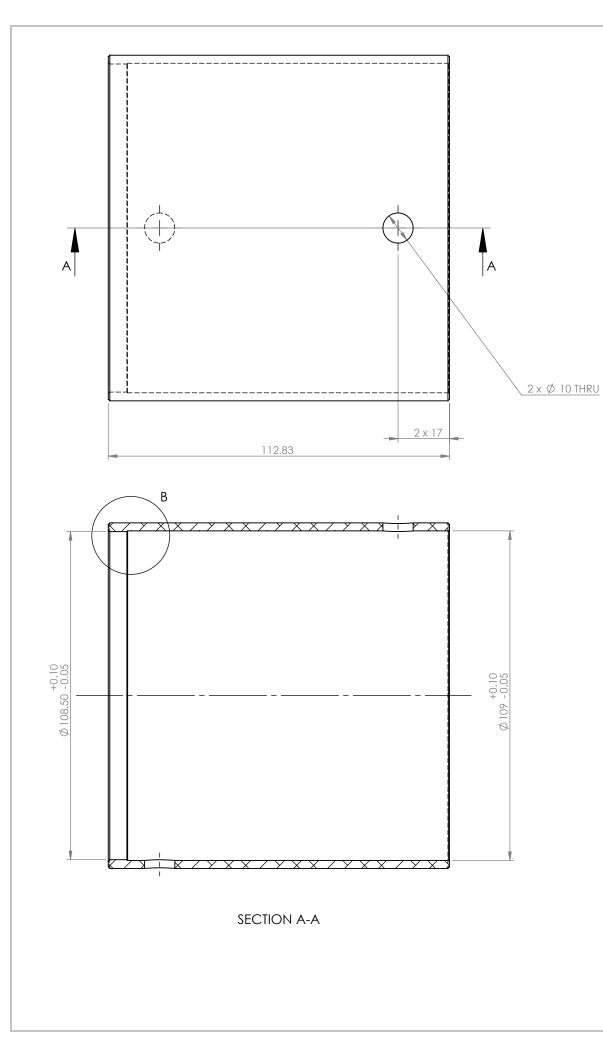


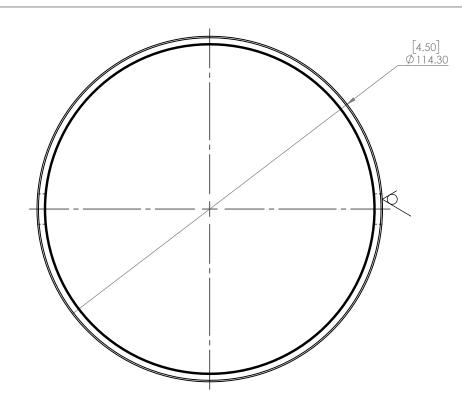
UASolve TEC Edmonton Department of Mechanical Engineering UNIVERSITY OF ALBERTA UNLESS OTHERWISE SPECIFIED: DIMENSIONS ARE IN MILLIMETERS NOBES RESEARCH TOLERANCES: LINEAR: 0.1 ANGULAR: 1.0° GROUP TITLE: DRAWN Jiacheng Yao Comments SOLID by Jiacheng Yao Possible Supplier: McMaster-**Cylinder Liner** Carr 9056K49 CHK'D Connor Speer Quantity: 1 APPV'D NOT APPROVED Material: DWG NO. REVISION B-PC-Z-02-CYL_LINER 6061-T6 (SS) А Wednesday, April 13, 2016 3:27:56 PM DO NOT SCALE DRAWING GSE-1 Mass: 1032.26952 SCALE:1:1 SHEET 2 OF 2 DRW File: 022_B-PC-Z-02-CYL_LINER Project:

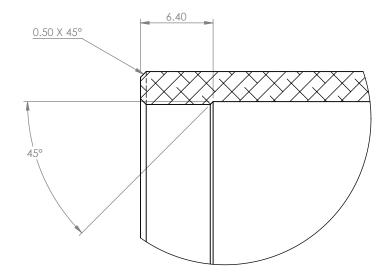


DETAIL J SCALE 5 : 1

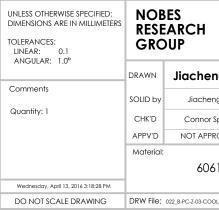
O-Ring Information Material: Nitrile Size: 98 x 3.5mm Supplier: Hi-Tech Seals Part #: MN7 35098

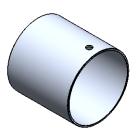






DETAIL B SCALE 3 : 1

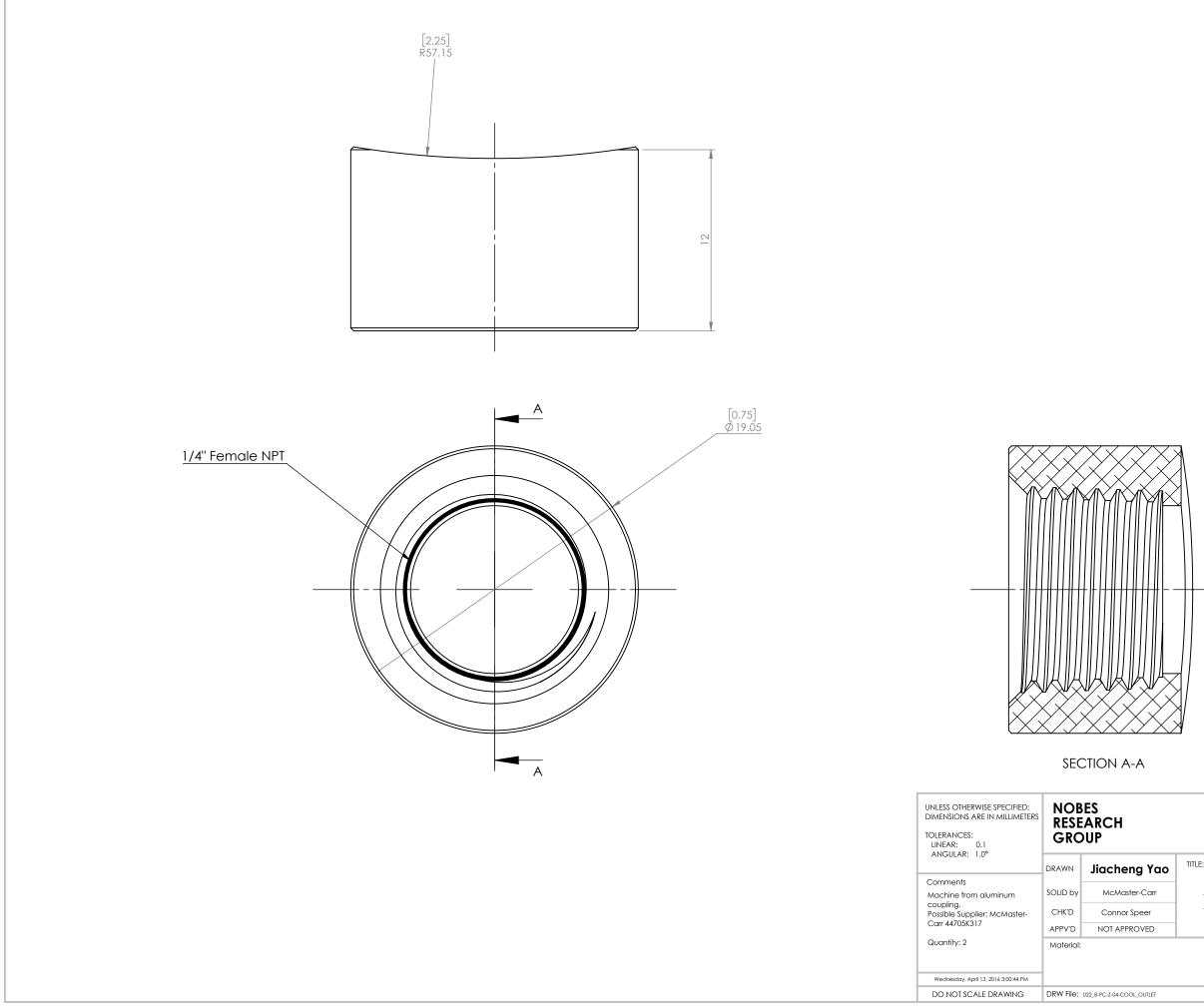




SCALE 1 : 5

Please fillet/chamfer all edges to R0.3 General Surface Finish $\sqrt{Rz 10}$

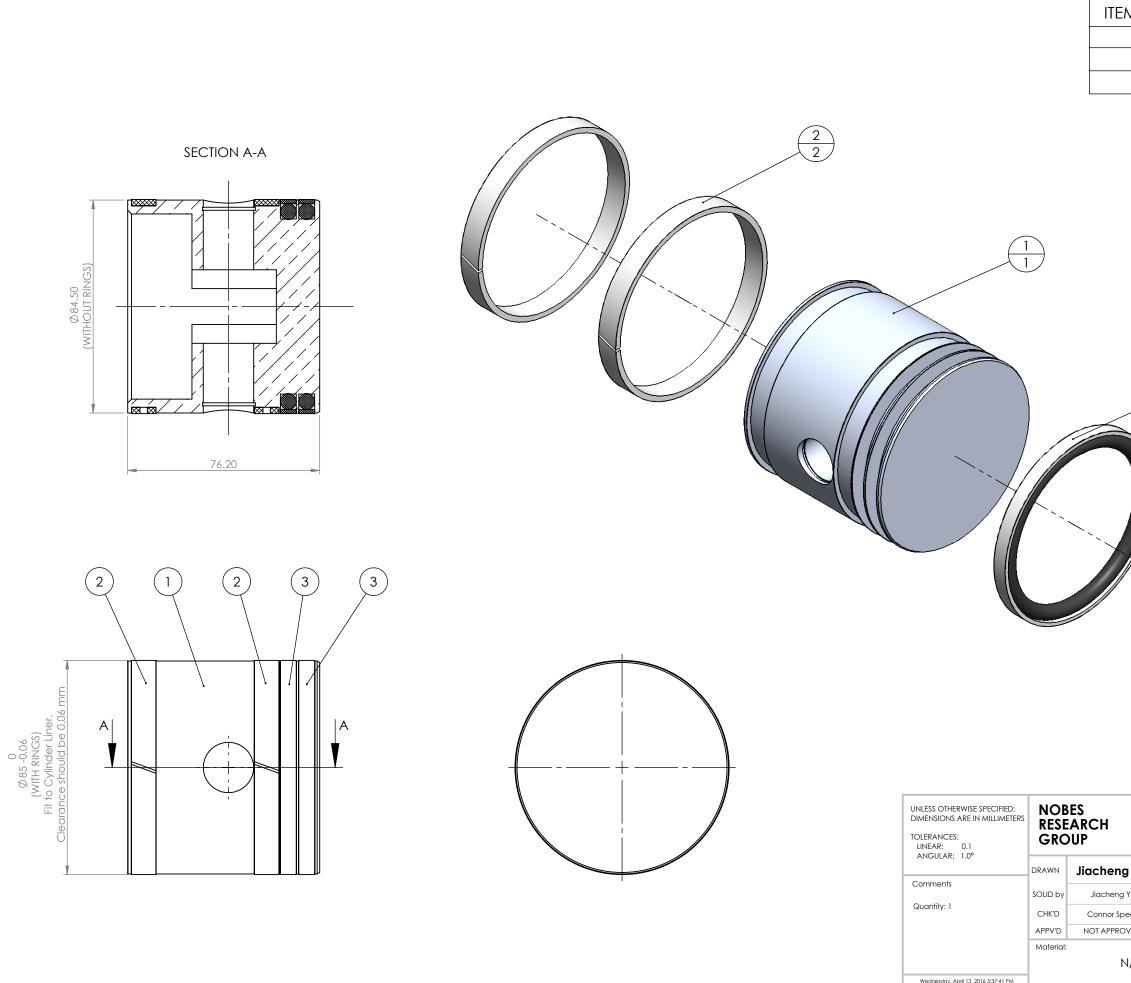
g Yao	TITLE:								
g Yao	De		r Diston	Outor C	ooling	اممار	ot		
peer	10	Power Piston Outer Cooling Jacket							
OVED									
			DWG NO.				REVISION		
1-T6 (SS)	B-PC-Z-03-COOL_JACKET A					А			
JACKET Project: GSE-1 Mass: 283.10333 SCALE:4:5 SHEE				SHEET	1 OF 1				





