

1 **Second-generation stoichiometric mathematical model to predict methane**  
2 **emissions from oil sands tailings**

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16 **Abstract**

17

18 Microbial metabolism of fugitive hydrocarbons produces greenhouse gas (GHG) emissions from  
19 oil sands tailings ponds (OSTP) and end pit lakes (EPL) that retain fluid tailings from surface  
20 mining of oil sands ores. Predicting GHG production, particularly methane (CH<sub>4</sub>), would help oil  
21 sands operators mitigate tailings emissions and may assist regulators evaluating the trajectory of  
22 reclamation scenarios. Using empirical datasets from laboratory incubation of OSTP sediments  
23 with pertinent hydrocarbons, we developed a stoichiometric model for CH<sub>4</sub> generation by

24 indigenous microbes. This model improved on previous first-approximation models by  
25 considering long-term biodegradation kinetics for 18 relevant hydrocarbons from three different  
26 oil sands operations, lag times, nutrient limitations, and microbial growth and death rates.  
27 Laboratory measurements were used to estimate model parameter values and to validate the new  
28 model. Goodness of fit analysis showed that the stoichiometric model predicted CH<sub>4</sub> production  
29 well; normalized mean square error analysis revealed that it surpassed previous models.  
30 Comparison of model predictions with field measurements of CH<sub>4</sub> emissions further validated  
31 the new model. Importantly, the model also identified parameters that are currently lacking but  
32 are needed to enable future robust modeling of CH<sub>4</sub> production from OSTP and EPL in-situ.  
33  
34 **Keywords:** modeling methane production; anaerobic hydrocarbon biodegradation;  
35 methanogenesis; greenhouse gas emissions; oil sands tailings pond; end pit lake

## 36 **1. Introduction**

37 Alberta's oil sands industry is a major economic driver in Canada, currently producing ~3  
38 million barrels oil d<sup>-1</sup> and expected to reach 4 million barrels d<sup>-1</sup> by 2024 (Government of  
39 Alberta, 2019a; <https://aer.ca/providing-information/data-and-reports/statistical-reports/st53>).  
40 However, the oil sands sector has come under international scrutiny regarding GHG emissions and other  
41 environmental issues. Oil sands operations including mining, upgrading and in-situ extraction were  
42 responsible for ~43% of Alberta's overall GHG emissions in 2012 (Alberta Greenhouse Gas Report,  
43 2016). In addition to these production operations, the storage and management of aqueous slurries of  
44 surface-mined ore processing wastes in oil sands tailings ponds (OSTP; Figure S1) contributes  
45 substantially to methane (CH<sub>4</sub>) and carbon dioxide (CO<sub>2</sub>) emissions (Burkus et al., 2014; Siddique et al.,  
46 2008). Total fugitive GHG emissions from major oil sands operators' OSTP, measured in-situ using  
47 floating flux chambers in 2011, were calculated to be 2.8 million tonnes CO<sub>2</sub> equivalent per year (Burkus  
48 et al., 2014), while in 2018 they were estimated at ~2.2 Mt of CO<sub>2</sub>e (Z. Burkus, personal communication).  
49 Furthermore, proposed implementation of EPL as a long-term reclamation strategy for OSTP sediments  
50 (Figure S1) may contribute additional GHG emissions for an unknown timespan.

51 During five decades of retention, enormous volumes of tailings have accumulated that is  
52 currently estimated at >1.2 billion m<sup>3</sup> (Government of Alberta, 2019b). As the fluid tailings in  
53 OSTP age, the suspended clay fines settle via several mechanisms (porewater and solid phase  
54 chemistry) including gravity (Siddique et al., 2014) to become anaerobic mature fine tailings  
55 (MFT) having a solids content >30 wt% and possessing both an active microbiota and residual  
56 diluent in progressive stages of selective biodegradation (Fig S2 in Foght et al., 2017). The use  
57 of EPL has been discussed to reintegrate the accumulated tailings into the on-site environment  
58 (Charette et al., 2012) and proposed by industry in their tailings management plans as one of  
59 their closure approaches (Alberta Energy Regulator, 2019). In this reclamation scenario, after

60 years or decades of residence in OSTP, MFT would be treated and transported to mined-out pits  
61 and capped with fresh water and/or process-affected water. This is intended to establish a  
62 sustainable aquatic system (i.e., an end pit lake; EPL) that, with time, should support economic,  
63 ecological and/or societal uses (Charette et al., 2012). However, ebullition of GHG from  
64 underlying sediments may delay EPL ecosystem development by dispersing fine sediments into  
65 the overlying water layer along, potentially co-transporting some constituents of concern. Thus,  
66 GHG emissions from oil sands tailings repositories are problematic from global warming as well  
67 as ecological standpoints.

68 GHG emissions from OSTP and EPL result primarily from anaerobic biodegradation of  
69 diluent hydrocarbons, naphtha or light paraffins, introduced into tailings after aqueous extraction  
70 of bitumen from oil sands ore and treatment of froth (Figure S1; reviewed in Foght et al., 2017)  
71 The diluents, specific to each operator, facilitate separation of bitumen from water and mineral  
72 solid particles during froth treatment and reduce bitumen viscosity in preparation for processing  
73 and/or transport. Most of the diluent is recovered from the froth treatment tailings for re-use, but  
74 a small proportion remains in the tailings slurry that comprises alkaline water, sand, silt, clays  
75 and unrecovered bitumen. These fresh tailings, as well as other tailings streams that have not  
76 been exposed to diluent, are deposited in OSTP where indigenous anaerobic microbial  
77 communities biodegrade the labile hydrocarbons to CH<sub>4</sub> and CO<sub>2</sub> (Abu Laban et al., 2015;  
78 Penner and Foght, 2010; Mohamad Shahimin et al., 2016; Siddique et al., 2011). Although  
79 naphtha and paraffinic diluents are considered to be the major carbon sources for microbes in  
80 OSTP (Foght et al., 2017), only certain of their hydrocarbon components are known to be  
81 biodegradable under anaerobic conditions, whereas others are recalcitrant (slowly or  
82 incompletely biodegraded) or are completely resistant to biodegradation (Siddique et al., 2018).

83 Although bitumen is the overwhelming organic constituent of fresh tailings, it predominantly  
84 comprises recalcitrant hydrocarbons: only a small proportion may be labile and the contribution  
85 of bitumen to biogenic GHG is thought to be negligible in proportion to that of diluent (Foght et  
86 al., 2017).

87 The importance of modeling GHG emissions is clear to oil sands operators, as it provides a  
88 rationale for mitigating GHG mitigation efforts and managing OSTP and EPL. However, field  
89 data (e.g., concentrations of individual hydrocarbons in OSTP, nutrient concentrations, biomass)  
90 needed for modeling are generally unavailable either because collection of such data is  
91 technologically difficult or because such key model parameters have not previously been  
92 identified as necessary. Therefore, we have cultivated MFT in laboratory cultures analogous to  
93 OSTP and EPL for use in initial modeling efforts. A previous study (Siddique et al., 2008) used  
94 limited data available from short-term (<1 yr) laboratory studies measuring biodegradation of a  
95 small subset of components (Siddique et al., 2007, 2006) in a single naphtha diluent to develop  
96 zero- and first-order kinetic models for estimating CH<sub>4</sub> production potential from a single OSTP.  
97 That first approximation model predicted in-situ CH<sub>4</sub> production volumes reasonably consistent  
98 with emissions measured in-situ (Siddique et al., 2008). However, in the decade since that work,  
99 additional components of naphtha and paraffinic diluent have been shown to support  
100 methanogenesis from MFT during extended laboratory incubation (up to 6.5 y; Abu Laban et al.,  
101 2015; Mohamad Shahimin et al., 2016; Siddique et al., 2015, 2011). This finding increases  
102 theoretical GHG emissions, especially from hydrocarbons previously assumed to be recalcitrant  
103 and thus not considered in the previous model and over extended time scales more relevant to  
104 long-term retention of tailings. Additionally, data are now available for additional OSTP  
105 receiving different diluents and therefore having unique microbial communities (Wilson et al.,

106 2016) with different CH<sub>4</sub> production potentials, and the effect of potentially growth-limiting  
107 nutrients in-situ such as nitrogen has begun to be examined (Collins et al., 2016). Also, the first  
108 EPL field trial was established in 2012/2013 where CH<sub>4</sub> has been detected within the water cap  
109 (Risacher et al., 2018). The greatly expanded data set and a broader understanding of oil sands  
110 tailings microbiology (Foght et al., 2017) enable and have driven development of the improved  
111 and flexible model for CH<sub>4</sub> generation described here.

112 The goals of the new stoichiometric model were: (1) to expand CH<sub>4</sub> predictive capability by  
113 considering methanogenic biodegradation of a wider range of hydrocarbons only recently shown  
114 to be labile over longer incubation times; (2) for the first time to consider OSTP that receive  
115 diluents having different compositions and that harbour different microbial communities; (3) to  
116 account for the effects of nutrient limitation on CH<sub>4</sub> generation, particularly available nitrogen;  
117 (4) to compare model predictions with field measurements of CH<sub>4</sub> emissions to validate the  
118 model and reveal any shortcomings; (5) to consider differences in GHG emission trajectories  
119 between OSTP and EPL; and (6) to identify parameters essential for future development of a  
120 model to predict CH<sub>4</sub> emissions in-situ in OSTP and EPL.

## 121 **2. Materials and Methods**

122 Although the gaseous products of methanogenic hydrocarbon biodegradation are CH<sub>4</sub> and CO<sub>2</sub>  
123 (Figure S2), the stoichiometric model developed here considers only CH<sub>4</sub> production for two  
124 reasons: CH<sub>4</sub> has a greater greenhouse effect than CO<sub>2</sub>; and measurement of emissions of CO<sub>2</sub>  
125 emissions produced in MFT is confounded by abiotic (carbonate dissolution) and  
126 biogeochemical (mineral precipitation and dissolution) interactions with tailings minerals  
127 (Siddique et al., 2014), complicating measurement and modeling.

128 Methane production from hydrocarbons involves two microbial processes: the oxidation of  
129 labile hydrocarbons to simple organic compounds by Bacteria and the conversion of those  
130 compounds to CH<sub>4</sub> and CO<sub>2</sub> by Archaea (Figure S2). Therefore, the model was developed in two  
131 modules. The first module (section 2.1) comprising two systems of equations describes bacterial  
132 biodegradation of 18 hydrocarbon substrates (see section 2.3.1 for selection rationale) and  
133 includes formation of microbial biomass. The second module (section 2.2) considers archaeal  
134 CH<sub>4</sub> generation from bacterial metabolites. Model parameters unavailable in the literature were  
135 estimated by data fitting using laboratory measurements (section 2.3). The model then was  
136 quantitatively validated by comparison (1) to measurements from independent but analogous  
137 laboratory experiments conducted using oil sands tailings incubated with whole diluents or  
138 components of naphtha or paraffinic diluents and (2) to field measurements of CH<sub>4</sub> emissions  
139 from OSTP (section 2.4). Finally the model was qualitatively assessed using phase plane analysis  
140 to illustrate CH<sub>4</sub> emission trajectories in OSTP and EPL (section 2.5 and supporting material  
141 section S3). Terms used in model development are defined in Table 1.

### 142 *2.1 Biodegradation and biomass module development.*

143 Direct measurement of hydrocarbon biodegradation kinetics in OSTP and EPL is technically  
144 infeasible. Therefore this module describes the dynamics of CH<sub>4</sub> production from MFT  
145 incubated with cognate naphtha or paraffinic diluents under laboratory conditions analogous to  
146 those expected in OSTP or EPL. A brief description of previously published cultivation methods  
147 used to generate model data is given in supporting material section S1.

148 Microbial biomass can change as a result of growth and death. Because hydrocarbon  
149 biodegradation is initiated by Bacteria and not by the archaeal methanogens (Figure S2), this  
150 module considers only bacterial kinetics. The per cell bacterial growth rate is assumed to follow

151 Liebig's law of the minimum (Sterner and Elser, 2002) stating that growth rate is proportional to  
 152 the most limiting resource available. The model assumes, based on chemical analysis of oil sands  
 153 tailings (Collins, 2013; Penner and Foght, 2010) that all relevant nutrients except biologically-  
 154 available nitrogen (defined in Table 1) and/or labile carbon are present at non-limiting  
 155 concentrations in OSTP and EPL. Therefore the bacterial growth rate is modeled as a function  
 156 only of the mass of biologically-available nitrogen ( $N_A$ ) and labile hydrocarbons ( $C_i$ , the mass of  
 157 labile hydrocarbons in the system for  $i=1 \dots n$ , assuming  $n$  discrete labile hydrocarbons in the  
 158 system). Assuming that there is negligible input of  $N_A$  with fresh tailings, no outflow of soluble  
 159  $N_A$  and no loss of gaseous  $NO_x$ , we take the total nitrogen ( $N_T$ ) in these systems to be constant.  
 160 With this assumption, the subset of  $N_T$  available for bacterial growth ( $N_A$ ) is given by  $N_A = N_T -$   
 161  $\theta B$  where  $\theta$  is the ratio of nitrogen to carbon in the total microbial biomass  $B$ , and  $\theta$  is assumed  
 162 to be constant (Makino et al., 2003). The Monod functions  $f(N_A) = \frac{N_A}{N_A + K_f}$  and  $g(C_i) = \frac{C_i}{C_i + K_{g_i}}$   
 163 are used to model the nitrogen- and carbon-dependent growth rates respectively, where  $K_f$  is the  
 164  $N_A$ -dependent half-saturation constant;  $K_{g_i}$  is the  $C_i$ -dependent half-saturation constant; and  $C_i^{in}$   
 165 is the inflow of  $C_i$  to the system. Thus, the  $C_i$ -dependent per cell bacterial growth rate  $\mu$  is given  
 166 by  $\mu_i \min\{f(N_A), g(C_i)\}$ , where  $\mu_i$  is the maximum growth rate of bacteria growing on only the  
 167 hydrocarbon  $C_i$  present and is unique for each labile hydrocarbon. Hence the total per cell  
 168 growth rate of bacteria is  $\sum_{i=1}^n \mu_i \min\{f(N_A), g(C_i)\}$ .

169 The biodegradation rate of each labile hydrocarbon  $i$  is assumed to be proportional to the  
 170 bacterial growth rate due to its consumption, i.e., [per cell bacterial growth rate due to each  
 171 hydrocarbon]  $\propto$  [biodegradation rate of hydrocarbon]. This implies that [the per cell bacterial  
 172 growth rate supported by each labile hydrocarbon  $i$ ] =  $r_i$ [the per cell biodegradation rate of that  
 173 hydrocarbon] where  $r_i$  is a proportionality constant reflecting the efficiency of bacterial



174 conversion of substrate into biomass. Hence, [the per cell biodegradation rate of each labile  
 175 hydrocarbon] =  $\frac{1}{r_i}$  [the per cell bacterial growth rate supported by labile hydrocarbons], i.e., [the  
 176 per cell biodegradation rate of each hydrocarbon] =  $\sum_{i=1}^n \frac{1}{r_i} \mu_i \min\{f(N_A), g(C_i)\}$ . Archaeal  
 177 growth and death are considered in the second module (section 2.2).

178 We assume that microbial death rate ( $d$ ) is constant in the laboratory cultures and that  
 179 nutrients in dead microbial biomass are quickly recycled back into labile carbon and nitrogen  
 180 ( $N_A$ ). The fraction of  $C_i$  recycled from dead biomass  $b$  is assumed to be a constant  $\beta_i$  where  $0 <$   
 181  $\beta_i < 1$ .

