

Predicting Survival, Reproduction and Abundance of Polar Bears under Climate Change

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1 **Abstract:** Polar bear (*Ursus maritimus*) populations are predicted to be negatively affected
2 by climate warming, but the timeframe and manner in which change to polar bear
3 populations will occur remains unclear. Predictions incorporating climate change effects are
4 necessary for proactive population management, the setting of optimal harvest quotas, and
5 conservation status decisions. Such predictions are difficult to obtain from historic data
6 directly because past and predicted environmental conditions differ substantially. Here, we
7 explore how models can be used to predict polar bear population responses under climate
8 change. We suggest the development of mechanistic models aimed at predicting reproduction
9 and survival as a function of the environment. Such models can often be developed,
10 parameterized, and tested under current environmental conditions. Model predictions for
11 reproduction and survival under future conditions could then be input into demographic
12 projection models to improve abundance predictions under climate change. We illustrate the
13 approach using two examples. First, using an individual-based dynamic energy budget model,
14 we estimate that 3% to 6% of adult males in western Hudson Bay would die of starvation
15 before the end of a 120 day summer fasting period but 28% to 48% would die if climate
16 warming increases the fasting period to 180 days. Expected changes in survival are nonlinear
17 (sigmoid) as a function of fasting period length. Second, we use an encounter rate model to
18 predict changes in female mating probability under sea ice area declines and declines in
19 mate-searching efficiency due to habitat fragmentation. The model predicts that mating
20 success will decline non-linearly if searching efficiency declines faster than habitat area, and
21 increase non-linearly otherwise. Specifically for the Lancaster Sound population, we predict
22 that female mating success would decline from 99% to 91% if searching efficiency declined
23 twice as fast as sea ice area, and to 72% if searching efficiency declined four times as fast as

24 area. Sea ice is a complex and dynamic habitat that is rapidly changing. Failure to
25 incorporate climate change effects into population projections can result in flawed
26 conservation assessments and management decisions.

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29 **Key words:** climate change, dynamic energy budgets, *Ursus maritimus*, population viability
30 analysis, starvation, mechanistic models

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47 **1. Introduction**

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49 Climate change effects on species and ecosystems have been identified as critical problems
50 for conservation biology (McCarty, 2001; Mawdsley et al., 2009). Describing, understanding,
51 and anticipating these effects are precursors to identifying mitigation strategies (Harley et al.,
52 2006; Root and Schneider, 2006). Anticipation can be particularly challenging and requires a
53 combination of good quantitative data along with precise hypotheses on the mechanisms by
54 which climate change will affect a species (Ådahl et al., 2006; Krebs and Berteaux, 2006).
55 Mathematical models can be a powerful tool in this process, and they can inform research,
56 monitoring, and conservation planning by indicating where and how change in a population
57 is most likely to occur. The type of projection model that can be applied depends to a large
58 degree on how similar predicted environmental conditions are to the ones observed. Berteaux
59 et al. (2006) discuss constraints to projecting the ecological effects of climate change, and
60 they suggest a distinction between forecast and prediction models. Forecast models are based
61 on correlational relationships between explanatory and dependent variables (e.g.,
62 environmental conditions and vital rates) and are useful if there is no extrapolation beyond
63 the observed range of explanatory variables. In contrast, predictive models mechanistically
64 describe the cause-effect relationships determining change (e.g., the link between
65 environmental conditions and vital rates via energetic constraints), and can be used beyond
66 the observed ranges.

67 The Arctic is warming faster than many other areas (IPCC, 2007), and habitat
68 alteration is well underway. One Arctic habitat showing profound effects is the sea ice, with
69 the perennial and annual ice cover shrinking, and sea ice thickness decreasing (Comiso,

70 2002; Maslanik et al., 2007; Comiso et al., 2008). The sea ice is declining at rates faster than
71 expected (Stroeve et al., 2007), and declines are projected to accelerate (Holland et al., 2006;
72 Serreze et al., 2007). Variability in predictive sea ice models exist but it is possible that the
73 Arctic Ocean will be ice-free in summer by the middle to the end of the 21st century
74 (Holland et al., 2006; Zhang and Walsh, 2006; Serreze et al., 2007; Boé et al., 2009). Among
75 the most vulnerable to these warming trends are ice-obligate species, such as polar bear
76 (*Ursus maritimus*), walrus (*Odobenus rosmarus*), bearded seal (*Erignathus barbatus*), and
77 ringed seal (*Pusa hispida*) (Laidre et al., 2008; Moore and Huntington, 2008). Polar bears in
78 particular have become the subject of intense political debate, and public interest in the future
79 of the species is increasing (e.g., Charles, 2008). The vulnerability of polar bears to climate
80 warming is clear (e.g., Stirling and Derocher, 1993; Derocher et al., 2004; Stirling and
81 Parkinson, 2006; Laidre et al., 2008; Wiig et al., 2008), but few predictions exist to address
82 how polar bear abundance might change numerically in response to a warming climate
83 (Amstrup et al., 2007; Hunter et al., 2007).

84 Prediction of polar bear population dynamics under climate change is challenging,
85 because observed and predicted environmental conditions differ substantially (Wiig et al.,
86 2008). Consequently, few data exist to inform us how reproduction and survival (and thus
87 population abundance) might change under future conditions. To date, only two studies have
88 incorporated climate change trends into quantitative projections of polar bear abundance
89 (Amstrup et al., 2007; Hunter et al., 2007), and each of these studies had to rely on some
90 form of extrapolation or expert judgment to parameterize suggested population models due to
91 the lack of data relating present to future conditions. These analyses are important steps, and
92 they provide new hypotheses on how populations may respond to further warming. However,

93 their projections may lack accuracy if unexpected non-linearities exist in vital rate response
94 curves to future environmental conditions.

95 Here, we follow the framework of Berteaux et al. (2006) to suggest how predictions
96 of population abundance under climate change could be improved. For this purpose, we first
97 review expected and observed climate change effects on polar bears with specific focus on
98 the biological mechanisms affecting survival and reproduction. We then summarize previous
99 attempts to forecast polar bear abundance under climate change and discuss limitations of
100 these studies. To improve predictions of population abundance, we suggest the development
101 of mechanistic models aimed at predicting reproduction and survival as a function of the
102 environment. Such predictions could inform demographic projection models to improve
103 population viability analyses (PVA) under climate change. We illustrate the approach with
104 two examples: a dynamic energy budget (DEB) model to predict changes in survival due to
105 prolonged summer fasts, and an encounter rate model to predict changes in female mating
106 success due to climate change induced habitat fragmentation and sea ice area declines. To aid
107 further development of such mechanistic models, we discuss data collection needs to
108 augment ongoing monitoring projects.

109

110 **2. Climate Change Threats to Polar Bears**

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112 Polar bears are vulnerable to climate warming primarily because they depend on sea ice as a
113 platform to access their main prey, ringed seals and bearded seals (Stirling and Archibald,
114 1977; Smith, 1980). Other marine mammals may locally complement the diet, but in general
115 all marine prey is expected to become less accessible to polar bears as the sea ice declines.

116 Terrestrial food sources may be opportunistically exploited but are unlikely to substitute for
117 the high energy diet polar bears obtain from seals (Derocher et al., 2004; Wiig et al., 2008;
118 Hobson et al., 2009; Molnár 2009). The sea ice is also used in other aspects of polar bear life
119 history, including traveling and mating (Ramsay and Stirling, 1986; Stirling et al., 1993).
120 With rising temperatures, areas of open water and ice floe drift rates are expected to increase,
121 and traveling in such a fragmented and dynamic sea ice habitat would become energetically
122 more expensive because polar bears would have to walk or swim increasing distances to
123 maintain contact with preferred habitats (Mauritzen et al., 2003).