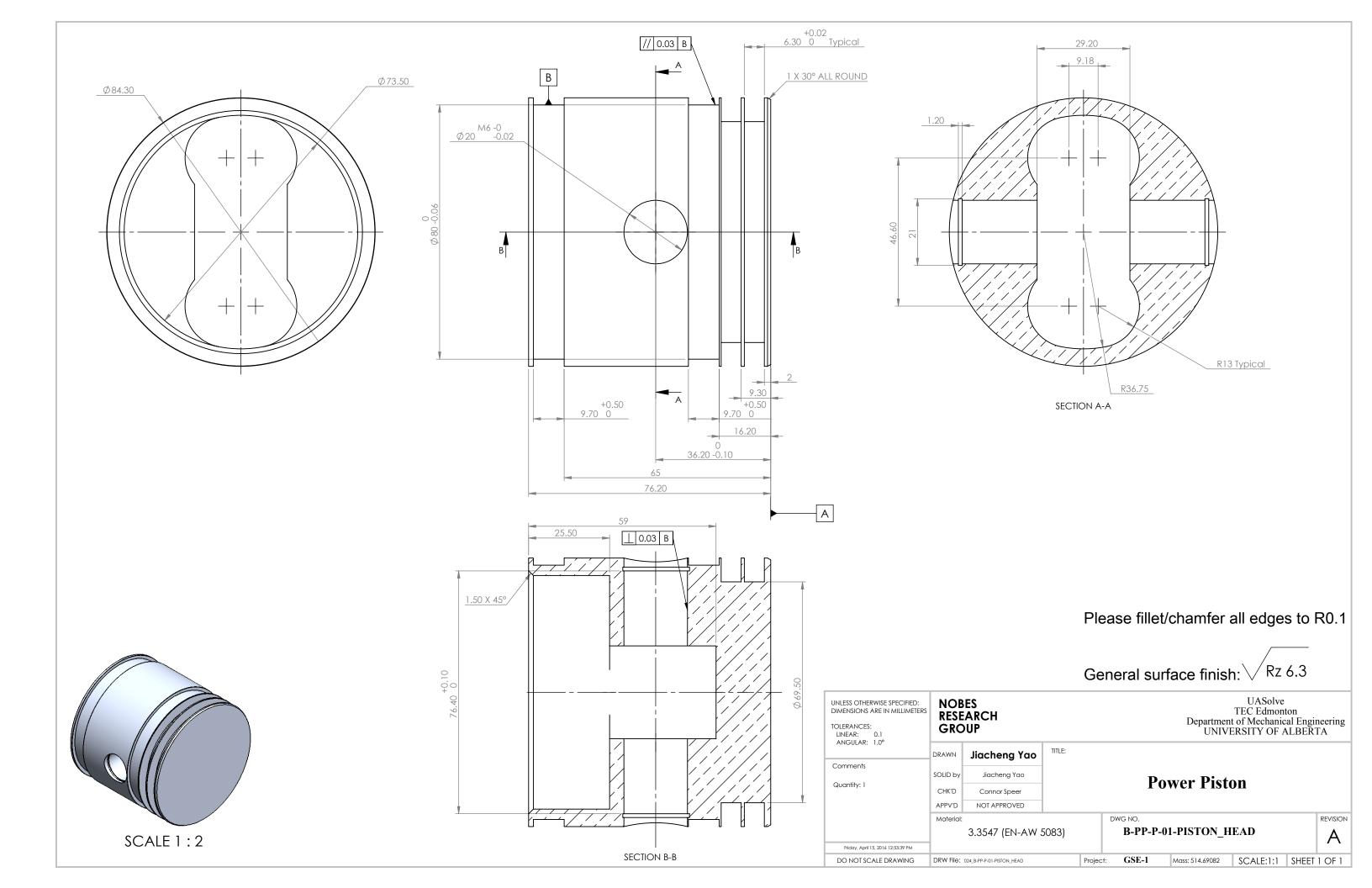
SCALE 2:1

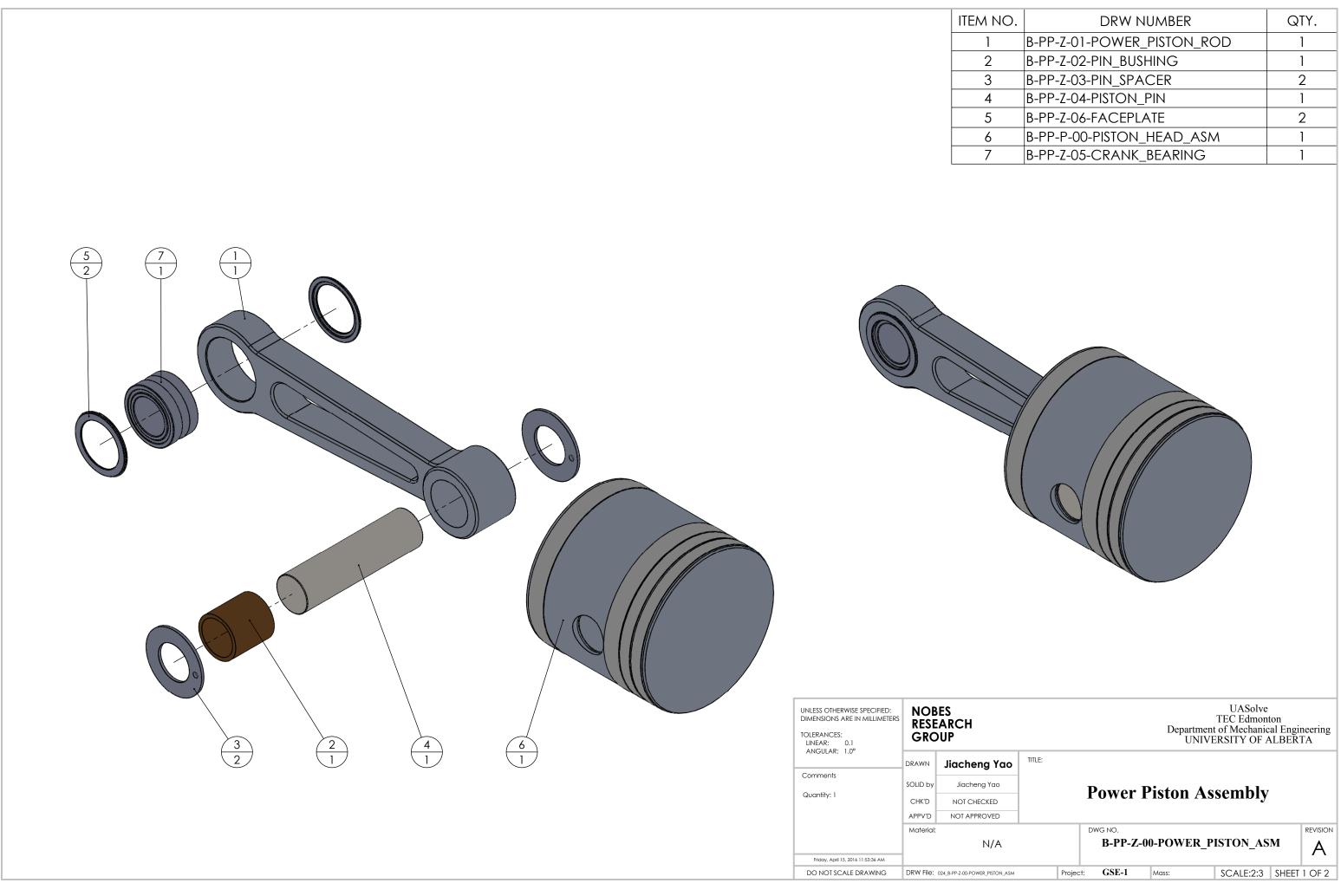
ig Yao	TITLE:							
er-Carr	F.	202		م میل ^د	n Alumi	num Ca	مامر	nt
peer	Ľ	pux	y C	JIUE-0	on Alumi		Juia	11
OVED								
DWG NO. B-PC-Z-04-AL_COOL_OUTLET								
L_OUTLET		Projec	et: (GSE-1	Mass:	SCALE:4:1	SHEET	1 OF 1



ANGULAR: 1.0°									
ANGULAR. 1.0	DRAWN	Jiacheng Yao	TITLE:						
Comments									
	SOLID by	Jiacheng Yao	Power Piston Assembly						
Quantity: 1	CHK'D	Connor Speer							
	APPV'D	NOT APPROVED							
	Material:		DWG NO.			REVISION			
		N/A			B-PP-P-00-PISTON_HEAD_ASM				
Wednesday, April 13, 2016 3:37:41 PM						-		· · · ·	
DO NOT SCALE DRAWING	DRW File:	024_B-PP-P-00-PISTON_HEAD_ASM		Projec	t: GSE-1	Mass:	SCALE:2:3	SHEET 1 OF 1	

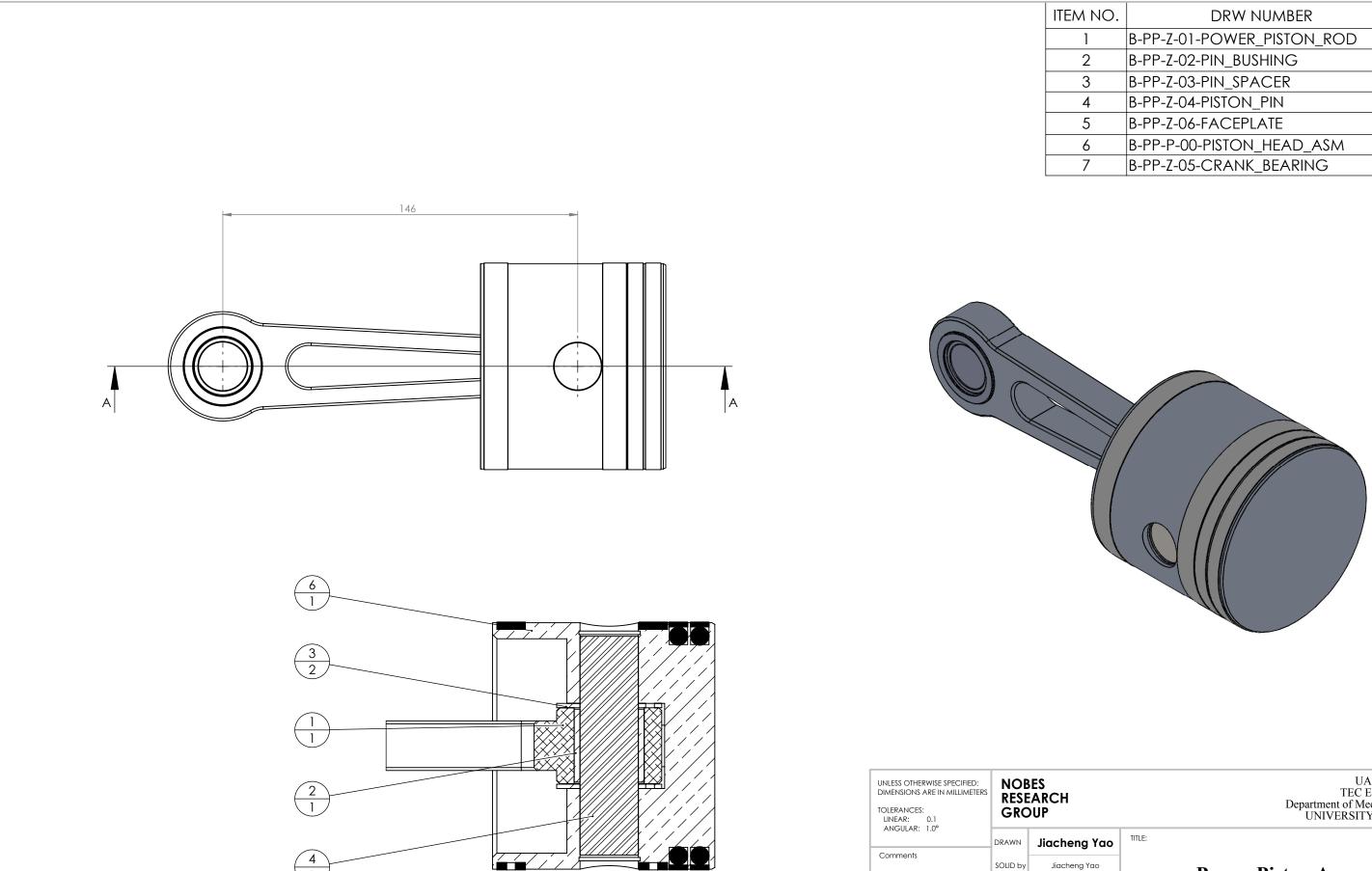
EM NO.	DRW NUMBER	QTY.
1	B-PP-P-01-PISTON_HEAD	1
2	B-PP-P-02-WEAR_RING_9.7MM	2
3	B-PP-P-03-POWER_PISTON_RING	2
	3	2





DRW NUMBER	QTY.
B-PP-Z-01-POWER_PISTON_ROD	1
B-PP-Z-02-PIN_BUSHING	1
B-PP-Z-03-PIN_SPACER	2
B-PP-Z-04-PISTON_PIN	1
B-PP-Z-06-FACEPLATE	2
B-PP-P-00-PISTON_HEAD_ASM	1
B-PP-Z-05-CRANK_BEARING	1
	B-PP-Z-01-POWER_PISTON_ROD B-PP-Z-02-PIN_BUSHING B-PP-Z-03-PIN_SPACER B-PP-Z-04-PISTON_PIN B-PP-Z-06-FACEPLATE B-PP-P-00-PISTON_HEAD_ASM

g Yao	TITLE:				
g Yao		Dowo	Diston	Assombly	
CKED		IUWEI	1 151011	Assembly	
OVED					
		DWG NO.			REVISION
N/A		B-PP-2	Z-00-POWE	R_PISTON_ASM	A
	Deel	CSE 1	11		



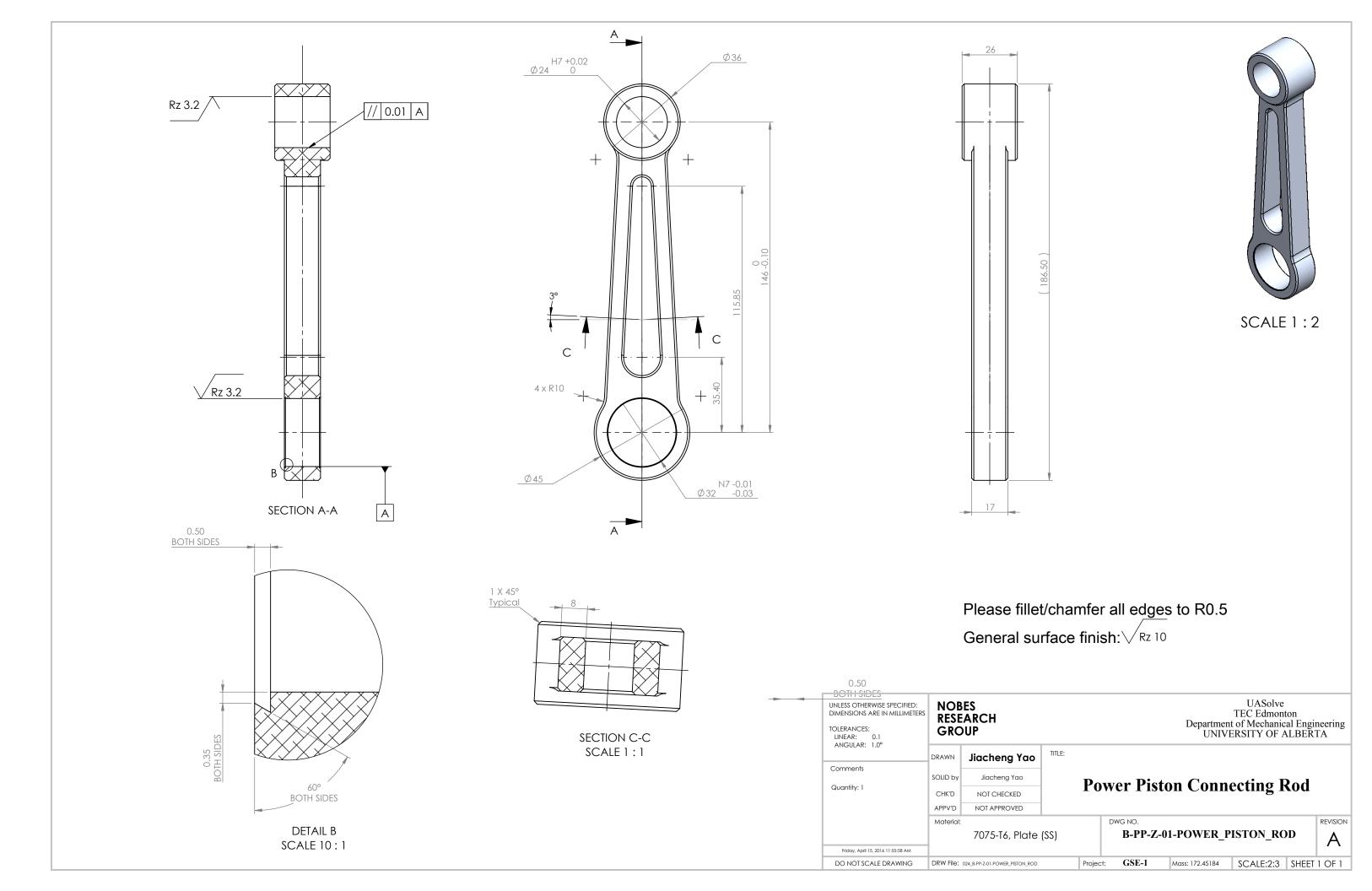
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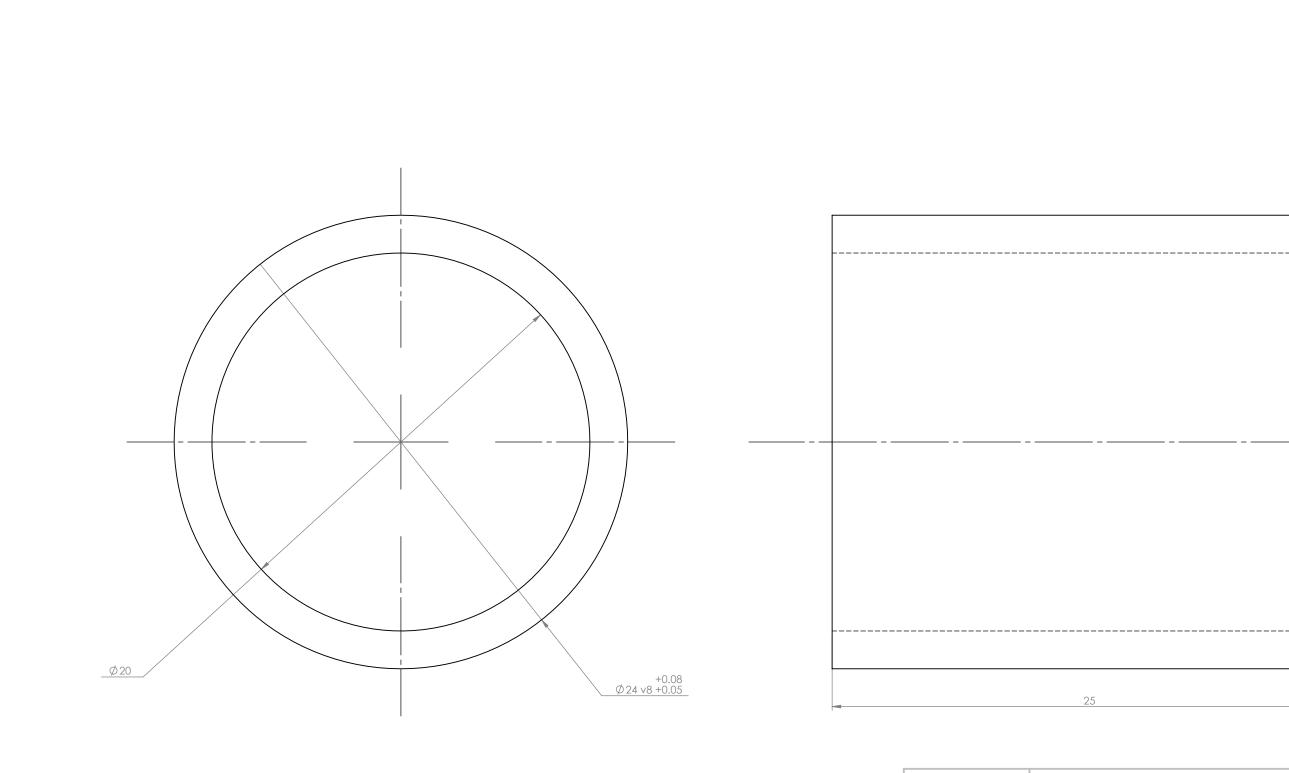
Friday, April 15, 2016 11:53:36 AM do not scale drawing