182 In accordance with laboratory observations (Mohamad Shahimin and Siddique, 2017a,  
 183 2017b, Siddique et al., 2007, 2006), the model assumes that onset of biodegradation of each  
 184 hydrocarbon begins after a unique lag period,  $\lambda_i$ . The above assumptions lead to the following  
 185 system of equations:

$$186 \quad g(C_i) = \begin{cases} 0, & t < \lambda_i \\ \frac{C_i}{K_{g_i} + C_i}, & t \geq \lambda_i \end{cases}$$

$$187 \quad \frac{dB}{dt} = B \sum_{i=1}^n \mu_i \min\left\{\frac{N_A}{K_f + N_A}, g(C_i)\right\} - dB, \quad (1)$$

$$188 \quad \frac{dC_i}{dt} = \frac{-1}{r_i} \mu_i B \min\left\{\frac{N_A}{K_f + N_A}, g(C_i)\right\} + \beta_i dB + C_i^{in},$$

$$189 \quad N_A = N_T - \theta B,$$

$$190 \quad B(0) > 0, C_i(0) \geq 0.$$

191 Since the carbon- and nutrient-dependent growth efficiency parameters describe the main  
 192 differences in bacterial utilization of different hydrocarbon, the model assumes that parameters  
 193 such as carbon conversion efficiency, intrinsic bacterial growth rate, and carbon recycling from

194 dead bacteria (negligible in our data fitting), are equivalent for different hydrocarbons; i.e.,  $\mu_i =$   
 195  $\mu, r_i = r$ , and  $\beta_i = \beta$ . With this assumption, the system of equations becomes:

196

$$197 \quad g(C_i) = \begin{cases} 0, & t < \lambda_i \\ \frac{C_i}{K_{g_i} + C_i}, & t \geq \lambda_i \end{cases}$$

$$198 \quad \frac{dB}{dt} = B \sum_{i=1}^n \mu \min \left\{ \frac{N_A}{K_f + N_A}, g(C_i) \right\} - dB, \quad (2)$$

$$199 \quad \frac{dC_i}{dt} = \frac{-1}{r} \mu B \min \left\{ \frac{N_A}{K_f + N_A}, g(C_i) \right\} + \beta dB + C_i^{in},$$

$$200 \quad N_A = N_T - \theta B,$$

$$201 \quad B(0) > 0, C_i(0) \geq 0.$$

202 To analyze the types of solutions that this model could produce, a steady state analysis was  
 203 performed. The algebraic analysis is described in supplementary material section S2 and is of  
 204 particular use because it allows solutions to be classified by parameter values.

## 205 *2.2 Methane biogenesis module development*

206 From the preceding biodegradation module, bacterial biodegradation of a hydrocarbon substrate  
 207 ( $C_i$ ) per unit time yields  $\frac{1}{r} \mu B \min \left\{ \frac{N_A}{K_f + N_A}, g(C_i) \right\}$  units of metabolite(s) corresponding to  $C_i$ . The  
 208 metabolite(s) ultimately are converted to  $\text{CH}_4$  and  $\text{CO}_2$  ( $G_i$ ) by methanogens (Figure S2). Since  
 209 methanogens have a slow growth rate compared to that of the hydrocarbon-degrading Bacteria  
 210 (being dependent on their metabolism), we assume that the biomass of methanogens in the  
 211 system is constant. With these additions, the system of equations (2) becomes:

$$212 \quad (C_i) = \begin{cases} 0, & t < \lambda_i \\ \frac{C_i}{K_{g_i} + C_i}, & t \geq \lambda_i \end{cases}$$

$$213 \quad \frac{dB}{dt} = B \sum_{i=1}^n \mu \min \left\{ \frac{N_A}{K_f + N_A}, g(C_i) \right\} - dB, \quad (3)$$

$$214 \quad \frac{dC_i}{dt} = \frac{-1}{r} \mu B \min \left\{ \frac{N_A}{K_f + N_A}, g(C_i) \right\} + \beta dB + C_i^{in},$$

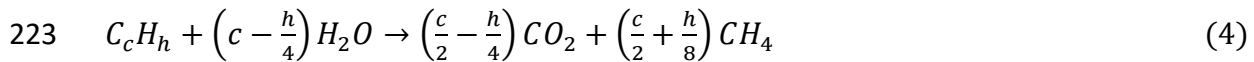
$$215 \quad \frac{dG_i}{dt} = \frac{1}{r} \mu B \min \left\{ \frac{N_A}{K_f + N_A}, g(C_i) \right\},$$

$$216 \quad CH_4 = \sum_{i=1}^n \eta_i \Gamma_i G_i,$$

$$217 \quad N_A = N_T - \theta B,$$

$$218 \quad B(0) > 0, C_i \geq 0, G_i(0) = 0$$

219 where,  $\Gamma_i$  is the maximum theoretical yield of  $CH_4$  expected from biodegradation of one mole of  
 220  $C_i$ . This value can be calculated from Equation (4) (derived from Symons and Buswell, 1933, as  
 221 implemented by Roberts, 2002) that describes the complete oxidation of hydrocarbons to  $CH_4$   
 222 and  $CO_2$  under methanogenic conditions, namely:



224 where  $c$  and  $h$  are, respectively, the numbers of carbon and hydrogen atoms in a  $C_i$  molecule.

225 From equation (4),  $\Gamma_i = \left(\frac{c}{2} + \frac{h}{8}\right)$ . Furthermore,  $\eta_i$  is the fraction of the theoretical  $CH_4$  yield  
 226 from the biodegradation of a mole of  $C_i$  (i.e., a conversion efficiency factor) and is assumed to be  
 227 the same for all  $C_i$ , i.e.,  $\eta_i = \eta$ , with  $0 < \eta_i < 1$ . The values of  $\eta_i$  used in numerical simulations  
 228 were obtained from (Mohamad Shahimin et al., 2016; Mohamad Shahimin and Siddique,  
 229 2017a, 2017b, Siddique et al., 2007, 2006) and Table S1.

230

### 231 *2.3 Acquisition of laboratory data, parameter estimation and model validation*

232 Our approach was to select a suite of 18 relevant labile hydrocarbons to generate model  
233 predictions, then estimate missing model parameters using empirical biodegradation kinetics and  
234 CH<sub>4</sub> measurements for these hydrocarbons, and finally to test the stoichiometric model  
235 quantitatively using measurements from an independent set of laboratory experiments.

#### 236 *2.3.1 Model hydrocarbon selection and testing*

237 Fugitive diluent in froth treatment tailings (Fig. S1) is the predominant substrate for  
238 methanogenesis in OSTP (Foght et al., 2017). The most commonly used diluents are naphtha and  
239 paraffinic solvent. Syncrude Canada Ltd. (Syncrude), Suncor, and Canadian Natural Resources  
240 Ltd. (CNRL) use naphtha, the composition of which differs slightly for each company but which  
241 comprises primarily paraffinic (*n*-, *iso*- and *cyclo*-alkanes) and monoaromatic hydrocarbons  
242 (predominantly toluene and three xylene isomers), typically in the C<sub>6</sub>-C<sub>10</sub> range (Siddique et al.,  
243 2008). Canadian Natural Upgrading Limited (CNUL; formerly Shell Albian), Imperial (Kearl  
244 Mine) and Suncor (Fort Hills Mine) uses a paraffinic diluent comprising *n*- and *iso*-alkanes  
245 primarily in the C<sub>5</sub>-C<sub>6</sub> range (Mohamad Shahimin and Siddique, 2017a). Published results from  
246 laboratory experiments incubating these whole diluents or their major constituents with MFT  
247 from Syncrude, CNUL or CNRL (Mohamad Shahimin et al., 2016; Mohamad Shahimin and  
248 Siddique, 2017a, 2017b, Siddique et al., 2007, 2006; and Table S1) revealed complete or  
249 significant biodegradation of 18 hydrocarbons under methanogenic conditions, including the *n*-  
250 alkanes *n*-pentane (C<sub>5</sub>), *n*-hexane (C<sub>6</sub>), *n*-heptane (C<sub>7</sub>), *n*-octane (C<sub>8</sub>), *n*-nonane (C<sub>9</sub>), and *n*-  
251 decane (C<sub>10</sub>); the *iso*-alkanes 2-methylpentane (2-MC<sub>5</sub>), 2-methylhexane (2-MC<sub>6</sub>), 3-  
252 methylhexane (3-MC<sub>6</sub>), 2-methylheptane (2-MC<sub>7</sub>), 4-methylheptane (4-MC<sub>7</sub>), 2-methyloctane

253 (2-MC<sub>8</sub>), 3-methyloctane (3-MC<sub>8</sub>) and 2-methylnonane (2-MC<sub>9</sub>); and the monoaromatics  
254 toluene, *o*-xylene and *m*- plus *p*-xylenes (the latter two are not resolved by our gas  
255 chromatography column and are therefore reported as a sum). Table 2 lists the 18 labile  
256 hydrocarbons selected for model development, the source of biodegradation data, the type of  
257 tailings used to generate the data and the parameters estimated using those data.

### 258 2.3.2 Parameter estimation

259 The values of many model parameters in the system of equations (3) are not available in the  
260 literature, including the initial microbial biomass in OSTP and EPL ( $B(0)$ ), the nitrogen half-  
261 saturation constant ( $K_f$ ), the half-saturation constants of the biodegradable hydrocarbons ( $K_{gi}$ )  
262 and  $\lambda_i$ . Because these parameters are related to the biodegradation module, we fit the  
263 biodegradation module (system of equations (2)) to data obtained from laboratory biodegradation  
264 studies cited above. To estimate these values, we used the nonlinear regression function *nlinfit(.)*  
265 in MATLAB, which uses the Levenberg-Marquardt algorithm (Moré, 1978), to fit the solution of  
266 the biodegradation module to the data. We provided the function with empirical data (see Table 2  
267 for sources), the time points at which the data were collected ( $X$ ), our simulated results at  $X$ , and  
268 a random initial guess of parameter values. The system was integrated by calling a function that  
269 takes as input the initial parameter values, the time at which the empirical data were collected,  
270 and for any given time  $X$  uses the MATLAB function *ode15s(.)* to perform the integration. The  
271 solution of the system obtained from the function was then evaluated at  $X$ , using the MATLAB  
272 function *deval(.)*. We also estimated the 95% confidence intervals of the predicted values by  
273 using the MATLAB function *nlparci(.)*. To achieve this, we provided this function with the  
274 coefficient estimates, residuals and the estimated coefficient covariance matrix from *nlinfit(.)*.  
275 Some of the microbial model parameters used in the simulation, namely  $\mu$ ,  $r$ , and  $\theta$ , were taken

276 from the literature: the units, values and source of these parameters are provided in Table S2. We  
277 assume here that no microbes died during laboratory incubation; thus, in fitting the data to our  
278 model, we take  $d$  to be zero.

### 279 *2.3.3 Model validation against laboratory data*

280 The new stoichiometric model was then validated against CH<sub>4</sub> production data generated in  
281 independent but parallel laboratory studies that measured biodegradation of paraffinic diluent in  
282 CNUL MFT (Mohamad Shahimin and Siddique, 2017a) and naphtha in Syncrude (Table S1)  
283 and CNRL MFT (Mohamad Shahimin and Siddique, 2017b). To this end, the concentrations of  
284 the labile hydrocarbons initially present in each diluent were used in the model to predict CH<sub>4</sub>  
285 production (Table S7). These predictions were compared with measured CH<sub>4</sub> produced by those  
286 tailings in independent laboratory experiments using the *goodnessOfFit(.)* function in MATLAB.  
287 As input, we provided this function with our test data, the simulated data from our model, and a  
288 cost function that determines the goodness of fit. We used the Normalized Mean Square Error  
289 (NMSE) function for this statistic, computed as

$$290 \quad \text{NMSE} = 1 - \frac{\|[\text{actual}] - [\text{predicted}]\|^2}{\|[\text{actual}] - [\text{mean of actual}]\|^2},$$

291 where  $\|\cdot\|$  indicates the 2-norm of a vector, *predicted* is the output simulated by our model,  
292 *actual* is the input test data and *mean of actual* is the mean of the test data.  $\text{NMSE} \in [-\infty, 1]$   
293 where  $-\infty$  indicates a bad fit and 1 a perfect fit.

### 294 *2.4 Quantitative comparison of model prediction and in-situ measurement of CH<sub>4</sub>* 295 *emissions from OSTP*

296 To further validate the applicability of model for predicting in-situ CH<sub>4</sub> emissions, we used (1) a  
297 modeling approach where kinetics of CH<sub>4</sub> production were estimated to determine the duration  
298 of CH<sub>4</sub> emissions, and (2) a direct approach that yielded a ballpark value of potential CH<sub>4</sub>

299 emissions. For both approaches, we estimated the total mass of diluent entrained in froth  
 300 treatment tailings entering Syncrude MLSB, CNRL Horizon and CNUL MRM OSTPs in 2016  
 301 and 2017 (Table S6) and estimated the mass of individual biodegradable hydrocarbons in diluent  
 302 (Table S7) using published diluent compositions. To employ the modeling approach, we  
 303 assumed that these masses of individual hydrocarbons were present at the start of each year (i.e.,  
 304 the model was run as if all the diluent was introduced on January 1 of the year), while  
 305 acknowledging the continuous input of similar amounts of diluents in the years preceding 2016.  
 306 Using the estimated parameter values in Table S4, we modeled CH<sub>4</sub> production and calculated  
 307 the predicted cumulative CH<sub>4</sub> produced by metabolism of the constituent hydrocarbons over 366  
 308 days. The model output was compared with cumulative CH<sub>4</sub> emissions measured in flux  
 309 chambers at the surface of OSTP as reported to the Government of Alberta (unpublished; raw  
 310 data available upon request) (Table S8). Notably, surface flux measurements of CH<sub>4</sub> are not yet  
 311 available for the single EPL that was established in 2013, so the current comparison is limited to  
 312 OSTP measurements. In the direct approach, theoretical CH<sub>4</sub> production was estimated from the  
 313 masses of individual hydrocarbons biodegraded to methane using stoichiometric equations as  
 314 described in Table S8.

315 In addition to quantitative analyses, the model was also qualitatively challenged to predict the  
 2.5 *Qualitative assessment of model predictions for OSTP and EPL*

trajectories of CH<sub>4</sub> generation from OSTP (continuous ) versus EPL (C<sub>r</sub>=0) under  
 316 hypothetical scenarios of carbon or nitrogen availability in-situ. Phase plane analysis was

317 performed (Supplemental Material section S3) by assuming  $C_i^{in} > 0$

318

319 that the diluent comprises C<sub>i</sub>,

320  $i=1,2,3,\dots,18$  are identical and sum up to C<sub>T</sub>, and that the rate input of all the C<sub>i</sub> per unit time

321 into the system is  $C_T^{in}$ . Equations were solved for microbial biomass versus total carbon content  
322 over time.

323

324

under eight combinations of  $C_i$  and  $N_A$  limitation

325

The mathematical model and code are available at <http://www.judekong.ca/publication/2019->

326

<sup>05-01</sup> Methanobiogenesis model or from the authors upon request. Previous zero- and first-order  $CH_4$  production models from oil sands tailings (Siddique et al.,

### 3. Results and Discussion

327

2008) used the available limited experimental data for diluent biodegradation and  $CH_4$

328

production from four short-chain *n*-alkanes and four monoaromatic compounds during <1 year

329

incubation with MFT from a single OSTP (Siddique et al., 2007, 2006). Those first

330

approximation models assumed that organic carbon was the sole limiting nutrient in-situ and that

331

microbial biomass was constant in OSTP despite receiving continuous and consistent inputs of

332

diluent in froth treatment tailings. The stoichiometric model described here accounts for

333

additional parameters including recently published biodegradation kinetics and  $CH_4$

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measurements for 18 relevant hydrocarbons including additional *n*-alkanes and, for the first time,

335

*iso*-alkanes, incubated for much longer (up to 6.5 years) with MFT from three different OSTP

336

impacted by distinct diluents. These additional experimental data allow the estimation of some

337

kinetic parameters not previously considered and enable the new model to account for more

338

biological factors than the previous models, so as to be adaptable to future modeling of in-situ

339

$CH_4$  production from OSTP and EPL.