124 The combined effects of decreasing food availability and increasing energetic
125 demands are predicted to result in decreasing polar bear body condition and a consequent
126 cascade of demographic effects (Stirling and Derocher, 1993; Derocher et al., 2004; Wiig et
127 al., 2008). Pregnant females, for instance, give birth in maternity dens, when food is
128 unavailable for 4-8 months (Atkinson and Ramsay, 1995). To meet the energetic demands of
129 survival, gestation, and early lactation, females need to accumulate sufficient energy stores
130 before denning. The lightest female observed to produce viable offspring weighed 189 kg at
131 den entry (Derocher et al., 1992), and the proportion of females below such a reproduction
132 threshold will increase with ongoing food stress (Molnár, 2009). Females above the threshold
133 may reproduce, but their reproductive success would still decline with reduced body
134 condition, because body condition is positively correlated with litter size and litter mass,
135 where the latter is also positively correlated with cub survival (Derocher and Stirling, 1996,
136 1998). After den exit, cubs are nursed for about 2.5 years, but maternal food stress may
137 reduce milk production, with negative consequences for cub growth and cub survival
138 (Derocher et al., 1993; Arnould and Ramsay, 1994). Adult survival rates, in contrast, are

139 probably only affected under more severe conditions because polar bears can survive
140 extended periods without feeding (Atkinson and Ramsay, 1995). Subadult mortality,
141 however, may increase before adult survival is affected, because young bears are less
142 proficient in finding food (Stirling and Latour, 1978) and thus more vulnerable to adverse
143 conditions. Such negative changes in reproduction and survival could lead to decreased
144 population growth rates or population declines.

145 There is evidence that some of these predicted changes are underway. For example,
146 polar bears in the Western Hudson Bay population (Fig. 1) have shown declines in body
147 condition, reproductive success, survival, and population abundance, and these declines are
148 thought to result from increasing food stress associated with prolonged open-water fasting
149 periods (Derocher and Stirling, 1995; Stirling et al., 1999; Regehr et al., 2007). Appropriate
150 time series to detect changes in body condition, reproduction, and survival do not exist for
151 most other populations (but see Regehr et al., 2010). However, food stress has been
152 documented for polar bears in the Beaufort Sea (Fig. 1) (Cherry et al., 2009), and recent
153 incidents of cannibalism and an increased presence of polar bears near human settlements
154 may provide further indicators for food stress in various populations (Amstrup et al., 2006;
155 Stirling and Parkinson, 2006; Towns et al., 2009).

156 Changes in energy availability and consequent demographic effects constitute the
157 biggest concern for polar bears under climate warming. However, energy-independent or
158 only partially energy-related effects of climate warming are also possible, such as increased
159 exposure and vulnerability to pollutants, the emergence of new diseases, loss of denning
160 habitat, and conflict with humans associated with industrial development. For reviews of

161 climate warming effects on polar bears, see Stirling and Derocher (1993), Derocher et al.
162 (2004) and Wiig et al. (2008).

163

164 **3. Towards an Understanding of the Future of Polar Bears**

165

166 Qualitative predictions regarding the future of polar bears under changing environmental
167 conditions abound (e.g., Stirling and Derocher, 1993; Derocher et al., 2004; Rosing-Asvid,
168 2006; Stirling and Parkinson, 2006; Moore and Huntington, 2008; Wiig et al., 2008), and
169 some of these predictions were outlined above. Such assessments are useful to identify
170 threats and to provide insights into complex interactions between ecological dynamics,
171 environmental variables, and anthropogenic influences, but they cannot provide quantitative
172 information on the manner and timeframe in which polar bear populations will be affected.
173 However, sound quantitative projections of population abundances are necessary to correctly
174 assess conservation status, to proactively direct conservation efforts, and to set sustainable
175 harvest quotas (Coulson et al., 2001; Mace et al., 2008).

176 Currently, most projections of polar bear population abundance are accomplished
177 using RISKMAN, a population simulation model that accounts for the three-year
178 reproductive cycle of female polar bears (Taylor et al., 2002). In its basic components, the
179 program is equivalent to a stage-structured matrix population model with parental care, such
180 as the one developed by Hunter et al. (2007; illustrated in Fig. 2). RISKMAN has been used
181 to determine harvest quotas (e.g., Taylor et al., 2002) and to assess polar bear conservation
182 status in Canada (COSEWIC, 2008). Model parameters in these studies were based on recent
183 mean estimates of reproduction and survival, and potential future changes in these

184 demographic parameters due to climate change were not considered. However, our
185 understanding of polar bear life history and ecology implies that such changes are likely.

186 Quantitative predictions of population dynamics under environmental change must
187 account for potential changes in reproduction and survival to be meaningful (Beissinger and
188 Westphal, 1998; Coulson et al., 2001), and are therefore possible if (a) predictions for future
189 environmental conditions exist, (b) the relationship between future conditions and
190 demographic parameters can be quantified, and (c) a population model integrating these
191 effects can be developed (Jenouvrier et al., 2009). In some species, such as Emperor
192 Penguins (*Aptenodytes forsteri*), a population viability approach incorporating these three
193 steps was possible because reproduction and survival data exist for environmental conditions
194 similar to those predicted to occur (Jenouvrier et al., 2009). For polar bears, the approach is
195 difficult because few data exist to inform us how demographic parameters might change in
196 the future. The only studies to attempt quantitative predictions of polar bear abundance under
197 climate change were consequently limited by the need to extrapolate from present conditions
198 (Amstrup et al., 2007; Hunter et al., 2007) and the reliance on expert judgment (Amstrup et
199 al., 2007) when parameterizing proposed population models.

200 Hunter et al. (2007) coupled general circulation models with matrix population
201 models (Fig. 2) to obtain population size projections for the southern Beaufort Sea (Fig. 1)
202 under projections for future sea ice. For model parameterization, the authors estimated the
203 functional relationship between polar bear survival, reproduction, and sea ice from six years
204 of capture-recapture data (2001-06). By classifying these demographic data into “good” and
205 “bad” years and assuming that future vital rates could be represented by these estimates, they
206 analyzed the effects of an increase in the frequency of bad years on population growth and

207 suggested a substantial extirpation risk for the Southern Beaufort Sea population within 45-
208 100 years. Although their conclusions of extirpation risk were robust against parameter
209 uncertainty, the authors noted wide prediction intervals in their projections, partially due to
210 the limited range of sea ice conditions considered when estimating demographic parameters.

211 Amstrup et al. (2007) took an alternative approach, coupling general circulation
212 models with a polar bear carrying capacity model and a Bayesian network model,
213 respectively, to project population trends throughout the Arctic. They suggested likely
214 extirpation of polar bears in two broad regions (Southern Hudson Bay, Western Hudson Bay,
215 Foxe Basin, Baffin Bay, and Davis Strait populations, as well as Southern Beaufort Sea,
216 Chukchi Sea, Laptev Sea, Kara Sea, and Barents Sea populations; Fig. 1), substantial
217 declines in all other populations, and an overall loss of approximately two-thirds of the
218 global population by mid-century given current sea ice projections. However, a lack of
219 appropriate data linking predicted environmental conditions to polar bear population
220 dynamics forced the authors to estimate future carrying capacities by extrapolating from
221 present densities, and to rely on expert judgment for other stressors.

222

223 **3.1 Using Mechanistic Models to Predict Changes in Survival and Reproduction**

224

225 Nonlinear dynamics and process uncertainty can lead to spurious predictions of population
226 dynamics and abundance, when vital rate estimates are extrapolated outside observed ranges
227 or when future vital rate estimates are based on expert judgment only (Beissinger and
228 Westphal, 1998; Berteaux et al., 2006; Sutherland, 2006). This kind of problem is illustrated,
229 for example, by the failure of demographers to accurately predict human population growth

230 (Sutherland, 2006). An example illustrating the limitations of extrapolation in estimating
231 future vital rates, specifically for polar bears, is given by Derocher et al. (2004). Based on
232 linear advances in spring sea ice break-up, they calculated that most females in western
233 Hudson Bay would be unable to give birth by 2100. The authors contrasted this estimate with
234 alternative calculations based on extrapolating observed linear declines in mean female body
235 mass, which implied unsuccessful parturition for most females by 2012.

236 Rather than estimating demographic parameters from limited data and attempting
237 extrapolation, we suggest using mechanistic models that explicitly consider the cause-effect
238 relationships by which environmental conditions affect reproduction and survival. Such
239 models would allow independent prediction of these demographic parameters for yet
240 unobserved environmental conditions (Berteaux et al., 2006), which could then be input into
241 demographic projection models. In sections 3.2 and 3.3, we discuss this approach, first for
242 changes in reproduction and survival as a consequence of changes in individual energy intake
243 and energy expenditure towards movement, and then for changes that are mostly independent
244 from an individual's energy budget. For both cases, we provide a simple example for
245 illustration.