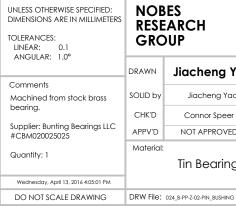
SECTION A-A	
SCALE 4 : 5	

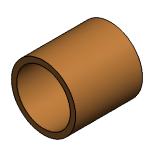
M NO.	DRW NUMBER	QTY.
1	B-PP-Z-01-POWER_PISTON_ROD	1
2	B-PP-Z-02-PIN_BUSHING	1
3	B-PP-Z-03-PIN_SPACER	2
4	B-PP-Z-04-PISTON_PIN	1
5	B-PP-Z-06-FACEPLATE	2
6	B-PP-P-00-PISTON_HEAD_ASM	1
7	B-PP-Z-05-CRANK_BEARING	1

DRAWN	Jiacheng Yao	TITLE:							
DIGUIN	Jucheng Tuo								
SOLID by	Jiacheng Yao		Power Piston Assembly						
CHK'D	NOT CHECKED		Power Piston Assembly						
APPV'D	NOT APPROVED								
Material:			DWG NO.				REVISION		
N/A			B-PP-Z-00-POWER_PISTON_ASM				A		
1						-	7.		
DRW File: 024_B-PP-Z-00-POWER_PISTON_ASM Project			ject: GSE-1	Mass:	SCALE:2:3	SHEET	2 OF 2		