340

#### *3.1 Data fitting to biodegradation and methane generation modules.*

341

The biodegradation module was evaluated by fitting system of equations (2) to published

342

experimental data sets for the 18 labile hydrocarbons listed in Table 2. Figures S3-S5 show the

343

simulated biodegradation of diluent *n*-alkanes, monoaromatics and *iso*-alkanes compared with



344 measured biodegradation of these components. We obtained goodness-of-fit statistics (NMSE)  
345 ranging from 0.85-1.00 (Table S3). These statistics show that the performance of the module  
346 with respect to the training data is good.

347 To integrate the methane generation module with the biodegradation module, only three  
348 model parameters were available in the literature (Table S2); others had to be estimated from  
349 experimental data (Tables 2 and S4). Using these calculated values we applied the full  
350 stoichiometric model to methane measurements from a suite of experiments analogous to but  
351 independent of those used to estimate the parameters. Specifically, the CH<sub>4</sub> measurements were  
352 acquired during long-term incubation of MFT samples from Syncrude, CNUL and CNRL with  
353 their cognate diluents (Table S1, Siddique et al., 2015, Mohamad Shahimin and Siddique, 2017a,  
354 respectively). Figure 1 shows that the model predicted methane generation very well for all three  
355 types of MFT over long incubation times (> 4 yr incubation for CNUL and CNRL cultures).  
356 Additional modeling of Syncrude MFT with mixtures of *n*-alkane or monoaromatic components  
357 of its diluent (rather than whole diluent) also showed very good methane prediction (Fig. S6).

### 358 *3.2 Model evaluation and comparison to previous models*

359 Goodness-of-fit analysis of the stoichiometric model was calculated using NMSE (Table 3) that  
360 showed excellent fit, ranging from 0.81 – 0.98 for the three combinations of MFT and diluent.  
361 These NMSE results indicate that the integrated biodegradation and CH<sub>4</sub> production modules  
362 rightly capture the behaviour of independent laboratory cultures and that the stoichiometric  
363 model is sufficiently flexible to accommodate different inocula and substrates over long  
364 incubation periods.

365 The new stoichiometric model was then compared with the previous zero- and first-order  
366 kinetic models, as performed previously (Siddique et al., 2008), using the current data set. To

367 this end, we first estimated the zero- and first-order kinetic model-related parameter values for  
368 the labile hydrocarbons that were not considered by Siddique et al. (2008) (Table S5). Figures 1  
369 and S6, and Table 3 show that the stoichiometric model provides improved predictions over the  
370 previous models for describing CH<sub>4</sub> biogenesis from Syncrude MFT and whole naphtha or its  
371 components, and is far superior (matching closely with the measured methane) to the simpler  
372 models for the CNUL MFT–paraffinic diluent and for CNRL–naphtha combinations, neither of  
373 which were available for the previous modeling study. The improved fit regarding lag time and  
374 extent of CH<sub>4</sub> production, and the improved NMSE values suggest that the stoichiometric model,  
375 which is based on laboratory cultures, would be useful for modeling in-situ CH<sub>4</sub> production from  
376 different OSTP and EPL.

### 377 *3.3 Quantitative comparison of stoichiometric model predictions to measured* 378 *cumulative CH<sub>4</sub> field emissions*

379 To evaluate the feasibility of applying this model based on laboratory cultures to field emissions  
380 of CH<sub>4</sub>, we compared the reported measured volumes of CH<sub>4</sub> emitted from the surfaces of  
381 OSTPs with cumulative CH<sub>4</sub> masses predicted by our model. Table 4 shows the comparison  
382 between the reported measured methane emissions from OSTPs in 2016 and 2017 and the  
383 maximum theoretical CH<sub>4</sub> yield predicted by our model based on the estimated diluent entering  
384 OSTPs (Table S6) for 2016 and 2017. The stoichiometric model predictions are 50-55 % of the  
385 measured emissions from Syncrude MLSB and 77-95% of the measured emissions from CNRL  
386 OSTP in both years. For CNUL where paraffinic solvent is used, the model predictions were  
387 48% of the measured emissions in 2017 but only 17% of the emissions in 2016. This latter  
388 difference may be attributed to markedly greater methane emission data from CNUL OSTP  
389 reported in 2016 compared to all other OSTPs (Tables 4 and S5). The overall trend is very clear

390 that the model predicted about 50% of emissions from Syncrude and CNUL OSTP and >75% of  
391 emissions from CNRL OSTP. This likely reflects the diluent compositions, with only ~40% of  
392 fugitive Syncrude and CNRL naphtha diluent being considered labile versus ~60% of CNUL  
393 paraffinic diluent, based on the mass of known biodegradable hydrocarbons in the diluents  
394 (Table S7).

395 This difference between predicted and measured CH<sub>4</sub> masses suggests that (other than  
396 possible inaccuracies associated with field measurements) there are other endogenous carbon  
397 sources present in OSTP that support methanogenesis but are not currently accounted for by the  
398 model. Such possible sources include (but are not limited to): (1) additional labile diluent  
399 hydrocarbons not yet identified in our laboratory incubations and therefore not included in the  
400 model; (2) recalcitrant hydrocarbons deposited in previous years (and therefore not included in  
401 the annual  $C_i^{in}$  model input) that are slowly degraded as the community adapts to residual  
402 naphtha after depletion of the labile hydrocarbons in lower strata, e.g., some *iso*-alkanes and  
403 cycloalkanes having extremely long lag times or slow degradation rates (e.g., Abu Laban et al.,  
404 2015); (3) slowly-degradable metabolites produced historically during incomplete  
405 biodegradation of hydrocarbon or from non-hydrocarbon carbon substrates; (4) organic matter  
406 associated with clays in oil sands ores (Sparks et al., 2003); (5) minor labile components of  
407 bitumen e.g., high molecular weight *n*-alkanes (Oberding and Gieg, 2018); and (6) organic  
408 additives used in ore processing and deposited with tailings, e.g., citrate that is used as an  
409 amendment in some OSTPs (Foght et al., 2017) and is a potentially large source of unaccounted  
410 CH<sub>4</sub> in CNUL MRM. Another explanation for larger masses of measured emissions is the  
411 delayed, stochastic release of methane produced years ago from labile HCs that is 'trapped' in  
412 lower strata of MFT (Guo, 2009) until (1) suitably-sized and -oriented channels are created (e.g.,

413 by microbial activity, Siddique et al., 2014) and/or (2) cumulative gas voids reach critical  
414 buoyancy and rise from deep tailings, and/or (3) MFT strata are disturbed by some physical  
415 activity in the pond (e.g., moving deposition pipes, transferring MFT to new pits, etc.) allowing  
416 escape of gas.

417 There is an agreement between the model predictions and measured field emissions despite  
418 the obvious reasons of discrepancy discussed above. However, additional qualitative factors  
419 must be addressed to expand the developed model to in-situ predictions while keeping in mind  
420 the inherent differences between laboratory cultures and field operations: (1) cultures are  
421 incubated with a single input of hydrocarbons, i.e., in “batch mode” with finite  $C_i^{in}$ , whereas the  
422 upper strata of OSTP receive ongoing input of diluent, i.e., “continuous mode” where  $C_i^{in} > 0$ .  
423 The laboratory cultures are more analogous to EPL, where  $C_i^{in} = 0$  or to the lower strata of OSTP  
424 to which fresh diluent deposited at the surface cannot effectively diffuse and where, essentially,  
425  $C_i^{in} = 0$ . (2) As discussed above, anaerobic biodegradation kinetics are currently available for  
426 only 18 hydrocarbons in cultures, whereas additional constituents of whole diluent and possibly a  
427 small subset of bitumen constituents may be susceptible to biodegradation in-situ. Restriction of  
428 the parameter  $C_i$  to the current 18 hydrocarbons would likely cause the model to under-estimate  
429 methane production in-situ. Selective depletion of naphtha constituents with depth in OSTP has  
430 been observed qualitatively (Figure S2 in Foght et al., 2017) and such information could be used  
431 in future to expand the substrate range of the stoichiometric model and better represent in-situ  
432 biodegradation. (3) The model currently includes a variable for lag time ( $\lambda$ ), the time elapsed  
433 between addition of hydrocarbon and appearance of measureable  $CH_4$ . In fact, lag times of 5-15  
434 years were observed between the inauguration of OSTP and the first observation of ebullition at  
435 the pond surface (Foght et al., 2017), likely reflecting the time required for establishment of

436 efficient methanogenic communities. However, this variable is likely relevant only to laboratory  
437 studies, due to disruption of the microbial consortia during initiation of the cultures, and to newly  
438 established OSTP and EPL when transfer of tailings begins. After onset of CH<sub>4</sub> production,  
439 OSTP subsequently do not exhibit any apparent lag phases because of continuous diluent input  
440 and  $\lambda=0$  in-situ. (4) Small scale culture bottles facilitate release of CH<sub>4</sub> from MFT to the  
441 headspace for measurement compared with static deep strata in OSTP and EPL that experience  
442 physical retention of GHG as methane voids (Guo, 2009). That is, the model predicts CH<sub>4</sub>  
443 production based on 100% release from MFT; the proportion of gas released to the pond surface  
444 versus that retained under hydraulic pressure in-situ is not a component of the model. (5)  
445 Methanogenesis depends completely upon the microbial community composition, which is  
446 complex (An et al., 2013) and specific to each OSTP and EPL (Wilson et al., 2016), and may  
447 diverge from cultured communities during incubation. Although some diversity data exist both  
448 for cultures and various MFT, the model does not include parameters to account for the presence  
449 or abundance of ‘keystone’ microbial species because, in tailings, such species currently are  
450 incompletely known or identified. Significant efforts in research and testing would be required to  
451 integrate microbial community analysis into any CH<sub>4</sub> model for oil sands operations. (6) Finally,  
452 the model does not currently include parameters that reflect potential changes to ore processing  
453 or OSTP practices such as subtle alterations in diluent composition, intermittent deposition of  
454 chemicals from related processes (e.g., ammonium; Foght et al., 2017), changes in froth  
455 treatment water temperature, etc.

### 456 *3.4 Qualitative test of model prediction*

457 Despite the inferred shortcomings of applying the model to field predictions, and in anticipation  
458 of acquiring in-situ measurements to provide parameters for use in future for field modeling, it is

459 possible to conduct a qualitative test of the stoichiometric model to determine whether it predicts  
460 expected trajectories under different expected field scenarios, e.g., limiting  $C_T$  and/or  $N_A$   
461 conditions. Whereas cultures receive hydrocarbons in excess of instantaneous microbial demand  
462 at the beginning of incubation, as do the upper strata of active OSTP, labile carbon may become  
463 limiting in lower (older) strata of OSTP and eventually in EPL and cultures, where diluent is not  
464 replenished. Similarly, cultures initially receive a very small but finite amount of soluble  
465 nitrogen and have a headspace of  $N_2$  gas (which may serve as a nitrogen source for tailings  
466 microbiota; Collins et al., 2016) but the lower strata of OSTP and EPL have no obvious input of  
467 biologically available nitrogen ( $N_A$ ). Therefore this nutrient (or others, currently unidentified)  
468 may become limiting with time. Thus, challenging a model developed using culture data with  
469 scenarios reflecting in-situ conditions should reveal the strength of the model. Phase plane  
470 analyses of eight forms of potential solutions of the stoichiometric model are shown in Figures  
471 S7 and S8 and described in Supplemental Material section S3. The model outputs describe the  
472 expected trajectories of OSTP and EPL under carbon and/or nitrogen limitation, solving for  
473 biomass and total carbon in the system with time, i.e., the sum of all microbial activity in-situ.  
474 The predicted behaviour of OSTP with continuous diluent input differs from EPL with no  
475 additional hydrocarbon input, and the effect of limiting nutrient (nitrogen) also changes the  
476 ultimate endpoints of biomass and carbon in the two scenarios. These outputs qualitatively  
477 support the validity of the model as well as indicating that the stoichiometric model could be  
478 used to predict specific OSTP and EPL behaviour, to predict the volumes of 'legacy'  $CH_4$  from  
479 OSTP and long-term duration of  $CH_4$  production in-situ (particularly from EPL), and to  
480 influence decisions about oil sands reclamation strategies. If additional in-situ model parameters  
481 are acquired, the model can be further refined to improve predictive power.

## 482 **4. Conclusions**

483 The stoichiometric model represents a significant advance over previous zero- and first-order  
484 kinetic models, particularly because it predicts well the GHG emissions from different operators  
485 using distinct diluents that may support different rates of CH<sub>4</sub> production or may ultimately  
486 generate greater CH<sub>4</sub> emissions. Application of the model to in-situ CH<sub>4</sub> production is still  
487 hampered by limited experimental data and field measurements; some of these gaps may be  
488 alleviated as relevant in-situ data are acquired and when future anaerobic studies provide both  
489 evidence for susceptibility of additional hydrocarbons to biodegradation and more precise values  
490 for model parameters. The model is sufficiently flexible that additional parameters can be added  
491 to the modules as laboratory or field data become available. Until such time, the stoichiometric  
492 model should assist regulators and oil sands operators in qualitatively assessing long-term GHG  
493 emissions from oil sands tailings deposits and EPL reclamation sites.

## 494 **Appendix A. Supplementary Material**

495 This manuscript is accompanied by Supplementary Material comprising stability analysis of our  
496 System, eight tables (Tables S1-S8) and eight figures (Figure S1-S8).

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600

601 **Table 1:** Definition of terms used in model development

Term	Definition
$C_i$	mass of individual labile hydrocarbons in the system, where $i=1 \dots n$ , assuming $n$ labile hydrocarbons in system *
$C_i^{in}$	mass of $C_i$ inflow to the system
$C_T$	total mass of labile (biodegradable) hydrocarbon in the system (i.e., the sum of all $C_i$ )
$\mu$	specific microbial growth rate of microbes (bacteria and archaea) supported by $C_T$
$\mu_i$	specific microbial growth rate supported by each labile hydrocarbon $C_i$
$N_T$	total mass of nitrogen in the system
$N_A$	mass of $N_T$ that is biologically available §
$B$	total biomass of living microbes
$b$	biomass of dead microbes
$\beta_i$	the proportion of $C_i$ contained in dead biomass that is available for microbial recycling
$\theta$	the ratio of nitrogen to carbon associated with microbial biomass $B$
$r$	proportionality constant defining efficiency of conversion of $C_T$ to $B$
$r_i$	proportionality constant defining efficiency of conversion of each $C_i$ to $B$ ; $r_i = B / C_i$ consumed
$\lambda_i$	lag period before the onset of biodegradation of each $C_i$
$d$	microbial cell death rate
$K_f$	$N_A$ -dependent half-saturation constant
$K_{gi}$	$C_i$ -dependent half-saturation constant
$\Gamma_i$	expected yield of $CH_4$ from biodegradation of one mole of $C_i$
$G_i$	Total $CH_4$ and $CO_2$ generated from the biodegradation of $C_i$
$\eta$	fraction of sum of $\Gamma_i$ for all $i$ , yielded by biodegradation of $C_T$ ; i.e., methane bioconversion efficiency factor
$\eta_i$	fraction of $\Gamma_i$ yielded by biodegradation of each $C_i$

602 \*, in developing the current model, we considered 18 specific hydrocarbons present in naphtha  
 603 and paraffinic diluents (see Table 2)

604 §, e.g., nitrate, nitrite, ammonium, dinitrogen ( $N_2$  gas), labile organic N compounds (e.g.,  
 605 macromolecules in biomass), but not complex molecules (e.g., resins found in bitumen)

606 **Table 2:** List of 18 labile diluent hydrocarbons used in model development, sources of data and  
 607 type of tailings used to generate data for the biodegradation module and to estimate model  
 608 parameter values, and the model parameters estimated using those data (see Table S4 for  
 609 parameter definitions and values).  
 610