246

247 **3.2 Predicting Changes in Survival, Reproduction, and Growth due to Changes in** 248 **Energy Intake and Movement**

249

250 Changes in energy availability through decreased feeding opportunities and an increased
251 necessity for movement would negatively affect individual body condition, and thereby
252 survival, reproduction and growth. Qualitatively, this causal relationship is clear, but

253 quantitative predictions of how body condition, survival, reproduction and growth would be
254 affected under changing environmental conditions do not exist. Empirical energetic studies
255 on feeding, movement, somatic maintenance, thermoregulation, reproduction and growth in
256 polar bears are available (e.g., Øritsland et al., 1976; Best, 1982; Watts et al., 1987; Arnould
257 and Ramsay, 1994; Stirling and Øritsland, 1995), but these studies alone are insufficient for
258 predictive purposes, because it is impractical to measure survival, reproduction and growth
259 under all possible scenarios of energy intake and movement. For prediction, a mathematical
260 energy budget framework is needed that synthesizes such data in a model that
261 mechanistically describes how available energy is prioritized and allocated within the
262 organism.

263 DEB models (*sensu* Kooijman, 2010) explicitly track how an individual utilizes
264 available energy, using mechanistic rules for energy allocation and prioritization between
265 somatic maintenance, thermoregulation, reproductive output, and structural growth. DEB
266 models thus have the potential to predict survival, reproduction and growth, in response to
267 expected changes in energy intake and movement associated with changing environmental
268 conditions (Gurney et al., 1990; Nisbet et al., 2000; Kooijman, 2010), and DEB models are
269 particularly useful to predict an individual's response to food limitation (Zonneveld and
270 Kooijman, 1989; Noonburg et al., 1998). To date, DEB models have been applied to
271 invertebrates, fish, amphibians, reptiles, and birds (Kooijman, 2010, and references therein),
272 and more recently also to whales (Klanjscek et al., 2007) and ungulates (De Roos et al.,
273 2009).

274 Assuming strong homeostasis (Molnár et al., 2009), a 2-compartment DEB model
275 that tracks changes in storage energy (E ; units: MJ) and structural volume (V ; units: m^3)
276 through time (t) can be written as follows:

277

$$(1) \quad \begin{aligned} \frac{dE}{dt} &= F_{\text{IE}} - F_{\text{EA}} - F_{\text{EM}} - F_{\text{ET}} - F_{\text{EG}} - F_{\text{ER}} \\ \frac{dV}{dt} &= g^{-1} F_{\text{EG}} \end{aligned}$$

279

280 where F_{IE} represents the influx of energy from the environment through food acquisition and
281 assimilation, and F_{EA} , F_{EM} , F_{ET} , F_{EG} , and F_{ER} represent the respective rates of storage energy
282 utilization for activity, somatic maintenance, thermoregulation, structural growth, and
283 reproduction. The parameter g represents the energetic cost of growing a unit volume of
284 structure (Klanjscek et al., 2007). For simplicity, we assume additivity of fluxes (Wunder,
285 1975), and that all energy is channeled through storage (Kooijman, 2010), although other
286 formulations are possible (e.g., Lika and Nisbet, 2000; Klanjscek et al., 2007). Note also that
287 the fluxes in equation (1) are not independent from each other: energy intake (F_{IE}), for
288 example, likely depends on how much energy is allocated to movement (F_{EA}), and energy
289 allocation to growth (F_{EG}) is usually assumed possible only after maintenance requirements
290 (F_{EM} and F_{ET}) are met (Kooijman, 2010).

291 The challenge in formulating a DEB model for a given species is threefold. First, a
292 method is needed that allows estimation of energy stores (E) and structural volume (V),
293 second, the functional forms of the fluxes F_{XY} need to be determined, and third, these
294 functions need to be parameterized. A full DEB model for polar bears is currently lacking,

295 but the first step was taken by Molnár et al. (2009) who described a polar bear body
296 composition model that distinguishes between storage and structure. Their model allows
297 estimation of E from total body mass and straight-line body length, and estimation of V from
298 straight-line body length. Molnár et al. also suggest that somatic maintenance rate (F_{EM}) in
299 polar bears should be proportional to lean body mass (i.e., the mass of all tissue that is not
300 body fat), and they parameterize this DEB model component from body mass changes in
301 fasting adult males. Below, we extend their model to include costs of movement (F_{EA}) and
302 illustrate the usefulness of the DEB approach for prediction by estimating future changes in
303 adult male survival due to expected extensions of the summer open-water fasting period in
304 western Hudson Bay. A full DEB model would also allow prediction of polar bear
305 reproduction and growth under food limitation, but insufficient data exist to fully determine
306 the necessary model components F_{ER} , and F_{EG} . Directed studies, however, may fill these data
307 gaps, and we outline key data requirements below to aid further model development.

308

309 ***3.2.1.Example: Predicting Changes in Survival due to Prolonged Fasting – Time to Death***
310 ***by Starvation***

311

312 Polar bears in the Western Hudson Bay population (Fig. 1) are forced ashore when the sea
313 ice melts in summer (Derocher and Stirling, 1990). On land, energetically meaningful food is
314 unavailable, and bears rely on their energy stores for survival (Ramsay and Stirling, 1988;
315 Hobson et al., 2009). In recent years, spring sea ice break-up in western Hudson Bay has
316 been occurring progressively earlier, resulting in shortened on-ice feeding and prolonged on-
317 shore fasting for polar bears in this population (Stirling and Parkinson, 2006). Further

318 extensions to the open-water period are expected under continued climatic warming, and
 319 polar bear survival rates for this period may eventually drop if bears cannot accumulate
 320 sufficient storage energy for the fast. To illustrate how future changes in survival due to
 321 prolonged fasting can be predicted, we use a DEB model to estimate how long a bear can
 322 survive on its energy stores before death by starvation. For simplicity, we consider adult
 323 males only.

324 We apply the DEB model for fasting, non-growing and non-reproducing polar bears
 325 in a thermoneutral state from Molnár et al. (2009), with an additional component to account
 326 for energy allocated to movement:

327

328 (2)
$$\frac{dE}{dt} = \underbrace{-m \text{ LBM}}_{\text{Somatic maintenance}} - \underbrace{(aM^b + cM^d v)}_{\text{Movement}}$$

329

330 The model assumes a somatic maintenance rate proportional to lean body mass, *LBM*, with *m*
 331 representing the energy required per unit time to maintain a unit mass of lean tissue (Molnár
 332 et al., 2009). Energy costs of movement, by contrast, are dependent on total body mass, *M*,
 333 because both lean tissue and body fat need to be moved. Movement costs are represented by
 334 an allometric equation, where the first part of the sum, aM^b , represents the metabolic cost of
 335 maintaining posture during locomotion (in addition to somatic maintenance). The second part,
 336 $cM^d v$, reflects the positive linear relationship between energy consumption and velocity, *v*
 337 (Schmidt-Nielsen, 1972; Taylor et al., 1982).

338 Using the body composition model of Molnár et al. (2009), equation (2) can be
 339 rewritten as:

340

341 (3)
$$\frac{dE}{dt} = - \underbrace{m \left(\alpha^{-1} (1 - \varphi) E + \rho_{STR} k L^3 \right)}_{\text{Somatic maintenance}} - \underbrace{\left(a \left(\alpha^{-1} E + \rho_{STR} k L^3 \right)^b + c \left(\alpha^{-1} E + \rho_{STR} k L^3 \right)^d v \right)}_{\text{Movement}}$$

342

343 where α represents the energy density of storage, φ is the proportion of storage mass that is
344 fat, and $\rho_{STR} k$ is a composite proportionality constant to estimate structural mass from
345 straight-line body length, L . Body composition and maintenance parameters were estimated
346 as $m = 0.089 \text{ MJ kg}^{-1} \text{ d}^{-1}$, $\alpha = 19.50 \text{ MJ kg}^{-1}$, $\varphi = 0.439$, $\rho_{STR} k = 14.94 \text{ kg m}^{-3}$ (Molnár et al.,
347 2009), movement parameters as $a = 0$, $c = 0.0214 \text{ MJ km}^{-1}$, $d = 0.684$ (Molnár 2009). For
348 model development and parameterization details, see Molnár (2009) and Molnár et al. (2009).