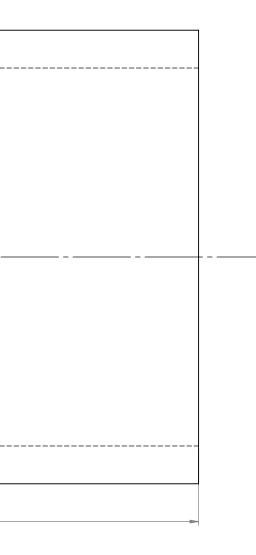




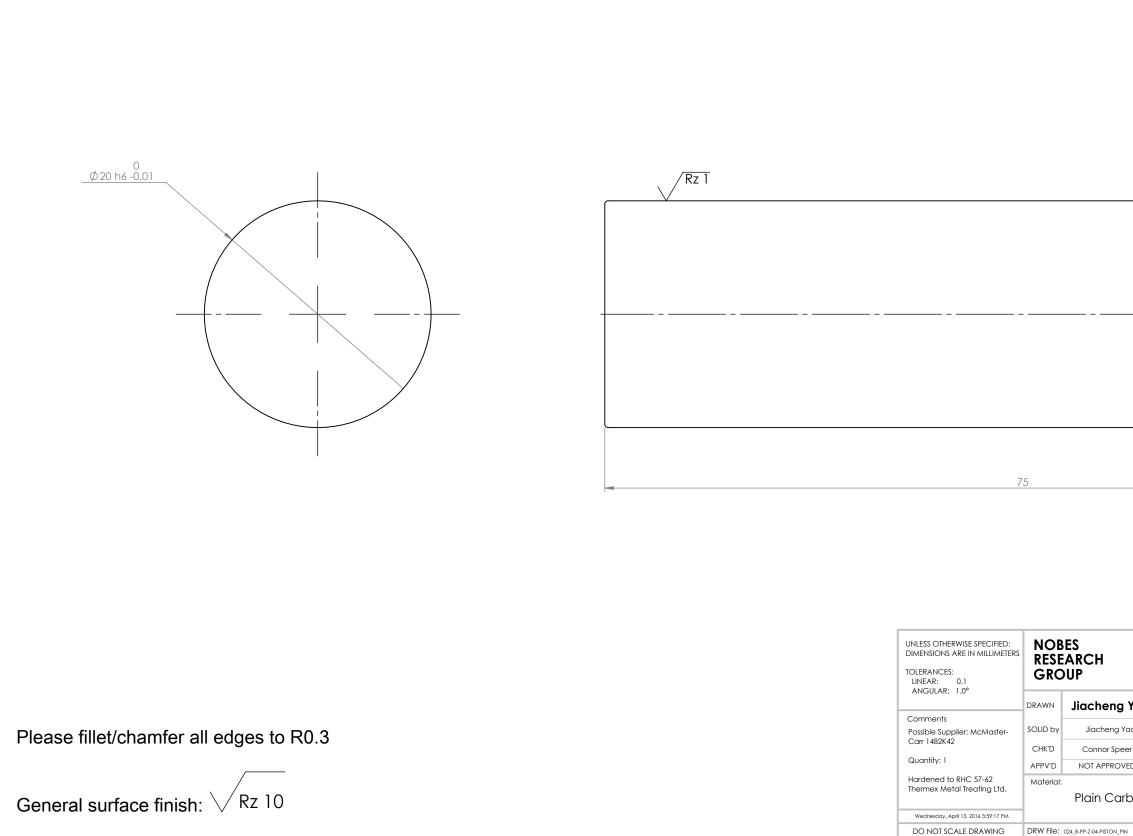




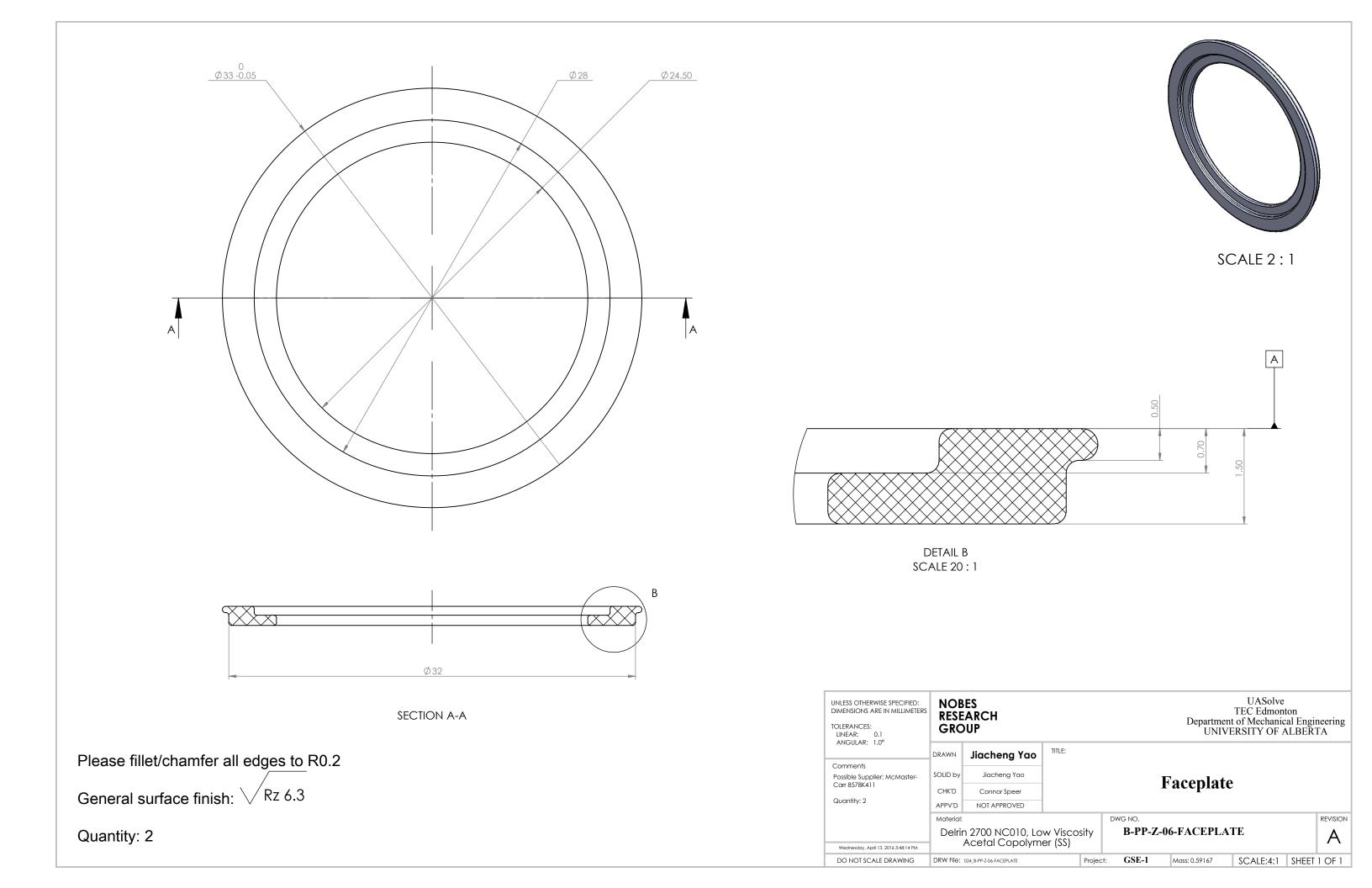
SCALE 1:1

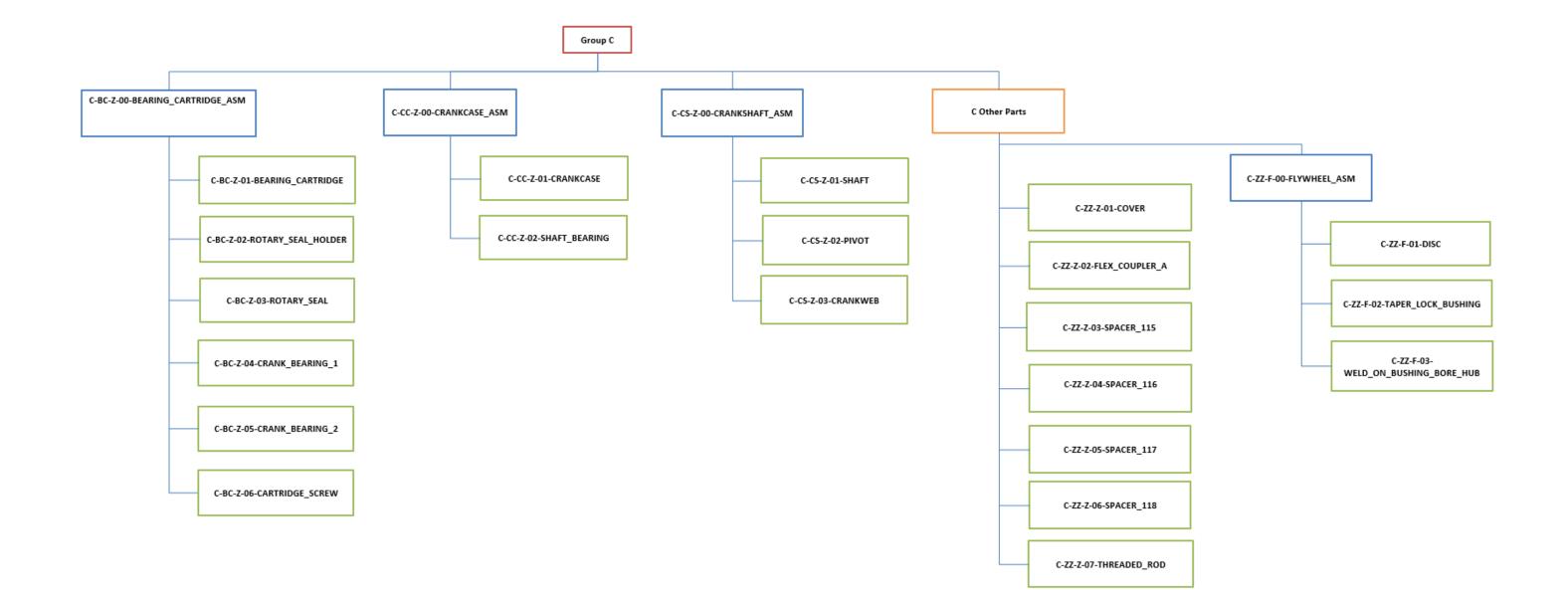


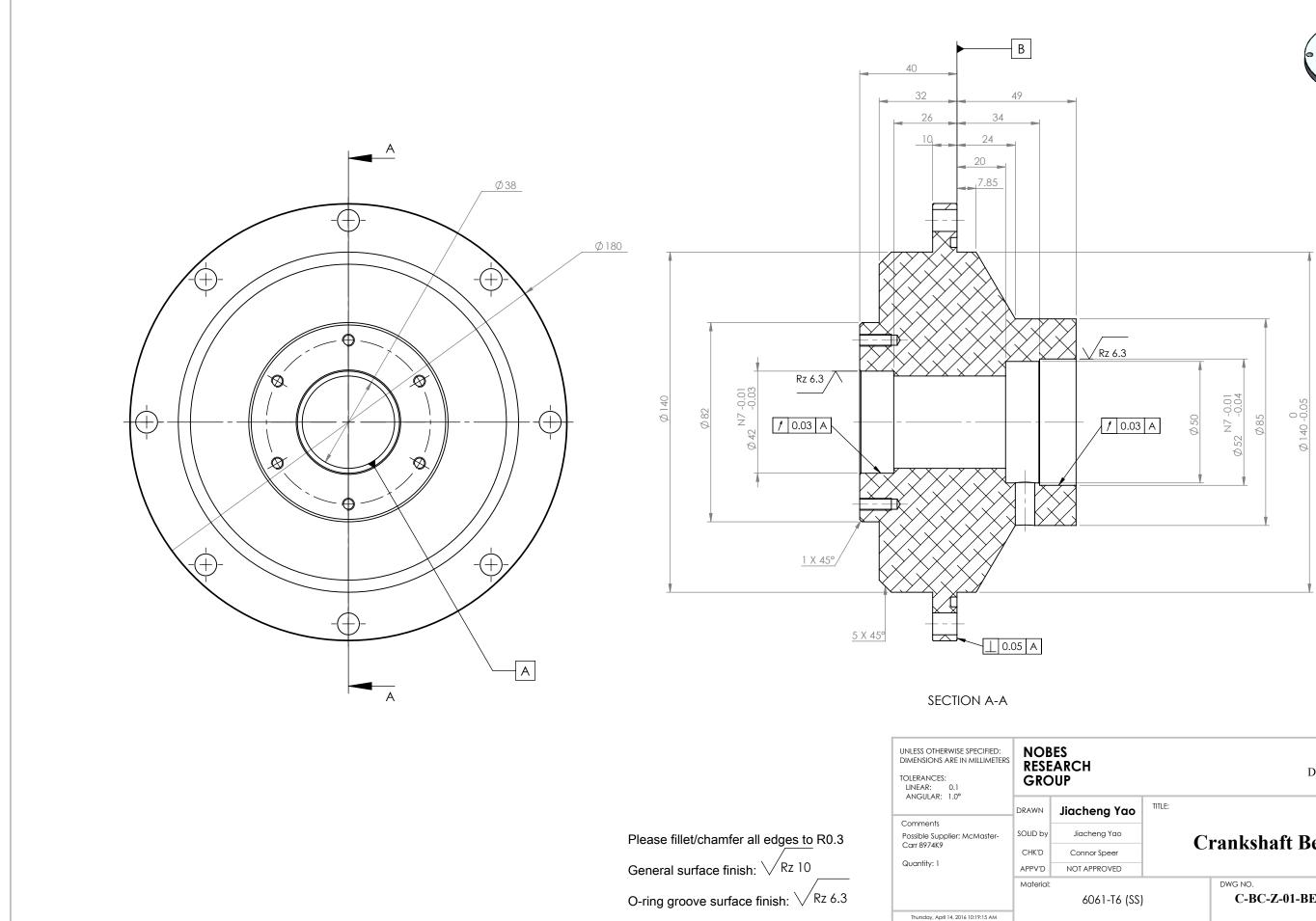
g Yao	TITLE:										
g Yao		Power Piston Pin Bushing									
beer		rower riston rin Dusning									
OVED											
			DWG NO.					REVISION			
ing Bronze B-PP-Z-02-PIN_BUSHING						А					
SHING		Projec	t: GSE-	1	Mass: 28.68274	SCALE:5:1	SHEET	1 OF 1			



				SCALE 1	: 1		
Υaο αο	ΤΙΤLΕ:				UASolve TEC Edmon t of Mechanic ERSITY OF 4	ton cal Engi ALBER	neering TA
^{ao} er ED bon S	teel		DWG NO.	ver Piston			REVISION A
4		Projec	t: GSE-1	Mass: 183.76437	SCALE:3:1	SHEET	1 OF 1







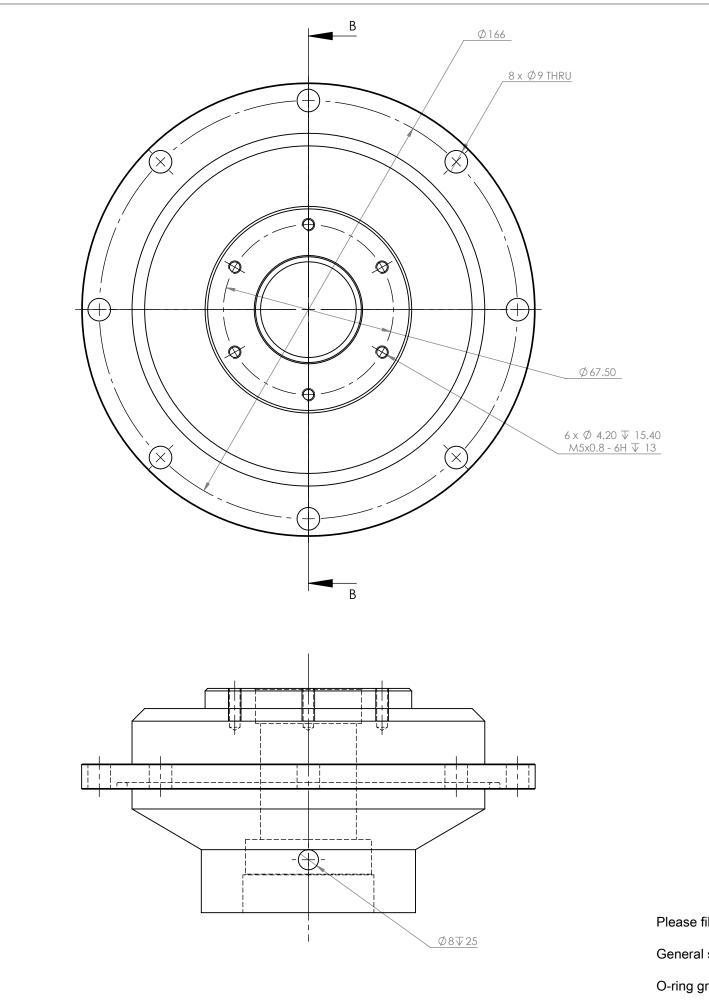


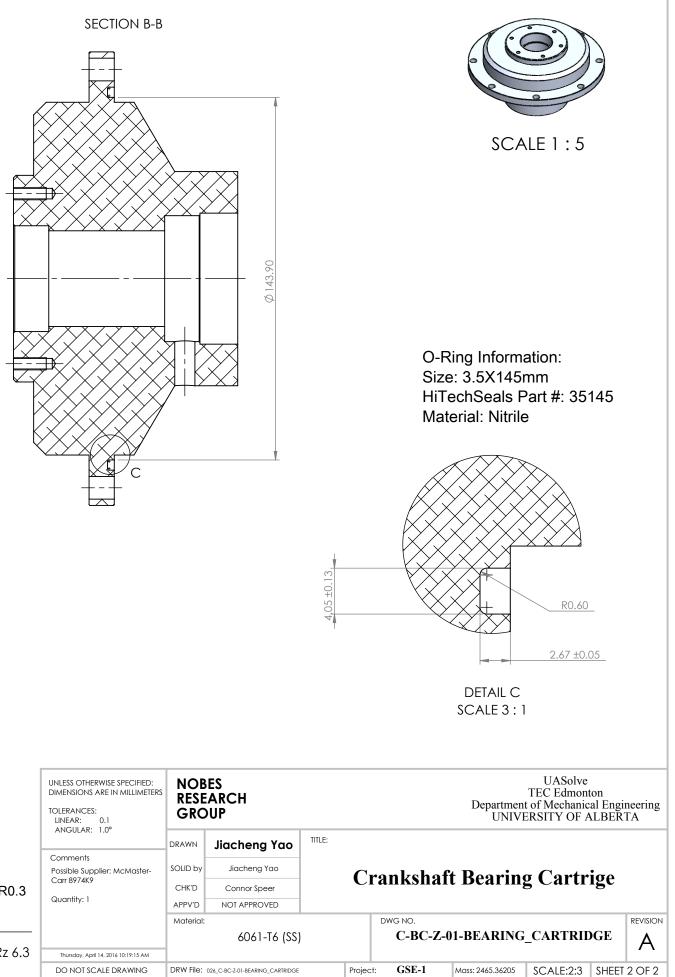
SCALE 1:5

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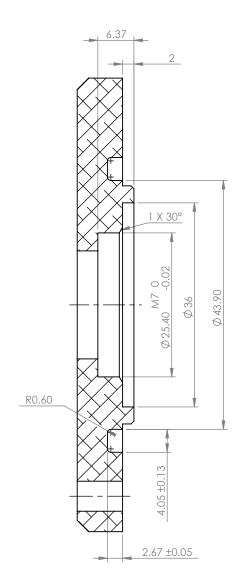
DRAWN	Jiacheng Yao	TITLE:					
SOLID by	Jiacheng Yao	C	nonkshof	t Dooring	a Contr	igo	
CHK'D	Connor Speer	U	Crankshaft Bearing Cartrige				
APPV'D	NOT APPROVED						
Material:			DWG NO.				REVISION
	6061-T6 (SS)		C-BC-Z-01-BEARING_CARTRIDGE				
DRW File: 026_C-BC-Z-01-BEARING_CARTRIDGE			ct: GSE-1	Mass: 2465.36205	SCALE:2:3	SHEET	1 OF 2

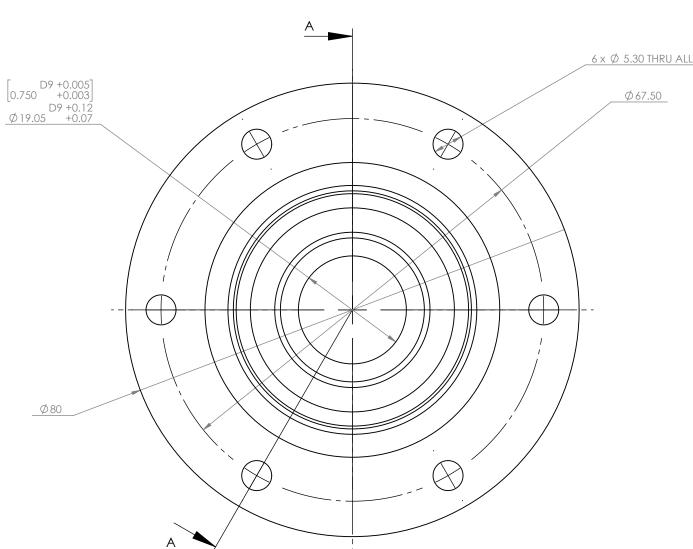
DO NOT SCALE DRAWING





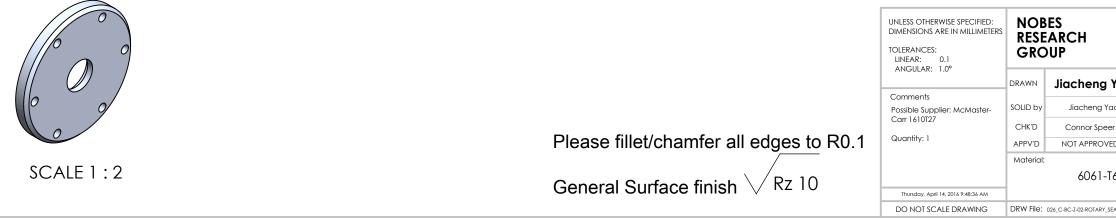
	DIMENSIONS ARE IN MILLIMETERS TOLERANCES: LINEAR: 0.1 ANGULAR: 1.0°			
	ANGULAR: 1.0"	DRAWN	Jiacheng Yo	
	Comments Possible Supplier: McMaster-	SOLID by	Jiacheng Yao	
fillet/chamfer all edges to R0.3	Carr 8974K9	CHK'D	Connor Speer	
	Quantity: 1	APPV'D	NOT APPROVED	
I surface finish: √Rz 10		Material:		
			6061-T6	
groove surface finish: \bigvee Rz 6.3	Thursday, April 14, 2016 10:19:15 AM	l		
	DO NOT SCALE DRAWING	DRW File:	026_C-BC-Z-01-BEARING_CAR	





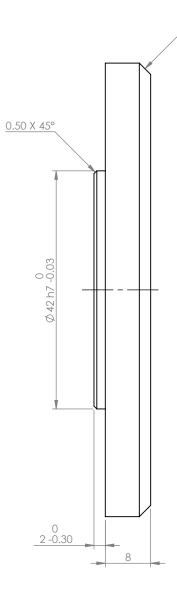
SECTION A-A

O-ring Information Size: 3.5x45mm Supplier: Hi Tech Seals Part#: 35045 Material: Nitrile