Hydrocarbon	Source of data	Type of tailings	Parameters estimated from the data
<i>n</i> -Alkanes			
C <sub>5</sub>	Mohamad Shahimin et al. (2016)	CNUL	$K_{g_{C_5}}$ and C <sub>5</sub> -lag
C <sub>6</sub> , C <sub>7</sub> , C <sub>8</sub> , C <sub>10</sub>	Siddique et al. (2006)	Syncrude	B(0), $K_f$ , $N_T$ , $K_{g_{C_6}}$ , $K_{g_{C_7}}$ , $K_{g_{C_8}}$ , $K_{g_{C_{10}}}$ , C <sub>6</sub> -lag, C <sub>7</sub> -lag, C <sub>8</sub> -lag and C <sub>10</sub> -lag.
C <sub>9</sub>	Table S1	Syncrude	$K_{g_{C_9}}$ and C <sub>9</sub> -lag
<i>iso</i> -Alkanes *			
2-MC <sub>6</sub> <sup>§</sup> , 3-MC <sub>6</sub> , 2-MC <sub>7</sub> , 4-MC <sub>7</sub> , 2-MC <sub>8</sub> , 3-MC <sub>8</sub> <sup>§</sup> , 2-MC <sub>9</sub> <sup>§</sup> ,	Siddique et al., unpublished	Syncrude	$K_{g_{3-MC_6}}$ , $K_{g_{2-MC_7}}$ , $K_{g_{4-MC_7}}$ , $K_{g_{2-MC_8}}$ , 3-MC <sub>6</sub> -lag, 2-MC <sub>7</sub> -lag, 4-MC <sub>7</sub> -lag, and 2-MC <sub>8</sub> -lag
2-MC <sub>5</sub>	Mohamad Shahimin and Siddique (2017a)	CNUL	$K_{g_{2-MC_5}}$ and 2-MC <sub>5</sub> -lag
Monoaromatics			
Toluene, <i>o</i> -Xylene, <i>m</i> - plus <i>p</i> -Xylene	Siddique et al. (2007)	Syncrude	$K_{g_{toluene}}$ , $K_{g_{o-xylene}}$ , $K_{g_{mp-xylene}}$ , toluene-lag, <i>o</i> -xylene-lag, and <i>m,p</i> -xylene-lag

611  
 612 \* M denotes a methyl group; i.e., 2-MC<sub>6</sub> is 2-methylhexane, etc. See Methods section 2.3.1 for  
 613 full list of abbreviations

614 § The values of model parameters  $K_g$  and lag for 2-MC<sub>6</sub>, 3-MC<sub>8</sub> and 2-MC<sub>9</sub> are not available  
 615 from empirical studies and are assumed to be the same as those for 3-MC<sub>6</sub>, 2-MC<sub>8</sub> and 2-MC<sub>8</sub>,  
 616 respectively, due to their similar molecular weights.

617 **Table 3:** Normalized mean square error (NMSE) analysis of model predictions and measured  
 618 CH<sub>4</sub> production from laboratory cultures comprising three MFT samples incubated with their  
 619 cognate diluents. The zero- and first-order models were implemented as described by Siddique et  
 620 al. (2008) using data reported in the current study. See Figures 1 and S6 for graphical  
 621 comparison of model outputs.

	<b>NMSE values</b>		
	MFT source and diluent type		
	<b>Syncrude</b>	<b>CNUL</b>	<b>CNRL</b>
Model	<b>Naphtha diluent</b>	<b>Paraffinic diluent</b>	<b>Naphtha diluent</b>
Zero-order	-0.28	-1.00	-1.10
First-order	-0.65	0.82	0.61
Stoichiometric	0.81	0.98	0.97

622

623 **Table 4:** Comparison of cumulative field measurements of CH<sub>4</sub> emissions in 2016 and 2017 in  
 624 three OSTP versus stoichiometric model predictions of cumulative in-situ CH<sub>4</sub> emissions from  
 625 those OSTP.

Operator and OSTP (date)	Field measurements of CH <sub>4</sub> emissions (moles x 10 <sup>6</sup> ) *	Stoichiometric model predictions of methane emissions (moles x 10 <sup>6</sup> )	Proportion of field emissions predicted by model (%) §
Syncrude MLSB (2016)	1191	656	55
Syncrude MLSB (2017)	991	492	50
CNRL Horizon (2016)	336	321	95
CNRL Horizon (2017)	599	459	77
CNUL MRM (2016)	2634	445	17
CNUL MRM (2017)	1051	506	48

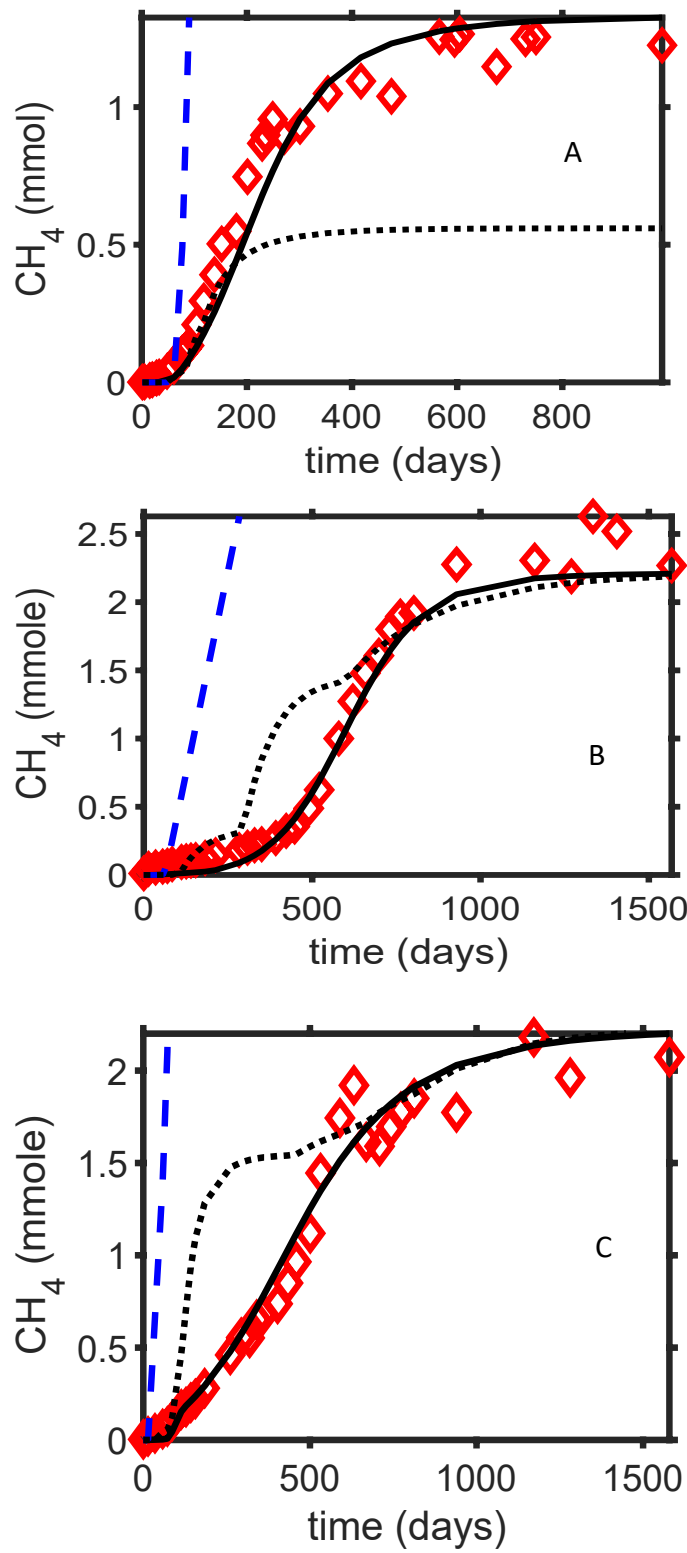
626 \* Unpublished surface flux measurements (Government of Alberta; raw data available upon  
 627 request), reported as tonnes and converted to moles at standard temperature and pressure

628 § for detailed calculations see Table S8



629 **FIGURE LEGEND**

630 **Figure 1:** Comparison of CH<sub>4</sub> production predicted by the stoichiometric model versus CH<sub>4</sub>  
631 measured in laboratory cultures independent of those used to generate the stoichiometric model  
632 and parameters (Table S4). Methane measurements (diamond symbols) are from cultures  
633 comprising: (A), Syncrude MFT incubated with its naphtha diluent (B), CNUL MFT incubated  
634 with its paraffinic diluent; and (C), CNRL MFT incubated with its naphtha diluent. Solid lines  
635 represent the stoichiometric model prediction; dashed lines and dotted lines respectively  
636 represent predictions made by applying the previous zero-order and first-order models  
637 ( Siddique et al., 2008) to the independent data set. The parameters values used in simulating  
638 the zero-order and first-order models were obtained from Siddique et al. (2008) and Table S5.



639  
640  
641

**Figure: 1**

642 **Appendix A:**

643 **Second-generation stoichiometric mathematical**  
644 **model to predict methane emissions from oil**  
645 **sands tailings**

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659

660 The following Supplementary Material contains the mathematical analysis of the system of

661 equations (2), eight tables (Tables S1- S8) and eight figures (Figures S1-S8).

662 **S1. Brief description of MFT laboratory culture methods used to generate**  
663 **data for model development and testing**

664 Details of laboratory culture preparation can be found in published papers ( Mohamad Shahimin  
665 et al., 2016; Mohamad Shahimin and Siddique, 2017a, 2017b, Siddique et al., 2007, 2006).  
666 Briefly and very generally, bulk samples of MFT were dispensed anaerobically into small serum  
667 bottles (microcosms) in replicate (typically triplicates) amended with an equal volume of sterile  
668 methanogenic medium comprising inorganic salts, trace vitamins, a redox indicator and sulfide  
669 as a reducing agent, but lacking organic carbon, and sealed under an atmosphere of 80% O<sub>2</sub>-free  
670 N<sub>2</sub>, balance CO<sub>2</sub>. The microcosms were allowed to incubate stationary in the dark at room  
671 temperature (ca. 22°C) for 2 weeks to acclimate, then the headspace was flushed with O<sub>2</sub>-free N<sub>2</sub>  
672 plus CO<sub>2</sub> to remove any CH<sub>4</sub> produced from endogenous substrates. The microcosms were then  
673 amended by injecting neat diluent supplied by the operator, or in one case defined mixtures of  
674 pure hydrocarbon constituents of the diluent (i.e., mixtures of *n*-alkanes or monoaromatics;  
675 Figure S6). During incubation headspace gases were sub-sampled at intervals for analysis by gas  
676 chromatography to determine cumulative CH<sub>4</sub> production. Likewise the MFT slurry was sub-  
677 sampled at intervals to analyze residual hydrocarbons using gas chromatography with mass  
678 spectrometry and thereby to calculate biodegradation by difference. Control microcosms  
679 containing MFT that had been heat-sterilized using an autoclave were included with each  
680 experiment to account for any abiotic losses of hydrocarbons.

681 **S2. Model development details**

682 ***S2.1 Mathematical analysis of the biodegradation module***

683 Here, a basic mathematical analysis of the system of equations (2) is provided. First we let C<sub>T</sub> to  
684 represent the sum of all the labile hydrocarbons in the system and the sum of all C<sub>i</sub><sup>in</sup> to be C<sub>T</sub><sup>in</sup>..  
685 We assume that  $\lambda_i = 0$ , for all i=1,2,3..n. This leads to a system of two differential equations.

Supplementary Material

686 To simplify our phase plane analysis in a meaningful way, we adjusted the second differential by  
 687 introducing a new variable:

688  $A = \frac{B}{r} + C_T$ . 'A' represents the sum of the total carbon available in the system and bacterial

689 biomass. We assume that  $f, g$  are linear and find their linear approximations:

690 
$$f(N_T - \theta B) \approx f(0) + f'(0)(N_T - \theta B)$$

691 
$$\Rightarrow f(N_T - \theta B) \approx \frac{N_T - \theta B}{K_f}$$

692 
$$g\left(A - \frac{B}{r}\right) \approx g(0) + g'(0)\left(A - \frac{B}{r}\right)$$

693 
$$\Rightarrow g\left(A - \frac{B}{r}\right) \approx \frac{A - \frac{B}{r}}{K_g}$$

694 We thus have the following system in which only one of the two differential equations has a  
 695 minimum function, greatly simplifying the analysis:

696 
$$\dot{A} = \frac{r-1}{r} dB + C_T^{in} = F(B) \quad (S1)$$

698 
$$\dot{B} = \mu B \min\left\{f(N_T - \theta B), g\left(A - \frac{B}{r}\right)\right\} - dB = BG(A, B).$$

697

699 Next, we look at the stability analysis of the system. For this purpose, we construct a phase plane  
 700 of the system, (i.e. a graph of the solution trajectories mapped out by points  $(A(t), B(t))$  as  $t$  varies  
 701 over  $(\infty, +\infty)$ ) in order to identify the steady state solutions. We call  $F(B) = 0$  and  $G(A, B) = 0$   
 702 (the lines on which trajectories are horizontal or vertical) the nullclines of system of equations  
 703 (S1). The steady state solutions are the points where the nullclines (but not different branches of  
 704 the same nullcline) cross each other. For the stability of the steady states, we compute the  
 705 Jacobian matrix corresponding to each equilibrium point  $J(A^*, B^*)$ , where  $(A^*, B^*)$  is a given

706 equilibrium point. We use the sign of the trace and determinant of  $J(A^*, B^*)$  to determine the  
 707 nature of the given equilibrium point. Let  $D = \det J(A^*, B^*)$  and  $T_r = \text{trace } J(A^*, B^*)$ . Note that:

708 1) If  $D < 0$ , the eigenvalues of  $J(A^*, B^*)$  are real and of opposite signs, and the phase  
 709 portrait is a saddle (which is always unstable).

710 2) If  $0 < D < \frac{T_r^2}{4}$ , the eigenvalues of  $J(A^*, B^*)$  are real, distinct, and of the same sign, and  
 711 the phase portrait is a node, stable if  $T_r < 0$  and unstable if  $T_r > 0$ .

712 3) If  $0 < T_r^2 < D$ , the eigenvalues of  $J(A^*, B^*)$  are neither real nor purely imaginary, and  
 713 the phase portrait is a spiral, stable if  $T_r < 0$  and unstable if  $T_r > 0$ . Using this idea, we  
 714 carried out the analysis as follows:

715

716 **S2.2 Stability Analysis of OSTP system ( $C_T^{in} \neq 0$ )**

717 **Steady states:**

718 **A-Nullclines:**

719  $\dot{A} = 0, \Rightarrow B = \frac{rC_T^{in}}{d(1-r)}.$

720 **B-Nullclines:**

721  $\dot{B} = 0, \Rightarrow B = 0 \text{ or } G(A, B) = 0.$

722 
$$G(A, B) = 0, \Rightarrow \begin{cases} B = Ar - \frac{dk_g r}{\mu} \text{ if } \frac{N_T - \theta B}{k_f} > \frac{A - \frac{B}{r}}{k_g} \\ B = \left(N_T - \frac{dk_f}{\mu}\right) \frac{1}{\theta} \text{ if } \frac{N_T - \theta B}{k_f} < \frac{A - \frac{B}{r}}{k_g} \end{cases}$$

723 **Case 1:** Suppose  $\theta - \frac{k_f}{k_g r} > 0$ , then

$$724 \quad G(A, B) = 0, \Rightarrow \begin{cases} B = Ar - \frac{dk_g r}{\mu} \text{ if } B < \left(N_T - \frac{Ak_f}{k_g}\right) \left(\frac{k_g r}{\theta k_g r - k_f}\right) \\ B = \left(N_T - \frac{dk_f}{\mu}\right) \frac{1}{\theta} \text{ if } B > \left(N_T - \frac{Ak_f}{k_g}\right) \left(\frac{k_g r}{\theta k_g r - k_f}\right) \end{cases}$$

725

726 **Case 1.1:** If  $C_T^{in} > \frac{d(1-r)}{r\theta} \left(N_T - \frac{dk_f}{\mu}\right)$ , there will be no intersection between the  $A$  and  $B$ -  
727 nullclines as shown in Panel A of Figure S7. Hence the system will have no equilibrium point.