349 Time to death by starvation can be estimated for a bear of straight-line body length L
350 and initial energy stores $E(0) = E_0$ by numerically integrating equation (3) and solving for
351 time T when $E(T) = 0$. Here, we considered two scenarios, one for resting bears ($v = 0$) and
352 one for bears moving at average speed $v = 2 \text{ km d}^{-1}$, which corresponds to observed on-land
353 movement rates (Derocher and Stirling, 1990). For resting bears, energy density (E/LBM)
354 was the sole determinant of time to death by starvation, whereas for moving bears starvation
355 time also depended on L . However, variation due to changes in L was small, so we used the
356 mean observed length of 2.34 m in all subsequent calculations. For both scenarios, time to
357 death by starvation increased nonlinearly with energy density (Fig. 3).

358 Predictions for changes in adult male survival in western Hudson Bay as a function of
359 fasting period length were then obtained by linking the time to death by starvation response
360 curves to observed energy densities. For this purpose, we used mass and length data from 97
361 adult male polar bears (≥ 7 years of age) caught on-land in 1989-96 in western Hudson Bay

362 (see Molnár et al., 2009, for handling procedures). All animal handling protocols were
363 consistent with the Canadian Council on Animal Care guidelines. Body masses were scaled
364 to August 1 (mean on-shore arrival date during 1990s; Stirling et al., 1999) using the mass
365 loss curve in Molnár et al. (2009). Energy densities on August 1 were calculated from these
366 body masses using the body composition model of Molnár et al. (2009).

367 Adult male survival rate as a function of observed energy densities can be estimated
368 for any fasting period length by considering the proportion of bears that would starve to
369 death before the end of the fasting period. For illustration we discuss survival predictions for
370 a fasting period length of 120 days, typical of the 1980s, and 180 days which reflects
371 potential future conditions (the fasting period has been increasing by about 7 days per decade
372 since the early 1980s; Stirling and Parkinson, 2006). Observed energy densities were
373 normally distributed, and with a fasting period of 120 days about 3% of these bears are
374 expected to die of starvation before the end of the fasting period when resting (line A in Fig.
375 3) and about 6% when moving (line B in Fig. 3). If the fasting period is extended to 180 days
376 (i.e., due to earlier spring ice break-up and delayed fall freeze-up), about 28% of these males
377 would die with no on-land movement (line C in Fig. 3) and about 48% if moving (line D in
378 Fig. 3). Expected changes in adult male survival are nonlinear due to the normal distribution
379 of energy densities, and to a smaller degree due to the nonlinearity of the time to death by
380 starvation curves. Estimates for changes in survival are conservative because death may
381 happen sooner if the strong homeostasis assumption is violated near death. Furthermore, with
382 progressively earlier spring sea ice break-up, energy densities at on-shore arrival are expected
383 to be reduced relative to those observed during the 1990s due to shortened on-ice feeding
384 (Stirling and Derocher, 1993), thereby further reducing expected time to death by starvation.

385 Such declines in body condition have already been documented in western Hudson Bay
386 (Derocher and Stirling, 1995; Stirling et al., 1999).

387 Predictions of starvation time and resultant changes in survival are also possible for
388 other groups, such as subadults or adult females with offspring, if the additional energy
389 expended on lactation and growth, respectively (F_{ER} and F_{EG} in equation (1)), can be
390 quantified. Generally, adult males may be the least affected group because they do not spend
391 energy on growth or lactation. However, due to their proportionally higher lean tissue content
392 in storage, they cannot fast as long as non-reproducing adult females (Molnár et al., 2009).

393

394 **3.3 Predicting Non-Energy Related Changes in Demographic Parameters**

395

396 Some effects of climate change will not be directly energy-related. Mechanistic models,
397 specific to the proposed cause-effect relationships, may nevertheless be used for prediction in
398 many cases, but a comprehensive discussion of all possible effects and models is impossible.
399 However, to illustrate the potential of mechanistic models in predicting changes in vital rates,
400 even when the primary mechanism for change is not energy-related, we explore how habitat
401 fragmentation and declines in sea ice area would affect female mating success.

402

403 ***3.3.1 Example: Potential Climate Change Impacts on Female Mating Success***

404

405 Derocher et al. (2004) put forth two contrasting hypotheses regarding changes in female
406 mating success under climate warming. First, increased areas of open water and increased ice
407 floe drift rates may impede mate-finding and result in reduced pregnancy rates because adult

408 males rely on contiguous female tracks for mate location. By contrast, declines in sea ice area
 409 may facilitate mate-finding to increase pregnancy rates by increasing bear density during the
 410 mating season. Here, we assess the respective importance of these contrasting effects.
 411 Specifically, we use the mating model of Molnár et al. (2008) to show how quantitative
 412 predictions for changes in female mating success due to changes in habitat fragmentation
 413 (mate-searching efficiency) and sea ice area can be obtained.

414 Polar bear pairing dynamics during the mating season are driven by mate location,
 415 pair formation, and pair separation, and can be described by the following system of
 416 differential equations (Molnár et al., 2008):

417

$$(4a) \quad \underbrace{\frac{dm}{dt}}_{\text{Solitary available males}} = - \underbrace{\frac{sq}{A} m f}_{\text{Pair formation}} + \underbrace{\mu p}_{\text{Pair separation}}$$

$$(4b) \quad \underbrace{\frac{df}{dt}}_{\text{Unfertilized females}} = - \underbrace{\frac{sq}{A} m f}_{\text{Pair formation}}$$

418

$$(4c) \quad \underbrace{\frac{dp}{dt}}_{\text{Breeding pairs}} = \underbrace{\frac{sq}{A} m f}_{\text{Pair formation}} - \underbrace{\mu p}_{\text{Pair separation}}$$

$$(4d) \quad \underbrace{\frac{df^*}{dt}}_{\text{Fertilized females}} = \underbrace{\mu p}_{\text{Pair separation}}$$

419

420 where $m(t)$, $f(t)$, $p(t)$, and $f^*(t)$ represent the respective numbers (at time t) of solitary males
 421 searching for mates, solitary unfertilized females, breeding pairs, and solitary fertilized
 422 females. The left-hand sides of equations (4a-d) represent the respective rates of change in

423 these quantities, and these rates depend on pair formation and pair separation. Pair formation
424 is modelled using the law of mass action, and pairs are formed at rate sq/A , where s
425 represents searching efficiency (units: $\text{km}^2 \text{d}^{-1}$), q is the probability of pair formation upon
426 encounter (i.e., mate choice), and A is habitat area (units: km^2). Pairs remain together for μ^{-1}
427 time units (units: d), thus separating at rate μ . The mating season begins at $t = 0$, when $m(0) =$
428 m_0 , $f(0) = f_0$, $p(0) = 0$, $f^*(0) = 0$, and lasts T time units. Female mating success is defined as
429 the proportion of females fertilized at the end of the mating season and is estimated as $1 -$
430 $f(T)/f_0$. To explore how changes in sea ice area and habitat fragmentation would affect female
431 mating success, we rewrote the model of Molnár et al. (2008) considering bear numbers
432 rather than densities, thereby explicitly representing sea ice area, mate-searching efficiency
433 and mate choice. We also assumed maximal male mating ability (i.e., all solitary males
434 search for mates at all times), considering a simplified version of the model in Molnár et al.
435 (2008). However, it is noteworthy that male mating ability may also decline under climate
436 warming induced food stress, and such declines could reduce female mating success (Molnár
437 et al., 2008).

438 The model explicitly considers the mechanisms determining female mating success,
439 describes observed pairing dynamics well, and can thus be used to predict female mating
440 success from initial male and female numbers, m_0 and f_0 , and model parameters s , q , A , and μ
441 (Molnár et al., 2008). We consider changes in sea ice area (A) and mate-searching efficiency
442 (s), and illustrate predictions using the example of Lancaster Sound (Fig. 1), where $m_0 = 489$,
443 $f_0 = 451$, $sq/A = 0.00021 \text{d}^{-1}$, $\mu^{-1} = 17.5 \text{d}$ and $T = 60 \text{d}$ were estimated for 1993-1997,
444 implying a female mating success of 99% (Molnár et al., 2008). Female mating success
445 depends on the ratio sq/A and is predicted to decline non-linearly if searching efficiency s

446 declines faster than habitat area A , and to increase non-linearly otherwise. For example,
447 assuming that m_0, f_0, μ^{-1}, T , and q remain constant in Lancaster Sound, female mating success
448 is predicted to decline from 99% to 91% if s declined twice as fast as A , and to 72% if s
449 declined four times as fast as A . By contrast, if A declined faster than s , mating success would
450 remain essentially unchanged at around 100% in this population (Fig. 4).