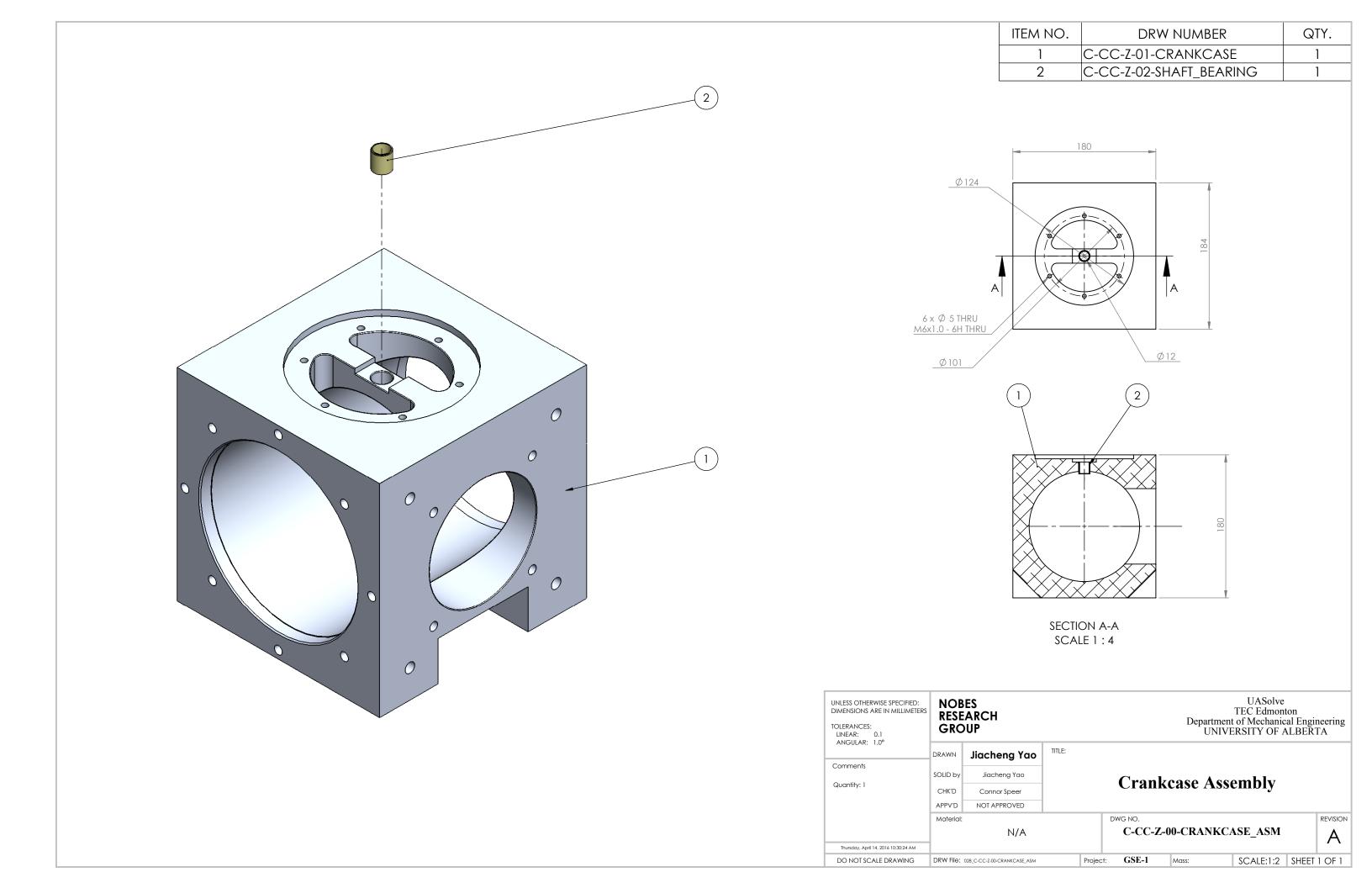


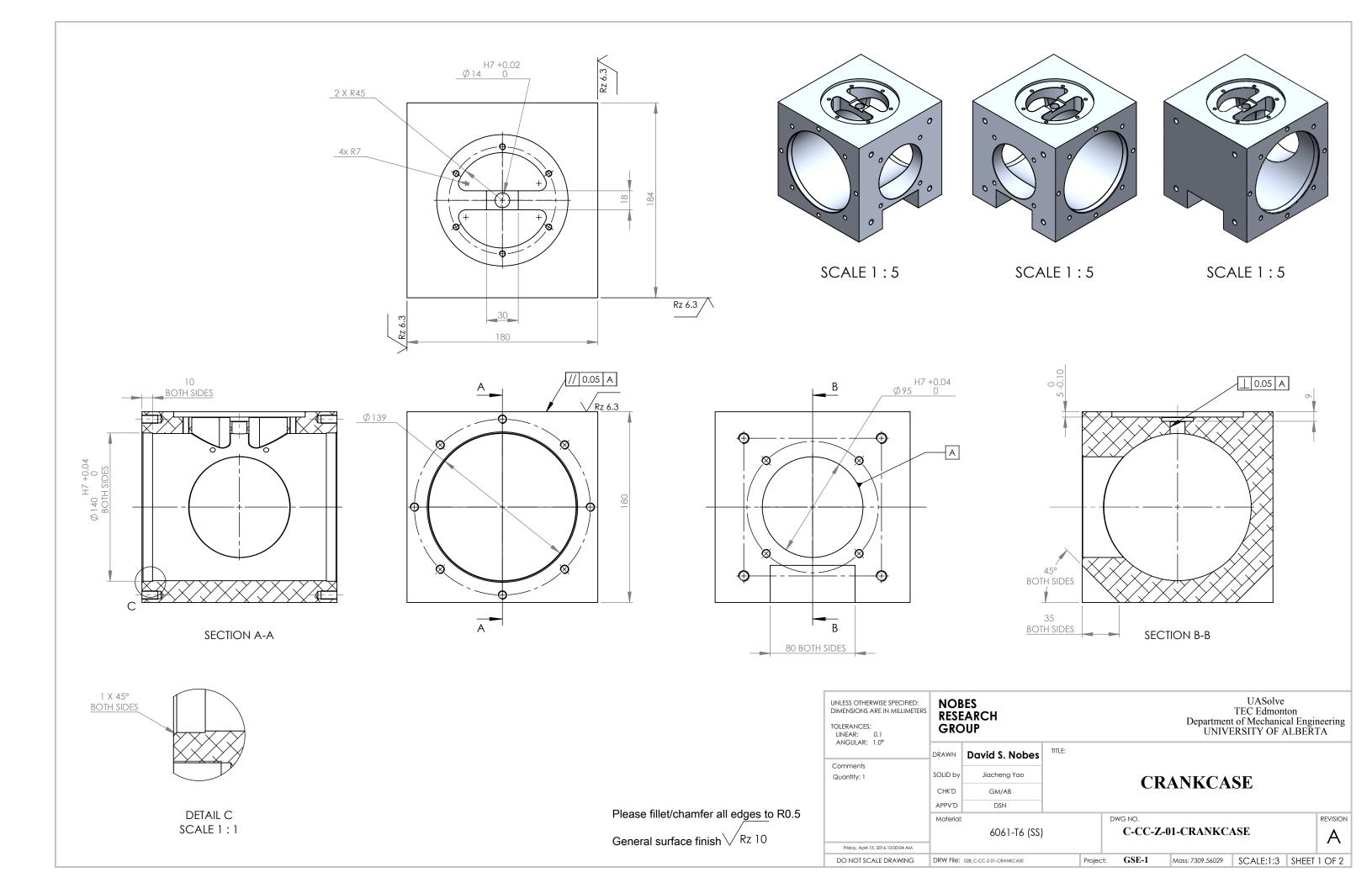
ng Yao	TITLE:								
g Yao	ROTARY SEAL HOLDER								
peer	KOTAKI SEAL HOLDEK								
OVED									
			DWG NO.				REVISION		
1-T6 (SS)			C-BC-Z-02-ROTARY_SEAL_HOLDER A						
ARY_SEAL_HOLDER Pr		Project:	GSE-1	Mass: 93.15171	SCALE:3:2	SHEET	1 OF 1		

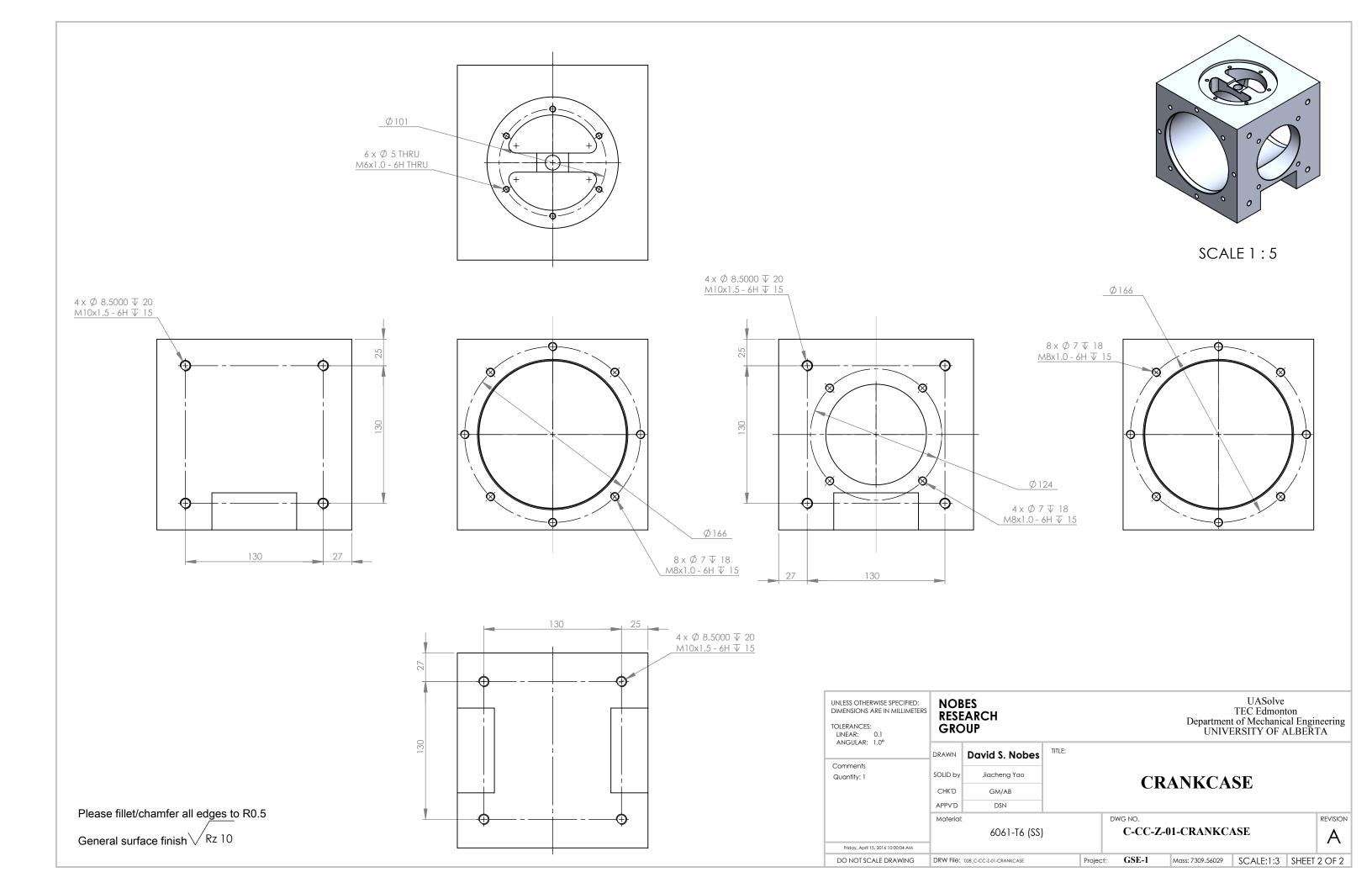
UASolve TEC Edmonton Department of Mechanical Engineering UNIVERSITY OF ALBERTA

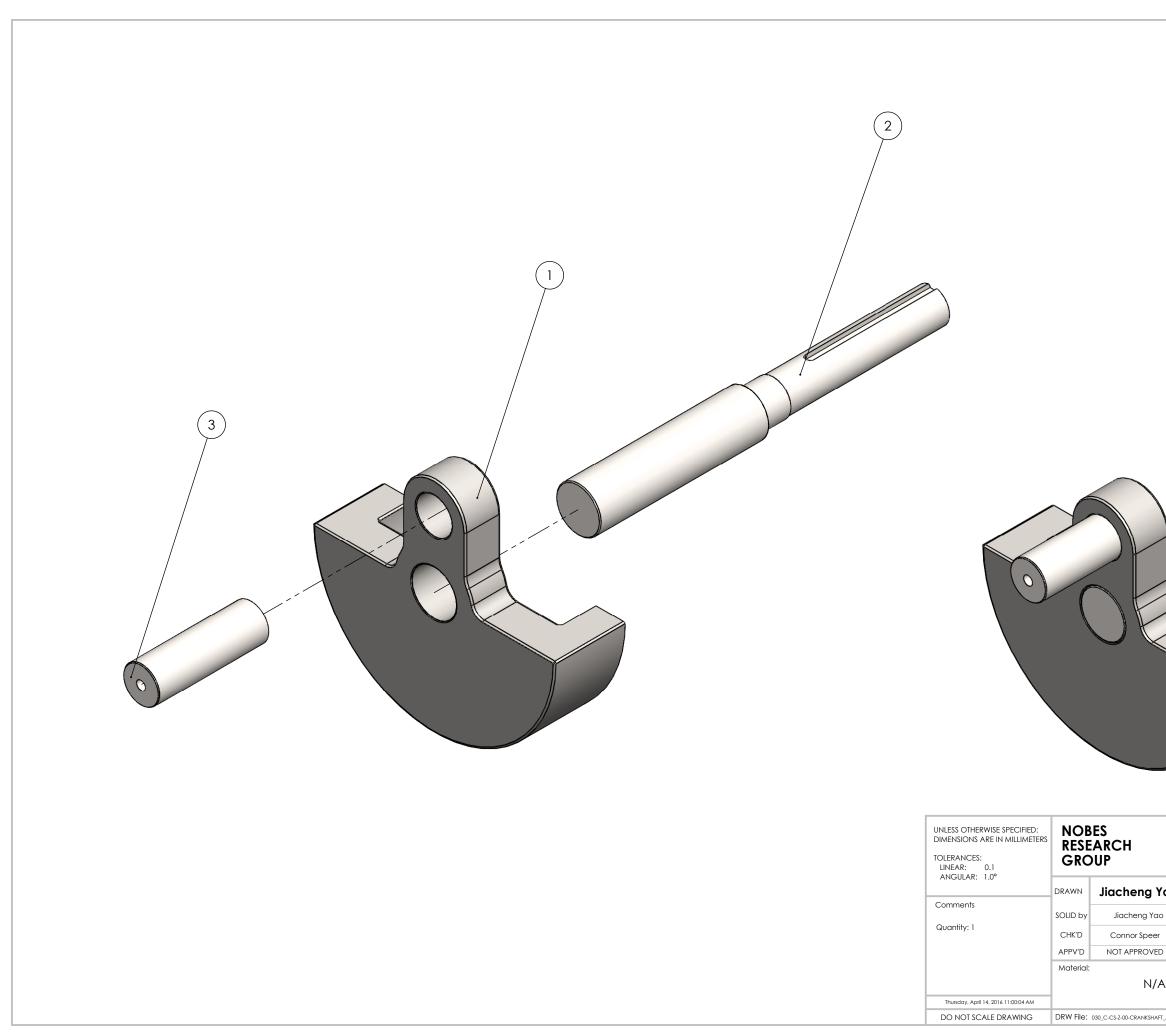


<u>2 X 45°</u>



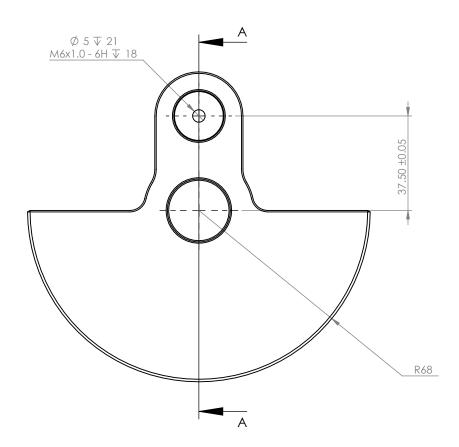


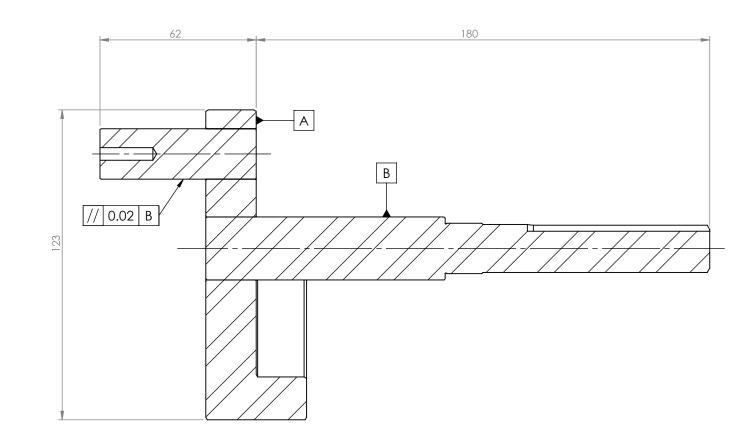




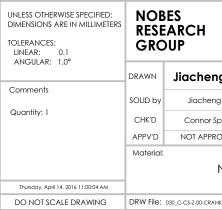
	ITEM N	O.	DR	W NUN	ABER		QTY.
	1	C	C-CS-Z-	03-CR/	ANKWE	В	1
	2	C	C-CS-Z-	01-SHA	\FT		1
	3	C	C-CS-Z-	02-PIV	TC		1
					UAS	monton	
				UNI	ent of Mech VERSITY	OF ALBE	RTA
Yao	TITLE:						
'ao er		Cra	anksh	aft As	semb	ly	
/ED		DWG NO.		CRANKS	SHAFT_A	ASM	revision A
AFT ASA4	Proioc	+ CSF	7-1	1001	SCALE	0.2 511	