728

729 **Case 1.2:** If  $C_T^{in} < \frac{d(1-r)}{r\theta} \left(N_T - \frac{dk_f}{\mu}\right)$ , the two nullclines will intersect at one unique point  $E_1 =$

730  $\left(\frac{\mu C_T^{in} + d^2 k_g (1-r)}{d(1-r)\mu}, \frac{r C_T^{in}}{d(1-r)}\right)$  as shown in Panel B of Figure S7. Hence if

731  $C_T^{in} < \frac{d(1-r)}{r\theta} \left(N_T - \frac{dk_f}{\mu}\right)$ , the system will have a unique internal equilibrium point  $E_1$ .

732

733 **Case 1.3:** If  $C_T^{in} = \frac{d(1-r)}{r\theta} \left(N_T - \frac{dk_f}{\mu}\right)$ , the two nullclines will intersect on the line

734  $\left\{\left(A, \left(T - \frac{dk_f}{\mu}\right) \frac{1}{\theta}\right) : A > \frac{1}{r} \left[\left(T - \frac{dk_f}{\mu}\right) \frac{1}{\theta} + \frac{dk_g r}{\mu}\right]\right\}$  as can be seen in Panel A of Figure S8.

735 Consequently, If  $C_T^{in} = \frac{d(1-r)}{r\theta} \left(N_T - \frac{dk_f}{\mu}\right)$ , the system will have an infinite number of

736 equilibrium points  $E_2 = \left\{\left(A, \left(N_T - \frac{dk_f}{\mu}\right) \frac{1}{\theta}\right) : A > \frac{1}{r} \left[\left(N_T - \frac{dk_f}{\mu}\right) \frac{1}{\theta} + \frac{dk_g r}{\mu}\right]\right\}$

737

738 **Case 2:** Suppose  $\theta - \frac{k_f}{k_g r} < 0$ , then

$$739 \quad G(A, B) = 0, \Rightarrow \begin{cases} B = Ar - \frac{dk_g r}{\mu} \text{ if } B > \left(N_T - \frac{Ak_f}{k_g}\right) \left(\frac{k_g r}{\theta k_g r - k_f}\right) \\ B = \left(N_T - \frac{dk_f}{\mu}\right) \frac{1}{\theta} \text{ if } B < \left(N_T - \frac{Ak_f}{k_g}\right) \left(\frac{k_g r}{\theta k_g r - k_f}\right). \end{cases}$$

740

741 Note that the slope of the line  $B = Ar - \frac{dk_g r}{\mu}$  is less than that of  $B = \left(N_T - \frac{Ak_f}{k_g}\right) \left(\frac{k_g r}{\theta k_g r - k_f}\right)$ ,

742 since  $\frac{k_f}{k_f - \theta k_g r} > 1$ . Therefore, the point where the line  $B = Ar - \frac{dk_g r}{\mu}$  intersects the A-axis,  $\frac{dk_g}{\mu}$ ,

743 must be less than  $\frac{Tk_g}{k_f}$ , the point where the  $B = \left(N_T - \frac{Ak_f}{k_g}\right) \left(\frac{k_g r}{\theta k_g r - k_f}\right)$  intersect the A-axis, for

744 the two lines to intersect on the first quadrant.

745

746 **Case 2.1:** If  $C_T^{in} > \frac{d(1-r)}{r\theta} \left(N_T - \frac{dk_f}{\mu}\right)$ , as with Case 1.1, there will be no intersection between

747 the A and B-nullclines as shown in Panel B of Figure S8. Hence the system will have no

748 equilibrium point.

749

750 **Case 2.2:**  $C_T^{in} < \frac{d(1-r)}{r\theta} \left(N_T - \frac{dk_f}{\mu}\right)$ , the two nullclines will intersect at one unique point  $E_3 =$

751  $\left(\frac{\mu C_T^{in} + d^2 k_g (1-r)}{d(1-r)\mu}, \frac{r C_T^{in}}{d(1-r)}\right)$  as shown in Panel C of Figure S8. Hence if  $\theta C_T^{in} < \frac{d(1-r)}{r\theta} \left(N_T - \frac{dk_f}{\mu}\right)$ ,

752 the system will have a unique internal equilibrium point  $E_3$ .

753

754 **Case 2.3:** If  $C_T^{in} = \frac{d(1-r)}{r\theta} \left(N_T - \frac{dk_f}{\mu}\right)$ , the two nullclines will intersect on the line

755  $\left\{ \left(A, \left(N_T - \frac{dk_f}{\mu}\right) \frac{1}{\theta}\right) : A > \frac{1}{r} \left[ \left(N_T - \frac{dk_f}{\mu}\right) \frac{1}{\theta} + \frac{dk_g r}{\mu} \right] \right\}$  as shown in Panel D of Figure S8. Thus, If

756  $C_T^{in} = \frac{d(1-r)}{r\theta} \left(N_T - \frac{dk_f}{\mu}\right)$ , the system will have an infinite number of equilibrium points  $E_4 =$

757  $\left\{ \left(A, \left(N_T - \frac{dk_f}{\mu}\right) \frac{1}{\theta}\right) : A > \frac{1}{r} \left[ \left(N_T - \frac{dk_f}{\mu}\right) \frac{1}{\theta} + \frac{dk_g r}{\mu} \right] \right\}$

758



759 Thus an OSTP system may have 0, 1, or an infinite number of equilibrium points depending on  
 760 the volume of fresh labile hydrocarbons input into the system,  $C_T^{in}$ . If  $C_T^{in} > \frac{d(1-r)}{r\theta} \left( N_T - \frac{dk_f}{\mu} \right)$ ,  
 761  $\frac{dk_f}{\mu}$ , the system will have no equilibrium point; if  $C_T^{in} < \frac{d(1-r)}{r\theta} \left( N_T - \frac{dk_f}{\mu} \right)$ , it will have one  
 762 unique equilibrium point,  $\left( \frac{\mu C_T^{in} + d^2 k_g (1-r)}{d(1-r)\mu}, \frac{r C_T^{in}}{d(1-r)} \right)$ ; and if  $\frac{r C_T^{in}}{d(1-r)} = \left( N_T - \frac{dk_f}{\mu} \right) \frac{1}{\theta}$ , it will have an  
 763 infinite number of equilibrium points given by  $\left\{ \left( A, \left( N_T - \frac{dk_f}{\mu} \right) \frac{1}{\theta} \right) : A > \frac{1}{r} \left[ \left( N_T - \frac{dk_f}{\mu} \right) \frac{1}{\theta} + \frac{dk_g r}{\mu} \right] \right\}$ .

765

766 ***S2.2.1 Stability of equilibrium points in OSTP scenario:***

767 To determine the local stability of the equilibria above, we consider the Jacobian matrix of  
 768 System of equations (S1),

769 
$$J(A, B) = \begin{pmatrix} 0 & \frac{(r-1)d}{r} \\ BG_A(A, B) & G(A, B) + BG_B(A, B) \end{pmatrix} \quad (S1.)$$

770 Where

772 
$$G(A, B) = \begin{cases} \frac{\mu \left( A - \frac{B}{r} \right)}{k_g} - d \text{ if } \frac{N_T - \theta B}{k_f} > \frac{A - \frac{B}{r}}{k_g} \\ \frac{\mu(N_T - \theta B)}{k_f} - d \text{ if } \frac{N_T - \theta B}{k_f} < \frac{A - \frac{B}{r}}{k_g}, \end{cases}$$

773 
$$G_A(A, B) = \begin{cases} \frac{\mu}{k_g} \text{ if } \frac{N_T - \theta B}{k_f} > \frac{A - \frac{B}{r}}{k_g} \\ 0 \text{ if } \frac{N_T - \theta B}{k_f} < \frac{A - \frac{B}{r}}{k_g} \end{cases}$$

771 and

$$G_B(A, B) = \begin{cases} \frac{-\mu}{k_g} \text{ if } \frac{N_T - \theta B}{k_f} > \frac{A - \frac{B}{r}}{k_g} \\ \frac{-\theta}{k_f} \text{ if } \frac{N_T - \theta B}{k_f} < \frac{A - \frac{B}{r}}{k_g} \end{cases}$$

775

776 **Stability of  $E_1$ :**

$$J(E_1) = \begin{pmatrix} 0 & \frac{(r-1)d}{r} \\ \frac{\mu r C_T^{in}}{k_g d(1-r)} & \frac{-C_T^{in} \mu}{d(1-r)k_g} \end{pmatrix} \quad (S2.)$$

778 Since  $\det(J(E_1)) = \frac{\mu C_T^{in}}{k_g}$  is greater than zero and  $T_r(J(E_1)) = \frac{-C_T^{in} \mu}{d(1-r)k_g} < 0$ , this implies that

779 both eigenvalues of  $J(E_1)$  have negative real parts. Hence  $E_1$  is a locally stable equilibrium

780 point. It is easy to see that  $E_1$  is a stable spiral.

781

782 **Stability of  $E_2$ :**

$$J(E_2) = \begin{pmatrix} 0 & \frac{(r-1)d}{r} \\ 0 & \frac{-r C_T^{in} \mu \theta}{d(1-r)k_f} \end{pmatrix} \quad (S3.)$$

784  $\det(J(E_2)) = 0$  and  $T_r(J(E_2)) = \frac{-r C_T^{in} \mu \theta}{d(1-r)k_f} < 0$ .

785

786 Since the  $T_r(J(E_2))$  is negative and  $\det(J(E_2))$  is zero, one eigenvalue is zero and the other is

787 negative. Thus  $E_2$  is a line of locally asymptotically stable equilibrium points. Hence both the

788 internal equilibrium point  $E_1$  and the line of equilibrium points  $E_2$  are locally asymptotically  
 789 stable.

790

791 **S2.2.2 End pit lake scenario ( $C_T^{in} = 0$ ):**

792 **Steady states:**

793 **A-Nullclines:**

$$794 \quad \dot{A} = 0 \implies B = 0$$

795 **B-Nullclines:**

$$796 \quad \dot{B} = 0 \implies B = 0 \text{ or } G(A, B) = 0.$$

797

798 Panels C and D of Figure S7 show that, irrespective of the slope of the line  $B = Ar - \frac{dk_g r}{\mu}$ , the

799 A- and B-nullclines have an infinite number of intersections, given by

800  $E_5 = \{(A, 0) : A \geq 0\}$ . Thus for  $C_T^{in} = 0$ , system of equations (S1) has an infinite number of  
 801 equilibrium points given by  $E_5$ .

802

803 **Stability of  $E_5$ :**

$$804 \quad J(E_5) = \begin{pmatrix} 0 & \frac{(r-1)d}{r} \\ 0 & \frac{\mu A}{k_g} - d \end{pmatrix} \quad (4.)$$

805  $\det(J(E_5)) = 0$  and  $T_r(J(E_5)) = \frac{\mu A}{k_g} - d$ . If  $A < \frac{dk_g}{\mu}$ ,  $T_r(J(E_5))$  will be less than zero and hence

806  $E_5$  will be asymptotically stable. On the other hand, if  $A \geq \frac{dk_g}{\mu}$ , then  $T_r(J(E_5))$  will be greater

807 than 0 and thus  $E_5$  will be a line of unstable equilibrium points.

### 808 S3. Qualitative challenge of model prediction

809 Figures S7 and S8 show eight theoretical in-situ scenarios presented as phase plane  
 810 diagrams showing solutions for microbial biomass versus total carbon content (both unitless)  
 811 under conditions of carbon or nitrogen limitation. The directional arrows account for time,  
 812 nullclines define the vector fields, and nullcline intersections (fixed points) indicate regions  
 813 where trajectories are horizontal or vertical; i.e., steady states. Panels S7A, S7B and S8A-S8D  
 814 are relevant to the upper strata of OSTP where the input of labile hydrocarbon is continuous (i.e.  
 815  $C_T^{in} > 0$ ) whereas Panels S7C and S7D represent an established EPL where labile carbon (as  
 816 partially biodegraded diluent) enters the system with deposited MFT but is not replenished (i.e.,  
 817  $C_T^{in} = 0$ ) Furthermore, the availability of nitrogen ( $N_A$ ) differs for each panel, as described  
 818 below.

819 Let  $C_0^{in}$ ,  $C_1^{in}$  and  $C_2^{in}$  denote sums of labile hydrocarbons with values  $\left(N_T - \frac{dk_f}{\mu}\right) \frac{d(1-r)}{\theta r}$ ,  
 820  $\left(\frac{C_T^{in}}{d(1-r)} + \frac{dk_g}{\mu}\right)$  and  $\frac{1}{r} \left[\left(T - \frac{dk_f}{\mu}\right) \frac{1}{\theta} + \frac{dk_g r}{\mu}\right]$  respectively. Also, let  $B_0$  and  $B_1$  denote two  
 821 different values of bacterial biomass.  $B_0 = \left(N_T - \frac{dk_f}{\mu}\right) \frac{1}{\theta}$  and  $B_1 = \frac{d(1-r)}{\theta r}$ . Figures S7A and S8B  
 822 show the predicted behaviour of OSTP in which the rate of input of hydrocarbons into the OSTP  
 823 per unit time is  $> C_0^{in}$ . In this scenario, biomass moves towards  $B_0$  (i.e., steady state). As  
 824 biomass stabilizes, nitrogen becomes the limiting factor in microbial growth and thus bacteria  
 825 consume only the amount of hydrocarbon permitted by  $N_A$ . This leads to an accumulation of  
 826 hydrocarbon in the system due to the continuous influx of diluent and inability of bacteria to  
 827 degrade all the carbon input. Such a scenario would require addition of  $N_A$  to the ponds to  
 828 achieve additional diluent consumption, if that was the management goal. Conversely, restricting  
 829  $N_A$  in the pond should decrease  $CH_4$  and  $CO_2$  emissions although the potential for gas biogenesis

830 would persist for an indefinite period. Figures S7B and S8D illustrates the case of an OSTP  
831 where the rate of input of hydrocarbons into the OSTP per unit time is  $< C_0^{in}$ . In this case,  
832 biomass moves to a value of  $B_1$  and total  $C_T^{in}$  moves to  $C_1^{in}$ . Because the total labile hydrocarbon  
833 deposited into the pond per unit time  $C_T^{in}$  is  $< C_0^{in}$ , carbon becomes the limiting factor for  
834 bacterial growth. Thus, biomass will increase to achieve a steady state at which carbon intake is  
835 maximized and all  $C_T$  is degraded as it enters the system. This scenario requires a continuous  
836 (but currently undiscovered) source of  $N_A$  in the tailings or the addition of exogenous  $N_A$ , i.e., as  
837 a management practice. The final possible scenario in OSTP is that depicted in Figures S8A and  
838 S8C. As with the other two cases above, we are equally looking at the OSTP as defined by the  
839 continuous input of carbon. Here the rate of input of hydrocarbons into the OSTP per unit time is  
840  $C_0^{in}$ . At this influx value per unit time, nitrogen would be the limiting element for microbial  
841 growth. In this scenario, we have microbes growing to  $B_0$ , a point where they can maximize they  
842 nitrogen intake. Carbon in turn changes to a value that is greater than  $C_2^{in}$ .