451 The parameters s and A may change independent of each other because mate-
452 searching efficiency depends on movement speeds, movement patterns, detection distance,
453 and male tracking ability, parameters that are affected more by the degree of habitat
454 fragmentation (areas of open water between ice floes) than by total habitat area. The degree
455 to which s and A will be affected by climate change cannot be predicted from the mating
456 model itself. However, such predictions could be obtained independently for s from
457 mechanistic encounter rate models that account for changes in movement patterns, tracking
458 ability and detection distance due to habitat fragmentation (Kiørboe and Bagøien, 2005). The
459 degree of future habitat fragmentation and changes to sea ice area (A) could in turn be
460 predicted from sea ice models. Resultant predictions for s and A could then be input into the
461 mating model to obtain more specific predictions of female mating success under climate
462 change than presented here. Potential future changes in mate choice (q) should hereby also be
463 considered, because mate choice may vary adaptively as a function of male densities, sex
464 ratios, and expected mating success (Kokko and Mappes, 2005). Potential declines in s may
465 be compensated by increases in q , because pair formation rate is determined by the
466 composite term sq/A (but note that q cannot be increased to values larger than 1). The
467 predictions outlined here are insensitive to the parameters μ^{-1} and T , but may be affected
468 significantly by harvest-induced changes in m_0 and f_0 (Molnár et al., 2008).

469

470 **4. Integrating Predicted Changes in Demographic Parameters** 471 **into Population Models**

472

473 The stage-structured population dynamics of polar bears can be formalized in matrix models
474 (Fig. 2), which are useful for population projections and PVAs (Hunter et al., 2007).

475 However, such analyses are only accurate if future vital rates (reproduction and survival) are
476 accurately represented by existing estimates, or if future changes in vital rates can be
477 accurately predicted from present conditions. The lack of data on vital rates under not yet
478 experienced conditions has thus been a major limitation to PVA accuracy (Beissinger and
479 Westphal, 1998; Ludwig, 1999; Coulson et al., 2001; Sutherland, 2006). To avoid this
480 problem, we have advocated mechanistic models to predict changes in survival and
481 reproduction because such models can often be developed and parameterized independent of
482 environmental conditions. A second advantage of such mechanistic models is their ability to
483 identify expected nonlinearities and threshold events in vital rate response curves to
484 environmental conditions (Figs. 3, 4), which will affect PVAs (Ludwig, 1999; Harley et al.,
485 2006)

486 The mathematical integration of vital rate predictions into matrix population models
487 is often straightforward, and we outline this process for the two examples considered above.
488 Adult male survival rate from one spring to the next (parameter σ_{10} in the matrix model of
489 Hunter et al. (2007); Fig. 2) can be written as the product of adult male survival during the
490 fasting and feeding periods, respectively. Expected changes in survival during the fasting
491 period (Fig. 3) can thus be incorporated to predict changes in σ_{10} due to this survival

492 component. The probability of a female without offspring breeding (β_4 in Fig. 2) can
493 similarly be decomposed into the probabilities of successful mating, successful implantation,
494 successful parturition, and early cub survival. Expected changes in mating success caused by
495 habitat fragmentation and sea ice area declines (Fig. 4) could thus also be incorporated into a
496 matrix population model.

497 The biggest limitation to this component-wise approach of predicting changes in
498 reproduction and survival relates to uncertainty in initial conditions. For example, the
499 distribution of energy densities at the beginning of the fasting period in any given year, and
500 thus the period-specific survival rate, may depend on the date of sea ice break-up in that year
501 (and thus the length of the preceding on-ice feeding period), but also on the lengths of the
502 feeding and fasting periods in previous years (i.e., time lags). This problem of uncertainty
503 could be avoided if a full DEB model was available that tracks the energy intake and
504 expenditure of polar bears through the entire year. Population projections would in that case
505 be a matter of tracking individuals over time. However, until a fully predictive model
506 becomes available, a component-wise analysis of expected changes in vital rates and
507 resultant effects on population growth is possible because the direction of the expected
508 changes in initial conditions is often clear. For example, polar bear energy densities at on-
509 shore arrival in western Hudson Bay are already declining and are expected to decline further.
510 Models that assume all else equal (in particular, on-shore arrival energy densities as observed
511 during the 1990s) to predict future fasting period survival rates as a function of predicted
512 fasting period lengths would thus be conservative and could set boundaries to expected
513 changes in survival. Until different effects of climate change on vital rates, addressed by
514 different mechanistic models, can be connected into a single predictive framework,

515 component-wise prediction of changes in vital rates (treating different aspects of climate
516 change on polar bears separately) could provide a series of conservation indicators that
517 should be considered in conservation assessments and population management.

518

519 **5. A Call for Data**

520

521 The type of data required to further mechanistic models for reproduction and survival is in
522 many cases different from data collected for monitoring these demographic parameters (such
523 as mark-recapture data). The development of such models will require the integration of field
524 research to specifically address the mechanisms determining change in reproduction and
525 survival. The areas of investigation will be specific to the mechanisms considered, and as it is
526 impossible to provide a comprehensive summary of all potential modelling approaches, it is
527 similarly impossible to outline all data that might prove useful for model development,
528 parameterization, and validation. However, because most expected climate change effects on
529 polar bears are energy-related, we believe that DEB models may provide one of the most
530 useful venues for understanding and predicting climate change effects on polar bears.

531 Changes in growth, reproduction, and survival, in response to expected changes in feeding
532 and movement can be predicted from DEB models, provided that sufficient physiological
533 data can be gathered to specify energy allocation rules and parameterize model terms
534 (Gurney et al., 1990; Noonburg et al., 1998; Kooijman et al., 2008; Kooijman, 2010). Long-
535 term research on polar bears has already provided much of the required physiological data for
536 DEB development, and missing pieces could be addressed with directed studies. To aid the
537 development of a full polar bear DEB model, we next outline key data requirements.

538 DEB models consider two distinct components of energy flow: net energy intake
539 from the environment (the difference between terms F_{IE} and F_{EA} in equation (1)) and the
540 allocation of assimilated energy within the organism towards somatic maintenance,
541 thermoregulation, reproduction, and growth (F_{EM} , F_{ET} , F_{ER} , and F_{EG}). The physiological
542 terms F_{EM} , F_{ET} , F_{ER} , and F_{EG} can be understood independently from the environment, and
543 they could be determined under current conditions. In fact, the term for somatic maintenance
544 (F_{EM}) has already been specified (Molnár et al., 2009; cf. also equations (2) and (3)), and the
545 thermoregulation term F_{ET} can probably be determined from published data (e.g., Best, 1982).
546 By contrast, insufficient data exist to fully determine the model terms F_{ER} , and F_{EG} , which
547 specify the magnitude of energy allocation towards reproduction and growth and the
548 conditions under which energy allocation to these processes ceases.

549 Reproduction in female polar bears consists of a short gestation period (*ca.* 60 days;
550 Derocher et al., 1992), and a lactation period that normally lasts up to 2.5 years (Derocher et
551 al., 1993). The energetic costs of gestation are small compared to those of lactation (Oftedal,
552 1993), so that data collection should prioritize quantifying milk energy transfer. Milk energy
553 transfer rates may depend on maternal body condition (e.g., storage energy or energy density),
554 cub demand, and cub age. Cub demand, in turn, may be determined by cub body condition,
555 cub growth, and the amount of solid food consumed (Lee et al., 1991; Oftedal, 1993;
556 Arnould and Ramsay, 1994). Although it may be straightforward to formulate lactation
557 within a DEB model (e.g., Klanjscek et al., 2007), relatively large amounts of data may be
558 required for model parameterization due to the number of factors involved. Milk energy
559 transfer data covering a range of feeding conditions (e.g., on-shore fasting and on-ice
560 feeding) as well as a range of maternal and cub body conditions are required for model

561 development. Data on the presence or absence of lactation in relation to maternal energy
562 stores, particularly during the on-shore fasting period in southern populations, may provide
563 further insight into the mechanisms determining cessation of lactation. Cessation of lactation
564 has been reported for food-stressed females (Derocher et al., 1993), implying a storage
565 energy (or energy density) threshold below which lactation stops. The existence of such a
566 threshold is supported by DEB theory (Lika and Nisbet, 2000), and would have implications
567 for lactation (and consequent cub survival) for females food-stressed by climate warming.