					, , ,
_ASM	Project:	GSE-1	Mass:	SCALE:2:3	SHEET 1 OF 2

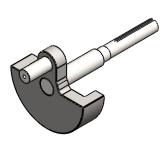




SECTION A-A

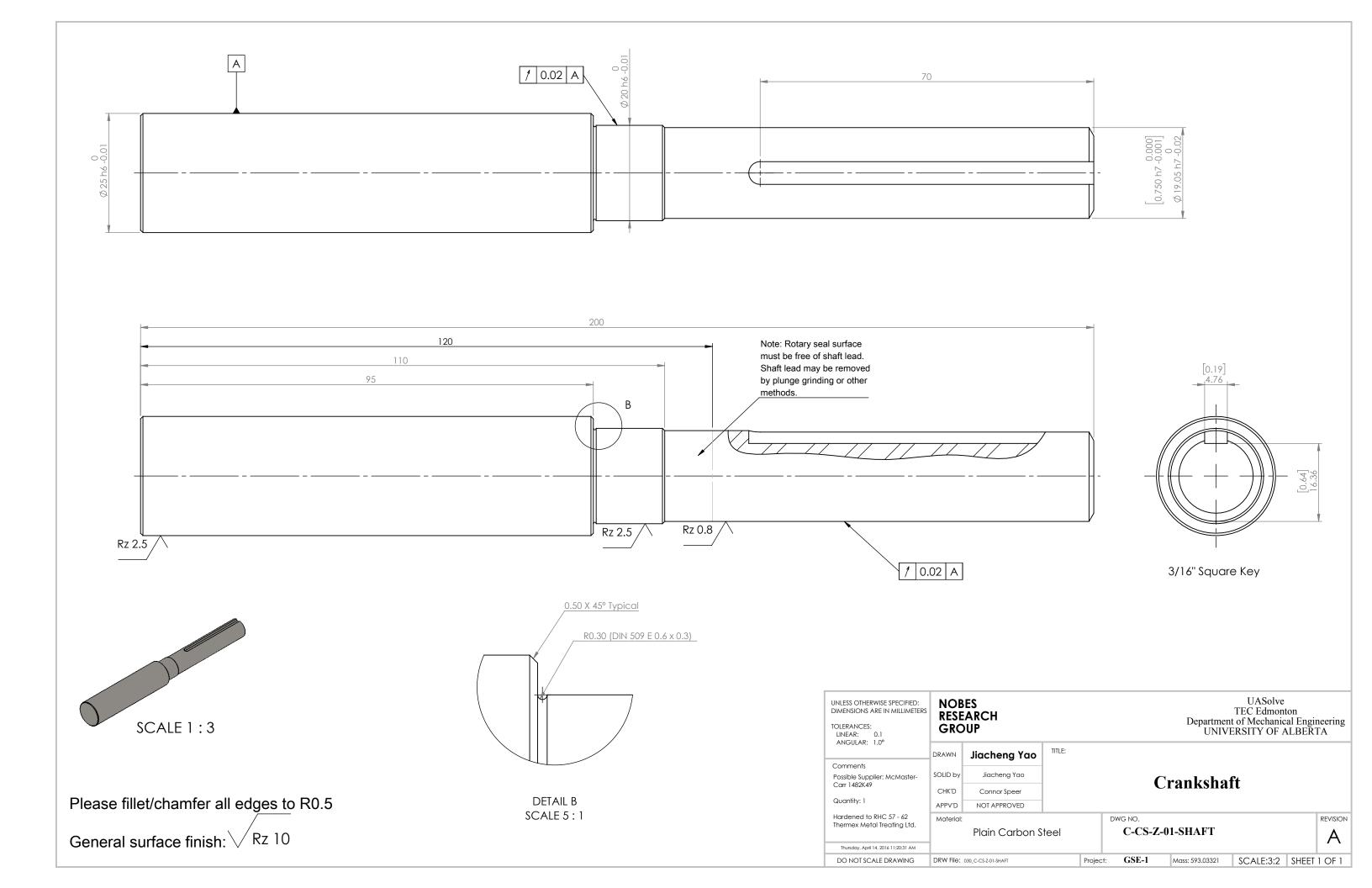


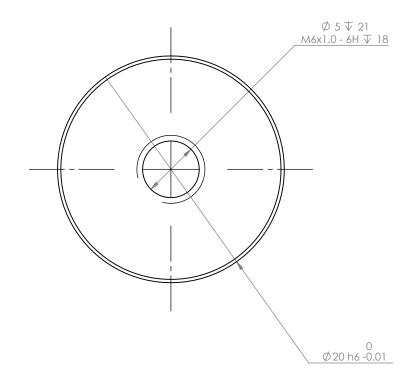
Interference fit: allowance 1/350 of diameter. Use deer tallow as a pressing aid.

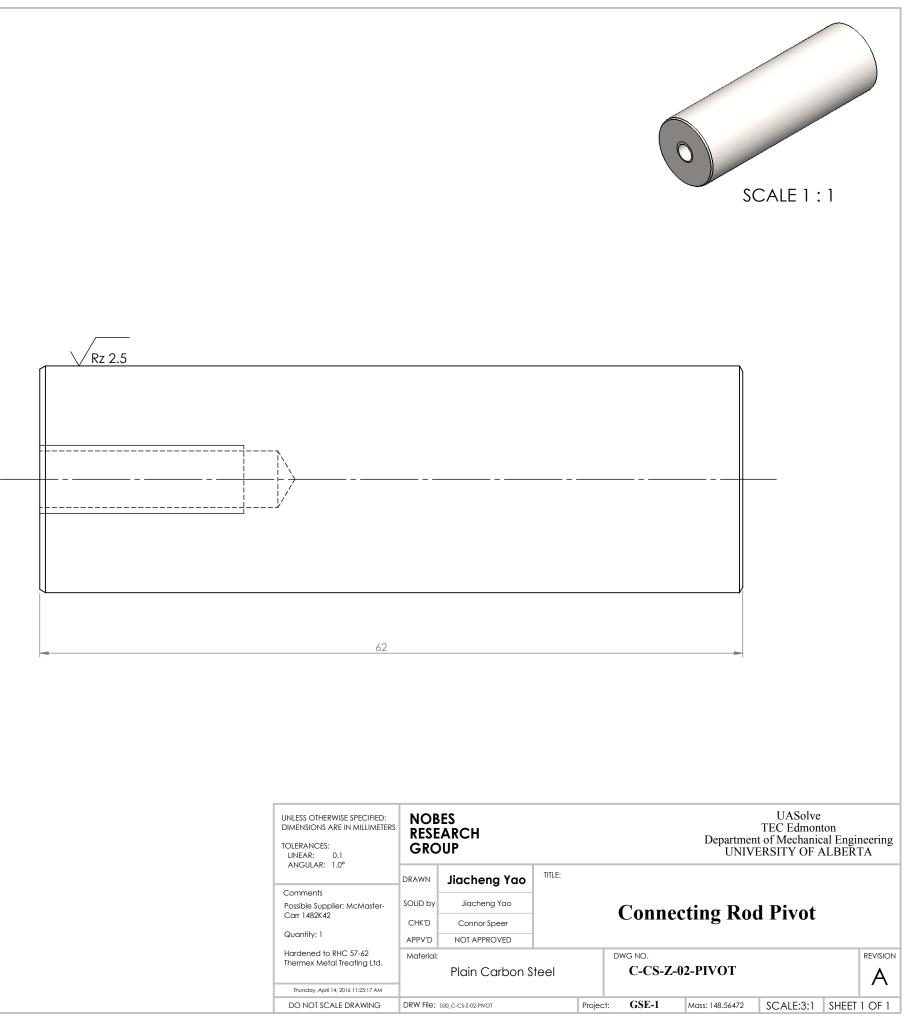


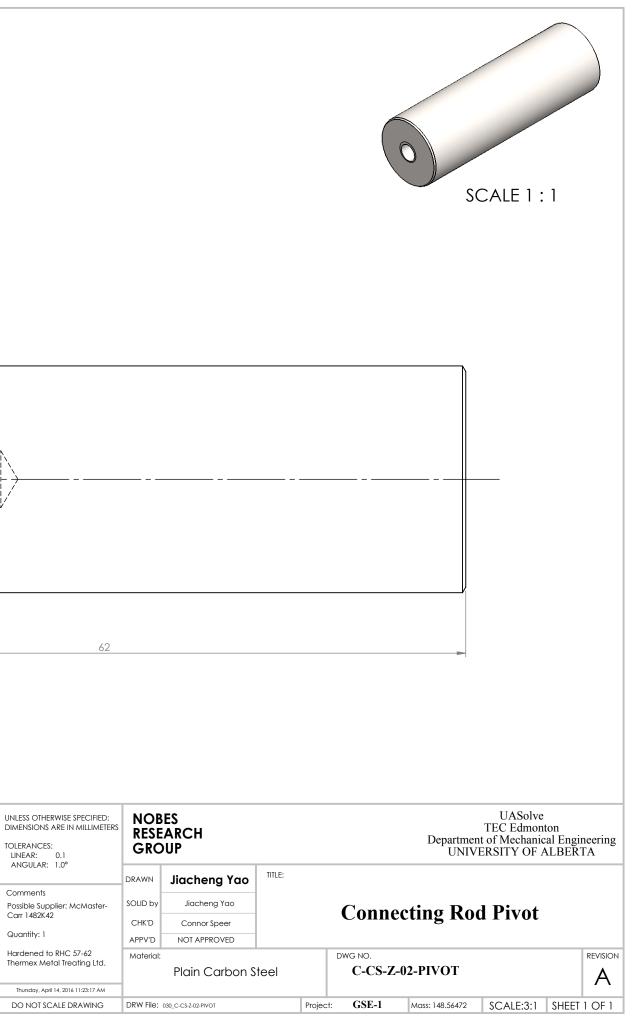
SCALE 1:5

g Yao	TITLE:						
y Yao			Crank	ahaft Acc	ombly		
beer			Clair	shaft Ass	emply		
DVED							
			DWG NO.				REVISION
N/A			C-CS-Z-	00-CRANKSE	IAFT_ASM		A
KSHAFT_ASM		Projec	t: GSE-1	Mass:	SCALE:2:3	SHEET	2 OF 2

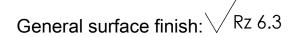


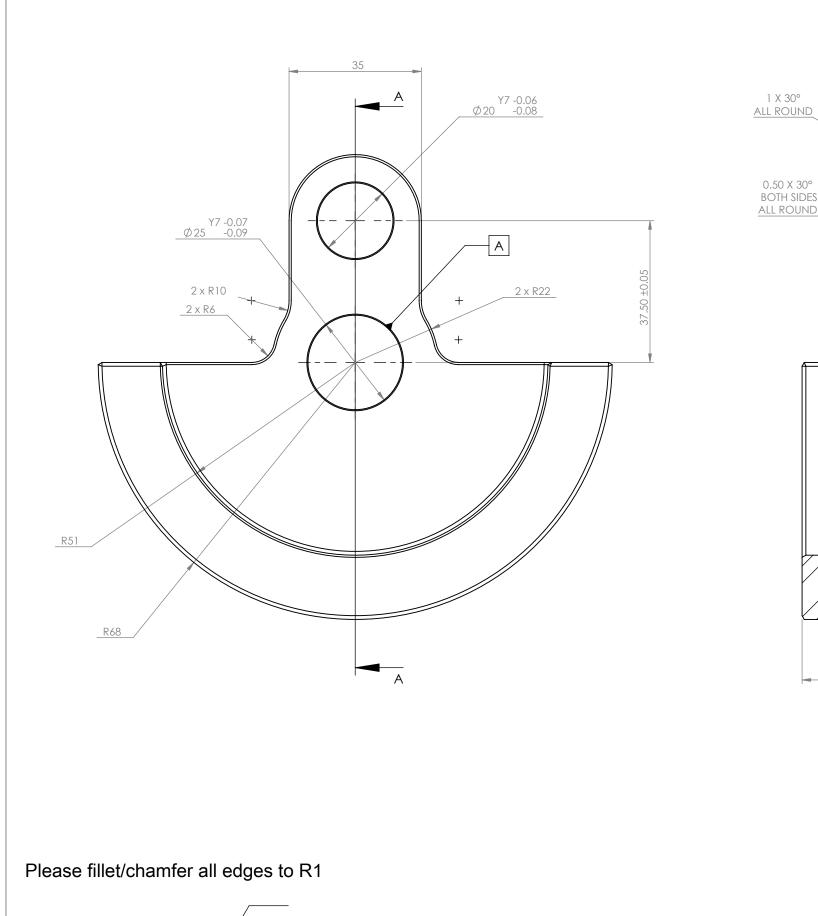


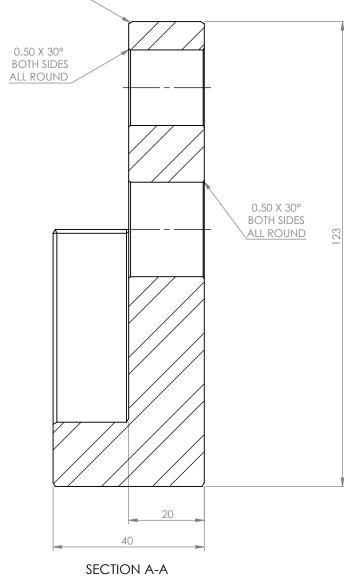




Please fillet/chamfer all edges to R0.5

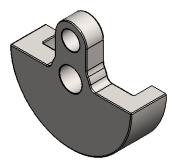




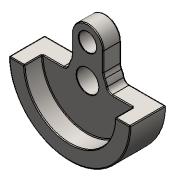


UNLESS OTHERWISE SPECIFIED: DIMENSIONS ARE IN MILLIMETERS TOLERANCES: LINEAR: 0.1 ANGIL AR: 1.0°	NOBES RESEARCH GROUP				
ANGULAR. 1.0	DRAWN	Jiacheng			
Comments Possible Supplier: McMaster- Carr 8910K102 Quantity: 1	SOLID by CHK'D APPV'D	Jiacheng N Connor Spe NOT APPRON			
Thursday, April 14, 2016 11:30:46 AM	Material:	AISI			
DO NOT SCALE DRAWING	DRW File:	030_C-CS-Z-03-CRANKW			