843 The scenarios in Figures S7C and S7D simulate EPL conditions because  $C_T^{in} = 0$ . With  
844 extended time,  $C_T$  will approach a minimum (theoretically zero) as  $C_T$  is converted to  $CH_4$  and  
845 dead biomass is likewise degraded after labile hydrocarbons are depleted. Figure S7C describes a  
846 scenario where the ratio of the nitrogen carrying capacity to carbon carrying capacity of the pond  
847 is  $< \theta r$ . Since there is no supply of exogenous carbon to the system, when the bacteria degrade  
848 all residual diluent, they ultimately have no carbon source other than dead biomass, which is  
849 converted to  $CH_4$  and  $CO_2$ ; eventually gas generation ceases in this closed system. Figure S7D  
850 predicts the situation where the ratio of the nitrogen carrying capacity to carbon carrying  
851 capacity of the pond is  $> \theta r$  but  $C_T$  still approaches zero because of the complete conversion of  
852  $C_T$  and  $\beta_T dB$  to gases, where  $\beta_T$  is the proportion of  $C_T$  contained in dead biomass that is

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- 853 available for microbial recycling. Note that in the interim, biomass was greater than in Figure
- 854 S7C because of the continuous presence of  $N_A$ .

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896 **Table S1:** Biodegradation and cumulative CH<sub>4</sub> production in cultures of Syncrude MFT  
 897 incubated with Syncrude naphtha diluent.

Hydrocarbon (mg L <sup>-1</sup> )	Incubation period (days)									
	28	77	142	216	249	271	365	475	605	730
Toluene	46.0	38.2	0	0	0	0	0	0	0	0
Ethylbenzene	19.0	21.6	15.2	0	0	0	0	0	0	0
<i>m-,p</i> -Xylenes	35.0	46.2	35.0	36.9	28.7	10.1	7.7	0	0	0
<i>o</i> -Xylene	14.0	17.7	11.3	0	0	0	0	0	0	0
<i>n</i> -Hexane	5.0	2.5	2.7	1.2	0.7	0.4	0.4	0.3	0.3	0
<i>n</i> -Heptane	34.0	18.2	13.9	6.5	3.7	2.3	1.0	2.6	0	0
<i>n</i> -Octane	46.0	30.2	23.9	13.8	8.0	4.5	2.5	0	0	0
<i>n</i> -nonane	15.0	15.2	6.2	3.5	1.3	0	0	0	0	0
2-Methylhexane (2-MC <sub>6</sub> )	10.0	6.8	6.0	6.9	6.4	5.3	4.7	5.7	2.7	1.6
3-Methylhexane (3-MC <sub>6</sub> )	12.0	8.2	7.7	6.7	5.5	2.4	3.2	2.7	1.9	1.9
2-Methylheptane (2MC <sub>7</sub> )	37.0	25.0	22.1	25.5	23.8	19.7	17.3	21.3	10.2	5.8
4-Methylheptane (4-MC <sub>7</sub> )	14.0	9.6	8.4	8.4	4.4	3.5	4.4	4.5	3.4	0
<b>Cumulative CH<sub>4</sub> production (μmol) *</b>	16	114	416	774	955	893	1049	1039	1266	1248

898 \* Cumulative methane is calculated by subtracting CH<sub>4</sub> produced by parallel endogenous control  
 899 cultures (i.e., MFT not receiving additional naphtha) from CH<sub>4</sub> measured in test cultures (MFT  
 900 receiving naphtha).

901 **Table S2:** Literature values for selected microbial parameters in system of equations (2)

<b>Parameter *</b>	<b>Value Range</b>	<b>Unit</b>	<b>References</b>
$\mu$	1-4	d <sup>-1</sup>	(Codeco and Grover, 2001; Connolly et al., 1992)
$r$	0.31-0.75	– §	(Del Giorgio and Cole, 1998; Wang et al., 2009)
$\theta$	$\frac{1}{9} - \frac{1}{4}$	– §	(Sterner and Elser, 2002)

902 \* see Table 1, main text, for parameter definitions

903 –, unitless parameters

904 **Table S3:** Normalized mean square error (NMSE) values obtained by comparing the simulated  
905 biodegradation kinetics (generated using the system of equations (2) and parameter values in  
906 Table S4) to published experimental data for the 15 labile hydrocarbons (Table 2).  
907

Hydrocarbon *	NMSE
<i>n</i> -Pentane	0.92
<i>n</i> -Hexane	0.99
<i>n</i> -Heptane	0.99
<i>n</i> -Octane	0.99
<i>n</i> -Nonane	0.98
<i>n</i> -Decane	0.99
Toluene	1.00
<i>o</i> -Xylene	1.00
<i>m</i> - plus <i>p</i> -Xylene	0.99
2-Methylpentane	1.00
3-Methylhexane	0.99
2-Methylheptane	0.95
4-Methylheptane	0.98
2-Methyloctane	0.85

908 \*, NMSE values for 2-methylhexane, 2-methyloctane and 2-methylnonane cannot be calculated  
909 because the model-related parameter values for these hydrocarbons are not available from our  
910 laboratory experiments.

911 **Table S4:** Model parameters and their estimated values obtained from fitting data to the  
 912 solutions of the systems of equation (3).  
 913

Parameter *	Value	95% C.I.	Unit
$B(0)$	0.0004	0.0001-0.0138	mmol C
$K_f$	0.3	0.3	mmol
$N_T$	327.6	327.1	mmol
$K_{gC_5}$	56.3	16.2-96.4	mmol
$K_{gC_6}$	430.3	366.1-494.5	mmol
$K_{gC_7}$	270.7	238.9-302.5	mmol
$K_{gC_8}$	90.1	69.3-110.9	mmol
$K_{gC_9}$	0.9	0.71-1	mmol
$K_{gC_{10}}$	12.0	10.2-13.9	mmol
$K_{g\text{toluene}}$	4.5	4.1-4.8	mmol
$K_{g\text{m,p-Xylenes}}$	85.1	76.9-93.2	mmol
$K_{g\text{o-Xylenes}}$	17.5	14.2-20.8	mmol
$K_{g2-MC_6}$ §	144.6	102.7-186.5	mmol
$K_{g3-MC_6}$	144.6	102.7-186.5	mmol
$K_{g2-MC_7}$	320.4	183.8-457.1	mmol
$K_{g4-MC_7}$	170.3	121.0-219.7	mmol
$K_{g2-MC_8}$	335.9	179.1-492.9	mmol
$K_{g3-MC_8}$ §	335.9	179.1-492.9	mmol
$K_{g2-MC_9}$ §	335.9	179.1-492.9	mmol
$K_{g2-MC_5}$	165.9	130.2-201.7	mmol
$C_5 - \text{lag}$	200	200	days
$C_6 - \text{lag}$	26	26	days
$C_7 - \text{lag}$	60	40-80	days
$C_8 - \text{lag}$	60	60	days
$C_9 - \text{lag}$	70	70	days
$C_{10} - \text{lag}$	5	5	days
$\text{Toluene} - \text{lag}$	30	30	days
$m - \text{and } p$ $- \text{Xylenes} - \text{lag}$	70	70	days
$o - \text{Xylenes} - \text{lag}$	60	60	days
$2 - \text{MC}_6 - \text{lag}$ §	25	25	days
$3 - \text{MC}_6 - \text{lag}$	25	25	days
$2 - \text{MC}_7 - \text{lag}$	25	25	days
$4 - \text{MC}_7 - \text{lag}$	25	25	days

<b>2 – MC<sub>8</sub> – lag</b>	25	25	days
<b>3 – MC<sub>8</sub> – lag §</b>	25	25	days
<b>2 – MC<sub>9</sub> – lag §</b>	25	25	days
<b>2 – MC<sub>5</sub> – lag</b>	23	23	days

914  
915 \*  $K_f$  represents the nitrogen-dependent half-saturation constant for microbial growth;  $N_T$  is the  
916 total nitrogen available in the system;  $K_{g_{C_5}}, K_{g_{C_6}}, K_{g_{C_7}}, K_{g_{C_8}}, K_{g_{C_9}}, K_{g_{C_{10}}}, K_{g_{toluene}},$   
917  $K_{g_{o-xylenes}},$   
918  $K_{g_{m,p-xylenes}}, K_{g_{2-MC_6}}, K_{g_{3-MC_6}}, K_{g_{2-MC_7}}, K_{g_{4-MC_7}}, K_{g_{2-MC_8}}, K_{g_{3-MC_8}}, K_{g_{2-MC_8}}, K_{g_{2-MC_9}},$   
919  $K_{g_{2-MC_5}}$  respectively represent the half-saturation constants for microbial growth on C<sub>5</sub>-, C<sub>6</sub>-,  
920 C<sub>7</sub>-, C<sub>8</sub>-, C<sub>9</sub>-, C<sub>10</sub>- *n*-alkanes, toluene, *o*-xylene, *m*- plus *p*-xylene, 2-methylhexane-, 3-  
921 methylhexane-, 2-methylheptane-, 4-methylheptane-, 2-methyloctane-, 3-methyloctane-, 2-  
922 methylnonane- and , 2-methylpentane-. *Z*-lag denotes a lag period of *Z*, where *Z* is one of C<sub>5</sub>, C<sub>6</sub>,  
923 C<sub>7</sub>, C<sub>8</sub>, C<sub>9</sub>, C<sub>10</sub>, toluene, *o*-xylene, *m*- plus *p*-xylene, 2-methylhexane-, 3-methylhexane, 2-  
924 methylheptane, 4-methylheptane, 2-methyloctane 3-methyloctane, 2-methylnonane or 2-  
925 methylpentane.  
926  
927 § The values of model parameters  $K_g$  and lag for 2-MC<sub>6</sub>, 3-MC<sub>8</sub> and 2-MC<sub>9</sub> were not available  
928 from empirical studies and are assumed to be the same as those for 3-MC<sub>6</sub>, 2-MC<sub>8</sub> and 2-MC<sub>8</sub>,  
929 respectively, based on their similar molecular weights.

930 **Table S5:** Estimated zero-and first-order model parameter values for labile diluent hydrocarbons  
931 not reported by Siddique et al. (2008).

932

Hydrocarbon	Lag phase (d)	Zero-order parameter (mmole d <sup>-1</sup> )	First-order parameter (d <sup>-1</sup> )
<i>n</i> -Pentane	294	0.0008576	0.01117
<i>n</i> -Nonane	77	2.664e-05	0.01276
2-Methylpentane	600	0.0002281	0.003501
3-Methylhexane	455	0.0001816	0.003849
2-Methylheptane	845	0.00023	0.005258
4-Methylheptane	665	0.0001936	0.005663
2-Methyloctane	665	0.0001772	0.0006584

933

934 **Table S6.** Calculation of mass balance of diluent entering OSTP in 2016 and 2017. These values  
 935 are used in Table S8 calculations.

936

	Syncrude MLSB		CNRL Horizon		CNUL MRM	
	2016	2017	2016	2017	2016	2017
Reported mass of diluent lost to fresh tailings before deposition in OSTP (t) <sup>a</sup>	57,336	43,032	24,722	35,295	28,558	32,494
Estimated mass of diluent lost from OSTP by volatilization (t) <sup>b</sup>	(-17,201)	(-12,910)	(-7,416)	(-10,589)	(-11,423)	(-12,998)
Calculated net mass of diluent remaining in OSTP (t)	40,135	30,122	17,305	24,706	17,135	19,496

937

938 a, Data retrieved from Alberta Energy Regulator ST 39 report (AER, 2018) and calculated using  
 939 the reported volume of diluent loss (m<sup>3</sup>) and multiplying by the respective densities of diluents  
 940 (Syncrude naphtha, 0.76 t m<sup>-3</sup>; CNRL naphtha, 0.73 t m<sup>-3</sup>; and CNUL paraffinic solvent, 0.65 t  
 941 m<sup>-3</sup> (Burkus et al., 2014).

942 b, A factor of 0.7 (i.e., 30% volatilization) was used for Syncrude and CNRL naphtha diluents  
 943 and a factor of 0.6 (i.e., 40% volatilization) was used for CNUL paraffinic diluent to calculate  
 944 the mass of diluent volatilized from OSTP per Burkus et al. (2014) .

945 **Table S7.** Concentrations of 18 labile hydrocarbons in diluents and calculated masses of labile  
 946 diluent hydrocarbons present in tailings entering OSTP in 2016 and 2017. Values are used in  
 947 Table S8 calculations.

Labile hydrocarbon	Syncrude MSLB			CNRL Horizon			CNUL MRM		
	% of naphtha diluent <sup>a</sup>	mass in OSTP (t) 2016 <sup>b</sup>	mass in OSTP (t) 2017 <sup>b</sup>	% of naphtha diluent <sup>a</sup>	mass in OSTP (t) 2016 <sup>b</sup>	mass in OSTP (t) 2017 <sup>b</sup>	% of paraffinic diluent <sup>a</sup>	mass in OSTP (t) 2016 <sup>b</sup>	mass in OSTP (t) 2017 <sup>b</sup>
Toluene	6.11	2452	1840	0	0	0	0	0	0
<i>m-, p</i> -Xylene	4.64	1862	1398	0	0	0	0	0	0
<i>o</i> -Xylene	1.78	714	536	0	0	0	0	0	0
<i>n</i> -C <sub>5</sub>	0	0	0	0	0	0	24.00	4112	4679
<i>n</i> -C <sub>6</sub>	0.60	241	181	3.85	666	951	11.26	1929	2195
<i>n</i> -C <sub>7</sub>	4.50	1806	1356	9.35	1618	2310	0	0	0
<i>n</i> -C <sub>8</sub>	6.05	2428	1822	4.65	805	1149	0	0	0
<i>n</i> -C <sub>9</sub>	1.99	799	599	1.70	294	420	0	0	0
<i>n</i> -C <sub>10</sub>	0.31	126	94	1.65	286	408	0	0	0
2-MC <sub>5</sub>	0	0	0	1.25	216	309	23.50	4027	4582
2-MC <sub>6</sub>	1.30	522	392	5.30	917	1309	0	0	0
3-MC <sub>6</sub>	1.51	607	456	5.05	874	1248	0	0	0
2-MC <sub>7</sub>	4.92	1976	1483	3.85	666	951	0	0	0
4-MC <sub>7</sub>	1.86	747	561	1.25	216	309	0	0	0
2-MC <sub>8</sub>	1.16	465	349	1.00	173	247	0	0	0
3-MC <sub>8</sub>	1.55	623	467	0.55	95	136	0	0	0
2-MC <sub>9</sub>	0.31	124	93	2.90	502	717	0	0	0
% of diluent considered labile	39			42			59		
Total mass of labile hydrocarbon entering OSTP (t)		15492	11627		7329	10463		10068	11456

948  
 949 <sup>a</sup> The concentrations of individual hydrocarbons in Syncrude and CNRL naphtha diluents were  
 950 calculated using PONA analysis reported by (Siddique et al., 2007) and (Mohamad Shahimin,  
 951 and Siddique, 2017b), respectively, and the concentrations of individual hydrocarbons in CNUL  
 952 paraffinic diluent were calculated using the PONA analysis reported by (Mohamad Shahimin  
 953 and Siddique, 2017a).