568 The allocation of energy to structural growth is probably the least understood
569 component in the energy budget of polar bears. It may also be the most difficult term to
570 specify in a DEB model, because energy allocation to growth may depend on energy intake
571 (Lika and Nisbet, 2000; Kooijman, 2010), and may also be size-dependent (Nisbet et al.,
572 2004). Structural growth data, estimated through changes in straight-line body length, is
573 needed for bears of different ages, sizes and body conditions with known energy intake.
574 Captive bears may aid in determining this model component because energy intake is known
575 and changes in storage energy and body length could be determined. Growth in bears under
576 food limitation should also be considered to specify the conditions under which energy
577 allocation to growth ceases. While growth data from food-stressed bears may not be available
578 from captive studies, such data could also be obtained from cubs and subadults caught during
579 the on-shore fasting period in southern populations. Energy intake for nursing cubs could in
580 this case be measured through isotope dilution methods (Arnould and Ramsay, 1994), or
581 approximated through changes in maternal energy stores. For both growth and reproduction
582 (and, in fact, for all DEB components), longitudinal data (i.e., repeated measurements of

583 individuals over weeks or months) is preferable over population cross-sections because
584 individual-based processes are assessed.

585 Changes to the second component of an individual's energy budget, net energy intake
586 ($F_{IE}-F_{EA}$), under changing environmental conditions cannot be predicted from single-species
587 DEB models. Multi-species DEB models, modelling the flow of energy between trophic
588 levels (Nisbet et al., 2000), may be able to provide such predictions, but insufficient data on
589 the polar bear-seal predator-prey system currently prevents the construction of such models.
590 Little is known about Arctic seal abundance, distribution, and population dynamics, and even
591 less is known about the mechanisms regulating the polar bear-seal predator-prey system. To
592 date, only a handful of studies have documented kill frequency and meal size in polar bears,
593 and these studies are restricted in space and time (Stirling, 1974; Stirling and Latour, 1978;
594 Stirling and Øritsland, 1995). Kill frequencies are unknown for most populations and almost
595 all seasons. A mechanistic link between habitat characteristics, prey population dynamics,
596 and polar bear energy intake is also missing. Comprehensive feeding data are needed to
597 illuminate these links and should become a research priority if we are to move towards a
598 predictive framework for changes in polar bear energy intake (and consequent changes in
599 reproduction and survival) under climate warming. The collection of detailed dietary
600 information can be difficult because polar bears forage in remote sea ice habitats, but new
601 statistical methods, such as state-space models (Franke et al., 2006) or behavioural change
602 point analyses (Gurarie et al., 2009), could be used to extract feeding events from GPS
603 movement data. Moreover, given longitudinal mass and length data, energy intake could also
604 be inferred from DEB models, provided that the energy expenditure terms F_{EA} , F_{EM} , F_{ET} , F_{ER} ,
605 and F_{EG} can be specified a priori.

606 In addition to the new set of research priorities outlined here, we advocate continued
607 mark-recapture studies to estimate survival and reproduction. Although such studies may be
608 of limited use for predicting polar bear population dynamics under climate change (given the
609 lack of long-term studies for most populations and the discussed problems associated with
610 extrapolating vital rates into yet unobserved environmental conditions), they are useful for
611 monitoring past and current change, crucial to population management, conservation status
612 assessment, and the setting of harvest quotas. Additionally, in the context outlined here,
613 mark-recapture studies may provide valuable reproduction and survival data that could be
614 used to validate proposed DEB and other mechanistic models aimed at predicting these
615 demographic parameters.

616

617 **6. Conclusions**

618

619 There is no doubt that climate warming is occurring, and climatologists and other scientists
620 have provided a number of predictive models for temperature, precipitation, sea ice,
621 permafrost, and other issues (IPCC, 2007). Ecologists, by contrast, are still facing
622 considerable challenges to obtain quantitative predictions for the resultant effects on species
623 and ecosystems. It is clear that many species are already affected (Walther et al., 2002;
624 Parmesan, 2006), but quantitative predictions are lacking for most species, and existing
625 predictions are often associated with large uncertainty, largely due to limited data and
626 insufficiently understood causal chains (Berteaux et al., 2006; Krebs and Berteaux, 2006;
627 Sutherland, 2006). The mechanistic framework advocated here may help to incorporate
628 cause-effect relationships into ecological predictions, could link expected effects of climate

629 change over various levels of biological organization, and could alert us to the presence of
630 yet unobserved nonlinearities in reproduction and survival in response to changing
631 environmental conditions.

632 Whether or not climate change effects on survival and reproduction are incorporated
633 into PVAs may have significant effects on conservation status assessments and other aspects
634 of population management. Polar bears were listed globally as “Threatened” in 2008 under
635 the U.S. *Endangered Species Act* due to the threats posed by climate change (Federal
636 Register, 2009). In contrast, the assessment of polar bears in Canada by the Committee on the
637 Status of Endangered Wildlife in Canada (COSEWIC) did not account for possible climate
638 change effects, and their finding of “Special Concern” (COSEWIC, 2008) identified a lower
639 level of threat than the U.S. assessment. The U.S. and Canadian assessments used similar
640 population projection models in their PVAs, but they differed in their approaches towards
641 model parameterization. The COSEWIC report used mean reproduction and survival rates
642 from earlier studies and projected these forward, specifically stating that they “...do not
643 account for the possible effects of climate change.” (COSEWIC, 2008: page iii). The U.S.
644 approach included environmental trends in their PVA, but they assumed that future vital rates
645 would correspond to estimates from three “good” and two “bad” habitat years observed
646 between 2001 and 2005 (Hunter et al., 2007). Mechanistic models for reproduction and
647 survival were not used in either approach, but may affect status assessments in both countries.
648 If there are nonlinear relationships between environmental conditions and polar bear vital
649 rates, as suggested by the two models considered above, then population projections may be
650 direr than suggested by existing assessments.

651 Moreover, polar bear vital rates may also be affected by other stressors, not always
652 directly caused but possibly amplified by climate change, such as harvest, pollution, or the
653 emergence of new diseases. Harvest-induced changes in population composition, for instance,
654 may lead to a mate-finding Allee effect (Molnár et al., 2008). Increased exposure of polar
655 bears to persistent organic pollutants (Derocher et al., 2004) may affect their endocrine
656 system (Skaare et al., 2002), their immune system (Bernhoft et al., 2000), and by extension
657 survival and reproduction (Derocher et al., 2003). Climate change may lead to the emergence
658 of new diseases in Arctic wildlife (Bradley et al., 2005). These stressors should also be
659 considered in status assessments and population management (Amstrup et al., 2007) and the
660 suggested approach for predicting changes in reproduction and survival remains applicable.
661 However, the degree to which these effects will be amenable to prediction depends on the
662 level at which causal chains are understood and the availability of data to develop appropriate
663 mechanistic models (Jonzén et al., 2005; Berteaux et al., 2006; Krebs and Berteaux, 2006).
664 Molnár et al. (2008), for instance, developed a mechanistic model for the polar bear mating
665 system (cf. equation (4)) to predict female mating success from male and female densities for
666 yet unobserved population compositions, and they showed that a sudden reproductive
667 collapse could occur if males are severely depleted. Their results could be incorporated into a
668 2-sex population matrix model and would allow predicting the effects of a continued sex-
669 selective harvest on female mating success, and thus population growth. The effects of
670 increasing pollution levels on reproduction and survival could also be predicted with
671 mechanistic models, specifically pharmacokinetic models coupled with DEB models
672 (Klanjscek et al., 2007), but no such efforts are underway for polar bears. By contrast,

673 potential future effects of emerging diseases on vital rates remain currently unquantifiable in
674 polar bears due to unclear causal chains and a lack of empirical data.

675 The methods we have outlined in this paper for polar bears are broadly applicable to
676 other species. Linking energy availability to demographic parameters will be a key means of
677 understanding species responses to climate change. The increase in fasting period modelled
678 here can be considered a form of shifting phenology and can be applied to any species. For
679 example, breeding schedules in birds are closely tied to the phenology of their food supplies,
680 and the disruption of this pairing can affect reproductive success (Visser et al., 1998; Thomas
681 et al., 2001). DEB modeling may be a means to explore these relationships to aid
682 conservation planning.