General surface finish: $\bigvee Rz \ 10$



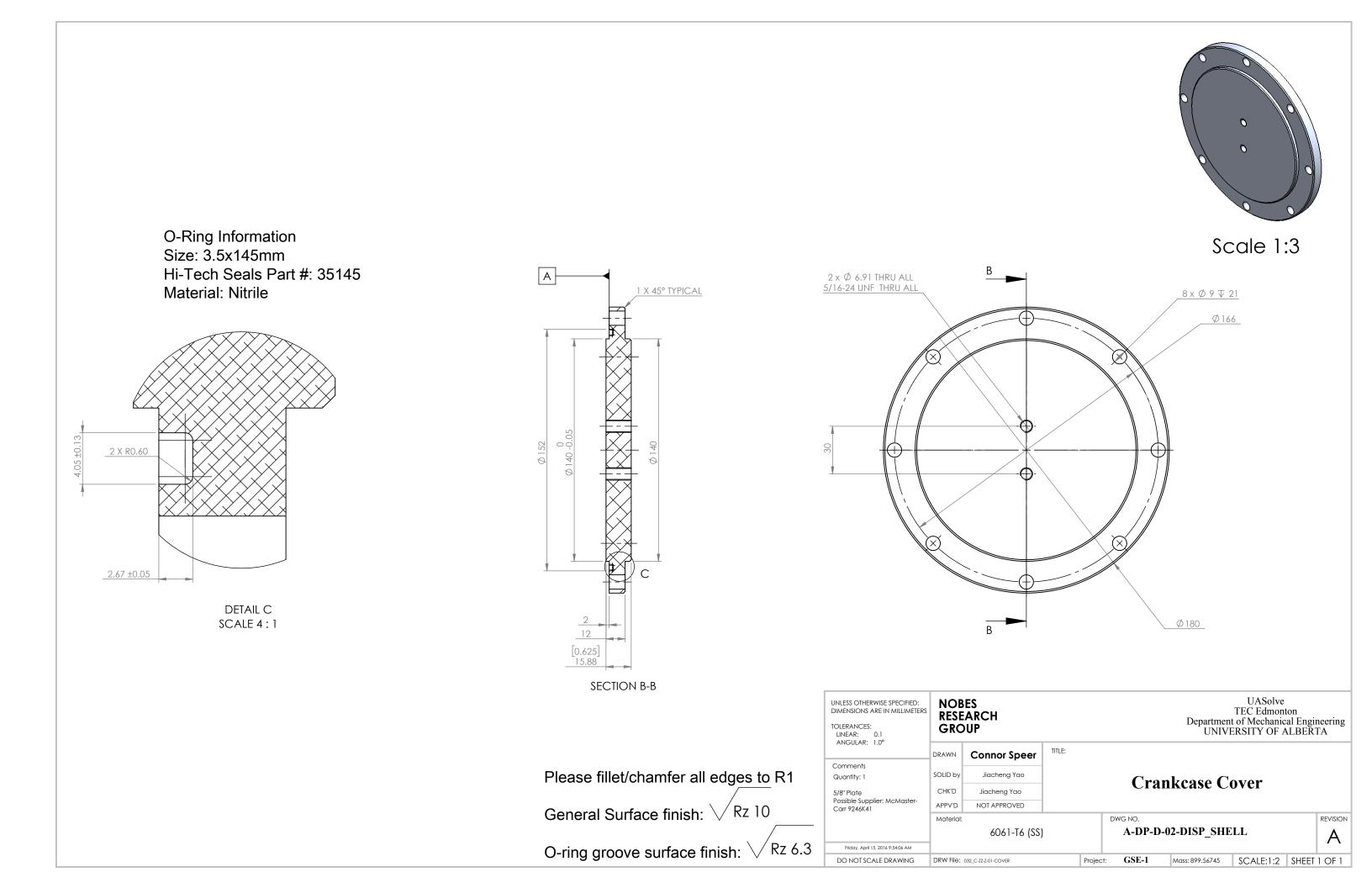
SCALE 1:3

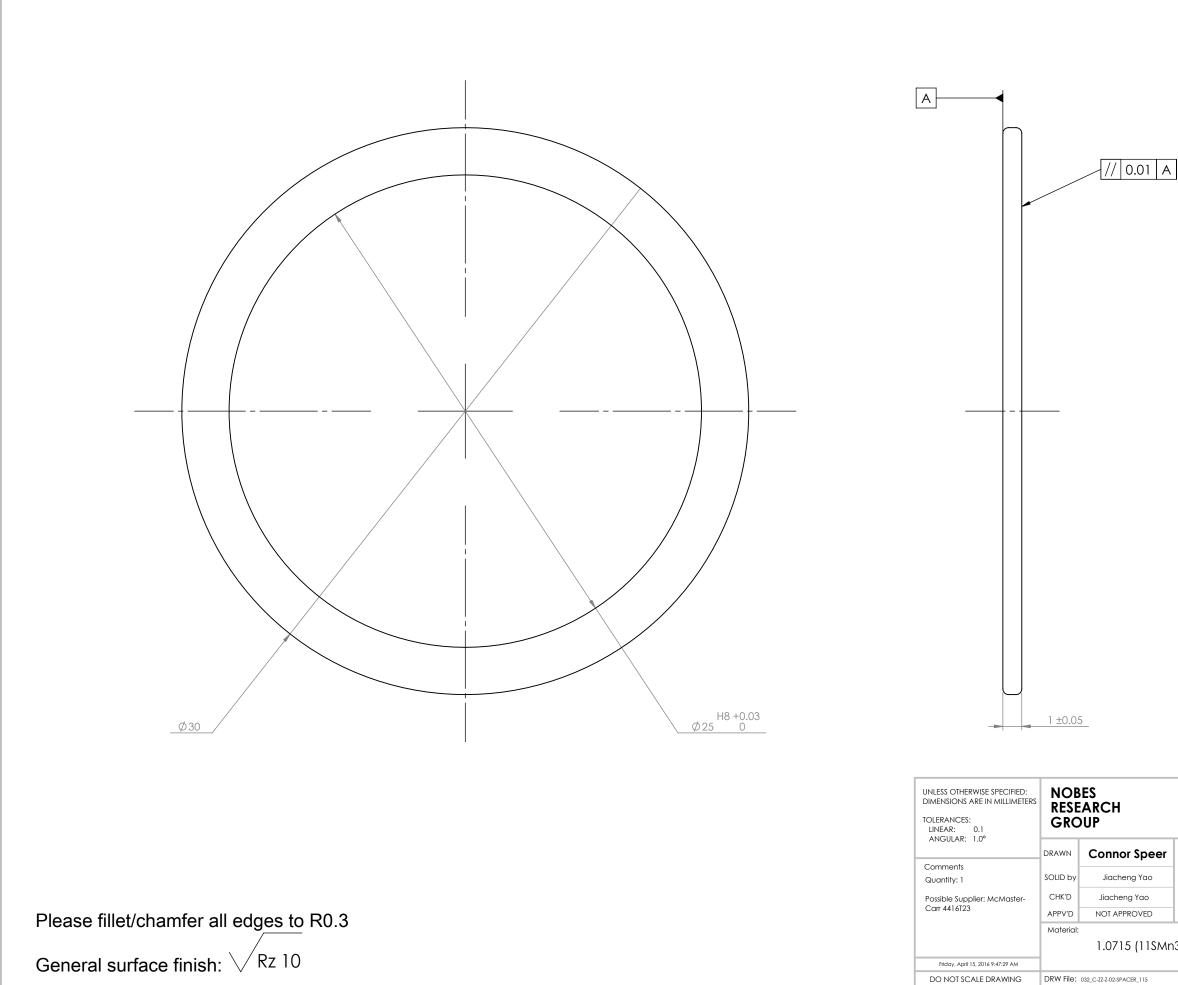


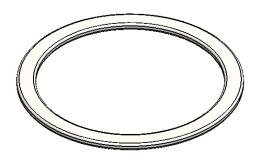
SCALE 1:3

g Yao	TITLE:						
y Yao			C	rank We	h		
beer			U		U		
OVED							
		DW	G NO.				REVISION
il 1020 C-CS-Z-03-CRANKWEB							А
KWEB	Proj	ect:	GSE-1	Mass: 1818.39287	SCALE:1:1	SHEET	1 OF 1

C Other Parts

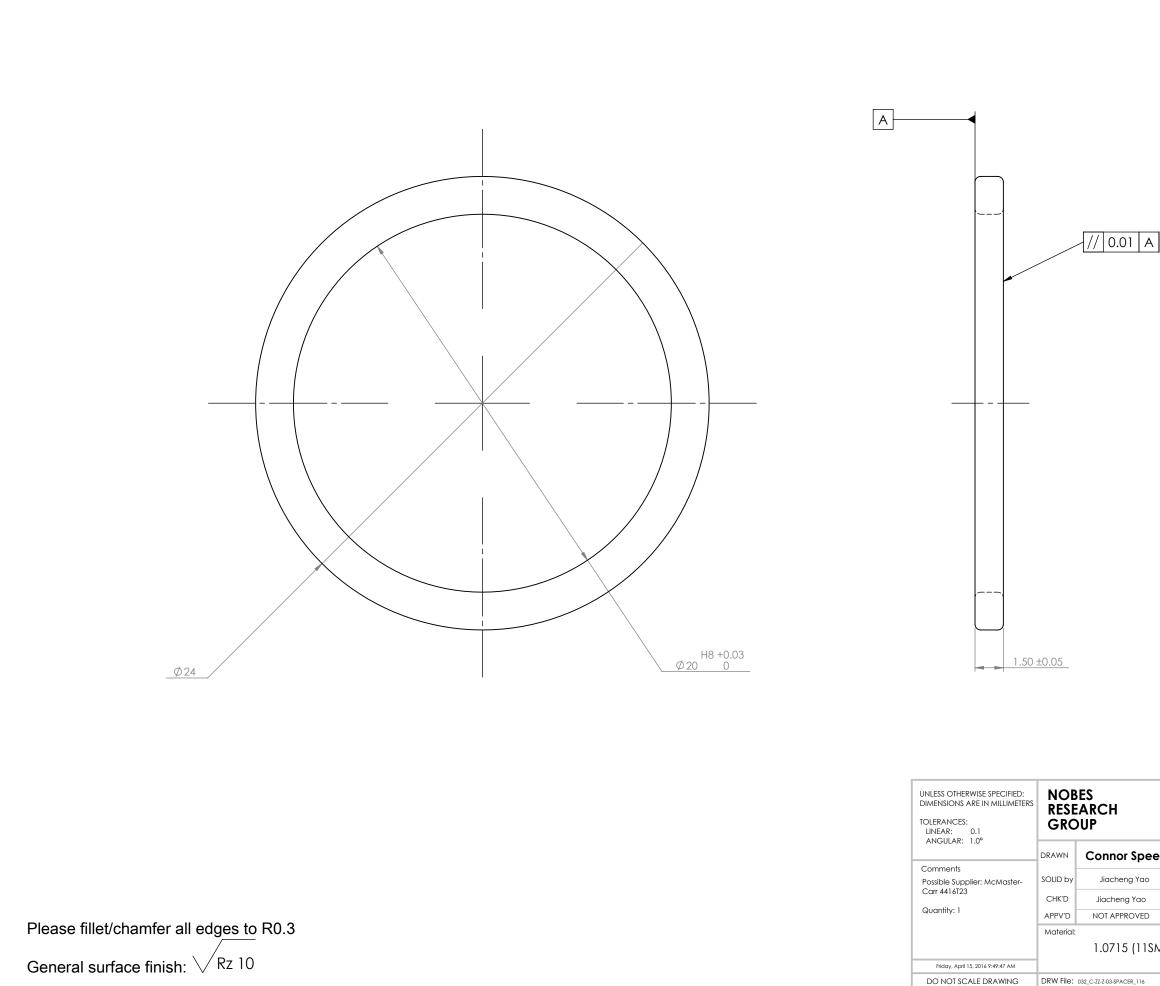






Scale 2:1

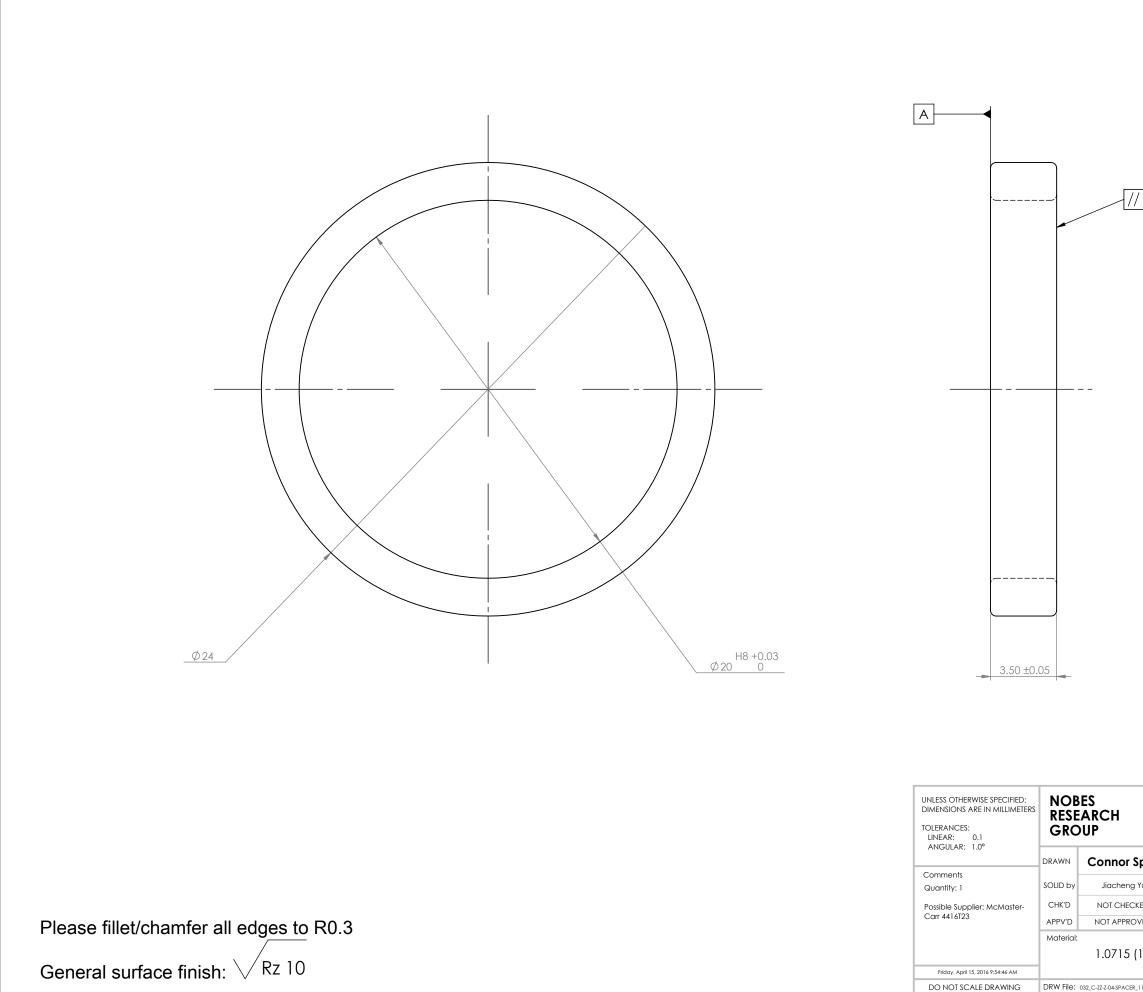
Speer	TITLE:										
g Yao			Cron	70	haft Sna	oor 115					
Yao		Crankshaft Spacer 115									
DVED											
(11SMn30)			DWG NO. C-ZZ-	-Z-0	2-SPACER_1	15		REVISION A			
R_115 Proje			t: GSE-1		Mass: 1.63262	SCALE:5:1	SHEET	1 OF 1			