954 <sup>b</sup> The data were retrieved from Alberta Energy Regulator report ST 39 (AER, 2018)

955



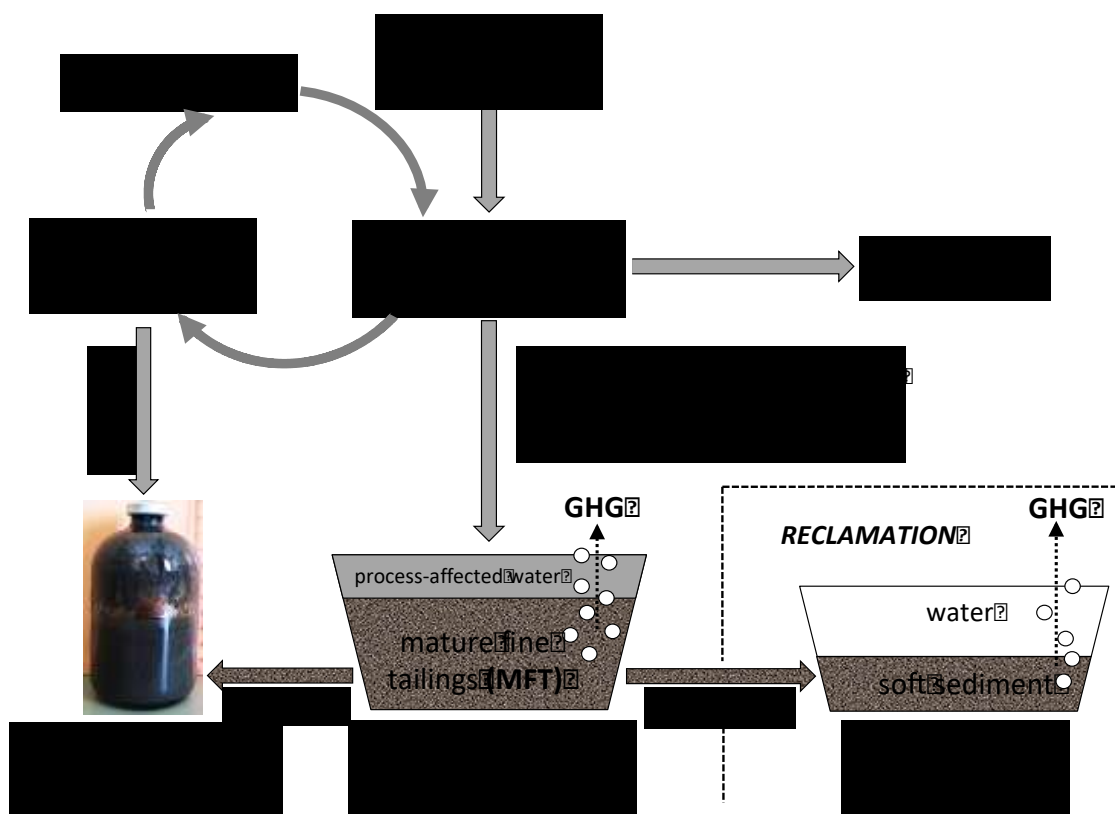
956 **Table S8:** Contribution of individual labile diluent hydrocarbons to the maximum theoretical  
 957 cumulative yield of CH<sub>4</sub> from OSTPs in 2016 and 2017, based on masses calculated in Tables S5  
 958 and S6). Methane yield was calculated using equation (4) in main text, per Symons and Buswell  
 959 (1933) as implemented by Roberts (2002).

Labile hydrocarbon	Calculated theoretical methane production (moles x 10 <sup>6</sup> )					
	Syncrude MLSB	CNRL Horizon	CNUL MRM	Syncrude MLSB	CNRL Horizon	CNUL MRM
	2016			2017		
Toluene	120	0	0	90	0	0
<i>m-, p-Xylene</i>	92	0	0	69	0	0
<i>o-Xylene</i>	35	0	0	27	0	0
<i>n-C<sub>5</sub></i>	0	0	228		0	259
<i>n-C<sub>6</sub></i>	13	37	106	10	52	121
<i>n-C<sub>7</sub></i>	99	89	0	74	127	0
<i>n-C<sub>8</sub></i>	133	44	0	100	63	0
<i>n-C<sub>9</sub></i>	44	16	0	33	23	0
<i>n-C<sub>10</sub></i>	7	16	0	5	22	0
2-MC <sub>5</sub>	0	12	222	0	17	253
2-MC <sub>6</sub>	29	50	0	21	72	0
3-MC <sub>6</sub>	33	48	0	25	69	0
2-MC <sub>7</sub>	108	36	0	81	52	0
4-MC <sub>7</sub>	41	12	0	31	17	0
2-MC <sub>8</sub>	25	9	0	19	14	0
3-MC <sub>8</sub>	34	5	0	25	7	0
2-MC <sub>9</sub>	7	27	0	5	39	0
Total theoretical methane (moles x 10 <sup>6</sup> ) <sup>a</sup>	820	401	556	615	574	633
Microbial hydrocarbon conversion to methane (moles x 10 <sup>6</sup> ) <sup>b</sup>	656	321	445	492	459	506
Total methane emissions from ponds (moles x 10 <sup>6</sup> ) <sup>c</sup>	1191	336	2634	991	599	1051
Contribution of diluent hydrocarbons to total methane emissions from ponds (%)	55	95	17	50	77	48

960 <sup>a</sup> The masses of individual hydrocarbons from Table S6 were converted into moles using the respective molecular  
 961 weights and then Symons and Buswell equation (per Roberts, 2002) was used to calculate theoretical maximum  
 962 methane production from individual hydrocarbons.

963 <sup>b</sup> A factor of 0.8 determined during our hydrocarbon biodegradation studies (Siddique et al., 2007, 2006) was used  
 964 to calculate the efficiency of microbial conversion of hydrocarbons to methane; i.e.,  $r_i$

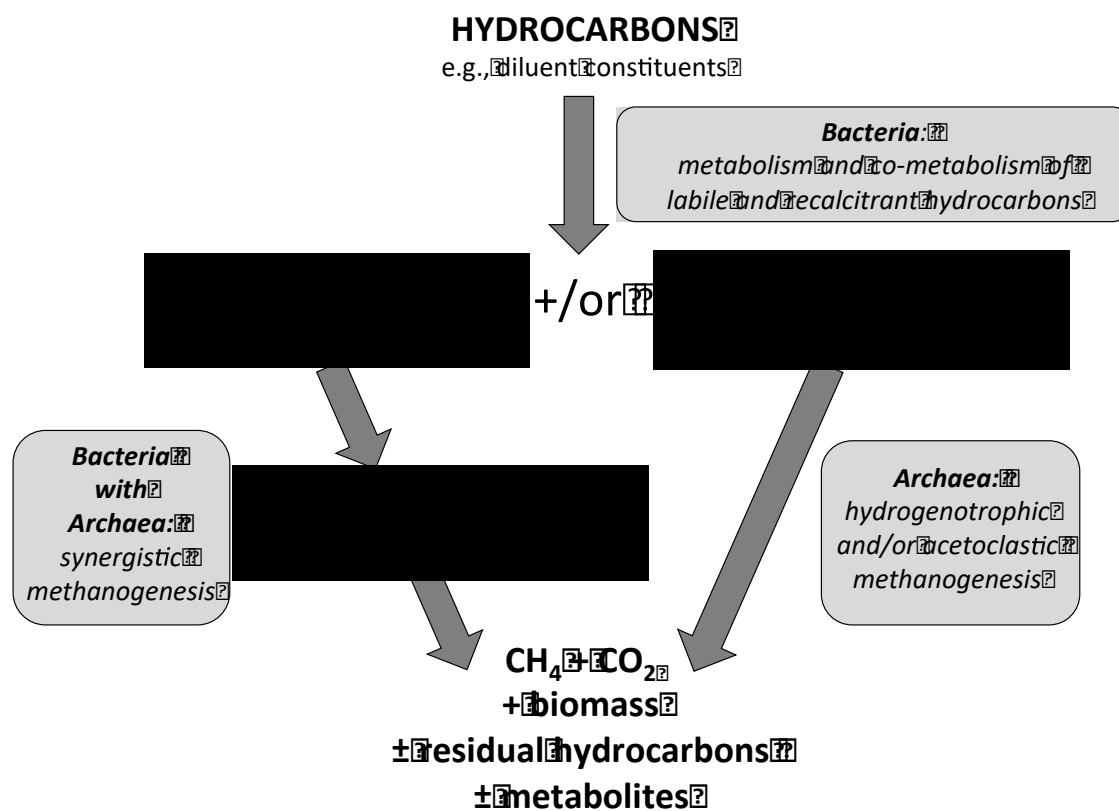
965 <sup>c</sup> CH<sub>4</sub> emission data (unpublished data, Government of Alberta) were converted into moles for comparison. The  
 966 Government of Alberta data includes CH<sub>4</sub> emissions from all units. We considered only those units that had been  
 967 receiving froth treatment tailings (solvent containing stream) for the most recent two or three years. Therefore, for  
 968 comparison, the bubbling zone of Syncrude MLSB, the entire CNRL Horizon pond and Cells 1-3 of CNUL  
 969 receiving diluent containing streams were used for field emissions data.



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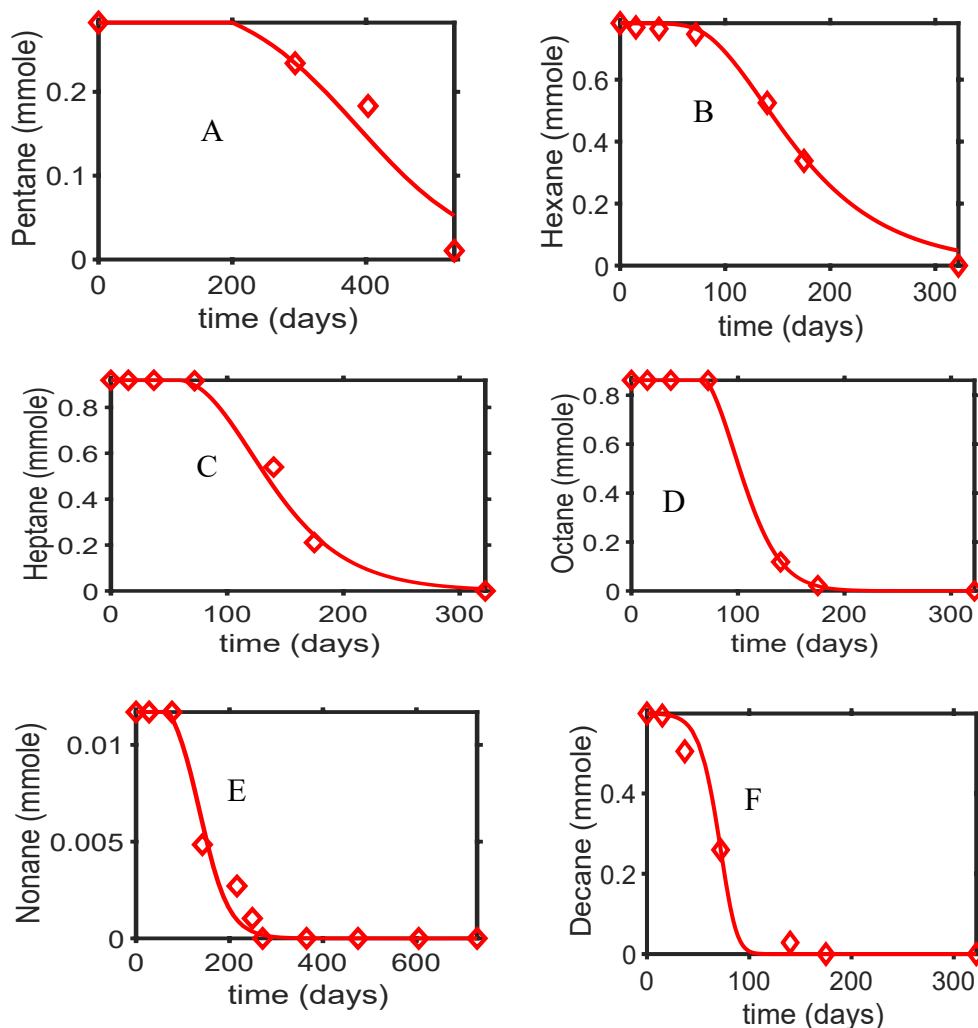
972 **Figure S1.** Simplified schematic of aqueous bitumen extraction from surface-mined oil sands,  
973 with subsequent retention of tailings in oil sands tailings ponds (OSTP) and reclamation in end  
974 pit lakes (EPL) (reviewed Foght et al., 2017). Biogenic gases in tailings (1) may escape to the  
975 atmosphere from shallow sediments via ebullition as greenhouse gas (GHG) emissions during  
976 retention or from deeper sediments when physically disturbed (e.g., by mechanical transfer), or  
977 (2) may be trapped as temporary or permanent gas voids (Guo, 2009) in dense sediments as  
978 latent GHG emissions, or (3) may be immobilized and transformed via geochemical interactions  
979 with clay minerals and pore water (Siddique et al., 2014).

980



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 982 **Figure S2.** Simplified biochemical flowchart for methanogenic biodegradation of hydrocarbons.  
 983 Metabolic processes carried out by bacteria or archaea alone or by synergistic consortia are  
 984 indicated in italics. If sulfate is present in sufficient concentrations (e.g., via addition of gypsum  
 985 [CaSO<sub>4</sub>•2H<sub>2</sub>O] in some oil sands tailing processes; Foght et al., 2017), anaerobic biodegradation  
 986 may still proceed but will be skewed toward accumulation of metabolites plus CO<sub>2</sub> and biomass,  
 987 with minimal CH<sub>4</sub> production. The ultimate end products include GHG, biomass, non-degradable  
 988 hydrocarbons and dead-end metabolites, e.g., from partial oxidation of recalcitrant hydrocarbons.

Supplementary Material



989

990 **Figure S3.** System of equations (2) fit to measured *n*-alkane biodegradation values for laboratory  
991 cultures. Symbols denote measured values and lines represent best fits to the data. Panels A, B,  
992 C, D, E and F show results for *n*-pentane, *n*-hexane, *n*-heptane, *n*-octane, *n*-nonane, and *n*-  
993 decane, respectively.