683 It seems clear that not all species will be currently amenable to the mechanistic
684 framework outlined above. For mechanistic models to be successful in prediction, initial
685 conditions must be well described, all important variables must be included in the model, and
686 model variables must be related to each other in an appropriate way (Berteaux et al., 2006).
687 Whether or not these conditions are fulfilled cannot be known a priori (Berteaux et al., 2006).
688 However, modelling is an iterative approach, where proposed models should be tested
689 against independent data to decide whether the models were successful in predicting. Models
690 can then be improved and tested again, until they converge to satisfactory performance.
691 Arctic species, in particular, may be among the most amenable to prediction because low
692 species diversity, relatively simple food webs, and a limited range of species interactions
693 result in comparatively simple relationships between environmental variables and their
694 effects on individuals and populations.

695 Mechanistic models are not the only means of predicting the climate change effects
696 on species, but given their potential to predict into yet unobserved conditions, we believe
697 they have been underutilized and present a fruitful line of research to address conservation
698 challenges in a changing world.

699

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709

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928 **Figure Legends:**

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930 **Figure 1:** Circumpolar polar bear populations. BB: Baffin Bay; DS: Davis Strait; FB: Foxe
931 Basin; GB: Gulf of Boothia; KB: Kane Basin; LS: Lancaster Sound; MC: M'Clintock
932 Channel; NB: Northern Beaufort Sea; NW: Norwegian Bay; QE: Queen Elizabeth Islands;
933 SB: Southern Beaufort Sea; SH: Southern Hudson Bay; VM: Viscount Melville Sound; WH:
934 Western Hudson Bay. The figure is from Aars et al. (2006).

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936 **Figure 2:** Schematic representation of the polar bear life cycle, as modeled by Hunter et al.
937 (2007), using a stage-structured two-sex matrix population model with parental care. Stages
938 1-6 are females, stages 7-10 are males. σ_i is the probability of survival for an individual in
939 stage i from one spring to the next, σ_{L0} and σ_{L1} are the probabilities of at least one member of
940 a cub-of-the-year (COY) or yearling (yrlg) litter surviving from one spring to the next, f is
941 the expected size of yearling litters that survive to 2 years, and β_i is the conditional
942 probability, given survival, of an individual in stage i breeding, thereby producing a COY
943 litter with at least one member surviving to the following spring. The figure is redrawn from
944 Hunter et al. (2007).

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946 **Figure 3:** Estimated time to death by starvation for fasting adult male polar bears, when
947 resting (solid line) and when moving at average speed $v = 2 \text{ km d}^{-1}$ (dotted line). The
948 horizontal dotted line indicates a fasting period of 120 days, the horizontal dashed line a
949 fasting period of 180 days. Crosses show the cumulative distribution of energy densities at
950 the beginning of the fasting period (right axis) for 97 adult males caught in 1989-1996 in the

951 Western Hudson Bay population. Lines A-D illustrate the proportion of these males that
952 would die from starvation following a fast of 120 days and 180 days, with and without
953 movement, respectively (see text for details).

954

955 **Figure 4:** Potential climate change impacts on female mating success (the proportion of
956 females fertilized at the end of the mating season), arising from declines in mate-searching
957 efficiency, s , and sea ice habitat area, A , assuming constant mate choice. Predictions are
958 shown for the population of Lancaster Sound, with male and female numbers assumed
959 unchanged relative to 1993-1997, and the estimate of s/A for this period marked by a circle.
960 Also indicated are scenarios where s declines twice (square) and four times (diamond) as fast
961 as A , respectively. A scenario where A declines faster than s by a factor of 1.5 is indicated by
962 a triangle (see text for details).

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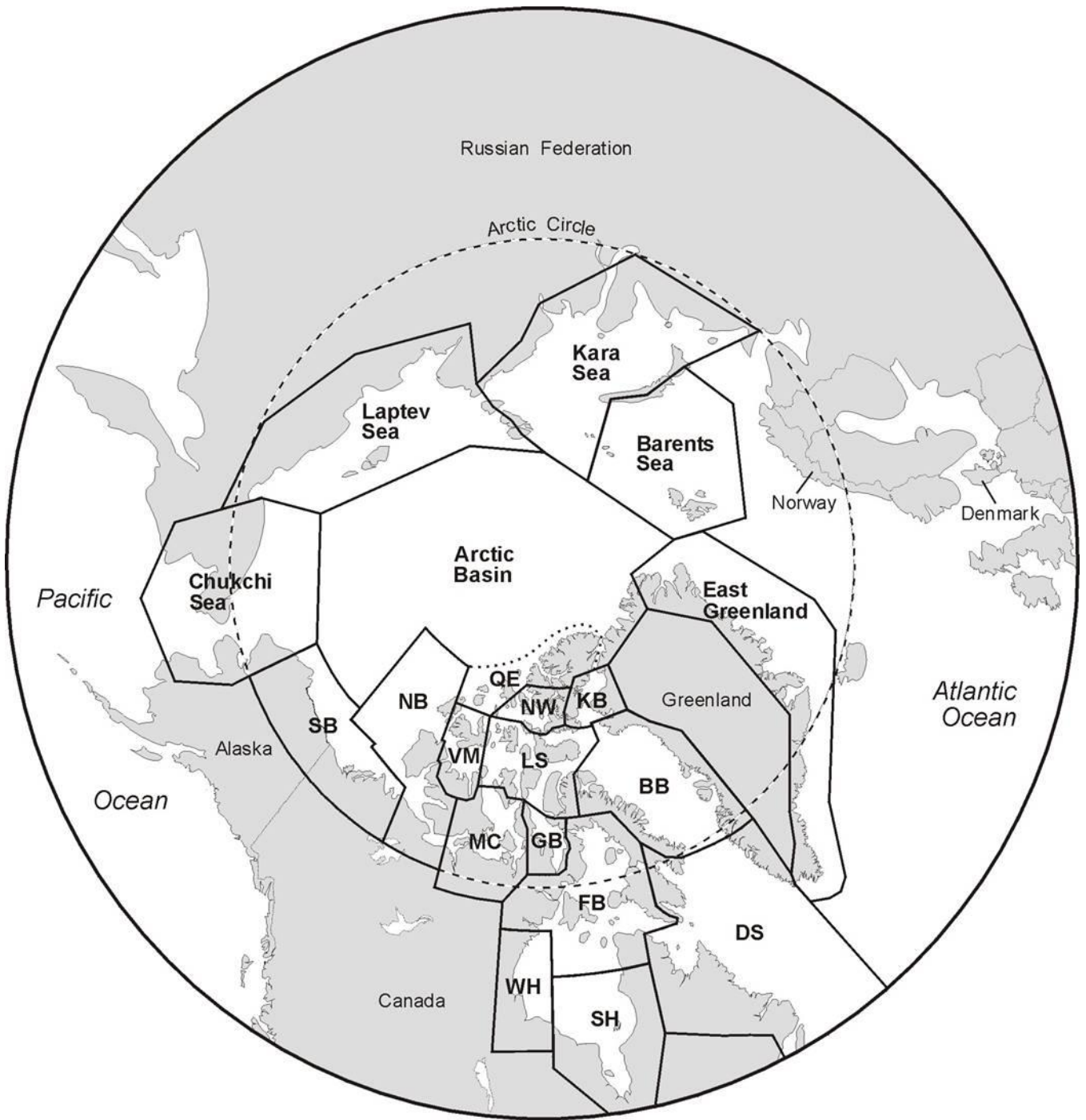
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974 **Figure 1:**