Scale 2:1

Speer	TITLE:										
g Yao			C	onkal	naft Snad	oor 116					
Yao		Crankshaft Spacer 116									
DVED											
(11SMn	30)		DWG NO. C-ZZ-Z-03-SPACER_116					REVISION			
R_116		Projec	at: C	GSE-1	Mass: 1.57564	SCALE:5:1	SHEET	1 OF 1			

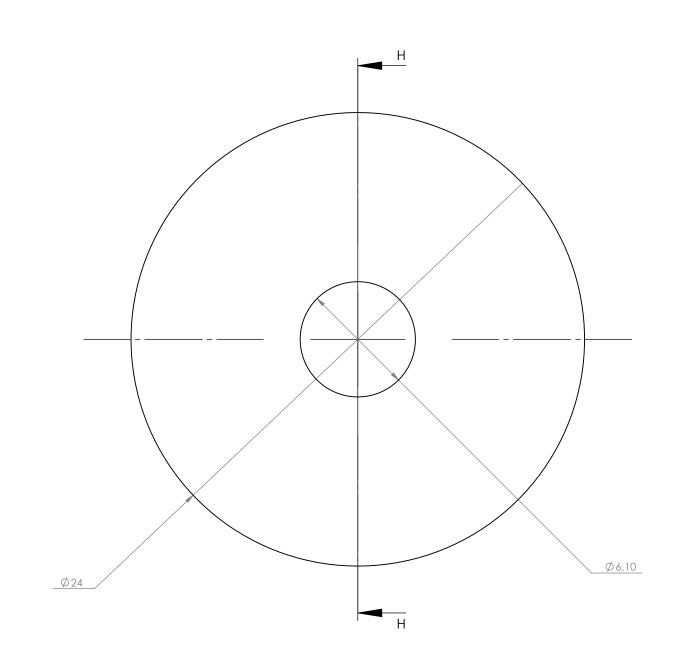




Scale 2:1

// 0.01 A

Speer	TITLE:										
g Yao			Cronk	shaft Sna	oor 117						
CKED		Crankshaft Spacer 117									
OVED											
(11SMn	30)		DWG NO. C-ZZ-Z-04-SPACER_117				REVISION				
R_117		Projec	t: GSE-1	Mass: 3.73203	SCALE:5:1	SHEET	1 OF 1				



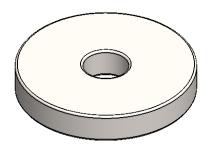


SECTION H-H

UNLESS OTHERWISE SPECIFIED: DIMENSIONS ARE IN MILLIMETERS TOLERANCES: LINEAR: 0.1	S NOBES RESEARCH GROUP				UASolve TEC Edmonton Department of Mechanical Engineering UNIVERSITY OF ALBERTA				
ANGULAR: 1.0°	DRAWN	Connor Speer	TITLE:						
Comments Quantity: 1	SOLID by	Jiacheng Yao			(Snacor 11	Q		
Possible Supplier: McMaster-	CHK'D	NOT CHECKED			r r	Spacer 11	0		
Carr 4416T23	APPV'D	NOT APPROVED							
	Material:		-	C	WG NO.			REVISI	
		1.0715 (11SMn30)			C-ZZ-05-SPACER_118				
Friday, April 15, 2016 9:51:17 AM									
do not scale drawing	DRW File:	032_C-ZZ-Z-05-SPACER_118		Project:	GSE-1	Mass: 13.17425	SCALE:5:1	SHEET 1 OF	

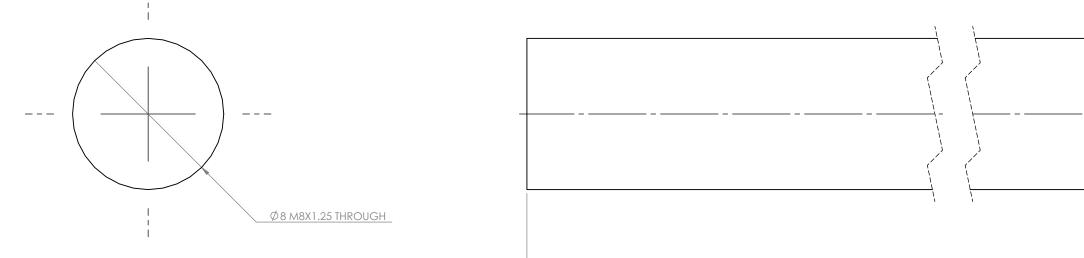
Please fillet/chamfer all edges to R0.3

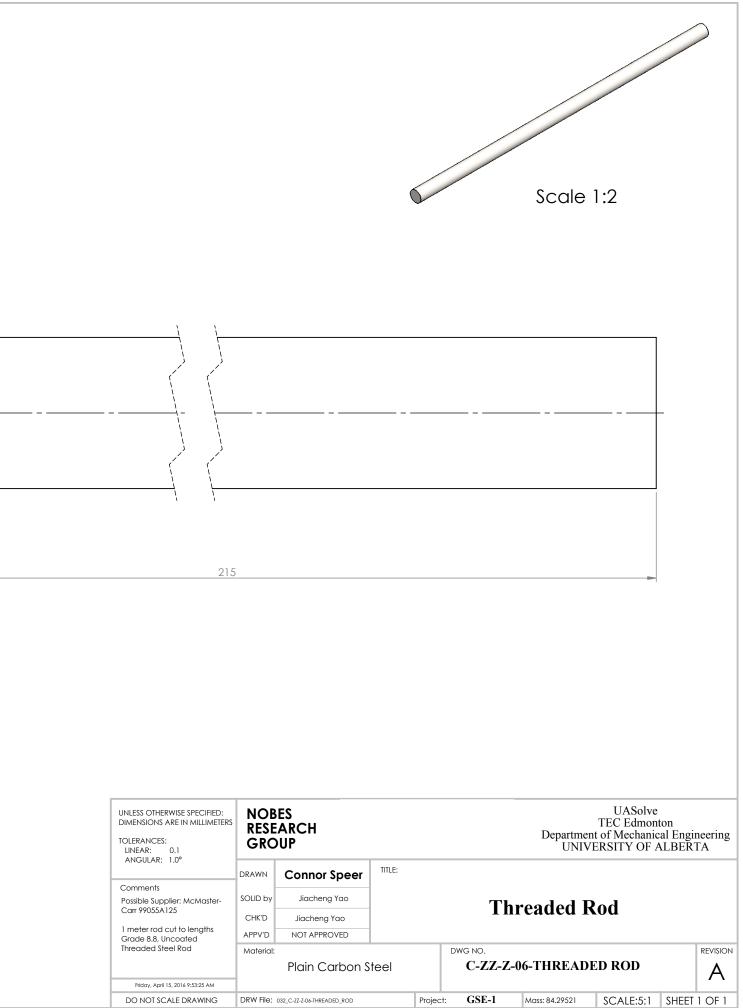
General surface finish: \bigvee Rz 10



Scale 2:1

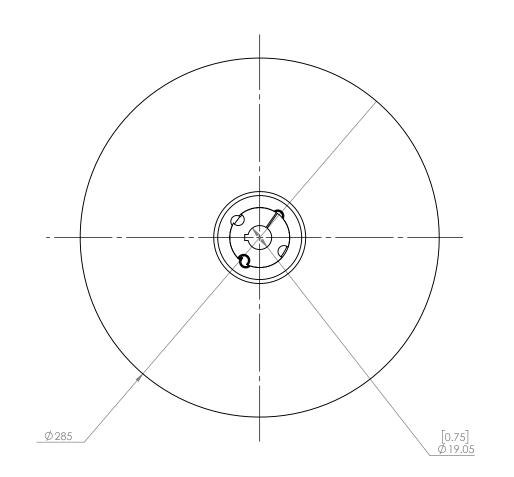


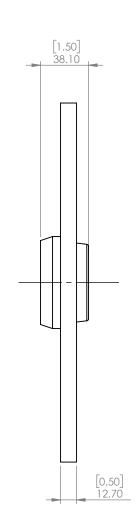


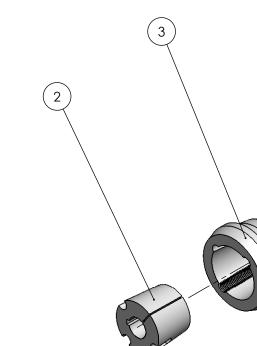


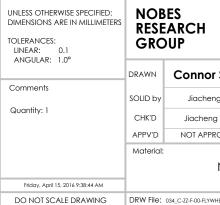
Quantity: 4 Threaded Rods

ITEM NO. 1 2 3



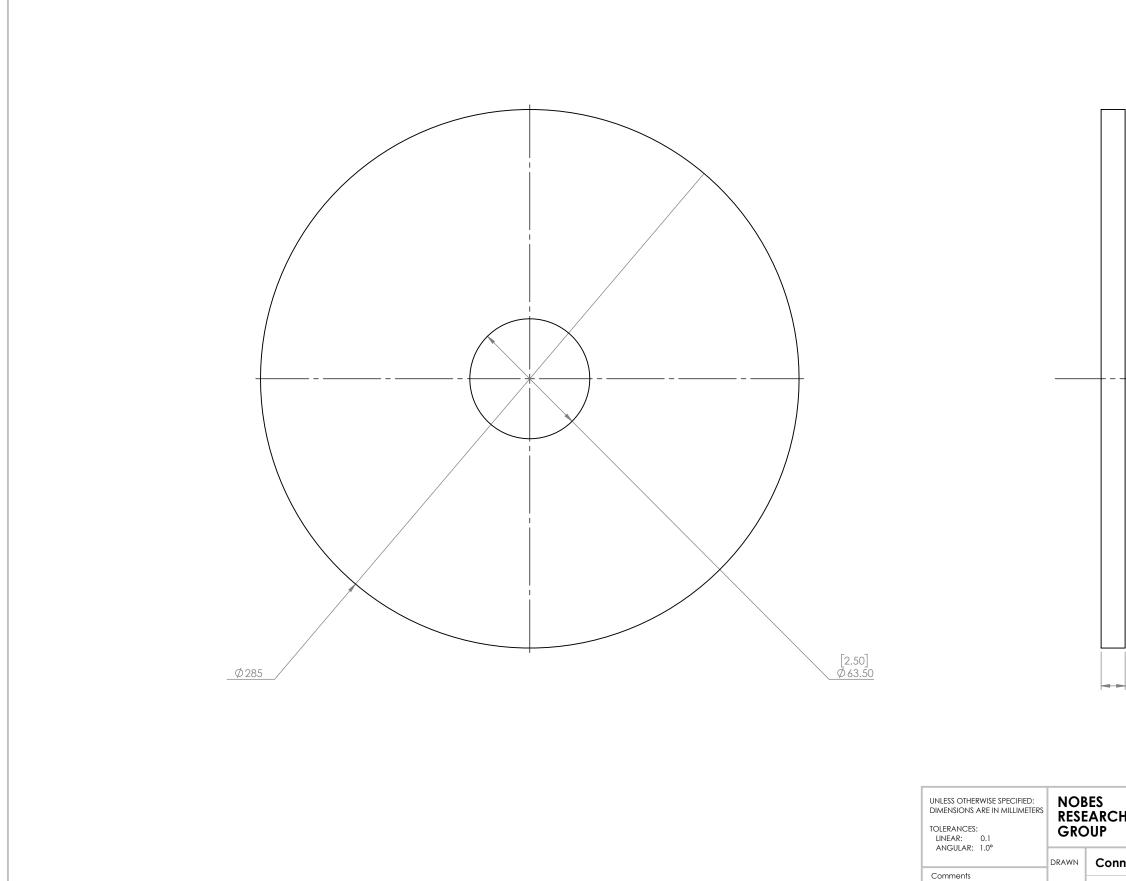




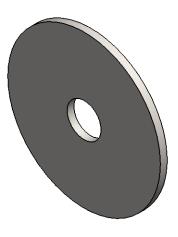


Note: Dynamic balancing after assembly is recommended.

]		D	RW NUM	BER		Q	ΓY.
		С	-ZZ-F-01-C	DISC			1
	C-ZZ	-F-02-T	APER_LO	CK_BUSHII	٧G		1
	C-ZZ-F-03	B-WELD	ON_BUS	HING_BO	RE_HUB		1
					UASolve TEC Edmon	ton	
				UNIV	t of Mechanic ERSITY OF A	ALBER	ГА
r	Speer TITLE:						
n	g Yao		Flvwk	neel Asse	mhlv		
			1°19 WI	1001 (1330	11101y		
	oved N/A		DWG NO. C-ZZ-F-()	00-FLYWHEI	EL_ASM		REVISION
WH	HEEL_ASM	Project:	GSE-1	Mass:	SCALE:1:3	SHEET	1 OF 1



DIMENSIONS ARE IN MILLIMETERS TOLERANCES: LINEAR: 0.1 ANGULAR: 1.0°	RESEARCH GROUP				Department of Mechanical Engineering UNIVERSITY OF ALBERTA				
ANOULAR. 1.0	DRAWN	Connor Speer	TITLE:						
Comments		•							
	SOLID by	Jiacheng Yao			TI.	wheel D	alt		
Quantity: 1	CHK'D	Jiacheng Yao	Flywheel Disk						
	APPV'D	NOT APPROVED							
	Material:				DWG NO.		REVISION		
		AISI 1020			C-ZZ-F-01-DISC				A
Friday, April 15, 2016 9:33:52 AM									· ·
DO NOT SCALE DRAWING	DRW File:	034_C-ZZ-F-01-DISC		Projec	t: GSE-1	Mass: 6082.71133	SCALE:1:2	SHEET	1 OF 1



Scale 1:5

[0.50] 12.70

UASolve