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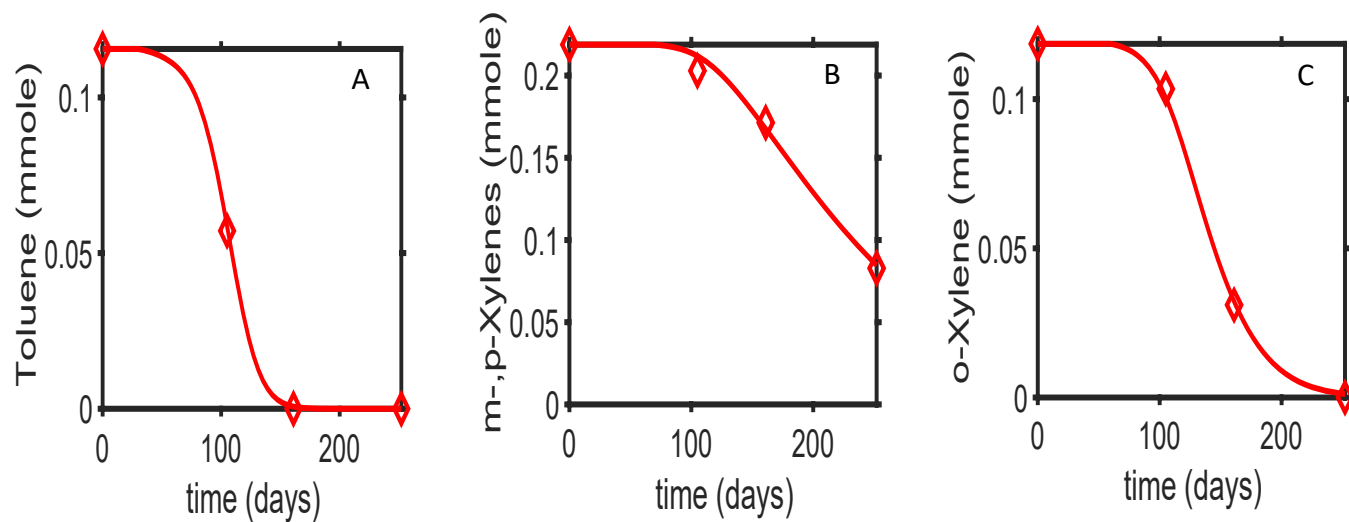
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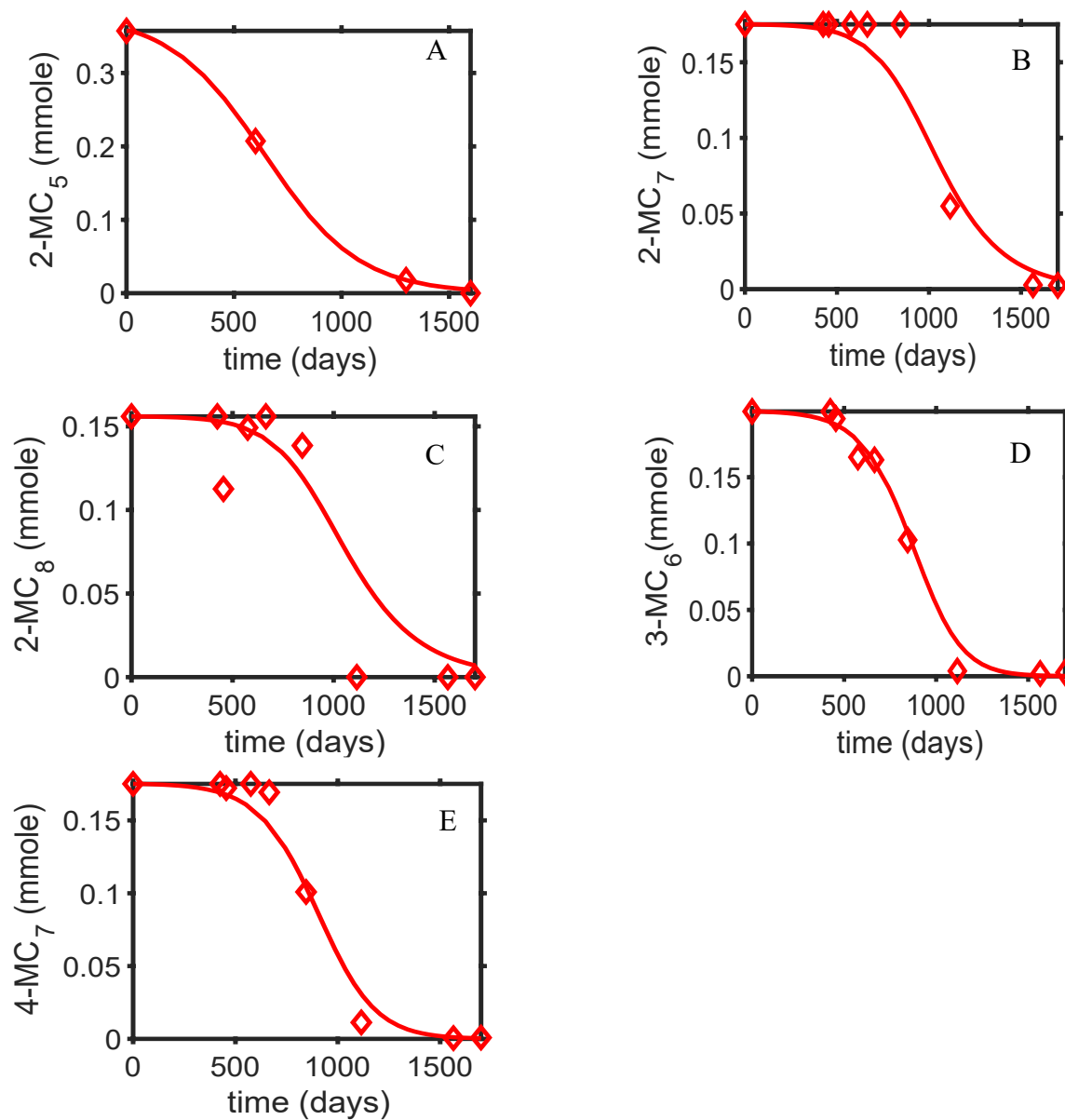
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1004 **Figure S4.** System (2) fit to measured biodegradable monoaromatic compound data for  
1005 laboratory cultures. Diamond symbols denote measured values and solid lines represent fitted  
1006 values. Panels A, B and C respectively show results for toluene, *m*- plus *p*-xylene, and *o*-xylene.

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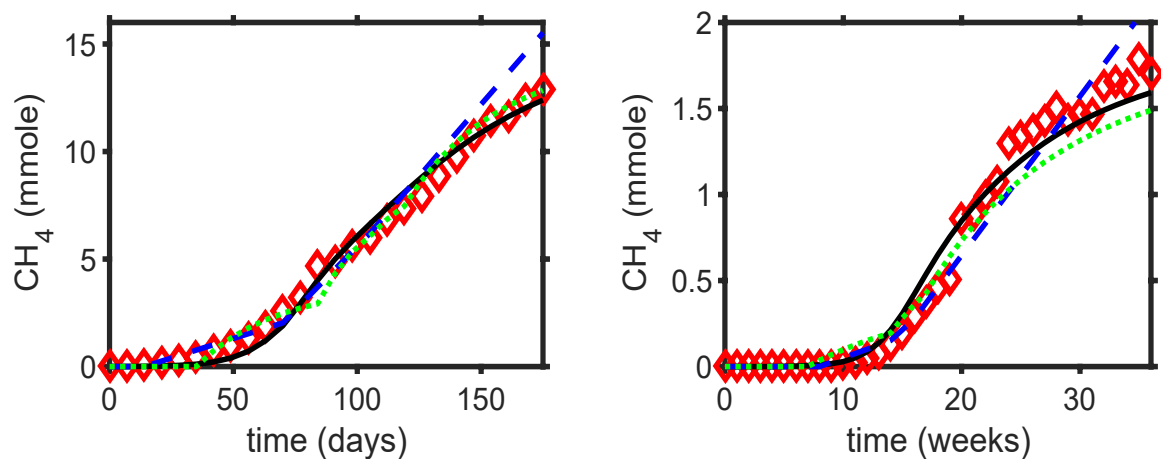
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1012 **Figure S5.** System (2) fit to *iso*-alkane biodegradation measurements for laboratory cultures.

1013 Solid lines represent fitted values and diamonds denote measured values. Panels A, B, C, D and

1014 E show results for 2-methylheptane, 2-methyloctane, 2-methylpentane, 3-methylhexane and 4-

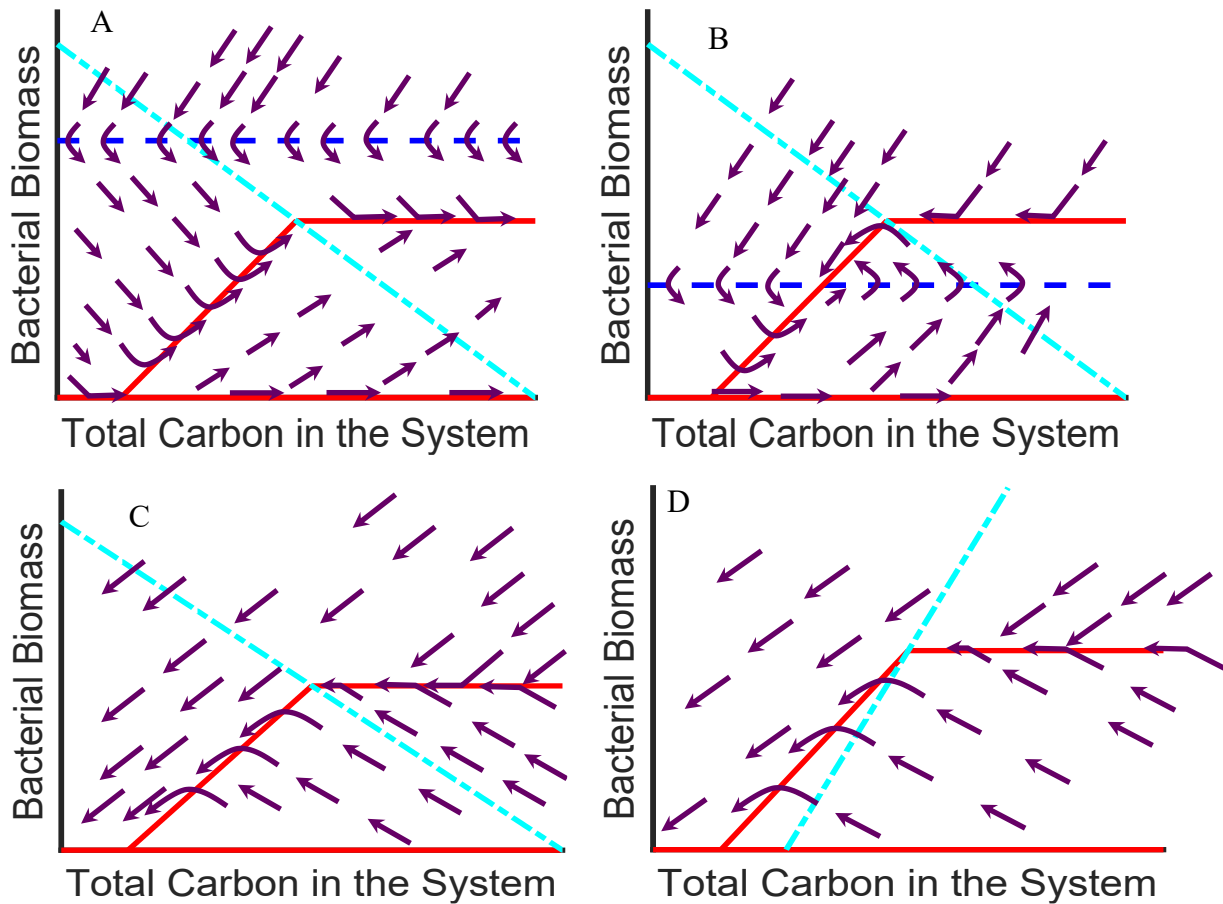
1015 methylheptane, respectively.



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1018 **Figure S6:** Comparison of stoichiometric model predictions of methane production from  
1019 laboratory cultures of Syncrude MFT incubated with mixtures of either *n*-alkane (C<sub>6</sub>, C<sub>7</sub>, C<sub>8</sub> and  
1020 C<sub>10</sub>) or monoaromatic (toluene, *o*-, *m*- and *p*-xylenes) components of naphtha diluent (left and  
1021 right panels, respectively). Measured methane values, from laboratory experiments independent  
1022 of those used to develop the model, are shown by diamond symbols. Solid black lines represent  
1023 the stoichiometric model prediction; broken blue lines and dotted green lines respectively  
1024 represent predictions made by using the previous zero-order and first-order models (Siddique et  
1025 al., 2008).

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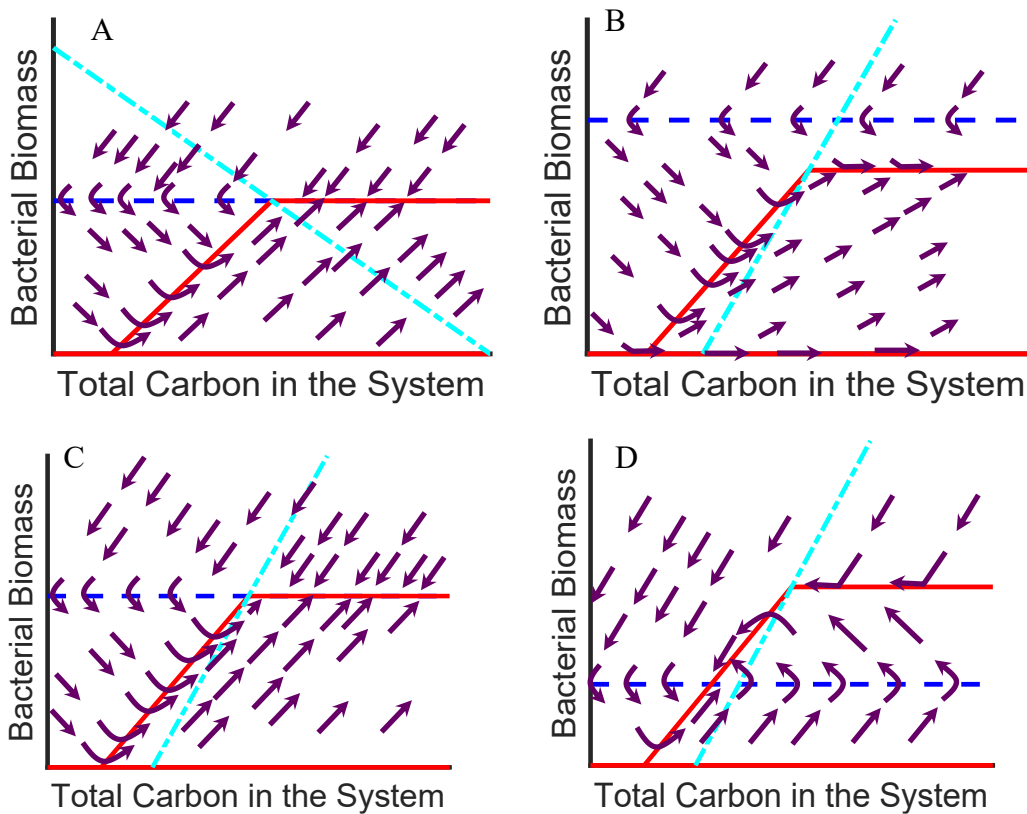
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1029 **Figure S7:** Phase plane analysis of solution states for microbial biomass and total carbon content  
 1030 in OSTP (Panels A and B, where  $C_T^{in} > 0$ ) or EPL (Panels C and D, where  $C_T^{in} = 0$ ) under  
 1031 different assumed initial conditions of  $C_T^{in}$  and ratio of the nitrogen carrying capacity to carbon  
 1032 carrying capacity ( $k_f:k_g$ ). In Panel A:  $C_T^{in} > \left(N_T - \frac{dk_f}{\mu}\right) \frac{d(1-r)}{\theta r}$  and  $k_f:k_g < \theta r$ . In Panel B,  
 1033  $C_T^{in} < \left(N_T - \frac{dk_f}{\mu}\right) \frac{d(1-r)}{\theta r}$  and  $k_f:k_g < \theta r$ . In Panel C:  $k_f:k_g < \theta r$ . In Panel D:  $k_f:k_g > \theta r$ .  
 1034 Solid red lines are nullclines for total biomass, broken blue lines are nullclines for total carbon  
 1035 content and broken light blue lines indicate where  $B = \left(N_T - \frac{(C_T + \frac{B}{r})k_f}{k_g}\right) \left(\frac{k_g r}{\theta k_g r - k_f}\right)$ , to the left of  
 1036 which nitrogen is limiting and to the right of which carbon is limiting. The slope of this line is  
 1037 determined by the ratio:  $k_f:k_g$ . Purple directional arrows account for time.



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1042 **Figure S8:** Phase plane analysis of solution states for microbial biomass and total carbon content  
 1043 in OSTP (where  $C_T^{in} > 0$ ) under different assumed initial conditions of  $C_T^{in}$  and ratio of the

1044 nitrogen carrying capacity to carbon carrying capacity ( $k_f:k_g$ ). In Panel A:  $C_T^{in} =$   
 1045  $\left(N_T - \frac{dk_f}{\mu}\right) \frac{d(1-r)}{\theta r}$  and  $k_f:k_g < \theta r$ . In Panel B,  $C_T^{in} > \left(N_T - \frac{dk_f}{\mu}\right) \frac{d(1-r)}{\theta r}$  and  $k_f:k_g > \theta r$ . In

1046 Panel C:  $C_T^{in} = \left(N_T - \frac{dk_f}{\mu}\right) \frac{d(1-r)}{\theta r}$  and  $k_f:k_g > \theta r$ . In Panel D:  $C_T^{in} < \left(N_T -$

1047  $\frac{dk_f}{\mu}\right) \frac{d(1-r)}{\theta r}$  and  $k_f:k_g > \theta r$ . Solid red lines are nullclines for total biomass, broken blue lines

1048 are nullclines for total carbon content and broken light blue lines indicate where the line  $B =$

1049  $\left(N_T - \frac{(C_T + \frac{B}{r})k_f}{k_g}\right) \left(\frac{k_g r}{\theta k_g r - k_f}\right)$  to the left of which nitrogen is limiting and to the right of which

1050 carbon is limiting. The slope of this line is determined by the ratio:  $k_f:k_g$ . Purple directional

1051 arrows account for time.