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979 **Figure 2:**

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981 **Females**

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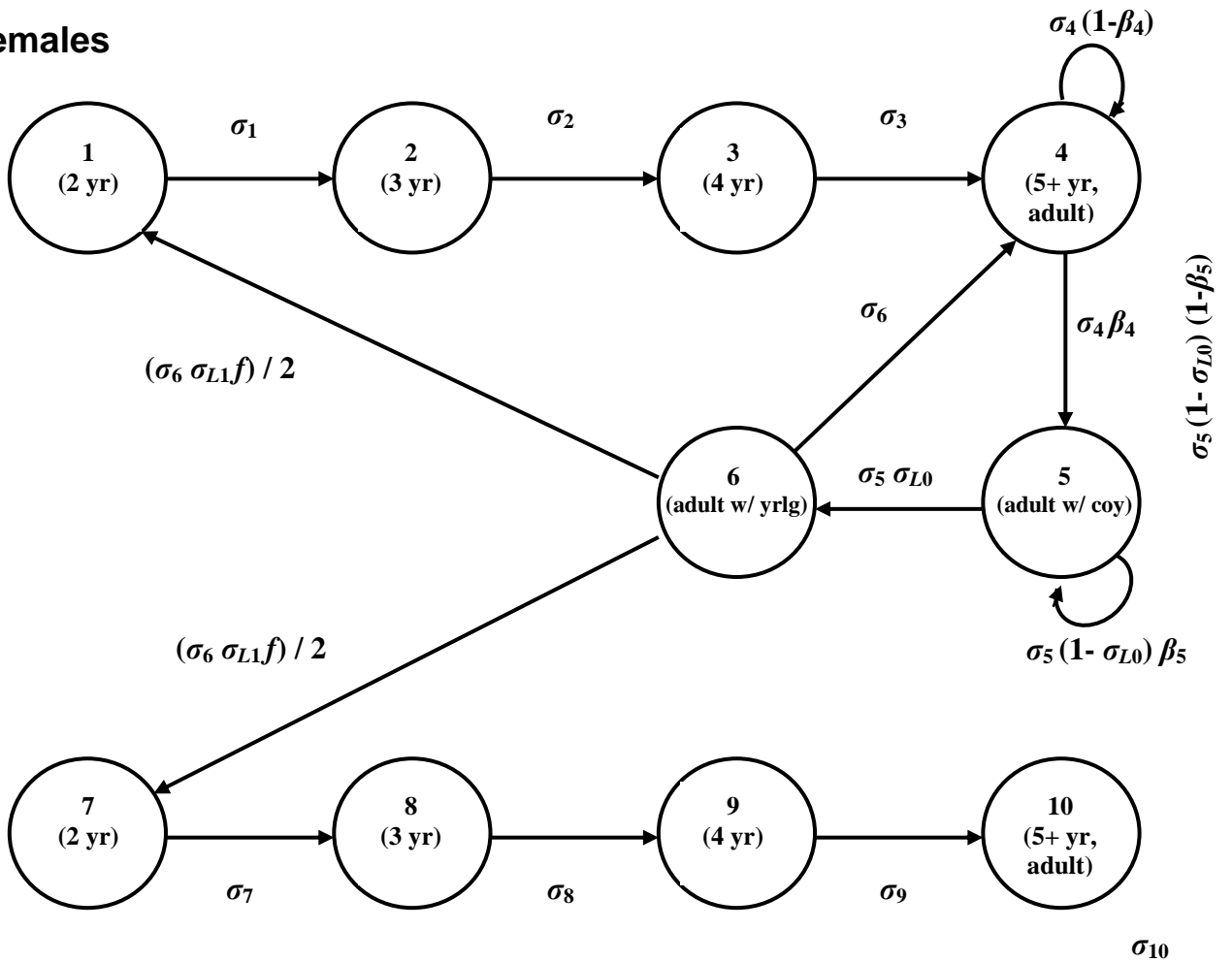
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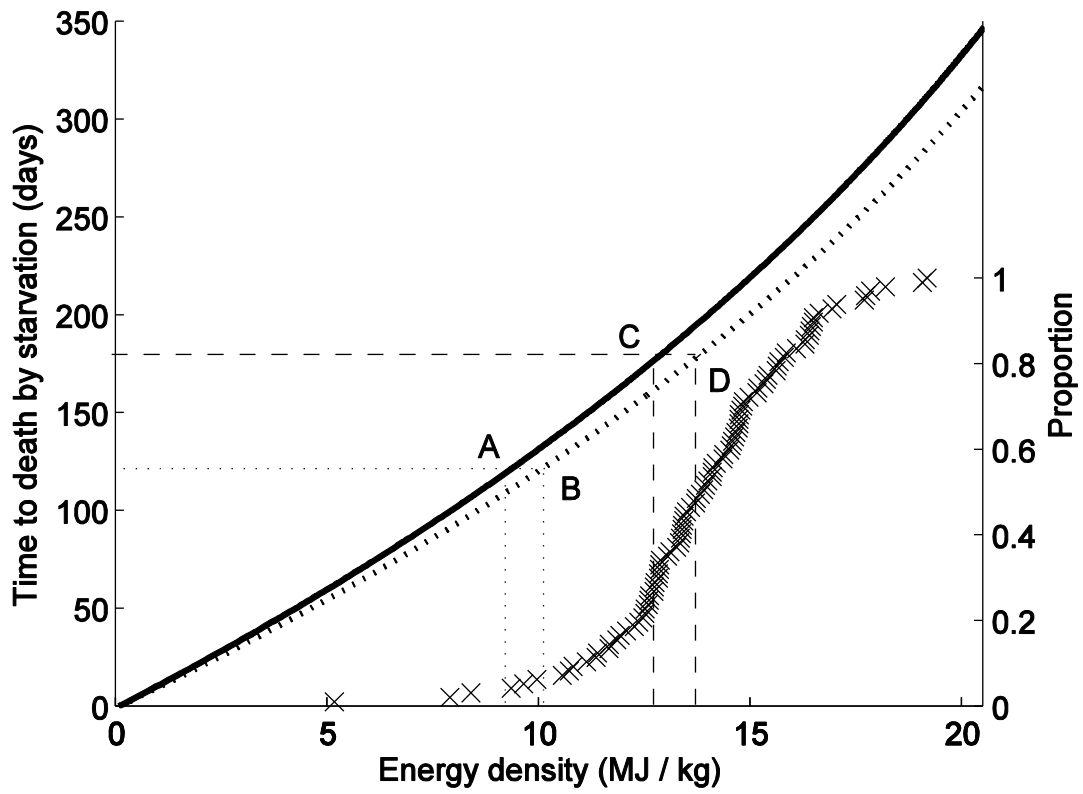
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1002 **Figure 3:**



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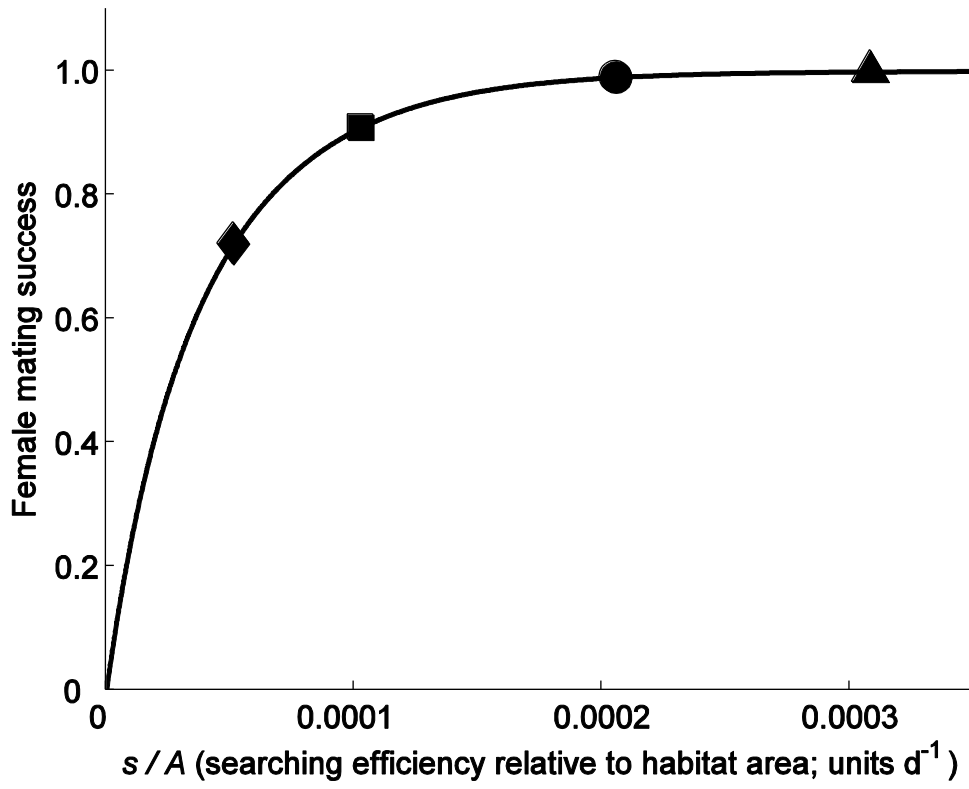
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1015 **Figure 4:**



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